

State and Property

↓
Intensive
(size doesn't matter).

↓
Extensive
(size matters)

Mostly used → Pressure (P), Volume (V), Temperature (T), Entropy, Enthalpy, Internal energy.

④ Three forms of - internal Energy :

Intermolecular potential energy (Between molecules).

Molecular kinetic energy (translational and rotational velocity of each molecules).

Intra-molecular energy (within molecular/atomic structures).

④ Enthalpy → combination of internal and pressure energy of the fluid. $H = U + pV$ (extensive) | SI → kJ/kg.
 $h = U + pr$. (intensive)

func
of
temp

④ Entropy → molecular disorder / randomness.

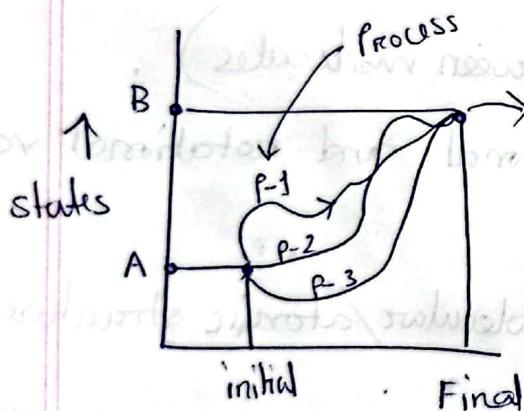
④ State → condition of a system ;
 depends on properties → if even one property changes state changes.

Equilibrium: no unbalanced potentials.

thermodynamic equilibrium requirements ↴

- ① Thermal Equilibrium → NO HEAT FLOW,
- ② Mechanical " → No unbalanced forces acting.
- ③ Chemical " → No change in chemical composition

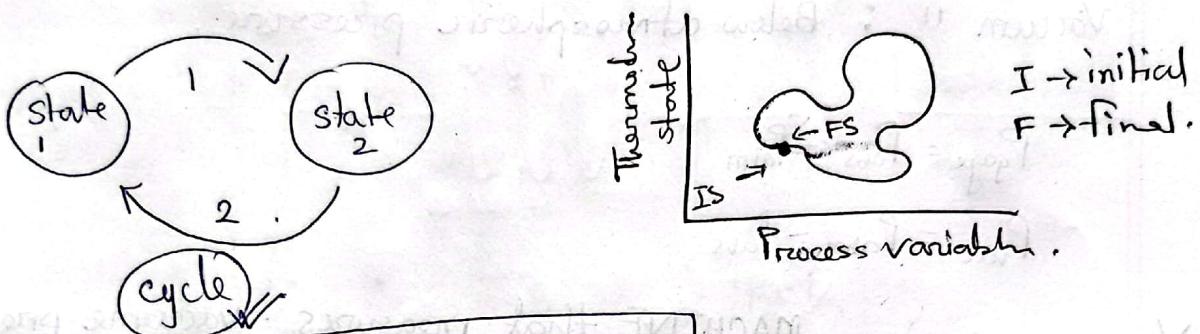
- ④ Process → thermodynamic states — from initial state to final
- ⑤ Path → series of states during a process.



Path & Process :

- ① Isothermal (T)
- ② Isobaric (P)
- ③ Isochoric (V)
- ④ Isentropic (S)
- ⑤ Isenthalpic (Δh)
- ⑥ Isosteric (concentration)
- ⑦ Adiabatic (no heat gain or removal)

Cycle or Cyclic process: Process that return the system to the initial state. (Zero change of any property)
Initial state same as Final state.



Quasi-static or Quasi-equilibrium

deviation from thermodynamic equilibrium is infinitesimal

slow process that allows the system to adjust itself internally so that properties in one part changes not faster than others.

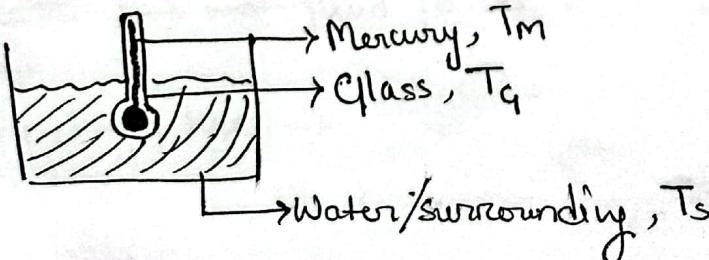
CS → Non flow process.

OS → flow process

Zeroth law:

→ Basis of Temperature Measurement,

if $T_1 = T_2$ and $T_2 = T_3$ then $Q_3 = 0$.



If $T_s = T_g$ and $T_g = T_m$ then, $T_m = T_s$.

Formula

$$P_{atm} = P_{abs} + P_{vac}$$

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Absolute pressure : actual pressure

Gage " : Diff between absolute pressure and the local atmospheric pressure.

Vacuum " : Below atmospheric pressure.

$$P_{gage} = P_{abs} - P_{atm}$$

$$P_{vac} = P_{atm} - P_{abs}$$

Vacuum gage is a MACHINE that measures vacuum pressure.

MATH: Atmospheric pressure measured by a vacuum gage is 5.8 psi where atm pressure is 14.5 psi. So what is the absolute pressure.

$$\text{Here, } P_{vac} = 5.8 \text{ psi}$$

$$P_{atm} = 14.5 \text{ psi}$$

$$\text{So, } P_{abs} = P_{atm} - P_{vac}$$

$$= 14.5 - 5.8$$

$$= 8.7 \text{ psi}$$

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$$E = U + KE + PE$$

1st Law for Closed System $\rightarrow \oint \delta Q = \oint \delta W$

For non-cyclic process $\rightarrow Q - W = \Delta E$

Heat transfer $\rightarrow Q = U_2 - U_1 = mC_v(T_2 - T_1)$ [const - V]

~~Q = m C_p (T_2 - T_1)~~ [Const - P]

$$\boxed{C_p - C_v = R}$$

$$C_v = \frac{R}{k-1}$$

$$C_p = \frac{kR}{k-1}$$

Gas Laws: $\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$

$$\frac{P_2}{P_1} = \left(\frac{V_1}{V_2}\right)^r$$

$$\frac{T_2}{T_1} = \left(\frac{V_1}{V_2}\right)^{r-1} = \left(\frac{P_2}{P_1}\right)^{\frac{r-1}{r}}$$

$$PV = mRT$$

$$P = \frac{m}{V} RT = PRT$$

~~Turbine~~ \rightarrow low pressured fluid $\xrightarrow{\text{compress}} \rightarrow$ high pressure

~~Rotary Compressor~~ \rightarrow high pressured fluid $\xrightarrow{\text{expand}} \rightarrow$ low pressure

Nozzle \rightarrow duct where velocity rises, pressure drops.

Diffuser \rightarrow " " " drops, " rises.

Heat exchanger \rightarrow transfers heat from one fluid to another without work done

Throttling \rightarrow fluid passes a pore and pressure drops.

Heat exchanger types \rightarrow radiator (automobile), condenser (steam power + refrigeration), evaporator (refrigerator).

