## Connect

beyond learning – reasoning; why
logic
and its limits
fundamental, uncertainty
reasoning under uncertainty
back to learning - from text

### connecting the dots: motivation

"who is the leader of USA?" facts ... [X is prime-minister of C] ... [X is president of C] no such fact [X is leader of USA] ... now what? X is president of C => X is leader of C - rules (knowledge) √ Obama is president of USA => Obama is leader of USA example of reasoning ... reasoning can be tricky: Manmohan Singh is prime-minister of India Pranab Mukherjee is president of India "who is the leader of India"

... much more knowledge is needed

#### reasoning and web-intelligence

"book me an American flight to NY ASAP"

"this New Yorker who fought at the battle of Gettysburg was once considered the inventor of baseball"

Alexander Cartwright or Abner Doubleday – *Watson got it right* "who is the Dhoni of USA?"

- analogical reasoning X is to USA what Cricket is to India (?)
- + abductive reasoning there is no US baseball team ... so ? find best possible answer^
- + reasoning under uncertainty ... who is the "most" popular?

#### **Semantic Web:**

- web of linked data, inference rules and engines, query
  - pre-requisite: extracting facts from text, as well as rules

## logic: propositions

A, B – 'propositions' (either True or False)
A and B is True: A=True and B=True ( $A \land B$ )
A or B is True: either A=True or B=True ( $A \lor B$ )

if A then B (same as if A=True then B=True)

is the same as saying A=False or B=True

also written as:

**A=> B** is equivalent to  ${}^{\sim}A \lor B$  check: A=T,  ${}^{\sim}A=F$ , so  $({}^{\sim}A \lor B)$  =T only when B=T **Important**:

if A=F,  $\sim A=T$ , so ( $\sim A \lor B$ ) is true regardless of B being T or F

## logic: predicates

Obama is president of USA: isPresidentOf (Obama, USA) - predicates, variables X is president of C => X is leader of C isPresidentOf (X, C) => isLeaderOf (X, C) plus – the above is stating a rule for all X,C - quantification "Obama is president of USA": fact isPresidentOf (Obama, USA) using rule R and fact F, isLeaderOf (Obama, USA) is entailed (unification: X bound to Obama; C bound to USA) isLeaderOf (X, USA) – query reasoning = answering queries or deriving new facts

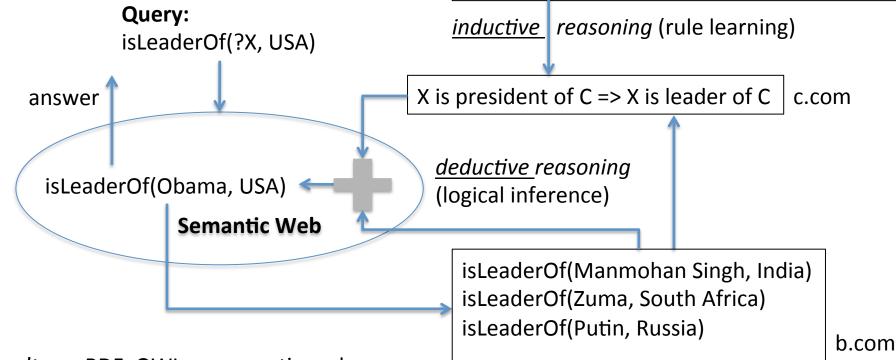
using unification + inference = resolution

#### semantic web vision

facts and rules in RDF-S & OWL-..
web of *data* and *semantics*web-scale inference

