

Digital Logic Design

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TODAY OUTLINE: $f_1, f_2, f_3 \leftarrow$ function signal design

Combinational (easy)

Sequential (tough)

i) Digital CKT

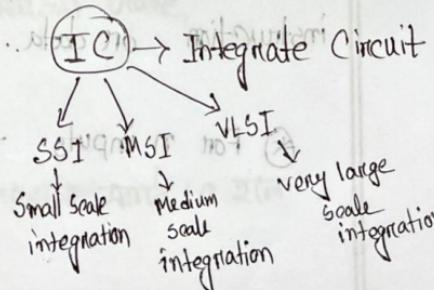
Discrete values

ii) Analog CKT

Continuous values

0, 1
Bit

0 → Low
1 → High



Logic / Digital / Switching Circuit → input → 0, 1 } → 0, 1
 Output → 0, 1 A TIPPAH
 two state → low & high

Basic logic Circuit → OR, AND, NOT

GATE : - one or more input but output Signal
 only one

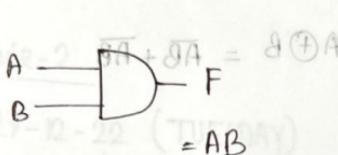
Truth Table : - all output and input possibilities
 input listed in Binary Progression.

WORD : - A string of bits that represent a coded instruction or data..

* For n inputs there are 2^n input combinations.

$$F = AB = \overline{(B-X_1)(B-X_3)} \quad \text{Explain OR}$$

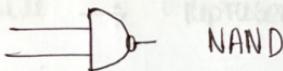
G-12-22 (TUESDAY) Chapter - 3 (cc → 1 to 1)



Symbol of AND Gate

Output rises at 1 main level

	0	1
0	0	0
1	1	0
1	0	1
1	1	1



A $\rightarrow A'$ Not

\rightarrow Buffer

* NAND and NOR \rightarrow Universal Gate

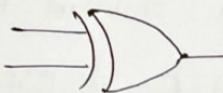
NAND

A	B	F
0	0	1
0	1	1
1	0	1
1	1	0

{

Truth Table of NAND Gate

The Exclusive OR (EX-OR / X-OR) :-

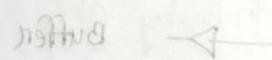


$$A \oplus B = \overline{AB} + \overline{A}\overline{B}$$

A	B	F
0	0	0
0	1	1
1	0	1
1	1	0

total num 1 is odd, output 1.

total num 1 is even, output 0.



word - A string of bits that represent a
stored program or data in memory.

NAND

A	B	F
1	0	0
1	1	0
0	0	1
0	1	1

For n inputs, there are 2^n possible combinations.

Quiz-16-12-2022 (TUESDAY) [Chapter - 1 & 2] ($1ec \rightarrow 1$ to 7)Quiz-2

27-12-22 (TUESDAY)

Boolean Algebra & Logic Simplification

Boolean \rightarrow always either true or false.Variable \rightarrow represent a logical quantity② Complement \rightarrow inverse of a variable.

$$(A \text{ is } 1 \text{ or } 0) \rightarrow A = 1, \bar{A} = 0$$

Laws of Boolean Algebra:-

① Commutative laws:-

$$\Rightarrow A + B = B + A$$

$$\Rightarrow AB = BA$$

$$I = I + A$$

$$0 = 0 \cdot A$$

② Associative Laws :-

$$\Rightarrow A + (B + C) = (A + B) + C$$

$$\Rightarrow A(BC) = (AB)C$$

$$(YADAVUT) 22-9-19$$

③ Distributive Laws :-

AND distributive over OR :- $A(B+C) = AB + AC$

OR distributive over AND :- $A+BC = (A+B)(A+C)$

Rules of Boolean Algebra : 12 rules (must)

* Dual :- Operators and fixed values will be changed
But variables will not be changed.

$$\begin{cases} A+1=1 \\ A \cdot 0=0 \end{cases}$$

$$\begin{cases} A+B+C=0 \\ AB=0 \\ A=0 \end{cases}$$

De-morgan's Theorem:

$$1. \overline{AB} = \overline{A} + \overline{B}$$

$$2. \overline{A+B} = \overline{A} \cdot \overline{B}$$

$$= (A + \bar{A}) \cdot (A + C) \quad [\text{using distributive law}]$$

$$= 1 \cdot (A+C) [B = C + B] \quad 0 \quad A + B + C + B = A + B + C$$

$$= A+C$$

$$= R.H.S$$

$$\textcircled{2} \quad L.H.S = x + xy$$

$$= (x+x)(x+y) \quad [A+BC = (A+B)(A+C)]$$

$$= x(x+y) \quad [A+A=A]$$

$$[D = \overline{SS}] \quad S(\overline{AA} + D \cdot A + S\overline{A}) =$$

= R.H.S

$$\textcircled{3} \quad \text{L.H.S} = x(\bar{x} + y)$$

$$= X\bar{X} + XY \quad [A(B+C) = AB + AC]$$

$$= 0 + XY$$

$$= x^2y$$

= R.H.S

Simplification using Boolean Algebra :

$$\text{i. } AB + A(B+C) + B(B+C) \quad \overline{B} + \overline{A} = \overline{BA}$$

$$= AB + AB + AC + BB + BC \quad [\text{Distributive Law}]$$

$$= AB + AB + AC + B + BC \quad [BB = B]$$

$$= AB + AC + B + BC \quad [AB + AB = AB]$$

$$= AB + AC + B \quad [B + BC = B]$$

$$= B + AC \quad [AB + B = B]$$

(Ans.)

$$\text{ii. } [A\bar{B}(C+BD) + A\bar{B}]C$$

$$= [ABC + A\bar{B}BD + A\bar{B}]C$$

$$= (ABC + A\cdot 0\cdot D + A\bar{B})C \quad [B\bar{B} = 0]$$

$$= (ABC + 0 + A\bar{B})C$$

$$= (A\bar{B}C + A\bar{B})C$$

$$= A\bar{B}CC + A\bar{B}C$$

$$= A\bar{B}C + A\bar{B}C \quad [\text{Distributive law}]$$

$$= BC(A+A)$$

$$= BC \cdot 1$$

$$= BC$$

$$[A+A=1]$$

both given

both given

both given

$\textcircled{*}$ $F_3 = x'y'z + x'y.z + xy'$

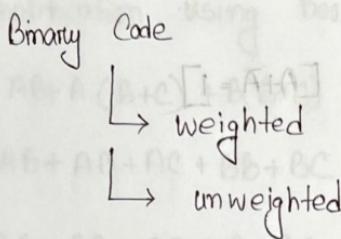
$$0\ 0\ 1 \quad 0\ 1\ 1 \quad 1\ 1\ 0$$

	x	y	z	F_3
0	0	0	0	0
1	0	0	1	1
2	0	1	0	0
3	0	1	1	1
4	1	0	0	1
5	1	0	1	0
6	1	1	0	0
7	1	1	1	0

Excess - 3 code

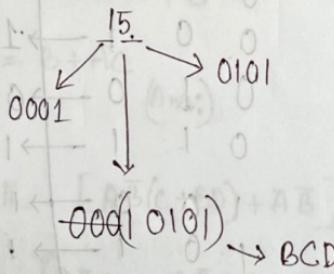
Decimal + 3

Decimal



Digit (0-9)
Number 10²

BCD (Binary - Coded Decimal) or 8,4,2,1 Code



Excess - 3 Code :-

Decimal + 3 then ये असूत अंकों का एक Binary

2,4,2,1 Code :- The 2,4,2,1 Code is the same as that in BCD from 0 to 4; it varies from 5 to 9.

Decimal

2 4 2 1 code

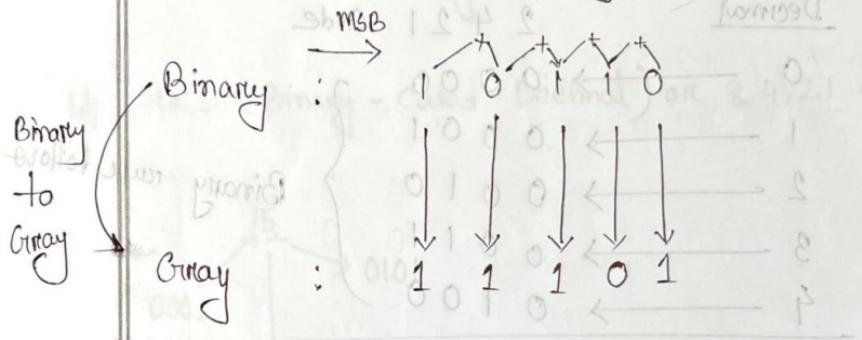
0	\rightarrow	0 0 0 0	<u>Binary rule follows</u>
1	\rightarrow	0 0 0 1	
2	\rightarrow	0 0 1 0	
3	\rightarrow	0 0 1 1	
4	\rightarrow	0 1 0 0	

5	\rightarrow	1 0 1 1	<u>MSB form</u>
6	\rightarrow	1 1 0 0	
7	\rightarrow	1 1 0 1	
8	\rightarrow	1 1 1 0	

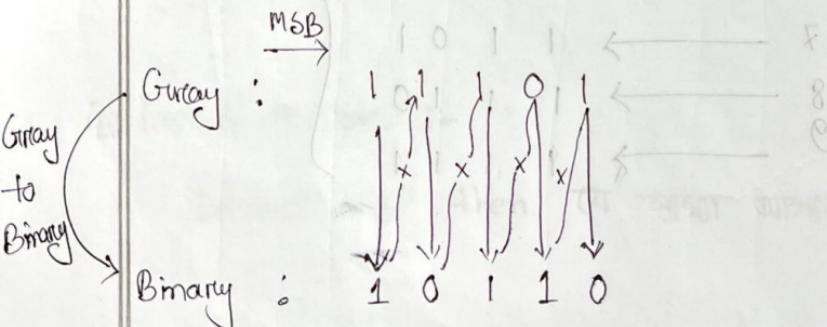
0 1 1 0 1

Coding & Conversion :-Table Design

Full

Q. The Reflected Code / Gray Code :-

$$(10110)_2 = (11101) \text{ Gray}$$



Parity Bit :- total number of 1's then extra bit add.

say message :- 10110 —

Odd parity :- $P(\text{odd}) : 0$

even parity :- $P(\text{even}) : 1$

Hamming Code :- \circledast Only one bit change detector.

