Section 1.1

We motivate the following discussion by noting that the syntax of a program in a language is usually a nested or tree like structure. Recursion is then an important technique in constructing and manipulating such structures.

Inductive specification is a method for specifying a set of values. For example, let's consider a set $S \subseteq \mathbb{N}$. We can define S as follows:

Definition 1. A natural number $n \in S$ if and only if

1.
$$n = 0$$
, or

2.
$$n-3 \in S$$
.

We call this definition the top down definition of S

Definition 2. Define the set S to be the smallest set contained in \mathbb{N} and satisfying the following two properties:

1.
$$0 \in S$$
, and

2. if
$$n \in S$$
, then $(n+3) \in S$.

We call this definition the **bottom up definition** of S

Definition 3.

$$\frac{0 \in S}{n \in S}$$

$$\frac{n \in S}{(n+3) \in S}$$

We call this definition the rules of inference of S