# Stefan Vigerske, Humboldt University Berlin, Germany

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# 1 Introduction

COIN-OR (COmputational INfrastructure for Operations Research, http://www.coin-or.org) is an initiative to spur the development of open-source software for the operations research community [22]. One of the projects hosted at COIN-OR is the GAMSlinks project (https://projects.coin-or.org/GAMSlinks). It is dedicated to the development of interfaces between GAMS and open source solvers. Some of these links and solvers have also found their way into the regular GAMS distribution. With the availability of source code for the GAMSlinks the user is not limited to the out of the box solvers that come with a regular GAMS distribution, but can extend and build these interfaces by themselves.

Available solvers and tools include:

- BONMIN: Basic Open-source Nonlinear Mixed Integer programming (model types: LP, RMIP, MIP, DNLP, NLP, RMINLP, MINLP, QCP, RMIQCP, MIQCP)
- CBC: COIN-OR Branch and Cut (model types: LP, RMIP, MIP)
- COUENNE: Convex Over and Under Envelopes for Nonlinear Estimation (model types: LP, RMIP, MIP, DNLP, NLP, RMINLP, MINLP, QCP, RMIQCP, MIQCP)
- IPOPT: Interior Point Optimizer (model types: LP, RMIP, DNLP, NLP, RMINLP, QCP, RMIQCP)
- OS: Optimization Services (model types: LP, RMIP, MIP, DNLP, NLP, RMINLP, MINLP, QCP, RMIQCP, MIQCP)
- OSICPLEX, OSIGUROBI, OSIMOSEK, OSISOPLEX, OSIXPRESS: Open Solver Interface (model types: LP, RMIP, MIP)

For more information see the COIN-OR/GAMSlinks web site at https://projects.coin-or.org/GAMSlinks.

# 2 BONMIN and BONMINH

BONMIN (Basic Open-source Nonlinear Mixed Integer programming) is an open-source solver for mixed-integer nonlinear programming (MINLPs). The code has been developed as part of a collaboration between Carnegie Mellon University and IBM Research. The COIN-OR project leader for BONMIN is Pierre Bonami.

BONMIN implements six different algorithms for solving MINLPs:

• B-BB (**default**): a simple branch-and-bound algorithm based on solving a continuous nonlinear program at each node of the search tree and branching on integer variables [18]; this algorithm is similar to the one implemented in the solver SBB

- B-OA: an outer-approximation based decomposition algorithm based on iterating solving and improving of a MIP relaxation and solving NLP subproblems [13, 14]; this algorithm is similar to the one implemented in the solver DICOPT
- B-QG: an outer-approximation based branch-and-cut algorithm based on solving a continuous linear program at each node of the search tree, improving the linear program by outer approximation, and branching on integer variables [25].
- B-Hyb: a branch-and-bound algorithm which is a hybrid of B-BB and B-QG and is based on solving either a continuous nonlinear or a continuous linear program at each node of the search tree, improving the linear program by outer approximation, and branching on integer variables [12]
- B-ECP: a Kelley's outer-approximation based branch-and-cut algorithm inspired by the settings used in the solver FILMINT [1]
- B-iFP: an iterated feasibility pump algorithm [8]

The algorithms are exact when the problem is **convex**, otherwise they are heuristics.

For convex MINLPs, experiments on a reasonably large test set of problems have shown that B-Hyb is the algorithm of choice (it solved most of the problems in 3 hours of computing time). Nevertheless, there are cases where B-OA (especially when used with CPLEX as MIP subproblem solver) is much faster than B-Hyb and others where B-BB is interesting. B-QG and B-ECP corresponds mainly to a specific parameter setting of B-Hyb but they can be faster in some cases. B-iFP is more tailored at finding quickly good solutions to very hard convex MINLP. For **nonconvex** MINLPs, it is strongly recommended to use B-BB (the outer-approximation algorithms have not been tailored to treat nonconvex problems at this point). Although even B-BB is only a heuristic for such problems, several options are available to try and improve the quality of the solutions it provides (see below).

NLPs are solved in BONMIN by IPOPT, which uses MUMPS [2, 3] as linear solver. In the commercially licensed GAMS/BONMINH version, also the linear solvers MA27, MA57, and MA86 from the Harwell Subroutines Library (HSL) are available in IPOPT. In this case, the default linear solver in IPOPT is MA27.

For more information we refer to [8, 9, 10, 12] and the BONMIN web site https://projects.coin-or.org/Bonmin. Most of the BONMIN documentation in this section is taken from the BONMIN manual [11].

# 2.1 Model requirements

BONMIN can handle mixed-integer nonlinear programming models which functions should be twice continuously differentiable. The BONMIN link in GAMS supports continuous, binary, and integer variables, special ordered sets, branching priorities, but no semi-continuous or semi-integer variables (see chapter 17.1 of the GAMS User's Guide).

If GAMS/BONMIN is called for a model with only continuous variables, the interface switches over to IPOPT. If GAMS/BONMIN is called for a model with only linear equations, the interface switches over to CBC.

# 2.2 Usage

The following statement can be used inside your GAMS program to specify using BONMIN:

```
Option MINLP = BONMIN; { or Option MIQCP = BONMIN; }
```

This statement should appear before the Solve statement. If BONMIN was specified as the default solver during GAMS installation, the above statement is not necessary.

To use BONMINH, one should use the statement

```
Option MINLP = BONMINH; { or Option MIQCP = BONMINH; }
```

GAMS/BONMIN currently does not support the GAMS Branch-and-Cut-and-Heuristic (BCH) Facility. If you need to use GAMS/BONMIN with BCH, please consider to use a GAMS system of version  $\leq 23.3$ , available at http://www.gams.com/download/download\_old.htm.

# 2.2.1 Specification of Options

A BONMIN options file contains both IPOPT and BONMIN options, for clarity all BONMIN options should be preceded with the prefix "bonmin.". The scheme to name option files is the same as for all other GAMS solvers. Specifying optfile=1 let GAMS/BONMIN read bonmin.opt, optfile=2 corresponds to bonmin.op2, and so on. The format of the option file is the same as for IPOPT (see Section 5.2.2).

The most important option in BONMIN is the choice of the solution algorithm. This can be set by using the option named bonmin.algorithm which can be set to B-BB, B-OA, B-QG, B-Hyb, B-ECP, or B-iFP (its default value is B-BB). Depending on the value of this option, certain other options may be available or not, cf. Section 2.3.

An example of a bonmin opt file is the following:

```
bonmin.algorithm B-Hyb
bonmin.oa_log_level 4
print_level 6
```

This sets the algorithm to be used to the hybrid algorithm, the level of outer approximation related output to 4, and sets the print level for IPOPT to 6.

GAMS/BONMIN understands currently the following GAMS parameters: reslim (time limit), iterlim (iteration limit), nodlim (node limit), cutoff, optca (absolute gap tolerance), and optcr (relative gap tolerance). One can set them either on the command line, e.g. nodlim=1000, or inside your GAMS program, e.g. Option nodlim=1000;. Further, under Linux and Windows, the option threads can be used to control the number of threads used in the linear algebra routines of IPOPT.

#### 2.2.2 Passing options to local search based heuristics and OA generators

Several parts of the algorithms in BONMIN are based on solving a simplified version of the problem with another instance of BONMIN: Outer Approximation Decomposition (called in B-Hyb at the root node) and Feasibility Pump for MINLP (called in B-Hyb or B-BB at the root node), RINS, RENS, Local Branching.

In all these cases, one can pass options to the sub-algorithm used through the option file. The basic principle is that the "bonmin." prefix is replaced with a prefix that identifies the sub-algorithm used:

- to pass options to Outer Approximation Decomposition: oa\_decomposition.,
- to pass options to Feasibility Pump for MINLP: pump\_for\_minlp.,
- to pass options to RINS: rins.,
- to pass options to RENS: rens.,
- to pass options to Local Branching: local\_branch.

For example, to run a maximum of 60 seconds of feasibility pump (FP) for MINLP until 6 solutions are found at the beginning of the hybrid algorithm, one sets the following options:

```
bonmin.algorithm B-Hyb
bonmin.pump_for_minlp yes # tells to run FP for MINLP
pump_for_minlp.time_limit 60 # set a time limit for the pump
pump_for_minlp.solution_limit 6 # set a solution limit
```

Note that the actual solution and time limit will be the minimum of the global limits set for BONMIN.

A slightly more complicated set of options may be used when using RINS. Say for example that one wants to run RINS inside B-BB. Each time RINS is called one wants to solve the small-size MINLP generated using B-QG (one may run any algorithm available in BONMIN for solving an MINLP) and wants to stop as soon as B-QG found one solution. To achieve this, one sets the following options

bonmin.algorithm B-BB bonmin.heuristic\_rins yes rins.algorithm B-QG rins.solution\_limit 1

This example shows that it is possible to set any option used in the sub-algorithm to be different than the one used for the main algorithm.

In the context of outer-approximation (OA) and feasibility pump for MINLP, a standard MILP solver is used. Several options are available for configuring this MILP solver. BONMIN allows a choice of different MILP solvers through the option bonmin.milp\_solver. Values for this option are: Cbc\_D which uses CBC with its default settings, Cbc\_Par which uses a version of CBC that can be parameterized by the user, and Cplex which uses CPLEX with its default settings. The options that can be set in Cbc\_Par are the number of strong-branching candidates, the number of branches before pseudo costs are to be trusted, and the frequency of the various cut generators, c.f. Section 2.3 for details. To use the Cplex option, a valid CPLEX licence (standalone or GAMS/CPLEX) is required.

#### 2.2.3 Getting good solutions to nonconvex problems

To solve a problem with nonconvex constraints, one should only use the branch-and-bound algorithm B-BB.

A few options have been designed in BONMIN specifically to treat problems that do not have a convex continuous relaxation. In such problems, the solutions obtained from IPOPT are not necessarily globally optimal, but are only locally optimal. Also the outer-approximation constraints are not necessarily valid inequalities for the problem. No specific heuristic method for treating nonconvex problems is implemented yet within the OA framework. But for the pure branch-and-bound B-BB, a few options have been implemented while having in mind that lower bounds provided by IPOPT should not be trusted and with the goal of trying to get good solutions. Such options are at a very experimental stage.

First, in the context of nonconvex problems, IPOPT may find different local optima when started from different starting points. The two options num\_resolve\_at\_root and num\_resolve\_at\_node allow for solving the root node or each node of the tree, respectively, with a user-specified number of different randomly-chosen starting points, saving the best solution found. Note that the function to generate a random starting point is very naïve: it chooses a random point (uniformly) between the bounds provided for the variable. In particular if there are some functions that can not be evaluated at some points of the domain, it may pick such points, and so it is not robust in that respect.

Secondly, since the solution given by IPOPT does not truly give a lower bound, the fathoming rule can be changed to continue branching even if the solution value to the current node is worse than the best-known solution. This is achieved by setting allowable\_gap and allowable\_fraction\_gap and cutoff\_decr to negative values.

#### 2.2.4 IPOPT options changed by BONMIN

IPOPT has a very large number of options, see Section 5.5 to get a complete description. To use IPOPT more efficiently in the context of MINLP, BONMIN changes some IPOPT options from their default values, which may help to improve IPOPT's warm-starting capabilities and its ability to prove quickly that a subproblem is infeasible. These are settings that IPOPT does not use for ordinary NLP problems. Note that options set by the user in an option file will override these settings.

- mu\_strategy and mu\_oracle are set, respectively, to adaptive and probing by default. These are strategies in IPOPT for updating the barrier parameter. They were found to be more efficient in the context of MINLP.
- gamma\_phi and gamma\_theta are set to  $10^{-8}$  and  $10^{-4}$  respectively. This has the effect of reducing the size of the filter in the line search performed by IPOPT.
- required\_infeasibility\_reduction is set to 0.1. This increases the required infeasibility reduction when IPOPT enters the restoration phase and should thus help to detect infeasible problems faster.
- expect\_infeasible\_problem is set to yes, which enables some heuristics to detect infeasible problems faster.
- warm\_start\_init\_point is set to yes when a full primal/dual starting point is available (generally for all the optimizations after the continuous relaxation has been solved).
- print\_level is set to 0 by default to turn off IPOPT output (except for the root node, which print level is controlled by the BONMIN option nlp\_log\_at\_root).

• bound\_relax\_factor is set to  $10^{-10}$ . All of the bounds of the problem are relaxed by this factor. This may cause some trouble when constraint functions can only be evaluated within their bounds. In such cases, this option should be set to 0.

# 2.3 Detailed Options Description

The following tables give the list of options together with their types, default values, and availability in each of the main algorithms. The column labeled 'Cbc\_Par' indicates the options that can be used to parametrize the MLIP subsolver in the context of OA and FP.

Table 26.1: List of options and compatibility with the different algorithms.

Option	type	default	B-BB	B-OA	B-QG	B-Hyb	В-Еср	B-iFP	Cbc_Par	
Algorithm choice										
algorithm	string	B-BB	✓	<b>√</b>	✓	✓	<b>√</b>	<b>√</b>	<b>√</b>	
Branch-and-bound options										
allowable_fraction_gap	Q	GAMS optcr	✓	✓	✓	✓	✓	✓	<b>√</b>	
allowable_gap	Q	GAMS optca	$\checkmark$	✓	$\checkmark$	✓	✓	✓	✓	
cutoff	Q	GAMS cutoff	✓	✓	$\checkmark$	✓	✓	✓	✓	
cutoff_decr	Q	$10^{-5}$	✓	✓	$\checkmark$	✓	✓	✓	✓	
enable_dynamic_nlp	string	no	✓	-	_	_	_	_	_	
integer_tolerance	Q	$10^{-6}$	$\checkmark$	✓	$\checkmark$	✓	✓	✓	✓	
iteration_limit	$\mathbb{Z}$	GAMS iterlim	$\checkmark$	✓	$\checkmark$	✓	✓	✓	✓	
nlp_failure_behavior	string	stop	$\checkmark$	-	_	_	_	_	_	
node_comparison	string	best-bound	$\checkmark$	✓	$\checkmark$	✓	✓	✓	_	
node_limit	$\mathbb{Z}$	GAMS nodlim	$\checkmark$	✓	$\checkmark$	✓	✓	✓	✓	
num_cut_passes	$\mathbb{Z}$	1	_	-	$\checkmark$	✓	✓	_	_	
num_cut_passes_at_root	$\mathbb{Z}$	20	_	-	$\checkmark$	✓	✓	_	_	
number_before_trust	$\mathbb{Z}$	8	$\checkmark$	✓	$\checkmark$	✓	✓	✓	✓	
number_strong_branch	$\mathbb{Z}$	20	$\checkmark$	✓	$\checkmark$	✓	✓	✓	✓	
random_generator_seed	$\mathbb{Z}$	0	$\checkmark$	✓	$\checkmark$	✓	✓	✓	✓	
read_solution_file	string	no	$\checkmark$	✓	$\checkmark$	✓	✓	✓	✓	
solution_limit	$\mathbb{Z}$	∞	$\checkmark$	✓	$\checkmark$	✓	✓	✓	✓	
time_limit	Q	GAMS reslim	$\checkmark$	✓	$\checkmark$	✓	✓	✓	✓	
tree_search_strategy	string	probed-dive	$\checkmark$	✓	$\checkmark$	✓	✓	✓	_	
variable_selection	string	strong-branching	$\checkmark$	-	$\checkmark$	✓	✓	_	_	
	ECP	cuts generation	"	'				1		
ecp_abs_tol	Q	$10^{-6}$	-	-	<b>√</b>	✓	_	_	_	
ecp_max_rounds	$\mathbb{Z}$	5	-1	-	$\checkmark$	✓	_	_	_	
ecp_probability_factor	Q	10	-	-	$\checkmark$	✓	_	_	_	
ecp_rel_tol	Q	0	_	-	$\checkmark$	✓	_	_	_	
filmint_ecp_cuts	$\mathbb{Z}$	0	-	-	$\checkmark$	✓	_	_	_	
Feasibility checker using OA cuts										
feas_check_cut_types	string	outer-approx	-	-	<b>√</b>	✓	<b>√</b>	_	_	
feas_check_discard_policy	string	detect-cycles	_	-	$\checkmark$	✓	✓	_	_	
generate_benders_after_so_many_oa	$\mathbb{Z}$	5000	-	-	$\checkmark$	✓	✓	_	_	
	MIL	P Solver								
cpx_parallel_strategy	$\mathbb{Z}$	0	-	-	_	_	_	_	<b>√</b>	
	•	1					contin	ued on r	ext page	

Option	type	default	B-BB	B-OA	B-QG	B-Hyb	В-Еср	B-iFP	Cbc_Par
milp_solver	string	Cbc_D	_	_		_	_	_	<b>√</b>
milp_strategy	string	solve_to_optimality	_	_	_	_	_	_	<b>√</b>
number_cpx_threads	$\mathbb{Z}$	0	_	_	_	_	_	_	<b>√</b>
MILP cutting planes in hybrid algorithm (B-Hyb)									
2mir_cuts	$\mathbb{Z}$	0		<b>√</b>	<u>√</u>	<b>√</b>	<b>√</b>	<b>√</b>	<b>√</b>
Gomory_cuts	$\mathbb{Z}$	-5	_	·	✓	· /	· ✓	<b>√</b>	· /
clique_cuts	$\mathbb{Z}$	-5	_	·	✓	· /	· ✓	<b>√</b>	· /
cover_cuts	$\mathbb{Z}$	0	_	\ \ \	✓	1	<b>√</b>	<b>√</b>	\ \frac{1}{\sqrt{1}}
flow_cover_cuts	$\mathbb{Z}$	-5	_	·	· ✓	· /	✓	√ ·	· /
lift_and_project_cuts	$\mathbb{Z}$	0	_	·	<ul><li>✓</li></ul>	· /	· ✓	<b>√</b>	· /
mir_cuts	$\mathbb{Z}$	-5	_	√	✓	· /	· ✓	<b>√</b>	· /
reduce_and_split_cuts	$\mathbb{Z}$	0	_	· /	· /	· /	·	<b>√</b>	· /
		LP Heuristics		,	•		,	,	
feasibility_pump_objective_norm	$\mathbb{Z}$	1	<b>√</b>	<b>√</b>	<b>√</b>	<b>√</b>	<b>√</b>	<b>√</b>	_
fp_pass_infeasible	string	no	<b>√</b>	<b>,</b>	<b>,</b> ✓	<b>,</b>	· /	<b>√</b>	<b>√</b>
heuristic_RINS	string	no	· /	<b>,</b>	<b>,</b> ✓	, ,	· /	<b>√</b>	.
heuristic_dive_MIP_fractional	string	no	· /	·	·	·	<b>√</b>	· /	_
heuristic_dive_MIP_vectorLength	string	no	·	· /	· ✓	· /	· /	· ✓	_
heuristic_dive_fractional	string	no	<i>'</i>	<i>'</i>	<b>,</b> ✓	· /	· /	· /	_
heuristic_dive_vectorLength	string	no	<i>'</i>	· /	<i>'</i>	· /	<b>√</b>	· /	_
heuristic_feasibility_pump	string	no	<i>'</i>	<b>,</b>	<b>,</b> ✓	· /	<b>√</b>	<b>√</b>	_
pump_for_minlp	string	no	· /	<b>,</b>	· /	./	· /	<b>√</b>	_
pump-ror-immp		interface	•	•	•	•	•		
solvefinal	string	yes	<b>√</b>	<b>√</b>	<b>√</b>	1	1	<b>√</b>	<i></i>
warm_start	string	none	<b>√</b>	_	_	_	_	_	<b>'</b> _
Wallingstart		solution robustness	<u> </u>						
max_consecutive_failures	$\mathbb{Z}$	10	<b>√</b>	_	_	_	_	_	_
max_random_point_radius	Q	100000	<b>√</b>	_	_	_	_	_	_
num_iterations_suspect	$\mathbb{Z}$	-1	<b>√</b>	./	./	./	./	./	
num_retry_unsolved_random_point	$\mathbb{Z}$	0	<i>'</i>	./	./	./	./	./	
random_point_perturbation_interval	Q		<b>√</b>	_	_	_	_	_	_
random_point_type	string	Jon	<b>√</b>	_	_	_	_	_	_
resolve_on_small_infeasibility	O	0	<b>√</b>	./	./	./	./	./	
resorve_on_sman_smeasterney	~	solves in hybrid algo		R-Hvh)	•	•		, , , , , , , , , , , , , , , , , , ,	<u> </u>
nlp_solve_frequency		10	_		_	<b>√</b>	_	_	
nlp_solve_max_depth	$\mathbb{Z}$	10			_	<b>√</b>	_		
nlp_solves_per_depth	Q	$10^{100}$	_	_	_	<b>√</b>	_	_	
mp_sorves_per_depth	-	convex problems		_		V	_	_	
coeff_var_threshold	Q	0.1	<b>√</b>	_	_	_	_	_	
dynamic_def_cutoff_decr	string	no	<b>∨</b> ✓	_	_	_	_	_	_
first_perc_for_cutoff_decr	Sumg	$\begin{vmatrix} -0.02 \end{vmatrix}$	<b>∨</b> ✓	_	_	_	_	_	_
max_consecutive_infeasible	$\mathbb{Z}$	-0.02	<b>∨</b> ✓	_	_	_	_	_	_
num_resolve_at_infeasibles	$\mathbb{Z}$	$\begin{vmatrix} 0 \\ 0 \end{vmatrix}$	<b>∨</b> √		_	_	_	_	_
num_resolve_at_inieasioles	$\mathbb{Z}$		<b>∨</b> ✓	_	_	_	_	_	_
num_resolve_at_node	$\mathbb{Z}$		<b>√</b>	_	_	_	_	_	_
second_perc_for_cutoff_decr	Q Q	$\begin{vmatrix} & & & & & & & & & & & & & & & & & & &$	<b>√</b>	_	_	_	_	_	_
second_pere_ror_cutorr_decr	•	er Approximation Dec	·	ion (R-C	-	_	_	_	_
	Jule	1 1 1 pproximation Dec	omposit	1011 ( <b>D</b> -C	<i>(</i> 11)		contin	ued on r	ext page
							COIIIII	iucu OII I	icat page

Option	type	default	B-BB	B-OA	B-QG	В-Нур	В-Еср	B-iFP	Cbc_Par
oa_decomposition	string	no	_	-	✓	✓	✓	_	_
Outer Approximation cuts generation									
add_only_violated_oa	string	no	_	✓	✓	✓	<b>√</b>	✓	<b>√</b>
oa_cuts_scope	string	global	_	✓	$\checkmark$	$\checkmark$	✓	✓	✓
oa_rhs_relax	$\mathbb{Q}$	$10^{-8}$	_	✓	$\checkmark$	$\checkmark$	✓	✓	✓
tiny_element	$\mathbb{Q}$	$10^{-8}$	_	✓	$\checkmark$	$\checkmark$	✓	✓	✓
very_tiny_element	$\mathbb{Q}$	$10^{-17}$	_	✓	$\checkmark$	$\checkmark$	✓	✓	✓
	Outp	out							
bb_log_interval	$\mathbb{Z}$	100	✓	✓	✓	✓	✓	✓	<b>√</b>
bb_log_level	$\mathbb{Z}$	1	✓	✓	$\checkmark$	$\checkmark$	✓	✓	✓
fp_log_frequency	$\mathbb{Q}$	100	_	_	$\checkmark$	$\checkmark$	_	_	_
fp_log_level	$\mathbb{Z}$	1	_	_	$\checkmark$	$\checkmark$	_	_	_
lp_log_level	$\mathbb{Z}$	0	_	✓	$\checkmark$	$\checkmark$	✓	✓	✓
milp_log_level	$\mathbb{Z}$	0	_	_	_	_	_	_	✓
nlp_log_at_root	$\mathbb{Z}$	5	✓	✓	$\checkmark$	$\checkmark$	✓	✓	_
nlp_log_level	$\mathbb{Z}$	1	✓	✓	$\checkmark$	$\checkmark$	✓	$\checkmark$	✓
oa_cuts_log_level	$\mathbb{Z}$	0	_	✓	$\checkmark$	$\checkmark$	✓	✓	✓
oa_log_frequency	$\mathbb{Q}$	100	✓	-	_	$\checkmark$	✓	_	-
oa_log_level	$\mathbb{Z}$	1	✓	-	_	$\checkmark$	✓	_	-
print_funceval_statistics	string	no	✓	✓	$\checkmark$	$\checkmark$	✓	$\checkmark$	✓
solvetrace	string		✓	✓	$\checkmark$	$\checkmark$	✓	$\checkmark$	✓
solvetracenodefreq	$\mathbb{Z}$	100	✓	✓	$\checkmark$	$\checkmark$	✓	$\checkmark$	✓
solvetracetimefreq	$\mathbb{Q}$	5	✓	$\checkmark$	$\checkmark$	$\checkmark$	✓	$\checkmark$	✓
	Stroi	ng branching	setup						
candidate_sort_criterion	string	best-ps-cost	<b>✓</b>	<b>√</b>	$\checkmark$	<b>√</b>	✓	<b>√</b>	-
maxmin_crit_have_sol	$\mathbb{Q}$	0.1	✓	✓	$\checkmark$	$\checkmark$	✓	$\checkmark$	_
maxmin_crit_no_sol	$\mathbb{Q}$	0.7	✓	✓	$\checkmark$	$\checkmark$	✓	$\checkmark$	_
min_number_strong_branch	$\mathbb{Z}$	0	✓	✓	$\checkmark$	$\checkmark$	✓	$\checkmark$	-
number_before_trust_list	$\mathbb{Z}$	0	✓	✓	$\checkmark$	$\checkmark$	✓	✓	_
number_look_ahead	$\mathbb{Z}$	0	✓	✓	$\checkmark$	$\checkmark$	✓	_	_
number_strong_branch_root	$\mathbb{Z}$	∞	✓	✓	$\checkmark$	✓	✓	✓	_
setup_pseudo_frac	$\mathbb{Q}$	0.5	✓	✓	$\checkmark$	$\checkmark$	✓	✓	_
trust_strong_branching_for_pseudo_cost	string	yes	✓	✓	✓	✓	✓	✓	_

In the following we give a detailed list of BONMIN options. The value on the right denotes the default value.