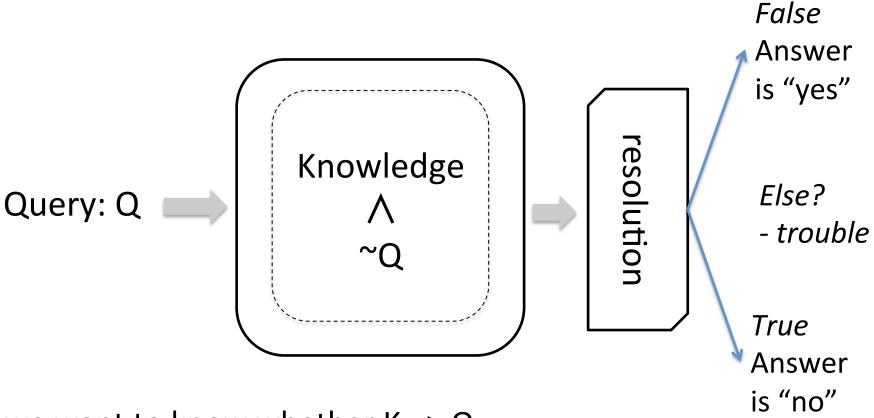
Google<sup>2</sup>; Wolfram-Alpha; Watson\*

Manmohan Singh is prime-minister of India
Pranab Mukherjee is president of India
Vladimir Putin is president of Russia
Obama is president of USA
.... is president of ....
a.com



\*don't use RDF, OWL or semantic-web \_\_\_\_\_ technology though they have similar intent, spirit ...

### logical inference: resolution



we want to know whether K => Q

i.e. ~K V Q is True

i.e.  $K \wedge ^{\sim} Q$  is False!

in other words K augmented with ~Q entails falsehood, for sure

### logic: fundamental limits

resolution may never end; never (whatever algorithm!)

- undecidability predicate logic undecidable (Godel, Turing, Church ...)
- intractability
  propositional logic is decidable, but intractable (SAT and NP ..)
- ? whither automated reasoning, semantic-web..? fortunately:
  - OWL-DL,OWL-lite (description logic: leader ⊂ person ...) decidable; still intractable in worst case
  - Horn logic (rules, i.e., person  $\land$  bornIn(C) => citizen(C) ... ) undecidable (except with caveats); but tractable

# logic and uncertainty

predicates A, B, C

- 1. For all x, A(x) => B(x).
- 2. For all x, B(x) => C(x)
- 1 and 2 entail For all x, A(x) => C(x) fundamental

however, consider the uncertain statements:

- 1': For most x, A(x) => B(x). "most firemen are men"
- 2'. For most x, B(x) => C(x). "most men have safe jobs" it does **not** follow that "For most x, A(x) => C(x)"!

$$A = C$$

# logic and causality

- if the sprinkler was on then the grass is wet
   S => W
- if the grass is wet then it had rained
   W => R

therefore it follows, i.e. S => R is *entailed* which states "the sprinkler is on, so it had rained"

problem is that causality was treated differently in each statement => absurdity

### causality and classification

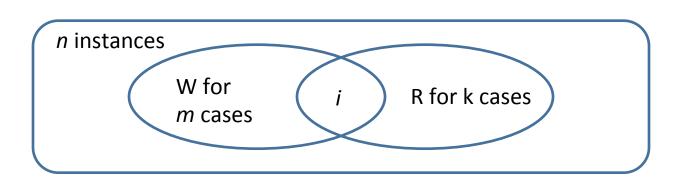
if S then W (W is an observable feature of S)  $S \longrightarrow W$ if R then W (W is an observable feature of R)  $R \longrightarrow W$ 

if W is observed then R happened (abduction) concluding which class of event observed S or R abductive reasoning

= from effects to likely causes

#### probability tables and 'marginalization'





consider p(R,W)

to get p(R) we can 'sum out' W:  $p(R) = \sum_{W} p(R,S)$ 

this is called *marginalization* of W

notice that marginalization is equivalent to aggregation on column P:

$$\sum_{W} p(R,W) = {}_{R}G_{SUM(P)} T^{R,W}$$

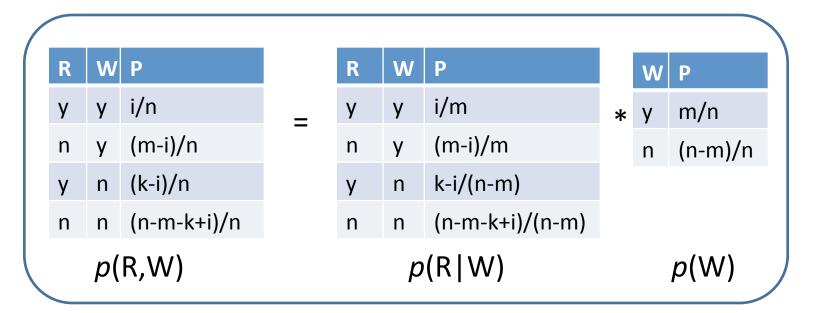
or, in SQL: SELECT R, SUM(P) from T<sup>R,W</sup> GROUP BY R