\circledast Can't detect if more than one bit

change.

1. Determine the Single error correcting code for

• 101110110, L hamming

Solution :- the number of data bits in the message, $n=9$. we can obtain the required no. of parity bits (P) from the following formula :

$$2^P \geq n+P+1$$

$$\text{if } P=1, 2^1 \geq 9+1+1 \text{ (false)}$$

If $P = 2$, $2^1 2 >= 9 + 2 + 1$ (false)

If $P = 3$, $2^1 3 >= 9 + 3 + 1$ (false)

If $P = 4$, $2^1 4 >= 9 + 4 + 1$ (true)

So, $P = 4$

We have to send total $m+n = 9+4 = 13$ bit message.

Bit position: 1 2 3 4 5 6 7 8 9 10 11 12 13

values: (P_1) (P_2) 1 (P_3) 0 11 (P_4) 1 0 11 0

Position	0	0	1	1	0
	0	1	1	0	6
	0	1	1	1	7
	1	0	0	0	11
	1	0	0	0	12

~~(XOR)~~ 1 1 0 $101 + 11 = 1010$

P_4 $(P_3) + P_2 + 1 = P_1 \leftarrow$ LSB

Ques. 1010001110

$$n = 10$$

$$2^P >= n + P + 1$$

$$\text{if } P = 1, 2^1 >= 10 + 1 + 1 \text{ (false)}$$

$$P = 2, 2^2 >= 10 + 2 + 1 \text{ (false)}$$

$$P = 3, 2^3 >= 10 + 3 + 1 \text{ (false)} \leftarrow \text{Ans}$$

$$P = 4, 2^4 >= 10 + 4 + 1 \text{ (true)}$$

$$\text{So, } P = 4 \\ \text{we have to send, } m + n = 10 + 4$$

$$1 - 14 \text{ bits are required}$$

Bit position :-

1 2 3 4 5 6 7 8 9 10 11 12 13 14

P ₁	P ₂	P ₃	P ₄	0	0	1	0	0	1	1	1	0
0	0	1	0	1	0	0	1	0	0	1	0	0
0	0	0	0	0	0	0	0	0	0	1	1	0
1	1	1	0	0	0	0	0	0	0	1	1	1
0	0	0	0	0	0	0	0	0	0	1	1	1
1	1	0	0	0	0	0	0	0	0	1	1	1
0	0	0	0	0	0	0	0	0	0	0	0	0

Topic Name : _____

Day : _____

Time : _____

Date : / /

0	0	1	0	1	3
0	1	1	0	0	6
1	0	1	1	1	11
1	1	0	0	0	12
1	0	0	1	1	13

XOR → $P_4 \oplus P_3 \oplus P_2 \oplus P_1 = 1 \oplus 1 \oplus 0 \oplus 1 = 1$ ← LSB

The sending Message Code will be : - 11110101000110

Receiving End :- Case - 1

0	0	0	1	1	1
0	1	0	1	0	2
0	0	1	1	1	3
0	1	0	0	0	4
0	1	1	1	0	6
1	0	0	0	0	8
1	0	1	1	1	11
1	1	0	0	0	12
1	1	0	1	1	13

XOR → 0 0 0 0 no error

Case - 2

If there is an error in the 5th position while transmitting the receiver will get:

11111101001110

0	0	0	1	1
0	0	1	0	2
0	0	1	1	3
0	1	0	0	4
0	1	0	1	5
0	1	1	0	6
1	0	0	0	7
1	0	1	1	8
1	1	0	0	9
1	1	0	1	10
1	1	1	0	11
1	1	1	1	12
1	1	0	1	13

$\text{XOR} \rightarrow 0 \quad 1 \quad 0 \quad 01$

All boolean expression can be converted into either of two standard forms:-

a. The Sum-of-products (SOP)

b. The product of sum (POS) [ফিল্টার সুম
বাইটেন্ড প্রোডুক্ট]

Canonical Form :-

a Sum of minterms.

a product of maxterms.

$$F = \overbrace{x'y'z + x'yz + xy'z + xyz}^{\text{SOP}}$$

$$F(x,y,z) = \sum(1, 3, 4, 5)$$

$$\rightarrow F = \sum(1, 3, 4, 5)$$

Topic Name : _____

Day : _____

Time : _____

Date : / /

$$\textcircled{A} \quad F = \sum (0, 2, 5, 7)$$

Practice

$$\sum (000, 010, 101, 111)$$

$$F = x'y'z' + x'y'z + xy'z + xyz$$

x	y	z	F
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	0
1	0	1	1
1	1	0	0
1	1	1	1

min-term \rightarrow दिए गए input का अनुसार output 1 calculate

max-term \rightarrow दिए गए input का अनुसार output 0 calculate
↓

0 थार्डले prime होते हैं & 1 थार्डले prime

\rightarrow 0 थार्डले prime & 1. 2 थार्डले not prime

Boolean to POS \rightarrow

1. First use Distributive law

2. missing variable P, add PP'

3. All the variable in POS term.

	X			
	0	0	0	0
	1	0	0	0
	0	0	0	0
	1	1	1	1

Minterm Complement Maxterm

$$F(x, y, z) = 1 \text{ minterms}$$

$$= \sum(0, 1, 2, 3, 4, 5, 6, 7)$$

$$= \prod(NIL)$$

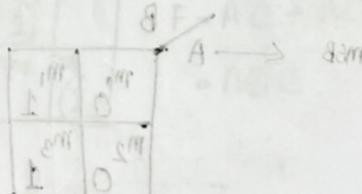
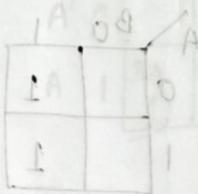
$$(0, 1) \otimes = 7$$

$$\beta A + \beta' A = 7$$

$$(\beta + \beta') \beta =$$

$$\beta =$$

	1	0	A
0	0	0	0
1	1	1	0
0	0	0	1
1	1	1	1



Chapter - 3

Karnaugh Map (K-Map)

2, 3, 4, 5, 6Variable ~~Min~~ Use करा याएं K-map

$Growth L = (S, L, R)^T$

$(J, I, A) \pi =$

Truth-table

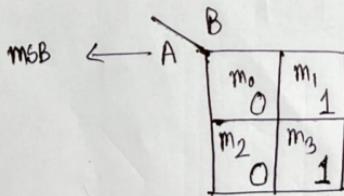
A	B	F
0	0	0
0	1	1
1	0	0
1	1	1

$F = \Sigma(1, 3)$

$F = A'B + AB$

$= B(A' + A)$

$= B$

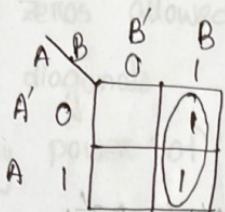
K-map cell $\rightarrow 2^n$ Here n is input variable.

A	B	0	1
0	0	1	
1		1	

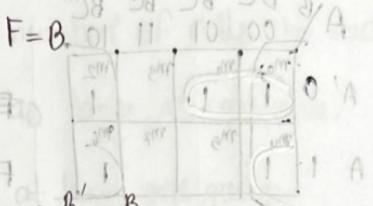
 $\rightarrow 0$ निष्पत्ति
 1 निष्पत्ति

$2^n = 1, 2, 4, 8, 16, 32 \dots$

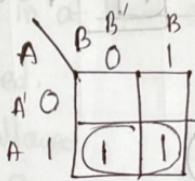
Group



$$F = \Sigma(1,3)$$



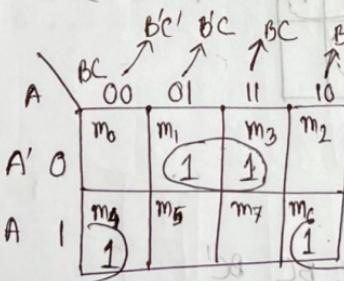
$$F = \Sigma(2,3)$$



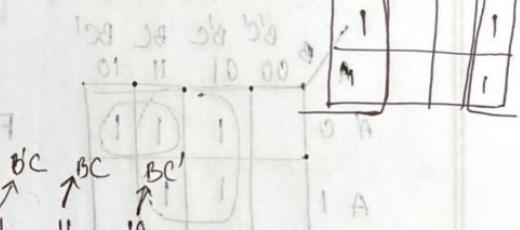
$$F = A$$

First Grouped

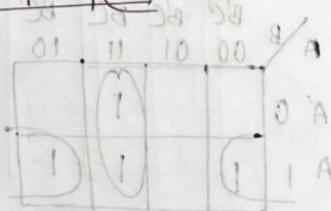
$$\textcircled{1} \quad F(A, B, C) = \Sigma(1, 3, 4, 6)$$



$$F = A'C + AC' \\ = A \oplus C$$



$$1'A + 1B = 7$$

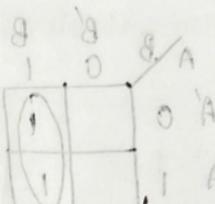


(2)

$$F = \sum (0, 1, 2, 4, 6)$$

(E, I) 3 = 4

		$B'C'$	$B'C$	BC	BC'
		00	01	11	10
A'	0	m_1	m_2	m_3	m_4
	1	m_5	m_6	m_7	m_8
A	1	1	1	1	1



$$F = A'B' + AC'$$

$$F = C' + A'B'$$

(E, S) 3 = 7

$$F = \sum (1, 2, 3, 5, 7)$$

		$B'C'$	$B'C$	BC	BC'
		00	01	11	10
A'	0	1	1	1	1
	1	1	1	1	1
A	1	1	1	1	1

$$F = C + A'B = \sum (1, 3)$$

(4)

$$F = \sum (3, 4, 6, 7)$$

		$B'C'$	$B'C$	BC	BC'
		00	01	11	10
A'	0	D		1	1
	1	1	1	1	1
A	1	1	1	1	1

$$F = BC + AC'$$

- * No zeros allowed.
 - * No diagonals.
 - * Only powers of '2 numbers' of cells in each group
 - * Groups should be as large as possible.
 - * Everyone must be in at least one group.
 - * Overlapping allowed.
 - * Wrap around allowed.
 - * Fewest number of groups possible.

