## Upper bound on $\sum_{i=1}^{N} w_i^{T+1}$ for **Hedge** $(\eta)$

Lemma (upper bound)

For any sequence of loss vectors  $\ell^1, \dots, \ell^T$  we have

$$\ln\left(\sum_{i=1}^N w_i^{T+1}\right) \leq -(1-e^{-\eta})L_{\mathsf{Hedge}(\eta)}.$$