Assignment 1 Applied Computational Science

Alifian Mahardhika Maulana

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1. Suppose,

$$r = \sqrt{x^2 + y^2 + z^2} \tag{1}$$

then we define:

$$f_x(r) = -\frac{\partial U(r)}{\partial x} = -\frac{x}{r} \frac{\partial U(r)}{\partial r}$$
: x-component of the force. (2)

with

$$U(r) = 4\left(\frac{1}{r^{12}} - \frac{1}{r^6}\right) \longrightarrow f_x(r) = \frac{48x}{r^2} \left(\frac{1}{r^{12}} - \frac{1}{2} \cdot \frac{1}{r^6}\right) : \text{Lennard-Jones Potential } (3)$$

Derive the f_x, f_y , and f_z component of Lennard-Jones Potential System.

From Equation (2), we know that:

$$f_x(r) = -\frac{\partial U(r)}{\partial x}$$

$$= -\frac{\partial r}{\partial x} \frac{\partial U(r)}{\partial r}$$
(4)

then we substitute r and U(r) from equation (1) and (3) \rightarrow (4), therefore:

$$f_{x}(r) = -\left(\frac{\partial}{\partial x}\sqrt{x^{2} + y^{2} + z^{2}} \frac{\partial}{\partial r} 4\left(\frac{1}{r^{12}} - \frac{1}{r^{6}}\right)\right)$$

$$= -\left(\frac{1}{2}\frac{1}{\sqrt{x^{2} + y^{2} + z^{2}}} 2x\left(\frac{-48}{r^{13}} + \frac{24}{r^{7}}\right)\right)$$

$$= -\left(\frac{x}{\sqrt{x^{2} + y^{2} + z^{2}}} \frac{48}{r}\left(\frac{-1}{r^{12}} + \frac{1}{2} \cdot \frac{1}{r^{6}}\right)\right)$$

$$= -\frac{x}{r} \frac{48}{r}\left(\frac{1}{r^{12}} - \frac{1}{2} \cdot \frac{1}{r^{6}}\right)$$

$$= -\frac{48x}{r^{2}}\left(\frac{1}{r^{12}} - \frac{1}{2} \cdot \frac{1}{r^{6}}\right)$$
(5)