4 Variable K-Map

	00	01	11	10	
AB\CD	C'D'	C'D	CD	CD'	
00	m ₀	m ₁	m ₃	m ₂	
01	A'B	m ₄	m ₅	m ₇	m ₆
11	AB	m ₁₂	m ₁₃	m ₁₅	m ₁₄
10	AB'	m ₈	m ₉	m ₁₁	m ₁₀

(i) $F(w, x, y, z) = \sum(0, 1, 2, 4, 5, 6, 8, 9, 12, 13, 14)$

(ii) $F(A, B, C, D) = \sum(0, 1, 2, 5, 8, 9, 10)$

(iii) $F(A, B, C, D) = \prod(3, 4, 6, 7, 11, 12, 13, 14, 15)$

Practice :-

(i)

wx'yz'	00	01	11	10
w'xz'	1	1		1
w'x	1	1		1
wx	1	1		
wx'	1	1		

$$F = y' + w'z' + wx'$$

(ii)

	CD	$C'D'$	$C'D$	CD	$C'D'$
AB	00	00	01	11	10
AB'	00	1	1		1
A'B	01				
AB	11				
AB'	10	1			

$$F = B'D' + B'C + A'C'D$$

$$(C \cdot 0) \Rightarrow 0$$

(iii)

	$C+D$	$C+D'$	$C'+D'$	$C'+D$
AB	00	01	11	10
$A+B'$	00	0	0	0
$A+B'$	01	0	0	0
$A+B'$	11	0	0	0
$A'+B$	10	0	0	0

$$F = (C'+D') (A'+B') (B'+D)$$

★ Don't Care Conditions ($'d'$ /' x ')

$$F = \sum (1, 3, 7)$$

$$F = \sum (0, 5)$$

input : BCD digit 4 bit
(0-9)

01	11	10	00	01	00	00	10	11	01
00	00	00	00	00	00	00	00	00	00
10	00	00	00	00	00	00	00	00	00
11	00	00	00	00	00	00	00	00	00
01	00	00	00	00	00	00	00	00	00

Minterm \rightarrow don't care
consider 1

Output : Excess-3 Code

4 bit (12)

01 11 10 00

Maxterm \rightarrow don't care

consider 0

A	BC	$B'C'$	$B'C$	BC	BC'
A' 00	d	1	1	1	1
A 01	d	d	1		

$$F = C$$

$$(0+A)(0+A) (0+D) = F$$

Solve

Five - variable K-map :-

		CDE	000	001	011	010	110	111	101	100	
		AB	m ₀	m ₁	m ₃	m ₂	m ₆	m ₅	m ₇	m ₄	
		00	m ₈	m ₉	m ₁₁	m ₁₀	m ₁₄	m ₁₅	m ₁₃	m ₁₂	000
		01	m ₂₄	m ₂₅	m ₂₃	m ₂₆	m ₃₀	m ₃₁	m ₂₉	m ₂₈	100
		10	m ₁₆	m ₁₇	m ₁₉	m ₁₈	m ₃₂	m ₃₃	m ₂₁	m ₂₀	110
		11									010
		11									011
		01									001
		00									

$$F = \sum (0, 2, 4, 6, 9, 11, 13, 15, 17, 21, 25, 27, 29, 31)$$

AB CDE C'D'E' C'DE' C'DE C'DE' CDE C'D'E C'D'E'

A'B'	1			1	1			1	
A'B		1	1			1	1		
AB		1	1			1	1	1	
AB'			1						
AB			1						

$$F = A'B'E' + BE + ADE$$

Q1

6-variable K-Map :-

ABC \ DEF	000	001	011	010	110	111	101	100
000	m_0	m_1	m_3	m_2	m_6	m_7	m_5	m_4
001	m_8	m_9	m_{11}	m_{10}	m_{14}	m_{15}	m_3	m_{12}
011	m_{24}	m_{25}	m_{27}	m_{26}	m_{30}	m_{31}	m_{20}	m_{28}
010	m_{16}	m_{17}	m_{19}	m_{18}	m_{20}	m_{23}	m_{21}	m_{20}
110	m_{48}	m_{49}	m_{51}	m_{50}	m_{54}	m_{55}	m_{53}	m_{52}
111	m_{56}	m_{57}	m_{59}	m_{58}	m_{62}	m_{63}	m_{61}	m_{60}
101	m_{40}	m_{41}	m_{43}	m_{42}	m_{46}	m_{47}	m_{45}	m_{44}
100	m_{32}	m_{33}	m_{35}	m_{34}	m_{38}	m_{39}	m_{37}	m_{36}

$$F = \sum (6, 9, 13, 18, 10, 25, 27, 29, 41, 45, 57, 61)$$

ABC \ DEF	000	001	011	010	110	111	101	100
000	1				1			
001		1					1	
011		1						
010			1	1				
110								
111			1				1	
101			1					
100								

$$F = C'E'F + A'B'C'DE'F + A'BD'E'F + A'B'C'D'E$$

Chapter 4 (Combinational Logic)

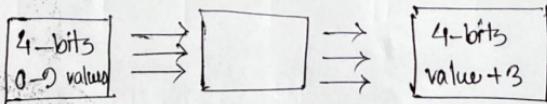
- ★ Present combination of inputs without regard to previous inputs.

Design procedure of Combinational logic circuit :-

- ① Determine input variables.
- ② Determine output variables.
- ③ Derive the truth table.
- ④ Boolean expression / K-map \rightarrow each output.
- ⑤ Produce the required circuit and verify it.

- ★ BCD digit to Excess -3

$(0-9) \left\{ \text{any digit } 8 \text{ digit } (0-9) \rightarrow \text{of fixed } 4 \text{ bit max} \right.$



* Design a 2-bit cube (Circuit) Ans: Q1

A	B	F_0	F_1	F_2	F_3	F_4	F_5	F_6	F_7
0	0	0	0	0	0	0	0	0	0
0	1	0	0	0	0	0	1	0	0
1	0	0	1	0	0	0	0	0	0

→ 2-bit binary input to 3-bit output

3-bit Cube

• addition logic - part 1 Q2

• addition logic - part 2 Q3

A	B	C	F_0	F_1	F_2	F_3	F_4	F_5	F_6	F_7
0	0	0	0	0	0	0	0	0	0	0
0	0	1	0	1	0	0	0	1	0	0

Cricket A 4 & 6 या असे

light असे

• addition logic - part 3 Q4

0 1 1 → 0

1 0 0 → 1

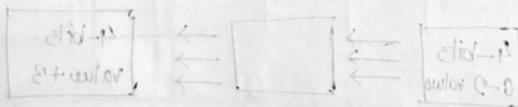
1 0 1 → 0

1 1 0 → 1

• addition of 1-bit Q5

↓

↑
कॉर्ट

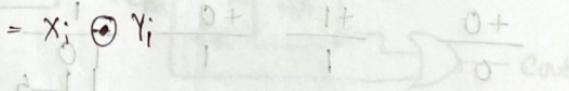


Magnitude Comparators :-1 bit

<u>input</u>	<u>Output</u>	$F_1(x_i > y_i)$	$F_2(x_i = y_i)$	$F_3(x_i < y_i)$
$x_i \quad y_i$		0	1	0
0 0		0	0	1
1 0		1	0	0

$$F_1(x_i > y_i) = x_i y_i'$$

$$F_2(x_i = y_i) = x_i' y_i + x_i y_i'$$



$$F_3(x_i < y_i) = x_i' y_i$$

Half Subtraction

$$\begin{array}{r} 0 \\ - 0 \\ \hline 0 \end{array}$$

$$\begin{array}{r} 1 \\ - 0 \\ \hline 1 \end{array}$$

i^y	i^x
0	0
1	0
0	1
1	1

$$x = x_2 \oplus x_1$$

$$y = y_2 \oplus y_1$$

$$f_1(x > y) = x_2 > y_2 + (x_2 = y_2)(x_1 > y_1)$$

$$f_1 = x_2' y_2' + (x_2 \odot y_2) x_1' y_1$$

$$(i) (x > y) = (x_2 > y_2) + (x_2 = y_2)(x_1 > y_1)$$

$$= (x_2 \odot y_2) (x_1 \odot y_1)$$

$$f_2(x == y) = (x_2 = y_2)(x_1 = y_1)$$

$$= x_2' y_2 + (x_2 \odot y_2) x_1' y_1$$

$$\begin{array}{r} 0 \\ + 0 \\ \hline 0 \end{array} \quad \begin{array}{r} 0 \\ + 1 \\ \hline 1 \end{array} \quad \begin{array}{r} i \\ + 0 \\ \hline i \end{array} \quad i = (i_2 = i_1)$$

Half adder:-

x_i	y_i	$Cout$	S
0	0	0	0
0	1	0	1
1	0	0	1
1	1	1	0

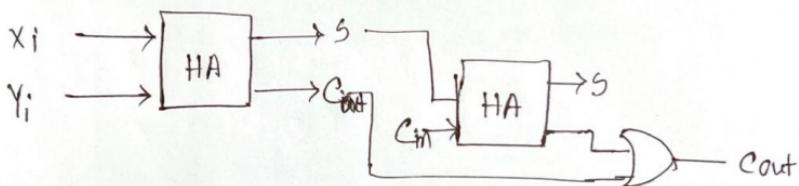
$$i = (i_2 = i_1)$$

$Cout$

$(i > y)$

Full adder

<u>A</u>	<u>B</u>	<u>C_{in}</u>	<u>C_{out}</u>	<u>S</u>
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	0	1

Half subtractor

$$\begin{array}{r}
 0 & 0 & 1 & 1 \\
 -0 & -1 & -0 & -1 \\
 \hline
 0 & 11 & 1 & 0
 \end{array}$$

