

Supplement for Estimated Judge Reliabilities for Weighted Bradley-Terry-Luce Are Not Reliable

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The following are additional data for the paper *Estimated Judge Reliabilities for Weighted Bradley-Terry-Luce Are Not Reliable* to provide transparency.

1 BROKEN SYMMETRY

In this section, we show results for all 20, $n^2 - n$, inversions for the example described in section 4.3 where every judge has an inversion from the s^* order at a single location based on their index, but one judge has two inversions such that they now agree with another judge in the set. As previously mentioned, since this scenario creates a pattern where the majority always agrees, the standard Bradley-Terry-Luce method of eq. (1) finds the s^* order, shown in table 1.

We show results both with, $\lambda = 1$, and without, $\lambda = 0$, Mease’s penalty. We caution that the results here are merely examples of what could happen; different solutions based on different starting positions are possible. The starting conditions, parameters, and tolerances are neither optimized nor cherry-picked.

Tables 1 and 2 show the results for the BTL method. Note that when $\lambda = 1$, s^* is no longer reliably recovered.

Tables 3 and 4 show the results for Crowd-BT. An important observation here is that the least reliable judge is often in \mathcal{D} : 85% of the time when $\lambda = 0$ and 100% of the time when $\lambda = 1$.

Tables 5 and 6 show the results for O’Donovan *et al.*’s method. With the $\lambda = 0$, the least reliable judge is a member of \mathcal{D} in 40% of the trials, but this increases to 100% when $\lambda = 1$. Since the least reliable judge is always in \mathcal{D} for $\lambda = 1$, the judge who shares that inversion, often is part of \mathcal{D} too. Interestingly, there is always some setting for which the least reliable judge can be elevated into \mathcal{D} .

2 FONTS

In section 4.3 we discussed the results from repeating O’Donovan *et al.*’s result along with a variation where the attributes were treated as independent scales. Here, we provide the full tables of Pearson correlation coefficients for both Crowd-BT, table 7, and O’Donovan *et al.*’s method, table 8, along with histograms fig. 1 and fig. 2. Our intention is to release these tables as CSV files with other supplemental materials since their reproduction is difficult to read.

3 SIMULATION DATA

Using the procedure we explained in section 6 and appendix A.3, we generated fig. 5. Tables 9 and 10 show $\omega = \{0.02, 0.1\}$, respectively, for 8 judges per pair, which closely approximate several of the Fonts attributes. In the tables, we provide the mean value of τ , μ_τ , as well as the standard deviation, σ_τ . In each, we highlight the 800 pair

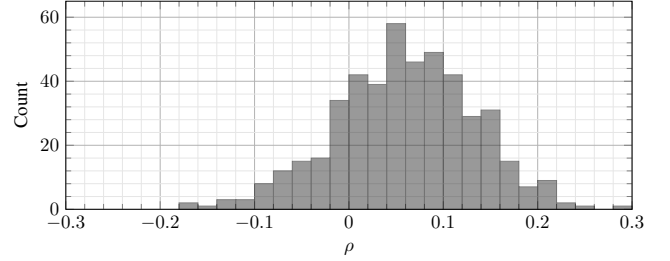


Figure 1: Distribution of ρ values for independently estimated scales using Crowd-BT. Tabular data is in table 7.

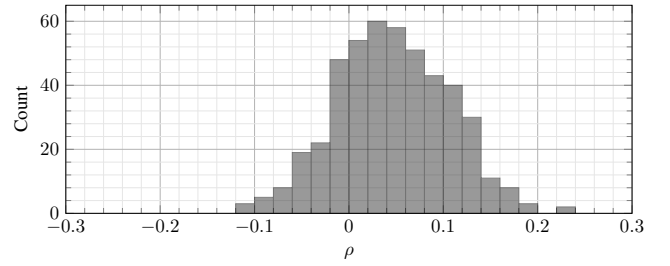


Figure 2: Distribution of ρ values for independently estimated scales using O’Donovan *et al.*’s method. Tabular data is in table 8.

line, since this represents data that are the same size as the Fonts dataset.

In tables 11 and 12, we provide a statistical comparison between the two experimental methods, Chen *et al.*’s Crowd-BT and O’Donovan *et al.*’s method, against the unweighted BTL order on a matched pair basis for the simulated data with 8 judges per pair, $\omega = \{0.02, 0.1\}$, and $\lambda = 0$. For each, we use a Bayesian Paired Samples T-Test, computed using JASP 0.16 [1]. We use Student-T where $H_a : \tau_{\text{experimental}} \neq \tau_{\text{BTL}}$ and the prior is Cauchy with scale 0.707. Values of $\log(BF_{10})$ are traditionally interpreted using the scale provided by Jeffreys [2].

We note that many of the values show strong evidence of being different from the BTL result; however, most are very slight underperformances. When $\omega = 0.02$, both methods underperform in all instances except when the pair count is 200. For $\omega = 0.1$, both methods perform much better than BTL when the pair count is 200, and still perform slightly better for a little while longer. However, by the time we reach the size of Fonts (pair count of 800), both methods underperform BTL very slightly. This trend of underperformance continues through the rest of the table, but is often quite small

Judge	“error”	Stimuli Positions						$\hat{s} = s^*$
		ζ_1	ζ_2	ζ_3	ζ_4	ζ_5	ζ_6	
u_1	$s_2 > s_3$	-2.368	-0.982	-0.576	0.810	2.197	3.583	Yes
	$s_3 > s_4$	-2.531	-1.145	0.242	0.647	2.033	3.420	Yes
	$s_4 > s_5$	-2.694	-1.308	0.078	1.464	1.870	3.256	Yes
	$s_5 > s_6$	-2.858	-1.472	-0.086	1.301	2.687	3.092	Yes
u_2	$s_1 > s_2$	-2.204	-1.799	-0.412	0.974	2.360	3.746	Yes
	$s_3 > s_4$	-2.531	-1.145	0.242	0.647	2.033	3.420	Yes
	$s_4 > s_5$	-2.694	-1.308	0.078	1.464	1.870	3.256	Yes
	$s_5 > s_6$	-2.858	-1.472	-0.086	1.301	2.687	3.092	Yes
u_3	$s_1 > s_2$	-2.204	-1.799	-0.412	0.974	2.360	3.746	Yes
	$s_2 > s_3$	-2.368	-0.982	-0.576	0.810	2.197	3.583	Yes
	$s_4 > s_5$	-2.694	-1.308	0.078	1.464	1.870	3.256	Yes
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	$s_2 > s_3$	-2.368	-0.982	-0.576	0.810	2.197	3.583	Yes
	$s_3 > s_4$	-2.531	-1.145	0.242	0.647	2.033	3.420	Yes
	$s_4 > s_5$	-2.694	-1.308	0.078	1.464	1.870	3.256	Yes

Table 1: Full results from adding an additional error to various judges solved using BTL with $\lambda = 0$.