#### Algorithm choice

algorithm (B-BB, B-OA, B-QG, B-Hyb, B-Ecp, B-iFP)

Choice of the algorithm.

This will preset some of the options of bonmin depending on the algorithm choice.

B-BB simple branch-and-bound algorithm,

B-OA OA Decomposition algorithm,

B-QG Quesada and Grossmann branch-and-cut algorithm,

B-Hyb hybrid outer approximation based branch-and-cut,

B-Ecp ecp cuts based branch-and-cut a la FilMINT.

B-iFP Iterated Feasibility Pump for MINLP.

# **Branch-and-bound options**

allowable\_fraction\_gap (real)

0.1

B-BB

Specify the value of relative gap under which the algorithm stops.

Stop the tree search when the gap between the objective value of the best known solution and the best bound on the objective of any solution is less than this fraction of the absolute value of the best known solution value.

allowable\_gap (real)

0

Specify the value of absolute gap under which the algorithm stops.

Stop the tree search when the gap between the objective value of the best known solution and the best bound on the objective of any solution is less than this.

cutoff  $(-10^{100} \le \text{real} \le 10^{100})$ 

 $10^{100}$ 

Specify cutoff value.

cutoff should be the value of a feasible solution known by the user (if any). The algorithm will only look for solutions better than cutoff.

cutoff\_decr  $(-10^{10} \le \text{real} \le 10^{10})$ 

 $10^{-5}$ 

Specify cutoff decrement.

Specify the amount by which cutoff is decremented below a new best upper-bound (usually a small positive value but in non-convex problems it may be a negative value).

enable\_dynamic\_nlp (no, yes)

no

Enable dynamic linear and quadratic rows addition in nlp

integer\_tolerance (0 < real)

 $10^{-6}$ 

Set integer tolerance.

Any number within that value of an integer is considered integer.

iteration\_limit  $(0 \le integer)$ 

 $\infty$ 

Set the cumulated maximum number of iteration in the algorithm used to process nodes continuous relaxations in the branch-and-bound.

value 0 deactivates option.

nlp\_failure\_behavior (stop, fathom)

stop

Set the behavior when an NLP or a series of NLP are unsolved by Ipopt (we call unsolved an NLP for which Ipopt is not able to guarantee optimality within the specified tolerances).

If set to "fathom", the algorithm will fathom the node when Ipopt fails to find a solution to the nlp at that node whithin the specified tolerances. The algorithm then becomes a heuristic, and the user will be warned that the solution might not be optimal.

stop Stop when failure happens.

fathom Continue when failure happens.

node\_comparison (best-bound, depth-first, breadth-first, dynamic, best-guess) best-bound Choose the node selection strategy.

Choose the strategy for selecting the next node to be processed.

best-bound choose node with the smallest bound,

depth-first Perform depth first search,

breadth-first Perform breadth first search,

dynamic Cbc dynamic strategy (starts with a depth first search and turn to best bound after 3 integer feasible solutions have been found).

best-guess choose node with smallest guessed integer solution

 $node\_limit (0 \le integer)$ 

 $\infty$ 

Set the maximum number of nodes explored in the branch-and-bound search.

 $num_cut_passes (0 \le integer)$ 

1

Set the maximum number of cut passes at regular nodes of the branch-and-cut.

 ${\tt num\_cut\_passes\_at\_root}\ (0 \leq integer)$ 

20

Set the maximum number of cut passes at regular nodes of the branch-and-cut.

 $number_before_trust (0 \le integer)$ 

8

Set the number of branches on a variable before its pseudo costs are to be believed in dynamic strong branching. A value of 0 disables pseudo costs.

number\_strong\_branch (0 \le integer)

. . .

20

Choose the maximum number of variables considered for strong branching.

Set the number of variables on which to do strong branching.

random\_generator\_seed  $(-1 \le integer)$ 

42

Set seed for random number generator (a value of -1 sets seeds to time since Epoch).

read\_solution\_file (no, yes)

no

Read a file with the optimal solution to test if algorithms cuts it.

For Debugging purposes only.

solution\_limit  $(0 \le integer)$ 

 $\infty$ 

Abort after that much integer feasible solution have been found by algorithm

value 0 deactivates option

1000

10 - 6

time\_limit  $(0 \le real)$ Set the global maximum computation time (in secs) for the algorithm.

tree\_search\_strategy (top-node, dive, probed-dive, dfs-dive, dfs-dive-dynamic) probed-dive Pick a strategy for traversing the tree

All strategies can be used in conjunction with any of the node comparison functions. Options which affect dfs-dive are max-backtracks-in-dive and max-dive-depth. The dfs-dive won't work in a non-convex problem where objective does not decrease down branches.

top-node Always pick the top node as sorted by the node comparison function

dive Dive in the tree if possible, otherwise pick top node as sorted by the tree comparison function.

probed-dive Dive in the tree exploring two childs before continuing the dive at each level.

dfs-dive Dive in the tree if possible doing a depth first search. Backtrack on leaves or when a prescribed depth is attained or when estimate of best possible integer feasible solution in subtree is worst than cutoff. Once a prescribed limit of backtracks is attained pick top node as sorted by the tree comparison function

dfs-dive-dynamic Same as dfs-dive but once enough solution are found switch to best-bound and if too many nodes switch to depth-first.

variable\_selection (most-fractional, strong-branching, reliability-branching, qp-strong-branching, lp-strong-branching, osi-simple, osi-strong, random) strong-branching Chooses variable selection strategy

most-fractional Choose most fractional variable

strong-branching Perform strong branching

reliability-branching Use reliability branching

qp-strong-branching Perform strong branching with QP approximation

1p-strong-branching Perform strong branching with LP approximation

nlp-strong-branching Perform strong branching with NLP approximation

Specify the frequency (in terms of nodes) at which some a la filmint ecp cuts are generated.

osi-simple Osi method to do simple branching

osi-strong Osi method to do strong branching

random Method to choose branching variable randomly

A frequency of 0 amounts to to never solve the NLP relaxation.

# ECP cuts generation

ecp_abs_tol (0 ≤ real)  Set the absolute termination tolerance for ECP rounds.	10 °
ecp_max_rounds $(0 \le integer)$ Set the maximal number of rounds of ECP cuts.	5
ecp_probability_factor (real) Factor appearing in formula for skipping ECP cuts. Choosing -1 disables the skipping.	10
ecp_rel_tol $(0 \le \text{real})$ Set the relative termination tolerance for ECP rounds.	0
$filmint_ecp_cuts (0 \le integer)$	0

Feasibility checker using OA cuts

feas\_check\_cut\_types (outer-approx, Benders)

outer-approx

Choose the type of cuts generated when an integer feasible solution is found

If it seems too much memory is used should try Benders to use less

outer-approx Generate a set of Outer Approximations cuts.

Benders Generate a single Benders cut.

feas\_check\_discard\_policy (detect-cycles, keep-all, treated-as-normal)

detect-cycles

How cuts from feasibility checker are discarded

Normally to avoid cycle cuts from feasibility checker should not be discarded in the node where they are generated. However Cbc sometimes does it if no care is taken which can lead to an infinite loop in Bonmin (usualy on simple problems). To avoid this one can instruct Cbc to never discard a cut but if we do that for all cuts it can lead to memory problems. The default policy here is to detect cycles and only then impose to Cbc to keep the cut. The two other alternative are to instruct Cbc to keep all cuts or to just ignore the problem and hope for the best

detect-cycles Detect if a cycle occurs and only in this case force not to discard.

keep-all Force cuts from feasibility checker not to be discarded (memory hungry but sometimes better).

treated-as-normal Cuts from memory checker can be discarded as any other cuts (code may cycle then)

 ${\tt generate\_benders\_after\_so\_many\_oa}\ (0 \leq {\tt integer})$ 

5000

Specify that after so many oa cuts have been generated Benders cuts should be generated instead.

It seems that sometimes generating too many oa cuts slows down the optimization compared to Benders due to the size of the LP. With this option we specify that after so many OA cuts have been generated we should switch to Benders cuts.

# **MILP Solver**

 $\texttt{cpx\_parallel\_strategy}\ (-1 \leq integer \leq 1)$ 

0

Strategy of parallel search mode in CPLEX.

-1 = opportunistic, 0 = automatic, 1 = deterministic (refer to CPLEX documentation)

milp\_solver (Cbc\_D, Cbc\_Par, Cplex)

Cbc\_D

Choose the subsolver to solve MILP sub-problems in OA decompositions.

To use Cplex, a valid license is required.

Cbc\_D Coin Branch and Cut with its default

Cbc\_Par Coin Branch and Cut with passed parameters

Cplex IBM Cplex

milp\_strategy (find\_good\_sol, solve\_to\_optimality)

solve\_to\_optimality

Choose a strategy for MILPs.

find\_good\_sol Stop sub milps when a solution improving the incumbent is found

solve\_to\_optimality Solve MILPs to optimality

 $\verb|number_cpx_threads| (0 \le integer)$ 

0

Set number of threads to use with cplex.

(refer to CPLEX documentation)

# MILP cutting planes in hybrid algorithm (B-Hyb)

 $2mir_cuts (-100 \le integer)$ 

0

Frequency (in terms of nodes) for generating 2-MIR cuts in branch-and-cut

If k > 0, cuts are generated every k nodes, if -99 < k < 0 cuts are generated every -k nodes but Cbc may decide to stop generating cuts, if not enough are generated at the root node, if k = -99 generate cuts only at the root node, if k = 0 or 100 do not generate cuts.

Gomory\_cuts  $(-100 \le integer)$ 

-5

Frequency (in terms of nodes) for generating Gomory cuts in branch-and-cut.

See option 2mir\_cuts for a detailed description.

 $\texttt{clique\_cuts}\ (-100 \leq integer)$ 

-5

Frequency (in terms of nodes) for generating clique cuts in branch-and-cut

See option 2mir\_cuts for a detailed description.

cover_cuts $(-100 \le \text{integer})$ Frequency (in terms of nodes) for generating cover cuts in branch-and-cut See option 2mir_cuts for a detailed description.	0
flow_cover_cuts $(-100 \le integer)$ Frequency (in terms of nodes) for generating flow cover cuts in branch-and-cut See option 2mir_cuts for a detailed description.	-5
lift_and_project_cuts $(-100 \le integer)$ Frequency (in terms of nodes) for generating lift-and-project cuts in branch-and-cut See option 2mir_cuts for a detailed description.	0
mir_cuts $(-100 \le \text{integer})$ Frequency (in terms of nodes) for generating MIR cuts in branch-and-cut See option 2mir_cuts for a detailed description.	-5
reduce_and_split_cuts $(-100 \le integer)$ Frequency (in terms of nodes) for generating reduce-and-split cuts in branch-and-cut See option 2mir_cuts for a detailed description.	0
MINLP Heuristics	
$\label{eq:continuous} \mbox{feasibility\_pump\_objective\_norm} \ \ (1 \leq integer \leq 2) \\ \mbox{Norm of feasibility pump objective function}$	1
fp_pass_infeasible (no, yes) Say whether feasibility pump should claim to converge or not	no
no When master MILP is infeasible just bail out (don't stop all algorithm). This is the option for using in B-Hyb yes Claim convergence, numerically dangerous.	
heuristic_RINS (no, yes) if yes runs the RINS heuristic	no
heuristic_dive_MIP_fractional (no, yes) if yes runs the Dive MIP Fractional heuristic	no
heuristic_dive_MIP_vectorLength (no, yes) if yes runs the Dive MIP VectorLength heuristic	no
heuristic_dive_fractional (no, yes) if yes runs the Dive Fractional heuristic	no
heuristic_dive_vectorLength (no, yes) if yes runs the Dive VectorLength heuristic	no
heuristic_feasibility_pump (no, yes) whether the heuristic feasibility pump should be used	no
pump_for_minlp (no, yes) if yes runs FP for MINLP	no
NLP interface	
solvefinal (no, yes) Switch to disable solving MINLP with discrete variables fixed to solution values after solve. If enabled, then the dual values from the resolved NLP are made available in GAMS.	yes
warm_start (none, fake_basis, optimum, interior_point) Select the warm start method This will affect the function getWarmStart(), and as a consequence the warm starting in the various algorithms.	none
none No warm start, just start NLPs from optimal solution of the root relaxation	
fake_basis builds fake basis, useful for cut management in Cbc (warm start is the same as in none)	
optimum Warm start with direct parent optimum	
interior_point Warm start with an interior point of direct parent	

#### **NLP** solution robustness

 $max\_consecutive\_failures$  ( $0 \le integer$ )

10

(temporarily removed) Number n of consecutive unsolved problems before aborting a branch of the tree.

When n > 0, continue exploring a branch of the tree until n consecutive problems in the branch are unsolved (we call unsolved a problem for which Ipopt can not guarantee optimality within the specified tolerances).

max\_random\_point\_radius (0 < real)

100000

Set max value r for coordinate of a random point.

When picking a random point, coordinate i will be in the interval  $[\min(\max(l,-r),u-r), \max(\min(u,r),l+r)]$  (where l is the lower bound for the variable and u is its upper bound)

 $num\_iterations\_suspect (-1 \le integer)$ 

-1

Number of iterations over which a node is considered "suspect" (for debugging purposes only, see detailed documentation). When the number of iterations to solve a node is above this number, the subproblem at this node is considered to be suspect and it will be outputed in a file (set to -1 to deactivate this).

 $num\_retry\_unsolved\_random\_point (0 \le integer)$ 

0

Number k of times that the algorithm will try to resolve an unsolved NLP with a random starting point (we call unsolved an NLP for which Ipopt is not able to guarantee optimality within the specified tolerances).

When Ipopt fails to solve a continuous NLP sub-problem, if k > 0, the algorithm will try again to solve the failed NLP with k new randomly chosen starting points or until the problem is solved with success.

 $random\_point\_perturbation\_interval (0 < real)$ 

1

Amount by which starting point is perturbed when choosing to pick random point by perturbating starting point

random\_point\_type (Jon, Andreas, Claudia)

Jon

method to choose a random starting point

Jon Choose random point uniformly between the bounds

Andreas perturb the starting point of the problem within a prescribed interval

Claudia perturb the starting point using the perturbation radius suffix information

resolve\_on\_small\_infeasibility  $(0 \le real)$ 

0

If a locally infeasible problem is infeasible by less than this, resolve it with initial starting point.

#### NLP solves in hybrid algorithm (B-Hyb)

 $nlp\_solve\_frequency (0 \le integer)$ 

10

Specify the frequency (in terms of nodes) at which NLP relaxations are solved in B-Hyb.

A frequency of 0 amounts to to never solve the NLP relaxation.

 $nlp\_solve\_max\_depth (0 \le integer)$ 

10

Set maximum depth in the tree at which NLP relaxations are solved in B-Hyb.

A depth of 0 amounts to to never solve the NLP relaxation.

 $nlp\_solves\_per\_depth (0 \le real)$ 

 $10^{100}$ 

Set average number of nodes in the tree at which NLP relaxations are solved in B-Hyb for each depth.

# Nonconvex problems

 $coeff_var_threshold (0 \le real)$ 

0.1

Coefficient of variation threshold (for dynamic definition of cutoff\_decr).

dynamic\_def\_cutoff\_decr (no, yes)

no

Do you want to define the parameter cutoff\_decr dynamically?

first\_perc\_for\_cutoff\_decr (real)

-0.02

The percentage used when, the coeff of variance is smaller than the threshold, to compute the cutoff\_decr dynamically.

 ${\tt max\_consecutive\_infeasible}\ (0 \leq integer)$ 

0

Number of consecutive infeasible subproblems before aborting a branch.

Will continue exploring a branch of the tree until "max\_consecutive\_infeasible" consecutive problems are infeasibles by the NLP sub-solver.

 $num\_resolve\_at\_infeasibles (0 \le integer)$ 

0

Number k of tries to resolve an infeasible node (other than the root) of the tree with different starting point.

The algorithm will solve all the infeasible nodes with k different random starting points and will keep the best local optimum found.

 $num\_resolve\_at\_node (0 \le integer)$ 

0

Number k of tries to resolve a node (other than the root) of the tree with different starting point.

The algorithm will solve all the nodes with k different random starting points and will keep the best local optimum found.

 $num\_resolve\_at\_root (0 \le integer)$ 

0

Number *k* of tries to resolve the root node with different starting points.

The algorithm will solve the root node with k random starting points and will keep the best local optimum found.

second\_perc\_for\_cutoff\_decr (real)

-0.05

The percentage used when, the coeff of variance is greater than the threshold, to compute the cutoff\_decr dynamically.

#### **Outer Approximation Decomposition (B-OA)**

 $oa\_decomposition (no, yes)$ 

no

If yes do initial OA decomposition

# **Outer Approximation cuts generation**

add\_only\_violated\_oa (no, yes)

no

Do we add all OA cuts or only the ones violated by current point?

no Add all cuts

yes Add only violated Cuts

oa\_cuts\_scope (local, global)

global

Specify if OA cuts added are to be set globally or locally valid

local Cuts are treated as locally valid

global Cuts are treated as globally valid

oa\_rhs\_relax  $(-0 \le real)$ Value by which to relax OA cut  $10^{-8}$ 

RHS of OA constraints will be relaxed by this amount times the absolute value of the initial rhs if it is  $\geq 1$  (otherwise by this amount).

tiny\_element  $(-0 \le real)$ 

 $10^{-8}$ 

Value for tiny element in OA cut

We will remove "cleanly" (by relaxing cut) an element lower than this.

 $\texttt{very\_tiny\_element}\ (-0 \leq real)$ 

 $10^{-17}$ 

Value for very tiny element in OA cut

Algorithm will take the risk of neglecting an element lower than this.

# Output

 $bb\_log\_interval (0 \le integer)$ 

100

Interval at which node level output is printed.

Set the interval (in terms of number of nodes) at which a log on node resolutions (consisting of lower and upper bounds) is given.

bb\_log\_level  $(0 \le integer \le 5)$ 

1

specify main branch-and-bound log level.

Set the level of output of the branch-and-bound: 0 - none, 1 - minimal, 2 - normal low, 3 - normal high

 ${\tt fp\_log\_frequency}\ (0 < real)$ 

100

display an update on lower and upper bounds in FP every n seconds

 $fp_log_level (0 \le integer \le 2)$ 

1

specify FP iterations log level.

Set the level of output of OA decomposition solver: 0 - none, 1 - normal, 2 - verbose

 $lp\_log\_level (0 \le integer \le 4)$ 

0

specify LP log level. Set the level of output of the linear programming sub-solver in B-Hyb or B-QG: 0 - none, 1 - minimal, 2 - normal low, 3 normal high, 4 - verbose milp\_log\_level  $(0 \le integer \le 4)$ 0 specify MILP solver log level. Set the level of output of the MILP subsolver in OA: 0 - none, 1 - minimal, 2 - normal low, 3 - normal high  $nlp_log_at_root (0 \le integer \le 12)$ 5 Specify a different log level for root relaxtion.  $nlp_log_level (0 \le integer \le 2)$ 1 specify NLP solver interface log level (independent from ipopt print\_level). Set the level of output of the OsiTMINLPInterface: 0 - none, 1 - normal, 2 - verbose 0  $oa_cuts_log_level (0 \le integer)$ level of log when generating OA cuts. 0: outputs nothing, 1: when a cut is generated, its violation and index of row from which it originates, 2: always output violation of the cut. 3: output generated cuts incidence vectors. 100 oa\_log\_frequency (0 < real)display an update on lower and upper bounds in OA every n seconds oa\_log\_level  $(0 \le integer \le 2)$ 1 specify OA iterations log level. Set the level of output of OA decomposition solver: 0 - none, 1 - normal, 2 - verbose print\_funceval\_statistics (no, yes) no Switch to enable printing statistics on number of evaluations of GAMS functions/gradients/Hessian. solvetrace (string) Name of file for writing solving progress information. solvetracenodefreq  $(0 \le integer)$ 100 Frequency in number of nodes for writing solving progress information. giving 0 disables writing of N-lines to trace file 5 solvetracetimefreq  $(0 \le real)$ Frequency in seconds for writing solving progress information. giving 0.0 disables writing of T-lines to trace file Strong branching setup candidate\_sort\_criterion (best-ps-cost, worst-ps-cost, most-fractional, least-fractional) best-ps-cost Choice of the criterion to choose candidates in strong-branching best-ps-cost Sort by decreasing pseudo-cost worst-ps-cost Sort by increasing pseudo-cost most-fractional Sort by decreasing integer infeasibility least-fractional Sort by increasing integer infeasibility 0.1  $maxmin\_crit\_have\_sol (0 \le real \le 1)$ Weight towards minimum in of lower and upper branching estimates when a solution has been found. 0.7  $maxmin\_crit\_no\_sol (0 \le real \le 1)$ Weight towards minimum in of lower and upper branching estimates when no solution has been found yet. 0  $min\_number\_strong\_branch (0 \le integer)$ Sets minimum number of variables for strong branching (overriding trust) 0 number\_before\_trust\_list  $(-1 \le integer)$ Set the number of branches on a variable before its pseudo costs are to be believed during setup of strong branching candidate

list.

