ME 1211: Basic Mechanical Engineering

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Course Outline

Academic Week No.	Description	Assessment Method(s)
1	Fundamental concepts (system, property, path and process, pressure	
2	Concepts of Heat and Work, Zeroth Law	Quiz 1
3	1st Law of Thermodynamics	
4	2 nd Law of Thermodynamics	
5	Flow and Non-flow processes	Quiz 2
6	Gas power cycle	
7	Refrigeration cycle	
8	Introduction to Mechanics: Statics Statics of Particles	
9	Equilibrium of a Particle	
10	Equilibrium of Rigid Bodies	
11	Analysis of Structures	Quiz 3
12	Introduction to Dynamics: Kinematics of Particles	
13	Kinetics of Particles: Newton's Second Law	Quiz 4
14	Introduction to Robotics	

Mark Distribution

Marks distribution for ME 1211 (Carry same weight for both part)

Attendance = 10

Class test = 20

Final exam = 70

Total = 100

Reference Books

A Textbook of Thermal Engineering by R.S Khurmi and J.K Guptas

Vector Mechanics for Engineers by Beer, Johnston, Mazurek, Cornwell & Sanghi, Tenth Edition (2013)

Engineering Mechanics: Statics by R.C Hibbeler (12th Edition)

Automobile Engineering (Volume 2) by Dr. Kirpal Singh (12th Edition)

A Textbook of Refrigeration and Air Conditioning by R.S Khurmi

Robotics by Wikibooks (https://en.wikibooks.org/wiki/Robotics)

Reference Books (Recommended)

Fundamentals of Thermal-Fluid Sciences by Çengel, Cimbala, & Turner, Fifth Edition (2017)

Introduction to Robotics: Analysis, Control, Applications by Saeed B, Niku 2nd Edition.

Department of Energy, Fundamentals Handbook: THERMODYNAMICS,

Heat Transfer, And Fluid Flow, Module 1 – Thermodynamics.

https://www.steamtablesonline.com/pdf/Thermodynamics- Volume1.pdf

MIT, Lecture Notes on "Internal Combustion Engines",

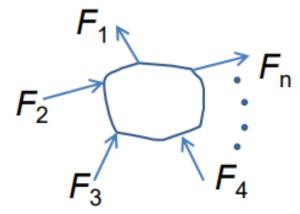
https://ocw.mit.edu/courses/mechanical-engineering/2-61-internal-combustion-engines-spring-2017/lecture-notes/

Prof. Mihir Kumar Sutar, Lectures notes on Engineering Mechanics

http://www.vssut.ac.in/lecture_notes/lecture1423904717.pdf

Chapter 1

Mechanics: It is that branch of science which describes and predicts the conditions of rest or motion of bodies under the action of forces.



- What is the condition for which the body will be in motion or at rest?
- The study of mechanics gives the Answer.

Classification of Mechanics

Mechanics is divided into three classes

 Mechanics of rigid bodies: The bodies that do not deform under the action of forces are called rigid bodies

It has two subdivisions:

- (a) Statics: It deals with the bodies at rest.
- (b) Dynamics: It deals with the bodies in motion.
- Mechanics of deformable bodies: Deformable bodies are those bodies that deform under the action of forces. Strength of material and Elasticity are concerned with deformable bodies.

Classification of Mechanics

3. Mechanics of fluid:

(a) Incompressible fluid: Volume or density does not change under the action of forces. Ex.: Liquid
(b) Compressible fluid: Volume or density does change under the action of forces. Ex.: Gas, air, etc.

Fundamental Concepts

The basic concepts used in mechanics are space, time, mass, and force.

Space: Associated with the notion of the position of a point P with respect to a frame of reference.

Time: To define an event, it is not sufficient to indicate its position in space. The time of the event should also be given.

Mass: Used to characterize and compare bodies on the basis of certain fundamental mechanical experiments.

