

# Fundamentals of Power Electronics

Third Edition



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### **Magnetics Design Tables**

Geometrical data for several standard ferrite core shapes are listed here. The geometrical constant  $K_g$  is a measure of core size, useful for designing inductors and transformers that attain a given copper loss [99]. The  $K_g$  method for inductor design is described in Chap. 11.  $K_g$  is defined as

$$K_g = \frac{A_c^2 W_A}{MLT} \tag{B.1}$$

where  $A_c$  is the core cross-sectional area,  $W_A$  is the window area, and MLT is the winding meanlength-per-turn. The geometrical constant  $K_{gfe}$  is a similar measure of core size, which is useful for designing ac inductors and transformers when the total copper plus core loss is constrained. The  $K_{gfe}$  method for magnetics design is described in Chap. 12.  $K_{gfe}$  is defined as

$$K_{gfe} = \frac{W_A A_c^{2(1-1/\beta)}}{MLT \,\ell_m^{2/\beta}} u(\beta)$$
 (B.2)

where  $\ell_m$  is the core mean magnetic path length, and  $\beta$  is the core loss exponent:

$$P_{fe} = K_{fe} B_{max}^{\beta} \tag{B.3}$$

For modern ferrite materials,  $\beta$  typically lies in the range 2.6 to 2.8. The quantity  $u(\beta)$  is defined as

$$u(\beta) = \left[ \left( \frac{\beta}{2} \right)^{-\left(\frac{\beta}{\beta+2}\right)} + \left( \frac{\beta}{2} \right)^{\left(\frac{2}{\beta+2}\right)} \right]^{-\left(\frac{\beta+2}{\beta}\right)}$$
(B.4)

 $u(\beta)$  is equal to 0.305 for  $\beta = 2.7$ . This quantity varies by roughly 5% over the range  $2.6 \le \beta \le 2.8$ . Values of  $K_{gfe}$  are tabulated for  $\beta = 2.7$ ; variation of  $K_{gfe}$  over the range  $2.6 \le \beta \le 2.8$  is typically quite small.

Thermal resistances are listed in those cases where published manufacturer's data are available. The thermal resistances listed are the approximate temperature rise from the center leg of the core to ambient, per watt of total power loss. Different temperature rises may be observed under conditions of forced air cooling, unusual power loss distributions, etc. Listed window areas are the winding areas for conventional single-section bobbins.

An American Wire Gauge table is included at the end of this appendix.

### **B.1 Pot Core Data**

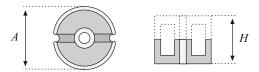


Fig. B.1 Pot core

| Core<br>type | Geometrical constant  | Geometrical constant | Cross-<br>sectional<br>area | Bobbin<br>winding<br>area |      | path     | Thermal resistance |     |
|--------------|-----------------------|----------------------|-----------------------------|---------------------------|------|----------|--------------------|-----|
| (AH)         | $K_g$                 | $K_{gfe}$            | $A_c$                       | $W_A$                     | MLT  | $\ell_m$ | $R_{th}$           |     |
| (mm)         | cm <sup>5</sup>       | cm <sup>x</sup>      | $(cm^2)$                    | $(cm^2)$                  | (cm) | (cm)     | (°C/W)             | (g) |
| 704          | $0.738 \cdot 10^{-6}$ | $1.61 \cdot 10^{-6}$ | 0.070                       | $0.22 \cdot 10^{-3}$      | 1.46 | 1.0      |                    | 0.5 |
| 905          | $0.183 \cdot 10^{-3}$ | $256 \cdot 10^{-6}$  | 0.101                       | 0.034                     | 1.90 | 1.26     |                    | 1.0 |
| 1107         | $0.667 \cdot 10^{-3}$ | $554 \cdot 10^{-6}$  | 0.167                       | 0.055                     | 2.30 | 1.55     |                    | 1.8 |
| 1408         | $2.107 \cdot 10^{-3}$ | $1.1 \cdot 10^{-3}$  | 0.251                       | 0.097                     | 2.90 | 2.00     | 100                | 3.2 |
| 1811         | $9.45 \cdot 10^{-3}$  | $2.6\cdot10^{-3}$    | 0.433                       | 0.187                     | 3.71 | 2.60     | 60                 | 7.3 |
| 2212         | 27.1 10-3             | $4.9 \cdot 10^{-3}$  | 0.625                       | 0.207                     | 4.42 | 2.15     | 20                 | 1.2 |
| _            | $27.1 \cdot 10^{-3}$  | , 10                 | 0.635                       | 0.297                     | 4.42 | 3.15     | 38                 | 13  |
| 2616         | $69.1 \cdot 10^{-3}$  | $8.2 \cdot 10^{-3}$  | 0.948                       | 0.406                     | 5.28 | 3.75     | 30                 | 20  |
| 3019         | 0.180                 | $14.2 \cdot 10^{-3}$ | 1.38                        | 0.587                     | 6.20 | 4.50     | 23                 | 34  |
| 3622         | 0.411                 | $21.7 \cdot 10^{-3}$ | 2.02                        | 0.748                     | 7.42 | 5.30     | 19                 | 57  |
| 4229         | 1.15                  | $41.1\cdot 10^{-3}$  | 2.66                        | 1.40                      | 8.60 | 6.81     | 13.5               | 104 |

