

The growth of cryptography

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James R. Killian Jr. Faculty Achievement Award Lecture
February 8, 2011

Outline

Some pre-1976 context

Invention of Public-Key Crypto and RSA

Early steps

The cryptography business

Crypto policy

Attacks

More New Directions

What Next?

Conclusion and Acknowledgments

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Euclid – 300 B.C.



There are infinitely many primes:
2, 3, 5, 7, 11, 13, ...

Euclid – 300 B.C.



There are infinitely many primes:
2, 3, 5, 7, 11, 13, ...

The greatest common divisor of two
numbers is easily computed
(using “Euclid’s Algorithm”):
 $\gcd(12, 30) = 6$

Greek Cryptography – The Scytale



An unknown *period* (the circumference of the scytale) is the secret key, shared by sender and receiver.

Pierre de Fermat (1601-1665)

Leonhard Euler (1707–1783)



Fermat's Little Theorem (1640):

For any prime p and any a , $1 \leq a < p$:

$$a^{p-1} = 1 \pmod{p}$$

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Euler's Theorem (1736):

If $\gcd(a, n) = 1$, then

$$a^{\phi(n)} = 1 \pmod{n},$$

where $\phi(n) = \#$ of $x < n$ such that $\gcd(x, n) = 1$.

Carl Friedrich Gauss (1777-1855)



Published *Disquisitiones Arithmeticae* at age 21

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“The problem of *distinguishing prime numbers from composite numbers and of resolving the latter into their prime factors* is known to be one of the most important and useful in arithmetic. . . . the dignity of the science itself seems to require solution of a problem so elegant and so celebrated.”

William Stanley Jevons (1835–1882)



Published *The Principles of Science* (1874)

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Gave world's first *factoring challenge*:

"What two numbers multiplied together will produce 8616460799 ? I think it unlikely that anyone but myself will ever know."

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"What two numbers multiplied together will produce 8616460799 ? I think it unlikely that anyone but myself will ever know."

Factored by Derrick Lehmer in 1903. ($89681 * 96079$)

World War I – Radio

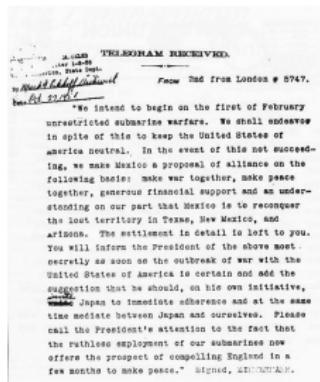
- ▶ A marvelous new communication technology—*radio* (Marconi, 1895)—enabled instantaneous communication with remote ships and forces, but also gave all transmitted messages to the enemy.

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Decipherment of
Zimmermann Telegram by
British made American
involvement in World War I
inevitable.

Alan Turing (1912–1954)



Developed foundations of theory of computability
(1936).

World War II – Enigma, Purple, JN25, Naval Enigma



- ▶ Cryptography performed by (typically, rotor) *machines*.

World War II – Enigma, Purple, JN25, Naval Enigma



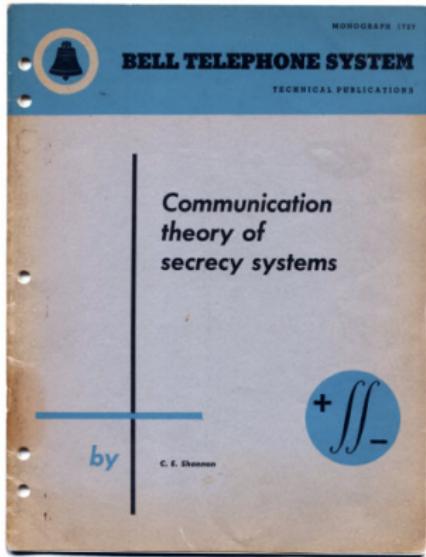
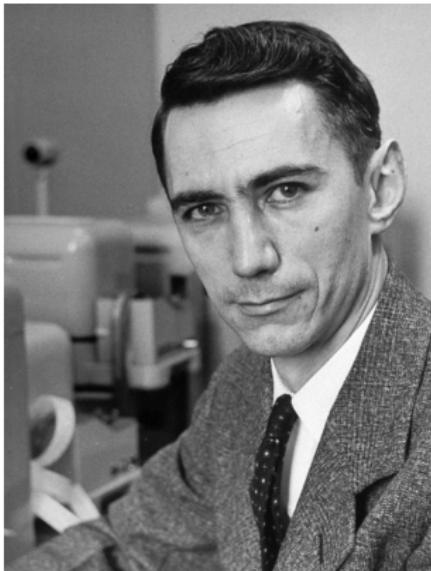
- ▶ Cryptography performed by (typically, rotor) *machines*.
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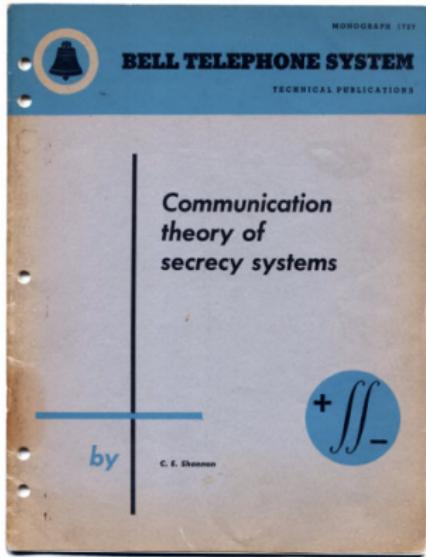
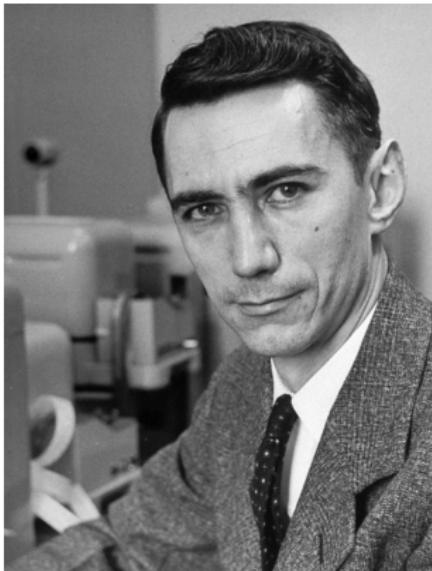
- ▶ Cryptography performed by (typically, rotor) *machines*.
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- ▶ Cryptanalytic effort involved development and use of early computers (Colossus).

