```
CHEME 6880 Homework 3
        Net ID: AF626
        Problem 1
        (Please feel free to use any machine learning software package for this problem) Consider the data set of Problem 2 in HW #1 (on regression). Please develop the following regression models to predict the value of y for x=0.7.
        (a) Support vector regression
        (b) Random forest
        (c) AdaBoost
        (d) Regression tree
        (e) Gradient boosting
        (f) XGBoost
        Solution
In [ ]: # Install necessary libraries
        # %pip install numpy
        # %pip install sklearn.svm
        # %pip install sklearn.ensemble
        # %pip install sklearn.tree
        # %pip install xgboost
In [ ]: # Importing required libraries
        import numpy as np
        import pandas as pd
        from sklearn.svm import SVR
        from sklearn.ensemble import RandomForestRegressor, AdaBoostRegressor, GradientBoostingRegressor
        from sklearn.tree import DecisionTreeRegressor
        import xgboost as xgb
        import matplotlib.pyplot as plt
        # Importing the required data as dataframe
        data_1 = pd.DataFrame(pd.read_csv('data/data_1.csv'))
        x = data_1[['x']]
        y = data_1['y']
        # Initializing the differeent Models
        models = {
             'Support Vector Regression': SVR(), # Default Kernel : Radial Basis Function (RBF)
             'Random Forest': RandomForestRegressor(),
             'AdaBoost': AdaBoostRegressor(),
             'Regression Tree': DecisionTreeRegressor(),
             'Gradient Boosting': GradientBoostingRegressor(),
             'XGBoost': xgb.XGBRegressor(objective ='reg:squarederror')
        # Creating an empty DataFrame to store the results
        results_df = pd.DataFrame(columns=['predicted_y'], index=models.keys())
        # Predicting the value of y for x=0.7
        x_{test} = [[0.7]]
        # Storing the predicted values in the DataFrame
        for name, model in models.items():
            model.fit(x, y)
            results_df.loc[name, 'predicted_y'] = model.predict(x_test)[0]
        # Displaying the results DataFrame
        print(results_df)
       c:\Python311\Lib\site-packages\sklearn\base.py:493: UserWarning: X does not have valid feature names, but SVR was fitted with feature names
         warnings.warn(
       c:\Python311\Lib\site-packages\sklearn\base.py:493: UserWarning: X does not have valid feature names, but RandomForestRegressor was fitted with feature names
         warnings.warn(
       c:\Python311\Lib\site-packages\sklearn\base.py:493: UserWarning: X does not have valid feature names, but AdaBoostRegressor was fitted with feature names
         warnings.warn(
       c:\Python311\Lib\site-packages\sklearn\base.py:493: UserWarning: X does not have valid feature names, but DecisionTreeRegressor was fitted with feature names
         warnings.warn(
                                  predicted_y
       Support Vector Regression -2.969096
       Random Forest
                                    -2.976859
                                      -2.9746
       AdaBoost
       Regression Tree
                                       -3.116
       Gradient Boosting
                                    -3.115718
       XGBoost
                                    -3.113697
       c:\Python311\Lib\site-packages\sklearn\base.py:493: UserWarning: X does not have valid feature names, but GradientBoostingRegressor was fitted with feature names
        warnings.warn(
In [ ]: # Plotting the predicted y values
        plt.figure(figsize=(10, 6))
        bars = plt.bar(results_df.index, results_df['predicted_y'], color='skyblue', width=0.5)
        plt.ylim(0, max(results_df['predicted_y']) * 1.2) # Adjusting y-axis scale
        for bar in bars:
            yval = bar.get_height()
            plt.text(bar.get_x() + bar.get_width()/2, yval, round(yval, 2), ha='center', va='bottom')
        plt.xlabel('Model')
        plt.ylabel('Predicted y value for x=0.7')
        plt.title('Predicted y values for different models')
        plt.xticks(rotation=45)
        plt.tight_layout()
        plt.show()
                                                      Predicted y values for different models
          -3.5
                                                                                   -3.12
                                                                                                       -3.12
                                                                                                                           -3.11
                        -2.97
                                            -2.98
                                                               -2.97
          -3.0
          -2.5
           -2.0
          -0.5
            0.0
                                                                         Model
        Problem 2
