# Quantum optimization through path-integral molecular dynamics:

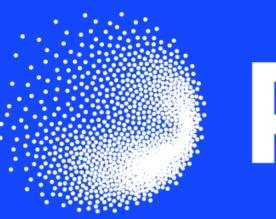
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## 1. Introduction

- Motivation
- Global optimization of atomic degrees of freedom is a key problem in physics whenever the number of candidate structures (local minima) is combinatorially large: cluster physics, polymer folding, interfaces...
- ► The idea
  - **Novel** implementation of **Quantum Annelealing** (QA) using **Path-Integral Molecular Dynamics** (PIMD), labeled QA-PIMD.

## 2. Methods

**QA-PIMD** is obtained by combining two powerful methods:

Quantum annealing: exploration trhough quantum delocalization

$$\hat{H}(t) = -\alpha(t) \sum_{i=1}^{N} \frac{\hbar^2}{2m_i} \nabla^2 + U(\hat{\mathbf{x}}_1, \dots, \hat{\mathbf{x}}_N)$$

- $ightharpoonup \lim_{t_{max}\to\infty} Tr[\rho(t_{max})U] = \min U$
- Path-Integral Molecular Dynamics Equilibrium nuclear quantum effects (NQEs) from P classical simulations ( $P \sim 10 - 100$ .

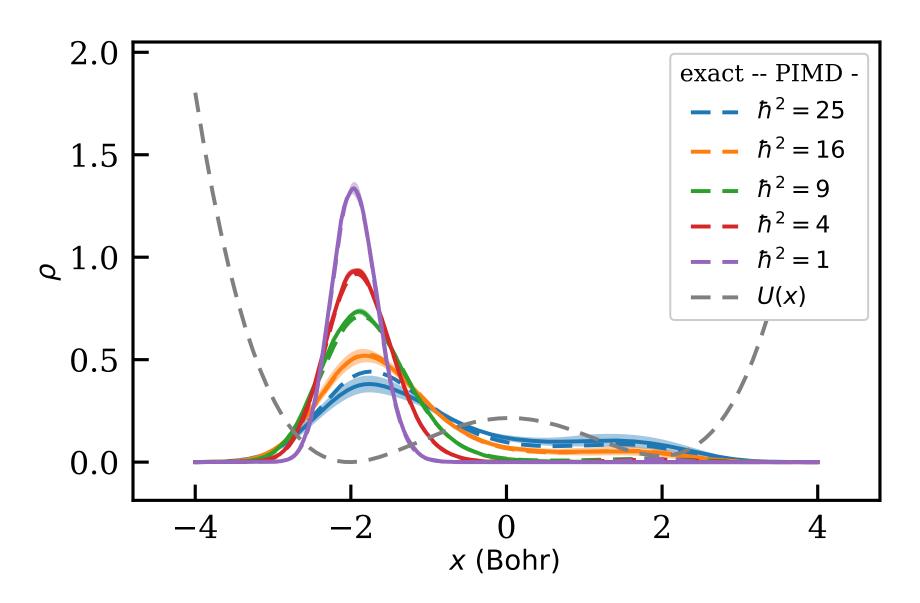
$$H_{P} = \sum_{i=1}^{N} \sum_{j=1}^{P} \left[ \frac{1}{2m_{i}} |\mathbf{p}_{i}^{(j)}|^{2} + \frac{1}{2} m_{i} \omega_{P}^{2} |\mathbf{x}_{i}^{(j)} - \mathbf{x}_{i}^{(j+1)}|^{2} \right] + \sum_{j=1}^{P} U(\mathbf{x}_{1j}, \dots, \mathbf{x}_{Nj}),$$

$$\omega_{P} = \frac{Pk_{B}T}{\mathbf{x}}$$

Classical correspondence: classical (or simulated) annealing (CA): MD simulation with time-dependent T(t).

## 3. Benchmark: asymmetric double well

The local density from 200-ps PIMD simulations follows adiabatically the exact instantaneous quantum density. T = 100 K.



## 4.1 Lennard-Jones clusters

LJ clusters: millions of estimated local minima with just a few tens of atoms!