Claude Shannon (1916–2001)



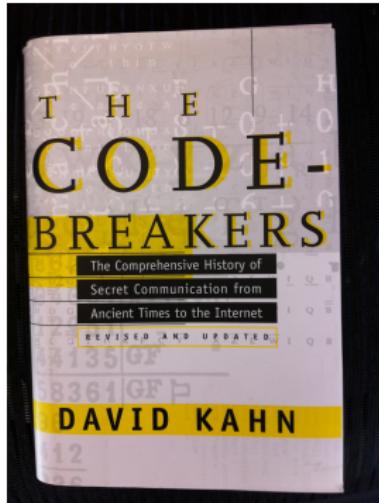
- ▶ “Communication Theory of Secrecy Systems” Sept 1945 (Bell Labs memo, classified).

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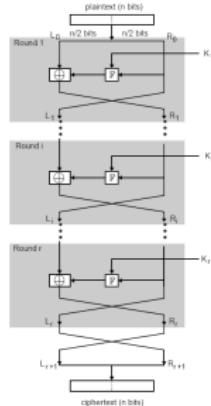
- ▶ “Communication Theory of Secrecy Systems” Sept 1945 (Bell Labs memo, classified).
- ▶ Information-theoretic in character—proves unbreakability of one-time pad. (Published 1949).

Kahn – The Codebreakers



In 1967 David Kahn published *The Codebreakers—The Story of Secret Writing*. A monumental history of cryptography. NSA attempted to suppress its publication.

DES – U.S. Data Encryption Standard (1976)



DES Designed at IBM; Horst Feistel supplied key elements of design, such as ladder structure. NSA helped, in return for keeping key size at 56 bits.(?)

Computational Complexity



- ▶ Theory of Computational Complexity started in 1965 by Hartmanis and Stearns; expanded on by Blum, Cook, and Karp.
- ▶ Key notions: polynomial-time reductions; NP-completeness.

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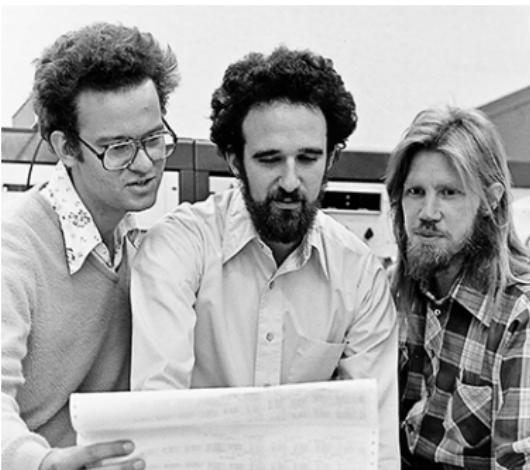
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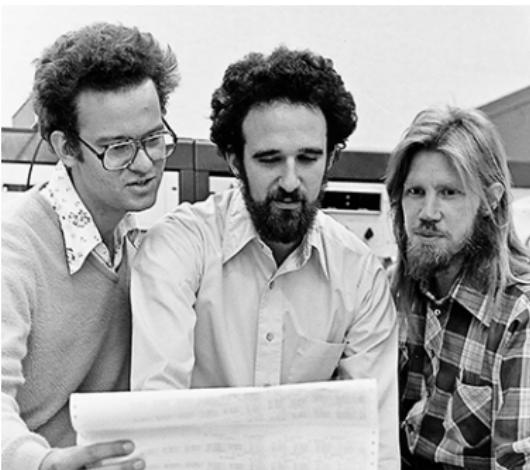
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Invention of Public Key Cryptography



- ▶ Ralph Merkle, and independently Marty Hellman and Whit Diffie, invented the notion of *public-key cryptography*.

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- ▶ In November 1976, Diffie and Hellman published *New Directions in Cryptography*, proclaiming

“We are at the brink of a revolution in cryptography.”

Public-key encryption (as proposed by Diffie/Hellman)

- ▶ Each party A has a *public key* PK_A others can use to encrypt messages to A :

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- ▶ It is easy to compute matching public/secret key pairs.
- ▶ Publishing PK_A does not compromise SK_A ! It is *computationally infeasible* to obtain SK_A from PK_A . Each public key can thus be safely listed in a public directory with the owner's name.

Digital Signatures (as proposed by Diffie/Hellman)

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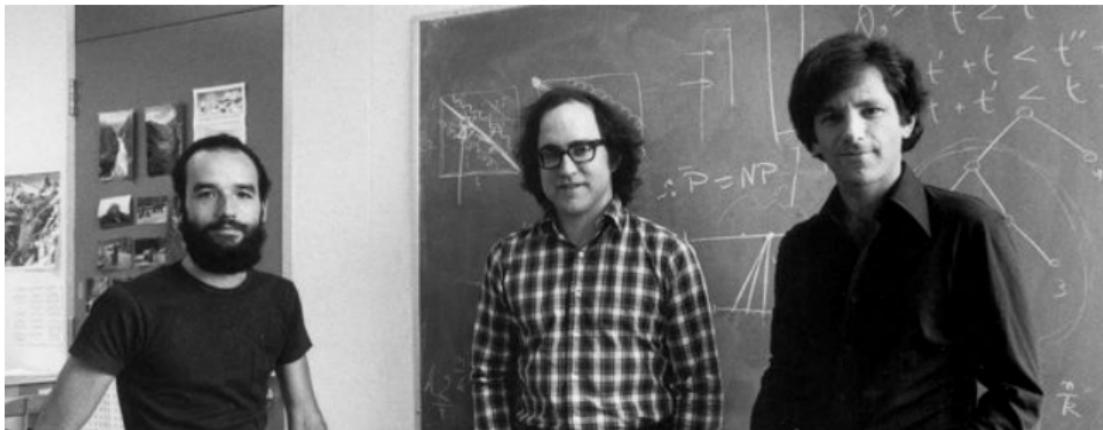
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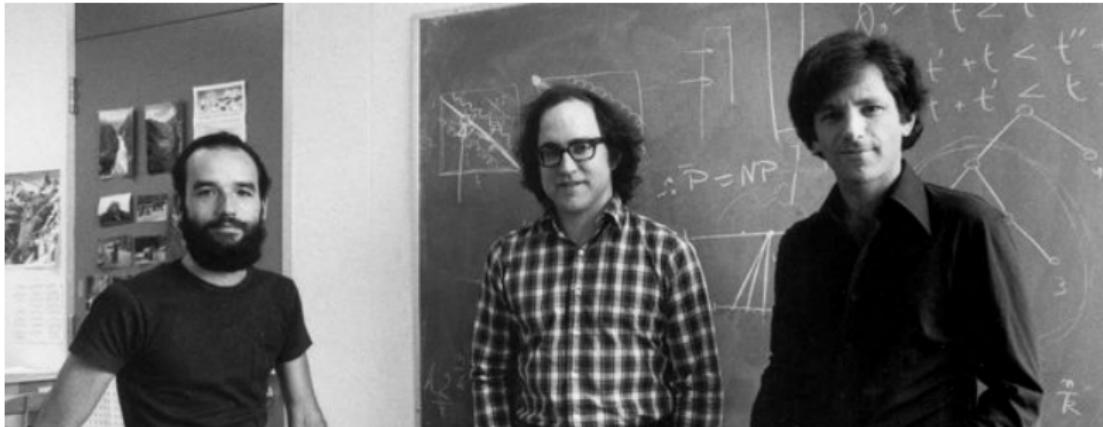
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- ▶ Amazing ideas!
- ▶ But they couldn't see how to implement them...

