Introduction and Theoretical Foundations Empirical Industrial Organization

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Organization

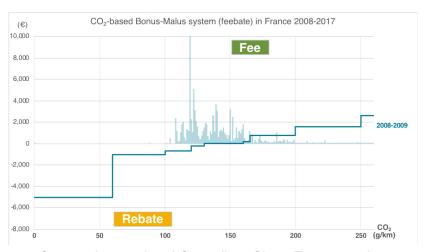
- additional material will be posted at https://github. com/afniedermayer/empiricalio2020bern
- if you have any questions, write to: andras.niedermayer@u-cergy.fr
- please bring along your laptops for the hands-on computer exercises
- please install Anaconda Python 3.7 on your laptops
 https://www.anaconda.com/distribution/
- we will have a combination of lectures, hands-on exercises in class and take home work
- the grade will be based on a take home exam/term paper

Examples of Application of Empirical Industrial Organization

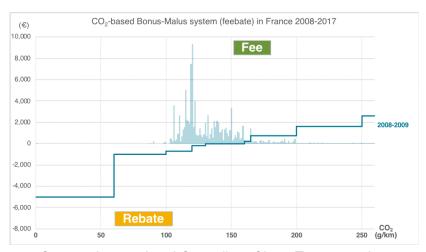
- car industry, environmental policy
- auctions
- price discrimination

- merger control
 - for example, in 2017 the PSA Group acquired Opel and Vauxhall
 - should competition authorities have cleared the acquisition?
 - counterfactual: what is the prediction on price changes for the acquisition?

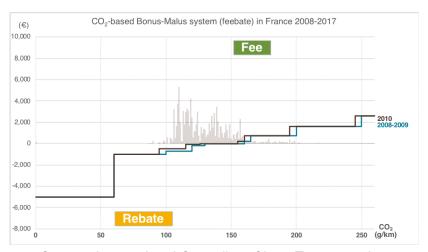
- environmental policy
 - for example, France introduced a feebate policy for cars in 2008
 - high CO2 emission cars get taxed, low CO2 emission cars get a rebate
 - the intention was to have a balanced budget



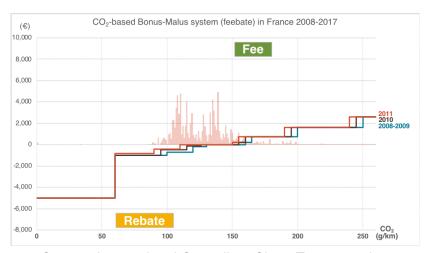
Source: International Council on Clean Transportation



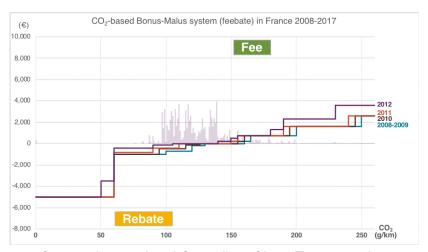
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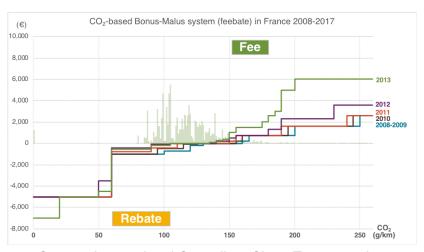
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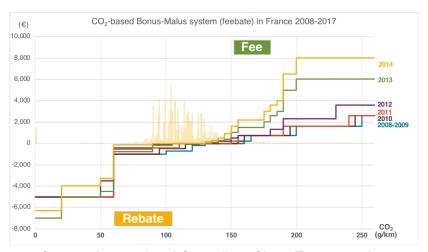
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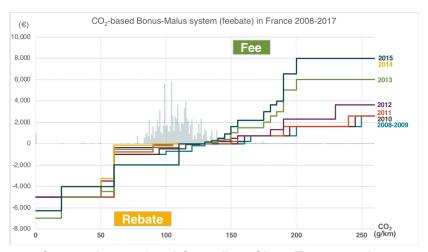
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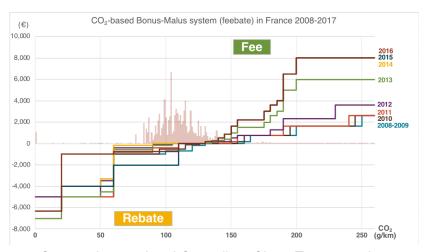
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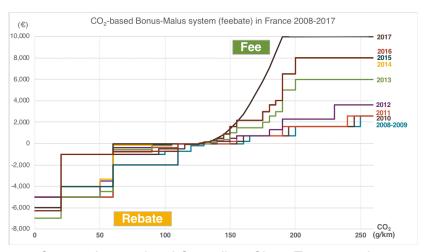
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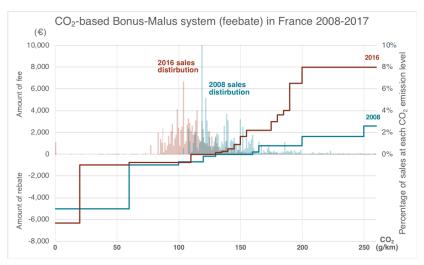