Force: A force represents the action of one body on another. It is characterized by its (i) point of application, (ii) its magnitude, and (iii) its direction; a force is represented by a vector

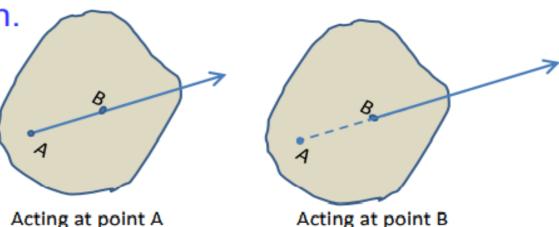
The study of elementary mechanics rests on six fundamental principles based on experimental evidence.

- 1. Parallelogram law for the addition of forces:
 - □ Two forces acting on a particle may be replaced by a single force, called their resultant.
 - □ The resultant is obtained by drawing a diagonal of the parallelogram with sides equal to the given forces.

☐Same effect on the particle A

2. The principle of transmissibility:

■ States that the conditions of equilibrium or of motion of a rigid body will remain unchanged if a force acting at a given point of the rigid body is replaced by a force of the same magnitude and same direction, but acting at a different point, provided that the two forces have the same line of action.



☐ Two forces have the same effect on the body.

Newton's first law:

If the resultant force acting on a particle is zero, the particle will remain at rest (if originally at rest) or will move with constant speed in a straight line (if originally in motion).

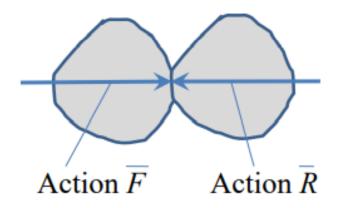
Newton's 2nd law:

If the resultant force acting on a particle is not zero, the particle will have an acceleration proportional to the magnitude of the resultant and in the direction of this resultant force.

$$\overline{F} = m\overline{a}$$

Newton's third law:

The forces of action and reaction between bodies in contact have the (i) same magnitude, (ii) same line of action, and (iii) opposite sense.



- (i) F = R (same magnitude)
- (ii) Same line of action \overline{F}

(iii) Opposite sense

6. Newton's law of gravitation:

This states that two particles of mass M and m are mutually attracted with equal and opposite forces \overline{F} and $-\overline{F}$ of magnitude F given by the formula

$$F = G \frac{Mm}{r^2}$$

$$M \qquad -\overline{F} \qquad m$$

G = constant of gravitation

System of Units

•International System of Units (SI) or Metric System:

The basic units of length, time, and mass which are defined as meter (m), second (s), and kilogram (kg).

•The unit of Force is derived as below, F = ma

$$1 N = (1 kg) \left(1 \frac{m}{s^2} \right)$$

$$W = mg \qquad g = 9.81 \text{ m/s}^2 = 32.2 \text{ ft/s}^2$$

	DIMENSIONAL	SI UNITS	
QUANTITY	SYMBOL	UNIT	SYMBOL
Mass Length Time Force	M L T F	$\begin{array}{c} \text{Base} \\ \text{units} \end{array} \begin{cases} \text{kilogram} \\ \text{meter} \\ \text{second} \\ \text{newton} \end{array}$	kg m s N

U. S. Customary UNITS

U.S. Customary units (or foot-pound-second (FPS) units):

- Mass : slugs (*No symbol*)
- Length: foot (symbol ft)
- Time: second (symbol sec)
- Force: pound (symbol lb)

Note: In U.S. units the pound is also used on occasion as a unit of mass. When distinction between the two units is necessary, the force unit is frequently written as lbf and the mass unit as lbm.

Other units of force in the U.S. system which are in frequent use, are the kilopound (= 1000 lb), and the ton (= 2000 lb)

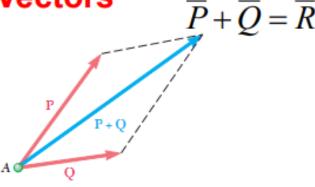
Chapter 2

- □ As mentioned earlier, a force is characterized by its (i) point of application, (ii) its magnitude, and (iii) its direction.
- □ Forces acting on a given particle have the same point of application. Thus, each force in this chapter will be defined by its (i) magnitude and (ii) its direction.