Judge	“error”	Stimuli Positions						$\hat{s} = s^*$
		ζ_1	ζ_2	ζ_3	ζ_4	ζ_5	ζ_6	
u_1	$s_2 > s_3$	-1.142	-0.310	-0.446	0.052	0.572	1.340	No
	$s_3 > s_4$	-1.269	-0.479	0.099	-0.099	0.479	1.269	No
	$s_4 > s_5$	-1.340	-0.572	-0.052	0.446	0.310	1.142	No
	$s_5 > s_6$	-1.381	-0.626	-0.138	0.293	0.847	0.907	Yes
u_2	$s_1 > s_2$	-0.907	-0.847	-0.293	0.138	0.626	1.381	Yes
	$s_3 > s_4$	-1.269	-0.479	0.099	-0.099	0.479	1.269	No
	$s_4 > s_5$	-1.340	-0.572	-0.052	0.446	0.310	1.142	No
	$s_5 > s_6$	-1.381	-0.626	-0.138	0.293	0.847	0.907	Yes
u_3	$s_1 > s_2$	-0.907	-0.847	-0.293	0.138	0.626	1.381	Yes
	$s_2 > s_3$	-1.142	-0.310	-0.446	0.052	0.572	1.340	No
	$s_4 > s_5$	-1.340	-0.572	-0.052	0.446	0.310	1.142	No
	$s_5 > s_6$	-1.381	-0.626	-0.138	0.293	0.847	0.907	Yes
u_4	$s_1 > s_2$	-0.907	-0.847	-0.293	0.138	0.626	1.381	Yes
	$s_2 > s_3$	-1.142	-0.310	-0.446	0.052	0.572	1.340	No
	$s_3 > s_4$	-1.269	-0.479	0.099	-0.099	0.479	1.269	No
	$s_5 > s_6$	-1.381	-0.626	-0.138	0.293	0.847	0.907	Yes
u_5	$s_1 > s_2$	-0.907	-0.847	-0.293	0.138	0.626	1.381	Yes
	$s_2 > s_3$	-1.142	-0.310	-0.446	0.052	0.572	1.340	No
	$s_3 > s_4$	-1.269	-0.479	0.099	-0.099	0.479	1.269	No
	$s_4 > s_5$	-1.340	-0.572	-0.052	0.446	0.310	1.142	No

Table 2: Full results from adding an additional error to various judges solved using BTL with $\lambda = 1$.

and not statistically interesting. Regardless, of the two methods, Crowd-BT tends to behave more similar to BTL than O'Donovan *et al.*'s method.

These results suggest that, at least for reliable judges, one would only want to use the weighted methods for very low number of pairs (a very low data density). Future work remains as to whether some

Judge	"error"	Judge Weights					$ \mathcal{D} $	Stimuli Positions						$\hat{s} = s^*$
		μ_1	μ_2	μ_3	μ_4	μ_5		ζ_1	ζ_2	ζ_3	ζ_4	ζ_5	ζ_6	
u_1	$s_2 > s_3$	0.000	<i>0.500</i>	1.000	1.000	1.000	4	-23.738	-7.492	8.116	8.116	8.116	8.116	No
	$s_3 > s_4$	<i>0.500</i>	1.000	1.000	1.000	1.000	4	-14.777	0.819	1.917	3.016	4.115	5.213	Yes
	$s_4 > s_5$	1.000	<i>0.500</i>	<i>0.500</i>	1.000	<i>0.500</i>	2	-15.843	-15.843	0.495	16.866	-1.690	15.923	No
	$s_5 > s_6$	<i>0.500</i>	1.000	1.000	1.000	1.000	4	-14.697	0.802	1.901	2.999	4.098	5.196	Yes
u_2	$s_1 > s_2$	<i>0.500</i>	0.000	1.000	1.000	1.000	4	-23.559	-7.828	8.148	8.148	8.148	8.148	No
	$s_3 > s_4$	<i>0.500</i>	1.000	1.000	<i>0.500</i>	<i>0.500</i>	2	-13.422	3.247	3.247	-13.722	2.399	18.137	No
	$s_4 > s_5$	1.000	<i>0.609</i>	1.000	1.000	<i>0.723</i>	3	-17.209	-16.167	2.859	3.901	4.688	21.783	Yes
	$s_5 > s_6$	1.000	0.000	1.000	1.000	<i>0.500</i>	4	-13.138	-13.138	2.462	2.462	2.462	18.674	No
u_3	$s_1 > s_2$	1.000	<i>0.500</i>	1.000	<i>0.500</i>	<i>0.500</i>	2	-4.718	-23.270	-5.580	-5.580	10.745	27.431	No
	$s_2 > s_3$	<i>0.500</i>	1.000	1.000	<i>0.500</i>	<i>0.500</i>	2	-11.161	6.716	-11.418	-11.418	4.576	21.994	No
	$s_4 > s_5$	<i>0.500</i>	<i>0.500</i>	1.000	1.000	<i>0.500</i>	2	-19.988	-3.174	12.729	12.729	-10.457	8.624	No
	$s_5 > s_6$	<i>0.500</i>	<i>0.500</i>	1.000	<i>0.500</i>	1.000	2	-26.631	-10.464	5.420	5.420	21.958	5.279	No
u_4	$s_1 > s_2$	1.000	<i>0.500</i>	<i>0.500</i>	1.000	<i>0.500</i>	2	-7.858	-24.247	-7.594	7.772	7.772	24.169	No
	$s_2 > s_3$	<i>0.500</i>	1.000	<i>0.500</i>	1.000	<i>0.500</i>	2	-13.343	3.307	-13.125	2.557	2.557	17.887	No
	$s_3 > s_4$	<i>0.500</i>	<i>0.500</i>	1.000	1.000	<i>0.500</i>	2	-18.763	-1.859	13.943	-3.007	-3.007	12.890	No
	$s_5 > s_6$	<i>0.500</i>	<i>0.500</i>	<i>0.500</i>	1.000	1.000	2	-30.911	-12.578	3.523	20.646	20.646	0.288	No
u_5	$s_1 > s_2$	<i>0.500</i>	1.000	1.000	1.000	0.000	4	-16.310	-0.121	-0.121	-0.121	-0.121	16.757	No
	$s_2 > s_3$	<i>0.500</i>	1.000	<i>0.500</i>	<i>0.500</i>	1.000	2	-15.456	1.664	-16.193	-0.373	15.227	15.227	No
	$s_3 > s_4$	<i>0.500</i>	<i>0.500</i>	1.000	<i>0.500</i>	1.000	2	-19.623	-4.329	10.991	-5.733	9.595	9.595	No
	$s_4 > s_5$	<i>0.500</i>	<i>0.500</i>	<i>0.500</i>	1.000	1.000	2	-27.338	-10.022	6.134	22.825	4.702	4.702	No

Table 3: Full results from adding an additional error to various judges solved using Chen *et al.*'s Crowd-BT with $\lambda = 0$. The *italic* entries represent the judges we expect to be in \mathcal{D} because the new "error" agrees with their position; bold entries are judges in \mathcal{D} . The cells with the red background highlight the least reliable judge.