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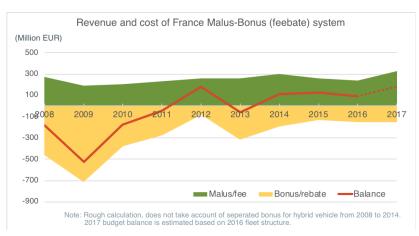
Source: International Council on Clean Transportation

2008 vs 2016



Source: International Council on Clean Transportation

Budget



Source: International Council on Clean Transportation

Examples: Auctions



Examples: Auctions

auctions

- for example, every year that Canadian government auctions off rights to log on government land
- What is the optimal auction format?
- Which minimal price should the government set?
- procurement auctions
 - (the government) buys from the lowest bidder on a project,
 e.g. the construction of roads
 - "Operation Hammer" in Quebec, started in 2009: uncovered widespread collusion in the bidding for government construction contracts
 - How do you detect collusion?
 - How do you compute damages from collusion?

Examples: Price Discrimination

Automobiles



Renault Clio €16,600, power: 58 kW

Examples: Price Discrimination

Automobiles



€11,300 power: 43 kW



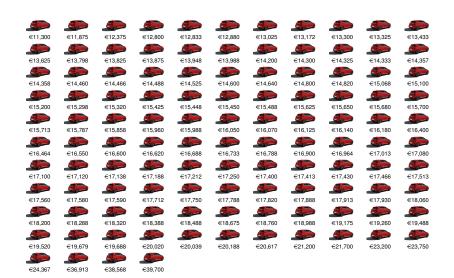
€16,600 power: 58 kW



€39,700 power: 187 kW

Examples: Price Discrimination

Automobiles



Outlook for Classes

- theory
 - monopoly
 - monopolistic price discrimination
 - auctions
 - discrete choice random utility models
- introduction to the Python programming language
- econometrics
 - auction econometrics
 - econometrics of price discrimination
 - discrete choice estimation

Monopoly

The theoretical part of this course is based on Régis Renault's slides.

- monopolist price above marginal costs
- monopolist causes a deadweight loss
- the deadweight loss is due to the trade-off between marginal and inframarginal buyers

Demand Elasticity

- monopoly markup is higher when demand is less elastic
- ⇒ demand elasticity is an important factor investigated by empirical industrial organization

Demand elasticity and deadweight loss

- A lower elasticity leads to a larger difference between the price and the marginal cost, but the effect on quantity is smaller
- ⇒ effect on deadweight loss is not obvious
- consider how a change of elasticity affects the ration of the deadweight loss (DWL) to the first best total surplus (the deadweight loss, consumer surplus (CS) and producer surplus (PS))
- for a constant elasticity of demand $D(p)=p^{-\epsilon}$ for some $\epsilon<-1$
- as ϵ decreases from -1 to $-\infty$, the ratio DWL/(DWL + PS + CS) increases

Demand curvature and deadweight loss

- constant elasticity is a special case of a more general class of demands: ρ-linear demands
- consider D(p) such that $D(p)^{\rho}$ is linear in p for some number ρ : e.g. constant elasticity of demands are ρ -linear for $\rho = 1/\epsilon$
- it can be shown that as ρ increases from -1 to $+\infty$, the ratio of DWL/(DWL+CS+PS) first increases and than decreases to zero where the turning point is for some $\rho>0$
- as ρ increases, the monopolist captures a larger share of overall surplus and if that share is sufficiently high, the firm causes less inefficiency
- the limit corresponds to a rectangular demand where there is no deadweight loss and the firm captures the entire surplus