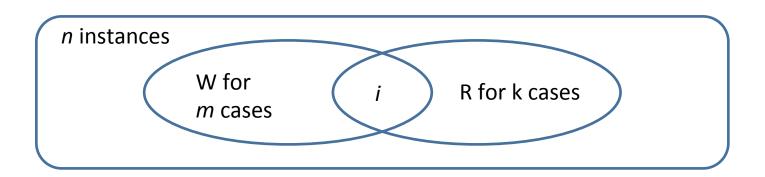
R	P	
У	k/n	$=\sum_{w}$
n	(n-k)/n	

R	W	P
У	У	i/n
n	У	(m-i)/n
У	n	(k-i)/n
n	n	(n-m-k+i)/n

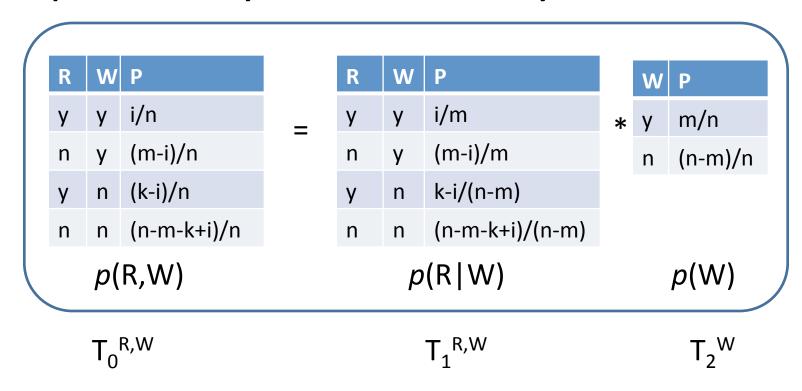
$$P(R,W) = T^{R,W}$$

#### probability tables and Bayes rule ...





#### probability tables and Bayes rule ...



notice that the product  $p(R|W) p(W) = T_1^{R,W} \bowtie_B T_2^W$  i.e., the *join* of the two tables  $T_1$  and  $T_2$  on the common attribute W! so, probability tables (also called *potentials*) can be multiplied in SQL!

SELECT R, SUM(P1\*P2) from  $T_1^{R,W}$ ,  $T_2^{W}$  WHERE W1=W2 GROUP BY R

### probability tables and evidence

=

R	W	Р
у	У	i/n
n	У	(m-i)/n
У	n	(k-i)/n
n	n	(n-m-k+i)/n

$$\mathbf{e}^{(B=y)} = \begin{array}{c|ccc} \mathbf{R} & \mathbf{W} & \mathbf{P} \\ \mathbf{y} & \mathbf{y} & \mathbf{i/n} \\ \mathbf{n} & \mathbf{y} & (\mathbf{m-i})/\mathbf{n} \end{array}$$

R	W	P	
У	У	i/m	* m/n
n	У	(m-i)/m	,

$$=T^{R,W}$$

$$P(R,W) e^{(W=y)}$$

$$P(R|W=y)$$

SELECT R,W,P from T<sup>R,W</sup> WHERE W=y

if we restrict p(R,W) to entries where evidence W=y holds:

$$p(R,W) e^{(W=y)} = p(R|W=y) * p(e^{(W=y)})$$

applying evidence is equivalent to the select operator on TR,W

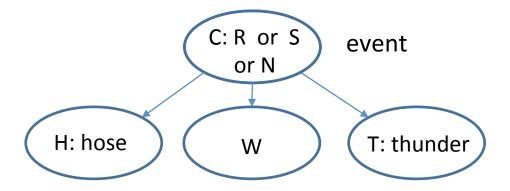
$$P(R,W) e^{(W=y)} = \sigma_{W=y} T^{R,W}$$

so the *a posteriori* probability of R given evidence **e** is just:

$$P(R | \mathbf{e}^{(W=y)}) = \rho(R,W) \mathbf{e}^{(W=y)} / \rho(\mathbf{e}^{(W=y)})$$

