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- MODULE ceph
```

This is a specification of the paxos algorithm implemented in Ceph. The specification is based on the following source file: $\frac{1}{2} \frac{1}{100} \frac$

For a more detailed overview of the specification: https://github.com/afonsonf/ceph-consensus-spec

EXTENDS Integers, FiniteSets, Sequences, TLC

Utils

```
\begin{array}{l} \textit{Max} \text{ element from a set.} \\ \texttt{@type: } \textit{Set}(\textit{Int}) \Rightarrow \textit{Int}; \\ \textit{Max}(S) \stackrel{\triangle}{=} \text{ Choose } x \in S : \forall \, y \in S : x \geq y \\ \\ \textit{Min} \text{ element from a set.} \\ \texttt{@type: } \textit{Set}(\textit{Int}) \Rightarrow \textit{Int}; \\ \textit{Min}(S) \stackrel{\triangle}{=} \text{ Choose } x \in S : \forall \, y \in S : x \leq y \\ \\ \text{Set of monitors to a sequence.} \\ \text{RECURSIVE } \textit{SetToSeq}(\_) \\ \texttt{@type: } \textit{Set}(\textit{MONITOR}) \Rightarrow \textit{Seq}(\textit{MONITOR}); \\ \textit{SetToSeq}(S) \stackrel{\triangle}{=} \\ \text{IF } S = \{\} \text{ THEN } \langle \rangle \\ \text{ELSE LET } x \stackrel{\triangle}{=} \text{ Choose } x \in S : \text{TRUE} \\ \text{IN } \langle x \rangle \circ \textit{SetToSeq}(S \setminus \{x\}) \\ \end{array}
```

Constants

Predicate used in the cfg file to define the symmetry set.

Workaround for typechecker.

 $@typeAlias{:}\ MONITOR = T;\\$

@typeAlias: VALUE = T;

 $SYMM \triangleq Permutations(Monitors) \cup Permutations(Value_set)$

Reserved value.

CONSTANTS @type: VALUE; Nil

Paxos states.

CONSTANTS @type: STATE_NAME; STATE_RECOVERING, @type: STATE_NAME; STATE_ACTIVE,

©type: STATE_NAME; STATE_WRITING, ©type: STATE_NAME; STATE_WRITING_PREVIOU

Paxos auxiliary phase states.

They are used to force some sequence of steps.

CONSTANTS @type: PHASE_NAME; PHASE_ELECTION,

@type: PHASE_NAME; PHASE_SEND_COLLECT, @type: PHASE_NAME; PHASE_COLLECT,

@type: PHASE_NAME; PHASE_BEGIN, @type: PHASE_NAME; PHASE_COMMIT

Paxos message types.

CONSTANTS @type: MESSAGE_OP; OP_COLLECT, @type: MESSAGE_OP; OP_LAST,

@type: MESSAGE_OP; OP_BEGIN, @type: MESSAGE_OP; OP_ACCEPT,

@type: MESSAGE_OP; OP_COMMIT,

@type: MESSAGE_OP; OP_LEASE, @type: MESSAGE_OP; OP_LEASE_ACK

Global variables

Integer representing the current epoch. If is odd trigger an election.

VARIABLE @type: Int; epoch

Store messages waiting to be handled.

VARIABLE @type: $MONITOR \rightarrow (MONITOR \rightarrow Seg(MESSAGE)); messages$

Stores history of messages. Can be useful to find specific states.

VARIABLE @type: $Set(MESSAGE); message_history$

Stores if a monitor is up or down. All available monitors, in a given epoch, are part of the quorum.

VARIABLE @type: $MONITOR \rightarrow Bool; quorum$

Size of the current quorum.

VARIABLE @type: Int; quorum_sz

State variables

A function that stores the current leader. isLeader[mon] is True iff mon is a leader, else False.

VARIABLE @type: $MONITOR \rightarrow Bool; isLeader$

A function that stores the state of each monitor.

VARIABLE @type: $MONITOR \rightarrow STATE_NAME; state$

A function that stores the phase of each monitor.

VARIABLE @type: $MONITOR \rightarrow PHASE_NAME; phase$

Restart variables

A function that stores, for each monitor, a proposal number when the commit phase starts.

This proposal number can be retrieved after a monitor crashes and restarts.

VARIABLE @type: $MONITOR \rightarrow PN; pending_pn$

A function that stores, for each monitor, a value version when the commit phase starts.

This value version can be retrieved after a monitor crashes and restarts.

VARIABLE @type: $MONITOR \rightarrow VALUE_VERSION; pending_v$

A function that stores, for each monitor, the best uncommitted pn received in the collect phase.

VARIABLE @type: $MONITOR \rightarrow PN; uncommitted_pn$

A function that stores, for each monitor, the best uncommitted value version received in the collect phase.

VARIABLE @type: $MONITOR \rightarrow VALUE_VERSION$; $uncommitted_v$

A function that stores, for each monitor, the best uncommitted value received in the collect phase.

VARIABLE @type: $MONITOR \rightarrow VALUE; uncommitted_value$

Data variables

A function that stores, for each monitor, the store where the transactions are applied.

In this model, a transaction represents changing the value in the store.

VARIABLE @type: $MONITOR \rightarrow VALUE; monitor_store$

A function that stores the transaction log of each monitor.

VARIABLE @type: $MONITOR \rightarrow (VALUE_VERSION \rightarrow VALUE); values$

A function that stores the last proposal number accepted by each monitor.

VARIABLE @type: $MONITOR \rightarrow PN; accepted_pn$

A function that stores the first value version committed by each monitor.

VARIABLE @type: $MONITOR \rightarrow VALUE_VERSION$; $first_committed$

A function that stores the last value version committed by each monitor.

VARIABLE @type: $MONITOR \rightarrow VALUE_VERSION; last_committed$

Collect phase variables

A function that stores the number of peers that accepted a collect request.

VARIABLE @type: $MONITOR \rightarrow Int; num_last$

Used by leader when receiving responses in collect phase.

VARIABLE @type: $MONITOR \rightarrow (MONITOR \rightarrow VALUE_VERSION); peer_first_committed$

Used by leader when receiving responses in collect phase.

VARIABLE @type: $MONITOR \rightarrow (MONITOR \rightarrow VALUE_VERSION); peer_last_committed$

Lease phase variables

A function that stores, for each monitor, which of the peers have acked the lease request. VARIABLE @type: $MONITOR \rightarrow (MONITOR \rightarrow Bool)$; $acked_lease$

Commit phase variables

A function that stores, for each monitor, the value proposed by a client.

VARIABLE @type: $MONITOR \rightarrow VALUE; pending_proposal$

A function that stores, for each monitor, the value to be committed in the begin phase.

VARIABLE @type: $MONITOR \rightarrow VALUE; new_value$

A function that stores, for each monitor, which of the peers have acked the begin request.

VARIABLE @type: $MONITOR \rightarrow (MONITOR \rightarrow Bool); accepted$

Debug variables

Variables to help debug a behavior.

step is the diameter of a behavior/path.

 $step_name$ the current predicate being called.

VARIABLE @type: Str; step_name

Variables to limit the number of monitors crashes that can occur over a behavior.

This variable is used to limit the search space.

VARIABLE @type: Int; number_crashes

Variables initialization

