

# Request that you should not refuse

- PLEASE SWITCH OFF AND PUT AWAY YOUR CELL PHONES
- LAPTOPS OK IF WORK IS ACADEMIC
- REMOVE BAGS AND OTHER MATERIALS THAT CAN CAUSE DISTRACTION
- STOP HAVING SIDE CONVERSATIONS
- PARTICIPATE IN CLASS

# Class 7

## Review

Automation: Robots and the Labor Market

Identifying Labor Demand Elasticities

(Women, War and Wages)

Minimum Wages if time permits

- **Read for Wednesday's Class (Class 8)**

- **3.2.3 – Characteristics of Minimum Wage Workers 2014**
- **3.2.4 – David Neumark – Minimum Wage Controversy**

**Work on The Problem Set – Disregard Quantitative Problems on Labor Supply (turn PS 1 in on Class 8 Wed)**

**We will start with Labor Supply on Class 8 (Wed) & continue with it till Week 6 (Class 11 & Class 12)**

Updated lecture 5 and lecture 6 after  
correcting for a small algebraic error

**Right before MT 2 and After MT 2 Exam we will  
discuss labor supply issues: returns to education,  
grade inflation, discrimination, poverty**

$$q = (\delta_1 E^\rho + \delta_2 K^\rho)^{\frac{1}{\rho}} \quad \frac{\partial q}{\partial E} = f(E, K) = \frac{1}{\rho} q^{\frac{1}{\rho}-1} \delta_1 E^{\rho-1} = MP_E$$

$$\frac{\partial q}{\partial K} = f(E, K) = \frac{1}{\rho} q^{\frac{1}{\rho}-1} \delta_2 K^{\rho-1} = MP_K$$

$$\Gamma = pq + \lambda[TC - wE - rK]$$

$$\frac{\partial \Gamma}{\partial E} = pMP_E - \lambda w = 0 \dots (1) \rightarrow pMP_E = \lambda w$$

$$\frac{\partial \Gamma}{\partial K} = pMP_K - \lambda r = 0 \dots (2) \rightarrow pMP_K = \lambda r$$

$$\left. \begin{array}{l} \dots (1) \\ \dots (2) \end{array} \right\} \rightarrow \frac{\delta_1}{\delta_2} \left( \frac{K^*}{E^*} \right)^{1-\rho} = \frac{w}{r} \dots (4)$$

$$\frac{\partial \Gamma}{\partial \lambda} = 0 \Rightarrow TC - wE^* - rK^* = 0 \dots (3)$$

$E^*$  will give Demand for Labor Function. Using 3 and 4

$$\left. \begin{array}{l} TC = wE^* + rK^* \\ K^* = \left( \frac{\delta_2 w}{\delta_2 r} \right)^{\frac{1}{1-\rho}} E^* = mE^* \end{array} \right\} \rightarrow TC = wE^* + rmE^*$$

$$\rightarrow E^* = \frac{TC}{(w + rm)}$$

Suppose the manufacturing industry in a US city has labor demand and supply curves estimated as

$$w = A - Bh^d \dots (1)$$

$$w = C + Dh^s \dots (2)$$

In the baseline the industry does not use any machines. Suppose the firms in the industry start employing **R** robots to substitute humans. Which equation will you modify (equation 1 or equation 2) and how? You might want to draw a graph to know. Find the equilibrium wage and employment in baseline and in the case of new equilibrium.

# Short Run Demand for Labor

$$q = A \log E + \bar{K}^\beta$$

$$\frac{\partial f(E, K)}{\partial E} = \frac{A}{E} = MP_E$$

$$\Gamma = p(A \log E + \bar{K}^\beta) - wE - r\bar{K}$$

$$\frac{\partial \Gamma}{\partial E} = p \frac{A}{E} - w = 0 \dots (1)$$

$$\rightarrow E^* = \frac{A}{pw} \dots (2)$$

$$\rightarrow \text{If } A=100; p=1 \text{ Then } E^* = \frac{100}{w}$$

$$q = E^\alpha \bar{K}^\beta$$

$$\frac{\partial f(E, K)}{\partial E} = \alpha E^{\alpha-1} \bar{K}^\beta = MP_E$$

$$\Gamma = p(E^\alpha \bar{K}^\beta) - wE - r\bar{K}$$

$$\frac{\partial \Gamma}{\partial E} = p \alpha E^{\alpha-1} \bar{K}^\beta - w = 0 \dots (1.1)$$

$$\rightarrow E^* = \left( \frac{w}{p \alpha \bar{K}^\beta} \right)^{\frac{1}{\alpha-1}} \dots (2.1)$$