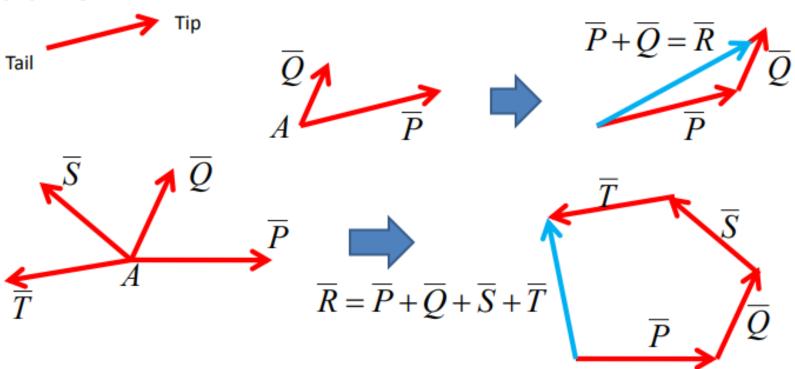


 $\overline{P} + \overline{Q} = \overline{R}$

(a) Parallelogram Law:



(b) Tip-to-Tail fashion:

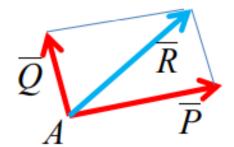


Resolution of a Force into Components

(a) One component is completely known (magnitude and direction)

Resultant \overline{R} is known

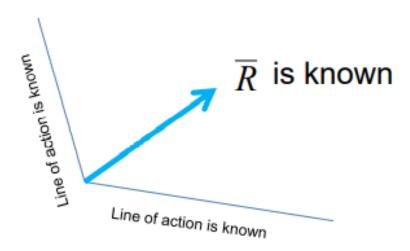
Component \overline{P} is known

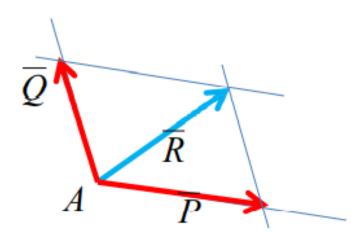


The second component \overline{Q} is determined by drawing the parallelogram with sides \overline{P} and \overline{Q} and diagonal \overline{R} .

Resolution of a Force into Components

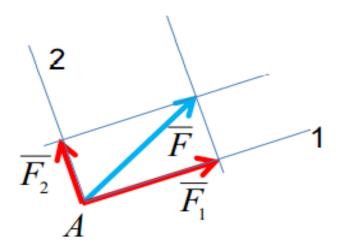
(a) Line of action of each component is known

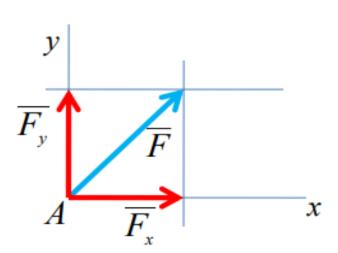




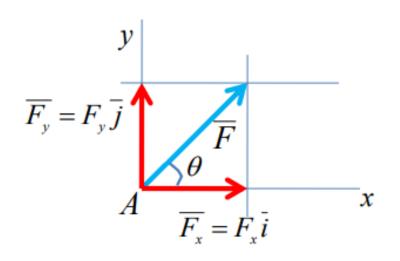
Rectangular Component of a Force

- Sometimes it is very helpful to resolve a force into its rectangular components.
- The components perpendicular to each other are called rectangular components.
- A force can be resolved into rectangular components in different orientation as shown below.





Rectangular Component of a Force



$$\overline{F}$$
 = resultant force

$$\overline{F_x}, \overline{F_y} = \text{components of } \overline{F}$$

$$\bar{i}, \bar{j} = \text{unit vectors of magnitude 1}$$

$$\overline{F} = \overline{F_x} + \overline{F_y}$$

$$\Rightarrow \overline{F} = F_x \overline{i} + F_y \overline{j}$$

$$\Rightarrow \overline{F} = (F\cos\theta)\overline{i} + (F\sin\theta)\overline{j}$$