Comparative statics

- consider two differentiable total cost functions C_1 and C_2 such that $C_1' > C_2'$ for all positive quantities
- q_i^m and p_i^m are monopoly quantity and price for cost function C_i
- because q_i^m and p_i^m maximize profit we have the two following inequalities:

$$p_1^m q_1^m - C_1(q_1^m) \ge p_2^m q_2^m - C_1(q_2^m)$$

and

$$p_2^m q_2^m - C_2(q_2^m) \ge p_1^m q_1^m - C_2(q_1^m)$$

• Taking the difference of the two inequalities yields:

$$[C_{2}(q_{1}^{m})-C_{1}(q_{1}^{m})]-[C_{2}(q_{2}^{m})-C_{1}(q_{2}^{m})]\geq 0$$

or equivalently

$$\int_{q_2^m}^{q_1^m} C_2'(q) - C_1'(q) dq \geq 0$$

- since $C_2' C_1' > 0$, we must have $q_1^m > q_2^m$ and hence (since demand is decreasing) $p_1^m < p_2^m$
- This shows that an increase in marginal cost leads to an increase in the monopoly price.

Some comparative statics: change in marginal costs

• Assume a constant marginal cost c > 0. From the price FOC monopoly price p^m satisfies

$$p^m-c=-rac{D\left(p^m
ight)}{D'\left(p^m
ight)}$$

• Let $g(p^m) = D(p^m)/D'(p^m)$. Standard comparative statics shows that

$$\frac{dp^{m}}{dc} = \frac{1}{1 + g'(p^{m})}$$

• The impact of a cost increase is < 1 (resp. > 1) if and only if g' > 0 (rep. g' < 0)

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- Note that g' > 0 over some price range iff D is log-concave (i.e. In D is concave) over that range.
- For instance linear demand, D(p) = 1 p, is logconcave on [0, 1]
- More generally, ρ -linear demand $D(p) = (1-p)^{\frac{1}{\rho}}$, with $\rho > 0$ is logconcave on [0,1]
- This is not the case for constant elasticity demands: $\ln D$ is convex on $[0, +\infty)$
- then an increase in marginal cost of 1 Euro causes an increase in price of more that 1 Euro.
- More generally, all ρ -linear demands with $\rho <$ 0 are log convex

Some comparative statics: Taxes

 Consider a unit tax t. Monopolist chooses price p^m to solve:

$$\max_{p^m} p^m D(p^m + t) - C(D(p^m + t))$$

Necessary FOCs are:

$$D(p^{m} + t) + [p^{m} - C'(D(p^{m} + t))]D'(p^{m} + t) = 0$$

• To restore efficiency, t must be set so that the price paid by consumers $p^m + t$ equals marg. cost $C'(D(p_t^m))$, so we have

$$t = \frac{D(p^m + t)}{D'(p^m + t)} < 0$$

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- Monopoly deadweight loss may be eliminated by using a unit subsidy.
- In practice, this solution is not used much, in particular because it would require some tax revenue thus causing distortions elsewhere.
- Typically, monopolies are regulated directly or government owned.

Some Second Order Conditions

- For FOCs to be not only nec. but also suf. we need restrictions on monopoly profit π^m : for quasiconcavity in price.
- Formally, the set of prices p at which $\pi^m(p) \ge k$ for some real number k should be convex.
- So profit is quasiconcave iff it does not have an interior local minimum.
- At an interior local min., 1st derivative must be zero and 2nd derivative must be > 0
- Hence profit is quasiconcave if whenever its first deriv. is 0 its second deriv. is > 0

- Assume constant marginal cost c.
- Profit is (p-c)D(p)
- first deriv. being 0 implies D(p) + (p c)D'(p) = 0
- second deriv. is 2D'(p) + (p-c)D''(p) so that by substituting the zero first deriv. in the second deriv. we have the following suf. condition for quasiconcavity:

$$2D'(p)^2 - D(p)D''(p) > 0$$
 (1)

ρ -concave demand functions

- A function D>0 with a convex domain is said to be ho-concave for some real number ho if $D^{
 ho}$ is concave for ho>0 and $-D^{
 ho}$ is concave for ho<0; D is zero-concave if it is logconcave.
- If D is ρ -concave for some ρ , then it is ρ' -concave for all $\rho'<\rho$

