A B1A003

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careeryuga.com Reg. No. Name: APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY THIRD SEMESTER B.TECH DEGREE EXAMINATION, DEC 2016 **Course Code: MA201** Course Name: LINEAR ALGEBRA AND COMPLEX ANALYSIS Duration: 3. Hours Max. Marks: 100 PART A (Answer any two questions) Show that $u = y^3 - 3x^2y$ is harmonic and hence find its harmonic conjugate. 1.a (8)Find the image of $\left|z-\frac{1}{2}\right| \leq \frac{1}{2}$ under the transformation $=\frac{1}{z}$. Also find the fixed points b of the transformation $w = \frac{1}{z}$ 2.a Define an analytic function and prove that an analytic function of constant modulus is (8)constant. Find the linear fractional transformation that maps $z_1 = 0$, $z_2 = 1$, $z_3 = \infty$ onto b $w_1 = -1$, $w_2 = -i$, $w_3 = 1$ respectively. (7)Show that $f(z) = e^{-x} \cos y - i e^{-x} \sin y$ is differentiable everywhere. Find 3.a (8)its derivative. Find the image of the lines x = c and y = k, where c & k are constants, under the b transformation w = sinz. (7) PART B (Answer any two questions) Evaluate $\int_C Re(z) dz$ where C is a straight line from 0 to 1 + 2i. 4.a (7) Show that $\int_0^\infty \frac{dx}{1+x^4} = \frac{\pi}{2\sqrt{2}}$ (8)b Integrate $\frac{z^2}{z^2-1}$ counterclockwise around the circle $|z-1-i|=\frac{\pi}{2}$ by Cauchy's 5.a (7)Integral Formula. Evaluate $\int_C \frac{z^{-23}}{z^2-4z-5} dz$ where C is |z-2-i|=3.5 by Cauchy's Residue Theorem b (8)If $f(z) = \frac{1}{z^2}$ find the Taylor series that converges in |z - i| < R and the Laurent's 6.a series that converges in |z - i| > R. (8)Define three types of isolated singularities with an example for each. b (7)

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PART C

(Answer any two questions)

7.a Solve by Gauss Elimination:

$$x_1 - x_2 + x_3 = 0,$$

$$-x_1 + x_2 - x_3 = 0,$$

$$10 \ x_2 + 25 \ x_3 = 90,$$

$$20 \ x_1 + 10 \ x_2 = 80.$$
(5)

b Find the rank. Also find a basis for the row space and column space for

$$\begin{bmatrix} 0 & 1 & 0 \\ -1 & 0 & -4 \\ 0 & 4 & 0 \end{bmatrix} \tag{5}$$

cFind out what type of conic section the quadratic form

 $Q = 17 x^2 - 30 xy + 17 y^2 = 128$ represents and transform it to the principal (10)axes.

- Find whether the vectors $\begin{bmatrix} 1 & 2-1 & 3 \end{bmatrix}$, $\begin{bmatrix} 2 & -13 & 2 \end{bmatrix}$ and $\begin{bmatrix} -1 & 8-9 & 5 \end{bmatrix}$ are 8.a linearly dependent. (5)
 - Show that the matrix $A = \begin{bmatrix} 1 & 2 \\ 2 & -2 \end{bmatrix}$ is symmetric. Find the spectrum. (5)
 - (10)
- Diagonalise $A = \begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{bmatrix}$ Determine whether the matrix $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1/\sqrt{2} & -1/\sqrt{2} \\ 0 & 1/\sqrt{2} & 1/\sqrt{2} \end{bmatrix}$ is orthogonal? 9. a. (5)
 - Find the Eigen values and Eigen vectors of $\begin{bmatrix} 1 & 1 & 2 \\ -1 & 2 & 1 \\ 0 & 1 & 3 \end{bmatrix}$ b. (5)
 - Define a Vector Space with an example. c. (10)