Judge	"error"	Judge Weights					$ \mathcal{D} $	Stimuli Positions						$\hat{s} = s^*$
		μ_1	μ_2	μ_3	μ_4	μ_5		ζ_1	ζ_2	ζ_3	ζ_4	ζ_5	ζ_6	
u_1	$s_2 > s_3$	1.000	1.000	0.000	0.477	0.291	3	0.699	0.203	-1.787	-0.013	0.027	0.552	No
	$s_3 > s_4$	1.000	0.000	1.000	0.303	0.410	3	0.216	-0.640	1.326	-0.883	-0.145	0.219	No
	$s_4 > s_5$	1.000	0.388	0.322	1.000	0.000	3	0.344	-0.433	0.076	0.809	-1.405	0.463	No
	$s_5 > s_6$	0.000	1.000	1.000	1.000	<i>0.146</i>	4	-0.848	0.551	0.119	-0.259	-0.754	1.270	No
u_2	$s_1 > s_2$	1.000	1.000	1.000	1.000	0.000	5	-0.058	-0.488	-0.302	-0.236	-0.264	1.608	No
	$s_3 > s_4$	0.289	1.000	1.000	0.000	0.541	3	-0.131	0.743	0.265	-1.692	0.214	0.324	No
	$s_4 > s_5$	0.429	1.000	0.242	1.000	0.258	2	-0.350	0.387	-0.443	1.158	-1.138	0.390	No
	$s_5 > s_6$	0.000	1.000	0.000	0.000	1.000	5	0.131	0.592	-0.400	0.137	0.733	-1.309	No
u_3	$s_1 > s_2$	1.000	0.000	1.000	0.312	0.332	3	0.852	-1.338	0.507	-0.469	-0.023	0.356	No
	$s_2 > s_3$	0.000	1.000	1.000	0.377	0.493	3	-0.515	1.642	-0.303	-0.769	-0.075	0.264	No
	$s_4 > s_5$	0.493	0.377	1.000	1.000	0.000	3	-0.264	0.075	0.769	0.303	-1.642	0.515	No
	$s_5 > s_6$	0.332	0.312	1.000	0.000	1.000	3	-0.356	0.023	0.469	-0.507	1.338	-0.852	No
u_4	$s_1 > s_2$	1.000	0.000	0.000	1.000	0.000	5	1.309	-0.733	-0.137	0.400	-0.592	-0.131	No
	$s_2 > s_3$	0.258	1.000	0.242	1.000	0.429	2	-0.390	1.138	-1.158	0.443	-0.387	0.350	No
	$s_3 > s_4$	0.541	0.000	1.000	1.000	0.289	3	-0.324	-0.214	1.692	-0.265	-0.743	0.131	No
	$s_5 > s_6$	0.000	1.000	1.000	1.000	1.000	5	-1.608	0.264	0.236	0.302	0.488	0.058	No
u_5	$s_1 > s_2$	<i>0.146</i>	1.000	1.000	1.000	0.000	4	-1.270	0.754	0.259	-0.119	-0.551	0.848	No
	$s_2 > s_3$	0.000	1.000	0.322	0.388	1.000	3	-0.463	1.405	-0.809	-0.076	0.433	-0.344	No
	$s_3 > s_4$	0.410	0.303	1.000	0.000	1.000	3	-0.219	0.145	0.883	-1.326	0.640	-0.216	No
	$s_4 > s_5$	0.000	1.000	1.000	1.000	1.000	5	-1.569	0.322	0.325	0.458	-0.039	0.260	No

Table 4: Full results from adding an additional error to various judges solved using Chen *et al.*'s Crowd-BT with $\lambda = 1$. The *italic* entries represent the judges we expect to be in \mathcal{D} because the new "error" agrees with their position; bold entries are judges in \mathcal{D} . The cells with the red background highlight the least reliable judge.

Judge	"error"	Judge Weights						\mathcal{D}	Stimuli Positions						$\hat{s} = s^*$
		μ_1	μ_2	μ_3	μ_4	μ_5	ζ_1		ζ_2	ζ_3	ζ_4	ζ_5	ζ_6		
u_1	$s_2 > s_3$	-0.235	0.016	10.000	0.238	0.238	1	-100.000	81.526	99.554	99.132	99.566	100.000	No	
	$s_3 > s_4$	1.039	-0.022	10.000	0.023	0.023	1	-100.000	-99.722	95.926	91.673	95.836	100.000	No	
	$s_4 > s_5$	10.000	-0.022	-0.022	1.009	-0.022	1	91.638	91.352	95.676	100.000	-100.000	-95.676	No	
	$s_5 > s_6$	-0.235	0.238	10.000	0.238	0.016	1	-100.000	81.526	81.960	81.538	81.972	100.000	No	
u_2	$s_1 > s_2$	0.016	-0.235	10.000	0.238	0.238	1	-100.000	-81.972	99.554	99.132	99.566	100.000	No	
	$s_3 > s_4$	0.023	1.039	10.000	0.023	-0.022	1	-100.000	-95.836	-95.558	-99.811	-95.648	100.000	No	
	$s_4 > s_5$	0.032	10.000	0.032	10.000	-0.032	2	-100.000	-99.290	-99.290	-98.580	-99.292	99.999	No	
	$s_5 > s_6$	-0.022	10.000	-0.022	-0.022	1.009	1	87.314	91.638	91.352	95.676	100.000	-100.000	No	
u_3	$s_1 > s_2$	10.000	0.032	10.000	0.032	-0.032	2	-99.289	-100.000	-99.290	-99.290	-98.581	100.000	No	
	$s_2 > s_3$	0.023	10.000	1.040	0.023	-0.022	1	-100.000	-95.794	-100.000	-99.722	-95.560	100.000	No	
	$s_4 > s_5$	0.032	0.032	10.000	10.000	-0.032	2	-100.000	-99.290	-98.580	-98.580	-99.292	100.000	No	
	$s_5 > s_6$	-0.022	-0.022	10.000	-0.022	1.009	1	87.314	91.638	95.962	95.676	100.000	-100.000	No	
u_4	$s_1 > s_2$	10.000	0.023	0.023	1.063	-0.023	1	-95.909	-100.000	-95.926	-91.853	-91.577	100.000	No	
	$s_2 > s_3$	-0.022	1.009	-0.022	10.000	-0.022	1	95.676	100.000	-100.000	-95.676	-95.962	-91.638	No	
	$s_3 > s_4$	0.023	0.023	10.000	1.039	-0.022	1	-100.000	-95.836	-91.673	-95.926	-95.648	100.000	No	
	$s_5 > s_6$	-0.023	0.023	0.023	1.063	10.000	1	-100.000	91.577	95.651	99.724	100.000	95.909	No	
u_5	$s_1 > s_2$	0.016	0.238	0.238	10.000	-0.235	1	-100.000	-81.972	-81.538	-81.104	-81.526	100.000	No	
	$s_2 > s_3$	-0.022	1.009	-0.022	-0.022	10.000	1	95.676	100.000	-100.000	-95.676	-91.352	-91.638	No	
	$s_3 > s_4$	0.023	0.023	10.000	-0.022	1.039	1	-100.000	-95.836	-91.673	-95.926	99.722	100.000	No	
	$s_4 > s_5$	-0.023	0.023	0.023	10.000	1.062	1	-100.000	91.843	95.922	100.000	95.904	96.180	No	

Table 5: Full results from adding an additional error to various judges solved using O'Donovan *et al.*'s method with $\lambda = 0$. The *italic* entries represent the judges we expect to be in \mathcal{D} because the new "error" agrees with their position; bold entries are judges in \mathcal{D} . The cells with the red background highlight the least reliable judge.