• Assume D is ρ -concave for $\rho < 0$. Then the second deriv. of D^{ρ} must be positive, which is equivalent to

$$-(\rho-1)D'(p)^2 - D(p)D''(p) \ge 0$$

- LHS strictly decreasing in ρ : so if $\rho > -1$, then the inequality is strict at $\rho = -1$, which yields the SOC (1)
- So ρ -concavity of demand, for $\rho > -1$, is sufficient for quasiconcavity of profit (in fact, (-1) -concavity is sufficient as well).
- This implies that logconcavity of demand is sufficient (this weaker assumption will be used in oligopolistic competition with product differentiation)

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- A population of L consumers.
- Monopolist sells one product.
- Then individual demand is characterized by a valuation for the product such that, consumer buys iff price is weakly below.

Linear random utility model LRUM.

• Consumer ℓ has the following utility:

$$U_{\ell} = \epsilon_{\ell} - p + y_{\ell}$$

if she buys at price p and $u_{\ell} = y_{\ell}$ if she does not buy, where y_{ℓ} is her revenue.

- $\epsilon_{\ell}, \ell = 1, ..., L$, are i.i.d. random variables with support [a, b] cumulative distribution function F and density f
- Then ℓ 's valuation is ϵ_{ℓ} , independent of her income (it is a quasilinear utility with no income effect).

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- Consumer ℓ buys iff $\epsilon_{\ell} \geq p$, which happens with probability 1 F(p)
- Then expected demand is

$$D(p) = L[1 - F(p)]$$

- L=1 and a uniform distribution on [0,1] for ϵ_ℓ yields linear demand D(p)=1-p
- If marginal cost is constant at $c \ge 0$ then price FOC is

$$p^{m}-c=\frac{1-F(p^{m})}{f(p^{m})}$$
 (2)

Increasing hazard rate and logconcavity

- RHS of (2) is the inverse of the hazard rate of ϵ_{ℓ} (which is $h = \frac{f}{1-F}$)
- Standard assumption is h increasing.
- This is equivalent to 1 F logconcave.
- Actually if f logconcave (which holds for many commonly used distributions) than 1 - F and F are logconcave as well (a consequence of the Prekopa-Borell theorem).

A durable goods monopoly

- A monopolist sells over several periods a good for which each consumer needs only one unit (a durable good).
- Then consumers engage in inter-temporal substitution and can wait if they expect price to fall.
- Then the monopolist creates competition for its sales in the current period if it cannot commit to not dropping the price in the future.

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Conjecture (The Coase Conjecture)

As the frequency of price changes becomes increasingly high, the monopoly profit tends to zero and all consumers by the product at a price close to marginal cost.

This result has been proved formally.

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Solutions to the Coase conjecture

- Renting.
- Most favored customer close whereby the firm commits to reimbursing a consumer if the price decreases.
- Planned obsolescence.

Price discrimination in the unit demand setting

Strict definition Price discrimination involves selling different units of "the same" product at different prices.

- Actual price discrimination practices often involve selling different products.
- A standard form of price discrimination with only one product is non linear pricing (e.g. quantity discounts).
- What about price discrimination when each buyer buys one unit?

Perfect discrimination

- Assume the firm knows ϵ_{ℓ} for each consumer and is allowed to charge a price conditional on ϵ_{ℓ} .
- By charging $p(\epsilon_{\ell}) = \epsilon_{\ell}$ and selling only to consumers for whom ϵ_{ℓ} exceeds marginal cost, the firm captures the entire social surplus..
- If social surplus is not max. then profit can be increased either by selling to a consumer for whom $\epsilon_\ell >$ marg. cost or by not selling to some consumer for whom $\epsilon_\ell <$ marg. cost.
- Constant marg. cost case can be illustrated graphically.

Screening

- Assume now that the firm only knows the distribution of ϵ_ℓ but not its realization for each consumer.
- Then price cannot be conditional on the realization of ϵ_{ℓ} .
- Hence, a consumer can freely choose within the menu of prices.
- Clearly, if the product can be purchased at two different prices, all consumers pick the lowest price and there is no price discrimination.
- To prevent such personal arbitrage the choice of a lower price must entail some cost.