Sub:

1st law of Thermodynamics

Law of nature

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3 types of Energy: -

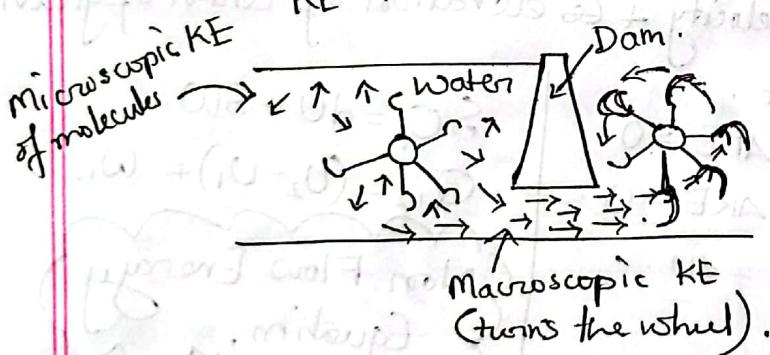
- External Kinetic (KE) — associated with motion
- Potential (PE) — " " a mass that's in
- Internal (U) — sum of all the molecules' rest energy of a system.

$$\text{So, } E = \text{External} + \text{Internal}$$

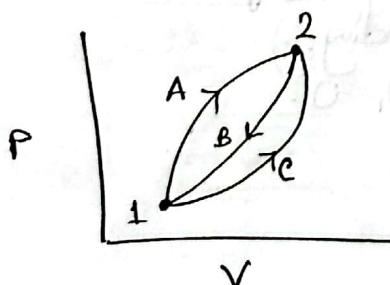
$$\text{or, } E = (KE + PE) + U$$

Statement (1st TD) :- Energy can neither be created nor destroyed, though it can be transformed from one form to another.

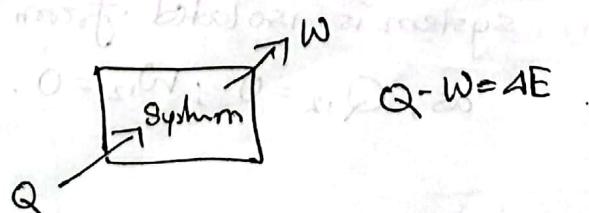
NOTE: KE of an object → organized + orderly (direction straight)
KE of molecules → disorganized + random.



1st TD in closed system : $\oint \delta Q = \oint \delta W$. [Joule's experiment]



cyclic process



non-cyclic process

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Closed System (non cyclic) (1st TD law)

$$E = U + KE + PE$$

$$\Rightarrow dE = dU + dKE + dPE$$

$$\Rightarrow (SQ - SW) = dU + dKE + dPE$$

$$\text{Now, } dU \Rightarrow \int_1^2 dU = U_2 - U_1 = m(U_2 - U_1)$$

$$d(KE) = mVdV \Rightarrow \int_1^2 d(KE) = \frac{1}{2}m(V_2^2 - V_1^2)$$

$$d(PE) = mgdZ \Rightarrow \int_1^2 d(PE) = mg(Z_2 - Z_1) = mgh$$

$$Q_{12} - W_{12} = [(U_2 - U_1) + \frac{1}{2}m(V_2^2 - V_1^2) + mg(Z_2 - Z_1)]$$

$$q_{12} - w_{12} = [(U_2 - U_1) + \frac{1}{2}(V_2^2 - V_1^2) + g(Z_2 - Z_1)]$$

Stationary system \rightarrow velocity + acceleration of center of gravity

is constant.

$$\text{So, } z_1 = z_2 \rightarrow \Delta PE = 0$$

$$v_1 = v_2 \rightarrow \Delta KE = 0$$

$$\text{So, } \Delta E = \Delta U$$

$$SQ = dU + SW$$

$$Q_{12} = (U_2 - U_1) + W_{12}$$

Non Flow Energy
Equation.

* Law of conservation of energy \rightarrow U is unchanged when the system is isolated from surroundings.

$$\text{as, } Q_{12} = 0; W_{12} = 0; \therefore U_2 - U_1 = 0.$$

Sub :

PMM-I

2nd TD तिर्यक बोर्ड PMM-II.

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④ Perpetual Motion Machine → that do not follow 1st Law of TD.
 ↗ (It's imaginary).

Application of Non-flow process.

Polytropic process $(pV^n) = \text{constant}$

$$Q_{12} = U_2 - U_1 + W_{12}$$

$$= U_2 - U_1 + \frac{P_1 V_1 - P_2 V_2}{n-1}$$

$$\text{So, } Q = \frac{mR(T_2 - T_1)}{n-1} + mC_v(T_2 - T_1)$$

④ Specific Heat : C (Heat capacity).

Amount of heat that raise temp by 1° per unit mass.

δQ → amount of heat

$$C = \left(\frac{1}{m}\right) \left(\frac{\delta Q}{\delta T}\right)$$

δT → temp.

m → mass (kg).

At Constant- V , C_V

$$\delta W = PdV = 0 \quad [\because dV = 0]$$

$$\therefore \delta Q = \delta U + \delta W = \delta U$$

$$\text{So, } C_V = \frac{1}{m} \cdot \left(\frac{dU}{dT}\right)_V$$

$$\Rightarrow \boxed{dU = m C_V dT}$$

ISOTHERMIC.

At const. P , C_P

$$\delta Q = dU + PdV$$

$$= (U_2 - U_1) + P(V_2 - V_1)$$

$$= (U_2 + P V_2) - (U_1 + P V_1)$$

$$= H_2 - H_1 \quad \therefore H = U + PV$$

$$\delta Q = dH$$

$$C_P = \frac{1}{m} \cdot \left(\frac{dH}{dT}\right)_P$$

$$\text{So, } \boxed{\delta Q = dH = m C_P dT}$$

ISOBARIC.

SPECIFIC HEAT RATIO: $\gamma = \frac{C_p}{C_v}$

$$C_p - C_v = R$$

$$C_v = \frac{R}{k-1}$$

$$C_p = \frac{kR}{k-1}$$

$$R \rightarrow 8.314 \text{ J K}^{-1} \text{ mol}^{-1}$$

universal gas const.

GAS LAWS:

$$(P_1 V_1)/T_1 = (P_2 V_2)/T_2$$

$$\Rightarrow P_1 V_1^n = P_2 V_2^n$$

For adiabatic $[\Phi=0]$ + frictionless - isentropic process.

$$n = \gamma = 1.4$$

$$\text{So, } P_1 V_1^\gamma = P_2 V_2^\gamma$$

$$R/P_1 = V_1/V_2$$

$$\frac{P_2}{P_1} = \left(\frac{V_1}{V_2}\right)^\gamma$$

$$\frac{T_2}{T_1} = \left(\frac{V_1}{V_2}\right)^{\gamma-1}$$

$$\frac{T_2}{T_1} = \left(\frac{P_2}{P_1}\right)^{\frac{\gamma-1}{\gamma}}$$

$$PV = mRT$$

$$P = \rho RT$$

$$\frac{H_b}{T_b} = q_1$$

$$(q_1)_{\text{m}} = H_b = \rho d$$

$$[0 = Vb] \Rightarrow 0 = Vb = w_2$$

$$Vb = w_2 + U_2 - P_2 V$$

$$\frac{(U_2)}{m} = \frac{1}{m} = \frac{1}{m} = Vb$$

$$1.5 Vb/m = U_2$$

DIAHEDAL

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✓ ISOTHERMAL

$$Q_{12} = P_1 P_2 V_1 \cdot \ln \frac{V_2}{V_1}$$
$$= P_1 V_1 \ln \frac{P_1}{P_2}$$

$$Q_{12} = \int_{V_1}^{V_2} P dV.$$

$$Q_{12} = W_{12} = P_1 V_1 \ln \frac{V_2}{V_1} = P_1 V_1 \ln \frac{P_1}{P_2}$$

$$U_2 - U_1 = 0$$

✓ ADIABETIC .

$$U_2 - U_1 = \frac{P_1 V_1 - P_2 V_2}{\gamma - 1}$$
$$= \frac{m R (T_1 - T_2)}{\gamma - 1}$$

↳ Poly tropic process .

$$Q_{12} = (U_2 - U_1) + \frac{P_1 V_1 - P_2 V_2}{n-1}$$
$$= \frac{m R (T_1 - T_2)}{(n-1)} + m C_v (T_2 - T_1)$$