### **B.2** EE Core Data

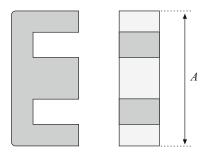


Fig. B.2 EE core

| Core<br>type | Geometrical constant  | Geometrical constant  | Cross-<br>sectional | Bobbin winding     |          | Magnetic path | Core weight |
|--------------|-----------------------|-----------------------|---------------------|--------------------|----------|---------------|-------------|
|              |                       |                       | area                | area               | per turn | length        |             |
| (A)          | $K_g$                 | $K_{gfe}$             | $A_c$               | $W_A$              | MLT      | $\ell_m$      |             |
| (mm)         | (cm <sup>5</sup> )    | $(cm^x)$              | $(cm^2)$            | (cm <sup>2</sup> ) | (cm)     | (cm)          | (g)         |
| EE12         | $0.731 \cdot 10^{-3}$ | $0.458 \cdot 10^{-3}$ | 0.14                | 0.085              | 2.28     | 2.7           | 2.34        |
| EE16         | $2.02 \cdot 10^{-3}$  | $0.842 \cdot 10^{-3}$ | 0.19                | 0.190              | 3.40     | 3.45          | 3.29        |
| EE19         | $4.07 \cdot 10^{-3}$  | $1.3 \cdot 10^{-3}$   | 0.23                | 0.284              | 3.69     | 3.94          | 4.83        |
| EE22         | $8.26 \cdot 10^{-3}$  | $1.8 \cdot 10^{-3}$   | 0.41                | 0.196              | 3.99     | 3.96          | 8.81        |
| EE30         | $85.7 \cdot 10^{-3}$  | $6.7 \cdot 10^{-3}$   | 1.09                | 0.476              | 6.60     | 5.77          | 32.4        |
|              |                       |                       |                     |                    |          |               |             |
| EE40         | 0.209                 | $11.8 \cdot 10^{-3}$  | 1.27                | 1.10               | 8.50     | 7.70          | 50.3        |
| EE50         | 0.909                 | $28.4 \cdot 10^{-3}$  | 2.26                | 1.78               | 10.0     | 9.58          | 116         |
| EE60         | 1.38                  | $36.4 \cdot 10^{-3}$  | 2.47                | 2.89               | 12.8     | 11.0          | 135         |
| EE70/68/19   | 5.06                  | $75.9 \cdot 10^{-3}$  | 3.24                | 6.75               | 14.0     | 18.0          | 280         |

### **B.3 EC Core Data**

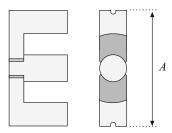


Fig. B.3 EC core

| Core | Geometrical        | Geometrical          | Cross-    | Bobbin             | Mean     | Magnetic | Thermal    | Core   |
|------|--------------------|----------------------|-----------|--------------------|----------|----------|------------|--------|
| type | constant           | constant             | sectional | winding            | length   | path     | resistance | weight |
|      |                    |                      | area      | area               | per turn | length   |            |        |
| (A)  | $K_g$              | $K_{gfe}$            | $A_c$     | $W_A$              | MLT      | $\ell_m$ | $R_{th}$   |        |
| (mm) | (cm <sup>5</sup> ) | $(cm^x)$             | $(cm^2)$  | (cm <sup>2</sup> ) | (cm)     | (cm)     | (°C/W)     | (g)    |
| EC35 | 0.131              | $9.9\cdot 10^{-3}$   | 0.843     | 0.975              | 5.30     | 7.74     | 18.5       | 35.5   |
| EC41 | 0.374              | $19.5 \cdot 10^{-3}$ | 1.21      | 1.35               | 5.30     | 8.93     | 16.5       | 57.0   |
| EC52 | 0.914              | $31.7 \cdot 10^{-3}$ | 1.80      | 2.12               | 7.50     | 10.5     | 11.0       | 111    |
| EC70 | 2.84               | $56.2 \cdot 10^{-3}$ | 2.79      | 4.71               | 12.9     | 14.4     | 7.5        | 256    |

