

Nama : Afina Putri Dayanti
NIM : 825200049
Jurusan : Sistem Informasi
Mata Kuliah : Applied Statistics

1. Selesaikan linear program berikut ini dengan metode Simplex

Maksimumkan $Z = 400X_1 + 300X_2$

Fungsi kendala/ batasan:

- 1) $4X_1 + 6X_2 \leq 1200$
- 2) $4X_1 + 2X_2 \leq 800$
- 3) $X_1 \leq 250$
- 4) $X_2 \leq 300$

1) Fungsi Tujuan

$$\begin{aligned} * Z &= 400x_1 + 300x_2 \Rightarrow Z - 400x_1 - 300x_2 = 0 \\ &= 400x_1 + 300x_2 \end{aligned}$$

Fungsi Batasan

$$\begin{aligned} * 4x_1 + 6x_2 &\leq 1200 \Rightarrow 4x_1 + 6x_2 + s_1 = 1200 \\ * 4x_1 + 2x_2 &\leq 800 \Rightarrow 4x_1 + 2x_2 + s_2 = 800 \\ * x_1 &\leq 250 \Rightarrow x_1 + s_3 = 250 \\ * x_2 &\leq 300 \Rightarrow x_2 + s_4 = 300 \end{aligned}$$

Var. Dasar	Z	x_1	x_2	s_1	s_2	s_3	s_4	NK	index
Z	1	-400	-300	0	0	0	0	0	
s_1	0	4	6	1	0	0	0	1200	300
x_1	0	4	2	0	1	0	0	800	200
s_3	0	1	0	0	0	1	0	250	250
s_4	0	0	1	0	0	0	1	300	~

baris baru kunci = baris kunci : angka kunci

$$\left[\begin{array}{ccccccccc} 1 & 1/2 & 0 & 1/4 & 0 & 0 & 0 & 200 \end{array} \right]$$

* baris Z
baris lama
NBBK
baris baru

$$\begin{array}{r} [-400 \quad -300 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0] \\ -400 \left[\begin{array}{cccccc|c} 1 & 1/2 & 0 & 1/4 & 0 & 0 & 200 \end{array} \right] \\ \hline \begin{array}{cccccc|c} 0 & -100 & 0 & -100 & 0 & 0 & 80.000 \end{array} \end{array}$$

* baris S₁
baris lama
NBBK
baris baru

$$\begin{array}{r} [\quad 4 \quad 6 \quad 1 \quad 0 \quad 0 \quad 0 \quad 1200] \\ 4 \left[\begin{array}{cccccc|c} 1 & 1/2 & 0 & 1/4 & 0 & 0 & 200 \end{array} \right] \\ \hline \begin{array}{cccccc|c} 0 & 4 & 1 & -1 & 0 & 0 & 400 \end{array} \end{array}$$

* baris S₂
baris lama
NBBK
baris baru

$$\begin{array}{r} [\quad 1 \quad 0 \quad 0 \quad 0 \quad 1 \quad 0 \quad 250] \\ 1 \left[\begin{array}{cccccc|c} 1 & 1/2 & 0 & 1/4 & 0 & 0 & 200 \end{array} \right] \\ \hline \begin{array}{cccccc|c} 0 & -1/2 & 0 & -1/4 & 1 & 0 & 50 \end{array} \end{array}$$

* baris S₄
baris lama
NBBK
baris baru

$$\begin{array}{r} [\quad 0 \quad 1 \quad 0 \quad 0 \quad 0 \quad 1 \quad 300] \\ 0 \left[\begin{array}{cccccc|c} 1 & 1/2 & 0 & 1/4 & 0 & 0 & 200 \end{array} \right] \\ \hline \begin{array}{cccccc|c} 0 & 1 & 0 & 0 & 0 & 1 & 300 \end{array} \end{array}$$

* karena baris Z masih terdapat minus, maka :

Var. Dsr	Z	u ₁	u ₂	s ₁	s ₂	s ₃	s ₄	NK	index
Z	1	0	-100	0	100	0	0	80.000	-300
u ₂	0	0	(4)	1	-1	0	0	400	100
u ₁	0	1	1/2	0	1/4	0	0	200	400
s ₃	0	0	-1/2	0	-1/4	1	0	50	-100
s ₄	0	0	1	0	0	0	1	300	300

baris kunci baru : $[\quad 0 \quad 1 \quad 0 \quad 1/4 \quad -1/4 \quad 0 \quad 0 \quad 100]$