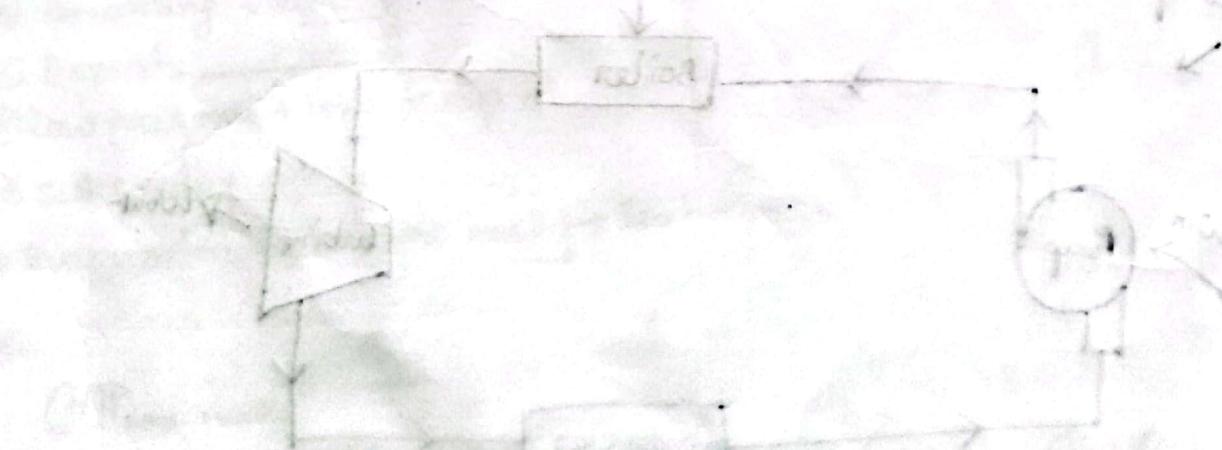
✓ ISOCORRIC

$$Q_{12} = \frac{U_2 - U_1}{V_2 - V_1} = m C_v (T_2 - T_1)$$

✓ ISOBARIC

$$Q_{12} = H_2 - H_1 = m C_p (T_2 - T_1)$$

(at) pressure kept constant - same final



Sub: 2nd law of TD.

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Reversible: A process that have no change in either system or surroundings by reversing. (No real process is reversible).

Conditions: ① No friction

② No heat transfer across finite temp diff.

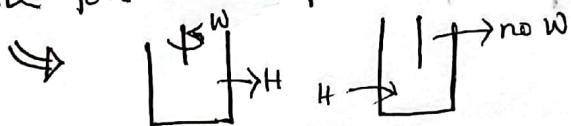
Irreversible - Not reversible.

Example: Frictionless motion, slow frictionless adiabatic expansion, spring extension.

Limits of 1st TD:

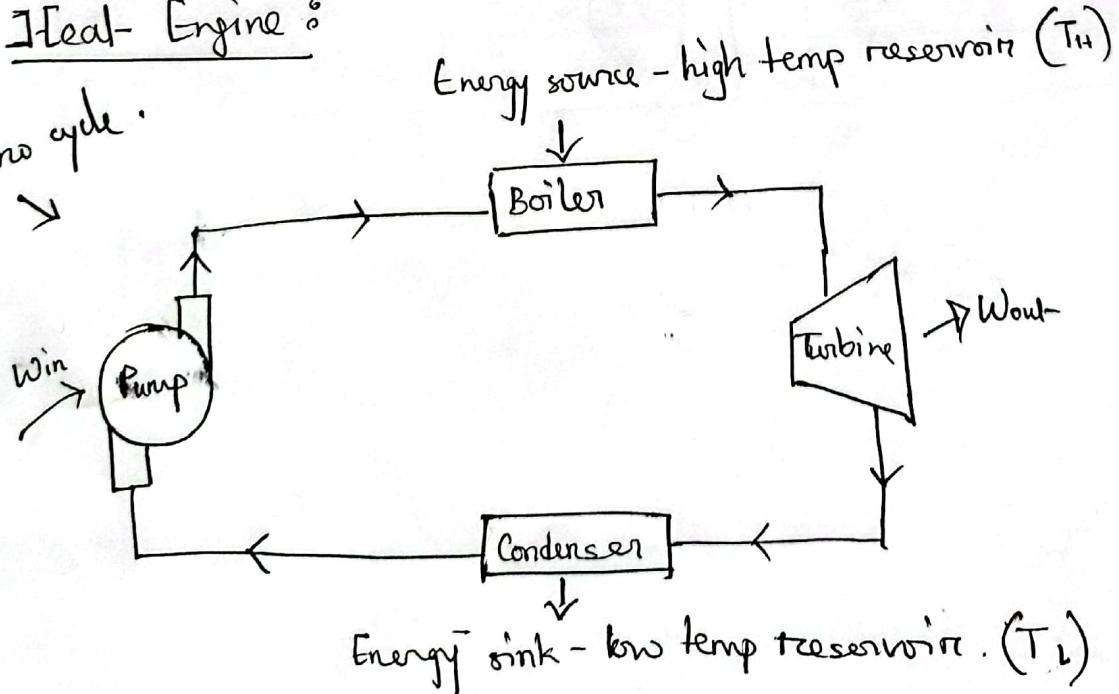
① No complete transformation of heat into work but work completely transform to heat.

② Not possible for some process — not reversible.



Ideal- Engine :

Thermo cycle.



Thermal Efficiency of HE :

$$\eta = \frac{W}{\Phi_H} = \frac{\Phi_H - \Phi_L}{\Phi_H} = 1 - \frac{\Phi_L}{\Phi_H}$$

Normally, $W < \Phi_H$.

Can never be 100%, so, $\eta > 0$; usually 30% - 50%.

3RD LAW

KELVIN PLANCK statement : "It is impossible to construct a system which will operate in a cycle, extract heat from a reservoir and do an equivalent amount of work on the surrounding."

Refrigeration / AC (split) cycle :

① Compressor - I low pressure + low temp

② Compressed .

③ High pressure + high temp

⑤ Superheating w

⑥ Release heat

⑦ Throttling valve

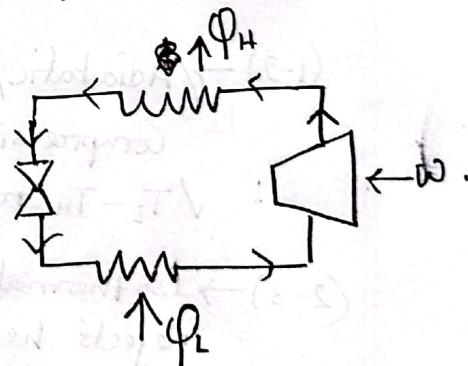
⑧ Expands

⑨ Low pressure + low temp .

⑩ sub cooling w

⑪ Evaporator + absorbs heat

Isentropic



$$COP_{heat\ pump} = \frac{\Phi_H}{W}$$

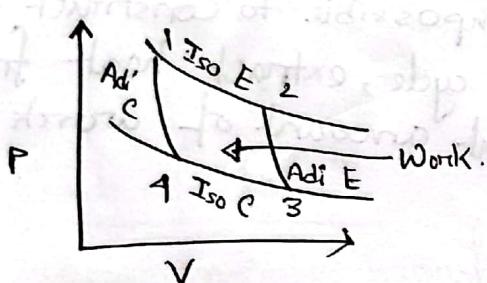
$$COP_{Refriger/AC} = \frac{\Phi_L}{W}$$

$$COP_{HP} = COP_R + 1$$

$$\text{as, } \frac{\Phi_H}{W} = \frac{\Phi_L + W}{W} \quad [\because \Phi_H = \Phi_L + W]$$

CLAUSIUS STATEMENT: It is impossible to construct a system that operates in a cycle and transfers heat from a lower temp body to a higher temp body without work being done on the system by surroundings.

