log loss encourages unbiased prediction

- ▶ Suppose the source is random and the probability of the next outcome is $p(c_t | c_1, c_2, ..., c_{t-1})$
- ► Then the prediction that minimizes the log loss is $p(c_t | c_1, c_2, ..., c_{t-1})$.
- Note that when minimizing expected number of mistakes, the best prediction in this situation is to put all of the probability on the most likely outcome.
- There are other losses with this property, for example, square loss.