```
@typeAlias:\ VALUE\_VERSION = Int;
```

@typeAlias: PN = Int;

 $global_vars \stackrel{\triangle}{=} \langle epoch, messages, message_history, quorum, quorum_sz \rangle$

 $state_vars \stackrel{\triangle}{=} \langle isLeader, state, phase \rangle$

 $restart_vars \triangleq \langle pending_pn, pending_v, uncommitted_pn, uncommitted_v, uncommitted_value \rangle$

 $data_vars \stackrel{\triangle}{=} \langle monitor_store, values, accepted_pn, first_committed, last_committed \rangle$

 $collect_vars \triangleq \langle num_last, peer_first_committed, peer_last_committed \rangle$

 $lease_vars$ $\stackrel{\triangle}{=}$ $acked_lease$

 $commit_vars \stackrel{\triangle}{=} \langle pending_proposal, new_value, accepted \rangle$

 $vars \triangleq \langle global_vars, state_vars, restart_vars, data_vars, collect_vars, lease_vars, commit_vars \rangle$

 $Init_global_vars \triangleq$

```
\wedge epoch = 1
     \land messages = [mon1 \in Monitors \mapsto [mon2 \in Monitors \mapsto \langle \rangle]]
     \land message\_history = \{\}
     \land quorum = [mon \in Monitors \mapsto TRUE]
     \land quorum\_sz = MonitorsLen
Init\_state\_vars \triangleq
     \land isLeader = [mon \in Monitors \mapsto FALSE]
     \land state = [mon \in Monitors \mapsto STATE\_RECOVERING]
     \land phase = [mon \in Monitors \mapsto PHASE\_ELECTION]
Init\_restart\_vars \triangleq
     \land pending\_pn = [mon \in Monitors \mapsto 0]
     \land pending\_v = [mon \in Monitors \mapsto 0]
     \land uncommitted\_pn = [mon \in Monitors \mapsto 0]
     \land uncommitted\_v = [mon \in Monitors \mapsto 0]
     \land uncommitted\_value = [mon \in Monitors \mapsto Nil]
Init\_data\_vars \triangleq
     \land monitor\_store = [mon \in Monitors \mapsto Nil]
     \land values = [mon \in Monitors \mapsto [version \in \{\} \mapsto Nil]]
     \land accepted\_pn = [mon \in Monitors \mapsto 0]
     \land first\_committed = [mon \in Monitors \mapsto 0]
     \land last\_committed = [mon \in Monitors \mapsto 0]
Init\_collect\_vars \triangleq
     \land num\_last = [mon \in Monitors \mapsto 0]
     \land peer\_first\_committed = [mon1 \in Monitors \mapsto [mon2 \in Monitors \mapsto -1]]
     \land peer\_last\_committed = [mon1 \in Monitors \mapsto [mon2 \in Monitors \mapsto -1]]
Init\_lease\_vars \triangleq
     \land acked\_lease = [mon1 \in Monitors \mapsto [mon2 \in Monitors \mapsto FALSE]]
Init\_commit\_vars \triangleq
     \land pending\_proposal = [mon \in Monitors \mapsto Nil]
     \land new\_value = [mon \in Monitors \mapsto Nil]
     \land accepted = [mon1 \in Monitors \mapsto [mon2 \in Monitors \mapsto FALSE]]
Init \triangleq
     \land Init\_global\_vars
     \land Init\_state\_vars
     \land Init_restart_vars
     \land Init\_data\_vars
     \land Init\_collect\_vars
     \land Init_lease_vars
     \land Init\_commit\_vars
     \land step\_name = "init" \land number\_crashes = 0
```

Message manipulation

```
@typeAlias: MESSAGE = [type: MESSAGE\_OP, from: MONITOR, dest: MO
                                                         first\_committed:
                                                                                                             VALUE\_VERSION,
                                                                                                                                                                  last\_committed:
                                                          VALUE\_VERSION, values: (VALUE\_VERSION \rightarrow VALUE),
                                                         uncommitted\_pn: PN, pn: PN;
@typeAlias: MESSAGE\_QUEUE = MONITOR \rightarrow (MONITOR \rightarrow Seq(MESSAGE));
  Note: Variable message_history has impact in performace, update only when debugging.
  Converts a set with at most one element to a sequence.
  SingleMessageSetToSeq(S) \triangleq
        If \exists \ elem \in S : \text{true then let} \ \ elem \ \stackrel{\triangle}{=} \ \ \text{choose} \ \ x \in S : \text{true}
                                                                          IN
                                                                                  \langle elem \rangle
                                                            ELSE \langle \rangle
  Add message m to the network msqs.
  Qtype: (MESSAGE, MESSAGE\_QUEUE) \Rightarrow MESSAGE\_QUEUE;
WithMessage(m, msgs) \stackrel{\Delta}{=}
        [msgs \ EXCEPT \ ![m.from] =
                [msgs[m.from] \ EXCEPT \ ![m.dest] = Append(msgs[m.from][m.dest], m)]]
  Remove message m from the network msqs.
  ©type: (MESSAGE, MESSAGE\_QUEUE) \Rightarrow MESSAGE\_QUEUE;
WithoutMessage(m, msgs) \stackrel{\Delta}{=}
        [msgs \ EXCEPT \ ![m.from] =
                 [msqs[m.from] \ EXCEPT \ ![m.dest] = Tail(msqs[m.from][m.dest])]]
  Adds the message m to the network.
  Variables changed: messages, message_history.
  @type: MESSAGE \Rightarrow Bool;
Send(m) \triangleq
            \land messages' = WithMessage(m, messages)
              \land message\_history' = message\_history \cup \{m\}
             ∧ UNCHANGED message_history
  Adds a set of messages to the network.
  Variables changed: messages, message_history.
  @type: (MONITOR, Set(MESSAGE)) \Rightarrow Bool;
Send\_set(from, m\_set) \triangleq
         \land messages' = [messages \ EXCEPT \ ![from] =
                 [mon \in Monitors \mapsto
                        messages[from][mon] \circ SingleMessageSetToSeq(\{m \in m\_set : m.dest = mon\})]]
           \land message\_history' = message\_history \cup m\_set
          ∧ UNCHANGED message_history
```