* एक full adder किसे 3 bit तरह कहा जाता है।

Ripple Carry effect \rightarrow एक full adder का

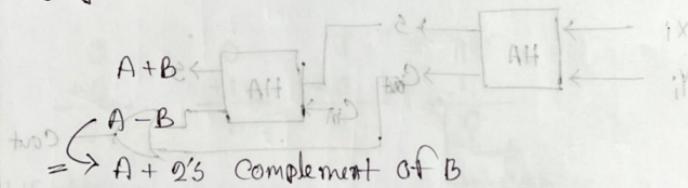
addition को कैसे depend करता है, ताकि slows होते जाएँ।

CLA (Carry Loop Adder)

$$\text{Carry Propagate} \leftarrow P_i = A_i \oplus B_i$$

$$G_i = A_i B_i$$

Carry generate



not generated bits

1	1	0	0
1	0	1	0
0	1	1	1

BCD Adder :-

যদি BCD digit যাই যোগ করা হচ্ছে (in parallel)

$$A(\text{BCD digit}) + B(\text{BCD digit})$$

$$= \text{SUM (BCD)}$$

$$\text{Maximum output } (9+9)+1 = 10$$

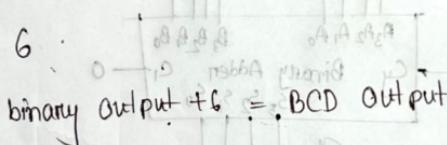
$$10 = 1 + 2^3$$

	1	0	1
1	1	1	0
1	1	0	1
1	0	1	1
1	1	1	1

if carry = 1

binary output এর যোগ আঁকা আবশ্যিক BCD output খুব যাবে

সময়ে



$$\text{binary output} + 6 = \text{BCD output}$$

6 যোগ করা যাবে যখন Output 9 প্রস্তুত হবে।

$$\text{if } (\text{sum} >= 10)$$

$$\text{sum} += 6$$

else

$$\text{sum} += 0$$

→ সময়ের ওপর যোগ করা হবে।
যাইহোক 6 যোগ করা জাতের না 0.

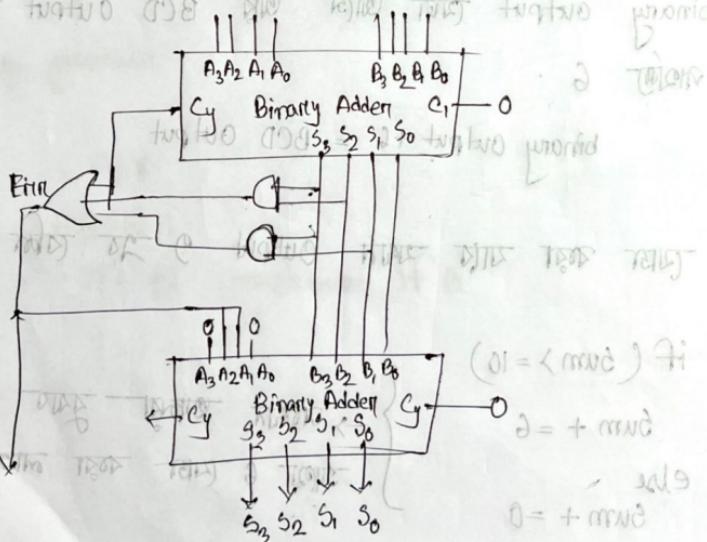
Carry out as value 1 হলে G যোগ করব।
 (assuming mi) $(H_{10} \oplus H_{11}) + (H_{11} \oplus H_{12})$
 (Carry out value 1 হলে 16, 17, 18 গুরুত্ব।
 $(H_{10} \oplus H_{11})A + (H_{11} \oplus H_{12})B$

		E _{rrr}
10 10		1
10 11		1
11 00		1
11 01		1
11 10		1
11 11		1

\rightarrow K map (A + C) তাহার মানিখন

thus if

$$E_{rrr} = S_3 S_2 + S_3 S_1$$

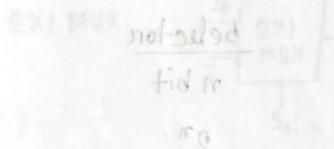
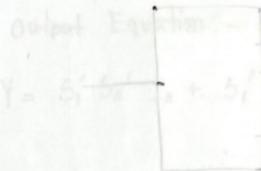


Switch Controlled adder A Subtractor

$$\begin{array}{l} S=0 \longrightarrow A+B \\ S=1 \longrightarrow A-B \end{array}$$

$$6+3=0$$

$6-3=3$ two bits from borrow



$R_0 \leftarrow$ serial borrow

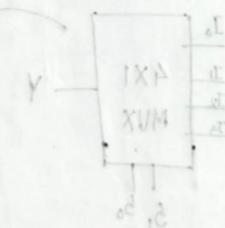
serial borrow sign bit \leftarrow

serial not selected \leftarrow

$$R = \bar{S} \leftarrow + \text{id } S$$

$$\begin{array}{r} S \\ \times \\ S \\ \hline 0 & 0 \\ 1 & 0 \\ 0 & 1 \\ 1 & 1 \end{array}$$

XUM IXA 00 tuperi w/ S



Sum

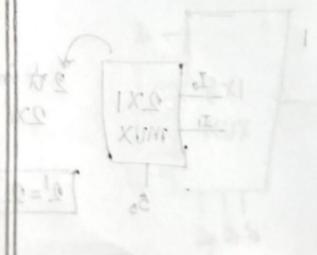
The system $S \leq 0$ not selected

$$D + S$$

$R = \text{not selected}$

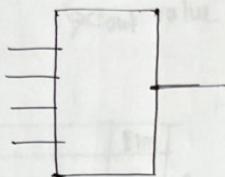
serial borrow \leftarrow $D \oplus S$

serial borrow total \leftarrow



題

MULTIPLEXERS / MUX / DATA SELECTORS



$$\begin{aligned} S_1 + S_0 &\leftarrow 0 = C \\ S_1 - S_0 &\leftarrow 1 = C \\ 0 = S_1 + S_0 \end{aligned}$$

input অনেক হলে পাই but output কম।

\Rightarrow input lines $\rightarrow 2^n$

\Rightarrow Single output line.

\Rightarrow n selection lines.

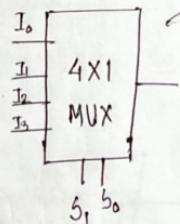
selector

n bit

2^n

S_1	S_0
0	0
0	1
1	0
1	1

$$2 \text{ bit} \rightarrow 2^2 = 4$$

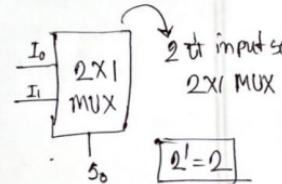


4 bit input so 4x1 MUX

$[n \neq 0]$ Selector 0 হলে নিচের হল।

$$\text{Selector} = n$$

$(2^n) \times 1 \rightarrow$ output line
 ↓ total input line



⇒ Function Table :- 4×1 MUX

S_1	S_0	Y
0	0	I_0
0	1	I_1
1	0	I_2
1	1	I_3

Output Equation :- $(S_1, S_0) =$

$$Y = S_1' S_0' I_0 + S_1' S_0 I_1 + S_1 S_0' I_2 +$$

$$S_1 S_0 I_3$$

XUM $[4 \times 1] \leftarrow [1 \times 4]$

⇒ 2×1 MUX



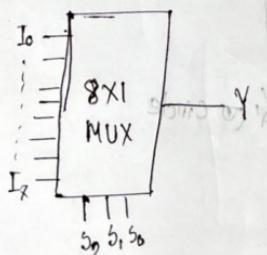
$$S_0 (2, 3, 4, 1) \rightarrow (3, 8, 1) =$$

S_0	Y
0	I_0
1	I_1

XUM

$$Y = S_0' I_0 + S_0 I_1$$

⇒ 8×1 MUX



S_2	S_1	S_0	Input 8
0	0	0	A
0	0	1	B
0	1	0	C
0	1	1	D
1	0	0	E
1	0	1	F
1	1	0	G
1	1	1	H

$2^3 = 8 \rightarrow$ input 8
 $n = 3 \rightarrow$ selector

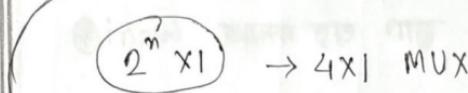
Q

Function implementation using MUX

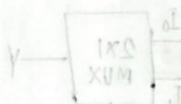
$$F(A, B, C)$$

$$n+1 = 3 \Rightarrow n = 2$$

	A'	A
0	0	0
1	1	0
2	0	1
3	1	1



Selector $\rightarrow 2$



XOR IXS

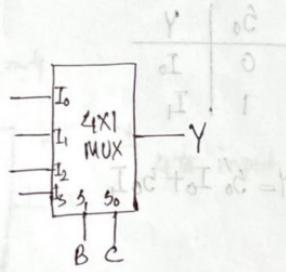
M6B

$$F(A, B, C) = \sum(1, 3, 5, 6)$$



selector

LGB फॉर्म रख



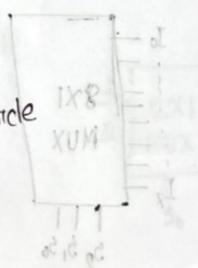
XOR IXS

MUX input line	I_0	I_1	I_2	I_3
A'	0	1	2	3
A	4	5	6	7
Input values	0	1	A	A'

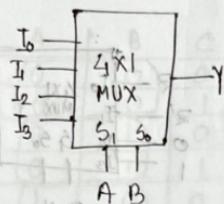
1st circle
 \oplus
2nd circle

$A \oplus$
Circle

$A' \oplus$ Circle



→ If A, B as selector (X, S, S, S) Z = (S, S, A)

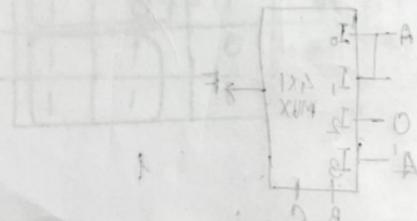


A	B	C ₁	C ₀
0	0	0	0
1	0	1	1
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	0

MUX input line	I ₀	I ₁	I ₂	I ₃
C ₁	0	2	4	6
C	1	3	5	X
Input Values	C	C	C	C

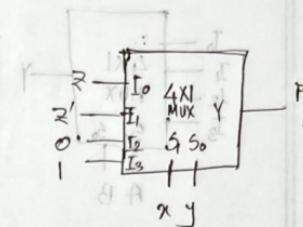
XUM XA Brieu (D, S, S, 0) Z = (D, S, A) (ii)

Brieu (D, S, S, 1, 0, 0, 0, 1, 0) Z = (D, S, A) (iii)



Q1 $F(x, y, z) = \sum (1, 2, 6, 7)$ Using 4x1 MUX

x	y	z	F
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	1



Sequence
follow
का सोल्यू
तो को सोल्यू
तो

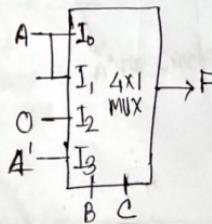
Implementation the following boolean expressions:-

(i) $F(A, B, C) = \sum (2, 3, 6, 7)$

(ii) $F(A, B, C) = \sum (0, 2, 5, 6)$ using 4x MUX

(iii) $F(A, B, C, D) = \sum (0, 1, 5, 6, 8, 10, 12, 15)$ using 8x1 MUX

(iv) For the given multiplexer CKT. determine the logic function.