        (Please feel free to use any machine learning software package for this problem 1 in HW #2 (on classification). Please develop the following classification models to make prediction for the approval outcome of the same new application from an
        unemployed, senior applicant with excellent credit rating and high available credit.
        (a) Random forest
        (b) AdaBoost
        (c) Gradient boosting
        (d) XGBoost
        Solution
In [ ]: # Importing necessary libararies
        import pandas as pd
        from sklearn.model_selection import train_test_split
        from sklearn.ensemble import RandomForestClassifier, AdaBoostClassifier, GradientBoostingClassifier
        import xgboost as xgb
        # Reading data for problem set 2 as dataframe
        data_2 = pd.read_csv('data/data_2.csv')
        # Convert categorical variables using the provided encoding in HW2
        encoding = {
             'Employment Status': {'Unemployed': 0, 'Employed': 1},
             'Credit Rating': {'Excellent': 1, 'Fair': 0},
             'Available Credit': {'High': 2, 'Medium': 1, 'Low': 0},
             'Age': {'Senior': 2, 'Middle Age': 1, 'Young': 0},
             'Approve Application ?': {'No': 0, 'Yes': 1}
        data_2.replace(encoding, inplace=True)
        # Split features and target variable
        X = data_2.drop('Approve Application ?', axis=1)
        y = data_2['Approve Application ?']
        # Initializing the different models
        models = {
             'Random Forest': RandomForestClassifier(),
             'AdaBoost': AdaBoostClassifier(algorithm='SAMME'),
             'Gradient Boosting': GradientBoostingClassifier(),
             'XGBoost': xgb.XGBClassifier(objective='binary:logistic')
        # Splitting the data into training and testing sets
        X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=42)
        # Train the models
        for name, model in models.items():
            model.fit(X_train, y_train)
        # New application data (unemployed, senior, excellent credit rating, high available credit)
        new_application = pd.DataFrame({
             'Employment Status': [0], # Unemployed
             'Credit Rating': [1], # Excellent
             'Available Credit': [2], # High
             'Age': [2] # Senior
        # Predicting the approval outcome for the new application
        predictions = {}
        for name, model in models.items():
            predictions[name] = model.predict(new_application)
        # Displaying the predictions
        for name, pred in predictions.items():
            print(f'Predicted approval outcome using {name}: {"Yes" if pred[0] == 1 else "No"}')
       Predicted approval outcome using Random Forest: Yes
       Predicted approval outcome using AdaBoost: Yes
       Predicted approval outcome using Gradient Boosting: Yes
       Predicted approval outcome using XGBoost: No
        Problem 3
        (Please feel free to use any machine learning software package for this problem) Consider the data set of Problem 5 in HW #2 (on classification via SVM). Please develop the following classification models to predict the outcome for [1.5 1.5].
        (b) AdaBoost
        (c) Gradient boosting
        (d) XGBoost
        Solution
In [ ]: import pandas as pd
        from sklearn.ensemble import RandomForestClassifier, AdaBoostClassifier, GradientBoostingClassifier
        from sklearn.preprocessing import LabelEncoder
        import xgboost as xgb
        # Reading the data from CSV file into a pandas DataFrame
        data_3 = pd.read_csv('data/data_3.csv')
        # Separate features (X1, X2, X3) and target variable (Y)
        X = data_3[['X1', 'X2', 'X3']]
        y = data_3['Y']
        # Convert categorical labels ('Yes' and 'No') into numerical values (1 and 0)
        label_encoder = LabelEncoder()
        y = label_encoder.fit_transform(y)
        # Initializing the different classification models
        models = {
             'Random Forest': RandomForestClassifier(),
             'AdaBoost': AdaBoostClassifier(algorithm='SAMME'),
             'Gradient Boosting': GradientBoostingClassifier(),
             'XGBoost': xgb.XGBClassifier(objective='binary:logistic')
        # Train the models
        for name, model in models.items():
            model.fit(X, y)
        # New input data [1.5, 1.5, 1.5]
        new_input = pd.DataFrame({'X1': [1.5], 'X2': [1.5], 'X3': [1.5]})
        # Predict the outcome for the new input using each model
        predictions = {}
        for name, model in models.items():
            predictions[name] = label_encoder.inverse_transform(model.predict(new_input))
        # Display the predictions
        for name, pred in predictions.items():
            print(f'Predicted outcome using {name}: {pred[0]}')
       Predicted outcome using Random Forest: Yes
       Predicted outcome using AdaBoost: Yes