```
Removes the request from network and adds the response.
 Variables changed: messages, message\_history.
 @type: (MESSAGE, MESSAGE) \Rightarrow Bool;
Reply(response, request) \stackrel{\Delta}{=}
    \land messages' = WithoutMessage(request, WithMessage(response, messages))
     \land \mathit{message\_history'} = \mathit{message\_history} \cup \{\mathit{response}\}
    ∧ UNCHANGED message_history
 Removes the request from network and adds a set of messages.
 Variables changed: messages, message_history.
 @type: (MONITOR, Set(MESSAGE), MESSAGE) \Rightarrow Bool;
Reply\_set(from, response\_set, request) \triangleq
    \land LET msgs \stackrel{\triangle}{=} WithoutMessage(request, messages)
      IN messages' = [msgs \ EXCEPT \ ![from] =
             [mon \in Monitors \mapsto
                 msgs[from][mon] \circ SingleMessageSetToSeq(\{m \in response\_set : m.dest = mon\})]]
     \land message\_history' = message\_history \cup response\_set
    ∧ UNCHANGED message_history
 Removes message m from the network.
 Variables changed: messages, message_history.
 @type: MESSAGE \Rightarrow Bool;
Discard(m) \triangleq
    \land messages' = WithoutMessage(m, messages)
    ∧ UNCHANGED message_history
                                      Helper predicates
 Computes a new unique proposal number for a given monitor.
```

```
Version A - Equal to the one in the source.
 This version breaks the symmetry of the monitor set.
 Example: oldpn = 305, rank(mon) = 5, newpn = 405.
 @type: (MONITOR, Int) \Rightarrow Int;
 qet\_new\_proposal\_number(mon, oldpn) \stackrel{\Delta}{=} ((oldpn \div 100) + 1) * 100 + rank(mon)
 Version B — Adapted to not break symmetry.
 Example: oldpn = 300, rank(mon) = 5, newpn = 400.
 @type: (MONITOR, Int) \Rightarrow Int;
get\_new\_proposal\_number(mon, oldpn) \stackrel{\triangle}{=} ((oldpn \div 100) + 1) * 100 + epoch
 Clear the variable peer_first_committed.
 Variables changed: peer\_first\_committed.
 @type: MONITOR \Rightarrow Bool;
clear\_peer\_first\_committed(mon) \triangleq
    peer\_first\_committed' = [peer\_first\_committed \ EXCEPT \ ![mon] = ]
```

```
[m \in Monitors \mapsto -1]]
 Clear the variable peer\_last\_committed.
 Variables changed: peer_last_committed.
 @type: MONITOR \Rightarrow Bool;
clear\_peer\_last\_committed(mon) \triangleq
   peer\_last\_committed' = [peer\_last\_committed \ EXCEPT \ ! [mon] =
                                    [m \in Monitors \mapsto -1]]
 Store peer values and update first_committed, last_committed and monitor_store accordingly.
 Variables changed: values, first_committed, last_committed, monitor_store.
 @type: (MONITOR, MESSAGE) \Rightarrow Bool;
store\_state(mon, msg) \triangleq
     Choose peer values from mon last committed +1 to peer last committed.
    \land LET logs \stackrel{\triangle}{=} (DOMAIN \ msg.values) \cap (last\_committed[mon] + 1 \dots msg.last\_committed)
           \land values' = [values \ EXCEPT \ ![mon] =
                [i \in \text{DOMAIN } values[mon] \cup logs \mapsto
                   If i \in logs
                    THEN msg.values[i]
                    ELSE values[mon][i]]
             Update last committed and first committed.
            \land last\_committed' = [last\_committed \ EXCEPT \ ![mon] = Max(logs \cup \{last\_committed[mon]\})]
            \land IF logs \neq \{\} \land first\_committed[mon] = 0
                THEN first\_committed' =
                             [first\_committed \ EXCEPT \ ![mon] = Min(logs)]
                ELSE first\_committed' =
                             [first\_committed \ EXCEPT \ ![mon] = Min(logs \cup \{first\_committed[mon]\})]
     Update monitor store.
    \wedge IF last\_committed'[mon] = 0
       THEN UNCHANGED monitor_store
       ELSE monitor\_store' = [monitor\_store \ EXCEPT \ ![mon] = values'[mon][last\_committed'[mon]]]
 Check if uncommitted value version is still valid, else reset it.
 Variables changed: uncommitted_pn, uncommitted_v, uncommitted_value.
 @type: MONITOR \Rightarrow Bool;
check\_and\_correct\_uncommitted(mon) \triangleq
   IF uncommitted\_v[mon] \leq last\_committed'[mon]
    THEN \land uncommitted\_v' = [uncommitted\_v \text{ EXCEPT } ![mon] = 0]
            \land uncommitted\_pn' = [uncommitted\_pn \ EXCEPT \ ![mon] = 0]
            \land uncommitted\_value' = [uncommitted\_value \ EXCEPT \ ![mon] = Nil]
    ELSE UNCHANGED (uncommitted_pn, uncommitted_v, uncommitted_value)
 Trigger new election by incrementing epoch.
 Variables changed: epoch.
 @type: Bool;
bootstrap \triangleq
```

```
\land \; epoch' = epoch + 1
```

Lease phase predicates

```
Changes mon state to STATE_ACTIVE.
 Variables changed: state.
 @type: MONITOR \Rightarrow Bool;
finish\_round(mon) \triangleq
    \wedge isLeader[mon] = TRUE
    \land state' = [state \ EXCEPT \ ![mon] = STATE\_ACTIVE]
 Resets the variable acked lease and send lease messages to peers.
 Variables changed: acked_lease, messages, message_history, phase.
 @type: MONITOR \Rightarrow Bool;
extend\_lease(mon) \triangleq
    \wedge isLeader[mon] = TRUE
    \land acked\_lease' = [acked\_lease \ EXCEPT \ ![mon] =
        [m \in Monitors \mapsto \text{if } m = mon \text{ then true else false}]
    \land Send\_set(mon,
        \{[type]
                             \mapsto OP\_LEASE,
          from
                             \mapsto mon,
                             \mapsto dest.
          dest
          last\_committed \mapsto last\_committed[mon]] : dest \in \{m \in Monitors \setminus \{mon\} : quorum[m]\}
         })
    \land phase' = [phase \ EXCEPT \ ![mon] = PHASE\_LEASE]
 Handle a lease message. The peon changes his state and replies with a lease ack message.
 The reply is commented because the lease ack is only used to check if all peers are up.
 In the model this is done by "randomly" triggering the predicate Timeout. In this way, the search space is reduced.
 Variables changed: messages, message_history, state.
 @type: (MONITOR, MESSAGE) \Rightarrow Bool;
handle\_lease(mon, msg) \triangleq
    \wedge discard if not peon or peon is behind
       IF \lor isLeader[mon] = TRUE
           \lor last\_committed[mon] \neq msg.last\_committed
        THEN \wedge Discard(msq)
                \land UNCHANGED state
        ELSE \land state' = [state \ EXCEPT \ ![mon] = STATE\_ACTIVE]
         \land Reply([type]
                              \mapsto OP\_LEASE\_ACK,
              from
                            \mapsto mon,
                           \mapsto \mathit{msg.from},
              dest
               first\_committed \mapsto first\_committed[mon],
              last\_committed \mapsto last\_committed[mon]], \ msg)
             \wedge Discard(msq)
    \land UNCHANGED \langle epoch, quorum, quorum\_sz, isLeader, phase <math>\rangle
```