The default value is that of "number\_before\_trust"

Proportion of strong branching list that has to be taken from most-integer-infeasible list.

trust\_strong\_branching\_for\_pseudo\_cost (no, yes)

Whether or not to trust strong branching results for updating pseudo costs.

# 3 CBC

CBC (COIN-OR Branch and Cut) is an open-source mixed integer programming solver working with the COIN-OR LP solver CLP and the COIN-OR Cut generator library CGL. The code has been written primarily by John J. Forrest.

For more information we refer to the website of CBC, CGL, and CLP: https://projects.coin-or.org/Cbc, https://projects.coin-or.org/Cgl, https://projects.coin-or.org/Clp. Most of the CBC documentation in the section was copied from the help in the CBC standalone version.

# 3.1 Model requirements

The CBC link in GAMS supports continuous, binary, integer, semicontinuous, semiinteger variables, special ordered sets of type 1 and 2, and branching priorities (see chapter 17.1 of the GAMS User's Guide).

# 3.2 Usage

The following statement can be used inside your GAMS program to specify using CBC

```
Option LP = CBC; { or MIP or RMIP }
```

The above statement should appear before the Solve statement. If CBC was specified as the default solver during GAMS installation, the above statement is not necessary.

There are many parameters which can affect the performance the CBCs Branch and Cut Algorithm. First just try with default settings and look carefully at the log file. Did cuts help? Did they take too long? Look at the output to see which cuts were effective and then do some tuning (see the option cuts). If the preprocessing reduced the size of the problem or strengthened many coefficients then it is probably wise to leave it on. Switch off heuristics which did not provide solutions. The other major area to look at is the search. Hopefully good solutions were obtained fairly early in the search so the important point is to select the best variable to branch on. See whether strong branching did a good job – or did it just take a lot of iterations? Adjust the options strongbranching and trustpseudocosts.

#### 3.2.1 Specification of Options

The GAMS/CBC options file consists of one option or comment per line. An asterisk (\*) at the beginning of a line causes the entire line to be ignored. Otherwise, the line will be interpreted as an option name and value separated by any amount of white space (blanks or tabs). Following is an example options file cbc.opt.

```
cuts root perturbation off
```

It will cause CBC to use cut generators only in the root node and turns off the perturbation of the LP relaxation.

GAMS/CBC currently does not support the GAMS Branch-and-Cut-and-Heuristic (BCH) Facility. If you need to use GAMS/CBC with BCH, please consider to use a GAMS system of version  $\leq 23.3$ , available at http://www.gams.com/download/download old.htm.

# 3.3 Options

Among all CBC options, the following GAMS parameters are currently supported in CBC: reslim, iterlim, nodlim, optca, optcr, cheat, cutoff, threads (only on non-Windows systems).

In the following, we summarize all available CBC options.

# 3.3.1 General Options

reslim resource limit

special options passed unseen to CBC writemps create MPS file for problem

# 3.3.2 LP Options

iterlimiteration limitidiotcrashidiot crashsprintcrashsprint crash

sifting synonym for sprint crash

crash use crash method to get dual feasible

maxfactor maximum number of iterations between refactorizations

crossover crossover to simplex algorithm after barrier

dualpivotdual pivot choice algorithmprimalpivotprimal pivot choice algorithmperturbationperturbation of problem

scaling scaling method

presolve switch for initial presolve of LP how many passes to do in presolve

tol\_dual dual feasibility tolerance
tol\_primal primal feasibility tolerance
tol\_presolve tolerance used in presolve
startalg LP solver for root node

# 3.3.3 MIP Options

threads number of threads to use (available on Unix variants only)

strategy switches on groups of features

mipstart whether it should be tried to use the initial variable levels as initial MIP solution

tol\_integer tolerance for integrality sollim limit on number of solutions

dumpsolutions name of solutions index gdx file for writing alternate solutions

maxsol maximal number of solutions to store during search

strongbranching strong branching

trustpseudocosts after howmany nodes we trust the pseudo costs

coststrategy how to use costs as priorities

nodestrategy how to select nodes preprocess integer presolve

printfrequency frequency of status prints

loglevel CBC loglevel

increment increment of cutoff when new incumbent solvefinal final solve of MIP with fixed discrete variables solvetrace name of trace file for solving information

solvetracenodefreq frequency in number of nodes for writing to solve trace file

solvetracetimefreq frequency in seconds for writing to solve trace file

nodelim node limit node limit

optca absolute stopping tolerance
optcr relative stopping tolerance
cutoff cutoff for objective function value

# 3.3.4 MIP Options for Cutting Plane Generators

cutdepthdepth in tree at which cuts are appliedcut\_passes\_rootnumber of cut passes at root nodecut\_passes\_treenumber of cut passes at nodes in the tree

cuts global switch for cutgenerators

clique Cuts
flow Cover Cuts
gomorycuts
knapsackcuts
liftandprojectcuts

Clique Cuts
Flow Cover Cuts
Gomory Cuts
Knapsack Cover Cuts
Lift and Project Cuts

mircuts Mixed Integer Rounding Cuts

twomircuts Two Phase Mixed Integer Rounding Cuts

probingcuts Probing Cuts

reduceandsplitcuts Reduce and Split Cuts residualcapacitycuts Residual Capacity Cuts

#### 3.3.5 MIP Options for Heuristics

heuristics global switch for heuristics combine solutions combine solutions heuristic

dins distance induced neighborhood search divingrandom turns on random diving heuristic divingcoefficient coefficient diving heuristic divingfractional fractional diving heuristic divingguided guided diving heuristic divinglinesearch line search diving heuristic divingpseudocost pseudo cost diving heuristic vector length diving heuristic divingvectorlength

feaspump feasibility pump

feaspump\_passes number of feasibility passes

greedyheuristic greedy heuristic

localtreesearch local tree search heuristic

naiveheuristics naive heuristics pivotandfix pivot and fix heuristic

randomizedrounding randomized rounding heuristis

rens relaxation enforced neighborhood search rins relaxed induced neighborhood search

roundingheuristic rounding heuristic vubheuristic VUB heuristic

# proximity search heuristic

In the following, we give a detailed description of all available CBC options.

# 3.3.6 General Options

#### reslim (real)

```
Maximum time in seconds. (default = GAMS reslim)
```

# special (string)

This parameter let you specify CBC options which are not supported by the GAMS/CBC interface.

The string value given to this parameter is split up into parts at each space and added to the array of parameters given to CBC (in front of the -solve command). Hence, you can use it like the command line parameters for the CBC standalone version.

# writemps (string)

Write the problem formulation in MPS format. The parameter value is the name of the MPS file.

# 3.3.7 LP Options

# iterlim (integer)

For an LP, this is the maximum number of iterations to solve the LP. For a MIP, this option is ignored.

```
(default = GAMS iterlim)
```

# idiotcrash (integer)

This is a type of 'crash' which works well on some homogeneous problems. It works best on problems with unit elements and right hand sides but will do something to any model. It should only be used before the primal simplex algorithm.

A positive number determines the number of passes that idiotcrash is called.

```
(default = -1)
```

- -1 Let CLP decide by itself whether to use it.
- 0 Switch this method off.

#### sprintcrash (integer)

For long and thin problems this method may solve a series of small problems created by taking a subset of the columns. Cplex calls it 'sifting'. A positive number determines the number of passes that sprintcrash is called.

```
(default = -1)
```

- -1 Let CLP decide by itself whether to use it.
- 0 Switch this method off.

#### sifting (integer)

```
Synonym for sprintcrash. (default = -1)
```

# crash (string)

Determines whether CLP should use a crash algorithm to find a dual feasible basis.

```
(default = off)
```

off Switch off the creation of dual feasible basis by the crash method.

on Switch on the creation of dual feasible basis by the crash method.

solow\_halim Switch on a crash variant due to Solow and Halim.

halim\_solow Switch on a crash variant due to Solow and Halim with modifications of John J. Forrest.

#### maxfactor (integer)

Maximum number of iterations between refactorizations in CLP.

If this is left at the default value of 200 then CLP will guess at a value to use. CLP may decide to refactorize earlier for accuracy.

```
(default = 200)
```

# crossover (integer)

Determines whether CLP should crossover to the simplex algorithm after the barrier algorithm finished.

Interior point algorithms do not obtain a basic solution. This option will crossover to a basic solution suitable for ranging or branch and cut.

```
(default = 1)
```

- 0 Turn off crossover to simplex algorithm after barrier algorithm finished.
- 1 Turn on crossover to simplex algorithm after barrier algorithm finished.

# dualpivot (string)

Choice of the pivoting strategy in the dual simplex algorithm.

```
(default = auto)
```

auto Let CLP use a variant of the steepest choice method which starts like partial, i.e., scans only a subset of the primal infeasibilities, and later changes to full pricing when the factorization becomes denser.

dantzig Let CLP use the pivoting strategy due to Dantzig.

steepest Let CLP use the steepest choice method.

partial Let CLP use a variant of the steepest choice method which scans only a subset of the primal infeasibilities to select the pivot step.

#### primalpivot (string)

Choice of the pivoting strategy in the primal simplex algorithm.

```
(default = auto)
```

auto Let CLP use a variant of the exact devex method.

dantzig Let CLP use the pivoting strategy due to Dantzig.

steepest Let CLP use the steepest choice method.

partial Let CLP use a variant of the exact devex method which scans only a subset of the primal infeasibilities to select the pivot step.

exact Let CLP use the exact devex method.

change Let CLP initially use Dantzig pivot method until the factorization becomes denser.

# perturbation (integer)

Determines whether CLP should perturb the problem before starting. Perturbation helps to stop cycling, but CLP uses other measures for this. However, large problems and especially ones with unit elements and unit right hand sides or costs benefit from perturbation. Normally CLP tries to be intelligent, but you can switch this off.

```
(default = 1)
```

- 0 Turns off perturbation of LP.
- 1 Turns on perturbation of LP.

# scaling (string)

Scaling can help in solving problems which might otherwise fail because of lack of accuracy. It can also reduce the number of iterations. It is not applied if the range of elements is small. Both methods do several passes alternating between rows and columns using current scale factors from one and applying them to the other.

```
(default = auto)
```

off Turns off scaling.

auto Let CLP choose the scaling method automatically. It decides for one of these methods depending on which gives the better ratio of the largest element to the smallest one.

equilibrium Let CLP use an equilibrium based scaling method which uses the largest scaled element.

geometric Let CLP use a geometric based scaling method which uses the squareroot of the product of largest and smallest element.

# presolve (integer)

Presolve analyzes the model to find such things as redundant constraints, constraints which fix some variables, constraints which can be transformed into bounds, etc. For the initial solve of any problem this is worth doing unless you know that it will have no effect.

```
(default = 1)
```

- 0 Turns off the initial presolve.
- 1 Turns on the initial presolve.

#### passpresolve (integer)

Normally Presolve does 5 passes but you may want to do less to make it more lightweight or do more if improvements are still being made. As Presolve will return if nothing is being taken out, you should not normally need to use this fine tuning.

```
(default = 5)
```

# tol\_dual (real)

The maximum amount the dual constraints can be violated and still be considered feasible.

```
(default = 1e-7)
```

# tol\_primal (real)

The maximum amount the primal constraints can be violated and still be considered feasible.

```
(default = 1e-7)
```

# tol\_presolve (real)

The tolerance used in presolve.

```
(default = 1e-8)
```

# startalg (string)

Determines the algorithm to use for an LP or the initial LP relaxation if the problem is a MIP.

```
(default = dual)
```

primal Let CLP use the primal simplex algorithm.

dual Let CLP use the dual simplex algorithm.

barrier Let CLP use a primal dual predictor corrector algorithm.

# 3.3.8 MIP Options

# threads (integer)

This option controls the multithreading feature of CBC.

```
(default = GAMS threads)
```

A number between 1 and 100 sets the number of threads used for parallel branch and bound. A number 100 + n with n between 1 and 100 says that n threads are used to parallelize the branch and bound, but also heuristics such as RINS which do branch and bound on a reduced model also use threads. A number 200 + n with n between 1 and 100 says that n threads are used to parallelize the branch and bound, but also the cut generators at the root node (i.e., before threads are useful) are run in parallel. A number 300 + n with n between 1 and 100 combines the 100 + n and 200 + n options. A number 400 + n with n between 1 and 100 says that n threads are used in sub-trees. Thus, n threads are used to parallelize the branch and bound, but also heuristics use threads and the cut generators at the root node are run in parallel. The 100 + n, 200 + n, and 300 + n options are experimental.

# strategy (integer)

Setting strategy to 1 (the default) uses Gomory cuts using tolerance of 0.01 at root, does a possible restart after 100 nodes if Cbc can fix many variables and activates a diving and RINS heuristic and makes feasibility pump more aggressive.

```
(default = 1)
```

- 0 Use this setting for easy problems.
- 1 This is the default setting.
- 2 Use this setting for difficult problems.

#### mipstart (integer)

This option controls the use of advanced starting values for mixed integer programs. A setting of 1 indicates that the variable level values should be checked to see if they provide an integer feasible solution before starting optimization.

```
(default = 0)
```

- 0 Do not use the initial variable levels.
- 1 Try to use the initial variable levels as a MIP starting solution.

# tol\_integer (real)

For an optimal solution, no integer variable may be farther than this from an integer value.

```
(default = 1e-6)
```

#### sollim (integer)

A limit on number of feasible solutions that CBC should find for a MIP.

```
(default = -1)
```

-1 No limit on the number of feasible solutions.

#### dumpsolutions (string)

The name of a solutions index gdx file for writing alternate solutions found by CBC. The GDX file specified by this option will contain a set called index that contains the names of GDX files with the individual solutions.

# maxsol (integer)

Maximal number of solutions to store during search and to dump into gdx files if dumpsolutions options is set.

```
(default = 100)
```

#### strongbranching (integer)

Determines the number of variables to look at in strong branching.

In order to decide which variable to branch on, the code will choose up to this number of unsatisfied variables and try minimal up and down branches. The most effective one is chosen. If a variable is branched on many times then the previous average up and down costs may be used - see the option trustpseudocosts.

```
(default = 5)
```

#### trustpseudocosts (integer)

Using strong branching computes pseudo-costs. This parameter determines after how many branches for a variable we just trust the pseudo costs and do not do any more strong branching.

```
(default = 5)
```

#### coststrategy (string)

This parameter influence the branching variable selection.

If turned on, then the variables are sorted in order of their absolute costs, and branching is done first on variables with largest cost. This primitive strategy can be surprisingly effective.

```
(default = off)
```

off Turns off a specific cost strategy.

priorities Assigns highest priority to variables with largest absolute cost.

columnorder Assigns the priorities 1, 2, 3,.. with respect to the column ordering.

binaryfirst Handles two sets of priorities such that binary variables get high priority.

binarylast Handles two sets of priorities such that binary variables get low priority.

length Assigns high priority to variables that are at most nonzero.

# nodestrategy (string)

This determines the strategy used to select the next node from the branch and cut tree.

(default = fewest)

hybrid Let CBC do first a breath search on nodes with a small depth in the tree and then switch to choose nodes with fewest infeasibilities.

fewest This will let CBC choose the node with the fewest infeasibilities.

depth This will let CBC always choose the node deepest in tree. It gives minimum tree size but may take a long time to find the best solution.

upfewest This will let CBC choose the node with the fewest infeasibilities and do up branches first.

downfewest This will let CBC choose the node with the fewest infeasibilities and do down branches first.

updepth This will let CBC choose the node deepest in tree and do up branches first.

downdepth This will let CBC choose the node deepest in tree and do down branches first.

# preprocess (string)

This option controls the MIP specific presolve routines. They try to reduce the size of the model in a similar way to presolve and also try to strengthen the model. This can be very useful and is worth trying.

```
(default = on)
```

off Turns off the presolve routines.

on Turns on the presolve routines.

equal Turns on the presolve routines and let CBC turn inequalities with more than 5 elements into equalities (cliques) by adding slack variables.

equalall Turns on the presolve routines and let CBC turn all inequalities into equalities by adding slack variables.

sos This option let CBC search for rows with upper bound 1 and where all nonzero coefficients are 1 and creates special ordered sets if the sets are not overlapping and all integer variables (except for at most one) are in the sets.

trysos This option is similar to sos, but allows any number integer variables to be outside of the sets.

# printfrequency (integer)

Controls the number of nodes that are evaluated between status prints.

```
(default = 0)
```

0 Automatic choice, which is 100 for large problems and 1000 for small problems.

# loglevel (integer)

Amount of output to print by CBC.

```
(default = 1)
```

# increment (real)

A valid solution must be at least this much better than last integer solution.

If this option is not set then it CBC will try and work one out. E.g., if all objective coefficients are multiples of 0.01 and only integer variables have entries in objective then this can be set to 0.01.

```
(default = GAMS cheat)
```

# solvefinal (integer)

whether the MIP with discrete variables fixed to solution values should be solved after CBC finished

```
(default = 1)
```

- 0 Turn off the final LP solve.
- 1 Turn on the final LP solve.

# solvetrace (string)

Name of file for writing solving progress information during solve.

# solvetracenodefreq (integer)

frequency in number of nodes for writing solving progress information

```
(default = 100)
```

# solvetracetimefreq (real)

frequency in seconds for writing solving progress information

```
(default = 5)
```

#### nodelim (integer)

Maximum number of nodes that are considered in the Branch and Bound.

```
(default = GAMS nodlim)
```

# nodlim (integer)

Maximum number of nodes that are considered in the Branch and Bound. This option is overwritten by nodelim, if

```
(default = GAMS nodlim)
```

# optca (real)

Absolute optimality criterion for a MIP. CBC stops if the gap between the best known solution and the best possible solution is less than this value.

```
(default = GAMS \ optca)
```

# opter (real)

Relative optimality criterion for a MIP. CBC stops if the relative gap between the best known solution and the best possible solution is less than this value.

```
(default = GAMS \ optcr)
```

#### cutoff (real)

CBC stops if the objective function values exceeds (in case of maximization) or falls below (in case of minimization) this value.

```
(default = GAMS cutoff)
```

# 3.3.9 MIP Options for Cutting Plane Generators

# cutdepth (integer)

If the depth in the tree is a multiple of cutdepth, then cut generators are applied.

Cut generators may be off, on only at the root, on if they look useful, or on at some interval. Setting this option to a positive value K let CBC call a cutgenerator on a node whenever the depth in the tree is a multiple of K.

```
(default = -1)
```

-1 Does not turn on cut generators because the depth of the tree is a multiple of a value.

#### cut\_passes\_root (integer)

Determines the number of rounds that the cut generators are applied in the root node.

A negative value -n means that n passes are also applied if the objective does not drop.

(default = 100 passes if the MIP has less than 500 columns, 100 passes (but stop if the drop in the objective function value is small) if it has less than 5000 columns, and 20 passes otherwise)

# cut\_passes\_tree (integer)

Determines the number of rounds that the cut generators are applied in the nodes of the tree other than the root node.

A negative value -n means that n passes are also applied if the objective does not drop.

```
(default = 1)
```

# cuts (string)

A global switch to turn on or off the cutgenerators.

This can be used to switch on or off all default cut generators. Then you can set individual ones off or on using the specific options.

```
(default = on)
```

off Turns off all cut generators.

on Turns on all default cut generators and CBC will try them in the branch and cut tree (see the option cutdepth on how to fine tune the behaviour).

root Let CBC generate cuts only at the root node.

ifmove Let CBC use cut generators in the tree if they look as if they are doing some good and moving the objective value.

forceon Turns on all default cut generators and force CBC to use the cut generator at every node.

# cliquecuts (string)

Determines whether and when CBC should try to generate clique cuts. See the option cuts for an explanation on the different values.

Clique cuts are of the form "sum of a set of variables  $\leq 1$ ".

Reference: M. Eso, Parallel branch and cut for set partitioning, Cornell University, 1999.

```
(default = ifmove)
```

#### flowcovercuts (string)

Determines whether and when CBC should try to generate flow cover cuts.

See the option cuts for an explanation on the different values.

The flow cover cut generator generates lifted simple generalized flow cover inequalities. Since flow cover inequalities are generally not facet-defining, they are lifted to obtain stronger inequalities. Although flow cover inequalities requires a special problem structure to be generated, they are quite useful for solving general mixed integer linear programs.

Reference: Z. Gu, G.L. Nemhauser, M.W.P. Savelsbergh, Lifted flow cover inequalities for mixed 0-1 integer programs, Math. Programming A 85 (1999) 439-467.

```
(default = ifmove)
```

# gomorycuts (string)

Determines whether and when CBC should try to generate mixed-integer Gomory cuts.

See the option cuts for an explanation on the different values.

Reference: Laurence A. Wolsey, Integer Programming, Wiley, John & Sons, (1998) 124-132.

(default = ifmove)

# knapsackcuts (string)

Determines whether and when CBC should try to generate knapsack cover cuts.

See the option cuts for an explanation on the different values.

The knapsack cover cut generator looks for a series of different types of minimal covers. If a minimal cover is found, it lifts the associated minimal cover inequality and adds the lifted cut to the cut set.

Reference: S. Martello, and P. Toth, Knapsack Problems, Wiley, 1990, p30.

(default = ifmove)

# liftandprojectcuts (string)

Determines whether and when CBC should try to generate lift and project cuts. They might be expensive to compute, thus they are switched off by default.

See the option cuts for an explanation on the different values.

Reference: E. Balas and M. Perregaard, A precise correspondence between lift-and-project cuts, simple disjunctive cuts, and mixed integer Gomory cuts for 0-1 programming. Math. Program., 94(203,Ser. B):221-245,2003.

(default = off)

#### mircuts (string)

Determines whether and when CBC should try to generate mixed integer rounding cuts.

See the option cuts for an explanation on the different values.

Reference: H. Marchand and L. A. Wolsey, Aggregation and Mixed Integer Rounding to Solve MIPs, Operations Research, 49(3), (2001).

(default = ifmove)

#### twomircuts (string)

Determines whether and when CBC should try to generate two phase mixed integer rounding cuts.

See the option cuts for an explanation on the different values.

Reference: S. Dash, and O. Guenluek, Valid Inequalities Based on Simple Mixed-integer Sets, to appear in Math. Programming.

(default = root)

# probingcuts (string)

Determines whether and when CBC should try to generate cuts based on probing.

Additional to the values for the option cuts three more values are possible here.

Reference: M. Savelsbergh, Preprocessing and Probing Techniques for Mixed Integer Programming Problems, ORSA Journal on Computing 6 (1994), 445.

(default = ifmove)

off Turns off Probing.

on Turns on Probing and CBC will try it in the branch and cut tree (see the option cutdepth how to fine tune this behaviour).

root Let CBC do Probing only at the root node.

ifmove Let CBC do Probing in the tree if it looks as if it is doing some good and moves the objective value.

forceon Turns on Probing and forces CBC to do Probing at every node.

forceonbut Turns on Probing and forces CBC to call the cut generator at every node, but does only probing, not strengthening etc.

forceonstrong If CBC is forced to turn Probing on at every node (by setting this option to force), but this generator produces no cuts, then it is actually turned on only weakly (i.e., just every now and then). Setting forceonstrong forces CBC strongly to do probing at every node.

forceonbutstrong This is like forceonstrong, but does only probing (column fixing) and turns off row strengthening, so the matrix will not change inside the branch and bound.