Judge	"error"	Judge Weights						\mathcal{D}	Stimuli Positions						$\hat{s} = s^\star$
		μ_1	μ_2	μ_3	μ_4	μ_5	ζ_1		ζ_2	ζ_3	ζ_4	ζ_5	ζ_6		
u_1	$s_2 > s_3$	10.000	10.000	-1.277	-1.153	-1.125	2	0.617	0.588	-0.782	-0.441	-0.141	0.150	No	
	$s_3 > s_4$	10.000	-1.157	10.000	-1.118	-1.017	2	0.303	0.274	0.635	-0.743	-0.396	-0.086	No	
	$s_4 > s_5$	10.000	-1.058	-1.147	10.000	-1.132	2	0.069	0.036	0.348	0.694	-0.748	-0.408	No	
	$s_5 > s_6$	-10.000	2.327	2.325	2.384	-1.002	1	-0.587	0.195	0.006	-0.182	-0.380	1.004	No	
u_2	$s_1 > s_2$	-1.112	10.000	10.000	-1.218	-1.084	2	0.227	0.547	0.520	-0.776	-0.422	-0.113	No	
	$s_3 > s_4$	-1.025	10.000	-1.177	10.000	-1.128	2	-0.006	0.297	0.267	0.626	-0.773	-0.431	No	
	$s_4 > s_5$	-1.025	10.000	-1.177	10.000	-1.128	2	-0.006	0.297	0.267	0.626	-0.773	-0.431	No	
	$s_5 > s_6$	-1.101	10.000	-1.122	-1.197	10.000	2	-0.215	0.079	0.044	0.346	0.677	-0.974	No	
u_3	$s_1 > s_2$	10.000	-1.241	10.000	-1.112	-1.109	2	1.003	-0.614	-0.276	-0.310	-0.019	0.271	No	
	$s_2 > s_3$	-1.242	10.000	10.000	-1.151	-1.099	2	0.464	0.808	-0.523	-0.550	-0.236	0.061	No	
	$s_4 > s_5$	0.974	1.001	10.000	10.000	-1.352	2	-0.511	-0.233	0.033	0.032	-0.370	1.143	No	
	$s_5 > s_6$	-1.109	-1.112	10.000	-1.241	10.000	2	-0.271	0.019	0.310	0.276	0.614	-1.003	No	
u_4	$s_1 > s_2$	10.000	-1.197	-1.122	10.000	-1.101	2	0.974	-0.677	-0.346	-0.044	-0.079	0.215	No	
	$s_2 > s_3$	-1.128	10.000	-1.177	10.000	-1.025	2	0.431	0.773	-0.626	-0.267	-0.297	0.006	No	
	$s_3 > s_4$	1.034	1.057	10.000	10.000	-1.321	2	-0.455	-0.175	0.096	-0.274	-0.275	1.196	No	
	$s_5 > s_6$	-1.198	-1.193	-1.241	10.000	10.000	2	-0.317	-0.031	0.253	0.553	0.521	-1.039	No	
u_5	$s_1 > s_2$	10.000	-1.215	-1.133	-1.116	10.000	2	0.943	-0.727	-0.403	-0.108	0.180	0.144	No	
	$s_2 > s_3$	-1.132	10.000	-1.147	-1.058	10.000	2	0.408	0.748	-0.694	-0.348	-0.036	-0.069	No	
	$s_3 > s_4$	-1.017	-1.118	10.000	-1.157	10.000	2	0.086	0.396	0.743	-0.635	-0.274	-0.303	No	
	$s_4 > s_5$	-1.125	-1.153	-1.277	10.000	10.000	2	-0.150	0.141	0.441	0.782	-0.588	-0.617	No	

Table 6: Full results from adding an additional error to various judges solved using O'Donovan *et al.*'s method with $\lambda = 1$. The *italic* entries represent the judges we expect to be in \mathcal{D} because the new "error" agrees with their position; bold entries are judges in \mathcal{D} . The cells with the red background highlight the least reliable judge.

artistic										attention-grabbing										boring										wide									
angular	0.049	-0.024	-0.040	0.031	-0.128	0.023	0.082	0.072	0.065	0.100	0.007	0.105	0.046	-0.082	-0.046	0.115	-0.021	-0.105	-0.039	0.016	-0.053	-0.106	0.146	0.092	0.039	-0.091	0.063	0.088	-0.051	0.152									
artistic	0.076	0.064	0.122	0.076	0.064	0.061	-0.035	0.066	0.074	0.020	0.193	0.134	0.056	0.065	0.047	0.089	0.119	0.032	0.076	0.069	0.143	0.150	-0.151	0.042	0.088	0.076	0.006	0.090	-0.028	-0.055									
attention-grabbing	0.135	-0.004	0.127	-0.006	0.096	0.038	0.019	0.017	0.080	-0.032	-0.042	-0.132	0.061	-0.102	0.047	-0.005	0.128	-0.047	-0.005	0.128	-0.047	0.109	0.115	-0.088	0.001	0.012	0.178	-0.038	0.193	-0.001	-0.014								
attractive	0.050	-0.145	-0.028	0.076	-0.022	-0.019	0.038	0.066	-0.017	-0.050	0.013	0.160	0.020	0.088	0.188	-0.066	0.028	0.035	0.048	-0.014	-0.008	0.054	0.062	-0.008	-0.001	0.028	-0.044	0.049	0.069										
bad	-0.145					0.093	-0.010	0.085	0.042	-0.119	0.050	0.031	0.183	0.159	0.072	0.078	0.087	-0.003	0.086	-0.020	-0.033	0.082	0.058	0.046	0.002	-0.008	-0.001	0.028	-0.044	0.023									
boring						-0.028	0.072	0.095	0.017	0.116	-0.033	-0.026	-0.020	-0.183	0.011	0.057	0.087	0.130	0.010	-0.062	0.027	0.078	-0.093	-0.054	-0.023	-0.001	-0.054	0.061	0.013	-0.083									
calm						0.076	0.145	0.052	0.010	0.015	0.183	0.089	0.048	0.017	0.111	0.074	-0.002	-0.078	0.069	0.130	0.139	-0.018	-0.089	0.115	-0.048	-0.112	0.133	-0.133	0.126										
charming						-0.022	0.044	0.027	0.203	0.066	-0.077	0.014	0.090	-0.070	0.123	0.079	-0.001	0.091	0.061	0.040	-0.004	0.108	0.101	0.093	-0.012	0.038	0.004	0.008											
clumsy									-0.019	-0.095	0.100	0.139	0.063	0.074	0.016	0.048	0.034	0.184	-0.012	0.049	0.036	0.261	0.023	0.095	-0.079	0.138	-0.023	0.044	0.025	0.050									
complex									0.038	0.069	0.116	0.071	0.046	-0.066	0.025	0.051	0.225	0.089	0.066	0.116	0.191	0.022	0.142	0.149	0.139	0.058	0.136	0.038	0.023										
delicate											0.066	-0.008	0.002	-0.129	-0.062	0.177	0.102	0.048	0.083	-0.025	-0.010	0.025	0.139	0.033	0.126	-0.104	-0.188	-0.064	-0.106	-0.011									
disorderly											-0.017	0.139	-0.100	0.026	-0.053	0.149	0.070	0.022	-0.023	0.178	0.003	-0.005	0.218	0.036	0.081	0.019	0.095	0.081	0.124										
dramatic											-0.050	0.056	0.047	0.190	0.084	0.037	0.024	0.028	0.152	0.014	0.069	0.064	0.128	0.106	0.126	0.043	0.051	0.041											
formal											0.132	0.029	-0.006	0.051	0.023	0.064	0.040	0.050	-0.098	0.027	0.005 <th>-0.033</th> <th>0.107</th> <th>-0.078</th> <th>0.119</th> <th>0.099</th> <th>0.174</th> <th></th> <th></th> <th></th>	-0.033	0.107	-0.078	0.119	0.099	0.174												
fresh																0.057	-0.039	0.006	0.029	0.049	-0.015	0.075	0.054	0.116	0.118	0.087	0.020	0.160	0.112	0.061									
friendly											0.160	-0.039	0.006	0.029	0.049	0.020	-0.076	-0.039	0.098	-0.167	-0.025	0.046	-0.026	0.075	0.113	0.093	0.024	0.019	0.087	0.085									
gentle											0.088	0.044	-0.028	-0.021	0.027	0.142	0.091	0.061	0.113	-0.046	-0.111	0.038	-0.030	0.038	0.081	0.019	0.095	0.081	0.124										
graceful											0.188	0.012	-0.026	0.028	-0.019	-0.019	0.143	0.011	-0.026	-0.097	-0.014	0.027	-0.054	-0.026	-0.097	-0.014	0.027	-0.054											
happy											-0.066	0.034	0.120	0.100	0.121	0.035	0.016	-0.094	-0.013	-0.069	0.076	-0.032	0.079	-0.092	0.025	0.042	0.145												
legible											0.028	0.003	-0.040	-0.015	-0.040	0.003	-0.040	-0.015	-0.040	0.003	-0.040	-0.015	-0.040	0.003	-0.040	-0.015	-0.040	0.003											
modern											0.035	0.092	0.098	0.025	0.159	0.048	-0.007	-0.066	0.053	0.116	0.064	0.156	0.017	0.106	0.127	0.003	0.001	-0.021	0.020										
playful																0.048	-0.007	-0.066	0.053	0.047	0.066	-0.014	0.047	0.066	0.127	0.003	0.001	-0.021	0.020										
pretentious																-0.008	-0.072	-0.033	0.014	0.035	0.027	0.011	0.120	0.023	0.084	0.011	0.047												
sharp											0.053																												
sloppy																																							
soft																																							
strong																																							
technical																																							
thin																																							
warm																																							
wide																																							