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- To illustrate, assume that ϵ_{ℓ} can take on value θ_{1} with probability $\lambda \in (0,1)$ and θ_{2} with prob. $1 \lambda, \theta_{1} < \theta_{2}$
- Firm has marginal cost $c \ge 0$ and consumers are risk neutral.
- To circumvent personal arbitrage, we allow for stochastic pricing mechanisms.
- Formally, the firm offers a menu of pricing schemes (q, T) where q is the probability that the product is delivered to the consumer and T is the money transfer between the consumer and the firm..

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- We have a two stage leader follower game where:
 - in stage 1 the firm offers a menu of pricing schemes;
 - 2 In stage 2 each consumer selects one of the pricing schemes or does not buy.
- Let (q_i, T_i) be the pricing scheme selected in equilibrium by a type i consumer, i = 1, 2
- The firm needs only offer two pricing schemes (one of them could be (q, T) = (0, 0) if it is optimal not to sell to one of the consumer types).

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- As a benchmark, consider the first best case where the firm knows the realization θ_i
- Then it maximizes its expected profit $T_i q_i c$ subject to the participation constraint that the consumer is willing to "buy", $q_i\theta_i T_i \ge 0$
- It can be seen graphically that the solution is $(q_i, T_i) = (1, \theta_i)$ if $\theta_i \ge c$ and $(q_i, T_i) = (0, 0)$ otherwise.
- This is the perfect discrimination solution.
- Interesting case is when $\theta_2 > \theta_1 > c$ (so both types are served in the first best).

• If the firm does not know θ_i , it maximizes expected profit

$$\lambda (T_1 - q_1 c) + (1 - \lambda) (T_2 - q_2 c)$$
 (3)

subject to two participation constraints,

$$q_1\theta_1-T_1\geq 0 \tag{4}$$

$$q_2\theta_2-T_2\geq 0 \tag{5}$$

and two incentive compatibility constraints,

$$q_1\theta_1-T_1\geq q_2\theta_1-T_2\tag{6}$$

$$q_2\theta_2 - T_2 \ge q_1\theta_2 - T_1 \tag{7}$$

- since $\theta_2 > \theta_1$, (5) is implied by (4) and (7): so (5) is not binding.
- Then IC constraint (7) must bind: else T₂ could be increased without violating (4)
- Now let us look at the solution to the problem while ignoring IC constraint (6)
- Then PC constraint (4) must bind (the low type has no rent): else, T₁ could be increased without violating the IC constraint (7)

 Substituting binding constraints (4) and (7) into the expected profit, the firm selects q₁ and q₂ so as to maximize

$$\lambda (\theta_1 - c) q_1 + (1 - \lambda) ((\theta_2 - c) q_2 - (\theta_2 - \theta_1) q_1)$$

• Then the solution is $q_2 = 1$ and $q_1 = 1$ iff

$$\theta_1 - (1 - \lambda)\theta_2 \ge \lambda c$$

• Corresponding transfers are $T_1 = T_2 = \theta_1$ if $q_1 = 1$ and $T_1 = 0$ and $T_2 = \theta_2$ if $q_1 = 0$

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- This is the optimal solution under uniform pricing.
- Note that this is incentive compatible for type θ_1 so (6) is satisfied and we have characterized the optimal solution.
- Hence, price posting is the optimal solution when selling one product with unit demand.
- Three ways around this:
 - assuming demand is price sensitive.
 - assuming different product varieties (qualities).
 - Assuming some capacity constraint and the possibility to auction off the product.

Price discrimination with heterogeneous qualities

ullet Assume now that the utility of consume ℓ is

$$U_{\ell} = \theta_{\ell} q - p + y_{\ell}$$

if she purchases the product at price p and $u_{\ell} = y_{\ell}$ if she does not purchase.

- θ_ℓ are l.i.d random variables with a support in $[0,+\infty)$ and q>0 is the product's quality, where the marg. cost of producing a product of quality q is c(q), where c is strictly increasing, strictly convex and twice continuously differentiable.
- The realization of θ_{ℓ} is unknown to the firm.