RSA (Ron Rivest, Adi Shamir, Len Adleman, 1977)

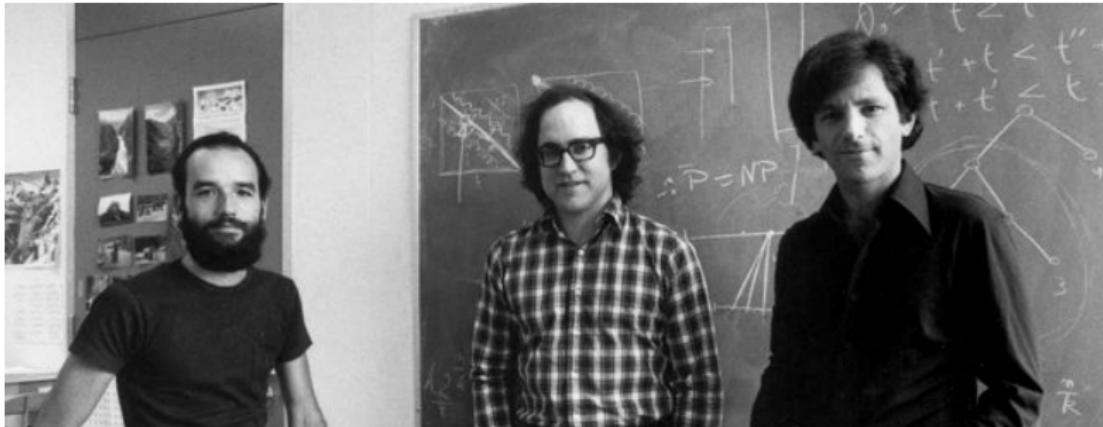


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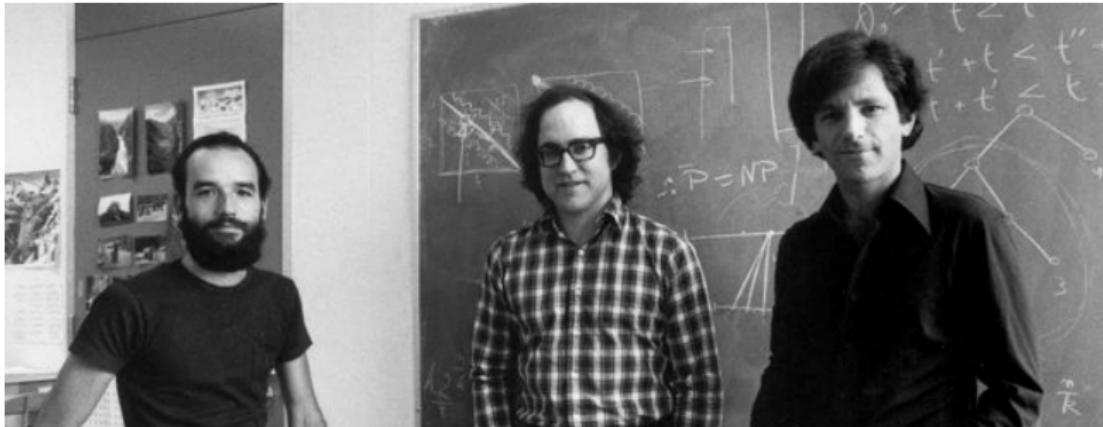
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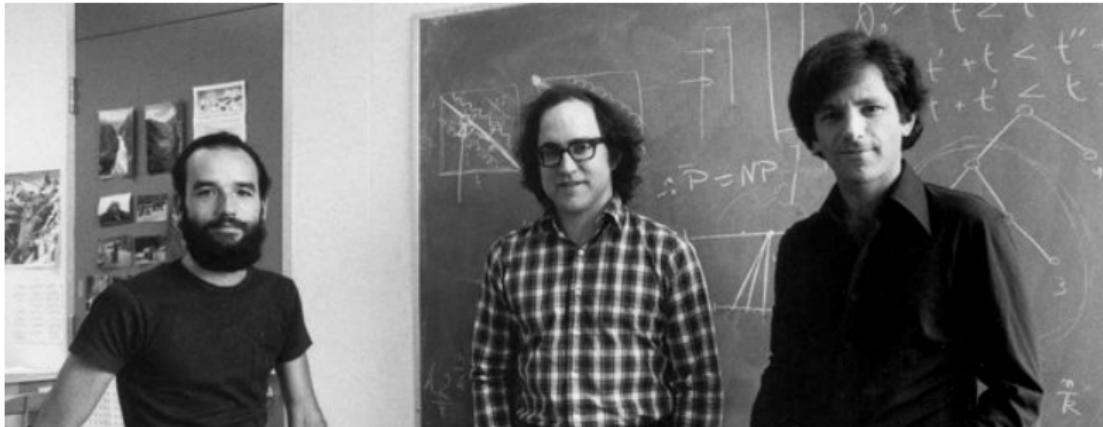
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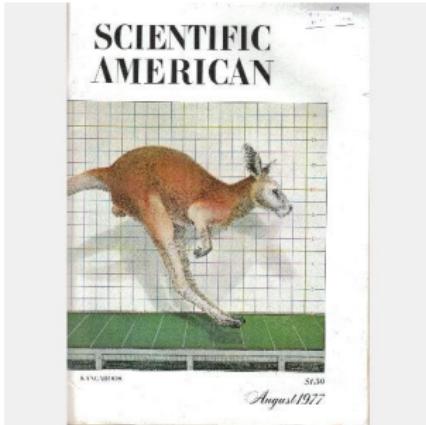
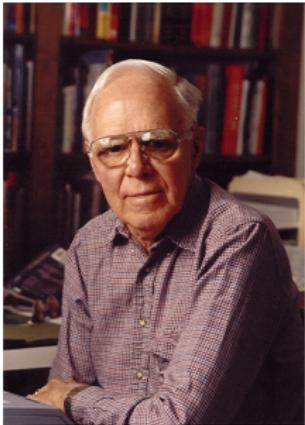
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- ▶ $PK = (n, e)$ where $n = pq$ and $\gcd(e, \phi(n)) = 1$
- ▶ $SK = d$ where $de = 1 \pmod{\phi(n)}$
- ▶ Encryption/decryption (or signing/verify) are simple:

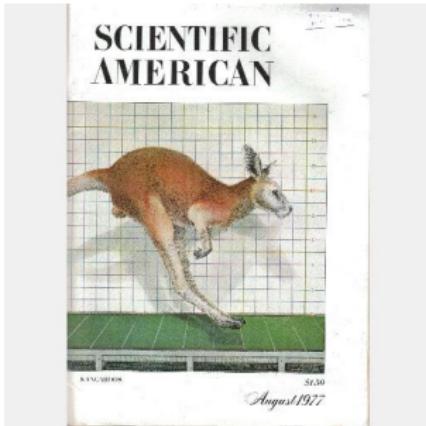
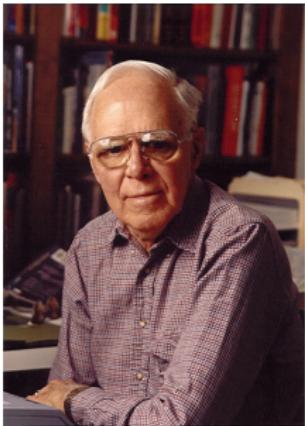
$$\begin{aligned} C &= PK(M) = M^e \pmod{n} \\ M &= SK(C) = C^d \pmod{n} \end{aligned}$$

Martin Gardner column and RSA-129 challenge



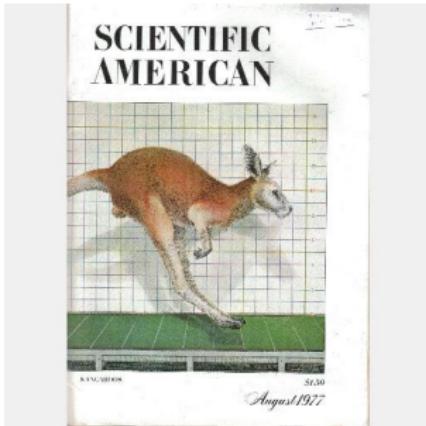
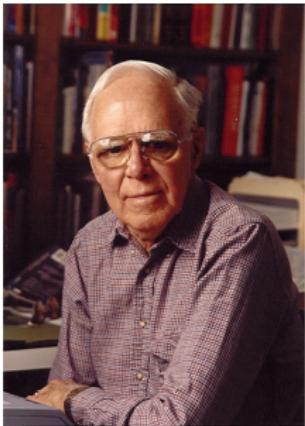
- ▶ Described public-key and RSA cryptosystem in his Scientific American column, *Mathematical Games*

Martin Gardner column and RSA-129 challenge



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- ▶ Offered copy of RSA technical memo.

Martin Gardner column and RSA-129 challenge



- ▶ Described public-key and RSA cryptosystem in his Scientific American column, *Mathematical Games*
- ▶ Offered copy of RSA technical memo.
- ▶ Offered \$100 to first person to break challenge ciphertext based on 129-digit product of primes.
(Our) estimated time to solution: 40 quadrillion years

Publication of RSA memo and paper

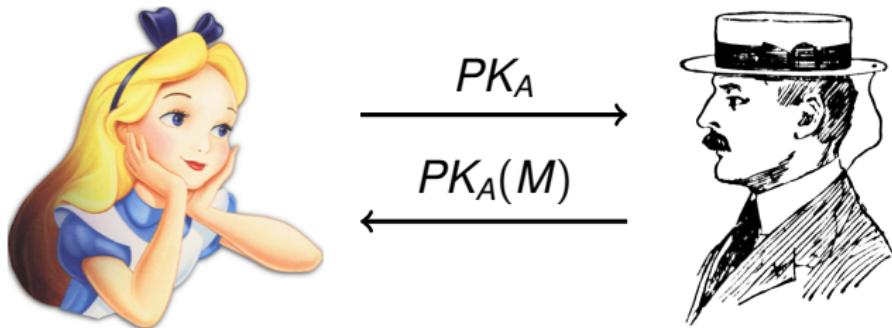


LCS-82 Technical Memo (April 1977)
CACM article (Feb 1978)

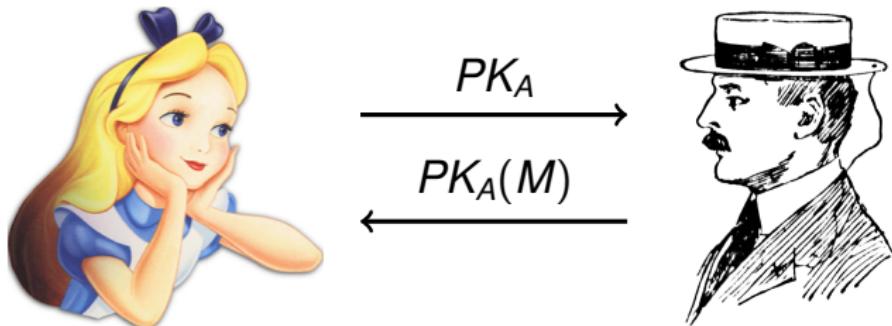
Alice and Bob (1977, in RSA paper)



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Alice and Bob now have a life of their own—they appear in hundreds of crypto papers, in `xkcd`, and even have their own Wikipedia page:

The screenshot shows the Wikipedia article for "Alice and Bob". The page includes the standard Wikipedia header with the logo and navigation links. The main content is titled "Alice and Bob" and describes them as common placeholders in cryptography. It explains that names like Alice and Bob are used for convenience and provides context about their use in RSA and other cryptographic protocols.

Article Discussion

Alice and Bob

From Wikipedia, the free encyclopedia

The names **Alice** and **Bob** are commonly used [placeholder](#) names are used for convenience; for example, "Alice sends a message to Party B encrypted by Party B's public key" is a common way to describe a [public key exchange](#) within these fields—helping technical topics to be explained more easily. In [cryptography](#) and [computer security](#), there are a number of [various protocols](#). The names are conventional, somewhat arbitrary, and do not refer to any real persons.

Independent Invention of Public-Key Revealed



In 1999 GCHQ announced that James Ellis, Clifford Cocks, and Malcolm Williamson had invented public-key cryptography, the “RSA” algorithm, and “Diffie-Hellman key exchange” in the 1970’s, before their invention outside.

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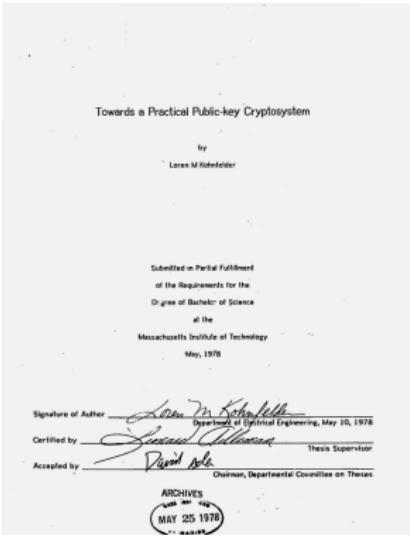
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Loren Kohnfelder – Invention of Digital Certificates



- ▶ Loren Kohnfelder's B.S. thesis (MIT 1978, supervised by Len Adleman), proposed notion of *digital certificate*—a digitally signed message attesting to another party's public key.

