AP Calculus – Worksheet – 7.4 – Lengths of Curves

Find the length of each curve **analytically**. Intervals are in terms of the equation.

1.
$$y = \frac{1}{2}x$$
 from [1,5]

2.
$$y = x^{\frac{3}{2}}$$
 from $\left[\frac{4}{3}, 5\right]$

3.
$$y = \frac{x^3}{6} + \frac{1}{2x}$$
 from $\left[\frac{1}{2}, 2\right]$

4.
$$y = x^{\frac{2}{3}} + 1$$
 from $[0,8]$

5.
$$x = (y-1)^{\frac{3}{2}}$$
 from [1,5]

6.
$$x = \frac{y^4}{8} + \frac{1}{4y^2}$$
 from $[-2, -1]$

7.
$$x = \ln(\cos y)$$
 from $\left[0, \frac{\pi}{3}\right]$

8. $x = y^2 - \frac{1}{8} \ln y$ from [1,3]

Setup the integral and find the length of the arc by any method.

9.
$$y = 2^x$$
 from [0,3]

10.
$$x = y + y^3$$
 from [1,4]

11.
$$y = xe^{-x}$$
 from $[0,5]$

12.
$$x = y + \sqrt{y}$$
 from [1,2]