Table 7: Full correlation data for the attributes in Fonts using Crowd-BT. The maximum correlation is between *clumsy* and *pretentious*, shown in bold. Histogram of this data is shown in fig. 1

	artistic	attention-grabbing	attractive	bad	boring	calm	charming	clumsy	complex	delicate	disorderly	dramatic	formal	fresh	friendly	gentle	graceful	happy	legible	modern	playful	pretentious	sharp	sloppy	soft	strong	technical	thin	warm	wide
angular	0.152	-0.007	0.021	0.025	0.007	-0.071	0.069	-0.010	-0.011	-0.058	0.002	0.090	-0.016	-0.061	-0.009	0.079	-0.005	0.047	0.041	-0.005	0.081	-0.083	0.049	-0.044	0.062	-0.031	-0.017	-0.021	0.012	0.079
artistic		-0.021	-0.049	0.025	0.047	-0.087	0.010	0.130	-0.112	-0.102	0.000	0.027	-0.021	-0.010	-0.042	-0.107	0.038	0.069	0.070	-0.080	0.068	-0.012	0.020	0.036	0.039	0.068	0.064	0.017	0.062	0.051
attention-grabbing			0.086	-0.017	0.036	0.041	0.109	0.092	0.057	0.121	0.158	0.043	0.026	0.012	0.037	-0.022	0.082	0.007	-0.040	-0.028	0.098	0.022	-0.027	0.138	0.142	0.090	-0.022	0.036	-0.053	0.112
attractive				0.027	-0.017	-0.100	0.023	0.051	0.096	0.049	0.119	0.061	0.097	0.096	0.056	-0.036	-0.001	0.024	0.048	0.078	-0.039	0.083	-0.046	-0.027	0.118	0.058	0.116	0.054	0.031	-0.028
bad					-0.017	0.108	0.047	0.095	0.062	0.001	0.089	-0.008	0.026	-0.007	-0.007	0.027	0.017	0.079	0.018	0.012	0.012	-0.092	-0.022	0.092	0.015	-0.033	0.048	-0.001	0.045	0.106
boring						-0.100	-0.034	0.053	0.103	0.067	0.036	0.029	0.042	0.038	-0.066	0.048	0.078	0.048	0.089	-0.040	0.161	-0.016	0.111	-0.004	0.050	0.069	0.019	0.019	0.043	-0.062
calm							0.023	-0.068	-0.000	-0.028	0.115	0.002	0.102	0.090	0.201	-0.005	0.007	0.069	-0.120	-0.006	0.080	0.005	0.005	0.007	0.007	-0.017	-0.084	-0.003	-0.035	0.033
charming								0.051	-0.017	-0.000	0.174	0.074	-0.074	0.075	0.021	-0.033	0.121	0.112	0.012	0.013	0.088	0.027	-0.024	0.006	0.167	0.049	-0.075	-0.060	0.052	0.068
clumsy									0.096	-0.073	0.044	-0.060	-0.020	0.068	-0.023	-0.042	0.072	-0.111	0.068	0.000	0.016	0.008	-0.123	0.039	0.032	0.092	0.042	0.022	-0.021	0.108
complex										0.049	0.070	0.123	-0.060	0.091	-0.043	-0.100	0.101	-0.056	0.010	-0.056	0.114	0.073	0.134	0.060	-0.008	-0.016	0.016	0.010	0.014	0.207
delicate											0.119	0.112	-0.046	-0.024	-0.033	-0.041	0.152	0.013	0.101	0.062	0.034	0.029	0.023	0.056	0.058	-0.026	-0.069	0.005	-0.026	-0.005
disorderly												0.061	0.080	-0.022	-0.024	-0.016	0.065	-0.041	0.023	0.049	0.047	-0.019	-0.028	0.146	-0.019	-0.016	-0.035	0.099	-0.006	0.134
dramatic													0.097	-0.006	0.002	0.050	0.037	0.046	0.089	0.106	-0.007	-0.019	0.008	0.067	0.147	0.022	0.013	0.110	0.037	0.014
formal														0.096	-0.135	0.021	-0.050	0.052	-0.006	0.034	-0.042	0.054	0.047	0.018	0.022	0.003	-0.005	0.096	0.017	0.022
fresh															0.056	0.008	-0.093	-0.044	-0.034	0.095	0.005	0.013	0.009	-0.068	0.020	-0.003	-0.006	0.016	-0.000	0.062
friendly																-0.036	0.004	0.027	0.025	-0.007	0.115	0.140	0.021	-0.042	0.008	-0.010	0.071	0.082	0.036	0.094
gentle																	-0.001	0.049	0.100	-0.066	0.019	0.068	-0.038	0.051	0.075	0.004	0.008	0.012	-0.079	0.095
graceful																		0.024	0.130	-0.004	0.107	0.005	-0.026	0.100	0.119	0.091	-0.090	0.061	0.053	-0.009
happy																			0.048	0.126	0.159	0.105	-0.026	0.089	0.093	0.097	0.147	0.034	0.008	0.041
legible																				0.078	0.036	0.013	-0.068	-0.062	0.136	0.017	0.026	0.026	0.088	0.064
modern																					-0.039	0.093	-0.065	-0.029	0.006	-0.024	-0.023	0.091	-0.006	-0.002
playful																						0.083	0.035	0.058	-0.033	0.058	0.018	0.093	0.081	0.066
pretentious																							-0.046	0.115	-0.078	0.029	-0.027	0.076	0.059	-0.017
sharp																								-0.027	-0.076	0.050	-0.005	-0.041	0.027	0.027
sloppy																									0.118	0.102	0.015	0.076	-0.029	-0.048
soft																										0.058	-0.049	0.105	0.021	-0.034
strong																											0.116	0.034	0.015	-0.014
technical																												0.054	-0.034	0.035
thin																													0.031	-0.073
warm																														-0.028