IACR—International Assn. for Cryptologic Research

- ▶ Established 1982 by David Chaum, myself, and others, to promote academic research in cryptology.
- ▶ Sponsors three major conferences/year (Crypto, Eurocrypt, Asiacrypt) and four workshops; about 200 papers/year, plus another 600/year posted on web.
Publishes J. Cryptography
- ▶ Around 1600 members, (25% students), from 74 countries, 27 Fellows.



Theoretical Foundations of Security



- ▶ “Probabilistic Encryption” Shafi Goldwasser, Silvio Micali (1982) (Encryption should be *randomized!*)

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- ▶ “A Digital Signature Scheme Secure Against Adaptive Chosen Message Attacks” Goldwasser, Micali, Rivest (1988) (Uses well-defined *game* to define security objective.)

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- ▶ Extremely simple and fast: uses array $S[0..255]$ to keep a permutation of 0..255, initialized using secret key, and uses two pointers i, j into S .

To output a pseudo-random byte:

```
i = (i + 1) mod 256
j = (j + S[i]) mod 256
swap S[i] and S[j]
Output S[(S[i] + S[j]) mod 256]
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RC4 stream cipher (Rivest, 1987)

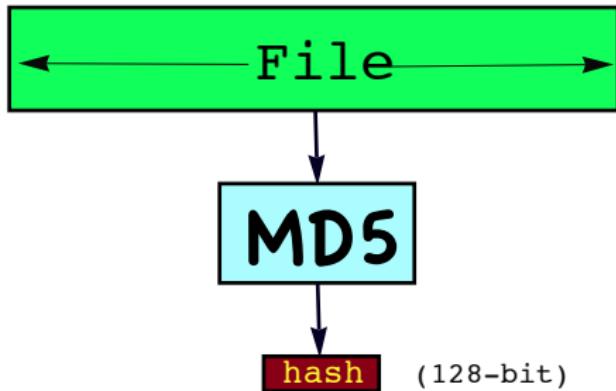
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```

- ▶ Used in: WEP, BitTorrent, SSL, Kerberos, PDF, Skype, ...

MD5 Cryptographic Hash Function (Rivest, 1991)



- ▶ MD5 proposed as pseudo-random function mapping files to 128-bit fingerprints. (variant of earlier MD4)
- ▶ Collision-resistance was a design goal – it should be infeasible to find two files with the same fingerprint.
- ▶ Many, many uses (e.g. in digital signatures) – very widely used, and a model for many other later hash function designs.

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U.S. Patent 4,405,829

United States Patent [19]

Rivest et al.

[11] 4,405,829

[45] Sep. 20, 1983

[54] CRYPTOGRAPHIC COMMUNICATIONS SYSTEM AND METHOD

[75] Inventors: **Ronald L. Rivest**, Belmont; **Adi Shamir**, Cambridge; **Leonard M. Adleman**, Arlington, all of Mass.

[73] Assignee: **Massachusetts Institute of Technology**, Cambridge, Mass.

[21] Appl. No.: 860,586

[22] Filed Dec. 14, 1977

[51] Int. Cl. 2 H04K 1/00; H04J 9/04

[52] U.S. Cl. 178/22, 178/23, 178/24

[58] Field of Search 178/22, 178/23, 178/24, 22.15

[56] References Cited

U.S. PATENT DOCUMENTS

3,657,476 4/1972 Aka

178/22

OTHER PUBLICATIONS

"New Directions in Cryptography", Diffie et al., *IEEE Transactions on Information Theory*, vol. IT-22, No. 6, Nov. 1976, pp. 644-654.

"Theory of Numbers" Stewart, MacMillan Co., 1952, pp. 133-138.

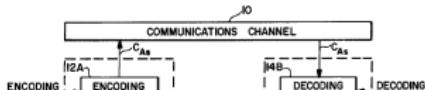
"Diffie et al., Multi-User Cryptographic Techniques", AFIPS Conference Proceedings, vol. 45, pp. 109-112, Jun. 3, 1976.

Primary Examiner—Sal Cangialosi
Attorneys, Agent, or Firm—Arthur A. Smith, Jr.; Robert J. Horn, Jr.

ABSTRACT