       Predicted outcome using Gradient Boosting: Yes
       Predicted outcome using XGBoost: Yes
        Problem 4
        Perform dimensionality reduction using principle component analysis (PCA) on the dataset includes 500 data samples, each of which has 33 dimensions/variables (d1 to d33). Please first preprocess the data, such that all input variables are
        scaled to zero mean and unit variance. Next, perform singular value decomposition (SVD) on the covariance matrix of the normalized data. Please answer the following questions using the principal component (PC) vectors and corresponding eigenvalues obtained from SVD.
        (a) What is the minimum number of principal components (PCs) that are required to capture 95% of the total variations of the data in R33?
        (b) What is the projection of the 5th data sample (in the original dataset) on the PC with the largest eigenvalue? [hint: please use the "normalized" value of the 5th data sample]
        Solution
In [ ]: import pandas as pd
        data_4 = pd.read_csv('data/data_4.csv')
        data_4.head(5)
Out[]:
           Data Sample No.
                                                                                      d9
                                                                                               d24
                                                                                                      d25
                                                                                                            d26
                                                                                                                    d27
                                                                                                                           d28
                                                                                                                                                              d33
                       1 0.24987 3642.6 4539.6 9.2784 27.200 42.248 2704.2 75.492 120.40 ... 53.617 24.708 62.265 22.224 39.724 41.975 50.223 47.411 41.093 18.351
                       2 0.25118 3694.8 4513.8 9.2831 27.077 42.736 2705.4 74.628 120.41 ... 53.926 24.579 61.306 21.975 40.249 34.187 44.741 47.442 41.303 19.831
        2
                       3 0.25185 3683.5 4504.9 9.4600 26.987 42.245 2705.2 74.315 120.42 ... 54.032 24.521 60.532 21.640 40.003 43.628 46.032 47.574 41.520 20.426
                       4 0.25147 3653.9 4531.9 9.3462 26.983 42.656 2706.3 75.487 120.39 ... 53.708 24.558 61.496 22.324 40.161 37.967 43.903 47.606 41.284 19.568
                       5 0.24107 3629.3 4527.0 9.3406 27.041 42.520 2705.6 75.332 120.38 ... 53.259 24.024 60.781 22.506 40.962 34.247 48.037 47.585 40.949 17.063
        5 rows × 34 columns
In [ ]: # Sacling the input data to zero mean and unit variance
        # Separate the Sample No. column
        sample_numbers = data_4['Data Sample No.']
        data = data_4.drop(columns=['Data Sample No.'])
        # scale the data to have zero mean and unit variance
        scaled_data = (data - data.mean()) / data.std()
        scaled_df = pd.DataFrame(scaled_data, columns=data.columns)
        scaled_df['Data Sample No.'] = sample_numbers
        # The sacled input is as follows:
        scaled_df
Out[]:
                   d1
                            d2
                                      d3
                                               d4
                                                         d5
                                                                            d7
                                                                                     d8
                                                                                                       d10 ...
                                                                                                                   d25
                                                                                                                             d26
                                                                                                                                      d27
                                                                                                                                                d28
                                                                                                                                                         d29
                                                                                                                                                                   d30
                                                                                                                                                                            d31