Table 8: Full correlation data for the attributes in Fonts using O'Donovan *et al.*'s method. The maximum correlation is between *complex* and *wide*, shown in bold.. Histogram of this data is shown in fig. 2

number of indifferent or adversarial judges changes that decision point.

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- [2] Sir Harold Jeffreys. 1961. *The Theory of Probability*. https://books-google-com.ezproxy.lib.utexas.edu/books/about/The_Theory_of_Probability.html?id=vh9Act9rtzQC

Pair Count	BTL		Crowd-BT		O'Donovan	
	μ_τ	σ_τ	μ_τ	σ_τ	μ_τ	σ_τ
200	0.159	6.388e-2	0.402	6.738e-2	0.326	4.386e-2
300	0.618	3.152e-2	0.630	2.386e-2	0.592	3.982e-2
400	0.712	2.189e-2	0.684	3.075e-2	0.699	2.416e-2
500	0.756	1.682e-2	0.735	3.000e-2	0.750	1.817e-2
600	0.786	1.714e-2	0.795	2.644e-2	0.782	1.746e-2
700	0.809	1.234e-2	0.838	1.766e-2	0.805	1.261e-2
800	0.822	1.071e-2	0.870	1.397e-2	0.819	1.147e-2
900	0.838	9.585e-3	0.887	1.640e-2	0.835	9.458e-3
1000	0.845	1.032e-2	0.904	1.553e-2	0.843	1.152e-2
1500	0.876	5.108e-3	0.941	6.072e-3	0.875	5.897e-3
2000	0.897	5.554e-3	0.954	4.039e-3	0.896	5.649e-3
2500	0.907	5.853e-3	0.962	3.220e-3	0.906	5.728e-3
3000	0.915	5.695e-3	0.968	2.432e-3	0.914	6.206e-3
3500	0.922	3.628e-3	0.970	1.555e-3	0.922	3.708e-3
4000	0.929	4.014e-3	0.973	2.040e-3	0.928	4.288e-3
4500	0.933	3.970e-3	0.976	2.003e-3	0.933	3.996e-3
5000	0.937	4.250e-3	0.977	1.628e-3	0.936	4.467e-3
5500	0.939	3.941e-3	0.979	1.286e-3	0.939	3.883e-3
6000	0.942	3.622e-3	0.980	1.447e-3	0.942	3.605e-3
6500	0.945	3.604e-3	0.981	1.268e-3	0.944	3.800e-3
7000	0.947	4.153e-3	0.982	1.226e-3	0.947	3.987e-3
7500	0.950	3.717e-3	0.983	1.432e-3	0.949	3.381e-3
8000	0.951	3.153e-3	0.984	1.229e-3	0.950	3.214e-3
8500	0.952	2.894e-3	0.984	1.124e-3	0.951	2.890e-3
9000	0.955	2.621e-3	0.985	1.201e-3	0.954	2.763e-3
9500	0.956	3.200e-3	0.986	1.308e-3	0.955	3.240e-3
10000	0.957	2.699e-3	0.986	1.156e-3	0.957	2.574e-3
10500	0.958	1.959e-3	0.986	9.190e-4	0.958	2.110e-3
11000	0.958	3.148e-3	0.987	1.362e-3	0.957	2.964e-3
11500	0.960	2.672e-3	0.987	1.126e-3	0.960	2.619e-3
12000	0.961	2.428e-3	0.988	1.164e-3	0.960	2.653e-3
12500	0.961	1.848e-3	0.988	1.200e-3	0.960	1.873e-3
13000	0.962	2.817e-3	0.988	1.141e-3	0.962	2.986e-3
13500	0.964	2.251e-3	0.989	8.040e-4	0.963	2.193e-3
14000	0.964	1.980e-3	0.989	9.820e-4	0.963	1.904e-3
14500	0.964	1.805e-3	0.989	7.530e-4	0.964	1.918e-3
15000	0.966	1.915e-3	0.990	9.960e-4	0.965	1.999e-3
15500	0.966	1.680e-3	0.989	9.980e-4	0.966	1.758e-3
16000	0.967	1.998e-3	0.990	1.126e-3	0.966	2.124e-3
16500	0.967	2.682e-3	0.990	8.210e-4	0.966	2.692e-3
17000	0.967	2.318e-3	0.991	7.880e-4	0.967	2.306e-3
17500	0.968	2.357e-3	0.991	1.009e-3	0.968	2.391e-3
18000	0.969	2.356e-3	0.991	1.000e-3	0.968	2.238e-3
18500	0.969	2.739e-3	0.991	7.680e-4	0.969	2.808e-3
19000	0.970	1.829e-3	0.991	1.104e-3	0.969	1.894e-3
19500	0.971	1.995e-3	0.991	9.350e-4	0.970	1.906e-3
19900	0.971	2.037e-3	0.991	9.620e-4	0.970	2.207e-3

Table 9: Mean τ , μ_τ , and standard deviation, σ_τ , for the simulated data with 8 judges per pair, $\omega = 0.02$, and $\lambda = 0$.