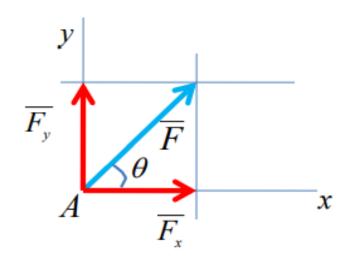
;
$$F_x$$
, F_y =magnitude of components

$$\Rightarrow \overline{F} = (F\cos\theta)\overline{i} + (F\sin\theta)\overline{j}$$
; $F = \text{magnitude of the resultant force}$

$$F_{x} = F \cos \theta \qquad (1a)$$

$$F_{v} = F \sin \theta \qquad (1b)$$

Rectangular Component of a Force



Conversely, if the components are known, the magnitude and direction of the resultant force are determined from the following equations

$$F = \sqrt{F_x^2 + F_y^2}$$

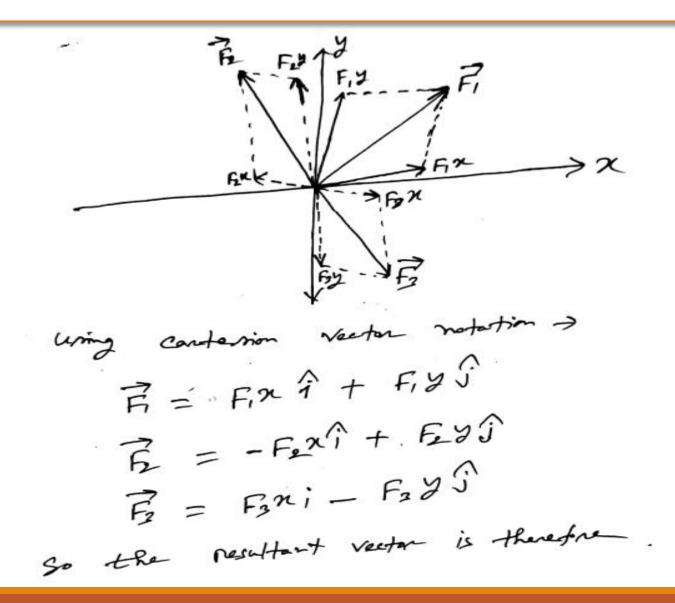
(2a) ; magnitude of the resultant force

$$\tan \theta = \frac{F_y}{F_x} \Rightarrow \theta = \tan^{-1} \frac{F_y}{F_x}$$
 (2b) ; direction of the resultant force

- \square Note that θ is measured from the +ve x-axis towards the resultant in CCW direction.
- □ A rectangular component is considered to be +ve if it is directed to a +ve direction of an axis; otherwise it is negative.

Here 0= 180-35= 1450 Fn= PCOSO= 800 COS 145 = [-655N] Fy = F sin 0 = 800 sin 145 = [459 N] # If can be solved by physically observing the sign of the components by taking the given angle of 35° beto -ve anis and the resultant. # It is seen that Fr is -ve. Thm, $F_{\lambda} = -F \cos 35 = \frac{[-655N]}{[459N]}$ $F_{\gamma} = F \sin 35 = \frac{[459N]}{[459N]}$

Resultant of Concurrent Force



Resultant of Concurrent Force

$$\vec{R} = \vec{F_1} + \vec{F_2} + \vec{F_3}$$

$$= f_1 \times \hat{i} + F_1 \times \hat{j} + (f_2 \times \hat{i} + F_2 \times \hat{j})$$

$$+ (F_3 \times \hat{i} - F_2 \times \hat{j})$$

$$= \hat{i} (F_1 \times F_2 \times F_3 \times F_$$

Resultant of Concurrent Force (Scaler Component)

$$\left(\frac{+1}{+1}\right) R_{x} = F_{1}x - F_{2}x + F_{3}x$$

$$\left(+1\right) R_{y} = F_{1}y + F_{2}y - F_{3}y$$

$$\therefore R = \sqrt{R_{x} + R_{y}} R_{y} R_{y}$$

$$R_{x} = \sqrt{R_{x} + R_{y}} R_{y}$$

$$R_{x} = \sqrt{R_{x} + R_{y}} R_{y}$$

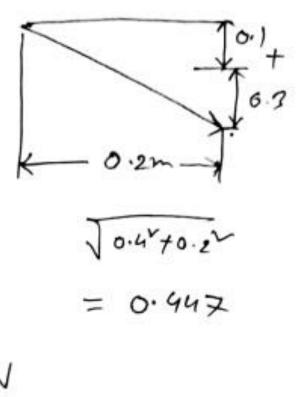
Problem The forces Fi, F2 & F3

: Fix = F, Cen35' = 600 cen35' : Fix = 491.49 N Fiy = Firm35' = 344.15 N

Scalar component of Fz:

$$F_{2x} = -F_{2} \times \frac{4}{5} \Rightarrow compared F_{2} \times \frac{7}{3} = \frac{7}{3} \times \frac{7}{4} \times$$

$$\begin{array}{rcl}
F_{3y} &=& -F_{3} \times \frac{0.4}{0.442} \\
&=& -715.88 \text{ N}
\end{array}$$



Now Resultant Force : Ra= 2Fa= Fat Fat Fax - 491.49 - 400 + 357.9H Rn = 449.43 N 4 Ry = 2Fy = Fig + Fzy + Fzy - 399.15 +300 - 715.8A - - 71.73 N R = JRX+Ry = 455.11 N & &= for == 9.068.

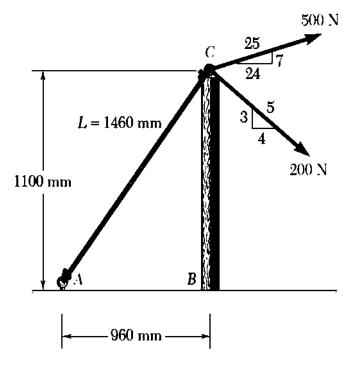
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Problems

Prob 2.36: Knowing that the tension in rope AC is 365 N, determine the resultant of the three forces exerted at point C of post BC.

Prob 2.40: For the post of Prob. 2.36, determine (a) the required tension in rope AC if the resultant of the three forces exerted at point C is to be horizontal,

(b) the corresponding magnitude of the resultant.



SOLUTION Problem 2.36

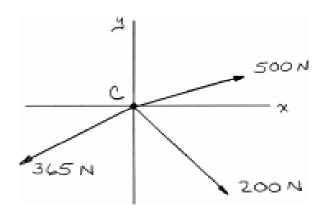
Determine force components:

$$F_x = -(365 \text{ N}) \frac{960}{1460} = -240 \text{ N}$$

$$F_y = -(365 \text{ N}) \frac{1100}{1460} = -275 \text{ N}$$

$$F_x = (500 \text{ N}) \frac{24}{25} = 480 \text{ N}$$

$$F_y = (500 \text{ N}) \frac{7}{25} = 140 \text{ N}$$



200-N Force:

$$F_x = (200 \text{ N}) \frac{4}{5} = 160 \text{ N}$$

$$F_y = -(200 \text{ N}) \frac{3}{5} = -120 \text{ N}$$

and

$$R_x = \Sigma F_x = -240 \text{ N} + 480 \text{ N} + 160 \text{ N} = 400 \text{ N}$$

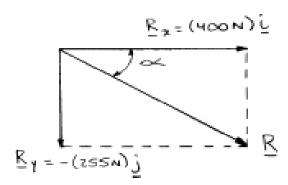
$$R_v = \Sigma F_v = -275 \text{ N} + 140 \text{ N} - 120 \text{ N} = -255 \text{ N}$$

$$R = \sqrt{R_x^2 + R_y^2}$$
= $\sqrt{(400 \text{ N})^2 + (-255 \text{ N})^2}$
= 474.37 N

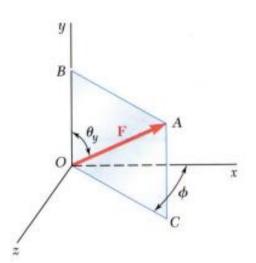
Further:

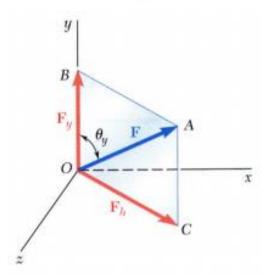
$$\tan \alpha = \frac{255}{400}$$

$$\alpha = 32.5^{\circ}$$



Rectangular Components in Space

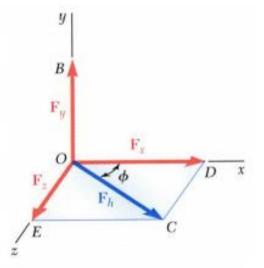




- The vector \vec{F} is contained in the plane *OBAC*.
- Resolve F into horizontal and vertical components.