CARNOT CYCLE



Reverse Carnot \rightarrow Refrigeration cycle

same as : refrigeration cycle

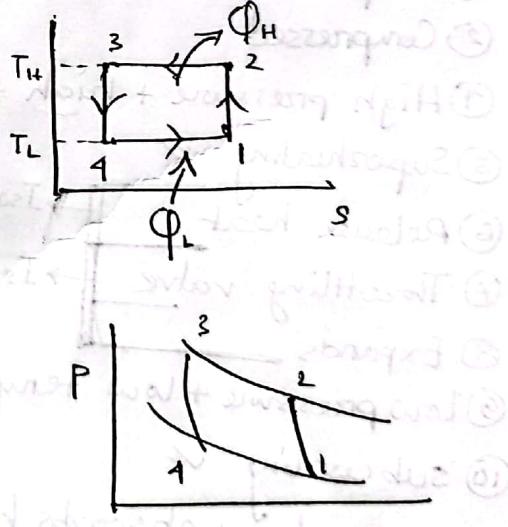
(1-2) \rightarrow Adiabatic / Isentropic compression.

$$\sqrt{T_L - T_H} \text{ rise} - \text{Heat} = \text{const}$$

(2-3) \rightarrow Isothermal compression
Rejects heat

(3-4) \rightarrow Isentropic expansion
 $T_H - T_L$ drops. Heat = const.

(4-1) \rightarrow Isothermal expansion
Heat absorbed



COP: Coefficient of Performance. is an index of performance of a thermodynamic cycle or a thermal system.

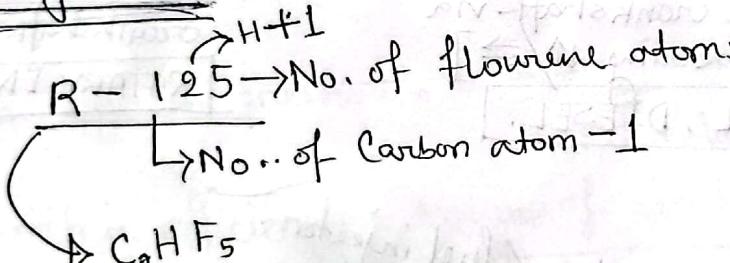
[As it can be greater than 1, it is used instead of

$$\eta \rightarrow COP_R = \frac{Q_L}{W}$$

1 British thermal Unit $h^{-1} = 0.293 \text{ W}$.

For AC \rightarrow VCR (Compression)
VAR (Absorption).
Air Refrigeration

Refrigerant (ASHRAE)



$CHFC_2 \rightarrow$ dichlorofluoromethane $\rightarrow R-21$.

$CHF_2Cl \rightarrow$ chlorodifluoromethane $\rightarrow R-22$.

$C_2H_2F_4 \rightarrow$ tetrafluoroethane $\rightarrow R-134a$.

EC → external. Combustion
 IC engine → internal Combustion
 CI → Compression Ignition engine
 Sub: SI → Spark Ignition engine

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Combustion of HC (exothermic).

Engine (thermal E → Mechanical E)

External (EC)

[Product of combustion ≠ working fluid. i.e. steam engine, sterling Engine]

Internal (IC)

[Product = working fluid. i.e. Petrol, diesel, biofuel engine]

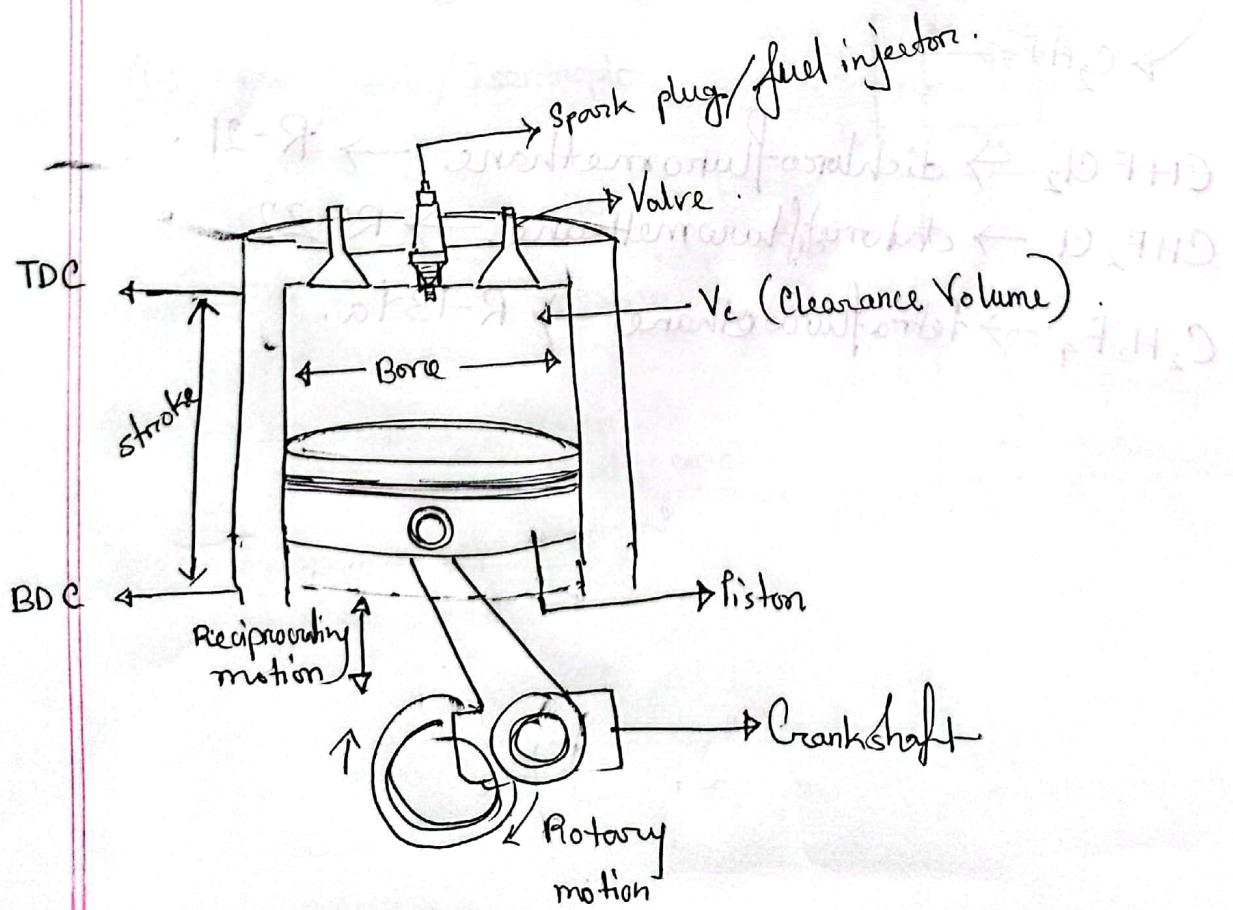
Reciprocating

[Pistons transfer power to the crankshaft via reciprocating \uparrow/\downarrow]

PETROL, DIESEL.

Rotary

[Pistons transfer P to crankshaft by rotating]
ROTARY ENGINE



Formulae :

Stroke = $2\pi r$ of crankshaft - (r = radius)

Piston Displacement = Volume between TDC and BDC.

Engine Capacity (Total piston Displacement) = No. of Pistons \times Piston Displacement.

Swept Volume, V_s = total V - V_c .

Compression ratio, $r_o = \frac{(V_s + V_c)}{V_c} \left[\frac{\text{Total V}}{V_c} \right]$

[NOTE: Normally for SI $\rightarrow 8-12$
" CI $\rightarrow 12-24$]

Mean Effective Pressure, $= \frac{\text{Work done}}{\text{total Volume}}$

Volumetric efficiency = Volume of air in cylinder / Total Volume

Petrol Engine < Diesel Engine < (Turbocharger + Supercharger) [Air compressing device]

Power :

Indicated Power (IP): Power developed within the engine cylinder.

Brake Power (BP): Delivered power at the crankshaft; always BP < IP.