Pair Count	BTL		Crowd-BT		O'Donovan	
	μ_τ	σ_τ	μ_τ	σ_τ	μ_τ	σ_τ
200	0.282	6.349e-2	0.402	6.738e-2	0.606	2.404e-2
300	0.626	2.331e-2	0.630	2.386e-2	0.681	2.446e-2
400	0.681	2.946e-2	0.684	3.075e-2	0.727	2.403e-2
500	0.741	2.870e-2	0.735	3.000e-2	0.765	1.850e-2
600	0.802	2.443e-2	0.795	2.644e-2	0.808	1.618e-2
700	0.843	1.761e-2	0.838	1.766e-2	0.842	1.732e-2
800	0.873	1.406e-2	0.870	1.397e-2	0.870	1.386e-2
900	0.890	1.510e-2	0.887	1.640e-2	0.889	1.358e-2
1000	0.907	1.367e-2	0.904	1.553e-2	0.905	1.343e-2
1500	0.942	6.226e-3	0.941	6.072e-3	0.940	6.366e-3
2000	0.954	3.868e-3	0.954	4.039e-3	0.953	3.996e-3
2500	0.962	3.301e-3	0.962	3.220e-3	0.961	3.522e-3
3000	0.968	2.553e-3	0.968	2.432e-3	0.967	2.297e-3
3500	0.970	1.604e-3	0.970	1.555e-3	0.970	1.908e-3
4000	0.973	2.049e-3	0.973	2.040e-3	0.972	2.349e-3
4500	0.976	2.032e-3	0.976	2.003e-3	0.975	1.936e-3
5000	0.977	1.625e-3	0.977	1.628e-3	0.976	1.365e-3
5500	0.979	1.261e-3	0.979	1.286e-3	0.978	1.568e-3
6000	0.980	1.486e-3	0.980	1.447e-3	0.979	1.630e-3
6500	0.981	1.258e-3	0.981	1.268e-3	0.980	1.302e-3
7000	0.982	1.176e-3	0.982	1.226e-3	0.981	1.400e-3
7500	0.983	1.383e-3	0.983	1.432e-3	0.982	1.226e-3
8000	0.984	1.277e-3	0.984	1.229e-3	0.983	1.286e-3
8500	0.984	1.211e-3	0.984	1.124e-3	0.984	1.156e-3
9000	0.985	1.255e-3	0.985	1.201e-3	0.985	1.101e-3
9500	0.986	1.284e-3	0.986	1.308e-3	0.985	1.225e-3
10000	0.986	1.124e-3	0.986	1.156e-3	0.986	1.075e-3
10500	0.986	9.010e-4	0.986	9.190e-4	0.986	9.450e-4
11000	0.987	1.346e-3	0.987	1.362e-3	0.986	1.245e-3
11500	0.987	1.104e-3	0.987	1.126e-3	0.987	1.168e-3
12000	0.988	1.201e-3	0.988	1.164e-3	0.988	1.171e-3
12500	0.988	1.248e-3	0.988	1.200e-3	0.988	1.175e-3
13000	0.988	1.060e-3	0.988	1.141e-3	0.988	1.291e-3
13500	0.989	8.260e-4	0.989	8.040e-4	0.988	1.037e-3
14000	0.989	9.140e-4	0.989	9.820e-4	0.988	1.022e-3
14500	0.989	7.530e-4	0.989	7.530e-4	0.989	9.090e-4
15000	0.990	9.540e-4	0.990	9.960e-4	0.989	8.090e-4
15500	0.990	9.980e-4	0.989	9.980e-4	0.989	9.160e-4
16000	0.990	1.079e-3	0.990	1.126e-3	0.990	1.005e-3
16500	0.990	7.200e-4	0.990	8.210e-4	0.990	9.230e-4
17000	0.991	8.070e-4	0.991	7.880e-4	0.990	8.530e-4
17500	0.991	9.970e-4	0.991	1.009e-3	0.990	8.880e-4
18000	0.991	1.000e-3	0.991	1.000e-3	0.990	9.200e-4
18500	0.991	8.640e-4	0.991	7.680e-4	0.991	7.240e-4
19000	0.991	9.870e-4	0.991	1.104e-3	0.991	1.257e-3
19500	0.991	9.400e-4	0.991	9.350e-4	0.991	8.430e-4
19900	0.991	9.840e-4	0.991	9.620e-4	0.991	9.850e-4

Table 10: Mean τ , μ_τ , and standard deviation, σ_τ , for the simulated data with 8 judges per pair, $\omega = 0.1$, and $\lambda = 0$.

Pair Count	Crowd-BT - BTL			O'Donovan - BTL		
	μ_τ	σ_τ	$\log(\text{BF}_{10})$	μ_τ	σ_τ	$\log(\text{BF}_{10})$
200	5.664e-2	5.745e-2	7.823	1.671e-1	0.068458	25.437
300	-3.695e-2	2.123e-2	17.792	-2.567e-2	0.022218	10.178
400	-2.775e-2	2.007e-2	13.264	-1.348e-2	0.014034	7.464
500	-1.403e-2	1.426e-2	7.792	-6.184e-3	0.005163	10.761
600	-7.377e-3	6.312e-3	10.362	-4.134e-3	0.003772	9.353
700	-5.236e-3	3.542e-3	14.512	-3.568e-3	0.003370	8.834
800	-3.869e-3	3.730e-3	8.537	-3.307e-3	0.003269	8.179
900	-3.598e-3	3.638e-3	7.865	-3.022e-3	0.003212	7.194
1000	-3.447e-3	3.118e-3	9.487	-1.933e-3	0.003129	2.863
1500	-1.534e-3	2.472e-3	2.898	-1.558e-3	0.002241	3.849
2000	-1.588e-3	1.280e-3	11.353	-1.702e-3	0.001675	8.239
2500	-1.146e-3	1.475e-3	4.937	-1.102e-3	0.001742	3.051
3000	-7.600e-4	1.342e-3	2.240	-9.410e-4	0.001692	2.115
3500	-4.590e-4	1.227e-3	0.186	-6.260e-4	0.001114	2.189
4000	-5.960e-4	1.034e-3	2.357	-5.860e-4	0.001362	0.729
4500	-6.570e-4	1.100e-3	2.604	-5.660e-4	0.001164	1.318
5000	-7.810e-4	1.252e-3	2.933	-5.860e-4	0.001199	1.349
5500	-1.340e-4	8.270e-4	-1.277	-6.630e-4	0.000971	3.697
6000	-5.530e-4	1.145e-3	1.279	-5.800e-4	0.001073	1.926
6500	-5.090e-4	9.390e-4	1.953	-1.092e-3	0.001005	9.232
7000	-6.430e-4	1.079e-3	2.593	-6.230e-4	0.000973	3.149
7500	-2.510e-4	1.030e-3	-0.832	-5.090e-4	0.001258	0.474
8000	-3.920e-4	8.940e-4	0.810	-6.670e-4	0.000964	3.806
8500	-4.360e-4	8.620e-4	1.525	-5.190e-4	0.001043	1.444
9000	-6.200e-4	7.800e-4	5.179	-9.250e-4	0.000905	8.316
9500	-1.070e-4	9.220e-4	-1.451	-5.160e-4	0.001106	1.103
10000	-4.190e-4	7.510e-4	2.129	-3.520e-4	0.000853	0.548
10500	-3.920e-4	1.051e-3	0.175	-6.100e-4	0.000972	2.986
11000	-3.580e-4	8.270e-4	0.759	-4.960e-4	0.000758	3.325
11500	-3.580e-4	5.690e-4	3.016	-5.460e-4	0.000914	2.613
12000	-2.910e-4	8.060e-4	0.072	-6.030e-4	0.001161	1.689
12500	-3.690e-4	8.140e-4	0.955	-7.470e-4	0.000795	7.182
13000	-2.980e-4	6.910e-4	0.739	-5.700e-4	0.001045	1.983
13500	-2.750e-4	7.670e-4	0.043	-5.860e-4	0.000686	6.002
14000	-1.570e-4	7.370e-4	-1.017	-6.130e-4	0.000788	4.959
14500	-2.950e-4	6.710e-4	0.817	-8.780e-4	0.000850	8.467
15000	-1.680e-4	7.190e-4	-0.902	-4.020e-4	0.000755	1.834
15500	-1.410e-4	7.090e-4	-1.100	-3.580e-4	0.000760	1.157
16000	-3.520e-4	7.670e-4	1.019	-7.970e-4	0.000813	7.741
16500	-5.400e-5	8.290e-4	-1.580	-4.090e-4	0.000949	0.729
17000	-2.000e-5	5.760e-4	-1.621	-3.180e-4	0.000654	1.321
17500	-1.980e-4	5.680e-4	-0.044	-3.220e-4	0.000834	0.294
18000	-3.220e-4	8.510e-4	0.219	-6.730e-4	0.000770	6.280
18500	-2.550e-4	7.450e-4	-0.098	-5.590e-4	0.000825	3.627
19000	-2.580e-4	6.070e-4	0.674	-6.030e-4	0.000731	5.591
19500	-2.080e-4	5.980e-4	-0.054	-4.760e-4	0.000931	1.590
19900	-3.950e-4	6.700e-4	2.523	-6.300e-4	0.000557	9.827

