

The **Hedge**(η) Algorithm

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Outline

Hedge(η) Algorithm

Hedging vs. Halving

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Bound on total loss

Upper bound on $\sum_{i=1}^N w_i^{T+1}$

Lower bound on $\sum_{i=1}^N w_i^{T+1}$

Combining Upper and Lower bounds

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Lower Bounds

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- ▶ Fits nicely in game theory

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- ▶ Basic idea - reduce probability of lossy actions, but **not all the way to zero**.
- ▶ **Modified Goal:** minimize **difference between** expected total loss and minimal total loss of repeating one action.

$$\sum_{t=1}^T \mathbf{p}^t \cdot \ell^t - \min_i \left(\sum_{t=1}^T \ell_i^t \right)$$

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 - ▶ Experts make predictions $e_i^t \in \{0, 1\}$
 - ▶ Algorithm predicts **1** with probability $\sum_{i: e_i^t = 1} p_i^t$.
 - ▶ outcome o_i^t is revealed. $\ell_i^t = 0$ if $e_i^t = o_i^t$, $\ell_i^t = 1$ otherwise.

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Consider action i at time t

► Total loss:

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- ▶ Plays a similar role to prior distribution in Bayesian algorithms.

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► Theorem (main theorem)

For any sequence of loss vectors ℓ^1, \dots, ℓ^T , and for any $i \in \{1, \dots, N\}$, we have

$$L_{\text{Hedge}(\eta)} \leq \frac{-\ln(w_i^1) + \eta L_i}{1 - e^{-\eta}}.$$

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- **Proof:** by combining upper and lower bounds on $\sum_{i=1}^N w_i^{T+1}$

Hedge(η)

└ Bound on total loss

└ Upper bound on $\sum_{i=1}^N w_i^{T+1}$

Upper bound on $\sum_{i=1}^N w_i^{T+1}$

Lemma (upper bound)

For any sequence of loss vectors ℓ^1, \dots, ℓ^T we have

$$\ln \left(\sum_{i=1}^N w_i^{T+1} \right) \leq -(1 - e^{-\eta}) L_{\text{Hedge}(\eta)}.$$

Hedge(η)

└ Bound on total loss

└ Upper bound on $\sum_{i=1}^N w_i^{T+1}$

Proof of upper bound (slide 1)

- ▶ If $a \geq 0$ then a^r is convex.

Hedge(η)

└ Bound on total loss

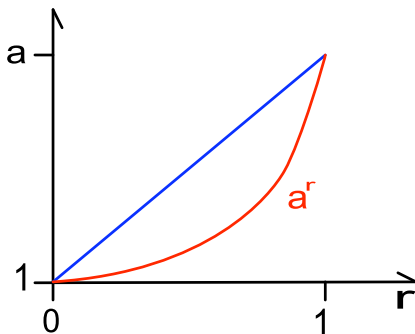
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Proof of upper bound (slide 2)

Applying $a^r \leq 1 - (1 - a)^r$ where $a = e^{-\eta}$, $r = \ell_i^t$

$$\sum_{i=1}^N w_i^{t+1} = \sum_{i=1}^N w_i^t e^{-\eta \ell_i^t}$$

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$$\begin{aligned}\sum_{i=1}^N w_i^{t+1} &= \sum_{i=1}^N w_i^t e^{-\eta \ell_i^t} \\ &\leq \sum_{i=1}^N w_i^t (1 - (1 - e^{-\eta}) \ell_i^t)\end{aligned}$$

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 &\leq \sum_{i=1}^N w_i^t (1 - (1 - e^{-\eta}) \ell_i^t) \\
 &= \left(\sum_{i=1}^N w_i^t \right) \left(1 - (1 - e^{-\eta}) \frac{\mathbf{w}^t}{\sum_{i=1}^N w_i^t} \cdot \boldsymbol{\ell}^t \right) \\
 &= \left(\sum_{i=1}^N w_i^t \right) (1 - (1 - e^{-\eta}) \mathbf{p}^t \cdot \boldsymbol{\ell}^t)
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Hedge(η)

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Proof of upper bound (slide 3)

► Combining

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$$\begin{aligned} \sum_{i=1}^N w_i^{T+1} &\leq \prod_{t=1}^T (1 - (1 - e^{-\eta}) \mathbf{p}^t \cdot \ell^t) \\ &\leq \exp \left(-(1 - e^{-\eta}) \sum_{t=1}^T \mathbf{p}^t \cdot \ell^t \right) \end{aligned}$$

since $1 + x \leq e^x$ for $x = -(1 - e^{-\eta})$.

Hedge(η)

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└ Lower bound on $\sum_{i=1}^N w_i^{T+1}$

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For any $j = 1, \dots, N$:

$$\sum_{i=1}^N w_i^{T+1} \geq w_j^{T+1} = w_j^1 e^{-\eta L_j}$$

Combining Upper and Lower bounds

- Combining bounds on $\ln \left(\sum_{i=1}^N w_i^{T+1} \right)$

$$\ln w_j^1 - \eta L_j \leq \ln \sum_{i=1}^N w_i^{T+1} \leq -(1 - e^{-\eta}) \sum_{t=1}^T \mathbf{p}^t \cdot \ell^t$$

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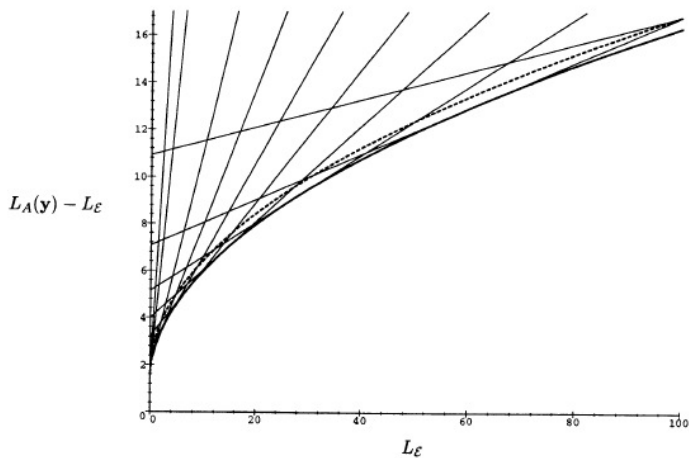
- ▶ Reversing signs, using $L_{\text{Hedge}(\eta)} = \sum_{t=1}^T \mathbf{p}^t \cdot \ell^t$ and reorganizing we get

$$L_{\text{Hedge}(\eta)} \leq \frac{-\ln(w_i^1) + \eta L_i}{1 - e^{-\eta}}$$

Tuning η

How to Use Expert Advice

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- ▶ Then

$$L_{\text{Hedge}(\eta)} \leq \frac{-\ln(w_i^1) + \eta L_i}{1 - e^{-\eta}} \leq \min_i L_i + \sqrt{2\tilde{L} \ln N} + \ln N$$

Tuning η as a function of T

- trivially $\min_i L_i \leq T$, yielding

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- ▶ per iteration we get:

$$\frac{L_{\text{Hedge}(\eta)}}{T} \leq \min_i \frac{L_i}{T} + \sqrt{\frac{2 \ln N}{T}} + \frac{\ln N}{T}$$

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- ▶ The adversarial strategy is random, extremely simple, and does not depend on the hedging strategy!

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- ▶ Detailed proof quite involved. See games paper.

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- ▶ A trivial random data, in which there is nothing to be learned forces **any** algorithm to suffer this total loss

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- ▶ Office hour: 2-3pm on tuesdays.