### **B.4 ETD Core Data**

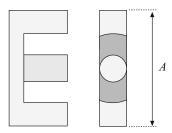


Fig. B.4 ETD core

| Core  | Geometrical        | Geometrical          | Cross-    | Bobbin   | Mean     | Magnetic | Thermal    | Core   |
|-------|--------------------|----------------------|-----------|----------|----------|----------|------------|--------|
| type  | constant           | constant             | sectional | winding  | length   | path     | resistance | weight |
|       |                    |                      | area      | area     | per turn | length   |            |        |
| (A)   | $K_g$              | $K_{gfe}$            | $A_c$     | $W_A$    | MLT      | $\ell_m$ | $R_{th}$   |        |
| (mm)  | (cm <sup>5</sup> ) | $(cm^x)$             | $(cm^2)$  | $(cm^2)$ | (cm)     | (cm)     | (°C/W)     | (g)    |
| ETD29 | 0.0978             | $8.5 \cdot 10^{-3}$  | 0.76      | 0.903    | 5.33     | 7.20     |            | 30     |
| ETD34 | 0.193              | $13.1 \cdot 10^{-3}$ | 0.97      | 1.23     | 6.00     | 7.86     | 19         | 40     |
| ETD39 | 0.397              | $19.8 \cdot 10^{-3}$ | 1.25      | 1.74     | 6.86     | 9.21     | 15         | 60     |
| ETD44 | 0.846              | $30.4 \cdot 10^{-3}$ | 1.74      | 2.13     | 7.62     | 10.3     | 12         | 94     |
| ETD49 | 1.42               | $41.0 \cdot 10^{-3}$ | 2.11      | 2.71     | 8.51     | 11.4     | 11         | 124    |

## **B.5 PQ Core Data**

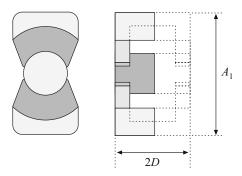


Fig. B.5 PQ core

| Core       | Geometrical          | Geometrical          | Cross-    | Bobbin             | Mean     | Magnetic | Core   |
|------------|----------------------|----------------------|-----------|--------------------|----------|----------|--------|
| type       | constant             | constant             | sectional | winding            | length   | path     | weight |
|            |                      |                      | area      | area               | per turn | length   |        |
| $(A_1/2D)$ | $K_g$                | $K_{gfe}$            | $A_c$     | $W_A$              | MLT      | $\ell_m$ |        |
| (mm)       | (cm <sup>5</sup> )   | $(cm^x)$             | $(cm^2)$  | (cm <sup>2</sup> ) | (cm)     | (cm)     | (g)    |
|            | $22.4\cdot10^{-3}$   | $3.7\cdot 10^{-3}$   | 0.62      | 0.256              | 4.4      | 3.74     | 13     |
|            | $33.6 \cdot 10^{-3}$ | $4.8 \cdot 10^{-3}$  | 0.62      | 0.384              | 4.4      | 4.54     | 15     |
| PQ26/20    | $83.9 \cdot 10^{-3}$ | $7.2 \cdot 10^{-3}$  | 1.19      | 0.333              | 5.62     | 4.63     | 31     |
| PQ26/25    | 0.125                | $9.4 \cdot 10^{-3}$  | 1.18      | 0.503              | 5.62     | 5.55     | 36     |
|            |                      |                      |           |                    |          |          |        |
| PQ32/20    | 0.203                | $11.7 \cdot 10^{-3}$ | 1.70      | 0.471              | 6.71     | 5.55     | 42     |
| PQ32/30    | 0.384                | $18.6 \cdot 10^{-3}$ | 1.61      | 0.995              | 6.71     | 7.46     | 55     |
| PQ35/35    | 0.820                | $30.4 \cdot 10^{-3}$ | 1.96      | 1.61               | 7.52     | 8.79     | 73     |
| PQ40/40    | 1.20                 | $39.1 \cdot 10^{-3}$ | 2.01      | 2.50               | 8.39     | 10.2     | 95     |