Soln :-

$$(i) F(A, B, C) = \sum(2, 3, 6, 7)$$

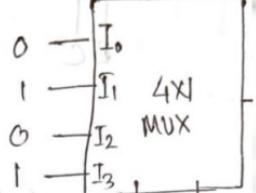
A	B	C	F
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	1

$$\} \rightarrow F = 0$$

$$\} \rightarrow F = 1$$

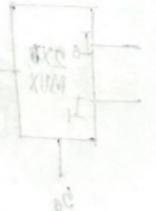
$$\} \rightarrow F = 0$$

$$\} \rightarrow F = 1$$

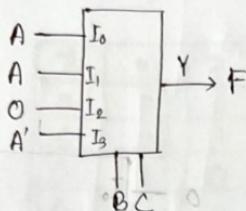


$$(ii) F(A, B, C) = \sum(0, 2, 5, 6)$$

A	B	C	F
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	0

 $\rightarrow c'$ $\rightarrow c'$ $\rightarrow c$ $\rightarrow c$ $\rightarrow c'$ 

(iv) Solve :-

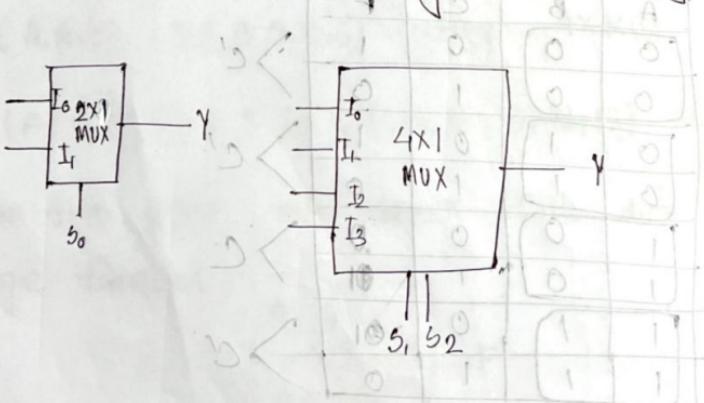


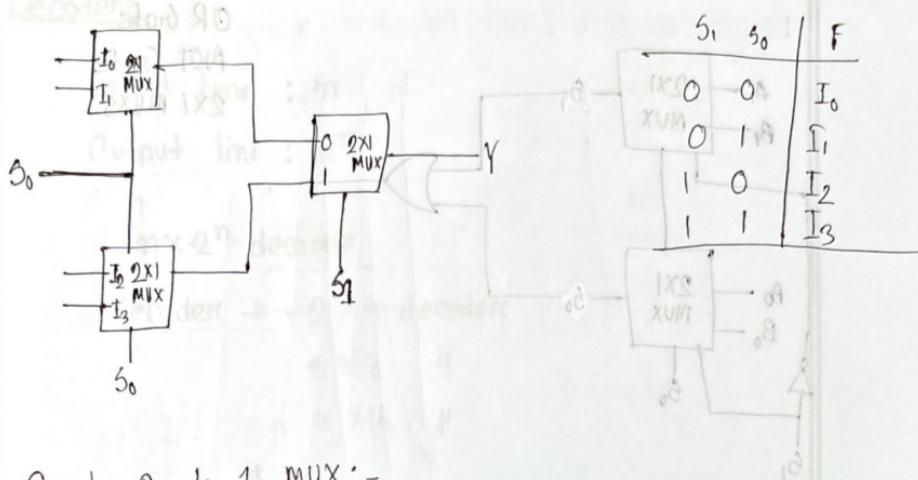
$$\begin{aligned}
 F &= B'C'A + B'CA + BCA' \\
 &= AB'C' + AB'C + A'BC \\
 &= \sum(4, 5, 3) \\
 &= \sum(3, 4, 5)
 \end{aligned}$$

$$\text{F} = (B, C) | F = (3, 4, 5) \quad (ii)$$

B	C	F	A
0	0	0	0
0	1	1	0
1	0	0	1
1	1	1	1

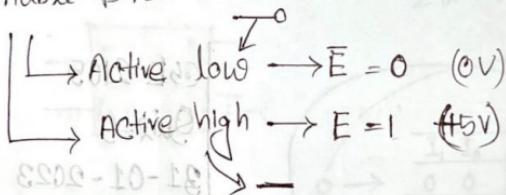
Q. Construct a 4x1 MUX using 2x1 MUX Only.



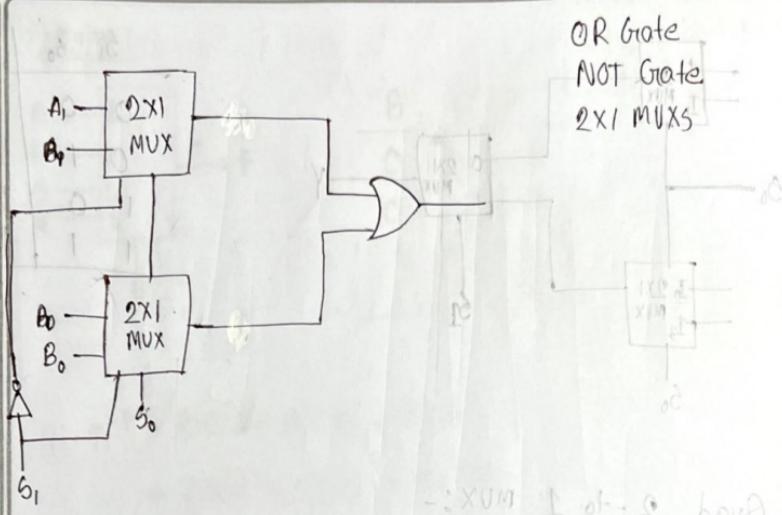


Quad 2-to-1 MUX :-

Enable pin



* Construction of 4x1 MUX using two 2x1 MUX, enable pin & basic gate(s).



OR Gate

NOT Gate

2x1 MUX

XOR 1 of 2 board

reg address

(V0) 0 = 3 ← B0

(V1) 1 = 3 ← B1

CBSE 2105

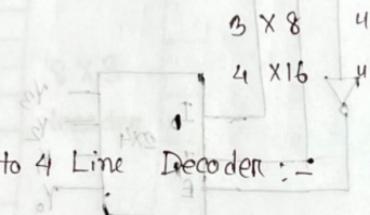
Quiz-3

31-01-2023

TUESDAY

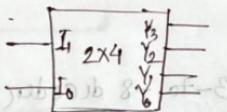
Chapter-4

XII IX D 007 prior XOR IX D
(a) show how to reg address

Decodersinput line : m, I_1, I_2 Output line : 2^n $n \times 2^n$ decoderdecoder :- 2×4 decoder

2 to 4 Line Decoder :- (selector 2 bit input)

2 bit input 4 bit output



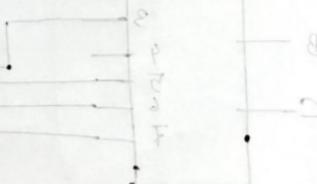
Truth Table for 2-to-4 Line Decoder

	I ₁ , I ₂	Y ₃	Y ₂	Y ₁	Y ₀
0 →	0 0	0	0	0	1
1 →	0 1	0	0	1	0
2 →	1 0	0	1	0	0
3 →	1 1	1	0	0	0

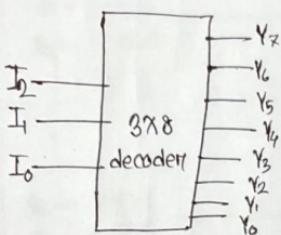
{ Active High → 1 use 25 }

{ Active low → 0 use 25 }

High Priority

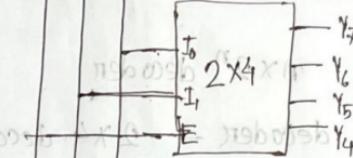


Design a 3x8 Line Decoder using 2x4 Decoders



I_2, I_1, I_0 : mid trigno

I_2, I_1 : mid trigno



(mid trigno reduce)