$$F_{y} = F \cos \theta_{y}$$

$$F_h = F \sin \theta_y$$



Resolve F_h into rectangular components

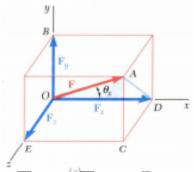
$$F_x = F_h \cos \phi$$

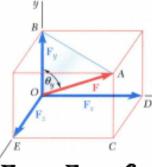
$$= F \sin \theta_y \cos \phi$$

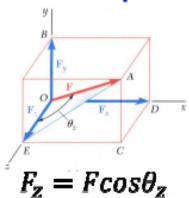
$$F_z = F_h \sin \phi$$

$$= F \sin \theta_y \sin \phi$$

Rectangular Components in Space







$$F_x = F \cos \theta_x$$

$$F_{y} = F \cos \theta_{y}$$

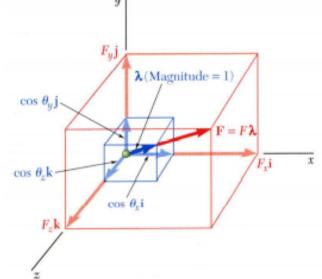
$$F = F_{\chi}i + F_{y}j + F_{z}k$$

$$F = F\cos\theta_x \mathbf{i} + F\cos\theta_y \mathbf{j} + F\cos\theta_z \mathbf{k}$$

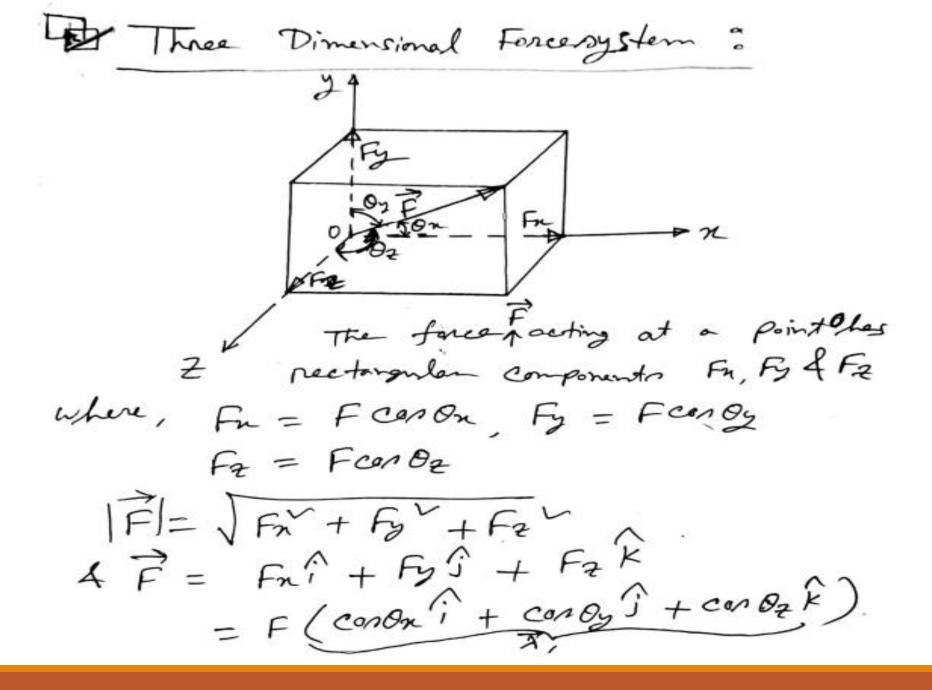
$$F = F(\cos\theta_x i + \cos\theta_y j + \cos\theta_z k)$$

$$F = F\lambda$$

Where
$$\lambda = \cos\theta_x \mathbf{i} + \cos\theta_y \mathbf{j} + \cos\theta_z \mathbf{k}$$



 λ is a unit vector along the line of action of F and $cos\theta_x$, $cos\theta_y$ and $cos\theta_z$ are the direction cosine for F



