## Zachet/exam syllabus. 6 points of your final grade

Theoretical Deep Learning #2, MIPT

All proofs are needed, if not stated otherwise.

## 1 Main part (4 points total).

- 1. Problem statement for bounding test-train risk difference. Worst-case bounds.
- 2. Worst-case bound for 0-1 loss. VC-lemma (without proof). Growth function. VC-dimension. Sauer's lemma (without proof)
- 3. The reason to introduce  $\gamma$ -margin loss instead of 0-1 loss. Bounding  $R \hat{R}_{n,\gamma}$  with  $l_{\infty}$ -covering numbers (without proof; analogy with 0-1 loss case). Fat-shattering dimension. Connection of the latter with  $l_{\infty}$ -covering numbers (without proof; analogy with VC-dimension). Example of function class with finite fat-shattering dimension, but with infinite VC-dimension.<sup>2</sup>
- 4. McDiarmid's inequality (without proof). Rademacher complexity. Bounding test-train risk difference with Rademacher complexity.<sup>3</sup>
- 5. PAC-bayesian bound for at most countable hypothesis classes.
- 6. PAC-bayesian bound for uncountable hypothesis classes (in the form of McAllester)<sup>4</sup>.
- 7. Failure of PAC-bayesian bounds for deterministic learning algorithms. Way to leverage: stochastization<sup>5</sup>.

 $<sup>^1{\</sup>rm In}$  a similar manner as in Theorem 2 of Bartlett (1998): https://ieeexplore.ieee.org/stamp/stamp.jsp?arnumber=661502

<sup>&</sup>lt;sup>2</sup>Based on Bartlett (1998)

<sup>&</sup>lt;sup>3</sup>Have a look at lecture notes by Geoffrey Decrouez: https://1f912c10-a4be-4e1b-a1e2-6af556aeef2a.filesusr.com/ugd/dd0cbc\_ 95c300090eb64378aaa1e0218987cbf9.pdf

<sup>&</sup>lt;sup>4</sup>Theorem 2 of McAllester (1999): http://citeseerx.ist.psu.edu/viewdoc/download?doi=10.1.1.21.1908&rep=rep1&type=pdf

<sup>&</sup>lt;sup>5</sup>Based on Dziugaite & Roy (2017): https://arxiv.org/abs/1703.11008

8. PAC-bayesian bound for a deterministic learning algorithm (Neyshabur et al.,  $2018^6$ ).

## 2 Auxiliary part (2 points total).

- 1. Proof of bound for  $R \hat{R}_{n,\gamma}$  with  $l_{\infty}$ -covering numbers.<sup>7</sup>
- 2. Bounding Rademacher complexity for 0-1 loss with growth function (Hoeffding's lemma without proof).  $^8$
- 3. Bounding  $R \hat{R}_{n,\gamma}$  for deep ReLU nets with spectral complexity (Dudley's integral and a covering number for a set of vectors without proof)<sup>9</sup>.
- 4. Compression approach. Deriving a bound of Neyshabur et al. (2018) with compression approach (Arora et al.,  $2018^{10}$ ) (omit estimates for K in weight discretization step).

 $<sup>^6 {\</sup>rm https://openreview.net/forum?id=Skz\_WfbCZ}$ 

<sup>&</sup>lt;sup>7</sup>Theorem 2 in Bartlett (1998)

<sup>&</sup>lt;sup>8</sup>Again, have a look at lecture notes by Geoffrey Decrouez

<sup>&</sup>lt;sup>9</sup>Main result of Bartlett et al. (2017): https://arxiv.org/abs/1706.08498

 $<sup>^{10} \</sup>mathtt{http://proceedings.mlr.press/v80/arora18b.html}$