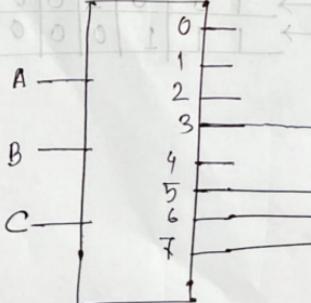
trigno to trigno trigno

Q4

$F = \sum(3, 5, 6, 7)$ using

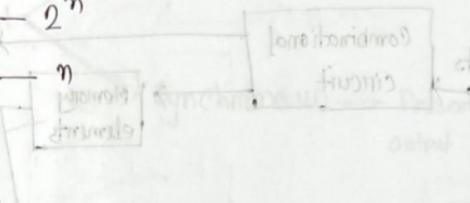
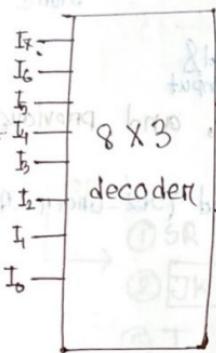
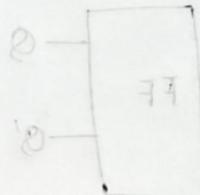
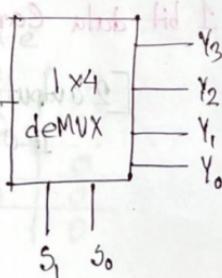
	0	1	2	3	4	5	6	7
1	0	0	0	0	0	0	0	0
0	1	0	0	1	0	0	1	0
0	0	1	0	0	1	0	0	1
0	0	0	1	0	0	1	0	0

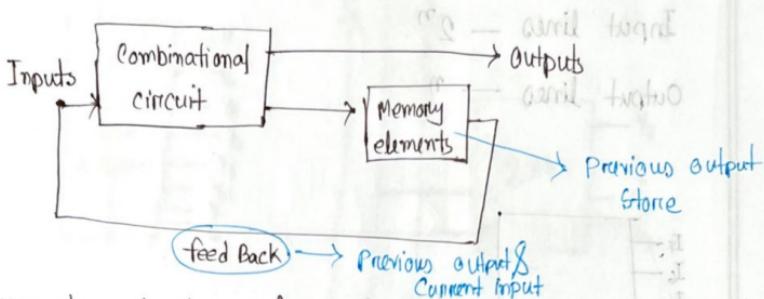
3-to-8 decoder



But for active low
we need to use
NAND Gate

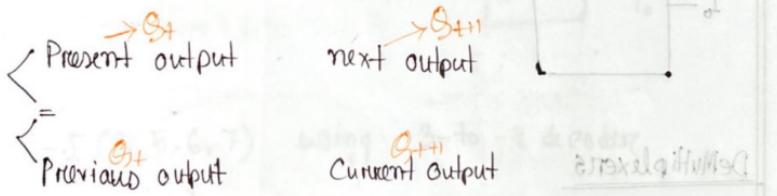
active low \leftarrow digit switch
active high \leftarrow word switch

EncoderInput lines $\rightarrow 2^n$ Output lines $\rightarrow n$ DeMultiplexers

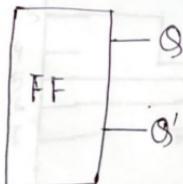
Chapter - 5 (Synchronous Sequential Logic)

$$\text{Present output} = f(\text{Present input}, \text{and previous output})$$

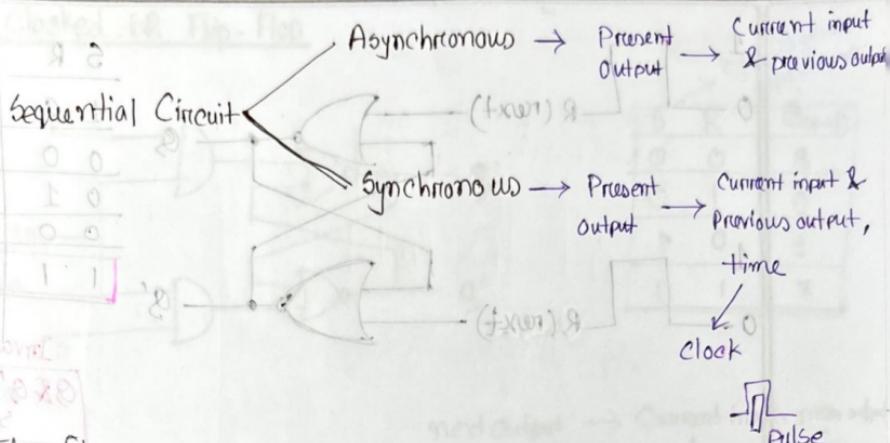
④ Input in order that output will be in order of 2ⁿ



FLIP FLOP (FF) → Only 1 bit data can store



[2 outputs provide:
 If one is Q & another
 its not]

Flip-Flop

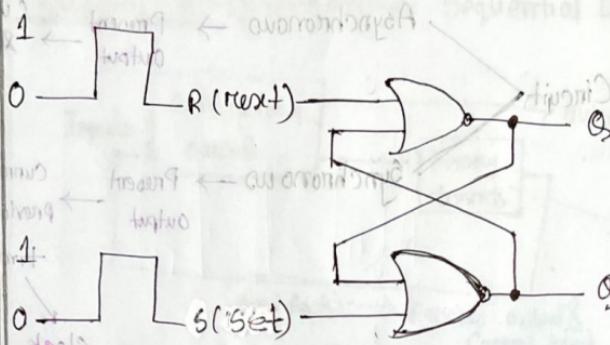
- ① SR Flip-Flop
- ② JK Flip-Flop → LAB available
- ③ T flip-flop
- ④ D flip-flop

Basic Flip-flop Circuit

NOR Gate

A	B	F
0	0	1
0	1	0
1	0	0
1	1	0

2 NAND Gate or two NOR Gate
can use to construct .



S	R	Q	Q'
1	0	1	0
0	0	1	0
0	1	0	1
0	0	0	1
1	1	0	0

Invalid State
 $Q \& Q'$ can't be same

q011-q111 ①
 addition 811 ← q011-q111 ②
 next q011-q111 + 1 ③
 q011-q111 ④

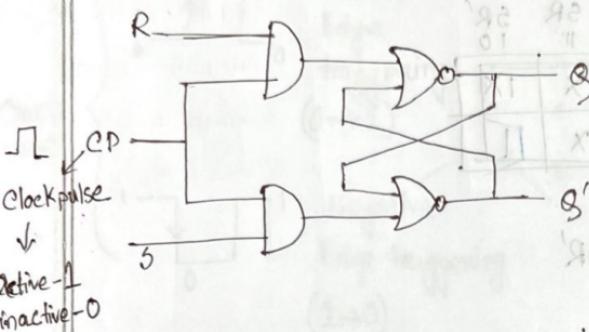
Carry output

q011-q111 carry

start with no carry

fourth bit goes to 0

S	R	A
1	0	0
0	1	0
0	0	1
0	1	1

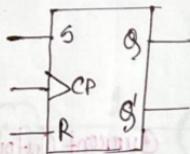
Clocked SR Flip-Flop

logic diagram dependent

S	R	$Q(t+1)$
0	0	0
0	1	0
1	0	1
1	1	X

$Q(t+1) = Q(t)$

next output \rightarrow Current input, prev output



(S, R) \rightarrow (Q(t+1)) \rightarrow (Q(t)) \rightarrow (S, R)

$S, R \rightarrow Q_t \rightarrow Q_{t+1} \rightarrow S, R$

Q	S	R	$Q(t+1)$
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	indeterminate X
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	indeterminate X

$Q(t+1)$ is dependent on S, R
 $Q(t+1)$ always 0
 SR both can't be 1
 $Q(t+1)$ value always 1
 $Q(t+1)$ value always 0

Topic Name :

K-map use :-

S'	R	SR	SR'	$S'R$	SR'
S	0			X	1
S	1	1		X	1
1					

$$\mathcal{G}_{(t+1)} = \mathcal{G}_t + \mathcal{G} R'$$

Most important

SR Flip-Flop (excitation table)

\mathcal{S}_+	$\mathcal{S}_{(t+1)}$	S	R
0	0	0	X
0	1	1	0
1	0	0	1
1	1	X	0

Current Output

desired Output

87

84+1

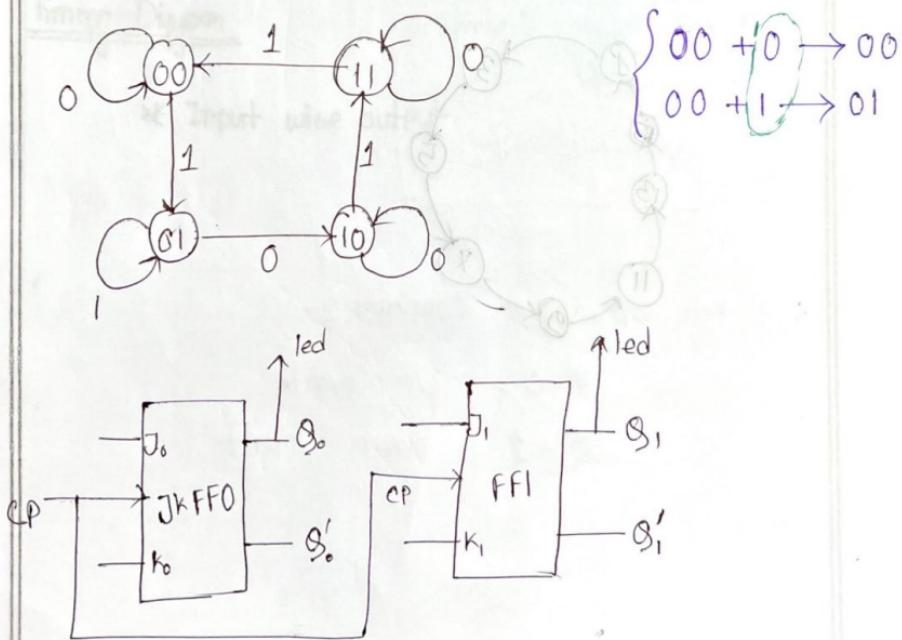
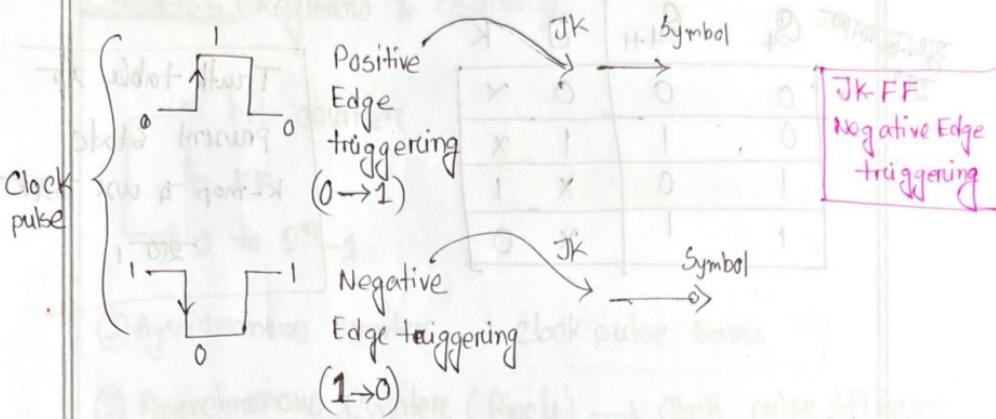
R यार value 0/1 तरामाता द