Table 11: Statistical comparison between the two experimental methods, Crowd-BT and O'Donovan *et al.*'s method, and the unweighted BTL order on a matched pair basis for the simulated data with 8 judges per pair, $\omega = 0.02$, and $\lambda = 0$. A positive value of μ_τ indicates that the experimental method is *better*. We show the mean and standard deviation along with a Bayesian Paired Samples T-Test, computed using JASP 0.16 [1]. We use Student-T where $H_a : \tau_{\text{experimental}} \neq \tau_{\text{BTL}}$ and the prior is Cauchy with scale 0.707. Values of $\log(\text{BF}_{10})$ are traditionally interpreted using the scale provided by Jeffreys [2]; we highlight values above 1.5 in bold, which are generally regarded as having strong evidence.

Pair Count	Crowd-BT - BTL			O'Donovan - BTL		
	μ_τ	σ_τ	$\log(\text{BF}_{10})$	μ_τ	σ_τ	$\log(\text{BF}_{10})$
200	1.202e-1	8.178e-2	14.405	3.240e-1	6.826e-2	42.488
300	4.429e-3	8.860e-3	1.467	5.543e-2	3.383e-2	16.550
400	2.593e-3	1.875e-2	-1.374	4.566e-2	3.443e-2	12.505
500	-5.853e-3	1.776e-2	-0.202	2.461e-2	2.906e-2	5.894
600	-6.697e-3	1.608e-2	0.588	6.533e-3	1.610e-2	0.483
700	-5.079e-3	6.025e-3	5.839	-7.140e-4	7.468e-3	-1.511
800	-2.945e-3	3.559e-3	5.624	-2.228e-3	4.498e-3	1.416
900	-3.712e-3	3.830e-3	7.587	-1.648e-3	4.042e-3	0.504
1000	-2.647e-3	4.127e-3	3.159	-2.054e-3	3.699e-3	2.102
1500	-6.767e-4	1.070e-3	3.046	-1.776e-3	1.707e-3	8.577
2000	-3.451e-4	8.680e-4	0.405	-1.236e-3	1.246e-3	7.909
2500	-2.044e-4	6.220e-4	-0.211	-9.580e-4	1.136e-3	5.847
3000	-9.045e-5	4.900e-4	-1.171	-9.310e-4	1.202e-3	4.913
3500	-8.710e-5	4.810e-4	-1.189	-4.760e-4	9.970e-4	1.218
4000	-1.709e-4	4.690e-4	0.100	-9.950e-4	1.081e-3	6.910
4500	4.020e-5	3.290e-4	-1.432	-8.210e-4	8.190e-4	8.054
5000	-1.005e-4	4.030e-4	-0.797	-7.770e-4	8.490e-4	6.845
5500	1.480e-17	4.180e-4	-1.638	-7.840e-4	6.790e-4	10.171
6000	-1.206e-4	2.800e-4	0.734	-8.740e-4	7.270e-4	10.825
6500	-1.575e-4	3.050e-4	1.648	-8.140e-4	7.640e-4	8.927
7000	-1.240e-4	3.370e-4	0.132	-7.600e-4	6.590e-4	10.155
7500	-2.680e-5	3.390e-4	-1.551	-3.250e-4	7.120e-4	0.993
8000	3.685e-5	2.320e-4	-1.292	-5.260e-4	7.830e-4	3.544
8500	-1.273e-4	2.530e-4	1.503	-6.060e-4	6.720e-4	6.665
9000	1.005e-5	3.090e-4	-1.623	-3.820e-4	6.880e-4	2.097
9500	-3.015e-5	2.820e-4	-1.480	-4.590e-4	5.920e-4	4.910
10000	-1.005e-4	2.990e-4	-0.144	-5.830e-4	5.590e-4	8.617
10500	-6.030e-5	3.150e-4	-1.137	-6.700e-4	5.680e-4	10.526
11000	1.110e-17	2.790e-4	-1.638	-4.760e-4	7.090e-4	3.535
11500	-9.380e-5	2.990e-4	-0.327	-2.910e-4	6.490e-4	0.921
12000	6.700e-6	2.470e-4	-1.628	-2.040e-4	5.730e-4	0.029
12500	-1.005e-4	2.420e-4	0.579	-4.790e-4	6.710e-4	4.102
13000	-1.206e-4	2.660e-4	0.969	-6.400e-4	6.230e-4	8.391
13500	-6.365e-5	2.890e-4	-0.976	-4.150e-4	6.270e-4	3.426
14000	-4.020e-5	2.850e-4	-1.363	-3.220e-4	5.760e-4	2.139
14500	-7.401e-18	2.090e-4	-1.638	-5.560e-4	6.020e-4	6.950
15000	9.380e-5	2.790e-4	-0.149	-4.050e-4	3.710e-4	9.312
15500	-1.005e-4	2.490e-4	0.463	-4.660e-4	5.730e-4	5.422
16000	2.345e-5	2.140e-4	-1.471	-4.190e-4	5.320e-4	5.079
16500	-2.680e-5	2.400e-4	-1.466	-4.860e-4	5.080e-4	7.396
17000	2.680e-5	2.360e-4	-1.459	-3.350e-4	6.890e-4	1.317
17500	6.700e-5	3.040e-4	-0.976	-4.050e-4	5.060e-4	5.267
18000	-4.355e-5	2.340e-4	-1.164	-4.860e-4	4.930e-4	7.809
18500	2.345e-5	2.970e-4	-1.551	-2.610e-4	4.370e-4	2.625
19000	-3.350e-5	2.980e-4	-1.463	-4.720e-4	5.080e-4	7.045
19500	-6.030e-5	2.260e-4	-0.684	-2.480e-4	3.880e-4	3.135
19900	1.005e-5	2.660e-4	-1.618	-3.790e-4	5.460e-4	3.820

Table 12: Statistical comparison between the two experimental methods, Crowd-BT and O'Donovan *et al.*'s method, and the unweighted BTL order on a matched pair basis for the simulated data with 8 judges per pair, $\omega = 0.1$, and $\lambda = 0$. A positive value of μ_τ indicates that the experimental method is *better*. We show the mean, the standard deviation, and a Bayesian Paired Samples T-Test, computed using JASP 0.16 [1]. We use Student-T where $H_a : \tau_{\text{experimental}} \neq \tau_{\text{BTL}}$ and the prior is Cauchy with scale 0.707. Values of $\log(\text{BF}_{10})$ are traditionally interpreted using the scale provided by Jeffreys [2]; we highlight values above 1.5 in bold, which are generally regarded as having strong evidence.