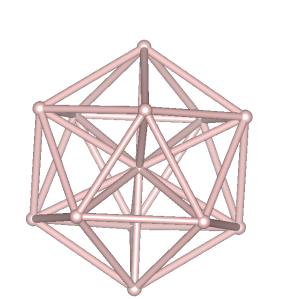
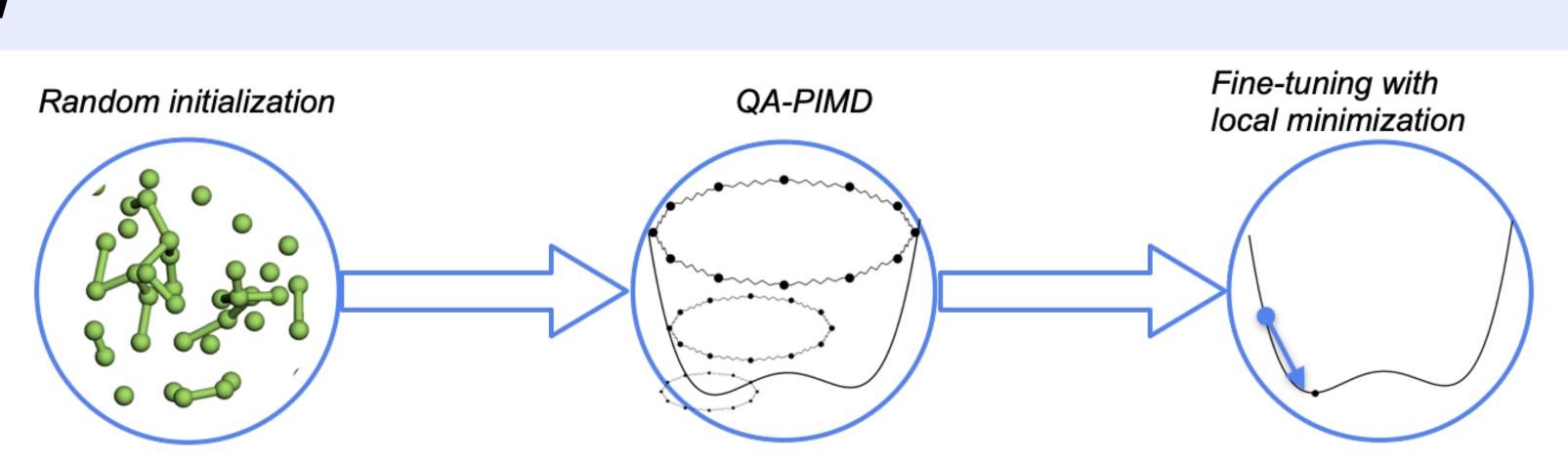


Figure: Global minimum of a LJ cluster with N=13.

## 7. Summary of the workflow



## 4.2 LJ clusters: classical vs quantum

3.2 Missing hydrogens' sites

Hydrogen's positions are hardly detected in X-ray scattering, resulting in a large dataset of structures missing hydrogen positions. The 10 materials are simulated with MACE's foundational **MLIP** 

## 3. Results

#### 4. Conclusion

- QA-PIMD is an unbiased and general novel global optimization algorithm using quantum fluctuations.
- It can outperform classical annealing. E.g., shorter annealing time needed for LJ clusters.
- Material discovery: new candidate stable crystals from the MC3D database

### Open questions and challenges

- Small, but finite, temperature. Not a ground-state method.
- PIMD time-evolution is not exactly quantum, dynamically  $QA - PIMD \neq QA$ . Work in progress.

#### 5. References

- 1. A. Fiorentino and N. Marzari. *Quantum* annealing for material sciences. Manuscript in preparation
- 2. R. P. Feynman et al., Quantum Mechanics and Path Integrals, Physics Today 19, 89 (1966).
- 3. T. Gregor et al., Chem. Phys. Lett. 412, 125 (2005).
- 4. L. Stella et al., Phys. Rev. B 72, 014303 (2005).

## 6. Acknowledgements

The authors are thankful for insightful discussions with S. Baroni, L. Vojáček, A. Carta, V. Sanella, and S. Schären. The authors acknowledge financial support by the NCCR MARVEL, a National Centre of Competence in Research, funded by the Swiss National Science Foundation (grant number 205602).