A	P
У	i/m
n	(m-i)/m

### naïve Bayes classifier

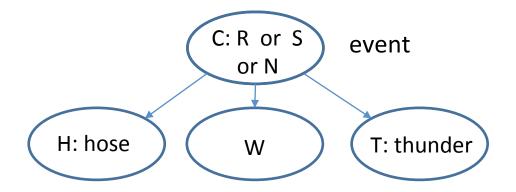


assumption – independence of features H,W,T | C =>  $p(C|H,W,T) = \sigma p(H,W,T|C) = \sigma p(H|C) p(W|C) p(T|C)$  and in general for n features:

$$p(C|F_1...F_n) = \sigma p(F_1...F_n|C) = \sigma p(F_1|C) ... p(F_n|C)$$

- remember, these are <u>tables</u> (multiplied as before: SQL!) now given observations  $\mathbf{e}^{f1, \dots fn}$  we get the likelihood rule  $p(C|F_1 \dots F_n) \mathbf{e}^{f1, \dots fn} = \sigma' p(f_1 \dots f_n | C) = \sigma' p(f_1 | C) \dots p(f_n | C)$ 

#### naïve Bayes classifier and partial evidence



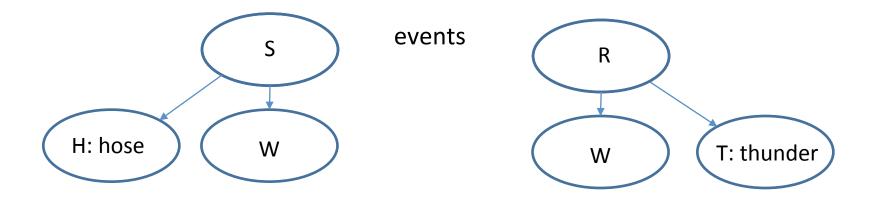
given observations  $\mathbf{e}^{f_1, \dots f_n}$  we get the likelihood rule  $p(C|F_1...F_n)$   $\mathbf{e}^{f_1, \dots f_n} = \sigma' p(f_1...f_n|C) = \sigma' p(f_1|C) \dots p(f_n|C)$  again, ... even if some features are *not* measured, e.g.  $F_1$ :  $p(C|F_1F_2...F_n)$   $\mathbf{e}^{f_2, \dots f_n} = \sigma'' \Sigma_{F_1} p(F_1|C) p(f_2|C) \dots p(f_n|C)$  in SQL:

SELECT C, SUM( $\Pi_i P_i$ ) FROM  $T_1...T_n$  WHERE  $F_2 = f_2 ... F_n = f_n$  {evidence} AND

GROUP by C

(finally, normalize so that  $\Sigma_c = 1$ , i.e.  $\sigma''$  can effectively be ignored)

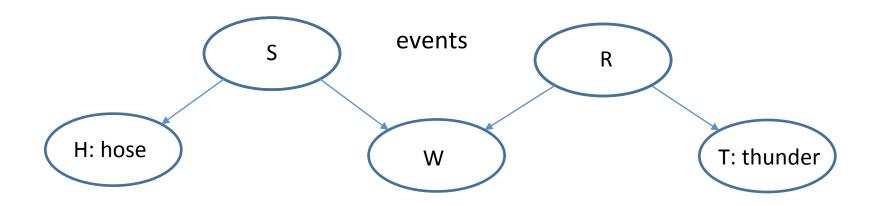
### multiple naïve Bayes classifiers



but ... R and S can happen *together*, so we need 2 classifiers  $P(R|W,T) = \sigma_1 p(W|C) p(T|C)$  $P(S|H,W) = \sigma_2 p(H|C) p(W|C)$ 

but ... W is the same observation ...