Because of frictional + pumping losses, and reciprocating mechanism.

Engine Torque: Force of rotation acting about the crankshaft axis at any given instant.

[NOTE: - High BP + low torque \rightarrow easy to accelerate but speed \rightarrow difficult to maintain]

Low BP + High torque \rightarrow difficult to accelerate but highest speed \rightarrow maintain

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Engine Classification :

No. of cylinders : V1, V6 etc.

Arrangement of cylinders : Inline, V type, Opposed.

"valves" : Overhead camshaft, Pushrod camshaft, valveless.

Cooling : Water cooled, air cooled.

Strokes : 2, 4.

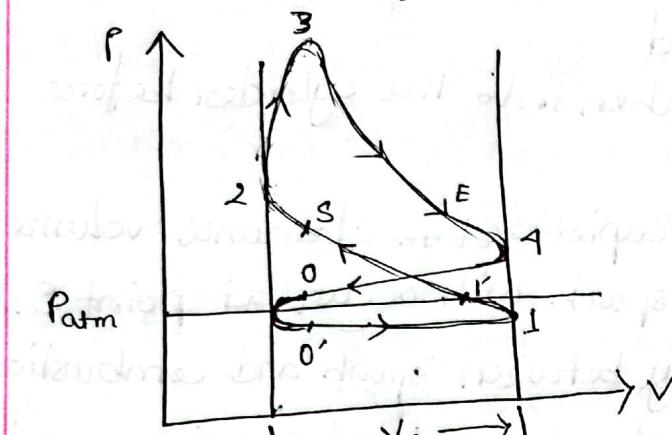
Fuel : Gasoline, Diesel, Ethanol, CNG

Ignition : Spark, Self or Compression.

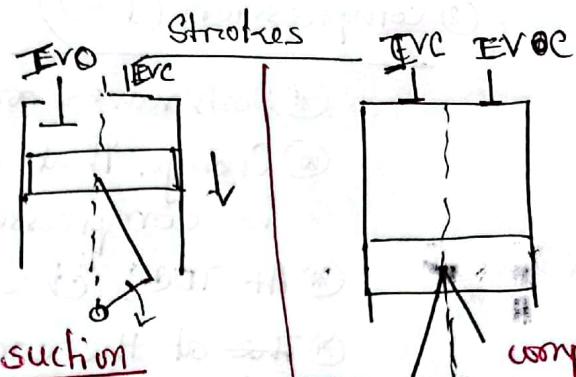
Firing order : (For 4 cylinders) $\rightarrow 1-2-4-3$

$1-3-4-2$

4-stroke SI Engine :



(P-V diagram)



IVO → Inlet valve Closed

EVC → Exhaust " "

IVC → Inlet " opened

EVO → Exhaust " "

Expansion/power

Exhaust stroke

The cycle is completed in 4 strokes of the pistons or 2 revolutions of the crankshaft. So, 720° CA is required for a complete cycle.

Steps:

- ① Induction/Suction Stroke: (0-1)
 - Before the TDC, inlet valve opens at point 0.
 - Piston moves from TDC to BDC, mixture of air and fuel enters the cylinder via IV.
 - Pressure reduces in the cylinder than that of atmosphere. So the charge flows through induction system.
 - Valve should close at point 1 which does not happen until piston moves to point 1'.

Next slide for diagram showing effect of this suction rate.

(2) Compression (1'-2)

- ④ Both valves are closed
- ④ Charge that was taken into the cylinder before is compressed
- ④ At TDC, charge occupies ~~volume~~ clearance volume.
- ④ ~~The~~ at the end the spark will occur at point S.
- ④ There is a time delay between spark and combustion.
- ④ Combustion occurs at almost const. volume, increased pressure and temp. during the process (2-3)

(3) Expansion or power stroke (3-1)

- ④ Hot high pressured burnt gases pushes the piston to BDC.
- ④ Both Inlet- and Exhaust valves are closed.
- ④ At point E, ^{just} before BDC happens, the gaseous products are exhausted as exhaust valve opens.
- ④ Power is obtained
- ④ Pressure and temp. decreases.
- ④ Expansion completes at point 1.

(4) Exhaust stroke (1-0')

- ④ Piston moves from BDC to TDC sweeping burnt gas through EV while TV is closed.
- ④ At this time pressure slightly rises than Patm.
- ④ EV closes at point 0'.
- ④ Vc is full of exhaust gas from previous cycle which are called residual gases.

Later, the mixture will be compressed consisting both fresh and residual gases.

4 stroke CI engine:

Same as SI but ~~more~~ high compression ratio is used in the CI.

① Suction Stroke : ④ IV opens and air enters (no fuel).

- * ④ Piston moves from TDC to BDC.

② Compression:

- * ④ IV and EV remains closed.

- * ④ Air is compressed.

- * ④ Air pressure + temp. rises.

- * ④ As the piston reaches to TDC, fuel is injected finely into the hot compressed air.

- * ④ After a short delay, ignition occurs.

- * ④ Pressure rises (gas).

③ Expansion:

- * ④ Work done is occurred by gas pressure as piston sweeps maximum cylinder volume.

- * ④ Temp. and pressure of burnt gas fall as it expands just before piston approaches BDC.

④ Exhaust stroke: ④ EV opens at BDC and products (burnt gases)

- are rejected.

- * BDC to TDC, IV opens again and cycle repeated.

Valve timing →

IVO about 30° before TDC

IVC " 50° after BDC

EVO " 45° before BDC

EVC " 30° after TDC.

Fuel injection 15° before TDC.

2stroke

- ① Simpler, compact, lighter and cheaper.
- ② Power stroke ~~time~~ per crankshaft revolution.
- ③ Torque output is smoother.
- ④ In low rpm power produced is lower.
- ⑤ Lubrication system is simpler.
- ⑥ Less volumetric efficiency.
- ⑦ Develops less power and torque.
- ⑧ Greater tendency to build up carbon deposit on the cylinder wall.
- ⑨ Overheats faster.

4 stroke

- ① Complicated, heavy, expensive.
- ② Power stroke ~~enters~~ at 2 crankshaft revolution.
- ③ Torque output is not smoother.
- ④ Higher power.
- ⑤ Complicated.
- ⑥ High volumetric efficiency.
- ⑦ High power + torque.
- ⑧ No.
- ⑩ Takes time to overheat.

Air standard cycle :

The cycle we use to evaluate important engine terms with mathematical equations is known as ideal cycle or air standard cycle.

Assumptions (in short) :

- ① Working fluid is always - ideal gas, pure air with const. specific heat .
- ② Fixed mass of air is the working fluid throughout the entire cycle.
- ③ Closed loop.
- ④ Combustion process is replaced by const. heat addition process.
- ⑤ Cycle is reversible.
- ⑥ Compression and expansion are reversible adiabatic.
- ⑦ No chemical change .
- ⑧ Frictionless operation .

Sub: Otto Cycle. (-Nikolaus Otto . 1876)

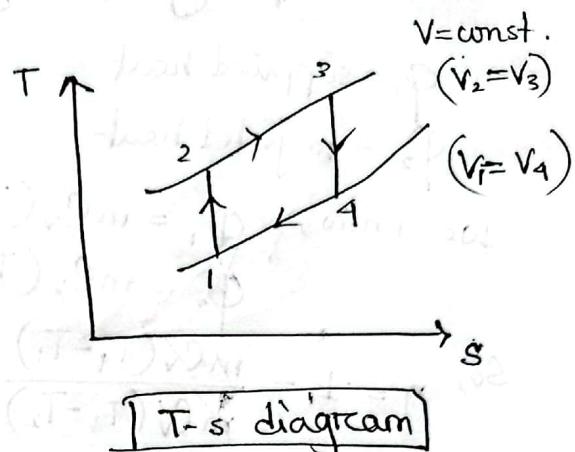
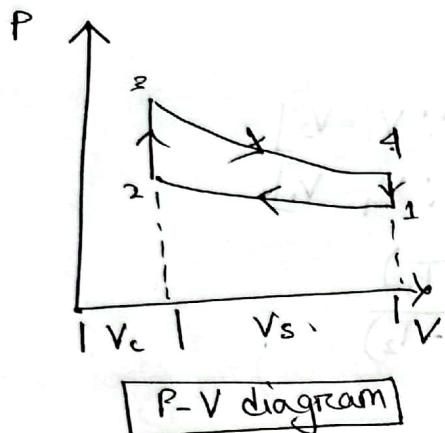
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Happens in Petrol and Gas engines.