```
\(\text{\text{UNCHANGED}}\)\(\text{restart_vars, data_vars, collect_vars, lease_vars, commit_vars}\)\)
 Handle a lease ack message. The leader updates the acked_lease variable.
 Because the lease_ack messages are not sent, this predicate is never called.
 The reasoning for this is given in handle_lease comment.
 Variables changed: acked_lease, messages, message_history.
 @type: (MONITOR, MESSAGE) \Rightarrow Bool;
handle\_lease\_ack(mon, msq) \triangleq
    \land phase[mon] = PHASE\_LEASE
    \land acked\_lease' = [acked\_lease \ EXCEPT \ ![mon] =
        [acked\_lease[mon] \ EXCEPT \ ![msg.from] = TRUE]]
    \wedge Discard(msg)
    \land UNCHANGED \langle epoch, quorum, quorum\_sz \rangle
    \(\triangle \) UNCHANGED \(\state_vars, restart_vars, data_vars, collect_vars, commit_vars\)
 Predicate that is called when all peers ack the lease. The phase is changed to prevent loops.
 Because the lease_ack messages are not sent, this predicate is never called.
 The reasoning for this is given in handle_lease comment.
 Variables changed: phase.
 @type: MONITOR \Rightarrow Bool;
post\_lease\_ack(mon) \stackrel{\Delta}{=}
    \land phase[mon] = PHASE\_LEASE
    \land phase' = [phase \ EXCEPT \ ![mon] = PHASE\_LEASE\_DONE]
    \land \forall m \in Monitors : quorum[m] \Rightarrow acked\_lease[mon][m] = TRUE
    \land UNCHANGED \langle isLeader, state \rangle
    \land UNCHANGED \langle global\_vars, restart\_vars, data\_vars, collect\_vars,
                        lease\_vars, commit\_vars \rangle
```

Commit phase predicates

```
\land values' = [values \ EXCEPT \ ![mon] =
       ((last\_committed[mon] + 1) :> new\_value'[mon]) @@ values[mon]]
    \land Send\_set(mon,
                           \mapsto OP\_BEGIN,
       \{[type]
         from
                          \mapsto mon,
          dest
                          \mapsto dest,
          last\_committed \mapsto last\_committed[mon],
                           \mapsto values'[mon],
         values
                           \mapsto accepted\_pn[mon]]: dest \in \{m \in Monitors \setminus \{mon\}: quorum[m]\}
         pn
         })
    \land pending\_pn' = [pending\_pn \ EXCEPT \ ![mon] = accepted\_pn[mon]]
    \land pending\_v' = [pending\_v \ EXCEPT \ ![mon] = last\_committed[mon] + 1]
 Handle a begin message. The monitor will accept if the proposal number in the message is greater
 or equal than the one he accepted.
 Similar to what happens in begin, values and pending\_pn are assigned in order for
 the monitor to recover in case of a crash.
 Variables changed: messages, message_history, state, values, pending_pn, pending_v.
 @type: (MONITOR, MESSAGE) \Rightarrow Bool;
handle\_begin(mon, msg) \stackrel{\triangle}{=}
    \wedge isLeader[mon] = FALSE
    \land IF msg.pn < accepted\_pn[mon]
       THEN
        \land Discard(msq)
        \land UNCHANGED \langle state, values, pending_pn, pending_v \rangle
       ELSE
        \land msg.pn = accepted\_pn[mon]
        \land msg.last\_committed = last\_committed[mon]
         assign values[mon][last\_committed[mon] + 1]
        \land values' = [values \ EXCEPT \ ![mon] =
           ((last\_committed[mon] + 1) :> msg.values[last\_committed[mon] + 1]) @@ values[mon]]
        \land state' = [state \ EXCEPT \ ![mon] = STATE\_UPDATING]
        \land pending\_pn' = [pending\_pn \ EXCEPT \ ![mon] = accepted\_pn[mon]]
        \land pending\_v' = [pending\_v \ EXCEPT \ ![mon] = last\_committed[mon] + 1]
        \land Reply([type]
                                    \mapsto OP\_ACCEPT,
                  from
                                    \mapsto mon,
                                    \mapsto msg.from,
                  dest
                  last\_committed \mapsto last\_committed[mon],
                                    \mapsto accepted\_pn[mon]], msg)
    ∧ UNCHANGED ⟨epoch, quorum, quorum_sz, isLeader, phase, monitor_store,
                      accepted_pn, first_committed, last_committed, uncommitted_pn,
                      uncommitted\_v, uncommitted\_value \rangle
    ∧ UNCHANGED ⟨collect_vars, lease_vars, commit_vars⟩
```