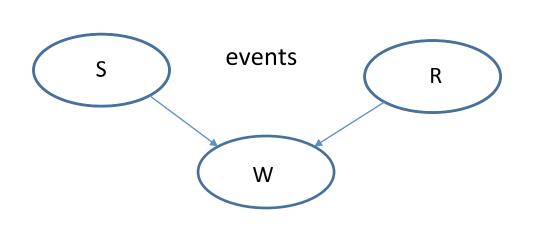
## Bayesian network



P(R|H,W,T,S) = p(H,W,T,S|R) [p(R)/p(H,W,T,S)]  $p(R,H,W,T,S) = p(H,W,T,S|R) p(R) = \sigma p(H,W,T,S|R)$ assumption – independence of features H, T, W| S,R =>  $p(R,H,W,T,S) = \sigma p(H,W,T,S|R) = \sigma p(H|S,R) p(W|S,R) p(T|S,R)$ But ... and this is tricky ... H,R and S,T also independent  $p(R,H,W,T,S) = \sigma p(H|S) p(W|S,R) p(T|R)$ 

once we have the joint – "sum out everything but R" – SQL!

#### simple example



CPT
p(W|S,R)
not joint!

W	S	R	P
У	У	У	.9
У	У	n	.7
У	n	У	.8
У	n	n	.1
n	n	n	.9
n	n	У	.2
n	У	n	.3
n	У	У	.1

$$P(W,R,S) = p(W|S,R) p(S) p(R) \square$$

evidence<sub>1</sub>: "grass is wet", W=y

$$P(R|W) = \Sigma_S P(W,R,S) e^{W=y} = \Sigma_S \sigma P(W|R,S) e^{W=y}$$
 in SQL:

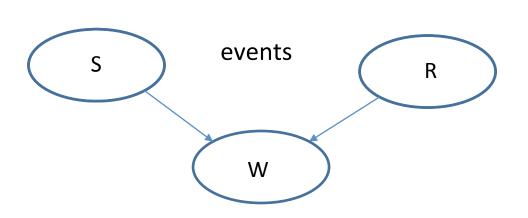
SELECT R, SUM(P) FROM T WHERE W=Y GROUP BY R

normalizing so that sum is 1:

$$p(R=y|W=y) = 1.7/(1.7+.8) = .68$$
, i.e. 68%

W	R	Р
У	У	1.7
У	n	.8

#### example continued: "explaining away" effect



evidence<sub>1</sub>: "grass is wet", W=y

AND evidence<sub>2</sub>: "sprinkler on", S=y

 $P(R|W,S) = P(W,R,S) e^{W=y,S=y} = p(R) P(W|R,S) e^{W=y,S=y}$  in SQL:

SELECT R, SUM(P) FROM T WHERE W=Y, S=y GROUP BY R

normalizing so that sum is 1:

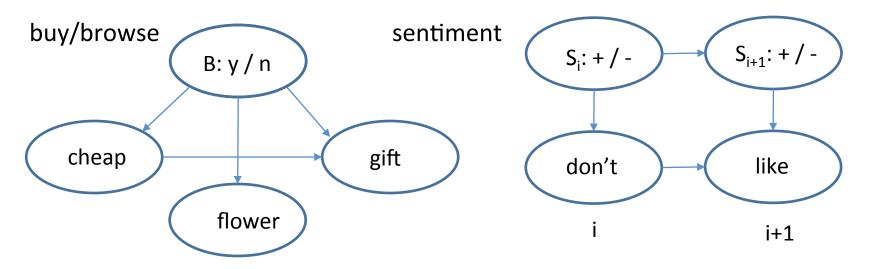
p(R=y|W=y,S=Y) = .9/1.6 = .56, i.e. 56%

less than the earlier 68% - belief propagation

W	S	R	Р	
У	У	У	.9	
У	У	n	.7	
У	n	У	.8	
У	n	n	.1	
n	n	n	.9	
n	n	У	.2	
n	У	n	.3	
n	У	У	.1	
<sup>/=y,S=y</sup> in SQL:				
ROUP BY R				
<b>\</b> \/	D	D		