[Low volumetric Efficiency]



(1-2) reversible adiabatic or isentropic compression

④ Piston moves upwards and air is compressed. No heat transferred

(2-3) Const. volume heating

④ piston is at TDC

④ Heat is supplied to air.

\dot{Q}_1 (supplied)

(3-4) Adiabatic or isentropic expansion.

④ Pressure + temp is high.

④ Piston is pushed to BDC.

④ Work is done. (No heat transfer).

\dot{Q}_2 (rejected)

(4-1) Constant volume heat rejection.

V_s = Swept Volume

V_c = Clearance Volume

V = total Volume .

$$\text{Compression ratio, } r_o = \frac{V}{V_c} = \frac{(V_s + V_c)}{V_c} = \frac{V_1}{V_2} \quad [\text{Let. } V=V_1 \text{ and } V_c=V_2]$$

Sub :

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Thermal efficiency of any cycle $\Rightarrow \eta = \frac{W}{Q_1(\text{supplied})} = \frac{Q_1 - Q_2}{Q_1} = 1 - \frac{Q_2(\text{sink})}{Q_1}$

Q_1 = supplied heat

Q_2 = rejected heat

$$\text{we know, } Q_1 = mC_v(T_3 - T_2) \quad [\because V_3 = V_2]$$

$$Q_2 = mC_v(T_4 - T_1) \quad [\because V_4 = V_1]$$

$$\text{So, } \eta = 1 - \frac{mC_v(T_4 - T_1)}{mC_v(T_3 - T_2)} = 1 - \frac{(T_4 - T_1)}{(T_3 - T_2)}$$

For, isentropic (1-2),

$$\frac{T_2}{T_1} = \left(\frac{V_1}{V_2} \right)^{\gamma-1} = r^{\gamma-1}$$

$$\Rightarrow T_2 = T_1 r^{\gamma-1}$$

$$\text{Similarly, for (3-4)}$$

$$T_3 = T_4 r^{\gamma-1}$$

So, for Otto cycle,

$$\eta = 1 - \frac{(T_4 - T_1)}{(T_4 r^{\gamma-1} - T_1 r^{\gamma-1})} = 1 - \frac{(T_4 - T_1)}{(T_4 - T_1)r^{\gamma-1}}$$

$$\eta = 1 - \frac{1}{r^{\gamma-1}}$$

(Ans)

$$\text{Ansatz 1: } \Delta p \Delta V = \Delta V$$

$$\text{Ansatz 2: } \Delta V = \Delta V$$

$$\text{Ansatz 3: } \Delta V_{\text{tot}} = V$$

$$\frac{V_f - V_i}{V_i} = \frac{(V_f + V_i)}{2V} = \frac{V}{2V} = \alpha \quad \text{einen missverstanden}$$

For mean effective pressure,

$$\text{we know, } w = \phi_1 - \phi_2 = mC_v(T_3 - T_2) - mC_v(T_1 - T_0) \\ = mC_v [(T_3 - T_2) - (T_1 - T_0)]$$

Again for, (2-3),

$$\frac{-P_2}{T_2} = \frac{P_3}{T_3}$$

$$\Rightarrow T_3 = \frac{P_3}{P_2} T_2 = \alpha T_2 = \alpha T_1 r^{n-1}$$

~~Similarly for (3-4), $T_4 = \frac{P_4}{P_3} T_3 = \alpha T_3 r^{n-1} = \alpha T_1 r^{n-1} (\alpha - 1)$~~

~~$T_3 = \alpha T_2 r^{n-1}, T_4 = \alpha T_3 r^{n-1} = \alpha^2 T_2 r^{n-1} = \alpha^2 T_1 r^{n-1} (\alpha - 1)$~~

putting the value,

$$w = mC_v [(\alpha T_1 r^{n-1} - T_1 r^{n-1}) - (\alpha^2 T_1 - T_1)] \\ = mC_v [T_1 (\alpha r^{n-1} - 1) - T_1 (\alpha - 1)] \\ = mC_v [(\alpha - 1) (T_1 r^{n-1} - T_1)]$$

we know,

mean effective pressure, $P_m = \frac{w}{V_s}$

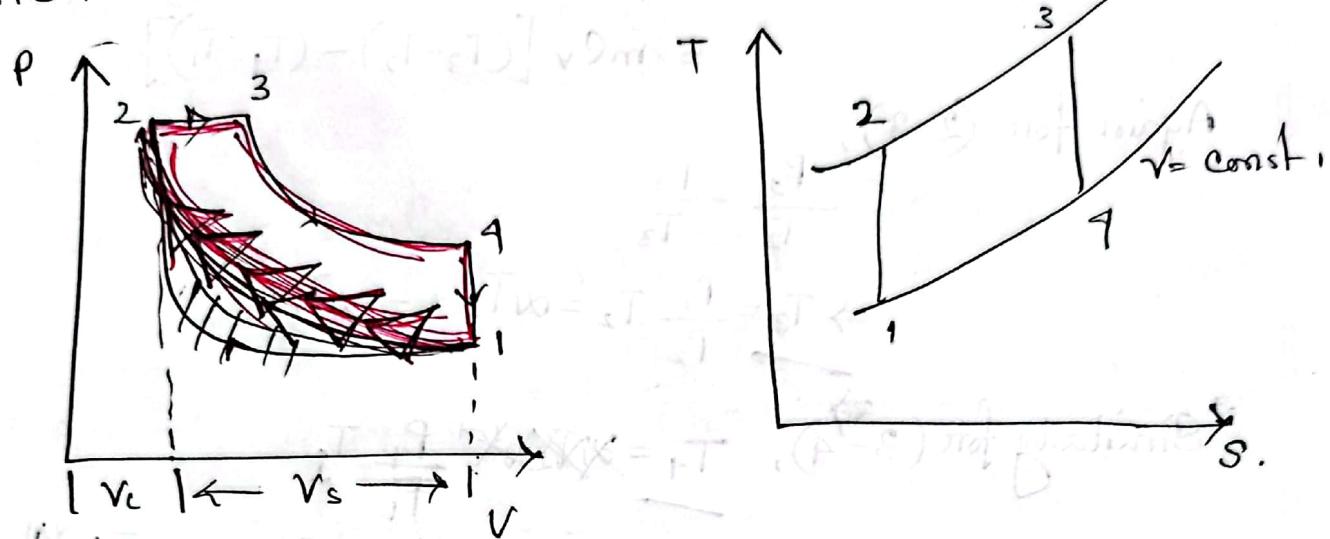
$$\text{and } V_s = V - V_c = V_1 - V_2 = 1 - \frac{V_2}{V_1} = \frac{mRT_1}{P_1} \left(1 - \frac{1}{r}\right)$$

$$\text{so, } P_m = \frac{mC_v [(\alpha - 1) (T_1 r^{n-1} - T_1)]}{mRT_1 \left(1 - \frac{1}{r}\right)} = \frac{C_v}{R} \cdot \frac{T_1 (\alpha - 1) (r^{n-1} - 1)}{T_1 (n-1)}$$

$$\Rightarrow P_m = \frac{P_1 (\alpha - 1) (r^{n-1} - 1) r}{(\gamma - 1)(n-1)} = \frac{P_1 (\alpha - 1) (1 - \frac{1}{r^n}) r}{(\gamma - 1)(n-1)} \\ = \frac{P_1 (\alpha - 1) n r^{n-1}}{(\gamma - 1)(n-1)} \quad (Ans)$$

Slow speed compression-ignition engine.

heat is added at const. pressure.