A cryptographic communications system and method. The system includes a communications channel coupled to at least one terminal having an encoding device and to at least one terminal having a decoding device. A message-to-be-transferred is enciphered to ciphertext at the encoding terminal by first encoding the message as a number M in a predetermined set, and then raising that number to a first predetermined power (associated with the intended receiver), and finally computing the residue C of the number M raised to the power k divided by the product of two predetermined prime numbers (associated with the intended receiver). The ciphertext C is deciphered to the original message at the decoding terminal in a similar manner by raising the ciphertext to a second predetermined power (associated with the intended receiver), and then computing the residue M' when the enciphered ciphertext is divided by the product of the two predetermined prime numbers associated with the intended receiver. The residue M' corresponds to the original encoded message M .

40 Claims, 7 Drawing Figures



Filed December 1977 (MIT TLO)
Issued September 1983

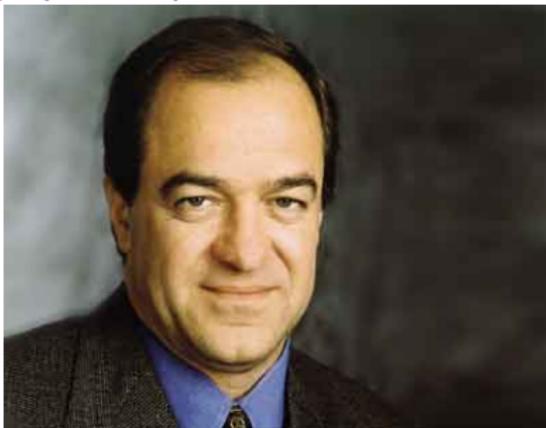
RSA the company (1983)

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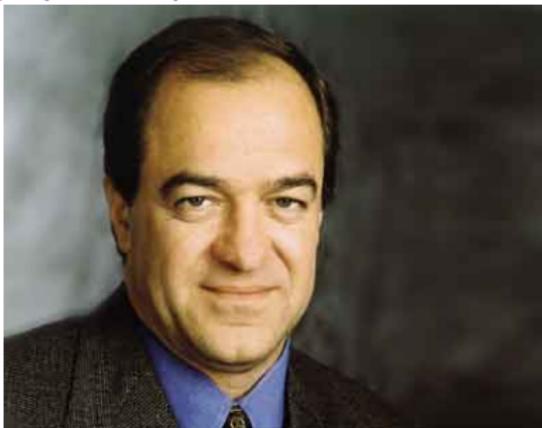
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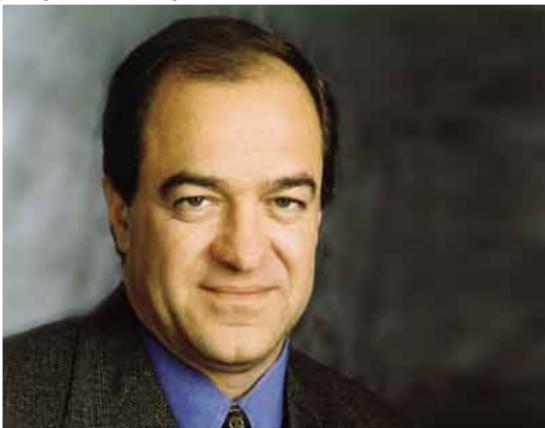
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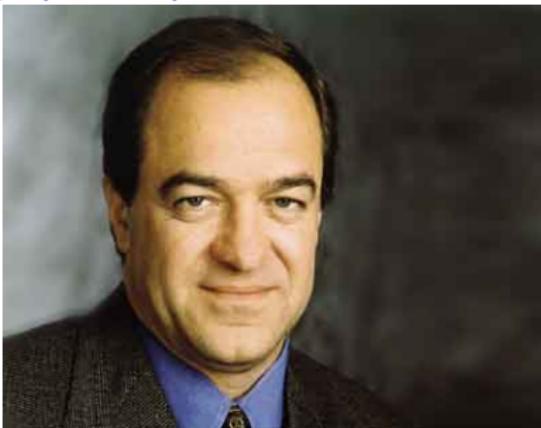
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 - 1.3 billion certificate status checks/day
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- ▶ RSA acquired by Security Dynamics in 1996, now part of EMC.

World Wide Web (Sir Tim Berners-Lee, 1990)



- ▶ Just as radio did, this new communication medium, the World-Wide Web, drove demand for cryptography to new heights.
- ▶ Cemented transition of cryptography from primarily military to primarily commercial.

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U.S. cryptography policy evolves

- ▶ U.S. government initially tried to control and limit public-sector research and use of cryptography
- ▶ Attempt to chill research via ITAR (1977)
- ▶ MIT “Changing Nature of Information” Committee (1981; Dertouzos, Low, Rosenblith, Deutch, Rivest,...)

MIT Committee Seeks Cryptography Policy

Questions of who should do research on cryptography and how results should be disseminated are the first order of business

Within the next 10 years, networks consisting of tens of thousands of computers will connect businesses, corporations,

and individuals. The consequences for individuals and for society if computers continue to be connected, as they are now, according to local deci-

easy to send computer programs between connected machines and to instruct a program to search for, select,

Science, 13 Mar 1981

U.S. cryptography policy evolves

- ▶ U.S. government tried to mandate availability of all encryption keys via “key escrow” and/or “Clipper Chip” (1993)

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- ▶ Today, US policy leans toward strong cybersecurity, including strong cryptography, for all information systems as a matter of national security.

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Factorization of RSA-129 (April 1994)

► RSA-129 =

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- ▶ 8 months work by about 600 volunteers from more
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- ▶ secret message:

The Magic Words Are Squeamish Ossifrage



BayBank For Solving the Scientific American RSA Challenge