# reduceandsplitcuts (string)

Determines whether and when CBC should try to generate reduced and split cuts.

See the option cuts for an explanation on the different values.

Reduce and split cuts are variants of Gomory cuts. Starting from the current optimal tableau, linear combinations of the rows of the current optimal simplex tableau are used for generating Gomory cuts. The choice of the linear combinations is driven by the objective of reducing the coefficients of the non basic continuous variables in the resulting row.

Reference: K. Anderson, G. Cornuejols, and Yanjun Li, Reduce-and-Split Cuts: Improving the Performance of Mixed Integer Gomory Cuts, Management Science 51 (2005).

(default = off)

# residualcapacitycuts (string)

Determines whether and when CBC should try to generate residual capacity cuts.

See the option cuts for an explanation on the different values.

These inequalities are particularly useful for Network Design and Capacity Planning models.

References:

T.L. Magnanti, P. Mirchandani, and R. Vachani, The convex hull of two core capacitated network design problems, Math. Programming, 60 (1993), pp. 233-250.

A. Atamturk and D. Rajan, On splittable and unsplittable flow capacitated network design arc-set polyhedra, Math. Programming, 92 (2002), pp. 315-333.

(default = off)

# 3.3.10 MIP Options for Heuristics

# heuristics (integer)

This parameter can be used to switch on or off all heuristics, except for the local tree search as it dramatically alters the search. Then you can set individual ones off or on.

(default = 1)

- 0 Turns all MIP heuristics off.
- 1 Turns all MIP heuristics on (except local tree search).

# combinesolutions (integer)

This parameter control the use of a heuristic which does branch and cut on the given problem by just using variables which have appeared in one or more solutions. It is obviously only tried after two or more solutions.

(default = 1)

- 0 Turns the combine solutions heuristic off.
- 1 Turns the combine solutions heuristic on.

# dins (integer)

This parameter control the use of the distance induced neighborhood search heuristic.

```
(default = 0)
```

- 0 Turns the distance induced neighborhood search off.
- 1 Turns the distance induced neighborhood search on.

# divingrandom (integer)

This switches on a random diving heuristic at various times.

```
(default = 0)
```

- 0 Turns the random diving heuristics off.
- 1 Turns the random diving heuristics on.

# divingcoefficient (integer)

This switches on the coefficient diving heuristic.

```
(default = 1)
```

- 0 Turns the coefficient diving heuristics off.
- 1 Turns the coefficient diving heuristics on.

# divingfractional (integer)

This switches on the fractional diving heuristic.

```
(default = 0)
```

- 0 Turns the fractional diving heuristics off.
- 1 Turns the fractional diving heuristics on.

# divingguided (integer)

This switches on the guided diving heuristic.

```
(default = 0)
```

- 0 Turns the guided diving heuristics off.
- 1 Turns the guided diving heuristics on.

# divinglinesearch (integer)

This switches on the line search diving heuristic.

```
(default = 0)
```

- 0 Turns the line search diving heuristics off.
- 1 Turns the linesearch diving heuristics on.

# divingpseudocost (integer)

This switches on the pseudo costs diving heuristic.

```
(default = 0)
```

- 0 Turns the pseudo costs diving heuristics off.
- 1 Turns the pseudo costs diving heuristics on.

# divingvectorlength (integer)

This switches on the vector length diving heuristic.

```
(default = 0)
```

- 0 Turns the vector length diving heuristics off.
- 1 Turns the vector length diving heuristics on.

# feaspump (integer)

This parameter control the use of the feasibility pump heuristic at the root.

This is due to Fischetti and Lodi and uses a sequence of LPs to try and get an integer feasible solution. Some fine tuning is available by the option feaspump\_passes. Reference: M. Fischetti, F. Glover, and A. Lodi, The feasibility pump, Math. Programming, 104 (2005), pp. 91-104.

```
(default = 1)
```

- 0 Turns the feasibility pump off.
- 1 Turns the feasibility pump on.

# feaspump\_passes (integer)

This fine tunes the feasibility pump heuristic by setting the number of passes.

```
(default = 20)
```

# greedyheuristic (string)

This parameter control the use of a pair of greedy heuristic which will try to obtain a solution. It may just fix a percentage of variables and then try a small branch and cut run.

```
(default = on)
```

- off Turns off the greedy heuristic.
- on Turns on the greedy heuristic.
- root Turns on the greedy heuristic only for the root node.

# localtreesearch (integer)

This parameter control the use of a local search algorithm when a solution is found.

It is from Fischetti and Lodi and is not really a heuristic although it can be used as one (with limited functionality). This heuristic is not controlled by the option heuristics.

Reference: M. Fischetti and A. Lodi, Local Branching, Math. Programming B, 98 (2003), pp. 23-47.

```
(default = 0)
```

- 0 Turns the local tree search off.
- 1 Turns the local tree search on.

# naiveheuristics (integer)

This parameter controls the use of some naive heuristics, e.g., fixing of all integers with costs to zero.;BR>

```
(default = 0)
```

- 0 Turns the naive heuristics off.
- 1 Turns the naive heuristics on.

# pivotandfix (integer)

This parameter controls the use of the pivot and fix heuristic.

```
(default = 0)
```

- 0 Turns the naive pivot and fix heuristic off.
- 1 Turns the naive pivot and fix heuristic on.

# randomizedrounding (integer)

This parameter controls the use of the randomized rounding heuristic.

```
(default = 0)
```

- 0 Turns the randomized rounding heuristic off.
- 1 Turns the randomized rounding heuristic on.

#### rens (integer)

This parameter controls the use of the relaxation enforced neighborhood search heuristic.

```
(default = 0)
```

- 0 Turns the relaxation enforced neighborhood search off.
- 1 Turns the relaxation enforced neighborhood search on.

#### rins (integer)

This parameter control the use of the relaxed induced neighborhood search heuristic.

This heuristic compares the current solution with the best incumbent, fixes all discrete variables with the same value, presolves the problem, and does a branch and bound for 200 nodes.

Reference: E. Danna, E. Rothberg, and C. Le Pape, Exploring relaxation induced neighborhoods to improve MIP solutions, Math. Programming, 102 (1) (2005), pp. 71-91.

```
(default = 0)
```

- 0 Turns the relaxed induced neighborhood search off.
- 1 Turns the relaxed induced neighborhood search on.

#### roundingheuristic (integer)

This parameter control the use of a simple (but effective) rounding heuristic at each node of tree.

```
(default = 1)
```

- 0 Turns the rounding heuristic off.
- 1 Turns the rounding heuristic on.

# vubheuristic (integer)

This parameter control the use of the VUB heuristic. If it is set (between -2 and 20), Cbc will try and fix some integer variables

```
(default = -1)
```

# proximitysearch (integer)

This parameter controls the use of the "No-Neighborhood Search" 0-1 MIP refinement heuristic proposed by Fischetti and Monaci (2012). The idea is to define a sub-MIP without additional constraints but with a modified objective function intended to attract the search in the proximity of the incumbent. The approach works well for 0-1 MIPs whose solution landscape is not too irregular (meaning the there is reasonable probability of finding an improved solution by flipping a small number of binary variables), in particular when it is applied to the first heuristic solutions found at the root node.

```
(default = 0)
```

- 0 Turns the proximity heuristic off.
- 1 Turns the proximity heuristic on.

# 4 COUENNE

COUENNE (Convex Over and Under Envelopes for Nonlinear Estimation) is an open-source solver for nonconvex mixed-integer nonlinear programming (MINLPs). The code has been developed originally in a cooperation of Carnegie Mellon University and IBM Research, and now at Clemson University. The COIN-OR project leader for COUENNE is Pietro Belotti.

COUENNE solves convex and nonconvex MINLPs by an LP based spatial branch-and-bound algorithm that is similar to the algorithm used in BARON. The implementation extends BONMIN by routines to compute valid linear outer approximations for nonconvex problems and methods for bound tightening and branching on nonlinear variables.

For more information on the algorithm we refer to [5, 6] and the COUENNE web site https://projects.coin-or.org/Couenne. Most of the COUENNE documentation in this section is taken from the COUENNE manual [4].

# 4.1 Model requirements

COUENNE can handle mixed-integer nonlinear programming models which functions can be nonconvex, but should be twice continuously differentiable. Further, an algebraic description of the model need to be made available, which makes the use of some GAMS functions and user-specified external functions impossible. The COUENNE link in GAMS supports continuous, binary, and integer variables, but no special ordered sets, semi-continuous or semi-integer variables (see chapter 17.1 of the GAMS User's Guide).

If GAMS/COUENNE is called for a linear model, the interface directly calls CBC.

# 4.2 Usage

The following statement can be used inside your GAMS program to specify using COUENNE

```
Option MINLP = COUENNE; { or LP, RMIP, MIP, DNLP, NLP, RMINLP, QCP, RMIQCP, MIQCP}
```

The above statement should appear before the Solve statement. If COUENNE was specified as the default solver during GAMS installation, the above statement is not necessary.

# 4.2.1 Specification of Options

A COUENNE option file contains IPOPT, BONMIN, and COUENNE options, for clarity all BONMIN options should be preceded with the prefix "bonmin." and all COUENNE options should be preceded with the prefix "couenne.". All IPOPT and many BONMIN options are available in COUENNE, please refer to the Sections 5.5 and 2.3 for a detailed description. The scheme to name option files is the same as for all other GAMS solvers. Specifying optfile=1 let GAMS/COUENNE read couenne.opt, optfile=2 corresponds to couenne.op2, and so on. The format of the option file is the same as for IPOPT (see Section 5.2.2).

GAMS/COUENNE understands currently the following GAMS parameters: reslim (time limit), nodlim (node limit), cutoff, optca (absolute gap tolerance), and optcr (relative gap tolerance). One can set them either on the command line, e.g. nodlim=1000, or inside your GAMS program, e.g. Option nodlim=1000;. Further, under Linux and Windows, the option threads can be used to control the number of threads used in the linear algebra routines of IPOPT.

# 4.3 Detailed Options Description

In the following we give a detailed list of options available for COUENNE solely. The value on the right denotes the default value. Note that options specific to IPOPT and BONMIN are not listed her, see Sections 2.3 and 5.5 instead.

 $2mir_cuts (-100 < integer)$ 

Frequency k (in terms of nodes) for generating 2mir\_cuts cuts in branch-and-cut.

If k > 0, cuts are generated every k nodes, if -99 < k < 0 cuts are generated every -k nodes but Cbc may decide to stop generating cuts, if not enough are generated at the root node, if k=-99 generate cuts only at the root node, if k=0 or 100 do not generate cuts.

Gomory\_cuts  $(-100 \le integer)$  0

Frequency k (in terms of nodes) for generating Gomory\_cuts cuts in branch-and-cut.

See option 2mir\_cuts for the meaning of k.

aggressive\_fbbt (no, yes)

yes

Aggressive feasibility-based bound tightening (to use with NLP points)

Aggressive FBBT is a version of probing that also allows to reduce the solution set, although it is not as quick as FBBT. It can be applied up to a certain depth of the B&B tree – see "log\_num\_abt\_per\_level". In general, this option is useful but can be switched off if a problem is too large and seems not to benefit from it.

art\_cutoff (real) ∞

Artificial cutoff

Default value is infinity.

art\_lower (real)  $-\infty$ Artificial lower bound Default value is -COIN\_DBL\_MAX. 0 boundtightening\_print\_level  $(-2 \le integer \le 12)$ Output level for bound tightening code in Couenne branch\_conv\_cuts (no, yes) yes Apply convexification cuts before branching (for now only within strong branching) After applying a branching rule and before resolving the subproblem, generate a round of linearization cuts with the new bounds enforced by the rule. branch\_fbbt (no, yes) yes Apply bound tightening before branching After applying a branching rule and before re-solving the subproblem, apply Bound Tightening.  $branch_lp_clamp (0 \le real \le 1)$ 0.2 Defines safe interval percentage for using LP point as a branching point. branch\_lp\_clamp\_cube  $(0 \le real \le 0.5)$ 0.2 Defines safe interval percentage [0,0.5] for using LP point as a branching point. branch\_lp\_clamp\_div  $(0 \le real \le 0.5)$ 0.2 Defines safe interval percentage [0,0.5] for using LP point as a branching point. 0.2 branch\_lp\_clamp\_exp  $(0 \le real \le 0.5)$ Defines safe interval percentage [0,0.5] for using LP point as a branching point.  $branch_lp_clamp_log (0 \le real \le 0.5)$ 0.2 Defines safe interval percentage [0,0.5] for using LP point as a branching point. 0.2 branch\_lp\_clamp\_negpow  $(0 \le real \le 0.5)$ Defines safe interval percentage [0,0.5] for using LP point as a branching point. 0.2 branch\_lp\_clamp\_pow (0 < real < 0.5)Defines safe interval percentage [0,0.5] for using LP point as a branching point. 0.2 branch\_lp\_clamp\_prod  $(0 \le real \le 0.5)$ Defines safe interval percentage [0,0.5] for using LP point as a branching point. branch\_lp\_clamp\_sqr  $(0 \le real \le 0.5)$ 0.2 Defines safe interval percentage [0,0.5] for using LP point as a branching point. 0.2 branch\_lp\_clamp\_trig  $(0 \le real \le 0.5)$ Defines safe interval percentage [0,0.5] for using LP point as a branching point. 0.25 branch\_midpoint\_alpha  $(0 \le real \le 1)$ Defines convex combination of mid point and current LP point:  $b = alpha x_lp + (1-alpha) (lb+ub)/2$ . branch\_pt\_select (lp-clamped, lp-central, balanced, min-area, mid-point, no-branch) mid-point Chooses branching point selection strategy lp-clamped LP point clamped in [k,1-k] of the bound intervals (k defined by lp\_clamp) lp-central LP point if within [k,1-k] of the bound intervals, middle point otherwise(k defined by branch\_lp\_clamp) balanced minimizes max distance from curve to convexification min-area minimizes total area of the two convexifications mid-point convex combination of current point and mid point no-branch do not branch, return null infeasibility; for testing purposes only branch\_pt\_select\_cube (common, lp-clamped, lp-central, balanced, min-area, mid-point, no-branch) common Chooses branching point selection strategy for operator cube.

branch\_pt\_select\_div (common, lp-clamped, lp-central, balanced, min-area, mid-point, no-branch)

Default is to use the value of branch\_pt\_select (value common).

common

Chooses branching point selection strategy for operator div.

Default is to use the value of branch\_pt\_select (value common).

branch\_pt\_select\_exp (common, lp-clamped, lp-central, balanced, min-area, mid-point, no-branch)
common

Chooses branching point selection strategy for operator exp.

Default is to use the value of branch\_pt\_select (value common).

branch\_pt\_select\_log (common, lp-clamped, lp-central, balanced, min-area, mid-point, no-branch)
common

Chooses branching point selection strategy for operator log.

Default is to use the value of branch\_pt\_select (value common).

branch\_pt\_select\_negpow (common, lp-clamped, lp-central, balanced, min-area, mid-point, no-branch) common

Chooses branching point selection strategy for operator negpow.

Default is to use the value of branch\_pt\_select (value common).

branch\_pt\_select\_pow (common, lp-clamped, lp-central, balanced, min-area, mid-point, no-branch)
common

Chooses branching point selection strategy for operator pow.

Default is to use the value of branch\_pt\_select (value common).

branch\_pt\_select\_prod (common, lp-clamped, lp-central, balanced, min-area, mid-point, no-branch)
common

Chooses branching point selection strategy for operator prod.

Default is to use the value of branch\_pt\_select (value common).

branch\_pt\_select\_sqr (common, lp-clamped, lp-central, balanced, min-area, mid-point, no-branch)
common

Chooses branching point selection strategy for operator sqr.

Default is to use the value of branch\_pt\_select (value common).

branch\_pt\_select\_trig (common, lp-clamped, lp-central, balanced, min-area, mid-point, no-branch)
common

Chooses branching point selection strategy for operator trig.

Default is to use the value of branch\_pt\_select (value common).

branching\_object (vt\_obj, var\_obj, expr\_obj)
type of branching object for variable selection

vt\_obj use Violation Transfer from Tawarmalani and Sahinidis

var\_obj use one object for each variable

expr\_obj use one object for each nonlinear expression

 ${\tt branching\_print\_level}\ (-2 \leq integer \leq 12)$ 

var\_obj

Output level for braching code in Couenne

check\_lp (no, yes)
Check all LPs through an independent call to OsiClpSolverInterface::initialSolve()

clique\_cuts  $(-100 \le integer)$ 

0

no

0

Frequency k (in terms of nodes) for generating clique\_cuts cuts in branch-and-cut.

See option 2mir\_cuts for the meaning of k.

 $cont\_var\_priority (1 \le integer)$ 

2000

Priority of continuous variable branching

When branching, this is compared to the priority of integer variables, whose priority is given by int\_var\_priority, and SOS, whose priority is 10. Higher values mean smaller priority.

convexification\_cuts  $(-99 \le integer)$ 

1

Specify the frequency (in terms of nodes) at which couenne ecp cuts are generated.

A frequency of 0 amounts to never solve the NLP relaxation.

convexification\_points  $(0 \le integer)$ 4 Specify the number of points at which to convexify when convexification type is uniform-grid or around-current-point. convexification\_type (current-point-only, uniform-grid, around-current-point) current-point-only Determines in which point the linear over/under-estimator are generated For the lower envelopes of convex functions, this is the number of points where a supporting hyperplane is generated. This only holds for the initial linearization, as all other linearizations only add at most one cut per expression. current-point-only Only at current optimum of relaxation uniform-grid Points chosen in a uniform grid between the bounds of the problem around-current-point At points around current optimum of relaxation convexifying\_print\_level (-2 < integer < 12)0 Output level for convexifying code in Couenne 0 cover\_cuts  $(-100 \le integer)$ Frequency k (in terms of nodes) for generating cover\_cuts cuts in branch-and-cut. See option 2mir\_cuts for the meaning of k. delete\_redundant (no, yes) yes Eliminate redundant variables, which appear in the problem as  $x_k = x_h$ no Keep redundant variables, making the problem a bit larger yes Eliminate redundant variables (the problem will be equivalent, only smaller) disj\_active\_cols (yes, no) no Only include violated variable bounds in the Cut Generating LP (CGLP). This reduces the size of the CGLP, but may produce less efficient cuts. disj\_active\_rows (yes, no) no Only include violated linear inequalities in the CGLP. This reduces the size of the CGLP, but may produce less efficient cuts. disj\_cumulative (yes, no) no Add previous disjunctive cut to current CGLP. When generating disjunctive cuts on a set of disjunctions 1, 2, ..., k, introduce the cut relative to the previous disjunction i-1 in the CGLP used for disjunction i. Notice that, although this makes the cut generated more efficient, it increases the rank of the disjunctive cut generated. 5  $disj_depth_level (-1 \le integer)$ Depth of the B&B tree when to start decreasing the number of objects that generate disjunctions. This has a similar behavior as log\_num\_obbt\_per\_level. A value of -1 means that generation can be done at all nodes.  $disj_depth_stop (-1 < integer)$ 20 Depth of the B&B tree where separation of disjunctive cuts is stopped. A value of -1 means that generation can be done at all nodes 10  $disj_init_number (-1 \le integer)$ Maximum number of disjunction to consider at each iteration. -1 means no limit.  $disj_init_perc (0 < real < 1)$ 0.5 The maximum fraction of all disjunctions currently violated by the problem to consider for generating disjunctions. 0  $disjcuts\_print\_level (-2 < integer < 12)$ Output level for disjunctive cuts in Couenne display\_stats (yes, no) no display statistics at the end of the run enable\_lp\_implied\_bounds (no, yes) no Enable OsiSolverInterface::tightenBounds () - warning: it has caused some trouble to Couenne enable\_sos (no, yes) no

Use Special Ordered Sets (SOS) as indicated in the MINLP model

estimate\_select (normal, product) normal How the min/max estimates of the subproblems' bounds are used in strong branching normal as usual in literature product use their product feas\_pump\_convcuts (integrated, external, postcut, none) none Separate MILP-feasible, MINLP-infeasible solution during or after MILP solver. integrated Done within the MILP solver in a branch-and-cut fashion external Done after the MILP solver, in a Benders-like fashion postcut Do one round of cuts and proceed with NLP none Just proceed to the NLP feas\_pump\_heuristic (no, yes) nο Apply the nonconvex Feasibility Pump An implementation of the Feasibility Pump for nonconvex MINLPs feas\_pump\_iter  $(-1 \le integer)$ 10 Number of iterations in the main Feasibility Pump loop -1 means no limit feas\_pump\_level  $(-1 \le integer)$ 3 Specify the logarithm of the number of feasibility pumps to perform on average for each level of given depth of the tree. Solve as many nlp's at the nodes for each level of the tree. Nodes are randomly selected. If for a given level there are less nodes than this number nlp are solved for every nodes. For example if parameter is 8, nlp's are solved for all node until level 8, then for half the node at level 9, 1/4 at level 10.... Set to -1 to perform at all nodes. feas\_pump\_milpmethod (-1 < integer < 4)-1How should the integral solution be constructed? 0: automatic, 1: aggressive heuristics, large node limit, 2: default, node limit, 3: RENS, 4: Objective Feasibility Pump, -1: solve MILP completely 0 feas\_pump\_mult\_dist\_milp  $(0 \le real \le 1)$ Weight of the distance in the distance function of the milp problem 0: no weight, 1: full weight 0 feas\_pump\_mult\_dist\_nlp  $(0 \le real \le 1)$ Weight of the distance in the distance function of the nlp problem 0: no weight, 1: full weight feas\_pump\_mult\_hess\_milp  $(0 \le real \le 1)$ 0 Weight of the Hessian in the distance function of the milp problem 0: no weight, 1: full weight feas\_pump\_mult\_hess\_nlp  $(0 \le real \le 1)$ 0 Weight of the Hessian in the distance function of the nlp problem 0: no weight, 1: full weight feas\_pump\_mult\_objf\_milp  $(0 \le real \le 1)$ 0 Weight of the original objective function in the distance function of the milp problem 0: no weight, 1: full weight 0 feas\_pump\_mult\_objf\_nlp  $(0 \le real \le 1)$ Weight of the original objective function in the distance function of the nlp problem 0: no weight, 1: full weight feas\_pump\_nseprounds  $(1 \le integer \le 100000)$ 4 Number of rounds that separate convexification cuts. Must be at least 1 feas\_pump\_poolcomp  $(0 \le integer \le 2)$ 0 Priority field to compare solutions in FP pool 0: total number of infeasible objects (integer and nonlinear), 1: maximum infeasibility (integer or nonlinear), 2: objective

value.

feas\_pump\_tabumgt (pool, perturb, cut, none)

pool

Retrieval of MILP solutions when the one returned is unsatisfactory

pool Use a solution pool and replace unsatisfactory solution with Euclidean-closest in pool

perturb Randomly perturb unsatisfactory solution

cut Separate convexification cuts

none Bail out of feasibility pump

feas\_pump\_usescip (no, yes)

yes

Should SCIP be used to solve the MILPs?