* baris Z
baris lama
NBBK
baris baru

$$\begin{array}{r} \begin{bmatrix} 0 & -100 & 0 & 100 & 0 & 0 & 80.000 \end{bmatrix} \\ -100 \begin{bmatrix} 0 & 1 & 1/4 & -1/4 & 0 & 0 & 100 \end{bmatrix} \\ \hline \begin{bmatrix} 0 & 0 & 25 & -25 & 0 & 0 & 90.000 \end{bmatrix} \end{array}$$

* baris $2e_1$
baris lama
NBBK
baris baru

$$\begin{array}{r} \begin{bmatrix} 1 & 1/2 & 0 & 1/4 & 0 & 0 & 200 \end{bmatrix} \\ 1/2 \begin{bmatrix} 0 & 1 & 1/4 & -1/4 & 0 & 0 & 100 \end{bmatrix} \\ \hline \begin{bmatrix} 1 & 0 & -1/8 & 3/8 & 0 & 0 & 150 \end{bmatrix} \end{array}$$

* baris S_3
baris lama
NBBK
baris baru

$$\begin{array}{r} \begin{bmatrix} 0 & -1/2 & 0 & -1/4 & 1 & 0 & -50 \end{bmatrix} \\ -1/2 \begin{bmatrix} 0 & 1 & 1/4 & -1/4 & 0 & 0 & 100 \end{bmatrix} \\ \hline \begin{bmatrix} 0 & 0 & 1/8 & -3/8 & 1 & 0 & 100 \end{bmatrix} \end{array}$$

* baris S_4
baris lama
NBBK
baris baru

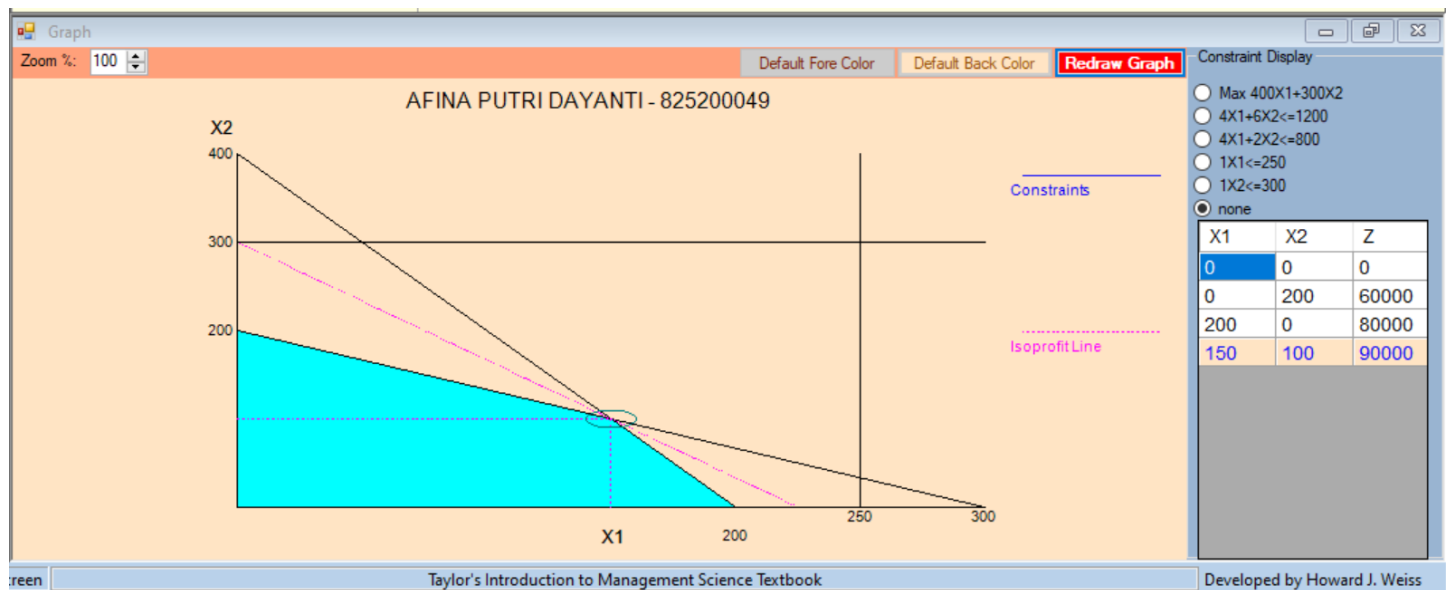
$$\begin{array}{r} \begin{bmatrix} 0 & 1 & 0 & 0 & 0 & 1 & 200 \end{bmatrix} \\ 1 \begin{bmatrix} 0 & 1 & 1/4 & -1/4 & 0 & 0 & 100 \end{bmatrix} \\ \hline \begin{bmatrix} 0 & 0 & -1/4 & 1/4 & 0 & 1 & 200 \end{bmatrix} \end{array}$$