(1-2) Isentropic compression

(1-2) Isentropic compression
(2-3) Const. Pressure, Heat is supplied (ϕ)

(3-4) Isentropic expansion, no heat transfer

(1-1) Const. Volume, Heat is rejected (\dot{Q}_2)

$$S_0, \quad Q_1 = m C_p (T_3 - T_2)$$

$$Q_2 = m C_v (T_2 - T_1) \cdot [1 - (1 - \alpha)] \sqrt{g_{mm}}$$

Thermal Efficiency , $\eta = 1 - \frac{\phi_2}{\phi_1}$

$$= 1 - \frac{m C_v (T_4 - T_1)}{m C_p (T_3 - T_2)}$$

$$= 1 - \frac{(T_4 - T_1)}{\gamma(T_3 - T_2)}$$

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$$\text{Here, } r = \frac{V_3}{V_2} - \frac{V}{V_c} = \frac{V_1}{V_2}$$

At point 3, fuel supply is cut off.

$$\text{So, cut off ratio, } \beta = \frac{V_3}{V_2}$$

$$\text{For } (1 \rightarrow 2), \frac{T_2}{T_1} = \left(\frac{V_1}{V_2} \right)^{\gamma-1} = r^{\gamma-1}$$

For (2-3),

$$\frac{V_2}{T_2} = \frac{V_3}{T_3}$$

$$T_3 = \beta T_1 r^{\gamma-1}$$

Similarly for (3-4), $T_4 = \beta T_3$

$$\text{So, } \eta = 1 - \frac{(P_{T_1} - T_1)}{\gamma (\beta T_1 r^{\gamma-1} - T_1 r^{\gamma-1})}$$

$$= 1 - \frac{(\beta - 1) r^{\gamma-1}}{\gamma (\beta - 1) r^{\gamma-1}}$$

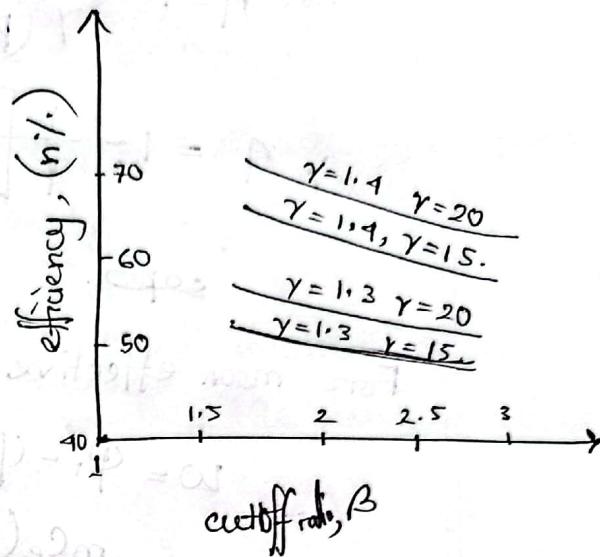
$$= 1 - \frac{1}{\gamma}$$

$$\text{Similarly, for (3-4), } T_4 = \frac{T_3}{\beta} \left(\frac{V_3}{V_4} \right)^{\gamma-1}$$

$$\Rightarrow T_4 = \frac{T_3}{\beta} \left(\frac{\beta}{r} \right)^{\gamma-1}$$

$$= \beta T_3 \cdot \beta^{\gamma-1}$$

$$= T_1 \cdot \beta^{\gamma-1}$$



Sub:

$$\text{So, } \eta = 1 - \frac{(T_1 \beta^{r-1} - T_1 \beta)}{\gamma (B T_1 r^{r-1} - T_1 r^{r-1})}$$

$$\Rightarrow \eta = 1 - \frac{1}{\gamma} \left[\frac{(\beta^r - 1)}{r^{r-1} (\beta - 1)} \right]$$

Ans.

For mean effective pressure,

$$\begin{aligned} w &= \Phi_1 - \Phi_2 \\ &= m C_p (T_3 - T_2) - m C_v (T_1 - T_2) \\ &= m C_p (T_1 \beta r^{r-1} - T_1 r^{r-1} \underbrace{(-T_1 \beta^{r-1} + T_1)}_{\gamma}) \\ &= m C_p T_1 \left(r^{r-1} (\beta - 1) - \frac{(\beta^{r-1} - 1)}{\gamma} \right) \\ &= \cancel{m C_p T_1} \end{aligned}$$

Swept Volume, $V_s = V_1 - V_2 = V_1 \left(1 - \frac{1}{r}\right) = \frac{m R T_1}{P_1} \left(\frac{r-1}{r}\right)$.

Mean effective pressure, $P_m = \frac{w}{V_s} = \frac{\cancel{m C_p T_1 / (r^{r-1} (\beta - 1) - (\beta^{r-1} - 1))} \cdot P_1 \cdot r}{m R T_1 / (r-1)}$

$$\begin{aligned} &= \frac{\gamma}{\gamma-1} \cdot \frac{P_1 \cdot r}{(r-1)} \cdot \left[r^{r-1} (\beta - 1) - \frac{1}{\gamma} (\beta^{r-1} - 1) \right] \\ &= \frac{\gamma \cdot P_1}{(\gamma-1)(r-1)} \left[\gamma r^r (\beta - 1) - \frac{1}{\gamma} (\beta^{r-1} - 1) \right] \\ &= \frac{P_1 \cdot \gamma r^r (\beta - 1)}{(\gamma-1)(r-1)} \left[1 - \frac{\frac{1}{\gamma} (\beta^{r-1} - 1)}{r^{r-1} \cdot \gamma (\beta - 1)} \right] \\ &= \frac{P_1 \cdot r^r (\beta - 1)}{(\gamma-1)(r-1)} \eta. \end{aligned}$$

SI vs CI

Sub: Petrol Engine Vs Diesel Engine

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PETROL (SI)

- ① In SI ; air and petrol is charged and compressed.
- ② Compression ratio is 8-12
- ③ Low thermal efficiency and fuel savings .
- ④ Low volumetric efficiency as throttle valve is there.
- ⑤ Expensive
- ⑥ Spark plug , Carburetor etc present
- ⑦ Higher accelerating power

DIESEL (CI)

- ① Only Air is compressed .
- ② Compression ratio is 12-24
- ③ High .
- ④ Higher volumetric efficiency as no throttle valve is there
- ⑤ Cheaper
- ⑥ Large capability to control fuel injection accurately .
- ⑦ High torque .