53-235 0254643
Massachusetts 113 Official Bank Check

Date April 22, 1994

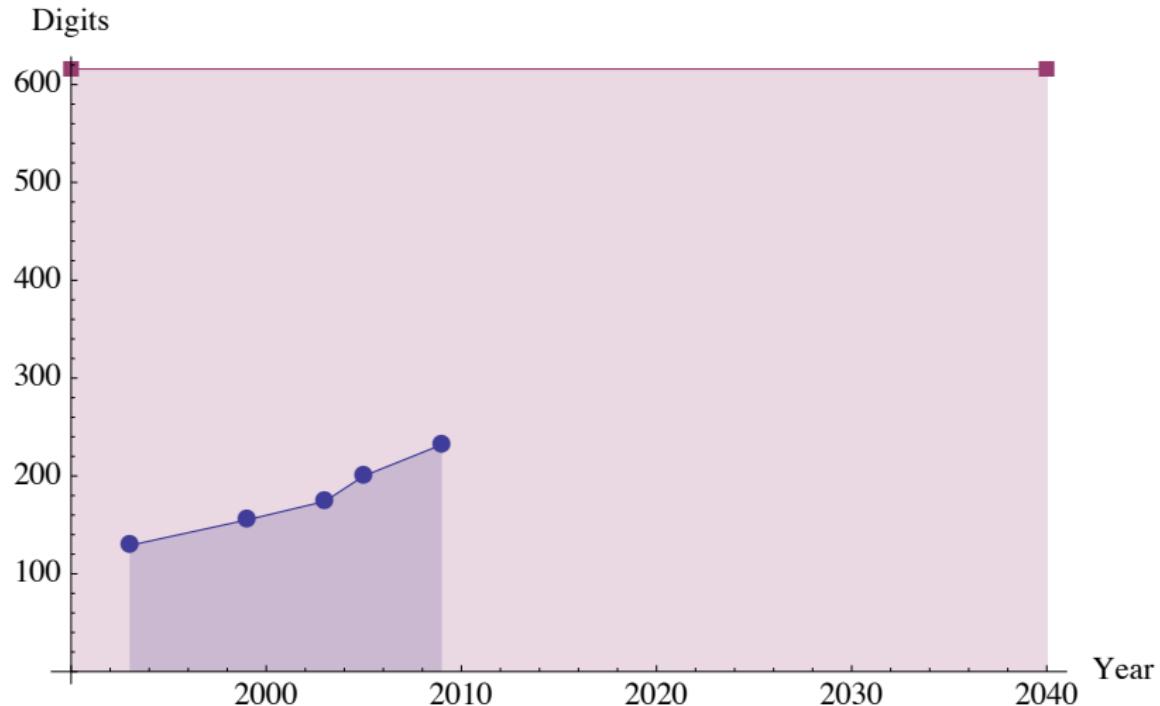
PAY The sum of 100 dollars 00 Cents \$ ****100.00****

AMOUNTS IN EXCESS OF \$100,000.00
REQUIRE TWO SIGNATURES

To the **Derek Atkins or Michael Graff or Arjen Lenstra or Paul Leyland**
order of J. B. H. Authorized Signature

BayBank #0254643#011302357#317 83321#
Authorized Signature

Factoring Records



Factoring on a Quantum Computer?



$$|\psi\rangle = \alpha|0\rangle + \beta|1\rangle$$
$$|\alpha|^2 + |\beta|^2 = 1$$
$$\alpha|0\rangle = \begin{pmatrix} 1 \\ 0 \end{pmatrix} \quad \beta|1\rangle = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

The diagram illustrates the concept of quantum superposition. On the left, a large circle represents the state $|\psi\rangle$. This state is shown as a sum of two smaller circles: one horizontal (representing $|0\rangle$) and one vertical (representing $|1\rangle$). Arrows point from the equation $|\psi\rangle = \alpha|0\rangle + \beta|1\rangle$ to the horizontal circle, and from the equation $|\alpha|^2 + |\beta|^2 = 1$ to the vertical circle. To the right, the horizontal circle is labeled $\alpha|0\rangle = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$ and the vertical circle is labeled $\beta|1\rangle = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$.

In 1994, Peter Shor invented a fast factorization algorithm that runs on a (hypothetical) *quantum computer* and works by determining multiplicative period of elements mod n .

Factoring on a Quantum Computer?



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The diagram shows a blue circle representing a quantum state $|\psi\rangle$. This state is shown as a sum of two other states: $|\alpha|0\rangle$ (represented by a circle with an upward arrow) and $\beta|1\rangle$ (represented by a circle with a downward arrow). The equation $|\alpha|^2 + |\beta|^2 = 1$ indicates that the total state is a unit vector in the complex plane.

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- ▶ In 2001, researchers at IBM used this algorithm on a (real) quantum computer to factor $15 = 3 \times 5$.

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- ▶ Dark clouds on horizon for RSA?

Hash Function Attacks



- ▶ In 2004 Xiaoyun Wang and colleagues found a way to produce *collisions* for MD5:

$$\text{MD5}(\textit{file1}) = \text{MD5}(\textit{file2}) \quad !!!$$

Also for SHA-1 and many other hash functions.
Major break!!

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- ▶ NIST now running competition for new hash function standard (SHA-3).

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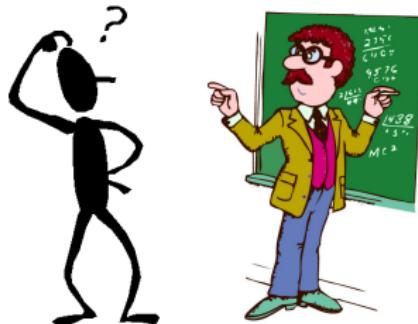
Many new research problems and directions

- ▶ secret-sharing
- ▶ anonymity
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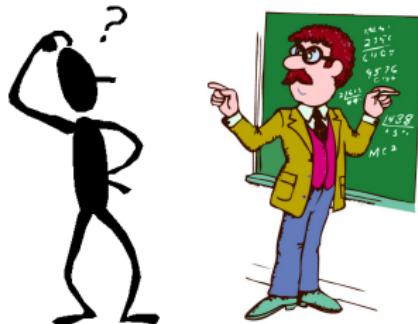
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Zero-Knowledge Proofs

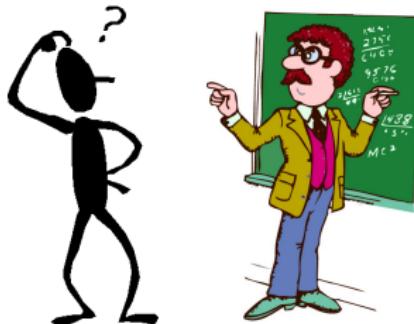


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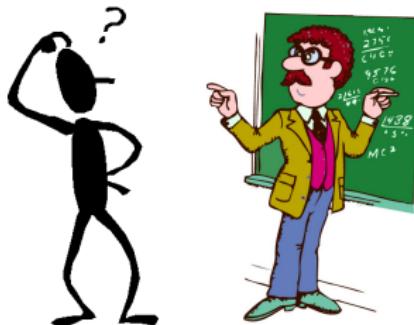
I can convince you

Zero-Knowledge Proofs



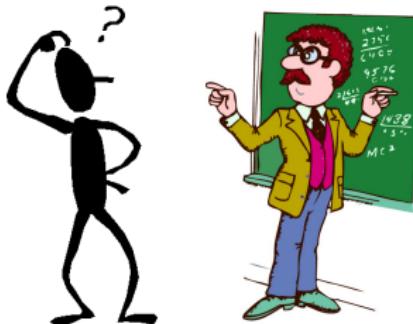
*I can convince you
I know a solution
