

5.1 R_{ZYX} (vgl. cg03-part3.pdf)

$$\begin{aligned} 0,5 &= -\sin \theta \Rightarrow \theta = -30^\circ \\ \frac{0,433}{0,75} &= \tan \psi \Rightarrow \psi = 30^\circ \\ \frac{0,433}{0,75} &= \tan \phi \Rightarrow \phi = 30^\circ \end{aligned}$$

$$R_{ZYX} = R_Z(\phi) R_Y(\psi) R_X(\theta)$$

$$\begin{aligned} &= \begin{pmatrix} \cos \phi & -\sin \phi & 0 \\ \sin \phi & \cos \phi & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \cos \psi & 0 & \sin \psi \\ 0 & 1 & 0 \\ -\sin \psi & 0 & \cos \psi \end{pmatrix} \begin{pmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{pmatrix} \\ &= \begin{pmatrix} \lambda & 0 & -\lambda^3 \\ 0 & -1 & 0 \\ -\lambda^2 & 0 & -\lambda^2 \end{pmatrix} \quad \lambda = \frac{\sqrt{2}}{2} \end{aligned}$$

$$^1 \cos \psi = -\lambda \Rightarrow \psi = 135^\circ$$

$$^2 -\sin \psi \cos \theta = -\lambda \xRightarrow{\sin \psi = \frac{1}{\sqrt{2}}} \cos \theta = 0,5 \Rightarrow \theta = 60^\circ$$

$$^3 \cos \phi \sin \psi = -\lambda \Rightarrow \cos \phi = -0,5 \Rightarrow \phi = 120^\circ$$