```
Handle an accept message. If the leader receives a positive response from the peer, it will
 add it to the variable accepted.
 Variables changed: messages, message_history, accepted
 @type: (MONITOR, MESSAGE) \Rightarrow Bool;
handle\_accept(mon, msg) \triangleq
    \wedge isLeader[mon] = TRUE
    \land \lor state[mon] = STATE\_UPDATING\_PREVIOUS
       \lor state[mon] = STATE\_UPDATING
    \land phase[mon] = PHASE\_BEGIN
    \land new\_value[mon] \neq Nil
    \land IF \lor msg.pn \neq accepted\_pn[mon]
          \lor \land last\_committed[mon] > 0
             \land msg.last\_committed < last\_committed[mon] - 1
       THEN UNCHANGED accepted
       ELSE accepted' = [accepted \ EXCEPT \ ![mon] =
                   [accepted[mon] \text{ EXCEPT } ![msq.from] = \text{TRUE}]]
    \wedge Discard(msg)
    \(\triangle \) UNCHANGED \(\langle epoch, \, quorum, \, quorum_sz, \, pending_proposal, \, new_value \rangle \)
    ∧ UNCHANGED ⟨restart_vars, state_vars, data_vars, collect_vars, lease_vars⟩
 Predicate that is enabled and called when all peers in the quorum accept begin request from leader.
 The leader commits the transaction in new_value and sends commit messages to his peers.
 Variables changed: first_committed, last_committed, monitor_store, new_value, messages, message_history, state, phase
 @type: MONITOR \Rightarrow Bool;
post\_accept(mon) \triangleq
    \land phase[mon] = PHASE\_BEGIN
    \land \forall m \in Monitors : quorum[m] \Rightarrow accepted[mon][m] = TRUE
    \land new\_value[mon] \neq Nil
    \land \lor state[mon] = STATE\_UPDATING\_PREVIOUS
       \lor state[mon] = STATE\_UPDATING
    \land last\_committed' = [last\_committed \ EXCEPT \ ![mon] = last\_committed[mon] + 1]
    \wedge IF first\_committed[mon] = 0
       THEN first\_committed' = [first\_committed \ EXCEPT \ ! [mon] = first\_committed[mon] + 1]
       ELSE UNCHANGED first_committed
    \land monitor\_store' = [monitor\_store \ EXCEPT \ ![mon] = values[mon][last\_committed[mon] + 1]]
    \land new\_value' = [new\_value \ EXCEPT \ ![mon] = Nil]
    \land Send\_set(mon,
       \{[type]
                           \mapsto OP\_COMMIT.
         from
                          \mapsto mon,
                           \mapsto dest.
         last\_committed \mapsto last\_committed'[mon],
                           \mapsto accepted\_pn[mon],
         pn
                           \mapsto values[mon]]: dest \in \{m \in Monitors \setminus \{mon\} : quorum[m]\}\}
         values
         })
```

```
\land state' = [state \ EXCEPT \ ![mon] = STATE\_REFRESH]
    \land phase' = [phase \ EXCEPT \ ![mon] = PHASE\_COMMIT]
    \(\text{\text{UNCHANGED}}\) \(\langle is Leader, values, accepted_pn, pending_proposal, accepted \)\)
    \(\triangle \) UNCHANGED \(\langle epoch, quorum, quorum_sz, restart_vars, collect_vars, lease_vars\)
 Predicate that is called after post_accept. The leader finishes the commit phase by updating his state to
 STATE_ACTIVE and by extending the lease to his peers.
 Variables changed: state, phase, acked_lease, messages, message_history.
 @type: MONITOR \Rightarrow Bool;
finish\_commit(mon) \triangleq
    \land state[mon] = STATE\_REFRESH
    \land phase[mon] = PHASE\_COMMIT
    \land finish_round(mon)
    \land extend\_lease(mon)
    \land UNCHANGED \langle epoch, quorum, quorum\_sz, isLeader <math>\rangle
    ∧ UNCHANGED ⟨restart_vars, data_vars, collect_vars, commit_vars⟩
 Handle a commit message. The monitor stores the values sent by the leader commit message.
 Variables changed: messages, message_history, values, first_committed, last_committed, monitor_store, uncommitted_v,
 uncommitted\_pn, uncommitted\_value.
 @type: (MONITOR, MESSAGE) \Rightarrow Bool;
handle\_commit(mon, msq) \triangleq
    \wedge isLeader[mon] = FALSE
    \land store\_state(mon, msq)
    \land check\_and\_correct\_uncommitted(mon)
    \wedge Discard(msg)
    \land UNCHANGED \langle epoch, quorum, quorum\_sz, accepted\_pn, pending\_pn, pending\_v <math>\rangle
    ∧ UNCHANGED ⟨state_vars, collect_vars, lease_vars, commit_vars⟩
```

Client Request

```
Request a transaction v to the monitor. The transaction is saved on pending proposal to be committed in the next available commit phase.

Variables changed: pending\_proposal.

@type: (MONITOR, VALUE) \Rightarrow Bool;

client\_request(mon, v) \triangleq

\land isLeader[mon] = \text{TRUE}

\land state[mon] = STATE\_ACTIVE

\land pending\_proposal[mon] = Nil

\land pending\_proposal' = [pending\_proposal \text{ EXCEPT }![mon] = v]

\land \text{ UNCHANGED } \langle new\_value, accepted \rangle

\land \text{ UNCHANGED } \langle global\_vars, state\_vars, restart\_vars, data\_vars, collect\_vars, lease\_vars \rangle
```

Start a commit phase with the value on pending proposal.

Variables changed: state, pending_proposal, accepted, new_value, phase, messages, message_history, values,

```
pending_pn, pending_v.
 @type: MONITOR \Rightarrow Bool;
propose\_pending(mon) \stackrel{\triangle}{=}
    \land phase[mon] = PHASE\_LEASE \lor phase[mon] = PHASE\_ELECTION
    \land state[mon] = STATE\_ACTIVE
    \land pending\_proposal[mon] \neq Nil
    \land pending\_proposal' = [pending\_proposal \ EXCEPT \ ![mon] = Nil]
    \land state' = [state \ EXCEPT \ ![mon] = STATE\_UPDATING]
    \land begin(mon, pending\_proposal[mon])
    ∧ UNCHANGED ⟨isLeader, monitor_store, accepted_pn, first_committed, last_committed,
                      epoch, quorum, quorum_sz, uncommitted_v, uncommitted_pn, uncommitted_value
    \land UNCHANGED \langle collect\_vars, lease\_vars \rangle
```

Collect phase predicates

```
Start collect phase. This first part of the collect phase is divided in two parts (collect and send_collect)
  in order to simplify variable changes (when collect is triggered from handle_last).
  Variables changed: accepted_pn, phase.
  @type: (MONITOR, Int) \Rightarrow Bool;
collect(mon, oldpn) \triangleq
         \land state[mon] = STATE\_RECOVERING
         \wedge isLeader[mon] = TRUE
         \land LET new\_pn \triangleq get\_new\_proposal\_number(mon, Max({oldpn, accepted\_pn[mon]}))
                          \land accepted\_pn' = [accepted\_pn \ EXCEPT \ ![mon] = new\_pn]
         \land phase' = [phase \ EXCEPT \ ![mon] = PHASE\_SEND\_COLLECT]
  Continue the start of the collect phase. Initialize the number of peers that accepted the proposal (num_last) and
  the variables with peers version numbers. Check if there is an uncommitted value.
  Send collect messages to the peers.
  Variables changed: peer_first_committed, peer_last_committed, uncommitted_pn, uncommitted_v, uncommitted_value, num_last_committed_value, num_last_c
  messages, message_history, phase.
  @type: MONITOR \Rightarrow Bool;
send\_collect(mon) \triangleq
         \land state[mon] = STATE\_RECOVERING
         \land isLeader[mon] = TRUE
         \land phase[mon] = PHASE\_SEND\_COLLECT
         \land \ clear\_peer\_first\_committed(mon)
         \land clear\_peer\_last\_committed(mon)
         \land IF last\_committed[mon] + 1 \in DOMAIN values[mon]
                 THEN \wedge uncommitted_v' =
                                         [uncommitted\_v \ EXCEPT \ ![mon] = last\_committed[mon] + 1]
                                 \land uncommitted\_value' =
                                         [uncommitted\_value \ EXCEPT \ ![mon] = values[mon][last\_committed[mon] + 1]]
                                  \land uncommitted\_pn' = [uncommitted\_pn \ EXCEPT \ ![mon] = pending\_pn[mon]]
```