Note, that SCIP is only available for GAMS users with an academic GAMS license.

no Use Cbc's branch-and-cut to solve the MILP

yes Use SCIP's branch-and-cut or heuristics (see feas\_pump\_milpmethod option) to solve the MILP

feas\_pump\_vardist (integer, all, int-postprocess)

integer

Distance computed on integer-only or on both types of variables, in different flavors.

integer Only compute the distance based on integer coordinates (use post-processing if numerical errors occur)

all Compute the distance using continuous and integer variables

int-postprocess Use a post-processing fixed-IP LP to determine a closest-point solution

feas\_tolerance (real)

Tolerance for constraints/auxiliary variables

Default value is 1e-5.

feasibility\_bt (no, yes)

yes

 $10^{-5}$ 

Feasibility-based (cheap) bound tightening (FBBT)

A pre-processing technique to reduce the bounding box, before the generation of linearization cuts. This is a quick and effective way to reduce the solution set, and it is highly recommended to keep it active.

fixpoint\_bt  $(-99 \le integer)$ 

0

The frequency (in terms of nodes) at which Fix Point Bound Tightening is performed.

A frequency of 0 (default) means these cuts are never generated. Any positive number n instructs Couenne to generate them at every n nodes of the B&B tree. A negative number -n means that generation should be attempted at the root node, and if successful it can be repeated at every n nodes, otherwise it is stopped altogether.

fixpoint\_bt\_model (extended, compact)

compact

Choose whether to add an extended fixpoint LP model or a more compact one.

flow\_covers\_cuts  $(-100 \le integer)$ 

0

Frequency k (in terms of nodes) for generating flow\_covers\_cuts cuts in branch-and-cut.

See option 2mir\_cuts for the meaning of k.

 $int\_var\_priority (1 \le integer)$ 

1000

Priority of integer variable branching

When branching, this is compared to the priority of continuous variables, whose priority is given by cont\_var\_priority, and SOS, whose priority is 10. Higher values mean smaller priority.

iterative\_rounding\_aggressiveness  $(0 \le integer \le 2)$ 

1

Aggressiveness of the Iterative Rounding heuristic

Set the aggressiveness of the heuristic; i.e., how many iterations should be run, and with which parameters. The maximum time can be overridden by setting the \_time and \_time\_firstcall options. 0 = non aggressive, 1 = standard (default), 2 = aggressive.

iterative\_rounding\_base\_lbrhs (0 \le integer)

15

Base rhs of the local branching constraint for Iterative Rounding

Base rhs for the local branching constraint that defines a neighbourhood of the local incumbent. The base rhs is modified by the algorithm according to variable bounds. This corresponds to k' in the paper. Default 15.

iterative\_rounding\_heuristic (no, yes)

no

Do we use the Iterative Rounding heuristic

If enabled, a heuristic based on Iterative Rounding is used to find feasible solutions for the problem. The heuristic may take some time, but usually finds good solutions. Recommended if you want good upper bounds and have Cplex. Not recommended if you do not have Cplex

iterative\_rounding\_num\_fir\_points (1 \le integer)

5

Max number of points rounded at the beginning of Iterative Rounding

Number of different points (obtained solving a log-barrier problem) that the heuristic will try to round at most, during its execution at the root node (i.e. the F-IR heuristic). Default 5.

iterative\_rounding\_omega (0 < real < 1)

0.2

Omega parameter of the Iterative Rounding heuristic

Set the omega parameter of the heuristic, which represents a multiplicative factor for the minimum log-barrier parameter of the NLP which is solved to obtain feasible points. This corresponds to  $\omega'$  in the paper. Default 0.2.

iterative\_rounding\_time (real)

-1

Specify the maximum time allowed for the Iterative Rounding heuristic

Maximum CPU time employed by the Iterative Rounding heuristic; if no solution found in this time, failure is reported. This overrides the CPU time set by Aggressiveness if positive.

iterative\_rounding\_time\_firstcall (real)

-1

Specify the maximum time allowed for the Iterative Rounding heuristic when no feasible solution is known

Maximum CPU time employed by the Iterative Rounding heuristic when no solution is known; if no solution found in this time, failure is reported. This overrides the CPU time set by Aggressiveness if posive.

 $lift_and_project_cuts (-100 \le integer)$ 

0

Frequency k (in terms of nodes) for generating lift\_and\_project\_cuts cuts in branch-and-cut.

See option 2mir\_cuts for the meaning of k.

local\_branching\_heuristic (no, yes)

no

Apply local branching heuristic

A local-branching heuristic based is used to find feasible solutions.

local\_optimization\_heuristic (no, yes)

yes

Search for local solutions of MINLPs

If enabled, a heuristic based on Ipopt is used to find feasible solutions for the problem. It is highly recommended that this option is left enabled, as it would be difficult to find feasible solutions otherwise.

 $log_num_abt_per_level (-1 \le integer)$ 

2

Specify the frequency (in terms of nodes) for aggressive bound tightening.

If -1, apply at every node (expensive!). If 0, apply at root node only. If  $k \ge 0$ , apply with probability 2(k - level), level being the current depth of the B&B tree.

 $log_num_local_optimization_per_level (-1 \le integer)$ 

2

Specify the logarithm of the number of local optimizations to perform on average for each level of given depth of the tree. Solve as many nlp's at the nodes for each level of the tree. Nodes are randomly selected. If for a given level there are less nodes than this number nlp are solved for every nodes. For example if parameter is 8, nlp's are solved for all node until level 8, then for half the node at level 9, 1/4 at level 10.... Value -1 specify to perform at all nodes.

 $log_num_obbt_per_level (-1 \le integer)$ 

1

Specify the frequency (in terms of nodes) for optimality-based bound tightening.

If -1, apply at every node (expensive!). If 0, apply at root node only. If  $k \ge 0$ , apply with probability 2(k - level), level being the current depth of the B&B tree.

lp\_solver (clp, cplex, gurobi, soplex, xpress-mp)

clp

Linear Programming solver for the linearization

clp Use the COIN-OR Open Source solver CLP

cplex Use the commercial solver Cplex (license is needed)

gurobi Use the commercial solver Gurobi (license is needed)

soplex Use the freely available Soplex

xpress-mp Use the commercial solver Xpress MP (license is needed)

 $max\_fbbt\_iter (-1 \le integer)$ 

Number of FBBT iterations before stopping even with tightened bounds. Set to -1 to impose no upper limit  $minlp_disj_cuts (-99 \le integer)$ 0 The frequency (in terms of nodes) at which Couenne disjunctive cuts are generated. A frequency of 0 (default) means these cuts are never generated. Any positive number n instructs Couenne to generate them at every n nodes of the B&B tree. A negative number -n means that generation should be attempted at the root node, and if successful it can be repeated at every n nodes, otherwise it is stopped altogether. 0  $mir_cuts (-100 \le integer)$ Frequency k (in terms of nodes) for generating mir\_cuts cuts in branch-and-cut. See option 2mir\_cuts for the meaning of k. tight multilinear\_separation (none, simple, tight) Separation for multilinear terms Type of separation for multilinear terms where the dependent variable is also bounded none No separation – just use the four McCormick inequalities simple Use one considering lower curve only tight Use one considering both curves pi(x) = 1 + 1 and pi(x) = u + 1 $nlpheur_print_level (-2 \le integer \le 12)$ 0 Output level for NLP heuristic in Couenne optimality\_bt (no, yes) yes Optimality-based (expensive) bound tightening (OBBT) This is another bound reduction technique aiming at reducing the solution set by looking at the initial LP relaxation. This technique is computationally expensive, and should be used only when necessary. orbital\_branching (yes, no) no detect symmetries and apply orbital branching 0 output\_level  $(-2 \le integer \le 12)$ Output level 0 probing\_cuts  $(-100 \le integer)$ Frequency k (in terms of nodes) for generating probing\_cuts cuts in branch-and-cut. See option 2mir\_cuts for the meaning of k. 0 problem\_print\_level  $(-2 \le integer \le 12)$ Output level for problem manipulation code in Couenne pseudocost\_mult (infeasibility, projectDist, interval\_lp, interval\_lp\_rev, interval\_br, interval\_br\_rev) interval\_br\_rev Multipliers of pseudocosts for estimating and update estimation of bound infeasibility infeasibility returned by object projectDist distance between current LP point and resulting branches' LP points interval\_lp width of the interval between bound and current lp point interval\_lp\_rev similar to interval\_lp, reversed interval\_br width of the interval between bound and branching point interval\_br\_rev similar to interval\_br, reversed pseudocost\_mult\_lp (yes, no) no Use distance between LP points to update multipliers of pseudocosts after simulating branching quadrilinear\_decomp (rAI, tri+bi, bi+tri, hier-bi) rAI type of decomposition for quadrilinear terms (see work by Cafieri, Lee, Liberti)

rAI Recursive decomposition in bilinear terms (as in Ryoo and Sahinidis):  $x5 = ((x1 \ x2) \ x3) \ x4)$ 

tri+bi Trilinear and bilinear term: x5 = (x1 (x2 x3 x4))bi+tri Bilinear, THEN trilinear term: x5 = ((x1 x2) x3 x4))

hier-bi Hierarchical decomposition:  $x5 = ((x1 \ x2) \ (x3 \ x4))$ red\_cost\_branching (no, yes) no Apply Reduced Cost Branching (instead of the Violation Transfer) – MUST have vt\_obj enabled no Use Violation Transfer with  $\sum |\pi_i i a_i j|$ yes Use Reduced cost branching with  $|\sum \pi_i i a_i j|$ redcost\_bt (no, yes) yes Reduced cost bound tightening This bound reduction technique uses the reduced costs of the LP in order to infer better variable bounds. 0 reduce\_split\_cuts  $(-100 \le integer)$ Frequency k (in terms of nodes) for generating reduce\_split\_cuts cuts in branch-and-cut. See option 2mir\_cuts for the meaning of k. 0 reformulate\_print\_level  $(-2 \le integer \le 12)$ Output level for reformulating problems in Couenne solvetrace (string) Name of file for writing solving progress information. 100 solvetracenodefreq  $(0 \le integer)$ Frequency in number of nodes for writing solving progress information. giving 0 disables writing of N-lines to trace file 5 solvetracetimefreq  $(0 \le \text{real})$ Frequency in seconds for writing solving progress information. giving 0.0 disables writing of T-lines to trace file trust\_strong (yes, no) yes Fathom strong branching LPs when their bound is above the cutoff 0 two\_implied\_bt  $(-99 \le integer)$ The frequency (in terms of nodes) at which Couenne two-implied bounds are tightened. A frequency of 0 (default) means these cuts are never generated. Any positive number n instructs Couenne to generate them at every n nodes of the B&B tree. A negative number -n means that generation should be attempted at the root node, and if successful it can be repeated at every n nodes, otherwise it is stopped altogether. two\_implied\_max\_trials (1 < integer)</pre> 2 The number of iteration at each call to the cut generator. 5 twoimpl\_depth\_level  $(-1 \le integer)$ Depth of the B&B tree when to start decreasing the chance of running this algorithm. This has a similar behavior as log\_num\_obbt\_per\_level. A value of -1 means that generation can be done at all nodes. 20 twoimpl\_depth\_stop  $(-1 \le integer)$ Depth of the B&B tree where separation is stopped. A value of -1 means that generation can be done at all nodes yes use\_auxcons (no, yes) Use constraints-defined auxiliaries, i.e. auxiliaries w = f(x) defined by original constraints f(x) - w = 0use\_quadratic (no, yes) no Use quadratic expressions and related exprQuad class If enabled, then quadratic forms are not reformulated and therefore decomposed as a sum of auxiliary variables, each associated with a bilinear term, but rather taken as a whole expression. Envelopes for these expressions are generated through alpha-convexification. no Use an auxiliary for each bilinear term yes Create only one auxiliary for a quadratic expression use\_semiaux (no, yes) yes Use semiauxiliaries, i.e. auxiliaries defined as  $w \ge f(x)$  rather than w := f(x)

no Only use auxiliaries assigned with "="

```
yes Use auxiliaries defined by w \le f(x), w >= f(x), and w = f(x)
violated_cuts_only (no, yes) yes if only violated convexification cuts should be added
```

# 5 IPOPT and IPOPTH

IPOPT (Interior Point **Opt**imizer) is an open-source solver for large-scale nonlinear programming. The code has been written primarily by Andreas Wächter, who is the COIN-OR project leader for IPOPT.

IPOPT implements an interior point line search filter method. For more information on the algorithm we refer to [24, 26, 27, 28, 29] and the IPOPT web site <a href="https://projects.coin-or.org/Ipopt">https://projects.coin-or.org/Ipopt</a>. Most of the IPOPT documentation in the section was taken from the IPOPT manual [20].

GAMS/IPOPT uses MUMPS [2, 3] as linear solver, cf. http://graal.ens-lyon.fr/MUMPS. In the commerically licensed GAMS/IPOPTH version, also the linear solvers MA27, MA57, and MA86 from the Harwell Subroutines Library (HSL) are available. In this case, the default solver is MA27.

MUMPS and MA57 use METIS for matrix ordering [19], cf. http://glaros.dtc.umn.edu/gkhome/views/metis/index.html and http://glaros.dtc.umn.edu/gkhome/fetch/sw/metis/manual.pdf. METIS is copyrighted by the regents of the University of Minnesota.

# 5.1 Model requirements

IPOPT can handle nonlinear programming models which functions can be nonconvex, but should be twice continuously differentiable.

# 5.2 Usage

The following statement can be used inside your GAMS program to specify using IPOPT

```
Option NLP = IPOPT; { or LP, RMIP, DNLP, RMINLP, QCP, RMIQCP }
```

The above statement should appear before the Solve statement. If IPOPT was specified as the default solver during GAMS installation, the above statement is not necessary.

To use IPOPTH, the statement should be

```
Option NLP = IPOPTH; { or LP, RMIP, DNLP, RMINLP, QCP, RMIQCP }
```

# **5.2.1** The linear solver in IPOPT

The performance and robustness of IPOPT on larger models heavily relies on the used solver for sparse symmetric indefinite linear systems. GAMS/IPOPT includes the sparse solver MUMPS [2, 3]. In a commercially licensed GAMS/IPOPTH version, also the Harwell Subroutine Library (HSL) solvers MA27, MA57, and MA86 are available and MA27 is used by default. Further, a user can provide the Parallel Sparse Direct Solver PARDISO or routines from HSL as shared (or dynamic) libraries.

**5.2.1.1** Using Harwell Subroutine Library routines with GAMS/IPOPT. GAMS/IPOPT can use the HSL routines MA27, MA28, MA57, and MC19 when provided as shared library. By telling IPOPT to use one of these routines (see options linear\_solver, linear\_system\_scaling, nlp\_scaling\_method, dependency\_detector), GAMS/IPOPT attempts to load the required routines from the library libhsl.so (Unix-Systems), libhsl.dylib (MacOS X), or libhsl.dll (Windows), respectively.

The HSL routines are available at <a href="http://www.hsl.rl.ac.uk/ipopt">http://www.hsl.rl.ac.uk/ipopt</a>. Note that it is your responsibility to ensure that you are entitled to download and use these routines!

**5.2.1.2** Using PARDISO with GAMS/IPOPT. Setting the option linear\_solver to pardiso, lets GAMS/IPOPT or GAMS/IPOPTH attempt to load the linear solver PARDISO from the library libpardiso.so (Unix-Systems), libpardiso.dylib (MacOS X), or libpardiso.dll (Windows), respectively.

PARDISO is available as compiled shared library for several platforms at http://www.pardiso-project.org. Note that it is your responsibility to ensure that you are entitled to download and use this package!

#### **5.2.2** Specification of Options

IPOPT has many options that can be adjusted for the algorithm (see Section 5.5). Options are all identified by a string name, and their values can be of one of three types: Number (real), Integer, or String. Number options are used for things like tolerances, integer options are used for things like maximum number of iterations, and string options are used for setting algorithm details, like the NLP scaling method. Options can be set by creating a ipopt.opt file in the directory you are executing IPOPT.

The ipopt opt file is read line by line and each line should contain the option name, followed by whitespace, and then the value. Comments can be included with the # symbol. Don't forget to ensure you have a newline at the end of the file. For example,

```
# This is a comment

# Turn off the NLP scaling
nlp_scaling_method none

# Change the initial barrier parameter
mu_init 1e-2

# Set the max number of iterations
max_iter 500
```

is a valid ipopt.opt file.

GAMS/IPOPT understand currently the following GAMS parameters: reslim (time limit), iterlim (iteration limit), domlim (domain violation limit). You can set them either on the command line, e.g. iterlim=500, or inside your GAMS program, e.g. Option iterlim=500; Further, under Linux and Windows, the option threads can be used to control the number of threads used in the basic linear algebra routines.

# 5.3 Output

This section describes the standard IPOPT console output. The output is designed to provide a quick summary of each iteration as IPOPT solves the problem.

Before IPOPT starts to solve the problem, it displays the problem statistics (number of nonzero-elements in the matrices, number of variables, etc.). Note that if you have fixed variables (both upper and lower bounds are equal), IPOPT may remove these variables from the problem internally and not include them in the problem statistics.

Following the problem statistics, IPOPT will begin to solve the problem and you will see output resembling the following,

```
iter    objective    inf_pr    inf_du lg(mu) ||d|| lg(rg) alpha_du alpha_pr ls
    0 1.6109693e+01 1.12e+01 5.28e-01 0.0 0.00e+00 - 0.00e+00 0.00e+00 0
    1 1.8029749e+01 9.90e-01 6.62e+01 0.1 2.05e+00 - 2.14e-01 1.00e+00f 1
    2 1.8719906e+01 1.25e-02 9.04e+00 -2.2 5.94e-02 2.0 8.04e-01 1.00e+00h 1
```

and the columns of output are defined as

**iter** The current iteration count. This includes regular iterations and iterations while in restoration phase. If the algorithm is in the restoration phase, the letter r will be appended to the iteration number.

**objective** The unscaled objective value at the current point. During the restoration phase, this value remains the unscaled objective value for the original problem.

- inf\_pr The unscaled constraint violation at the current point. This quantity is the infinity-norm (max) of the (unscaled) constraint violation. During the restoration phase, this value remains the constraint violation of the original problem at the current point. The option "inf\_pr\_output" can be used to switch to the printing of a different quantity. During the restoration phase, this value is the primal infeasibility of the original problem at the current point.
- inf\_du The scaled dual infeasibility at the current point. This quantity measure the infinity-norm (max) of the internal dual infeasibility [29, Eq. (4a)], including inequality constraints reformulated using slack variables and problem scaling. During the restoration phase, this is the value of the dual infeasibility for the restoration phase problem.
- **lg(mu)**  $\log_{10}$  of the value of the barrier parameter  $\mu$ .
- ||d|| The infinity norm (max) of the primal step (for the original variables x and the internal slack variables s). During the restoration phase, this value includes the values of additional variables, p and n [29, Eq. (10)].
- **lg(rg)**  $\log_{10}$  of the value of the regularization term for the Hessian of the Lagrangian in the augmented system ( $\delta_w$  in [29, Eq. (26)]). A dash ("-") indicates that no regularization was done.
- **alpha\_du** The stepsize for the dual variables ( $\alpha_k^z$  in [29, Eq. (14c)])...
- **alpha\_pr** The stepsize for the primal variables ( $\alpha_k$  in [29, Eq. (14a)]). The number is usually followed by a character for additional diagnostic information regarding the step acceptance criterion:
  - f f-type iteration in the filter method w/o second order correction
  - F f-type iteration in the filter method w/ second order correction
  - h h-type iteration in the filter method w/o second order correction
  - H h-type iteration in the filter method w/ second order correction
  - k penalty value unchanged in merit function method w/o second order correction
  - K penalty value unchanged in merit function method w/ second order correction
  - n penalty value updated in merit function method w/o second order correction
  - N penalty value updated in merit function method w/ second order correction
  - R Restoration phase just started
  - w in watchdog procedure
  - s step accepted in soft restoration phase
  - t/T tiny step accepted without line search
    - r some previous iterate restored

ls The number of backtracking line search steps (does not include second-order correction steps).

Note that the step acceptance mechanisms in IPOPT consider the barrier objective function [29, Eq. (3a)] which is usually different from the value reported in the objective column. Similarly, for the purposes of the step acceptance, the constraint violation is measured for the internal problem formulation, which includes slack variables for inequality constraints and potentially scaling of the constraint functions. This value, too, is usually different from the value reported in inf\_pr. As a consequence, a new iterate might have worse values both for the objective function and the constraint violation as reported in the iteration output, seemingly contradicting globalization procedure.

When the algorithm terminates, IPOPT will output a message to the screen. The following is a list of the possible output messages and a brief description.

# **Optimal Solution Found.**

This message indicates that IPOPT found a (locally) optimal point within the desired tolerances.

#### Solved To Acceptable Level.

This indicates that the algorithm did not converge to the "desired" tolerances, but that it was able to obtain a point satisfying the "acceptable" tolerance level as specified by acceptable-\* options. This may happen if the desired tolerances are too small for the current problem.

# Feasible point for square problem found.

This message is printed if the problem is "square" (i.e., it has as many equality constraints as free variables) and IPOPT found a feasible point.

# Converged to a point of local infeasibility. Problem may be infeasible.

The restoration phase converged to a point that is a minimizer for the constraint violation (in the  $\ell_1$ -norm), but is not feasible for the original problem. This indicates that the problem may be infeasible (or at least that the algorithm is stuck at a locally infeasible point). The returned point (the minimizer of the constraint violation) might help you to find which constraint is causing the problem. If you believe that the NLP is feasible, it might help to start the optimization from a different point.

# Search Direction is becoming Too Small.

This indicates that IPOPT is calculating very small step sizes and making very little progress. This could happen if the problem has been solved to the best numerical accuracy possible given the current scaling.

# Iterates divering; problem might be unbounded.

This message is printed if the max-norm of the iterates becomes larger than the value of the option diverging\_iterates\_tol. This can happen if the problem is unbounded below and the iterates are diverging.

#### Stopping optimization at current point as requested by user.

This message is printed if either the Ctrl+C was pressed or the domain violation limit is reached.

#### **Maximum Number of Iterations Exceeded.**

This indicates that IPOPT has exceeded the maximum number of iterations as specified by the IPOPT option max\_iter or the GAMS option iterlim.

#### Maximum CPU time exceeded.

This indicates that IPOPT has exceeded the maximum number of seconds as specified by the IPOPT option max\_cpu\_time or the GAMS option reslim.

# **Restoration Failed!**

This indicates that the restoration phase failed to find a feasible point that was acceptable to the filter line search for the original problem. This could happen if the problem is highly degenerate or does not satisfy the constraint qualification, or if an external function in GAMS provides incorrect derivative information.

#### Error in step computation (regularization becomes too large?)!

This messages is printed if IPOPT is unable to compute a search direction, despite several attempts to modify the iteration matrix. Usually, the value of the regularization parameter then becomes too large.

# Problem has too few degrees of freedom.

This indicates that your problem, as specified, has too few degrees of freedom. This can happen if you have too many equality constraints, or if you fix too many variables (IPOPT removes fixed variables).

# Not enough memory.

An error occurred while trying to allocate memory. The problem may be too large for your current memory and swap configuration.

