

Exercise 7

✓ return the clothes if (wrong sizes \cup defects \cup change mind)

return last month : $A = \frac{1}{2}$, $B = \frac{3}{10}$, $C = \frac{1}{5}$

i) $P(A \text{ return the cloth because change mind})$
 $= \frac{3}{10}$

ii) $P(C \text{ return because wrong size})$
 $= \frac{3}{8}$

iii) $P(B \text{ return because of defects})$
 $= \frac{1}{2}$

Exercise 8

51% adults = males = 0.51

1 adult is randomly selected

$$\begin{aligned} \text{a) } P(\text{female}) &= 1 - 0.51 \\ &= 0.49 \end{aligned}$$

$$\begin{aligned} \text{b) } 9.5\% &= 0.095 = M \cap R \text{ (males from rural area)} \\ 1.7\% &= 0.017 = \bar{M} \cap R \text{ (female from rural area)} \end{aligned}$$

$$\begin{aligned} \text{i) } P(R|M) &= \frac{P(R \cap M)}{P(M)} \\ &= \frac{0.095}{0.51} \\ &= 0.1863 \end{aligned}$$

$$\begin{aligned} \text{ii) } P(M|R) &= \frac{P(M \cap R)}{P(R)} \\ &= \frac{0.095}{0.112} \\ &= 0.8482 \end{aligned}$$

$$\begin{aligned} P(R) &= P(M \cap R) \\ &\quad + P(\bar{M} \cap R) \\ &= 0.095 + 0.017 \\ &= 0.112 \end{aligned}$$

$$\begin{aligned} \text{iii) Apple Country} &= 100,000 \text{ adults} \\ n(\bar{M} \cap \bar{R}) &= ? \end{aligned}$$

$$P(\bar{M}) = 0.49$$

$$\begin{aligned} P(\bar{R}) &= 1 - 0.112 \\ &= 0.888 \end{aligned}$$

$$n(\bar{M} \cap \bar{R}) =$$

$$P(\bar{M} \cap R) = 0.017$$

$$= 0.450216 \times 100,000$$

$$\begin{aligned} P(\bar{M}) &= 0.49 + 0.017 \\ &= 0.507 \end{aligned}$$

$$= 45021.6$$

$$\begin{aligned} P(\bar{M} \cap \bar{R}) &= 0.507 \times 0.888 \\ &= 0.450216 \end{aligned}$$

$$\approx 45022$$

Exercise 9

$$45\% = \text{prison} = P$$

$$40\% = P(G|P)$$

$$55\% = P(G|\bar{P})$$

$$\begin{aligned} \text{i) } P(\bar{P}) &= 1 - 0.45 \\ &= 0.55 \end{aligned}$$

$$\begin{aligned} \text{ii) } P(P|G) &= \frac{P(G|P)P(P)}{P(G|P)P(P) + P(G|\bar{P})P(\bar{P})} \\ &= \frac{0.4(0.45)}{0.4(0.45) + 0.55(0.55)} \\ &= 0.3731 \end{aligned}$$

$$\begin{aligned} \text{iii) } P(\bar{P}|G) &= \frac{P(G|\bar{P})P(\bar{P})}{P(G|\bar{P})P(\bar{P}) + P(G|P)P(P)} \\ &= \frac{0.55(0.55)}{0.55(0.55) + 0.4(0.45)} \\ &= 0.6269 \end{aligned}$$

$$\begin{aligned} \text{iv) } P(G) &= P(G|P)P(P) + P(G|\bar{P})P(\bar{P}) \\ &= 0.4(0.45) + 0.55(0.55) \\ &= 0.4825 \end{aligned}$$