                                                                                                                                                                                     d32
                                                                                                                                                                                               d33 Data Sample No.
          0 -0.044401 -0.653661 0.885207 -0.861360 1.400405 -0.410481 -0.227496 0.960375 0.030020 0.197452 ... -0.004696 0.795260 -0.068298 -0.248827
                                                                                                                                                    1.211723 1.575293 -0.023624 -0.003330 0.090802
          1 0.001481 0.975980 0.071957 -0.799933 0.810940 1.797914 0.000494 -0.675350 0.566090 -0.170456 ... -0.050358 -0.013818 -0.670200 0.116256 -1.347466 -0.752507 -0.009022 0.396246 1.085388
          2 0.024947 0.623204 -0.208583
                                         1.512065 0.379625 -0.424057 -0.037504 -1.267921 1.102160 0.001520 ... -0.070888 -0.666817 -1.479989 -0.054811 1.754909 -0.204315 0.053153 0.809141 1.485239
          3 0.011638 -0.300884 0.642493 0.024754 0.360455 1.435882 0.171487 0.950909 -0.506050 -0.109709 ... -0.057791 0.146479 0.173430 0.055062 -0.105333 -1.108344 0.068226 0.360094 0.908648
          4 -0.352618 -1.068876  0.488038 -0.048436  0.638414  0.820428  0.038492  0.657463 -1.042120  0.923857 ... -0.246810 -0.456743  0.613375  0.612074 -1.327750  0.647061  0.058334 -0.277325 -0.774757
        495 -0.551909 -1.043901 -0.460753 -0.426145 -1.082056 1.268443 -2.355404 0.352658 -1.578190 0.687711 ... -0.511223 -0.649100 -2.127820 0.185101 -2.730900 1.425825 0.468124 -0.992755 0.637824
                                                                                                                                                                                                              496
        496 0.919827 -1.199997 -0.114019 -0.903183 0.312531 -0.767988 -2.279408 -1.252775 0.030020 0.072534 ... 1.044818 0.386081 -1.646781 0.447265 -0.276537 0.703111 0.521349 -0.062315 0.872359
                                                                                                                                                                                                              497
                                                                                                                                                                                                              498
        497 0.968862 -0.588101 -0.460753 -0.164754 0.523397 0.738971 -1.994420 -1.235737 1.102160 0.038310 ... 0.995971 -1.177236 -0.786230 0.480644 -0.157581 -0.490088 0.566567 0.139376 0.055857
                                                                                                                                                                                                              499
        498 -0.031092 1.896946 -0.177062 1.079464 -0.880775 1.417781 -1.652435 -1.360688
                                                                                        1.638229 -2.156305 ... 0.002738 0.424890 -1.620191 -1.755056 1.136800 -1.149108 0.708816 1.813788 -0.934698
        499 -0.069269 1.781435 -0.794880 0.903026 0.719885 1.055749 -1.234453 1.679790 1.102160 -2.011708 ... 0.040612 -1.108055 -1.206836 -1.899003 0.751345 -0.888387 0.713998 0.679754 1.198287
                                                                                                                                                                                                              500
        500 rows × 34 columns
In [ ]: import pandas as pd
        import numpy as np
        scaled_data = scaled_df
        # Dropping the 'Data Sample No.' column before performing SVD
        scaled_data = scaled_data.drop(columns=['Data Sample No.'])
        # Computing the covariance matrix of the normalized data manually
        n = scaled_data.shape[0]
        covariance_matrix = np.dot(scaled_data.T, scaled_data) / n
        # Perform Singular Value Decomposition (SVD) on the covariance matrix manually
        eigenvalues, eigenvectors = np.linalg.eig(covariance_matrix)
        # Sorting eigenvalues and corresponding eigenvectors in descending order to select the most prominent one
        sorted_indices = eigenvalues.argsort()[::-1]
        eigenvalues = eigenvalues[sorted_indices]
        eigenvectors = eigenvectors[:, sorted_indices]
        # Display the singular values (eigenvalues)
        print("Singular values (eigenvalues):")
        print(eigenvalues)
        # Display the left singular vectors (principal components)
        print("Left singular vectors (principal components):")
        print(eigenvectors)
       Singular values (eigenvalues):
       [5.39750324e+00 3.16510613e+00 2.60981316e+00 2.18632781e+00
        2.04219873e+00 2.00157893e+00 1.86616721e+00 1.52987871e+00