$2e_1$: 150
 $2e_2$: 100
 Z_{max} : 90.000

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Cj	Basic Variables	Quantity	400 X1	300 X2	0 slack 1	0 slack 2	0 slack 3	0 slack 4
Iteration 1								
0	slack 1	1,200	4	6	1	0	0	0
0	slack 2	800	4	2	0	1	0	0
0	slack 3	250	1	0	0	0	1	0
0	slack 4	300	0	1	0	0	0	1
	zj	0	0	0	0	0	0	0
	cj-zj		400	300	0	0	0	0
Iteration 2								
0	slack 1	400	0	4	1	-1	0	0
400	X1	200	1	0.5	0	0.25	0	0
0	slack 3	50	0	-0.5	0	-0.25	1	0
0	slack 4	300	0	1	0	0	0	1
	zj	80,000	400	200	0	100	0	0
	cj-zj		0	100	0	-100	0	0

Iteration 3								
300	X2	100	0	1	0.25	-0.25	0	0
400	X1	150	1	0	-0.125	0.375	0	0
0	slack 3	100	0	0	0.125	-0.375	1	0
0	slack 4	200	0	0	-0.25	0.25	0	1
	zj	90,000	400	300	25	75	0	0
	cj-zj		0	0	-25	-75	0	0



Linear Programming Results

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	X1	X2		RHS	Dual
Maximize	400	300			
Constraint 1	4	6	\leq	1200	25
Constraint 2	4	2	\leq	800	75
Constraint 3	1	0	\leq	250	0
Constraint 4	0	1	\leq	300	0
Solution->	150	100		90000	

2. Selesaikan linear program berikut ini dengan metode Simplex

Maksimumkan $Z = 2X_1 + 3X_2 + X_3$

Dengan fungsi kendala:

1) $X_1 + X_2 + X_3 \leq 9$

2) $2X_1 + 3X_2 \leq 25$

3) $X_2 + 2X_3 \leq 10$

4) $X_1, X_2, X_3 \geq 0$

2) Fungsi Tujuan
 $* Z = 2x_1 + 3x_2 + x_3 \Rightarrow Z - 2x_1 - 3x_2 - x_3 = 0$

Fungsi Batasan
 $* x_1 + x_2 + x_3 \leq 9 \Rightarrow x_1 + x_2 + x_3 + s_1 = 9$
 $* 2x_1 + 3x_2 \leq 25 \Rightarrow 2x_1 + 3x_2 + s_2 = 25$
 $* x_2 + 2x_3 \leq 10 \Rightarrow x_2 + 2x_3 + s_3 = 10$
 $* x_1, x_2, x_3 \geq 0$

Var. der	Z	x_1	x_2	x_3	s_1	s_2	s_3	NK	index
Z	1	-2	-3	-1	0	0	0	0	
s_1	0	1	1	1	1	0	0	9	9
x_2	0	2	3	0	0	1	0	25	25/3
s_3	0	0	1	2	0	0	1	10	10

baris kunci baru = $\left[\frac{2}{3} \quad 1 \quad 0 \quad 0 \quad \frac{1}{3} \quad 0 \quad \frac{25}{3} \right]$

* baris Z
 baris lama
 NBBK
 baris baru

$$\begin{array}{r} \left[\begin{array}{ccccccc} -2 & -3 & -1 & 0 & 0 & 0 & 0 \end{array} \right] \\ -3 \left[\begin{array}{ccccccc} \frac{2}{3} & 1 & 0 & 0 & \frac{1}{3} & 0 & \frac{25}{3} \end{array} \right] \\ \hline \left[\begin{array}{ccccccc} 0 & 0 & -1 & 0 & 1 & 0 & 25 \end{array} \right] \end{array}$$