**B.6** American Wire Gauge Data

| AWG # | Bare area,             | Resistance,                 | Diameter, |
|-------|------------------------|-----------------------------|-----------|
|       | $10^{-3} \text{ cm}^2$ | $10^{-6}\Omega/\mathrm{cm}$ | cm        |
| 0000  | 1072.3                 | 1.608                       | 1.168     |
| 000   | 850.3                  | 2.027                       | 1.040     |
| 00    | 674.2                  | 2.557                       | 0.927     |
|       |                        |                             |           |
| 0     | 534.8                  | 3.224                       | 0.825     |
| 1     | 424.1                  | 4.065                       | 0.735     |
| 2     | 336.3                  | 5.128                       | 0.654     |
| 3     | 266.7                  | 6.463                       | 0.583     |
| 4     | 211.5                  | 8.153                       | 0.519     |
|       |                        |                             |           |
| 5     | 167.7                  | 10.28                       | 0.462     |
| 6     | 133.0                  | 13.0                        | 0.411     |
| 7     | 105.5                  | 16.3                        | 0.366     |
| 8     | 83.67                  | 20.6                        | 0.326     |
| 9     | 66.32                  | 26.0                        | 0.291     |
| 10    | 50.41                  | 22.0                        | 0.267     |
| 10    | 52.41                  | 32.9                        | 0.267     |
| 11    | 41.60                  | 41.37                       | 0.238     |
| 12    | 33.08                  | 52.09                       | 0.213     |
| 13    | 26.26                  | 69.64                       | 0.190     |
| 14    | 20.02                  | 82.80                       | 0.171     |
| 15    | 16.51                  | 104.3                       | 0.153     |
| 16    | 13.07                  | 131.8                       | 0.137     |
| 17    | 10.39                  | 165.8                       | 0.122     |
| 18    | 8.228                  | 209.5                       | 0.109     |
| 19    | 6.531                  | 263.9                       | 0.0948    |
|       |                        |                             |           |
| 20    | 5.188                  | 332.3                       | 0.0874    |
| 21    | 4.116                  | 418.9                       | 0.0785    |
| 22    | 3.243                  | 531.4                       | 0.0701    |
| 23    | 2.508                  | 666.0                       | 0.0632    |
| 24    | 2.047                  | 842.1                       | 0.0566    |
| 2.7   | 1.600                  | 1062.0                      | 0.0707    |
| 25    | 1.623                  | 1062.0                      | 0.0505    |
| 26    | 1.280                  | 1345.0                      | 0.0452    |
| 27    | 1.021                  | 1687.6                      | 0.0409    |
| 28    | 0.8046                 | 2142.7                      | 0.0366    |
| 29    | 0.6470                 | 2664.3                      | 0.0330    |

(continued)

| AWG # | Bare area, $10^{-3} \text{ cm}^2$ | Resistance, $10^{-6} \Omega/\text{cm}$ | Diameter,<br>cm |
|-------|-----------------------------------|--|-----------------|
| 30    | 0.5067                            | 3402.2                                 | 0.0294          |
| 31    | 0.4013                            | 4294.6                                 | 0.0267          |
| 32    | 0.3242                            | 5314.9                                 | 0.0241          |
| 33    | 0.2554                            | 6748.6                                 | 0.0236          |
| 34    | 0.2011                            | 8572.8                                 | 0.0191          |
| 35    | 0.1589                            | 10849                                  | 0.0170          |
| 36    | 0.1266                            | 13608                                  | 0.0152          |
| 37    | 0.1026                            | 16801                                  | 0.0140          |
| 38    | 0.08107                           | 21266                                  | 0.0124          |
| 39    | 0.06207                           | 27775                                  | 0.0109          |
| 40    | 0.04869                           | 35400                                  | 0.0096          |
| 41    | 0.03972                           | 43405                                  | 0.00863         |
| 42    | 0.03166                           | 54429                                  | 0.00762         |
| 43    | 0.02452                           | 70308                                  | 0.00685         |
| 44    | 0.0202                            | 85072                                  | 0.00635         |

# PRINCIPLES OF POWER ELECTRONICS

**Second Edition** 

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Page-685

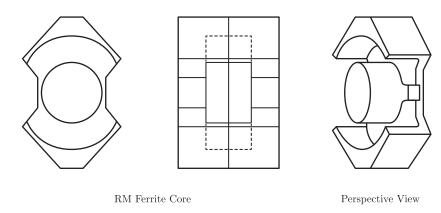


Figure 20.2 Representative core shape for the RM family of ferrite cores. The illustration shows the geometry of the RM8, RM10 and RM12 cores.