# INTERNAL ERROR: Unknown SolverReturn value - Notify IPOPT Authors.

An unknown internal error has occurred. Please notify the authors of the GAMS/IPOPT link or IPOPT (refer to https://projects.coin-or.org/GAMSlinks or https://projects.coin-or.org/Ipopt).

# 5.4 Diagnostic Tags for IPOPT

To print additional diagnostic tags for each iteration of IPOPT, set the options print\_info\_string to yes. With this, a tag will appear at the end of an iteration line with the following diagnostic meaning that are useful to flag difficulties for a particular IPOPT run. The following is a list of possible strings:

```
! Tighten resto tolerance if only slightly infeasible [29, Sec. 3.3]
```

- A Current iteration is acceptable (alternate termination)
- a Perturbation for PD Singularity can't be done, assume singular [29, Sec. 3.1]
- C Second Order Correction taken [29, Sec. 2.4]
- Dh Hessian degenerate based on multiple iterations [29, Sec. 3.1]
- Dhj Hessian/Jacobian degenerate based on multiple iterations [29, Sec. 3.1]
- Dj Jacobian degenerate based on multiple iterations [29, Sec. 3.1]
- dx  $\delta_x$  perturbation too large [29, Sec. 3.1]
- e Cutting back  $\alpha$  due to evaluation error (in backtracking line search)
- F- Filter should be reset, but maximal resets exceeded [29, Sec. 2.3]
- F+ Resetting filter due to last few rejections of filter [29, Sec. 2.3]
- L Degenerate Jacobian,  $\delta_c$  already perturbed [29, Sec. 3.1]
- 1 Degenerate Jacobian,  $\delta_c$  perturbed [29, Sec. 3.1]
- M Magic step taken for slack variables (in backtracking line search)
- Nh Hessian not yet degenerate [29, Sec. 3.1]
- Nhj Hessian/Jacobian not yet degenerate [29, Sec. 3.1]
- Nj Jacobian not yet degenerate [29, Sec. 3.1]
- NW Warm start initialization failed (in Warm Start Initialization)
- q PD system possibly singular, attempt to improve solution quality [29, Sec. 3.1]
- R Solution of restoration phase [29, Sec. 3.3]
- S PD system possibly singular, accept current solution [29, Sec. 3.1]
- s PD system singular [29, Sec. 3.1]
- s Square Problem. Set multipliers to zero (default initialization routine)
- Tmax Trial  $\theta$  is larger than  $\theta_{max}$  (filter parameter [29, Eq. (21)])
  - W Watchdog line search procedure successful [29, Sec. 3.2]
  - w Watchdog line search procedure unsuccessful, stopped [29, Sec. 3.2]
  - Wb Undoing most recent SR1 update [7, Sec. 5.4.1]
  - We Skip Limited-Memory Update in restoration phase [7, Sec. 5.4.1]
  - Wp Safeguard  $B^0 = \sigma I$  for Limited-Memory Update [7, Sec. 5.4.1]
  - Wr Resetting Limited-Memory Update [7, Sec. 5.4.1]
  - Ws Skip Limited-Memory Update since  $s^T y$  is not positive [7, Sec. 5.4.1]
  - WS Skip Limited-Memory Update since  $\Delta x$  is too small [7, Sec. 5.4.1]
  - y Dual infeasibility, use least square multiplier update (during IPOPT algorithm)
  - z Apply correction to bound multiplier if too large (during IPOPT algorithm)

# 5.5 Detailed Options Description

# **Barrier Parameter Update**

adaptive\_mu\_globalization (kkt-error, obj-constr-filter, never-monotone-mode) obj-constr-filter Globalization strategy for the adaptive mu selection mode.

To achieve global convergence of the adaptive version, the algorithm has to switch to the monotone mode (Fiacco-McCormick approach) when convergence does not seem to appear. This option sets the criterion used to decide when to do this switch. (Only used if option "mu\_strategy" is chosen as "adaptive".)

kkt-error nonmonotone decrease of kkt-error

obj-constr-filter 2-dim filter for objective and constraint violation

never-monotone-mode disables globalization

adaptive\_mu\_kkt\_norm\_type (1-norm, 2-norm-squared, max-norm, 2-norm)

2-norm-squared

Norm used for the KKT error in the adaptive mu globalization strategies.

When computing the KKT error for the globalization strategies, the norm to be used is specified with this option. Note, this options is also used in the QualityFunctionMuOracle.

1-norm use the 1-norm (abs sum)

2-norm-squared use the 2-norm squared (sum of squares)

max-norm use the infinity norm (max)

2-norm use 2-norm

adaptive\_mu\_kkterror\_red\_fact (0 < real < 1)

0.9999

Sufficient decrease factor for "kkt-error" globalization strategy.

For the "kkt-error" based globalization strategy, the error must decrease by this factor to be deemed sufficient decrease.

adaptive\_mu\_kkterror\_red\_iters  $(0 \le integer)$ 

4

Maximum number of iterations requiring sufficient progress.

For the "kkt-error" based globalization strategy, sufficient progress must be made for "adaptive\_mu\_kkterror\_red\_iters" iterations. If this number of iterations is exceeded, the globalization strategy switches to the monotone mode.

```
adaptive_mu_monotone_init_factor (0 < real)
```

0.8

Determines the initial value of the barrier parameter when switching to the monotone mode.

When the globalization strategy for the adaptive barrier algorithm switches to the monotone mode and fixed\_mu\_oracle is chosen as "average\_compl", the barrier parameter is set to the current average complementarity times the value of "adaptive\_mu\_monotone\_init\_factor".

```
adaptive_mu_restore_previous_iterate (no, yes)
```

no

Indicates if the previous iterate should be restored if the monotone mode is entered.

When the globalization strategy for the adaptive barrier algorithm switches to the monotone mode, it can either start from the most recent iterate (no), or from the last iterate that was accepted (yes).

no don't restore accepted iterate

yes restore accepted iterate

```
barrier_tol_factor (0 < real)
```

10

Factor for mu in barrier stop test.

The convergence tolerance for each barrier problem in the monotone mode is the value of the barrier parameter times "barrier\_tol\_factor". This option is also used in the adaptive mu strategy during the monotone mode. (This is kappa\_epsilon in implementation paper).

```
filter_margin_fact (0 < real < 1)
```

 $10^{-5}$ 

Factor determining width of margin for obj-constr-filter adaptive globalization strategy.

When using the adaptive globalization strategy, "obj-constr-filter", sufficient progress for a filter entry is defined as follows: (new obj) < (filter obj) - filter\_margin\_fact\*(new constr-viol) OR (new constr-viol) < (filter constr-viol) - filter\_margin\_fact\*(new constr-viol). For the description of the "kkt-error-filter" option see "filter\_max\_margin".

```
filter_max_margin (0 < real)
```

1

Maximum width of margin in obj-constr-filter adaptive globalization strategy.

fixed\_mu\_oracle (probing, loqo, quality-function, average\_compl)

average\_compl

Oracle for the barrier parameter when switching to fixed mode.

Determines how the first value of the barrier parameter should be computed when switching to the "monotone mode" in the adaptive strategy. (Only considered if "adaptive" is selected for option "mu\_strategy".)

probing Mehrotra's probing heuristic

logo LOQO's centrality rule

quality-function minimize a quality function

average\_compl base on current average complementarity

mu\_allow\_fast\_monotone\_decrease (no, yes)

yes

Allow skipping of barrier problem if barrier test is already met.

If set to "no", the algorithm enforces at least one iteration per barrier problem, even if the barrier test is already met for the updated barrier parameter.

no Take at least one iteration per barrier problem

yes Allow fast decrease of mu if barrier test it met

 $mu_init (0 < real)$ 

Initial value for the barrier parameter.

This option determines the initial value for the barrier parameter (mu). It is only relevant in the monotone, Fiacco-McCormick version of the algorithm. (i.e., if "mu\_strategy" is chosen as "monotone")

 $mu\_linear\_decrease\_factor (0 < real < 1)$ 

0.2

Determines linear decrease rate of barrier parameter.

For the Fiacco-McCormick update procedure the new barrier parameter mu is obtained by taking the minimum of mu\*"mu\_linear\_decrease\_fact and mu"superlinear\_decrease\_power". (This is kappa\_mu in implementation paper.) This option is also used in the adaptive mu strategy during the monotone mode.

 $mu\_max (0 < real)$  100000

Maximum value for barrier parameter.

This option specifies an upper bound on the barrier parameter in the adaptive mu selection mode. If this option is set, it overwrites the effect of mu\_max\_fact. (Only used if option "mu\_strategy" is chosen as "adaptive".)

 $mu_max_fact (0 < real)$ 

Factor for initialization of maximum value for barrier parameter.

This option determines the upper bound on the barrier parameter. This upper bound is computed as the average complementarity at the initial point times the value of this option. (Only used if option "mu\_strategy" is chosen as "adaptive".)

mu\_min (0 < real)

Minimum value for barrier parameter.

This option specifies the lower bound on the barrier parameter in the adaptive mu selection mode. By default, it is set to the minimum of 1e-11 and min("tol","compl\_inf\_tol")/("barrier\_tol\_factor"+1), which should be a reasonable value. (Only used if option "mu\_strategy" is chosen as "adaptive".)

mu\_oracle (probing, loqo, quality-function)

quality-function

Oracle for a new barrier parameter in the adaptive strategy.

Determines how a new barrier parameter is computed in each "free-mode" iteration of the adaptive barrier parameter strategy. (Only considered if "adaptive" is selected for option "mu\_strategy").

probing Mehrotra's probing heuristic

logo LOQO's centrality rule

quality-function minimize a quality function

mu\_strategy (monotone, adaptive)

adaptive

Update strategy for barrier parameter.

Determines which barrier parameter update strategy is to be used.

monotone use the monotone (Fiacco-McCormick) strategy

adaptive use the adaptive update strategy

 ${\tt mu\_superlinear\_decrease\_power} \ (1 < real < 2)$ 

1.5

Determines superlinear decrease rate of barrier parameter.

For the Fiacco-McCormick update procedure the new barrier parameter mu is obtained by taking the minimum of mu\*"mu\_linear\_decrease and mu"superlinear\_decrease\_power". (This is theta\_mu in implementation paper.) This option is also used in the adaptive mu strategy during the monotone mode.

quality\_function\_balancing\_term (none, cubic)

none

The balancing term included in the quality function for centrality.

This determines whether a term is added to the quality function that penalizes situations where the complementarity is much smaller than dual and primal infeasibilities. (Only used if option "mu\_oracle" is set to "quality-function".)

none no balancing term is added

cubic Max(0,Max(dual\_inf,primal\_inf)-compl)3

quality\_function\_centrality (none, log, reciprocal, cubed-reciprocal)

none

The penalty term for centrality that is included in quality function.

This determines whether a term is added to the quality function to penalize deviation from centrality with respect to complementarity. The complementarity measure here is the xi in the Loqo update rule. (Only used if option "mu\_oracle" is set to "quality-function".)

none no penalty term is added

log complementarity \* the log of the centrality measure

reciprocal complementarity \* the reciprocal of the centrality measure

cubed-reciprocal complementarity \* the reciprocal of the centrality measure cubed

 $quality\_function\_max\_section\_steps$  ( $0 \le integer$ )

8

Maximum number of search steps during direct search procedure determining the optimal centering parameter.

The golden section search is performed for the quality function based mu oracle. (Only used if option "mu\_oracle" is set to "quality-function".)

quality\_function\_norm\_type (1-norm, 2-norm-squared, max-norm, 2-norm) Norm used for components of the quality function.

2-norm-squared

(Only used if option "mu\_oracle" is set to "quality-function".)

1-norm use the 1-norm (abs sum)

2-norm-squared use the 2-norm squared (sum of squares)

max-norm use the infinity norm (max)

2-norm use 2-norm

 $quality\_function\_section\_qf\_tol (0 \le real < 1)$ 

(

Tolerance for the golden section search procedure determining the optimal centering parameter (in the function value space). The golden section search is performed for the quality function based mu oracle. (Only used if option "mu\_oracle" is set to "quality-function".)

quality\_function\_section\_sigma\_tol  $(0 \le real < 1)$ 

0.01

Tolerance for the section search procedure determining the optimal centering parameter (in sigma space).

The golden section search is performed for the quality function based mu oracle. (Only used if option "mu\_oracle" is set to "quality-function".)

 $sigma_max (0 < real)$ 

100

Maximum value of the centering parameter.

This is the upper bound for the centering parameter chosen by the quality function based barrier parameter update. (Only used if option "mu\_oracle" is set to "quality-function".)

 $sigma_min (0 \le real)$ 

 $10^{-6}$ 

Minimum value of the centering parameter.

This is the lower bound for the centering parameter chosen by the quality function based barrier parameter update. (Only used if option "mu\_oracle" is set to "quality-function".)

 $tau_min (0 < real < 1)$ 

0.99

Lower bound on fraction-to-the-boundary parameter tau.

(This is tau\_min in the implementation paper.) This option is also used in the adaptive mu strategy during the monotone mode.

# Convergence

 $acceptable\_compl\_inf\_tol (0 < real)$ 

0.01

"Acceptance" threshold for the complementarity conditions.

Absolute tolerance on the complementarity. "Acceptable" termination requires that the max-norm of the (unscaled) complementarity is less than this threshold; see also acceptable\_tol.

 $acceptable\_constr\_viol\_tol (0 < real)$ 

0.01

"Acceptance" threshold for the constraint violation.

Absolute tolerance on the constraint violation. "Acceptable" termination requires that the max-norm of the (unscaled) constraint violation is less than this threshold; see also acceptable\_tol.

acceptable\_dual\_inf\_tol (0 < real)

 $10^{10}$ 

"Acceptance" threshold for the dual infeasibility.

Absolute tolerance on the dual infeasibility. "Acceptable" termination requires that the (max-norm of the unscaled) dual infeasibility is less than this threshold; see also acceptable\_tol.

 $acceptable_iter (0 \le integer)$ 

15

Number of "acceptable" iterates before triggering termination.

If the algorithm encounters this many successive "acceptable" iterates (see "acceptable\_tol"), it terminates, assuming that the problem has been solved to best possible accuracy given round-off. If it is set to zero, this heuristic is disabled.

 $acceptable_obj_change_tol (0 \le real)$ 

 $10^{20}$ 

"Acceptance" stopping criterion based on objective function change.

If the relative change of the objective function (scaled by Max(1, -f(x))) is less than this value, this part of the acceptable tolerance termination is satisfied; see also acceptable\_tol. This is useful for the quasi-Newton option, which has trouble to bring down the dual infeasibility.

 $acceptable_tol (0 < real)$ 

 $10^{-6}$ 

"Acceptable" convergence tolerance (relative).

Determines which (scaled) overall optimality error is considered to be "acceptable." There are two levels of termination criteria. If the usual "desired" tolerances (see tol, dual\_inf\_tol etc) are satisfied at an iteration, the algorithm immediately terminates with a success message. On the other hand, if the algorithm encounters "acceptable\_iter" many iterations in a row that are considered "acceptable", it will terminate before the desired convergence tolerance is met. This is useful in cases where the algorithm might not be able to achieve the "desired" level of accuracy.

compl\_inf\_tol (0 < real)

0.0001

Desired threshold for the complementarity conditions.

Absolute tolerance on the complementarity. Successful termination requires that the max-norm of the (unscaled) complementarity is less than this threshold.

constr\_viol\_tol (0 < real)

0.0001

Desired threshold for the constraint violation.

Absolute tolerance on the constraint violation. Successful termination requires that the max-norm of the (unscaled) constraint violation is less than this threshold.

 $diverging\_iterates\_tol (0 < real)$ 

 $10^{20}$ 

Threshold for maximal value of primal iterates.

If any component of the primal iterates exceeded this value (in absolute terms), the optimization is aborted with the exit message that the iterates seem to be diverging.

 $dual_inf_tol (0 < real)$ 

1

Desired threshold for the dual infeasibility.

Absolute tolerance on the dual infeasibility. Successful termination requires that the max-norm of the (unscaled) dual infeasibility is less than this threshold.

 ${\tt max\_cpu\_time} \ (0 < real)$ 

1000

Maximum number of CPU seconds.

A limit on CPU seconds that Ipopt can use to solve one problem. If during the convergence check this limit is exceeded, Ipopt will terminate with a corresponding error message.

 $\max_{\text{iter}} (0 \leq \text{integer})$ 

 $\infty$ 

Maximum number of iterations.

The algorithm terminates with an error message if the number of iterations exceeded this number.

 $mu\_target (0 \le real)$ 

0

Desired value of complementarity.

Usually, the barrier parameter is driven to zero and the termination test for complementarity is measured with respect to zero complementarity. However, in some cases it might be desired to have Ipopt solve barrier problem for strictly positive value of the barrier parameter. In this case, the value of "mu\_target" specifies the final value of the barrier parameter, and the termination tests are then defined with respect to the barrier problem for this value of the barrier parameter.

 $s_max (0 < real)$ 100

Scaling threshold for the NLP error.

(See paragraph after Eqn. (6) in the implementation paper.)

 $10^{-8}$ tol (0 < real)

Desired convergence tolerance (relative).

Determines the convergence tolerance for the algorithm. The algorithm terminates successfully, if the (scaled) NLP error becomes smaller than this value, and if the (absolute) criteria according to "dual\_inf\_tol", "primal\_inf\_tol", and "compl\_inf\_tol" are met. (This is epsilon\_tol in Eqn. (6) in implementation paper). See also "acceptable\_tol" as a second termination criterion. Note, some other algorithmic features also use this quantity to determine thresholds etc.

# **Hessian Approximation**

hessian\_approximation (exact, limited-memory)

exact

Indicates what Hessian information is to be used.

This determines which kind of information for the Hessian of the Lagrangian function is used by the algorithm.

exact Use second derivatives provided by the NLP.

limited-memory Perform a limited-memory quasi-Newton approximation

hessian\_approximation\_space (nonlinear-variables, all-variables)

nonlinear-variables

Indicates in which subspace the Hessian information is to be approximated.

nonlinear-variables only in space of nonlinear variables.

all-variables in space of all variables (without slacks)

limited\_memory\_aug\_solver (sherman-morrison, extended)

sherman-morrison

Strategy for solving the augmented system for low-rank Hessian.

sherman-morrison use Sherman-Morrison formula

extended use an extended augmented system

limited\_memory\_init\_val (0 < real)</pre>

1

Value for B0 in low-rank update.

The starting matrix in the low rank update, B0, is chosen to be this multiple of the identity in the first iteration (when no updates have been performed yet), and is constantly chosen as this value, if "limited\_memory\_initialization" is "constant".

limited\_memory\_init\_val\_max (0 < real)</pre>

 $10^{8}$ 

Upper bound on value for B0 in low-rank update.

The starting matrix in the low rank update, B0, is chosen to be this multiple of the identity in the first iteration (when no updates have been performed yet), and is constantly chosen as this value, if "limited\_memory\_initialization" is "constant".

limited\_memory\_init\_val\_min (0 < real)</pre>

 $10^{-8}$ 

Lower bound on value for B0 in low-rank update.

The starting matrix in the low rank update, B0, is chosen to be this multiple of the identity in the first iteration (when no updates have been performed yet), and is constantly chosen as this value, if "limited\_memory\_initialization" is "constant".

limited\_memory\_initialization (scalar1, scalar2, scalar3, scalar4, constant)

scalar1

Initialization strategy for the limited memory quasi-Newton approximation.

Determines how the diagonal Matrix  $B_0$  as the first term in the limited memory approximation should be computed.

scalar1 sigma = 
$$s^T y/s^T s$$
  
scalar2 sigma =  $y^T y/s^T y$ 

scalar3 arithmetic average of scalar1 and scalar2

scalar4 geometric average of scalar1 and scalar2

constant sigma = limited\_memory\_init\_val

limited\_memory\_max\_history  $(0 \le integer)$ 

6

Maximum size of the history for the limited quasi-Newton Hessian approximation.

This option determines the number of most recent iterations that are taken into account for the limited-memory quasi-Newton approximation.

limited\_memory\_max\_skipping  $(1 \le integer)$ 

2

Threshold for successive iterations where update is skipped.

If the update is skipped more than this number of successive iterations, we quasi-Newton approximation is reset.

limited\_memory\_special\_for\_resto (no, yes)

no

Determines if the quasi-Newton updates should be special during the restoration phase.

Until Nov 2010, Ipopt used a special update during the restoration phase, but it turned out that this does not work well. The new default uses the regular update procedure and it improves results. If for some reason you want to get back to the original update, set this option to "yes".

no use the same update as in regular iterations

yes use the a special update during restoration phase

limited\_memory\_update\_type (bfgs, sr1)

bfgs

Quasi-Newton update formula for the limited memory approximation.

Determines which update formula is to be used for the limited-memory quasi-Newton approximation.

bfgs BFGS update (with skipping)

sr1 SR1 (not working well)

#### Initialization

bound\_frac  $(0 < \text{real} \le 0.5)$ 

0.01

Desired minimum relative distance from the initial point to bound.

Determines how much the initial point might have to be modified in order to be sufficiently inside the bounds (together with "bound\_push"). (This is kappa\_2 in Section 3.6 of implementation paper.)

bound\_mult\_init\_method (constant, mu-based)

constant

Initialization method for bound multipliers

This option defines how the iterates for the bound multipliers are initialized. If "constant" is chosen, then all bound multipliers are initialized to the value of "bound\_mult\_init\_val". If "mu-based" is chosen, the each value is initialized to the the value of "mu\_init" divided by the corresponding slack variable. This latter option might be useful if the starting point is close to the optimal solution.

constant set all bound multipliers to the value of bound\_mult\_init\_val

mu-based initialize to mu\_init/x\_slack

bound\_mult\_init\_val (0 < real)

1

Initial value for the bound multipliers.

All dual variables corresponding to bound constraints are initialized to this value.

bound\_push (0 < real)Desired minimum absolute distance from the initial point to bound. 0.01

Determines how much the initial point might have to be modified in order to be sufficiently inside the bounds (together with "bound\_frac"). (This is kappa\_1 in Section 3.6 of implementation paper.)

 $constr_mult_init_max (0 \le real)$ 

1000

Maximum allowed least-square guess of constraint multipliers.

Determines how large the initial least-square guesses of the constraint multipliers are allowed to be (in max-norm). If the guess is larger than this value, it is discarded and all constraint multipliers are set to zero. This options is also used when initializing the restoration phase. By default, "resto.constr\_mult\_init\_max" (the one used in RestoIterateInitializer) is set to zero.

least\_square\_init\_duals (no, yes)

no

Least square initialization of all dual variables

If set to yes, Ipopt tries to compute least-square multipliers (considering ALL dual variables). If successful, the bound multipliers are possibly corrected to be at least bound\_mult\_init\_val. This might be useful if the user doesn't know anything about the starting point, or for solving an LP or QP. This overwrites option "bound\_mult\_init\_method".

no use bound\_mult\_init\_val and least-square equality constraint multipliers

yes overwrite user-provided point with least-square estimates

least\_square\_init\_primal (no, yes)

no

Least square initialization of the primal variables

If set to yes, Ipopt ignores the user provided point and solves a least square problem for the primal variables (x and s), to fit the linearized equality and inequality constraints. This might be useful if the user doesn't know anything about the starting point, or for solving an LP or QP.

no take user-provided point

yes overwrite user-provided point with least-square estimates

 $slack_bound_frac (0 < real \le 0.5)$ 

0.01

Desired minimum relative distance from the initial slack to bound.