```
\land UNCHANGED \langle pending\_pn, pending\_v \rangle
        ELSE UNCHANGED (restart_vars)
    \land num\_last' = [num\_last \ EXCEPT \ ![mon] = 1]
    \land Send\_set(mon,
        \{[type]
                             \mapsto OP\_COLLECT,
                             \mapsto mon,
          from
          dest
                             \mapsto dest.
          first\_committed \mapsto first\_committed[mon],
          last\_committed \mapsto last\_committed[mon],
                             \mapsto accepted\_pn[mon]]: dest \in \{m \in Monitors \setminus \{mon\} : quorum[m]\}
         })
    \land phase' = [phase \ EXCEPT \ ! [mon] = PHASE\_COLLECT]
    \land UNCHANGED \langle isLeader, state \rangle
    \(\triangle \text{UNCHANGED \langle epoch, quorum, quorum_sz, data_vars, lease_vars, commit_vars\)}\)
 Handle a collect message. The peer will accept the proposal number from the leader if it is bigger than the last
 proposal number he accepted.
 Variables changed: messages, message_history, epoch, state, accepted_pn.
 @type: (MONITOR, MESSAGE) \Rightarrow Bool;
handle\_collect(mon, msg) \stackrel{\Delta}{=}
    \wedge isLeader[mon] = FALSE
    \land state' = [state \ EXCEPT \ ![mon] = STATE\_RECOVERING]
    \land \lor \land msg.first\_committed > last\_committed[mon] + 1
          \land bootstrap
          \land Discard(msg)
          \land UNCHANGED \langle accepted\_pn \rangle
       \lor \land msg.first\_committed \leq last\_committed[mon] + 1
          \land IF msg.pn > accepted\_pn[mon]
             THEN accepted\_pn' = [accepted\_pn \ EXCEPT \ ![mon] = msg.pn]
              ELSE UNCHANGED accepted_pn
          \land Reply([type]
                                         \mapsto OP\_LAST,
                     from
                                         \mapsto mon,
                     dest
                                         \mapsto msq.from,
                     first\_committed \mapsto first\_committed[mon],
                     last\_committed \mapsto last\_committed[mon],
                     values
                                          \mapsto values[mon],
                     uncommitted\_pn \mapsto pending\_pn[mon],
                                         \mapsto accepted\_pn'[mon], msg)
          \land UNCHANGED epoch
    ∧ UNCHANGED ⟨isLeader, phase, values, first_committed, last_committed, monitor_store⟩
    \(\triangle \text{UNCHANGED}\)\(\langle auorum, \, quorum_sz, \, restart_vars, \, collect_vars, \, lease_vars, \, commit_vars\)\(\)
```

Handle a last message (response from a peer to the leader collect message).

The peers first and last committed version are stored. If the leader is behind, bootstraps. Stores any value that the peer may have committed (*store_state*). If peer is behind send commit message with leader values.

```
If peer accepted proposal number increase num last, if he sent a bigger proposal number start a new collect phase.
 Variables changed: messages, message_history, epoch, phase, uncommitted_pn, uncommitted_v, uncommitted_value, monitor_s
 accepted\_pn, first\_committed, last\_committed, num\_last, peer\_first\_committed, peer\_last\_committed.
 @type: (MONITOR, MESSAGE) \Rightarrow Bool;
handle\_last(mon, msg) \triangleq
    \wedge isLeader[mon] = TRUE
    \land peer\_first\_committed' = [peer\_first\_committed \ EXCEPT \ ![mon] =
        [peer\_first\_committed[mon] \ EXCEPT \ ! [msg.from] = msg.first\_committed]]
    \land peer\_last\_committed' = [peer\_last\_committed \ EXCEPT \ ![mon] = ]
        [peer\_last\_committed[mon] \ EXCEPT \ ![msg.from] = msg.last\_committed]]
    \land IF msg.first\_committed > last\_committed[mon] + 1
        THEN
        \land bootstrap
        \wedge Discard(msg)
        \land UNCHANGED \langle num\_last, accepted\_pn, values, phase, monitor\_store <math>\rangle
        \land UNCHANGED \langle first\_committed, last\_committed, uncommitted\_pn, uncommitted\_v, uncommitted\_value.
        ELSE
        \land store\_state(mon, msq)
        \wedge IF \exists peer \in Monitors:
                 \land peer \neq mon
                 \land peer\_last\_committed'[mon][peer] \neq -1
                 \land peer\_last\_committed'[mon][peer] + 1 < first\_committed[mon]
                 \land first\_committed[mon] > 1
            THEN
            \land bootstrap
            \land check\_and\_correct\_uncommitted(mon)
            \wedge Discard(msg)
            \land UNCHANGED \langle phase, accepted\_pn, num\_last \rangle
            ELSE
            \land LET monitors_behind \stackrel{\triangle}{=} {peer \in Monitors :
                      \land peer \neq mon
                      \land peer\_last\_committed'[mon][peer] \neq -1
                      \land peer\_last\_committed'[mon][peer] < last\_committed[mon]
                      \land quorum[peer]
              IN Reply\_set(mon,
                      \{[type]
                                           \mapsto OP\_COMMIT,
                        from
                                          \mapsto mon,
                                           \mapsto dest,
                        last\_committed \mapsto last\_committed'[mon],
                                          \mapsto accepted\_pn[mon],
                        values
                                           \mapsto values[mon]]: dest \in monitors\_behind
                       \}, msg)
            \land \lor \land msg.pn > accepted\_pn[mon]
```

