Gravity Report

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Abstract

NOTHING FOR NOW

1 Introduction

Gravity is an open source code for studying the gravitational collapse of variouse fields in AdS spaces. It is developed in 2012, and 2013 by Arya Farahi for gravitational collapse project under guidance of Leo Pando Zayas at University of Michigan - Ann Arbor.

2 Results

2.1 Final Plots

Graphs 1, 2, and 3 show results of Π , ϕ , and Φ vs. r, respectively, at finalt time, t = 19.6349540849.

2.2 Black hole formation

One of the aim of Gravity is to study the black hole formation of different fields in anti de Sitter (AdS) geometry. Once the black hole forms the field stops its evolution. It is suggested that all fields forms a black hole at sometimes during their evolution, and it is the universal feature of all fields in AdS

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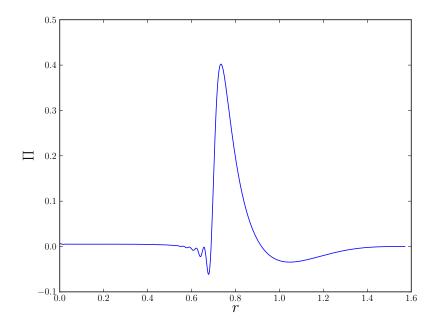


Figure 1: Plot of Π vs. r at final time.

. The time of fomation of black hole depends on the amplititude and shape of initial wave, the geometry of space, potential, and the field choice. Because it is not possible to run the code for ever an end condition implimented in the code to stop the evolution of field after some number of iteration. In this run the number of iteration is defined, $i_{\rm max}=50000$.

For black hole formation the code checks the value of A at each point, at each time. Theoretically once A=0 it means that the black hole formed so the condition A_{\min} is defined to check whether the black hole is formed or not. One should choose something close to zero, but independently, by changing the A_{\min} need to make sure that the condition do not affect the result. In this run $A_{\min}=0.01$.

In this run the black hole was not formed and the field stoped its evolution at time, t = 19.6349540849. There maybe two resoan why black hole did not form. First the number of iteration was not enough to get the balck hole so by increasing the nuber of iteration once can go furthur in time and see if the black holes forms. Second errors grow and become dominant so the

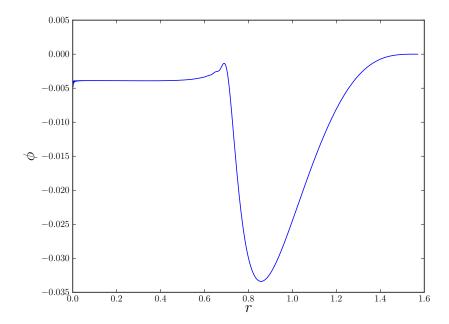


Figure 2: Plot of ϕ vs. r at final time.

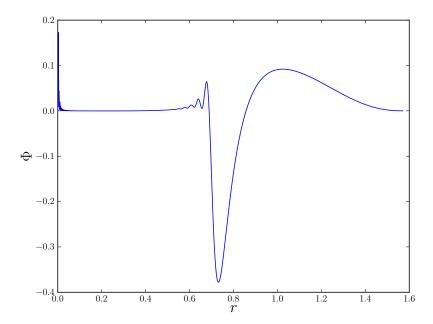


Figure 3: Plot of Φ vs. r at final time.

code failed to predict the behavoiur of field. For solving this problem one may want to increase the grid size, in this run grid size of, n = 1000, is used. There is another possibilities to improve the numerical solution, change the solver to something more accurate, in this run solver RK4 is used.

2.3 Power Spectrum

Assuming the evolution of each point in space following the power low in Fourier space, one can compute the power of power spectrum for large frequencies with finding the best fit line in log-log plot. Here it is assumed assume,

$$r(k) \propto k^n \tag{1}$$

In this run the power, n, is computed for 10 points.

r	n
0.141371669412	0.11998343265
0.282743338823	-0.00443192633823
0.424115008235	-0.516695148559
0.565486677646	-0.526293285502
0.706858347058	-0.730462922342
0.848230016469	-1.06385912273
0.989601685881	-0.651685506017
1.13097335529	-0.314456596941
1.2723450247	0.0719593560704
1.41371669412	0.487377128302

3 Parameters

The following parameters are used in this run,

Field proparties:

Geometry = AdS4
Cosmological constant = 1.0
Potential = Massive_Scalar

Initial Conditions:

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Initial Condition = Gaussian
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Numerical method:

Solver = RK4 Grid size = 1000

Ending conditions:

Horizon condition $(A_min) = 0.01$ Maximum number of iteration = 50000

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