୨୦ ମାତ୍ର

→ 5 तक value 0/

Page 111

1990-1991



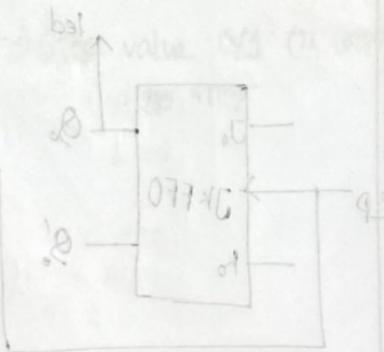
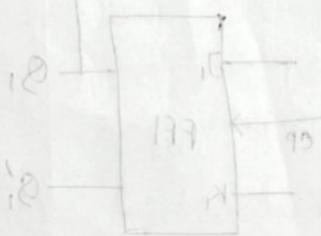
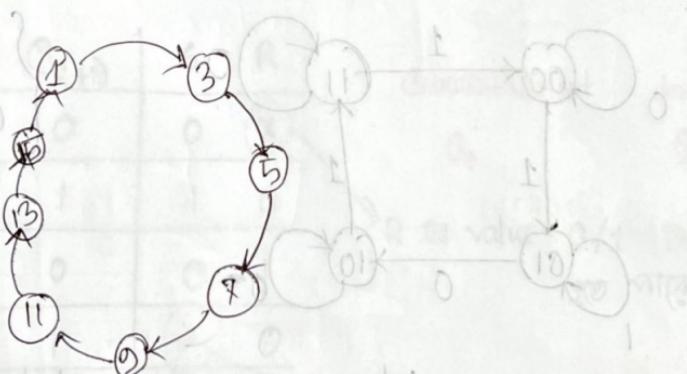
S_t	S_{t+1}	J	K
0	0	0	x
0	1	1	x
1	0	x	1
1	1	x	0

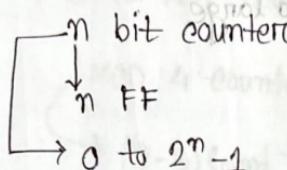
Truth table

Present state

K-map \rightarrow use ~~use~~ ~~simplifying~~ ~~simplifying~~LAB

4-bit odd counter



Chapter-6 (Registers & Counters)

① Synchronous Counter \rightarrow clock pulse same

② Asynchronous Counter (Ripple) \rightarrow clock pulse different

Timing Diagram

* Input wise output

0	0	0	0
1	1	1	1
0	0	1	1
1	0	0	1
1	1	0	0

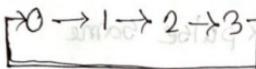
Binary Up/Down Counter

Up counter \rightarrow small to large

2 bit up counter

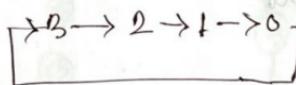


↓
10 → 01 → 00



Down counter \rightarrow large to small

2 bit down counter



\Rightarrow 2 bit Up-down Counter:-

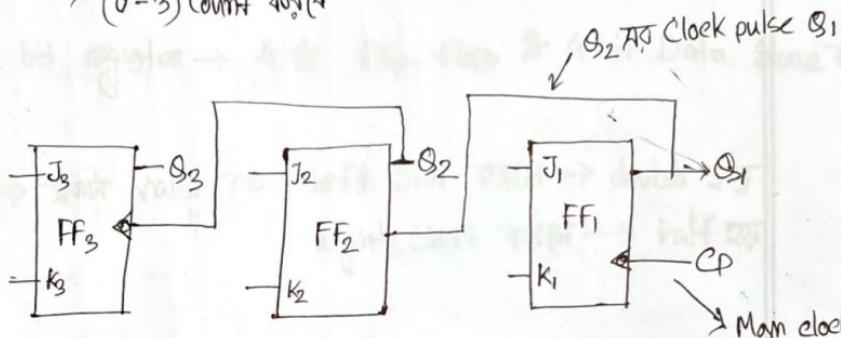
M = 0 , Up Counter

M = 1 , down count

MOD N Counter :-

→ 0 to N-1 Counter

→ MOD 4 Counter / 2 bit binary Counter
 → (0-3) Count



3 bit ripple counter (0-7)

ff₃ ff₂ ff₁
 Q₃ Q₂ Q₁

0	0	0
0	0	1
0	1	0
0	1	1
-1	0	0
1	0	1
1	1	0
1	1	1

clock Pulse after

BCD Ripple Counter

(0-9)
 4 bit use

MOD - 12

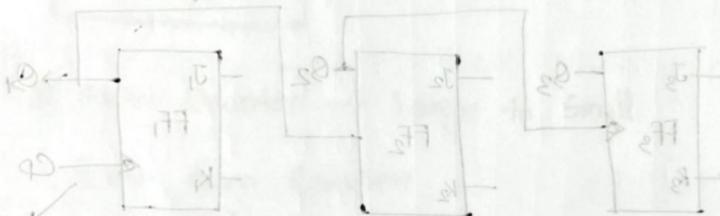
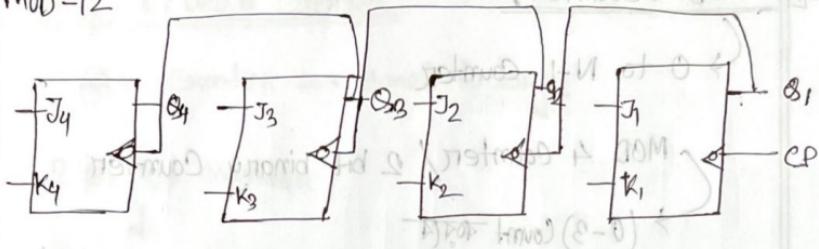
MOD - 25

MOD - 100

MOD - 147

} Using decade Counter

MOD-12



(Q=0) Modulo counter &



BCD Ripple Counter

(Q=0)

Set High

Counters	000 - 111

Count	0	0	0
0	1	0	0
1	0	1	0
2	0	0	1
3	1	0	1
4	0	1	1
5	1	1	1

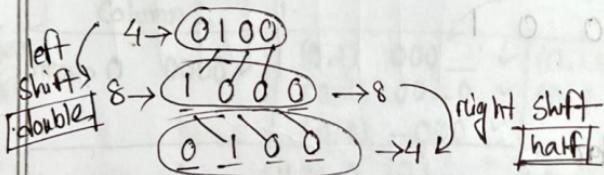
(Q=1)
State

REGISTER

A Group of flip-flops.

→ flip-flops + Combinational gates

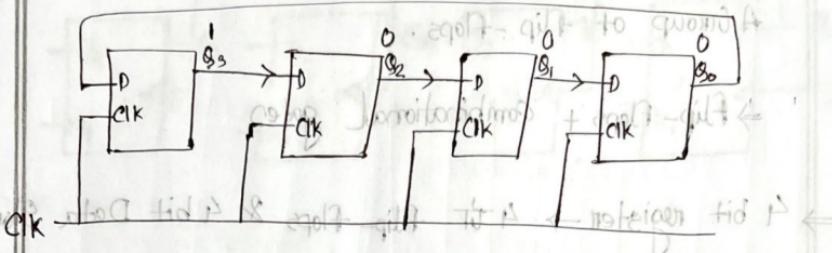
→ 4 bit register → 4 bit flip-flops & 4 bit Data Store

→ given value left shift → double
right shift → half

→ Universal Shift Register

S₁, S₀ | Operation

0 0	→ No change	→ A ₃ A ₂ A ₁ A ₀
0 1	→ Shift right	→ A ₃ A ₂ A ₁ —
1 0	→ left shift	→ A ₂ A ₃ A ₀ —
1 1	→ parallel load	→ I ₃ I ₂ I ₁ I ₀

Ring Counter :- $Q_3 \ Q_2 \ Q_1 \ Q_0$

1 0 0 0
 0 1 0 0 → 1 right shift
 0 0 1 0
 0 0 0 1

Jhonson Counter

$Q_0' \rightarrow$ Inversion of output fed back.