to a hard problem*

Zero-Knowledge Proofs



*I can convince you
I know a solution
to a hard problem
while telling you nothing
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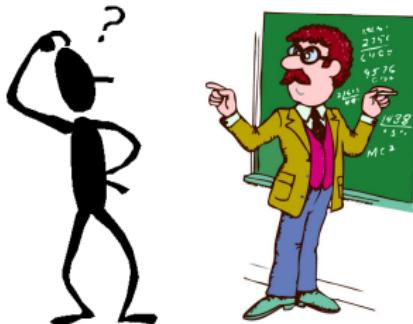
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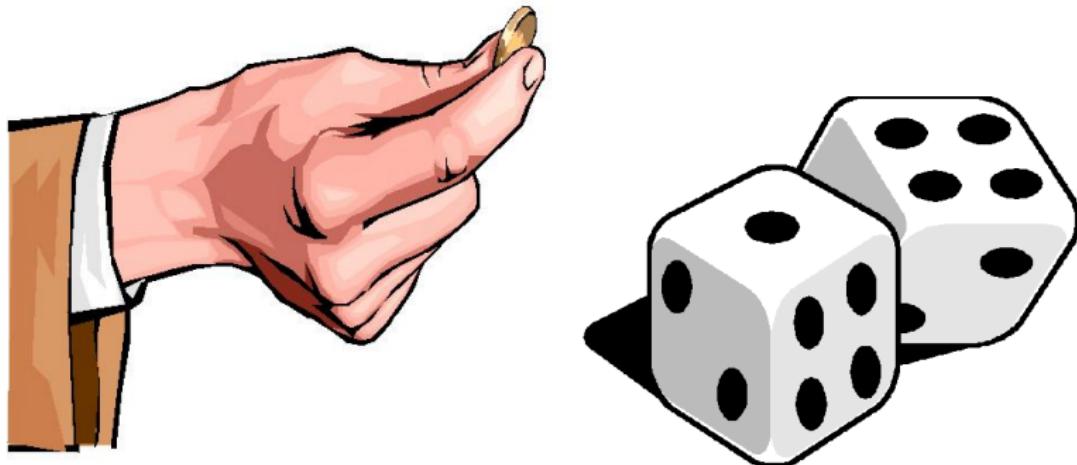


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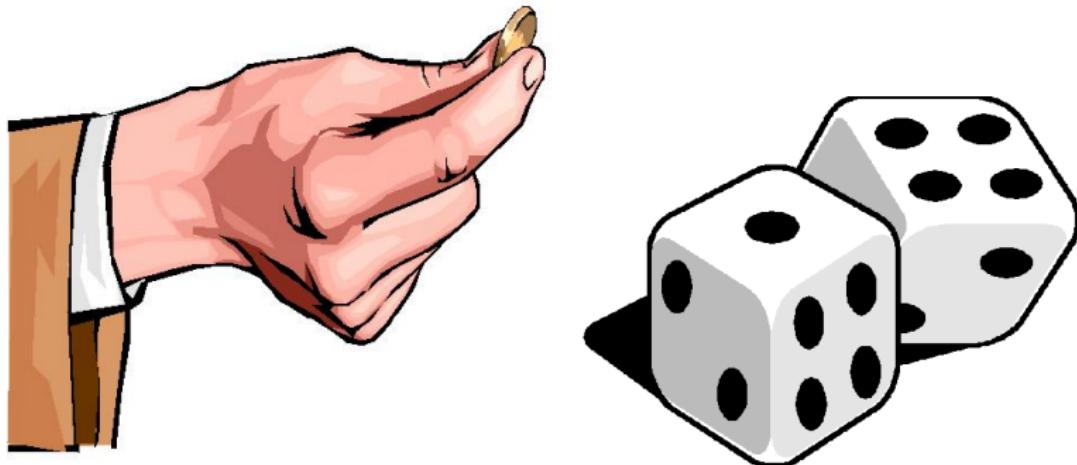
An enormously useful capability!

Probabilistic MicroPayment System



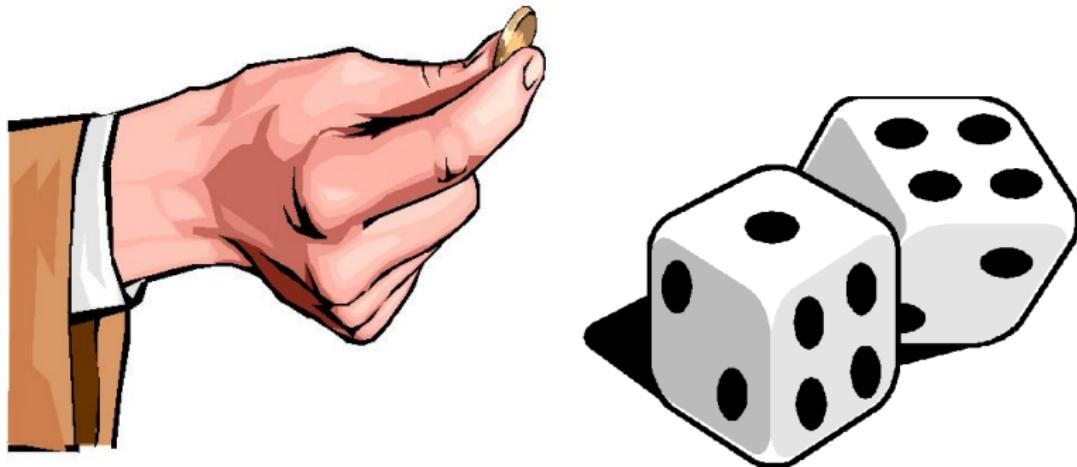
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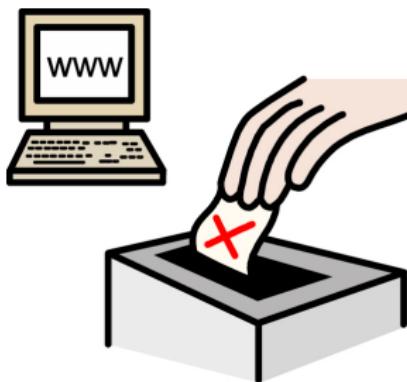
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- ▶ Peppercoin Company founded 2001, sold in 2007.

Voting Systems



New “end-to-end” cryptographic voting systems
(Chaum, Neff, Benaloh, Ryan, Rivest, Adida, ...):

- ▶ all ballots posted on web (encrypted)
- ▶ voters verify their votes are correct
(while preventing vote-selling and coercion)
- ▶ anyone can verify final tally
- ▶ may be done with paper ballots

Cryptography *increases* transparency and verifiability!

Fully Homomorphic Encryption



- ▶ In 1978, Rivest, Adleman, and Dertouzos asked,
*“Can one compute on encrypted data,
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Fully Homomorphic Encryption



?



!

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*“Can one compute on encrypted data,
while keeping it encrypted?”*
- ▶ In 2009, Craig Gentry (Stanford, IBM) gave solution
based on use of lattices. If efficiency can be greatly
improved, could be huge implications (e.g. for cloud
computing).

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Challenges

- ▶ Make more crypto theory results practical
- ▶ Is factoring really hard?
- ▶ Minimize assumptions
- ▶ Show $P \neq NP$!
- ▶ Is quantum computing practical?
- ▶ Give Alice and Bob smartphones!
- ▶ Ground crypto practice better in vulnerable computer systems

Stata Center Time Capsule Crypto Puzzle



“Time Capsule”
(really, a large lead bag)
sealed at LCS/AI 35th Celebration
April 1999

- ▶ Contains many historic LCS/AI artifacts
- ▶ There is an associated cryptographic puzzle I designed to be solvable around 2034, given predicted advances in computational power.
- ▶ When puzzle is solved, Time Capsule will be opened.

Conclusions

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- ▶ While we have accomplished a lot in a few decades, much remains to be done.
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- ▶ Cryptography is fun!

Acknowledgments

L. Adleman, R. Anderson, D. Bailey, M. Bellare, J. Benaloh, J. Bidzos, M. Bond, K. Bowers, M. Burmeister, J. Brainard, R. Canetti, D. Chaum, J. Clulow, M. Dertouzos, S. Devadas, Y. Dodis, W. Diffie, C. Ellison, M. Gardner, O. Goldreich, S. Goldwasser, M. Hellman, P. Hernson, M. Jakobsson, A. Juels, L. Knudsen, B. Lampson, R. Lee, R. Merkle, S. Micali, A. Oprea, M. Rabin, T. Rabin, L. Reyzin, V. Rijmen, M. Robshaw, P. Ryan, A. Shamir, A. Sherman, R. Silverman, M. Sudan, D. Sutherland, M. Szydlo, Y. Tauman, L. Trevisan, E. Tromer, S. Vadhan, M. Van Dijk, D. Wagner, P. Vora, H. Wee, T. Ylonen, M. Yung

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Be Blackburn

Mom and Dad, Gail, Alex, Chris.

Thank You!