Core factor, which has units of linear dimension to the fifth power (e.g.,  $m^5$ ), expresses a geometrical property of a magnetic core. Given a design requirement for a filter inductor as expressed by the left side of (20.15), we know the minimum value of  $K_g$  that a core must have to implement the inductor. A designer may calculate  $K_g$  for a given core from data sheet information, or leverage pre-tabulated values of  $K_g$ , which are available for a variety of cores. For example, Table 20.1 shows a variety of data about the RM (Rectangular Modular) family of ferrite cores, including the core factor  $K_g$ . The physical structure of RM-type cores is illustrated in Fig. 20.2. The core halves are designed to clamp around a toroidal bobbin and winding such that the inductor presents an approximately square footprint. The cylindrical centerpost may be machined down on one or both core halves to provide a gap for energy storage.

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686

|      | Effective       | Effective            | Minimum              | Core            | Bobbin               | Bobbin                        |
|------|-----------------|----------------------|----------------------|-----------------|----------------------|-------------------------------|
|      | Magnetic        | Core Area            | Core Area            | Window          | Window               | Mean                          |
| Core | Path Length     |                      |                      | Area            | Area                 | Turn Length                   |
|      | $\ell_c$        | $A_{c,e}$            | $A_{c,\mathrm{min}}$ | $W_{A,c}$       | $W_{A,b}$            | $\ell_t$                      |
|      | (mm)            | $(mm^2)$             | $(mm^2)$             | $(mm^2)$        | $(mm^2)$             | (mm)                          |
| RM4  | 22.7            | 14.0                 | 10.7                 | 15.6            | 7.7                  | 20                            |
| RM5  | 22.4            | 23.7                 | 17.3                 | 18.2            | 9.5                  | 25                            |
| RM6  | 28.6            | 36.6                 | 30.2                 | 26.0            | 15                   | 30                            |
| RM8  | 38.0            | 64.0                 | 53.5                 | 48.9            | 30.0                 | 42                            |
| RM10 | 44.0            | 98.0                 | 86.6                 | 69.5            | 41.5                 | 52                            |
| RM12 | 56.9            | 140                  | 121                  | 110             | 73.0                 | 61                            |
| RM14 | 70.0            | 178                  | 165                  | 155             | 107                  | 71.5                          |
|      | Effective       | Core                 | Effective            | Thermal         | Core                 | Core                          |
|      | Core            | $\operatorname{Set}$ | Surface              | Resistance      | Area                 | Factor                        |
| Core | Volume          | Weight               | Area                 |                 | Product              | $K_g$                         |
|      | $V_{c,e}$       |                      | $A_{s,e}$            | $R_{th}$        | $A_{c,e}W_{A,b}$     | $A_{c,\min}^2 W_{A,b}/\ell_t$ |
|      | $(\text{mm}^3)$ | (g)                  | $(mm^2)$             | $(^{\circ}C/W)$ | $(\mathrm{mm}^4)$    | $(\mathrm{mm}^5)$             |
| RM4  | 318             | 1.7                  | 586                  | 86              | $1.1 \times 10^{2}$  | $4.4 \times 10^{1}$           |
| RM5  | 530             | 3.0                  | 787                  | 69              | $2.3 \times 10^{2}$  | $1.1 \times 10^{2}$           |
| RM6  | 1050            | 5.5                  | 1130                 | 60              | $5.5 \times 10^{2}$  | $4.6 \times 10^{2}$           |
| RM8  | 2430            | 13                   | 2020                 | 38              | $1.92 \times 10^{3}$ | $2.0 \times 10^{3}$           |
| RM10 | 4310            | 23                   | 2960                 | 30              | $4.07 \times 10^{3}$ | $6.0 \times 10^{3}$           |
| RM12 | 7970            | 42                   | 4460                 | 23              | $1.02 \times 10^{4}$ | $1.8 \times 10^{4}$           |
| RM14 |                 |                      |                      |                 | $1.90 \times 10^{4}$ | $4.07 \times 10^{4}$          |

Core Data for the RM (Rectangular Modular) family of ferrite cores.  $\,$ **Table 20.1** 