Quiz-4

14-02-2023

Chapter - 5 & 6

I, I, I, I, I → boot loader

methodology | QD P

segment off | 0 0

hil bit + find | 1 0

find + si | 0 1

boot loader | 1 1

Quine-McCluskey / Tabulation Method



↓
easily Simplify করা যাবে

① Determination of prime implicants

② Selection of prime implicants

Example :-

$$F(a, b, c, d) = \sum(0, 1, 2, 5, 6, 7, 8, 9, 10, 14)$$

$$= \sum(0000, 0001, 0010, 0101, 0110, 0111, 1000, 01001, 1010, 1110)$$

Implicant chart

Column 1

Mismatch bit এর দাহু

বিপরীত মিল নেওয়া

Group 0	0000 ✓	(0, 1) 000 ✓	(0, 1, 8, 9) 00_ ✓
		(0, 2) 00_0 ✓	(0, 2, 8, 10) _0_0 ✓
		(0, 8) _000 ✓	
Group 1	10001 ✓	(1, 5) 0_01 ✓	(2, 6, 10, 14) _—10
	20010 ✓	(1, 9) _001 ✓	
	81000 ✓	(2, 6) 0_10 ✓ (8, 9) 100 ✓	
		(4, 10) _010 ✓ (8, 10) 10_0 ✓	
Group 2	50101 ✓	(5, 7) 01_1	
	60110 ✓	(6, 7) 011_	
	91001 ✓	(6, 14) _110 ✓	
	101010 ✓	(10, 14) 1_10 ✓	
Group 3	70111 ✓		
	141110 ✓		

* prime implicant: - (एक गुणन फल, एक फॉट)

$$a'c'd + a'b'c + a'b'cd + b'c' + b'd' + cd'$$

PIS	abed	0	1	2	5	6	7	8	9	10	11	12	13	14
(0,1,8,9)	-00-	b'c'	x	x					x	x				
(0,2,8,10)	-0-0	b'd'	x		x				x	x				
(2,6,10,14)	-1-0	cd'			x		x				x			x
(1,5)	0-01	a'c'd		x		x								
(5,7)	01-1	a'b'd				x	x							
(6,7)	011	a'bc	000		(1,5)	x	x							

$$\text{Ans: } b'c' + c'd' + \underline{a'b'd}$$

X अर्थात् eqn वाली

ज्ञानालय decimal form

प्र०, १०, ३०, ७० ते १०० वरील

असली दोनों eqn वाली

1-10 (F.O)	~101010 & quotient
~110 (F.O)	~0110 &
~011- (F.O)	~1001 &
~01-1 (F.O)	~0101 &

~1110 & quotient

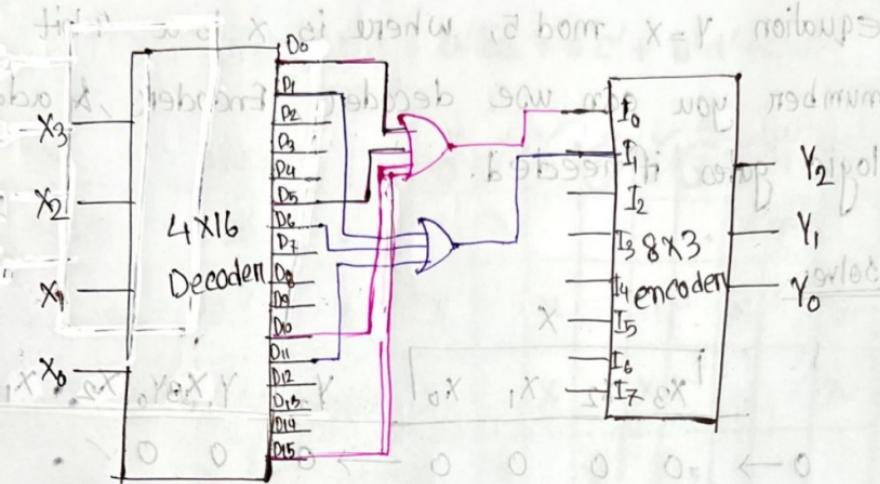
~0111 &

1. It is required to design a ckt to compute the equation $y = x \bmod 5$, where is, x is a 4 bit unsigned number you can use decoders, Encoders, & additional logic gates if needed.

Solve:-

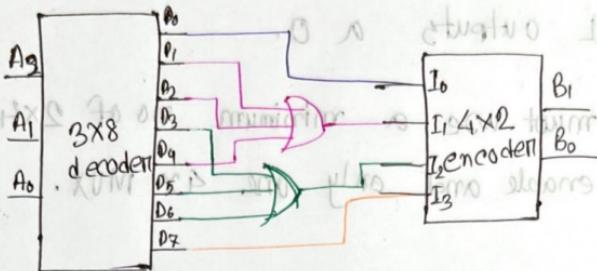
X	Y ₁₅	Y ₁₄	Y ₁₃	Y ₁₂	Y ₁₁	Y ₁₀	Y ₉	Y ₈	Y ₇	Y ₆	Y ₅	Y ₄	Y ₃	Y ₂	Y ₁	Y ₀	
0 → 0 0 0 0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	✓
1 → 0 0 0 1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	✓	
2 → 0 0 1 0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0		
3 → 0 0 1 1	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0		
4 → 0 1 0 0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0		
5 → 0 1 0 1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	✓	
6 → 0 0 1 0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0		
7 → 0 1 1 1	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0		
8 → 1 0 0 0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1		
9 → 1 0 0 1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0		
10 → 1 0 1 0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	✓	
11 → 1 0 1 1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0		
12 → 1 1 0 0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0		
13 → 1 1 0 1	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1		
14 → 1 1 1 0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0		
15 → 1 1 1 1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	✓	

functions of 4-to-16 decoder & 16-to-3 encoder



2. Draw a ckt that accepts a 3 bit input $A(A_2, A_1, A_0)$ and Output a 2 bit number $B(B_1, B_0)$ that is equal to the number of 1's that appear in the input A. You can use decoders, encoders & OR gates.

A_2	A_1	A_0	B_1	B_0	
0 → 0	0	0	0	0	0 ← 0
1 → 0	0	1	0	1	1 ← 1
2 → 0	1	0	0	1	1 ← 01
3 → 0	1	1	1	0	1 ← 11
4 → 1	0	0	0	1	1 ← 01
5 → 1	0	1	1	0	1 ← 11
6 → 1	1	0	1	1	1 ← 11
7 → 1	1	1	1	1	1 ← 11



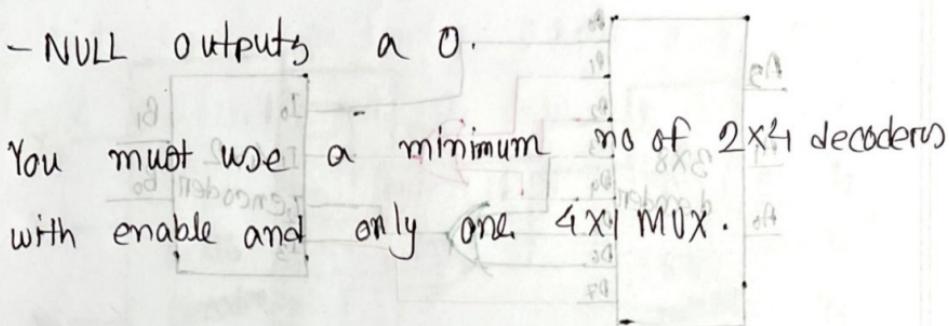
3. Implement a 1x16 demultiplexer using only 2 to 4 decoders with enable inputs & no other logic gates.

4. Using 2x4 decoders & one 4x1 MUX, design a ckt with the following properties. It has two 2 bit binary numbers inputs x(x₁ x₀), y(y₁ y₀) and 2 f₁, f₀

- F₀ outputs a1, if x = y
- GT outputs a1, if x > y

- LUT outputs a 1, if $x <= y$

- NULL outputs a 0.



You must use a minimum no of 2×4 decoders
with enable and only one 4×1 MUX.

In prior notes I have shown a trivial implementation
using one 4-to-1 MUX and two 2-to-1 multiplexers.
But this is not the best way to implement it.

Now, XUM 1XP and one 2-to-1 MUX can be used.
So, we can use one 2-to-1 MUX and one 2-to-1 MUX.
Let us consider, given that $x < y$ is to be
(or $y > x$) then we can use one 2-to-1 MUX.

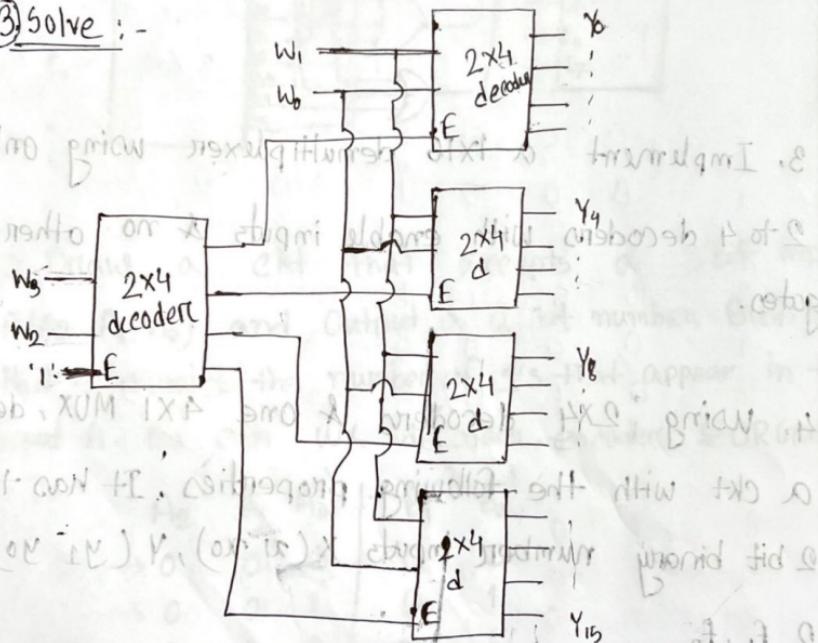
$y = x$, So output is 1
 $y < x$, So output is 0

- LTE outputs a 1, if $x <= y$

- NULL outputs a 0.

You must use a minimum no of 2×4 decoders with enable and only one 4×1 MUX.

③ Solve :-



$$0, 1, 2, 3 \rightarrow w_3 w_2 = 00$$

$$4, 5, 6, 7 \rightarrow w_3 w_2 = 01$$

Topic Name : _____

Day : _____

Time : _____ Date : / /

(4) Solve :-

$x = y$	$x > y$	$x \leq y$	0
<u>EQ</u>	<u>GT</u>	<u>LTE</u>	<u>NULL</u>
$x_2 \ x_1 \mid y_2 \ y_1$			
0 0 0 0	1	0	0
0 0 0 1	0	0	1
0 0 1 0			
0 0 1 1			
0 1 0 0			
⋮	⋮	⋮	⋮
⋮	⋮	⋮	⋮
⋮	⋮	⋮	⋮
1 1	1 1		

$$EQ = \sum (0, 5, 10, 15)$$

$$GT = \sum (4, 8, 9, 12, 13, 14)$$

$$LTE = \sum (0, 1, 2, 3, 5, 6, 7, 10, 11, 15)$$