- First we consider the case where θ_{ℓ} is either θ_{1} or θ_{2} $\theta_{2} > \theta_{1} > 0$ and $\Pr \{\theta_{\ell} = \theta_{1}\} = \lambda$
- The firm now offers a menu of qualities sold at different prices.
- The price quality pair selected by type θ_i is denoted (q_i, T_i)

- Before deriving the profit maximizing solution let us consider the case where the firm is perfectly informed about each consumer's type and may perfectly discriminate
- The firm would then charge $T_i = \theta_i q_i$ to type θ_i and select $q_i = q_i^*$ to maximize $\theta_i q_i c(q_i)$
- It is not incentive compatible because type θ_2 would pick (q_1^*, t_i^*)
- For further reference, this (first best) quality if it is > 0 solves the FOC, $\theta_i = c'\left(q_i^*\right)$

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• Firm chooses (q_i^s, T_i^s) , i = 1, 2 to solve

$$\max_{(q_i,T_i)_{i=1}^2} \lambda \left(T_1 - c(q_1) \right) + (1 - \lambda) \left(T_2 - c(q_2) \right)$$

s.t. participation constraints

$$q_1\theta_1-T_1\geq 0$$
$$q_2\theta_2-T_2\geq 0$$

and two incentive compatibility constraints,

$$q_1\theta_1-T_1\geq q_2\theta_1-T_2$$

$$q_2\theta_2-T_2\geq q_1\theta_2-T_1$$

- As before (5) is irrelevant and we first solve the problem ignoring IC (6)
- Substituting the 2 binding constraints (4) and (7) in expected profit, the optimal qualities q₁^s and q₂^s must solve

$$\max_{(q_1,q_2)} \lambda \left(\theta_1 q_1 - c\left(q_1\right)\right) + (1-\lambda) \left(\theta_2 q_2 - c\left(q_2\right)\right) - (1-\lambda) \left(\theta_2 - \theta_1\right) q_1$$

- The firm maximizes the expected total surplus minus the informational rent (which is the last term).
- If both types are served, quantities should be > 0 so that FOCs are

$$\theta_1 = c'(q_1^s) + \frac{1-\lambda}{\lambda}(\theta_2 - \theta_1) \tag{8}$$

$$\theta_2 = c'(q_2^s) \tag{9}$$

- From (9) the quality for the high valuation consumer is first best while from (8) the quality for the low valuation consumer is distorted downwards from the first-best (because c' is increasing by convexity of c).
- Intuition: the informational rent is the only source of discrepancy between expected profit and expected social surplus. since it is unaffected by q_2 and increasing in q_1 only the latter should be distorted from its socially optimal level and it should go down to reduce the informational rent.

Corresponding transfers are

$$T_1^s = \theta_1 q_1^s \ T_2^s = \theta_2 q_2^s + (\theta_2 - \theta_1) q_1^s$$

- To check that IC (6) is not violated first note that $q_2^s = q_2^* > q_1^* > q_1^s$
- We can rewrite (6) as $(\theta_2 \theta_1) (q_2^s q_1^s) \ge 0$ which is clearly the case since $\theta_2 > \theta_1$ and $q_2^s > q_1^s$

Takeaway

- High valuation consumers earn an informational rent and consume a first best quality.
- Low valuation consumers have no rent and consume a quality that is distorted downward from the first-best.

Communication

- The above pricing scheme requires no communication between the firm and consumers.
- It implements the same allocation as an optimal direct mechanism where consumers would be asked to announce their type.
- From the revelation principle for Bayesian implementation, a more general communication procedure (non direct mechanism) could not implement anything better.

Continuous type distribution

- Now θ can take on any value in [<u>θ</u>, <u>θ</u>], <u>θ</u> > 0 with c.d.f F and density f
- Firm selects a pricing scheme (q, t):
 - (q,t) is a two dimensional function with domain $[\underline{\theta}, \overline{\theta}]$
 - $(q(\theta), t(\theta))$ is the quality price pair selected by type θ in equilibrium.
- infinitely many IC constraints:

$$\theta q(\theta) - t(\theta) \ge \theta q(\hat{\theta}) - t(\hat{\theta})$$
 (10)

for all $\theta, \hat{\theta}$ in $[\underline{\theta}, \bar{\theta}]$, so type θ does not want to deviate and mimic type $\hat{\theta}$

Lemma

Pricing scheme (q, t) satisfies all incentive compatibility constraints (10) if and only if q is increasing and

$$U(\theta) = \underline{U} + \int_{\underline{\theta}}^{\theta} q(s)ds$$
 (11)

where $U(\theta) \equiv \theta q(\theta) - t(\theta)$ is the equilibrium utility of type θ , and $\underline{U} = U(\underline{\theta})$

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Proof.