```
\land collect(mon, msq.pn)
                 \land check\_and\_correct\_uncommitted(mon)
                 ∧ UNCHANGED num_last
               \lor \land msg.pn = accepted\_pn[mon]
                  \land num\_last' = [num\_last \ EXCEPT \ ![mon] = num\_last[mon] + 1]
                  \land if \land msg.last_committed + 1 \in domain msg.values
                       \land msg.last\_committed \ge last\_committed'[mon]
                       \land msg.last\_committed + 1 \ge uncommitted\_v[mon]
                       \land msg.uncommitted\_pn \ge uncommitted\_pn[mon]
                     THEN \wedge uncommitted_v' =
                                  [uncommitted\_v \ EXCEPT \ ![mon] = msg.last\_committed + 1]
                            \land uncommitted\_pn' =
                                  [uncommitted\_pn \ EXCEPT \ ! [mon] = msg.uncommitted\_pn]
                            \land uncommitted\_value' =
                                  [uncommitted\_value \ EXCEPT \ ![mon] = msg.values[msg.last\_committed + 1]]
                     ELSE check\_and\_correct\_uncommitted(mon)
                 \land UNCHANGED \langle phase, accepted\_pn \rangle
               \lor \land msq.pn < accepted\_pn[mon]
                 \land check\_and\_correct\_uncommitted(mon)
                  \land UNCHANGED \langle phase, accepted\_pn, num\_last \rangle
            \land UNCHANGED epoch
       \land UNCHANGED epoch
    \land UNCHANGED \langle quorum, quorum\_sz, isLeader, state, pending\_pn, pending\_v <math>\rangle
    \land UNCHANGED \langle lease\_vars, commit\_vars \rangle
 Predicate that is enabled and called when all peers in quorum accept collect request from leader. If there is an
 uncommitted value, a commit phase is started with that value, else the leader changes to ACTIVE\_STATE and extends
 the lease to his peers.
 Variables changed: peer_first_committed, peer_last_committed, state, accepted, new_value, phase, messages,
 message_history, values, pending_pn, pending_v, acked_lease.
 @type: MONITOR \Rightarrow Bool;
post\_last(mon) \triangleq
    \land isLeader[mon] = TRUE
    \land num\_last[mon] = quorum\_sz
    \land phase[mon] = PHASE\_COLLECT
    \land clear\_peer\_first\_committed(mon)
    \land clear\_peer\_last\_committed(mon)
    \land IF \land uncommitted_v[mon] = last_committed[mon] + 1
          \land uncommitted\_value[mon] \neq Nil
       THEN \land state' = [state \ EXCEPT \ ![mon] = STATE\_UPDATING\_PREVIOUS]
               \land begin(mon, uncommitted\_value[mon])
               \land UNCHANGED \langle acked\_lease, uncommitted\_v, uncommitted\_pn, uncommitted\_value <math>\rangle
```

```
ELSE \land finish\_round(mon)
 \land extend\_lease(mon)
 \land UNCHANGED \ \langle accepted, new\_value, values, restart\_vars \rangle
```

 \land UNCHANGED $\langle isLeader, monitor_store, accepted_pn, first_committed, last_committed <math>\rangle$ \land UNCHANGED $\langle epoch, quorum, quorum_sz, num_last, pending_proposal <math>\rangle$

Leader election

```
Elect one monitor as a leader and initialize the remaining ones as peons.
 \label{lem:lem:value} \mbox{Variables changed: } is Leader, \mbox{ state, phase, } new\_value, \mbox{ } pending\_proposal, \mbox{ epoch.}
 @type: Bool;
leader\_election \triangleq
     \wedge \exists mon \in Monitors :
         \land quorum[mon]
         \land isLeader' = [m \in Monitors \mapsto if \ m = mon \ then \ true \ else \ false]
         \land state' = [m \in Monitors \mapsto
             IF quorum\_sz = 1 Then STATE\_ACTIVE else STATE\_RECOVERING
     \land phase' = [m \in Monitors \mapsto PHASE\_ELECTION]
     \land new\_value' = [m \in Monitors \mapsto Nil]
     \land pending\_proposal' = [m \in Monitors \mapsto Nil]
     \wedge epoch' = epoch + 1
     \land messages' = [mon1 \in Monitors \mapsto [mon2 \in Monitors \mapsto \langle \rangle]]
     ∧ UNCHANGED ⟨quorum, quorum_sz, accepted, message_history⟩
     \land UNCHANGED \langle data\_vars, restart\_vars, collect\_vars, lease\_vars \rangle
 Start recovery phase if number of monitors in quorum is greater than 1.
 Variables changed: accepted_pn, phase.
 @type: MONITOR \Rightarrow Bool;
election\_recover(mon) \triangleq
     \land quorum\_sz > 1
     \land phase[mon] = PHASE\_ELECTION
     \land collect(mon, 0)
    \land \  \, \mathsf{UNCHANGED} \ \langle \mathit{isLeader}, \ \mathit{state}, \ \mathit{values}, \ \mathit{first\_committed}, \ \mathit{last\_committed}, \ \mathit{monitor\_store} \rangle
     \(\triangle \text{UNCHANGED} \langle qlobal_vars, restart_vars, collect_vars, lease_vars, commit_vars \rangle \)
                                        Timeouts and restart
 Remove monitor from quorum, if there are enough monitors in the quorum.
 @type: MONITOR \Rightarrow Bool;
```

```
Remove monitor from quorum, if there are enough monitors in the quorum.  
@type: MONITOR \Rightarrow Bool;
crash\_mon(mon) \stackrel{\triangle}{=} \\ \land quorum\_sz > (MonitorsLen \div 2) + 1 \\ \land quorum[mon] = \text{TRUE} \\ \land quorum' = [quorum \text{ EXCEPT } ![mon] = \text{FALSE}] \\ \land quorum\_sz' = quorum\_sz - 1
```

```
\land bootstrap
      \land number\_crashes' = number\_crashes + 1
     \land UNCHANGED \langle messages, message\_history \rangle
     \land \  \, \mathsf{UNCHANGED} \ \langle \mathit{state\_vars}, \ \mathit{restart\_vars}, \ \mathit{data\_vars}, \ \mathit{collect\_vars}, \ \mathit{lease\_vars}, \ \mathit{commit\_vars} \rangle
 Add monitor to the quorum.
 @type: MONITOR \Rightarrow Bool;
restore\_mon(mon) \stackrel{\triangle}{=}
     \land quorum[mon] = FALSE
     \land quorum' = [quorum \ EXCEPT \ ! [mon] = TRUE]
     \land quorum\_sz' = quorum\_sz + 1
     \land bootstrap
     \land UNCHANGED \langle messages, message\_history \rangle
     \(\triangle \) UNCHANGED \(\state_vars, \) restart_vars, \(data_vars, \) collect_vars, \(lease_vars, \) commit_vars\(\rangle \)
 Monitor timeout (simulate the various timeouts that can occur). Triggers new elections.
 Variables changed: epoch.
 @type: MONITOR \Rightarrow Bool;
Timeout(mon) \triangleq
     \land bootstrap
         UNCHANGED \(\langle messages, quorum, quorum_sz, message_history, state_vars, restart_vars, \)
                             data_vars, collect_vars, lease_vars, commit_vars
```

Dispatchers and next statement