У

#### Bayes nets: beyond independent features



if 'cheap' and 'gift' are *not* independent,  $P(G|C,B) \neq P(G|B)$  (or use P(C|G,B), depending on the order in which we *expand* P(G,C,B))

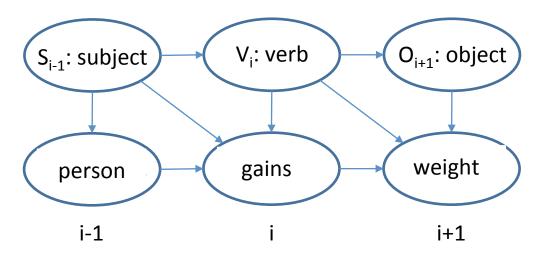
"I don't like the course" and "I like the course; don't complain!"

first, we might include "don't" in our list of features (also "not" ...)

still − might not be able to disambiguate: need *positional order*  $P(x_{i+1}|x_i, S)$  for each position *i*: hidden markov model (HMM)

we may also need to accommodate 'holes', e.g.  $P(x_{i+k}|x_i, S)$ 

#### where do facts come from? learning from text



suppose we want to learn *facts* of the form <subject, verb, object> from text single class variable is not enough; (i.e. we have many  $y_j$  in data [Y,X]) further, positional order is important, so we can use a (different) HMM .. e.g. we need to know  $P(x_i | x_{i-1}, S_{i-1}, V_i)$ 

whether 'kill' following 'antibiotics' is a verb will depend on whether 'antibiotics' is a subject more apparent for the case <person, gains, weight>, since 'gains' can be a verb or a noun problem reduces to estimating *all* the a-posterior probabilities  $P(S_{i-1}, V_i, O_{i+1})$  for every i, and also allowing 'holes' (i.e.,  $P(S_{i-k}, V_i, O_{i+p})$ ) and find the *best* facts from a collection of text? .... many solutions; apart from HMMs - CRFs after finding all facts from lots of text, we cull using support, confidence, etc.

### open information extraction

Cyc (older, semi-automated): 2 billion facts

Yago – largest to date: 6 billion facts, linked i.e., a graph

e.g. <Albert Einstein, wasBornIn, Ulm>

Watson – uses facts culled from the web internally

REVERB – recent, lightweight: 15 million S,V,O triples

- e.g. <potatoes, are also rich in, vitamin C>
- 1. part-of-speech tagging using NLP classifiers (trained on labeled corpora)
- 2. focus on verb-phrases; identify nearby noun-phrases
- 3. prefer proper nouns, especially if they occur often in other facts
- 4. extract more than one fact if possible:

"Mozart was born in Salzburg, but moved to Vienna in 1781" yields

<Mozart, moved to, Vienna>, in addition to <Mozart, was born in, Salzburg>

#### belief networks: learning, logic, big-data & Al

- network structure can be learned from data
- applications in [genomic] medicine
  - medical diagnosis
  - gene-expression networks
  - how do phenotype traits arise from genes
- logic and uncertainty
  - belief networks bridging the gap:
  - (Pearl Turing award; Markov logic n/w ...)
- big-data
  - inference can be done using SQL map-reduce works!
- hidden-agenda:
  - deep belief networks
  - linked to connectionist models of brain

#### recap and preview

search is not enough for Q&A: reasoning logic and semantic web

... but there are limits, fundamental + practicalreasoning under uncertainty Bayesian inference using SQL

... Bayesian networks and PGMs in general

#### Next few weeks:

next week (7) – 1 programming assignment lecture videos only to explain .... but start preparing week 8 (final lecture week) – "predict" putting everything together! 4<sup>th</sup> prog assgn.

week 9 complete all assignments + final exam