Necessary condition 1st, taking $\theta_2 > \theta_1$ the IC constraints between these two types imply that $q(\theta_2) > q(\theta_1)$. Hence q must be increasing. Then q is differentiable almost everywhere.

Proof.

Necessary condition ctd Furthermore, form IC constraint (10), t is differentiable whenever q is. Indeed we have

$$(\theta+h)\frac{q(\theta+h)-q(\theta)}{h}\geq \frac{t(\theta+h)-t(\theta)}{h}\geq \theta\frac{q(\theta+h)-q(\theta)}{h}$$

for h > 0, and for h < 0 we have the reverse inequalities. Then $t'(\theta)$ is the limit of the middle term when h tends to zero which exists whenever $q'(\theta)$ exists (sandwich theorem). And we have

$$\theta q'(\theta) = t'(\theta) \tag{12}$$

(Note: this is also the necessary FOC for IC, which requires that announcing $\hat{\theta} = \theta$ maximizes $\theta q(\hat{\theta}) - t(\hat{\theta})$, the surplus obtained by pretending she has type $\hat{\theta}$.)

Proof.

Necessary condition ctd 2nd, Integrating (12) between $\underline{\theta}$ and θ yields

$$\int_{\underline{ heta}}^{ heta} s q'(s) extit{d} s = t(heta) - t(\underline{ heta})$$

Integrating by parts:

$$[sq(s)]^{ heta}_{\underline{ heta}} - \int_{ heta}^{ heta} q(s) ds = t(heta) - t(\underline{ heta})$$

or

$$\theta q(\theta) - t(\theta) = \underline{\theta}q(\underline{\theta}) - t(\underline{\theta}) + \int_{\theta}^{\theta} q(s)ds$$

which is the desired condition (11).

Proof.

Sufficient conditions Now assume $q(\theta)$ is increasing and (11) holds. We need to show (10) which can be rewritten as

$$U(\theta) \ge \theta q(\hat{\theta}) - t(\hat{\theta}) = U(\hat{\theta}) + (\theta - \hat{\theta})q(\hat{\theta})$$

Using (11) this simplifies to

$$\int_{\hat{ heta}}^{ heta} q(s) - q(\hat{ heta}) ds \geq 0$$

which holds for *q* increasing.



• Using $t(\theta) = \theta q(\theta) - U(\theta)$ and the lemma, the firm's problem can be written as

$$\max_{q,U} \int_{\underline{\theta}}^{\overline{\theta}} \left(\theta q(\theta) - c(q(\theta)) - \underline{U} - \int_{\underline{\theta}}^{\theta} q(s) ds \right) f(\theta) d\theta$$

subject to q increasing and $\underline{U} \ge 0$

• Note that because of (11) the participation constraint is relevant only for $\underline{\theta}$ and it should clearly be binding.

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Using integration by parts we have

$$\begin{split} &\int_{\underline{\theta}}^{\bar{\theta}} \left(\int_{\underline{\theta}}^{\theta} q(s) ds \right) f(\theta) d\theta \\ &= \left[\left(\int_{\underline{\theta}}^{\theta} q(s) ds \right) F(\theta) \right]_{\underline{\theta}}^{\bar{\theta}} - \int_{\underline{\theta}}^{\bar{\theta}} q(\theta) F(\theta) d\theta \\ &= \int_{\theta}^{\bar{\theta}} [1 - F(\theta)] q(\theta) d\theta \end{split}$$

The firm then solves

$$\max_{q} \int_{\underline{\theta}}^{\overline{\theta}} \left(\left(\theta - \frac{1}{h(\theta)} \right) q(\theta) - c(q(\theta)) \right) f(\theta) d\theta \tag{13}$$

• The integral in (13) can be maximized point-wise and the FOC for $q(\theta)$ is

$$\theta - \frac{1}{h(\theta)} = c'(q(\theta))$$

- since c' increasing, a sufficient condition for q to be increasing is that hazard rate h is increasing.
- LHS is type θ 's virtual valuation for increasing the product's quality.