```
Handle a message.
 @type: MESSAGE \Rightarrow Bool;
Receive(msg) \triangleq
    \land \lor \land msg.type = OP\_COLLECT
           \land handle\_collect(msg.dest, msg)
           \land step\_name' = "receive collect"
        \lor \land msg.type = OP\_LAST
           \land handle\_last(msg.dest, msg)
           \land step\_name' = "receive last"
        \lor \land msq.type = OP\_LEASE
           \land handle\_lease(msg.dest, msg)
           \land step\_name' = "receive lease"
        \lor \land msg.type = OP\_LEASE\_ACK
           \land handle\_lease\_ack(msg.dest, msg)
           \land step\_name' = "receive lease\_ack"
        \lor \land msg.type = OP\_BEGIN
           \land handle\_begin(msg.dest, msg)
```

```
\land step\_name' = "receive begin"
         \lor \land msg.type = OP\_ACCEPT
            \land handle\_accept(msg.dest, msg)
            \land step\_name' = "receive accept"
         \lor \land msg.type = OP\_COMMIT
            \land handle\_commit(msg.dest, msg)
            \land step\_name' = "receive commit"
 Limit some variables to reduce search space.
 @type: Bool;
reduce\_search\_space \triangleq
    \land\; epoch \neq 8
    \land \lor \forall mon \in Monitors : last\_committed[mon] < 2
        \lor \forall \, mon2 \in Monitors \colon \, new\_value[mon2] = Nil
    \land \forall mon \in Monitors : accepted\_pn[mon] < 300
     \land number\_crashes \neq 4
 State transitions.
 @type: Bool;
Next \triangleq
    \land\ reduce\_search\_space
    \wedge IF epoch\%2 = 1 THEN
        \land leader_election
        \land step\_name' = "election"
        \land UNCHANGED number\_crashes
        ELSE
        \lor \land \exists mon \in Monitors : election\_recover(mon)
            \land step\_name' = "election\_recover"
           \land UNCHANGED number\_crashes
         \lor \land \exists mon \in Monitors : send\_collect(mon)
            \land step\_name' = "send\_collect"
           \land UNCHANGED number\_crashes
         \lor \land \exists mon \in Monitors : post\_last(mon)
           \land \mathit{step\_name'} = "\mathsf{post\_last"}
            \land UNCHANGED number\_crashes
         \vee \wedge \exists mon \in Monitors : post\_lease\_ack(mon)
           \land step\_name' = "post\_lease\_ack"
            \land UNCHANGED number\_crashes
         \lor \land \exists mon \in Monitors : post\_accept(mon)
           \land step\_name' = "post\_accept"
            ∧ UNCHANGED number_crashes
```

```
\lor \land \exists mon \in Monitors : finish\_commit(mon)
  \land step\_name' = "finish\_commit"
  ∧ UNCHANGED number_crashes
\lor \land \exists mon \in Monitors : \exists v \in Value\_set : client\_request(mon, v)
  \land step\_name' = "client\_request"
  ∧ UNCHANGED number_crashes
\lor \land \exists mon \in Monitors : propose\_pending(mon)
  \land step\_name' = "propose\_pending"
  ∧ UNCHANGED number_crashes
\lor \land \exists mon1, mon2 \in Monitors:
       \land \ mon1 \neq mon2
       \land Len(messages[mon1][mon2]) > 0
       \land Receive(messages[mon1][mon2][1])
  ∧ UNCHANGED number_crashes
\lor \land \exists mon \in Monitors : crash\_mon(mon)
  \land step\_name' = "crash\_mon"
  ∧ UNCHANGED number_crashes
\lor \land \exists mon \in Monitors : restore\_mon(mon)
  \land step\_name' = "restore\_mon"
  ∧ UNCHANGED number_crashes
\lor \land \exists mon \in Monitors : Timeout(mon)
  \land step\_name' = "timeout\_and\_restart"
  ∧ UNCHANGED number_crashes
```

Safety invariants

```
If two monitors are in state active then their monitor\_store must have the same value. @type: Bool; same\_monitor\_store \ \stackrel{\triangle}{=} \ \forall \ mon1, \ mon2 \in Monitors: \\ state[mon1] = STATE\_ACTIVE \land state[mon2] = STATE\_ACTIVE \\ \Rightarrow monitor\_store[mon1] = monitor\_store[mon2] Invariant. @type: Bool; Inv \ \stackrel{\triangle}{=} \ \land \ same\_monitor\_store
```

Test/Debug invariants

Invariant used to search for a state where 'x' happens. $Inv_find_state(x) \stackrel{\Delta}{=} \neg x$

```
Invariant used to search for a behavior of diameter equal to 'size'.
 TLCGet("level") not supported by snowcat typechecker.
 Inv\_diam(size) \stackrel{\Delta}{=} TLCGet("level") \neq size - 1
 Invariants to test in model check
DEBUG\_Inv \stackrel{\Delta}{=} \land TRUE
                     \wedge Inv\_diam(20)
Examples:
Find a behavior with a diameter of size 60.
Inv\_diam(60)
Find a behavior where two different monitors assume the role of a leader.
Inv\_find\_state(
  \exists msg1, msg2 \in message\_history:
     \land \ msg1.type = OP\_COLLECT \land msg2.type = OP\_COLLECT
     \land msg1.from \neq msg2.from
Find a state where a monitor crashed during the collect phase and fails to send a OP_LAST
message.
Inv\_find\_state(
   \land step\_name = "crash mon"
   \ * The system is in collect phase and no OP_LAST message has been received.
   \land \exists mon \in Monitors :
     \land isLeader[mon] = TRUE
     \land phase[mon] = PHASE\_COLLECT
     \land num\_last[mon] = 1
   \ * All the collect requests have been handled by the peers.
   \land \forall mon1, mon2 \in Monitors:
     \forall i \in 1 ... Len(messages[mon1][mon2]) : messages[mon1][mon2][i].type \neq OP\_COLLECT
   \land epoch = 2
Find a state where the leader crashes during the commit phase, failing to complete the commit.
Inv_find_state(
   \land step\_name = "crash mon"
   \land \exists mon1, mon2 \in Monitors:
     \exists \ i \in 1 \ . \ Len(messages[mon1][mon2]) : messages[mon1][mon2][i]. type = OP\_ACCEPT
   \land \ \forall \ mon \in \mathit{Monitors}:
     isLeader[mon] = False
   \land\ epoch=2
Note: After finding a state, that complete state can be used as an initial state to analyze behaviors
from there.
\ * Modification History
\ * Created Mon Jan 11 16:15:26 WET 2021 by afonsonf
```