        1.48713060e+00 1.24074489e+00 1.08661261e+00 1.06078891e+00
        9.97635537e-01 9.28645420e-01 8.83385268e-01 8.23397334e-01
        7.80831295e-01 6.38019728e-01 6.02950663e-01 4.48724269e-01
        4.02651865e-01 3.26433797e-01 2.37528969e-01 8.82716030e-02
        4.74136054e-02 2.50399737e-02 1.32239692e-02 9.08997819e-03
        3.87269952e-03 2.94412821e-03 8.88937442e-05 4.92516427e-08
        3.87224007e-08]
       Left singular vectors (principal components):
       [[-1.64427354e-03 3.49043801e-02 3.52585827e-01 ... -1.08206134e-02
          9.58673192e-06 -5.29297101e-05]
        [ 4.47513096e-02 -1.82180753e-01 1.58491226e-01 ... -4.14887387e-04
          9.59710618e-06 1.11745729e-05]
        [ 9.00106911e-02     4.06699841e-02     9.66973912e-03     ...     1.63884418e-04
          1.41546561e-06 7.38390496e-06]
        [-2.55005262e-01 -3.69232595e-01 -9.21097270e-02 ... -3.10444655e-02
          2.85383816e-05 6.57388368e-05]
        [ 8.73934996e-02 -2.58468939e-01 2.34605349e-01 ... 6.44198156e-04
          1.43625020e-05 5.55617002e-06]
        [-7.17899895e-03 -1.70583488e-02 1.38371301e-01 ... 7.06147829e-01
         -7.63252966e-04 -7.93268939e-05]]
In [ ]: # Calculate the cumulative explained variance ratio
        cumulative_variance_ratio = np.cumsum(eigenvalues) / np.sum(eigenvalues)
        # Find the number of principal components needed to capture 95% of the total variance
        min_components = np.argmax(cumulative_variance_ratio >= 0.95) + 1
        print(f"Minimum number of principal components required to capture 95% of total variance: {min_components}")
       Minimum number of principal components required to capture 95% of total variance: 19
In [ ]: # Extract the 5th data sample (normalized)
        sample_5_normalized = scaled_data.iloc[4].values # Indexing is 0-based
        # Project the normalized sample onto the principal components
        projection = np.dot(sample_5_normalized, eigenvectors[:, 0])
        print(f"Projection of the 5th data sample on the PC with the largest eigenvalue: {projection}")
       Projection of the 5th data sample on the PC with the largest eigenvalue: -0.5115145098789611
        Problem 5
        (Please feel free to use any machine learning software package for this problem) Consider the data set of Problem 5 in HW #2 (on classification via SVM). Please develop the following classification models to predict the outcome for [1.5 1.5].
        (a) Random forest
        (b) AdaBoost
        (c) Gradient boosting
        (d) XGBoost
        Solution
In [ ]: import pandas as pd
        import matplotlib.pyplot as plt
        from sklearn.manifold import TSNE
        # Read the data for problem 5
        data_5 = pd.read_csv('data/data_4.csv')
        # Separate features from the data
        X = data_5.drop(columns=['Data Sample No.'])
        # Define perplexity values
        perplexities = [5, 30, 50]
        # Applying t-SNE with different perplexity values and visualize the reduced-dimensional data
        plt.figure(figsize=(15, 5))
        for i, perplexity in enumerate(perplexities, 1):
            # Apply t-SNE
            tsne = TSNE(n_components=2, perplexity=perplexity, random_state=42)
            X_{embedded} = tsne.fit_transform(X)
            # Visualize the reduced-dimensional data
            plt.subplot(1, 3, i)
            plt.scatter(X_embedded[:, 0], X_embedded[:, 1])
            plt.title(f"Perplexity = {perplexity}")
            plt.xlabel('t-SNE Component 1')
            plt.ylabel('t-SNE Component 2')
        plt.tight_layout()
        plt.show()
                                   Perplexity = 5
                                                                                                    Perplexity = 30
                                                                                                                                                                     Perplexity = 50
            60
                                                                             20
            40
                                                                             10
           20
       t-SNE Component 2
                                                                                                                                          t-SNE Component 2
                                                                         t-SNE
                                                                            -10
          -40
                                                                                                                                             -10
                                                                            -20
          -60
```

-15

-15

-10

-5

t-SNE Component 1

10

15

20

-20

t-SNE Component 1

-60

-40

20

60

-20

-10

t-SNE Component 1