The unit vector i, i, i, x are in directions respectively in a mit vector of in a mit vector along the line of action of F & has a of conon = Fr , conoy = Fy of conoz = For

other : Determine (a)x, y, force 4

FL = F sin Qy

= 750 sin 30'

FL = 430.2 N

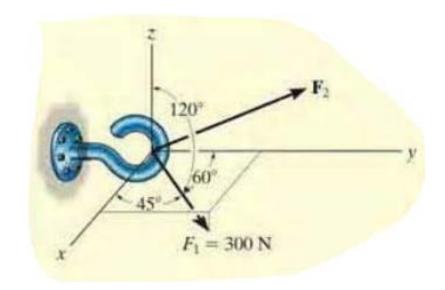
FR = FL
$$\mathbf{cor}$$
 25' = $\mathbf{390 N}$

Fy = F \mathbf{cor} 36' = $\mathbf{C14 N}$

Fz = FL \mathbf{cor} 25' = $\mathbf{107.8 N}$

2 \mathbf{cor} \mathbf{On} = \mathbf{Fn} ; \mathbf{cor} \mathbf{Oy} = \mathbf{Fy} + \mathbf{cor} \mathbf{Oz} = \mathbf{Fz}
 \mathbf{Oy} = \mathbf{Fy} = \mathbf{Oy} = \mathbf{Fy} + \mathbf{Cor} \mathbf{Oz} = \mathbf{Fz}
 \mathbf{Oy} = \mathbf{Fy} = \mathbf{Oy} = \mathbf{Fy} + \mathbf{Cor} \mathbf{Oz} = \mathbf{Fz}

Problem: Two forces act on the hook shown in Fig. Specify the magnitude of F_2 and its coordinate direction angles of F_2 that the resultant force F_R acts along the positive y axis and has a magnitude of 800 N.