Determines how much the initial slack variables might have to be modified in order to be sufficiently inside the inequality bounds (together with "slack\_bound\_push"). (This is kappa\_2 in Section 3.6 of implementation paper.)

slack\_bound\_push (0 < real)

0.01

Desired minimum absolute distance from the initial slack to bound.

Determines how much the initial slack variables might have to be modified in order to be sufficiently inside the inequality bounds (together with "slack\_bound\_frac"). (This is kappa\_1 in Section 3.6 of implementation paper.)

# Line Search

 $accept\_after\_max\_steps (-1 \le integer)$ 

-1

Accept a trial point after maximal this number of steps.

Even if it does not satisfy line search conditions.

accept\_every\_trial\_step (no, yes)

no

Always accept the first trial step.

Setting this option to "yes" essentially disables the line search and makes the algorithm take aggressive steps, without global convergence guarantees.

no don't arbitrarily accept the full step

yes always accept the full step

alpha\_for\_y (primal, bound-mult, min, max, full, min-dual-infeas, safer-min-dual-infeas, primal-and-full dual-and-full, acceptor) primal

Method to determine the step size for constraint multipliers.

This option determines how the step size (alpha\_y) will be calculated when updating the constraint multipliers.

primal use primal step size

bound-mult use step size for the bound multipliers (good for LPs)

min use the min of primal and bound multipliers

max use the max of primal and bound multipliers

full take a full step of size one

min-dual-infeas choose step size minimizing new dual infeasibility

safer-min-dual-infeas like "min\_dual\_infeas", but safeguarded by "min" and "max"

primal-and-full use the primal step size, and full step if delta\_x <= alpha\_for\_y\_tol

dual-and-full use the dual step size, and full step if delta\_x <= alpha\_for\_y\_tol

acceptor Call LSAcceptor to get step size for y

 $alpha_for_y_tol (0 \le real)$ 

10

Tolerance for switching to full equality multiplier steps.

This is only relevant if "alpha\_for\_y" is chosen "primal-and-full" or "dual-and-full". The step size for the equality constraint multipliers is taken to be one if the max-norm of the primal step is less than this tolerance.

 $alpha_min_frac (0 < real < 1)$ 

0.05

Safety factor for the minimal step size (before switching to restoration phase).

(This is gamma\_alpha in Eqn. (20) in the implementation paper.)

 $alpha_red_factor (0 < real < 1)$ 

0.5

Fractional reduction of the trial step size in the backtracking line search.

At every step of the backtracking line search, the trial step size is reduced by this factor.

constraint\_violation\_norm\_type (1-norm, 2-norm, max-norm)

1-norm

Norm to be used for the constraint violation in the line search.

Determines which norm should be used when the algorithm computes the constraint violation in the line search.

1-norm use the 1-norm

2-norm use the 2-norm

max-norm use the infinity norm

corrector\_compl\_avrg\_red\_fact (0 < real)

1

Complementarity tolerance factor for accepting corrector step (unsupported!).

This option determines the factor by which complementarity is allowed to increase for a corrector step to be accepted.

corrector\_type (none, affine, primal-dual)

none

1

 $10^{-8}$ 

5

The type of corrector steps that should be taken (unsupported!).

If "mu\_strategy" is "adaptive", this option determines what kind of corrector steps should be tried.

none no corrector

affine corrector step towards mu=0

primal-dual corrector step towards current mu

delta (0 < real)

Multiplier for constraint violation in the switching rule.

(See Eqn. (19) in the implementation paper.)

eta\_phi (0 < real < 0.5)

Relaxation factor in the Armijo condition.

(See Eqn. (20) in the implementation paper)

(See Eqn. (20) in the implementation paper)

filter\_reset\_trigger  $(1 \le integer)$ Number of iterations that trigger the filter reset.

If the filter reset heuristic is active and the number of successive iterations in which the last rejected trial step size was rejected because of the filter, the filter is reset.

 $gamma_phi (0 < real < 1)$ 

 $10^{-8}$ 

Relaxation factor in the filter margin for the barrier function.

(See Eqn. (18a) in the implementation paper.)

 $gamma_theta (0 < real < 1)$ 

 $10^{-5}$ 

Relaxation factor in the filter margin for the constraint violation.

(See Eqn. (18b) in the implementation paper.)

 $kappa_sigma (0 < real)$ 

 $10^{10}$ 

Factor limiting the deviation of dual variables from primal estimates.

If the dual variables deviate from their primal estimates, a correction is performed. (See Eqn. (16) in the implementation paper.) Setting the value to less than 1 disables the correction.

 $kappa\_soc (0 < real)$ 

0.99

Factor in the sufficient reduction rule for second order correction.

This option determines how much a second order correction step must reduce the constraint violation so that further correction steps are attempted. (See Step A-5.9 of Algorithm A in the implementation paper.)

line\_search\_method (filter, cg-penalty, penalty)

filter

Globalization method used in backtracking line search

Only the "filter" choice is officially supported. But sometimes, good results might be obtained with the other choices.

filter Filter method

cg-penalty Chen-Goldfarb penalty function

penalty Standard penalty function

 $max\_filter\_resets (0 \le integer)$ 

5

4

Maximal allowed number of filter resets

A positive number enables a heuristic that resets the filter, whenever in more than "filter\_reset\_trigger" successive iterations the last rejected trial steps size was rejected because of the filter. This option determine the maximal number of resets that are allowed to take place.

 $max\_soc (0 \le integer)$ 

Maximum number of second order correction trial steps at each iteration.

Choosing 0 disables the second order corrections. (This is pmax of Step A-5.9 of Algorithm A in the implementation paper.)

 $nu\_inc (0 < real)$  0.0001

Increment of the penalty parameter.

nu\_init (0 < real)

Initial value of the penalty parameter.

obj\_max\_inc (1 < real)

Determines the upper bound on the acceptable increase of barrier objective function.

Trial points are rejected if they lead to an increase in the barrier objective function by more than obj\_max\_inc orders of magnitude.

recalc\_y (no, yes)

Tells the algorithm to recalculate the equality and inequality multipliers as least square estimates.

This asks the algorithm to recompute the multipliers, whenever the current infeasibility is less than recalc\_y\_feas\_tol. Choosing yes might be helpful in the quasi-Newton option. However, each recalculation requires an extra factorization of the linear system. If a limited memory quasi-Newton option is chosen, this is used by default.

no use the Newton step to update the multipliers

Feasibility threshold for recomputation of multipliers.

yes use least-square multiplier estimates

 $recalc_y_feas_tol (0 < real)$ 

 $10^{-6}$ 

0.1

If recalc\_y is chosen and the current infeasibility is less than this value, then the multipliers are recomputed.

rho (0 < real < 1)

Value in penalty parameter update formula.

s\_phi (1 < real) 2.3

Exponent for linear barrier function model in the switching rule.

(See Eqn. (19) in the implementation paper.)

 $s_{-}$ theta (1 < real)

Exponent for current constraint violation in the switching rule.

(See Eqn. (19) in the implementation paper.)

skip\_corr\_if\_neg\_curv (no, yes)

yes

Skip the corrector step in negative curvature iteration (unsupported!).

The corrector step is not tried if negative curvature has been encountered during the computation of the search direction in the current iteration. This option is only used if "mu\_strategy" is "adaptive".

no don't skip

yes skip

skip\_corr\_in\_monotone\_mode (no, yes)

yes

Skip the corrector step during monotone barrier parameter mode (unsupported!).

The corrector step is not tried if the algorithm is currently in the monotone mode (see also option "barrier\_strategy"). This option is only used if "mu\_strategy" is "adaptive".

no don't skip

yes skip

 $slack\_move (0 \le real)$ 

 $1.81899 \cdot 10^{-12}$ 

Correction size for very small slacks.

Due to numerical issues or the lack of an interior, the slack variables might become very small. If a slack becomes very small compared to machine precision, the corresponding bound is moved slightly. This parameter determines how large the move should be. Its default value is mach\_eps3/4. (See also end of Section 3.5 in implementation paper - but actual implementation might be somewhat different.)

theta\_max\_fact (0 < real)

10000

Determines upper bound for constraint violation in the filter.

The algorithmic parameter theta\_max is determined as theta\_max\_fact times the maximum of 1 and the constraint violation at initial point. Any point with a constraint violation larger than theta\_max is unacceptable to the filter (see Eqn. (21) in the implementation paper).

theta\_min\_fact (0 < real)

0.0001

Determines constraint violation threshold in the switching rule.

The algorithmic parameter theta\_min is determined as theta\_min\_fact times the maximum of 1 and the constraint violation at initial point. The switching rules treats an iteration as an h-type iteration whenever the current constraint violation is larger than theta\_min (see paragraph before Eqn. (19) in the implementation paper).

 $tiny_step_tol (0 < real)$ 

 $2.22045 \cdot 10^{-15}$ 

Tolerance for detecting numerically insignificant steps.

If the search direction in the primal variables (x and s) is, in relative terms for each component, less than this value, the algorithm accepts the full step without line search. If this happens repeatedly, the algorithm will terminate with a corresponding exit message. The default value is 10 times machine precision.

 $tiny_step_y_tol (0 \le real)$ 

0.01

Tolerance for quitting because of numerically insignificant steps.

If the search direction in the primal variables (x and s) is, in relative terms for each component, repeatedly less than tiny\_step\_tol, and the step in the y variables is smaller than this threshold, the algorithm will terminate.

watchdog\_shortened\_iter\_trigger  $(0 \le integer)$ 

10

Number of shortened iterations that trigger the watchdog.

If the number of successive iterations in which the backtracking line search did not accept the first trial point exceeds this number, the watchdog procedure is activated. Choosing "0" here disables the watchdog procedure.

watchdog\_trial\_iter\_max  $(1 \le integer)$ 

3

Maximum number of watchdog iterations.

This option determines the number of trial iterations allowed before the watchdog procedure is aborted and the algorithm returns to the stored point.

#### Linear Solver

linear\_scaling\_on\_demand (no, yes)

yes

Flag indicating that linear scaling is only done if it seems required.

This option is only important if a linear scaling method (e.g., mc19) is used. If you choose "no", then the scaling factors are computed for every linear system from the start. This can be quite expensive. Choosing "yes" means that the algorithm will start the scaling method only when the solutions to the linear system seem not good, and then use it until the end.

no Always scale the linear system.

yes Start using linear system scaling if solutions seem not good.

linear\_solver (ma27, ma57, ma86, pardiso, mumps)

ma27

Linear solver used for step computations.

Determines which linear algebra package is to be used for the solution of the augmented linear system (for obtaining the search directions). Note, that MA27, MA57, and MA86 are only available with a commercially supported GAMS/IpoptH license, or when the user provides a library with HSL code separately. If no GAMS/IpoptH license is available, the default

linear solver is MUMPS. For using Pardiso, a pardiso library need to be provided.

ma27 use the Harwell routine MA27

ma57 use the Harwell routine MA57

ma86 use the Harwell routine MA86

pardiso use the Pardiso package

mumps use MUMPS package

linear\_system\_scaling (none, mc19, slack-based)

mc19

Method for scaling the linear system.

Determines the method used to compute symmetric scaling factors for the augmented system (see also the "linear\_scaling\_on\_demand" option). This scaling is independent of the NLP problem scaling. By default, MC19 is only used if MA27 or MA57 are selected as linear solvers. Note, that MC19 is only available with a commercially supported GAMS/IpoptH license, or when the user provides a library with HSL code separately. If no commercial GAMS/IpoptH license is available, the default scaling method is slack-based.

none no scaling will be performed

mc19 use the Harwell routine MC19

slack-based use the slack values

#### **MA27 Linear Solver**

ma27\_ignore\_singularity (no, yes)

no

Enables MA27's ability to solve a linear system even if the matrix is singular.

Setting this option to "yes" means that Ipopt will call MA27 to compute solutions for right hand sides, even if MA27 has detected that the matrix is singular (but is still able to solve the linear system). In some cases this might be better than using Ipopt's heuristic of small perturbation of the lower diagonal of the KKT matrix.

no Don't have MA27 solve singular systems

yes Have MA27 solve singular systems

 $ma27\_la\_init\_factor (1 \le real)$ 

5

Real workspace memory for MA27.

The initial real workspace memory = la\_init\_factor \* memory required by unfactored system. Ipopt will increase the workspace size by meminc\_factor if required. This option is only available if Ipopt has been compiled with MA27.

 $ma27\_liw\_init\_factor (1 \le real)$ 

5

Integer workspace memory for MA27.

The initial integer workspace memory = liw\_init\_factor \* memory required by unfactored system. Ipopt will increase the workspace size by meminc\_factor if required. This option is only available if Ipopt has been compiled with MA27.

ma27\_meminc\_factor (1 < real)

10

Increment factor for workspace size for MA27.

If the integer or real workspace is not large enough, Ipopt will increase its size by this factor. This option is only available if Ipopt has been compiled with MA27.

ma27-pivtol (0 < real < 1)

 $10^{-8}$ 

Pivot tolerance for the linear solver MA27.

A smaller number pivots for sparsity, a larger number pivots for stability. This option is only available if Ipopt has been compiled with MA27.

ma27\_pivtolmax (0 < real < 1)

0.0001

Maximum pivot tolerance for the linear solver MA27.

Ipopt may increase pivtol as high as pivtolmax to get a more accurate solution to the linear system. This option is only available if Ipopt has been compiled with MA27.

ma27\_skip\_inertia\_check (no, yes)

no

Always pretend inertia is correct.

Setting this option to "yes" essentially disables inertia check. This option makes the algorithm non-robust and easily fail, but it might give some insight into the necessity of inertia control.

no check inertia

yes skip inertia check

#### **MA28 Linear Solver**

 $ma28\_pivtol (0 < real \le 1)$ 

0.01

Pivot tolerance for linear solver MA28.

This is used when MA28 tries to find the dependent constraints.

#### **MA57 Linear Solver**

ma57\_automatic\_scaling (no, yes)

yes

Controls MA57 automatic scaling

This option controls the internal scaling option of MA57. This is ICNTL(15) in MA57.

no Do not scale the linear system matrix

yes Scale the linear system matrix

 $ma57\_block\_size (1 \le integer)$ 

16

Controls block size used by Level 3 BLAS in MA57BD

This is ICNTL(11) in MA57.

 $ma57\_node\_amalgamation (1 \le integer)$ 

16

Node amalgamation parameter

This is ICNTL(12) in MA57.

 $ma57\_pivot\_order (0 \le integer \le 5)$ 

5

Controls pivot order in MA57

This is ICNTL(6) in MA57.

 $ma57_pivtol (0 < real < 1)$ 

 $10^{-8}$ 

Pivot tolerance for the linear solver MA57.

A smaller number pivots for sparsity, a larger number pivots for stability. This option is only available if Ipopt has been compiled with MA57.

 ${\tt ma57\_pivtolmax}\ (0 < {\tt real} < 1)$ 

0.0001

Maximum pivot tolerance for the linear solver MA57.

Ipopt may increase pivtol as high as ma57\_pivtolmax to get a more accurate solution to the linear system. This option is only available if Ipopt has been compiled with MA57.

 $ma57\_pre\_alloc (1 \le real)$ 

1.05

Safety factor for work space memory allocation for the linear solver MA57.

If 1 is chosen, the suggested amount of work space is used. However, choosing a larger number might avoid reallocation if the suggest values do not suffice. This option is only available if Ipopt has been compiled with MA57.

 $ma57\_small\_pivot\_flag (0 \le integer \le 1)$ 

0

If set to 1, then when small entries defined by CNTL(2) are detected they are removed and the corresponding pivots placed at the end of the factorization. This can be particularly efficient if the matrix is highly rank deficient.

This is ICNTL(16) in MA57.

#### MA86 Linear Solver

 $ma86\_nemin (1 \le integer)$ 

32

Node Amalgamation parameter

Two nodes in elimination tree are merged if result has fewer than ma86\_nemin variables.

ma86\_order (auto, amd, metis)

auto

Controls type of ordering used by HSL\_MA86

This option controls ordering for the solver HSL\_MA86.

auto Try both AMD and MeTiS, pick best

amd Use the HSL\_MC68 approximate minimum degree algorithm

metis Use the MeTiS nested dissection algorithm (if available)

ma86\_print\_level (integer)

-1

Debug printing level for the linear solver MA86

Meep

ma86\_scaling (none, mc64, mc77)

mc64

Controls scaling of matrix

This option controls scaling for the solver HSL\_MA86.

none Do not scale the linear system matrix

mc64 Scale linear system matrix using MC64

mc77 Scale linear system matrix using MC77 [1,3,0]

 $ma86\_small (0 \le real)$ 

 $10^{-20}$ 

Zero Pivot Threshold

Any pivot less than ma86\_small is treated as zero.

 $ma86\_static (0 \le real)$ 

0

Static Pivoting Threshold

See MA86 documentation. Either ma86\_static=0.0 or ma86\_static>ma86\_static=0.0 disables static pivoting.

ma86\_u  $(0 \le real \le 0.5)$ 

 $10^{-8}$ 

Pivoting Threshold

See MA86 documentation.

 $\texttt{ma86\_umax} \ (0 \le real \le 0.5)$ 

0.0001

Maximum Pivoting Threshold

Maximum value to which u will be increased to improve quality.

# **Mumps Linear Solver**

mumps\_dep\_tol (real)

0

Pivot threshold for detection of linearly dependent constraints in MUMPS.

When MUMPS is used to determine linearly dependent constraints, this is determines the threshold for a pivot to be considered zero. This is CNTL(3) in MUMPS.

 $mumps_mem_percent (0 \le integer)$ 

1000

Percentage increase in the estimated working space for MUMPS.

In MUMPS when significant extra fill-in is caused by numerical pivoting, larger values of mumps\_mem\_percent may help use the workspace more efficiently. On the other hand, if memory requirement are too large at the very beginning of the optimization, choosing a much smaller value for this option, such as 5, might reduce memory requirements.

mumps\_permuting\_scaling  $(0 \le integer \le 7)$ 

7

Controls permuting and scaling in MUMPS

This is ICNTL(6) in MUMPS.

 $mumps_pivot_order (0 \le integer \le 7)$ 

7

Controls pivot order in MUMPS

This is ICNTL(7) in MUMPS.

mumps\_pivtol  $(0 \le real \le 1)$ 

 $10^{-6}$ 

Pivot tolerance for the linear solver MUMPS.

A smaller number pivots for sparsity, a larger number pivots for stability. This option is only available if Ipopt has been compiled with MUMPS.

 $mumps\_pivtolmax (0 \le real \le 1)$ 

0.1

Maximum pivot tolerance for the linear solver MUMPS.

Ipopt may increase pivtol as high as pivtolmax to get a more accurate solution to the linear system. This option is only available if Ipopt has been compiled with MUMPS.

mumps\_scaling  $(-2 \le integer \le 77)$ 

77

Controls scaling in MUMPS

This is ICNTL(8) in MUMPS.

bound\_relax\_factor  $(0 \le real)$ 

 $10^{-10}$ 

Factor for initial relaxation of the bounds.

Before start of the optimization, the bounds given by the user are relaxed. This option sets the factor for this relaxation. If it is set to zero, then then bounds relaxation is disabled. (See Eqn. (35) in implementation paper.)

check\_derivatives\_for\_naninf (no, yes)

no

Indicates whether it is desired to check for Nan/Inf in derivative matrices

Activating this option will cause an error if an invalid number is detected in the constraint Jacobians or the Lagrangian Hessian. If this is not activated, the test is skipped, and the algorithm might proceed with invalid numbers and fail. If test is activated and an invalid number is detected, the matrix is written to output with print\_level corresponding to J\_MORE\_DETAILED; so beware of large output!

no Don't check (faster).

yes Check Jacobians and Hessian for Nan and Inf.

dependency\_detection\_with\_rhs (no, yes)

no

Indicates if the right hand sides of the constraints should be considered during dependency detection

no only look at gradients

yes also consider right hand side

dependency\_detector (none, mumps, wsmp, ma28)

none

Indicates which linear solver should be used to detect linearly dependent equality constraints.

The default and available choices depend on how Ipopt has been compiled. This is experimental and does not work well.

none don't check; no extra work at beginning

mumps use MUMPS

wsmp use WSMP

ma28 use MA28

 ${\tt fixed\_variable\_treatment~(make\_parameter,~make\_constraint,~relax\_bounds)}$ 

make\_parameter

Determines how fixed variables should be handled.

The main difference between those options is that the starting point in the "make\_constraint" case still has the fixed variables at their given values, whereas in the case "make\_parameter" the functions are always evaluated with the fixed values for those variables. Also, for "relax\_bounds", the fixing bound constraints are relaxed (according to bound\_relax\_factor"). For both "make\_constraints" and "relax\_bounds", bound multipliers are computed for the fixed variables.

make\_parameter Remove fixed variable from optimization variables

make\_constraint Add equality constraints fixing variables

relax\_bounds Relax fixing bound constraints

honor\_original\_bounds (no, yes)

yes

Indicates whether final points should be projected into original bounds.

Ipopt might relax the bounds during the optimization (see, e.g., option "bound\_relax\_factor"). This option determines whether the final point should be projected back into the user-provide original bounds after the optimization.

no Leave final point unchanged

yes Project final point back into original bounds

jac\_c\_constant (no, yes)

no

Indicates whether all equality constraints are linear

Activating this option will cause Ipopt to ask for the Jacobian of the equality constraints only once from the NLP and reuse this information later.

no Don't assume that all equality constraints are linear

yes Assume that equality constraints Jacobian are constant

jac\_d\_constant (no, yes)

no

Indicates whether all inequality constraints are linear

Activating this option will cause Ipopt to ask for the Jacobian of the inequality constraints only once from the NLP and reuse this information later.

no Don't assume that all inequality constraints are linear

yes Assume that equality constraints Jacobian are constant

kappa\_d  $(0 \le \text{real})$  10<sup>-5</sup>

Weight for linear damping term (to handle one-sided bounds).

(see Section 3.7 in implementation paper.)

num\_linear\_variables  $(0 \le integer)$ 

0

Number of linear variables

When the Hessian is approximated, it is assumed that the first num\_linear\_variables variables are linear. The Hessian is then not approximated in this space. If the get\_number\_of\_nonlinear\_variables method in the TNLP is implemented, this option is ignored.

# **NLP Scaling**

 $nlp\_scaling\_constr\_target\_gradient (0 \le real)$ 

0

Target value for constraint function gradient size.

If a positive number is chosen, the scaling factor the constraint functions is computed so that the gradient has the max norm of the given size at the starting point. This overrides nlp\_scaling\_max\_gradient for the constraint functions.

 ${\tt nlp\_scaling\_max\_gradient} \ (0 < real)$ 

100

Maximum gradient after NLP scaling.

This is the gradient scaling cut-off. If the maximum gradient is above this value, then gradient based scaling will be performed. Scaling parameters are calculated to scale the maximum gradient back to this value. (This is g\_max in Section 3.8 of the implementation paper.) Note: This option is only used if "nlp\_scaling\_method" is chosen as "gradient-based".

nlp\_scaling\_method (none, user-scaling, gradient-based, equilibration-based) gradient-based Select the technique used for scaling the NLP.

Selects the technique used for scaling the problem internally before it is solved. For user-scaling, the parameters come from the NLP. If you are using AMPL, they can be specified through suffixes ("scaling\_factor")

none no problem scaling will be performed

user-scaling scaling parameters will come from the user

gradient-based scale the problem so the maximum gradient at the starting point is scaling\_max\_gradient

equilibration-based scale the problem so that first derivatives are of order 1 at random points (only available with MC19)

 $nlp\_scaling\_min\_value (0 \le real)$ 

 $10^{-8}$ 

Minimum value of gradient-based scaling values.