* baris s_1
 baris lama
 NBBK
 baris baru

$$\begin{array}{r} \left[\begin{array}{ccccccc} 1 & 1 & 1 & 1 & 0 & 0 & 9 \end{array} \right] \\ + \left[\begin{array}{ccccccc} \frac{1}{3} & 1 & 0 & 0 & \frac{1}{3} & 0 & \frac{25}{3} \end{array} \right] \\ \hline \left[\begin{array}{ccccccc} \frac{1}{3} & 0 & 1 & 1 & -\frac{1}{3} & 0 & \frac{2}{3} \end{array} \right] \end{array}$$

* baris s_3
 baris lama
 NBBK
 baris baru

$$\begin{array}{r} \left[\begin{array}{ccccccc} 0 & 1 & 2 & 0 & 0 & 1 & 10 \end{array} \right] \\ + \left[\begin{array}{ccccccc} \frac{2}{3} & 1 & 0 & 0 & \frac{1}{3} & 0 & \frac{25}{3} \end{array} \right] \\ \hline \left[\begin{array}{ccccccc} -\frac{2}{3} & 0 & 2 & 0 & -\frac{1}{3} & 1 & \frac{5}{3} \end{array} \right] \end{array}$$

Karena masih terdapat minus, maka

Var dst	Z	u_1	u_2	u_3	s_1	s_2	s_3	Nilai	index
Z	1	0	0	-1	0	1	0	25	
u_3	0	$\frac{1}{3}$	0	1	1	$-\frac{1}{3}$	0	$\frac{2}{3}$	$\frac{2}{3}$
u_2	0	$\frac{2}{3}$	1	0	0	$\frac{1}{3}$	0	$\frac{25}{3}$	~
s_3	0	$-\frac{2}{3}$	0	2	0	$-\frac{1}{3}$	1	$\frac{5}{3}$	$\frac{5}{6}$

baris kunci baru : $\left[\frac{1}{3} \quad 0 \quad 1 \quad 1 \quad -\frac{1}{3} \quad 0 \quad \frac{2}{3} \right]$

* baris Z

baris lama

NBBK

baris baru

$$\begin{array}{r} \left[\begin{array}{ccccccc} 0 & 0 & -1 & 0 & 1 & 0 & 25 \end{array} \right] \\ -1 \left[\begin{array}{ccccccc} \frac{1}{3} & 0 & 1 & 1 & -\frac{1}{3} & 0 & \frac{2}{3} \end{array} \right] \\ \hline \left[\begin{array}{ccccccc} \frac{1}{3} & 0 & 0 & 1 & \frac{2}{3} & 0 & \frac{77}{3} \end{array} \right] \end{array}$$

* baris u_2

baris lama

NBBK

baris baru

$$\begin{array}{r} \left[\begin{array}{ccccccc} \frac{2}{3} & 1 & 0 & 0 & \frac{1}{3} & 0 & \frac{25}{3} \end{array} \right] \\ 0 \left[\begin{array}{ccccccc} \frac{1}{3} & 0 & 1 & 1 & -\frac{1}{3} & 0 & \frac{2}{3} \end{array} \right] \\ \hline \left[\begin{array}{ccccccc} \frac{2}{3} & 1 & 0 & 0 & \frac{1}{3} & 0 & \frac{25}{3} \end{array} \right] \end{array}$$