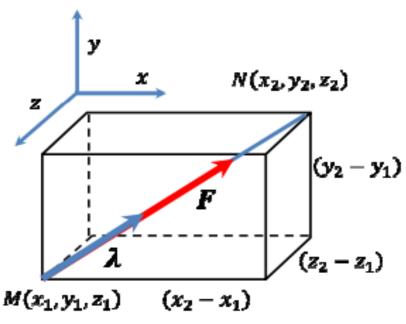


Self Study

Rectangular Components in Space

Direction of the force is defined by the location of two points

$$M(x_1, y_1, z_1)$$
 and $N(x_2, y_2, z_2)$



d is the vector joining M and N

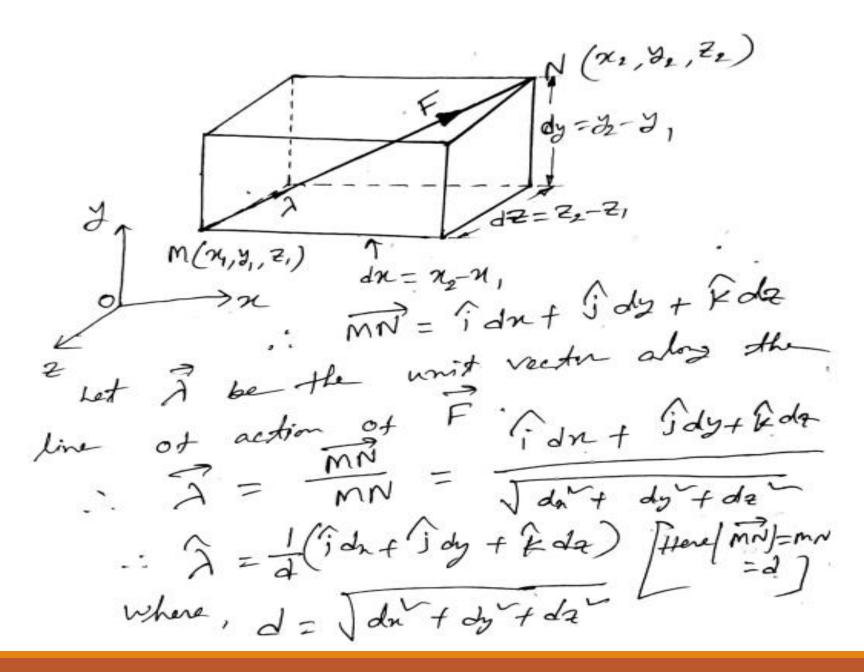
$$d = d_x i + d_y j + d_z k$$

$$d_x = (x_2 - x_1) \qquad d_y = (y_2 - y_1)$$

$$F = F\lambda$$

$$= F\left(\frac{d_x i + d_y j + d_z k}{d}\right)$$

$$F_{\mathbf{x}} = F \frac{d_{\mathbf{x}}}{d}$$
 $F_{\mathbf{y}} = F \frac{d_{\mathbf{y}}}{d}$ $F_{\mathbf{z}} = F \frac{d_{\mathbf{z}}}{d}$



But,
$$\vec{F} = \vec{\lambda} \vec{F}$$

$$= \vec{F} = \vec{F} (\vec{f} \cdot dn + \vec{f} \cdot dy + \vec{k} \cdot dy)$$

$$= \vec{f} (\vec{f} \cdot dn + \vec{f} \cdot dy) + \vec{k} (\vec{f} \cdot dy)$$

Again $\vec{F} = \vec{F} \cdot \vec{n} + \vec{F} \cdot \vec{j} + \vec{F} \cdot \vec{k}$

So companing we find,

$$\vec{F} \cdot \vec{k} = \vec{f} \cdot \vec{k} \cdot$$

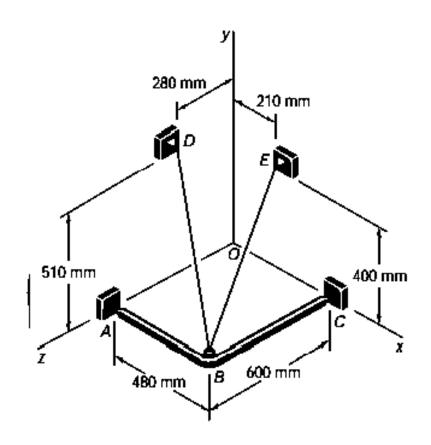
Now,
$$\overrightarrow{F} = \overrightarrow{J} F$$

$$\overrightarrow{J} \overrightarrow{F} = F \left[\frac{\widehat{J} dn + \widehat{J} dy + \widehat{K} dz}{\overline{J} dn + dy' + dz'} \right]$$

$$\overrightarrow{F} = F \cdot \frac{\widehat{J} (n_2 - n_1) + \widehat{J} (y_2 - y_1) + \widehat{K} (n_2 - n_2)}{\overline{J} (n_2 - n_1)'' + (n_2 - n_2)'' + (n$$

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Problem: A frame ABC is supported in part by cable DBE that passes through a frictionless ring at B. Knowing that the tension in the cable is 385 N, determine the components of the force exerted by the cable on the support at D



SOLUTION

$$\overline{DB} = (480 \text{ mm})\mathbf{i} - (510 \text{ mm})\mathbf{j} + (320 \text{ mm})\mathbf{k}$$

$$DB = \sqrt{(480 \text{ mm})^2 + (510 \text{ mm}^2) + (320 \text{ mm})^2}$$

$$= 770 \text{ mm}$$

$$\mathbf{F} = F\lambda_{DB}$$

$$= F \frac{\overline{DB}}{DB}$$

$$= \frac{385 \text{ N}}{770 \text{ mm}} [(480 \text{ mm})\mathbf{i} - (510 \text{ mm})\mathbf{j} + (320 \text{ mm})\mathbf{k}]$$

$$= (240 \text{ N})\mathbf{i} - (255 \text{ N})\mathbf{j} + (160 \text{ N})\mathbf{k}$$

$$F_x = +240 \text{ N}, \quad F_y = -255 \text{ N}, \quad F_z = +160.0 \text{ N} \blacktriangleleft$$

Self Study

Beer and Johnston (10th Edition)

2.31, 2.32, 2.33, 2.35, 2.36, 2.38, 2.40, 2.90, 2.95, 2.97

Hibbeler R.C. (12th Edition)

2.97



All the problems solved in class lectures