This is the lower bound for the scaling factors computed by gradient-based scaling method. If some derivatives of some functions are huge, the scaling factors will otherwise become very small, and the (unscaled) final constraint violation, for example, might then be significant. Note: This option is only used if "nlp\_scaling\_method" is chosen as "gradient-based".

 $nlp\_scaling\_obj\_target\_gradient (0 \le real)$ 

0

Target value for objective function gradient size.

If a positive number is chosen, the scaling factor the objective function is computed so that the gradient has the max norm of the given size at the starting point. This overrides nlp\_scaling\_max\_gradient for the objective function.

# Output

inf\_pr\_output (internal, original)

original

Determines what value is printed in the "inf\_pr" output column.

Ipopt works with a reformulation of the original problem, where slacks are introduced and the problem might have been scaled. The choice "internal" prints out the constraint violation of this formulation. With "original" the true constraint violation in the original NLP is printed.

internal max-norm of violation of internal equality constraints

original maximal constraint violation in original NLP

print\_eval\_error (no, yes)

yes

Switch to enable printing information about function evaluation errors into the GAMS listing file.

nο

print\_info\_string (no, yes)

Enables printing of additional info string at end of iteration output. This string contains some insider information about the current iteration. For details, look for "Diagnostic Tags" in the Ipopt documentation. no don't print string yes print string at end of each iteration output  $print\_level (0 \le integer \le 12)$ 5 Output verbosity level. Sets the default verbosity level for console output. The larger this value the more detailed is the output. print\_timing\_statistics (no, yes) no Switch to print timing statistics. If selected, the program will print the CPU usage (user time) for selected tasks. no don't print statistics yes print all timing statistics replace\_bounds (no, yes) nο Indicates if all variable bounds should be replaced by inequality constraints This option must be set for the inexact algorithm no leave bounds on variables yes replace variable bounds by inequality constraints report\_mininfeas\_solution (no, yes) no Switch to report intermediate solution with minimal constraint violation to GAMS if the final solution is not feasible. This option allows to obtain the most feasible solution found by Ipopt during the iteration process, if it stops at a (locally) infeasible solution, due to a limit (time, iterations, ...), or with a failure in the restoration phase. Pardiso Linear Solver pardiso\_iter\_coarse\_size (1 < integer)</pre> 5000 Maximum Size of Coarse Grid Matrix DPARM(3) 0.5 pardiso\_iter\_dropping\_factor (0 < real < 1)dropping value for incomplete factor DPARM(5) pardiso\_iter\_dropping\_schur (0 < real < 1)0.1 dropping value for sparsify schur complement factor DPARM(6)  $5 \cdot 10^{6}$ pardiso\_iter\_inverse\_norm\_factor (1 < real) DPARM(8) pardiso\_iter\_max\_levels (1 ≤ integer) 10 Maximum Size of Grid Levels DPARM(4)  ${\tt pardiso\_iter\_max\_row\_fill} \ (1 \leq integer)$ 10000000 max fill for each row DPARM(7)  $10^{-6}$ pardiso\_iter\_relative\_tol (0 < real < 1)Relative Residual Convergence DPARM(2) pardiso\_iterative (no, yes) no Switch on iterative solver in Pardiso library pardiso\_matching\_strategy (complete, complete+2x2, constraints) complete+2x2

Matching strategy to be used by Pardiso

This is IPAR(13) in Pardiso manual. This option is only available if Ipopt has been compiled with Pardiso.

complete Match complete (IPAR(13)=1)

complete+2x2 Match complete+2x2 (IPAR(13)=2)

constraints Match constraints (IPAR(13)=3)

pardiso\_max\_droptol\_corrections (1 ≤ integer)

Maximal number of decreases of drop tolerance during one solve.

This is relevant only for iterative Pardiso options.

pardiso\_max\_iter  $(1 \le integer)$ 

500

4

Maximum number of Krylov-Subspace Iteration

DPARM(1)

pardiso\_msglvl  $(0 \le integer)$ 

0

Pardiso message level

This determines the amount of analysis output from the Pardiso solver. This is MSGLVL in the Pardiso manual.

pardiso\_out\_of\_core\_power  $(0 \le integer)$ 

0

Enables out-of-core variant of Pardiso

Setting this option to a positive integer k makes Pardiso work in the out-of-core variant where the factor is split in  $2\hat{k}$  subdomains. This is IPARM(50) in the Pardiso manual. This option is only available if Ipopt has been compiled with Pardiso.

pardiso\_redo\_symbolic\_fact\_only\_if\_inertia\_wrong (no, yes)

no

Toggle for handling case when elements were perturbed by Pardiso.

This option is only available if Ipopt has been compiled with Pardiso.

no Always redo symbolic factorization when elements were perturbed

yes Only redo symbolic factorization when elements were perturbed if also the inertia was wrong

 ${\tt pardiso\_repeated\_perturbation\_means\_singular~(no,~yes)}$ 

no

Interpretation of perturbed elements.

This option is only available if Ipopt has been compiled with Pardiso.

no Don't assume that matrix is singular if elements were perturbed after recent symbolic factorization

yes Assume that matrix is singular if elements were perturbed after recent symbolic factorization

pardiso\_skip\_inertia\_check (no, yes)

no

Always pretend inertia is correct.

Setting this option to "yes" essentially disables inertia check. This option makes the algorithm non-robust and easily fail, but it might give some insight into the necessity of inertia control.

no check inertia

yes skip inertia check

#### **Restoration Phase**

bound\_mult\_reset\_threshold (0 < real)

1000

Threshold for resetting bound multipliers after the restoration phase.

After returning from the restoration phase, the bound multipliers are updated with a Newton step for complementarity. Here, the change in the primal variables during the entire restoration phase is taken to be the corresponding primal Newton step. However, if after the update the largest bound multiplier exceeds the threshold specified by this option, the multipliers are all reset to 1.

constr\_mult\_reset\_threshold  $(0 \le real)$ 

0

Threshold for resetting equality and inequality multipliers after restoration phase.

After returning from the restoration phase, the constraint multipliers are recomputed by a least square estimate. This option triggers when those least-square estimates should be ignored.

evaluate\_orig\_obj\_at\_resto\_trial (no, yes)

yes

Determines if the original objective function should be evaluated at restoration phase trial points.

Setting this option to "yes" makes the restoration phase algorithm evaluate the objective function of the original problem at every trial point encountered during the restoration phase, even if this value is not required. In this way, it is guaranteed that the original objective function can be evaluated without error at all accepted iterates; otherwise the algorithm might fail at a point where the restoration phase accepts an iterate that is good for the restoration phase problem, but not the original problem. On the other hand, if the evaluation of the original objective is expensive, this might be costly.

no skip evaluation

yes evaluate at every trial point

expect\_infeasible\_problem (no, yes)

no

Enable heuristics to quickly detect an infeasible problem.

This options is meant to activate heuristics that may speed up the infeasibility determination if you expect that there is a good chance for the problem to be infeasible. In the filter line search procedure, the restoration phase is called more quickly than usually, and more reduction in the constraint violation is enforced before the restoration phase is left. If the problem is square, this option is enabled automatically.

no the problem probably be feasible

yes the problem has a good chance to be infeasible

 ${\tt expect\_infeasible\_problem\_ctol}\ (0 \leq real)$ 

0.001

Threshold for disabling "expect\_infeasible\_problem" option.

If the constraint violation becomes smaller than this threshold, the "expect\_infeasible\_problem" heuristics in the filter line search are disabled. If the problem is square, this options is set to 0.

 $\verb|expect_infeasible_problem_ytol| (0 < real)$ 

 $10^{8}$ 

Multiplier threshold for activating "expect\_infeasible\_problem" option.

If the max norm of the constraint multipliers becomes larger than this value and "expect\_infeasible\_problem" is chosen, then the restoration phase is entered.

 $max\_resto\_iter (0 \le integer)$ 

3000000

Maximum number of successive iterations in restoration phase.

The algorithm terminates with an error message if the number of iterations successively taken in the restoration phase exceeds this number.

 $max\_soft\_resto\_iters (0 \le integer)$ 

10

Maximum number of iterations performed successively in soft restoration phase.

If the soft restoration phase is performed for more than so many iterations in a row, the regular restoration phase is called.

required\_infeasibility\_reduction  $(0 \le real < 1)$ 

0.9

Required reduction of infeasibility before leaving restoration phase.

The restoration phase algorithm is performed, until a point is found that is acceptable to the filter and the infeasibility has been reduced by at least the fraction given by this option.

resto\_failure\_feasibility\_threshold (0 < real)

0

Threshold for primal infeasibility to declare failure of restoration phase.

If the restoration phase is terminated because of the "acceptable" termination criteria and the primal infeasibility is smaller than this value, the restoration phase is declared to have failed. The default value is 1e2\*tol, where tol is the general termination tolerance.

 $resto_penalty_parameter (0 < real)$ 

1000

Penalty parameter in the restoration phase objective function.

This is the parameter rho in equation (31a) in the Ipopt implementation paper.

 $resto\_proximity\_weight$  ( $0 \le real$ )

1

Weighting factor for the proximity term in restoration phase objective.

This determines how the parameter zera in equation (29a) in the implementation paper is computed. zeta here is resto\_proximity\_weight\*sqrt(m where mu is the current barrier parameter.

 $soft_resto_pderror_reduction_factor (0 \le real)$ 

0.9999

Required reduction in primal-dual error in the soft restoration phase.

The soft restoration phase attempts to reduce the primal-dual error with regular steps. If the damped primal-dual step (damped only to satisfy the fraction-to-the-boundary rule) is not decreasing the primal-dual error by at least this factor, then

the regular restoration phase is called. Choosing "0" here disables the soft restoration phase.

start\_with\_resto (no, yes)

no

Tells algorithm to switch to restoration phase in first iteration.

Setting this option to "yes" forces the algorithm to switch to the feasibility restoration phase in the first iteration. If the initial point is feasible, the algorithm will abort with a failure.

no don't force start in restoration phase

yes force start in restoration phase

# **Step Calculation**

fast\_step\_computation (no, yes)

no

Indicates if the linear system should be solved quickly.

If set to yes, the algorithm assumes that the linear system that is solved to obtain the search direction, is solved sufficiently well. In that case, no residuals are computed, and the computation of the search direction is a little faster.

no Verify solution of linear system by computing residuals.

yes Trust that linear systems are solved well.

 $first_hessian_perturbation (0 < real)$ 

0.0001

Size of first x-s perturbation tried.

The first value tried for the x-s perturbation in the inertia correction scheme. (This is delta\_0 in the implementation paper.)

jacobian\_regularization\_exponent  $(0 \le real)$ 

0.25

Exponent for mu in the regularization for rank-deficient constraint Jacobians.

(This is kappa\_c in the implementation paper.)

jacobian\_regularization\_value  $(0 \le real)$ 

 $10^{-8}$ 

Size of the regularization for rank-deficient constraint Jacobians.

(This is bar delta\_c in the implementation paper.)

 $max\_hessian\_perturbation (0 < real)$ 

 $10^{20}$ 

Maximum value of regularization parameter for handling negative curvature.

In order to guarantee that the search directions are indeed proper descent directions, Ipopt requires that the inertia of the (augmented) linear system for the step computation has the correct number of negative and positive eigenvalues. The idea is that this guides the algorithm away from maximizers and makes Ipopt more likely converge to first order optimal points that are minimizers. If the inertia is not correct, a multiple of the identity matrix is added to the Hessian of the Lagrangian in the augmented system. This parameter gives the maximum value of the regularization parameter. If a regularization of that size is not enough, the algorithm skips this iteration and goes to the restoration phase. (This is delta\_wmax in the implementation paper.)

 $max\_refinement\_steps (0 \le integer)$ 

10

Maximum number of iterative refinement steps per linear system solve.

Iterative refinement (on the full unsymmetric system) is performed for each right hand side. This option determines the maximum number of iterative refinement steps.

mehrotra\_algorithm (no, yes)

no

Indicates if we want to do Mehrotra's algorithm.

If set to yes, Ipopt runs as Mehrotra's predictor-corrector algorithm. This works usually very well for LPs and convex QPs. This automatically disables the line search, and chooses the (unglobalized) adaptive mu strategy with the "probing" oracle, and uses "corrector\_type=affine" without any safeguards; you should not set any of those options explicitly in addition. Also, unless otherwise specified, the values of "bound\_push", "bound\_frac", and "bound\_mult\_init\_val" are set more aggressive, and sets "alpha\_for\_y=bound\_mult".

no Do the usual Ipopt algorithm.

yes Do Mehrotra's predictor-corrector algorithm.

 $min\_hessian\_perturbation (0 \le real)$ 

 $10^{-20}$ 

Smallest perturbation of the Hessian block.

The size of the perturbation of the Hessian block is never selected smaller than this value, unless no perturbation is necessary. (This is delta\_wm̂in in implementation paper.)

 $min\_refinement\_steps (0 \le integer)$ 

1

Minimum number of iterative refinement steps per linear system solve.

Iterative refinement (on the full unsymmetric system) is performed for each right hand side. This option determines the minimum number of iterative refinements (i.e. at least "min\_refinement\_steps" iterative refinement steps are enforced per right hand side.)

neg\_curv\_test\_tol (0 < real)

0

Tolerance for heuristic to ignore wrong inertia.

If positive, incorrect inertia in the augmented system is ignored, and we test if the direction is a direction of positive curvature. This tolerance determines when the direction is considered to be sufficiently positive.

perturb\_always\_cd (no, yes)

no

Active permanent perturbation of constraint linearization.

This options makes the delta\_c and delta\_d perturbation be used for the computation of every search direction. Usually, it is only used when the iteration matrix is singular.

no perturbation only used when required

yes always use perturbation

 $perturb_dec_fact (0 < real < 1)$ 

0.333333

Decrease factor for x-s perturbation.

The factor by which the perturbation is decreased when a trial value is deduced from the size of the most recent successful perturbation. (This is kappa\_w<sup>2</sup> in the implementation paper.)

perturb\_inc\_fact (1 < real)

8

Increase factor for x-s perturbation.

The factor by which the perturbation is increased when a trial value was not sufficient - this value is used for the computation of all perturbations except for the first. (This is kappa\_w<sup>2</sup> in the implementation paper.)

perturb\_inc\_fact\_first (1 < real)</pre>

100

Increase factor for x-s perturbation for very first perturbation.

The factor by which the perturbation is increased when a trial value was not sufficient - this value is used for the computation of the very first perturbation and allows a different value for the first perturbation than that used for the remaining perturbations. (This is bar\_kappa\_w+ in the implementation paper.)

residual\_improvement\_factor (0 < real)

1

Minimal required reduction of residual test ratio in iterative refinement.

If the improvement of the residual test ratio made by one iterative refinement step is not better than this factor, iterative refinement is aborted.

residual\_ratio\_max (0 < real)

 $10^{-10}$ 

Iterative refinement tolerance

Iterative refinement is performed until the residual test ratio is less than this tolerance (or until "max\_refinement\_steps" refinement steps are performed).

 $residual\_ratio\_singular (0 < real)$ 

 $10^{-5}$ 

Threshold for declaring linear system singular after failed iterative refinement.

If the residual test ratio is larger than this value after failed iterative refinement, the algorithm pretends that the linear system is singular.

### Warm Start

 $warm_start_bound_frac (0 < real \le 0.5)$ 

0.001

same as bound\_frac for the regular initializer.

 $warm\_start\_bound\_push (0 < real)$ 

0.001

same as bound\_push for the regular initializer.

warm\_start\_init\_point (no, yes)

no

Warm-start for initial point

Indicates whether this optimization should use a warm start initialization, where values of primal and dual variables are given (e.g., from a previous optimization of a related problem.)

no do not use the warm start initialization

yes use the warm start initialization	
$\label{lem:warm_start_mult_bound_push} $$ (0 < real)$ same as mult_bound_push for the regular initializer.$	0.001
<pre>warm_start_mult_init_max (real) Maximum initial value for the equality multipliers.</pre>	10 <sup>6</sup>
warm_start_slack_bound_frac $(0 < real \le 0.5)$ same as slack_bound_frac for the regular initializer.	0.001
warm_start_slack_bound_push (0 < real) same as slack_bound_push for the regular initializer.	0.001

# **6 Optimization Services**

OS (Optimization Services) is an initiative to provide a set of standards for representing optimization instances, results, solver options, and communication between clients and solvers in a distributed environment using Web Services. The code has been written primarily by Horand Gassmann, Jun Ma, and Kipp Martin. Kipp Martin is the COIN-OR project leader for OS.

For more information we refer to the OS manual [23], the papers [15, 16, 17], and the web sites http://www.optimizationservices.org and https://projects.coin-or.org/OS.

With the OS link in GAMS, you can send your instance to an Optimization Services Server for remote solving.

# **6.1** Model requirements

OS supports continuous, binary, integer, semicontinuous, and semiinteger variables and linear and nonlinear equations. Special ordered sets and indicator constraints are currently not supported. Initial values are currently not supported by the GAMS/OS link.

# 6.2 Usage

The following statement can be used inside your GAMS program to specify using OS

```
Option MINLP = OS; { or LP, RMIP, MIP, DNLP, NLP, RMINLP, QCP, RMIQCP, MIQCP }
```

The above statement should appear before the Solve statement.

By default, for a given instance of a GAMS model, nothing happens. To solve an instance remotely, you have to specify the URL of an Optimization Services Server via the option service. Usually, the server chooses an appropriate solver for your instance, depending on their availability on the server. A fully equipped server chooses CLP for continuous linear models (LP and RMIP), IPOPT for continuous nonlinear models (NLP, DNLP, RMINLP, QCP, RMIQCP), CBC for mixed-integer linear models (MIP), and BONMIN for mixed-integer nonlinear models (MIQCP, MINLP). An easy way to influence the choice of the solver on the server is the solver option.

Further options can be provided in an OSoL (Optimization Services Options Language) file, which is specified via the the readosol option. An example OSoL file looks like

It specifies that if CBC is used, then cutting planes are disabled, if SYMPHONY is used, then at most 2 nodes should be active, and if IPOPT is used, then a limit of 2000 iterations is imposed.

By default, the call to the server is a *synchronous* call. The GAMS process will wait for the result and then display the result. This may not be desirable when solving large optimization models. In order to use the remote solver service in an *asynchronous* fashion, one can make use of the GAMS Grid Computing Facility, see Appendix I in the GAMS manual.

# **6.3** Detailed Options Descriptions

# readosol (string)

Specifies the name of an option file in OSoL format that is given to the OS server. This way it is possible to pass options directly to the solvers interfaced by OS.

# writeosil (string)

Specifies the name of a file in which the GAMS model instance should be writting in OSiL format.

# writeosrl (string)

Specifies the name of a file in which the result of a solve process (solution, status, ...) should be writting in OSrL format.

# service (string)

Specifies the URL of an Optimization Services Server. The GAMS model is converted into OSiL format, send to the server, and the result translated back into GAMS format. Note that by default the server chooses a solver that is appropriate to the model type. You can change the solver with the solver option.

# solver (string)

Specifies the solver that is used to solve an instance on the OS server.

# 7 OSICPLEX, OSIGUROBI, OSIMOSEK, OSISOPLEX, OSIXPRESS

The "bare bone" solver links GAMS/OSICPLEX, GAMS/OSIGUROBI, GAMS/OSIMOSEK, GAMS/OSISOPLEX, and GAMS/OSIXPRESS allow users to solve their GAMS models with SOPLEX or a standalone license of CPLEX, GUROBI, MOSEK, or XPRESS. The links use the COIN-OR Open Solver Interface (OSI) to communicate with these solvers. The OSICPLEX link has been written primarily by Tobias Achterberg, the OSIGUROBI link has been written primarily by Stefan Vigerske, the OSIMOSEK link has been written primarily by Bo Jensen, the OSISOPLEX link has been written primarily by Tobias Achterberg, Ambros M. Gleixner, and Wei Huang, and the OSIXPRESS link has been written primarily by John Doe. Matthew Saltzman is the COIN-OR project leader for OSI.

For more information we refer to the OSI web site https://projects.coin-or.org/Osi.

# 7.1 Model requirements

The OSI links support linear equations and continuous, binary, and integer variables. Semicontinuous and Semiinteger variables, special ordered sets, branching priorities, and indicator constraints are not supported by OSI. OSISOPLEX solves only LPs, no MIPs.

# 7.2 Usage

The following statement can be used inside your GAMS program to specify using OSIGUROBI

```
Option MIP = OSIGUROBI; { or LP or RMIP }
```

The above statement should appear before the Solve statement.

The links support the general GAMS options reslim, optca, optcr, nodlim, iterlim, and threads (except for OSISOPLEX). For OSICPLEX, OSIGUROBI, OSIMOSEK, and OSIXPRESS an option file in the format required by the solver can be provided via the GAMS optfile option. See Section 7.3 for details.

If a MIP is solved via one of the OSI links, only primal solution values are reported by default. To receive also the dual values for the LP that is obtained from the MIP by fixing all discrete variables, the GAMS option integer1 must be set to a nonzero value. Note that this may lead to solving another LP after the MIP solve has finished.

Setting the GAMS option integer2 to a nonzero value makes variable and equation names available to the solver. This option may be useful for debugging purposes.

Setting the GAMS option integer3 to a nonzero value leads to writing the model instance to a file in LP or MPS format before starting the solution process (integer3=1 writes an MPS file, integer3=2 writes an LP files, integer3=4 writes a native MPS file; sum these values to write several files). The name of the MPS file is chosen to be the name of the GAMS model file with the extension .gms replaced by .mps. This option may be useful for debugging purposes.

For OSICPLEX, OSIGUROBI, and OSIXPRESS, setting the GAMS option integer4 to a nonzero value leads to passing the variable level values (.1 suffix) to the MIP solver as initial solution. This is analog to the mipstart option of the full CPLEX and GUROBI links and the loadmipsol option of the full XPRESS link.

# 7.3 Option files

# 7.3.1 OSICPLEX Options

In an OSICPLEX option file, each line lists one option setting, where the option name and value are separated by space. Example:

CPX\_PARAM\_MIPEMPHASIS 2
CPX\_PARAM\_HEURFREQ 42
CPX\_PARAM\_MIPDISPLAY 4

# 7.3.2 OSIGUROBI Options

In an OSICPLEX option file, each line lists one option setting, where the option name and value are separated by space.

Example:

Cuts 2 Heuristics 0.1

#### 7.3.3 OSIMOSEK Options

An OSIMOSEK option file begins with the line BEGIN MOSEK and terminates with END MOSEK. Comments are introduced with an '%', empty lines are ignored. Each other line starts with a MOSEK parameter value, followed by space, and a value for that parameter.

Example:

BEGIN MOSEK

% disable probing and solve the root node by the interior point solver

MSK\_IPAR\_MIO\_PRESOLVE\_PROBING MSK\_OFF
MSK\_IPAR\_MIO\_ROOT\_OPTIMIZER MSK\_OPTIMIZER\_INTPNT
END MOSEK

# 7.3.4 OSIXPRESS Options

In an OSIXPRESS option file, each line lists one option setting, where the option name and value are separated by an equal sign.

Example:

MIPLOG = 3 HEURFREQ = 2

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