OTTO CYCLE

- ① $\eta = 1 - \frac{1}{n^{\gamma-1}}$
- ② For efficiency compression ratio is greater
- ③ No cut off ratio is related

DIESEL CYCLE

- ① $\eta = 1 - \frac{1}{n^{\gamma-1}} \left[\frac{\beta^{\gamma} - 1}{\gamma(\beta - 1)} \right]$
- ② For the same n , η is less .
- ③ η increases with decrease of β but with const n and γ β decreases .

$$(T_1 - ST) \cdot V_{max} + (ST - ST') \cdot V_{avg} \cdot p_b$$

$$\frac{V_{max} \cdot V_{avg}}{V_{avg}} = \frac{p_b}{p_a} : \text{constant}$$

$$\frac{V_{max} \cdot V_{avg}}{V_{avg}} = p_b - w$$

$$O = Ub$$

Sub: Thermodynamics Formulae

Day

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$$P_{atm} = P_{abs} + P_{vac}. \quad [P_{atm} > P_{abs}]$$

$$P_{gauge} = P_{abs} - P_{atm}. \quad [P_{atm} < P_{abs}]$$

$$SPEE \rightarrow Q - W = mg(z_2 - z_1) + \frac{1}{2} m(c_2^2 - c_1^2) + m(h_2 - h_1)$$

$$q - w = g(z_2 - z_1) + \frac{1}{2} (c_2^2 - c_1^2) + (h_2 - h_1)$$

$$SFEE \rightarrow \text{Turbine}, w = h_2 - h_1 \quad [\because q=0; z_2=z_1; c_2 \approx c_1]$$

$$\text{Nozzle}, h_1 + \frac{c_1^2}{2} = h_2 + \frac{c_2^2} {2} \quad [\because q=0, w=0, z_1=z_2]$$

$$\text{Throttling}, h_1 = h_2 \quad [\because q=0, w=0, z_1=z_2, c_1 \approx c_2]$$

$$\text{Heat Exchanger}, q = h_2 - h_1 \quad [\because w=0, z_1=z_2, c_1 \approx c_2]$$

$$\text{1st TD: } \delta Q = dU + \delta W$$

$$\Phi_{12} = (U_2 - U_1) + W_{12}$$

$$C_p - C_v = R$$

$$\frac{C_p}{C_v} = \gamma ; \quad C_v = \frac{C_p}{\gamma} ; \quad C_p = \frac{\gamma}{\gamma-1} ; \quad C_v = \frac{1}{\gamma-1}$$

$$\frac{P_2}{P_1} = \left(\frac{V_1}{V_2} \right)^\gamma ; \quad \frac{T_2}{T_1} = \left(\frac{V_1}{V_2} \right)^{\gamma-1} = \left(\frac{P_2}{P_1} \right)^{\frac{\gamma-1}{\gamma}}$$

$$PV = mRT$$

$$P = PRT$$

$$\text{Isothermal: } \delta \Phi = P_1 V_1 \ln \frac{V_2}{V_1}$$

$$W = \Phi = P_1 V_1 \ln \frac{P_2}{P_1}$$

$$dU = 0.$$

∇ diabetie:

$$d\Phi = \frac{mR(T_2 - T_1)}{(n-1)} + mC_v(T_2 - T_1)$$

Isochoric: $d\phi = U_2 - U_1 = m c_v (T_2 - T_1)$

Isobaric: $d\phi = dH = m c_p (T_2 - T_1)$

$$\eta = \frac{\Phi_H - \Phi_L}{\Phi_H} = \frac{w}{\Phi_H} = 1 - \frac{\Phi_L}{\Phi_H}$$

$$w = \Phi_H - \Phi_L$$

$$COP_{HP} = \frac{\Phi_H}{w} = COP_R + 1$$

$$COP_R = COP_{AC} = \frac{\Phi_L}{w}$$

$$Ashraze \rightarrow R - (c-1)(H+1) (F)$$

Engine capacity \rightarrow No. of piston x. piston displacement.

$$V = V_s + \theta V_c$$

$$r = \frac{V}{V_c}$$

$$P_m = \frac{w}{V_s}$$

Otto Cycle

$$\eta = 1 - \frac{1}{r^{\gamma-1}}$$

$$P_m = \frac{P_i (\alpha-1)}{(\gamma-1)(r-1)} \cdot \eta r^\gamma$$

Diesel Cycle

$$\eta = 1 - \frac{1}{r^{\gamma-1}} \left[\frac{\beta^\gamma - 1}{\gamma(\beta-1)} \right]$$

$$P_m = \frac{P_i (\beta-1)}{(\gamma-1)(r-1)} \cdot \eta \gamma r^{\gamma-1}$$

With LOVE

-DUNA

For 2D cases $\cdot F = (\sum F_x) \hat{i} + (\sum F_y) \hat{j}$ as $\boxed{\sum F_x = 0, \sum F_y = 0}$

FBD \rightarrow ① Outline

- External forces
- ② Forces shown
- ③ Identify forces

Principle of Transmissibility.

$$F' = F$$

Vector Product $\rightarrow V$

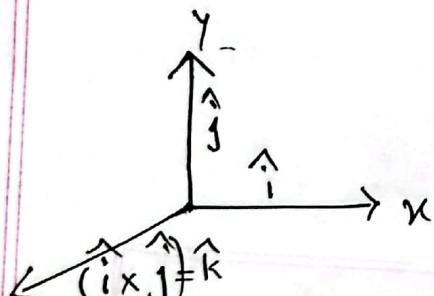
$$V = Q \times P$$

\otimes not commutative Here, $(Q \times P) \neq - (P \times Q)$.

$$\text{But } Q \times P = - (P \times Q)$$

① distributive $P \times (Q_1 + Q_2) = (P \times Q_1) + (P \times Q_2)$

\otimes not associative, $(P \times Q) \times S \neq P \times (Q \times S)$.



$$\begin{array}{ll} \hat{i} \times \hat{i} = 0, & \hat{j} \times \hat{i} = \hat{k} \\ \hat{i} \times \hat{j} = \hat{k}, & \hat{j} \times \hat{j} = 0 \\ \hat{i} \times \hat{k} = -\hat{j}, & \hat{i} \times \hat{k} = \hat{j} \end{array}$$

$$\begin{array}{ll} \hat{k} \times \hat{i} = \hat{j} \\ \hat{k} \times \hat{j} = -\hat{i} \\ \hat{k} \times \hat{k} = 0 \end{array}$$

$$V = P \times Q \Rightarrow \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ P_x & P_y & P_z \\ Q_x & Q_y & Q_z \end{vmatrix}$$

Scalar

commutative ✓
distributive ✓

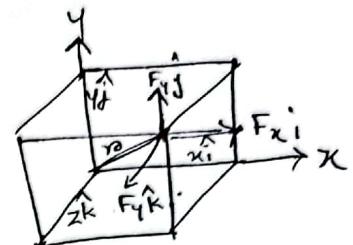
Not associative $(P \cdot Q) \cdot S = \text{undefined}$

$$\hat{i} \cdot \hat{i} = \hat{j} \cdot \hat{j} = \hat{k} \cdot \hat{k} = 1$$

$$\hat{i} \cdot \hat{j} = \hat{j} \cdot \hat{k} = \hat{k} \cdot \hat{i} = 0$$

Sub :

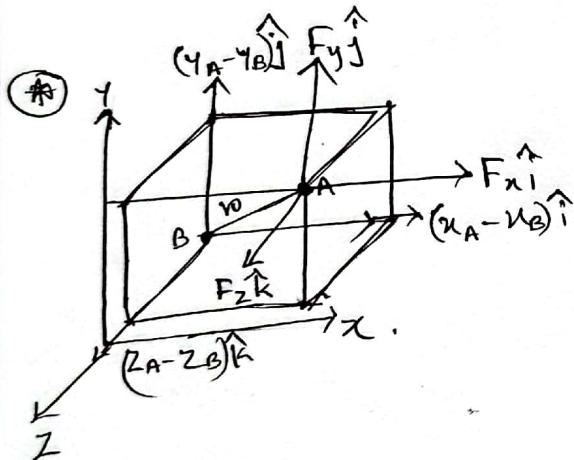
$$M = F \times d. \quad (\text{Torque}) . \\ = d \cdot F \sin \theta .$$



Vargignon's Theorem :

$$F_1 \times r_0 + F_2 \times r_0 + \dots = r_0 \dot{x} (F_1 + F_2 + \dots)$$

$$\bar{M}_0 = M_{x_1} \hat{i} + M_{y_1} \hat{j} + M_{z_1} \hat{k} \\ = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ x & y & z \\ F_x & F_y & F_z \end{vmatrix} = (y F_z - z F_y) \hat{i} + (z F_x - x F_z) \hat{j} + (x F_y - y F_x) \hat{k}$$



$$\text{For, 2D, } M_0 = x F_y - y F_x . \\ = (x_A - x_B) F_y - (y_A - y_B) F_x .$$

$$\text{Moment} = F \times r_0 .$$