* baris s_3

baris lama

NBBK

baris baru

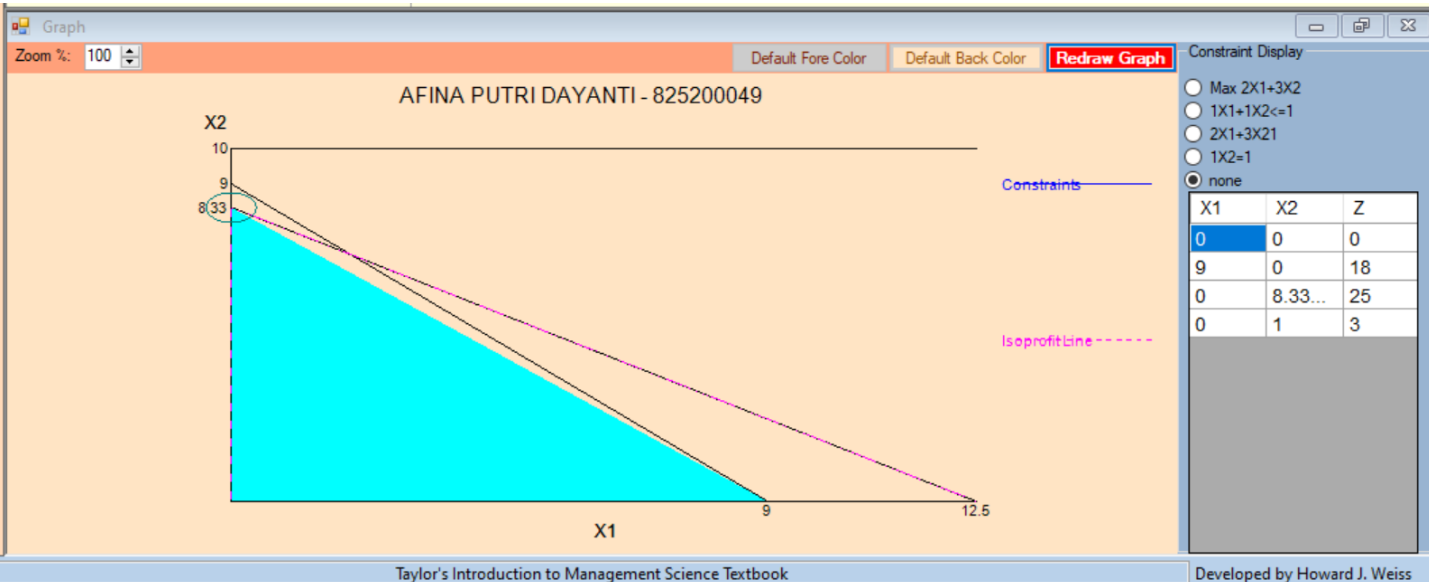
$$\begin{array}{r} \left[\begin{array}{ccccccc} -\frac{2}{3} & 0 & 2 & 0 & -\frac{1}{3} & 1 & \frac{5}{3} \end{array} \right] \\ 2 \left[\begin{array}{ccccccc} \frac{1}{3} & 0 & 1 & 1 & -\frac{1}{3} & 0 & \frac{2}{3} \end{array} \right] \\ \hline \left[\begin{array}{ccccccc} -\frac{4}{3} & 0 & 0 & -2 & \frac{1}{3} & 1 & \frac{1}{3} \end{array} \right] \end{array}$$

$$\begin{array}{lcl} u_1 & = & 0 \\ u_2 & = & \frac{25}{3} \\ u_3 & = & \frac{2}{3} \\ Z & = & \frac{77}{3} \end{array}$$

AFINA PUTRI DAYANTI - 825200049 Solution

Cj	Basic Variables	Quantity	2 X1	3 X2	1 X3	0 slack 1	0 slack 2	0 slack 3
Iteration 1								
0	slack 1	9	1	1	1	1	0	0
0	slack 2	25	2	3	0	0	1	0
0	slack 3	10	0	1	2	0	0	1
	zj	0	0	0	0	0	0	0
	cj-zj		2	3	1	0	0	0
Iteration 2								
0	slack 1	0.6667	0.3333	0	1	1	-0.3333	0
3	X2	8.3333	0.6667	1	0	0	0.3333	0
0	slack 3	1.6667	-0.6667	0	2	0	-0.3333	1
	zj	25	2	3	0	0	1	0
	cj-zj		0	0	1	0	-1	0

Iteration 3								
1	X3	0.6667	0.3333	0	1	1	-0.3333	0
3	X2	8.3333	0.6667	1	0	0	0.3333	0
0	slack 3	0.3333	-1.3333	0	0	-2	0.3333	1
	zj	25.6667	2.33	3	1	1	.67	0
	cj-zj		-0.3333	0	0	-1	-0.6667	0



Linear Programming Results

AFINA PUTRI DAYANTI - 825200049 Solution

	X1	X2	X3		RHS	Dual
Maximize	2	3	1			
Constraint 1	1	1	1	\leq	9	1
Constraint 2	2	3	0	\leq	25	.67
Constraint 3	0	1	2	\leq	10	0
Solution->	0	8.33	.67		25.67	