

Number of mistakes is smallest m such that

$$\frac{1}{2^{m+1}} \binom{m+1}{\leq k-i} = \frac{1}{2^{m+1}} \sum_{j=0}^{k-i} \binom{m+1}{j} < 1$$