$$\rightarrow \text{If } p=1; \alpha=0.5$$

$$\rightarrow \text{Then } E^{*(1-\alpha)} w = \frac{\bar{K}^\beta}{2}$$

4/24/2017 SHIFT of DD : The sign on beta is CRITICAL

# Why are there so many jobs?

## Labor Markets and Automation

*Figure 1*

**Average Change per Decade in US Occupational Employment Shares for Two Periods: 1940–1980 and 1980–2010**

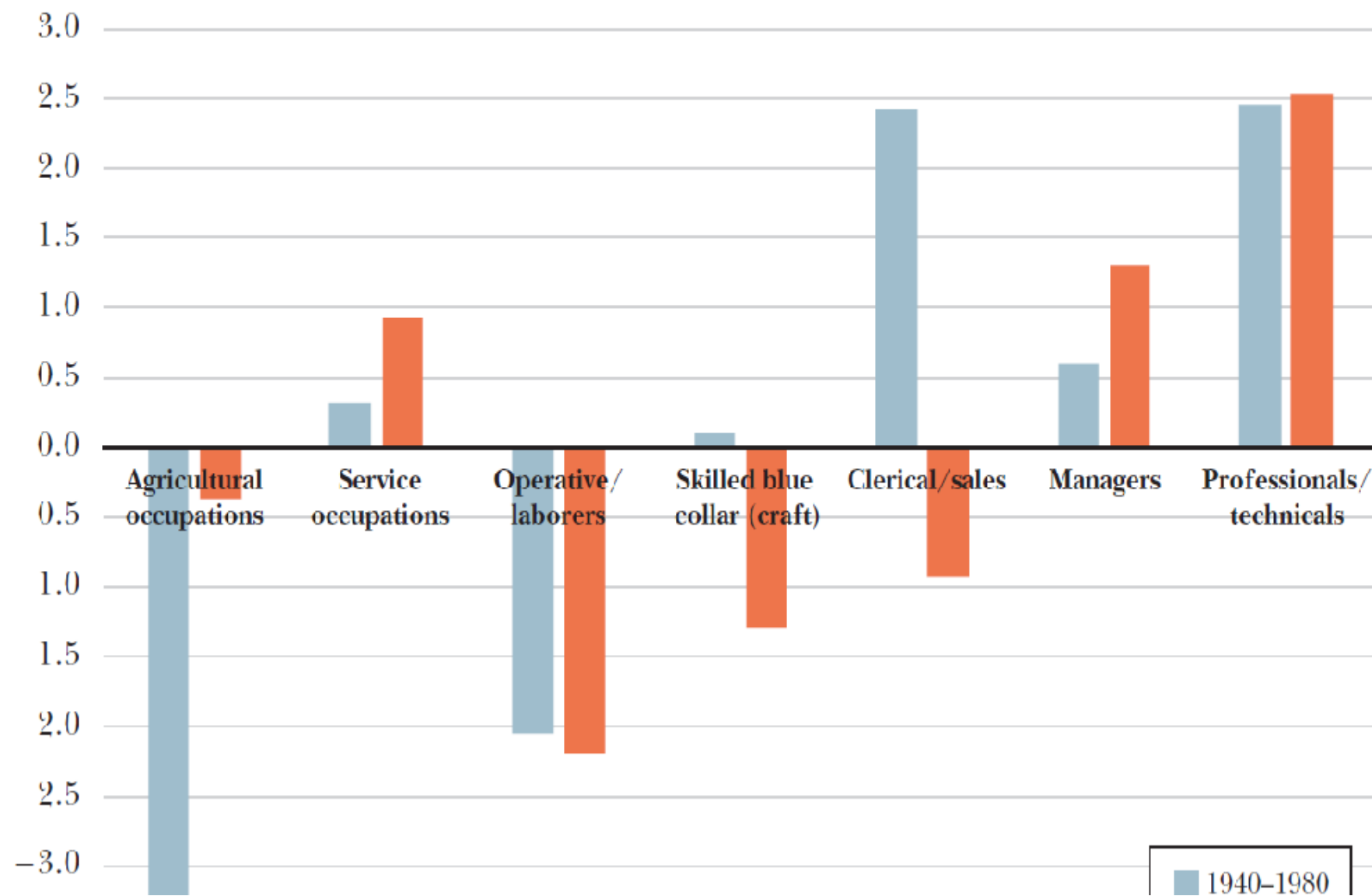




Figure 2

Change in Employment by Major Occupational Category, 1979–2012

(the y-axis plots 100 times log changes in employment, which is nearly equivalent to percentage points for small changes)

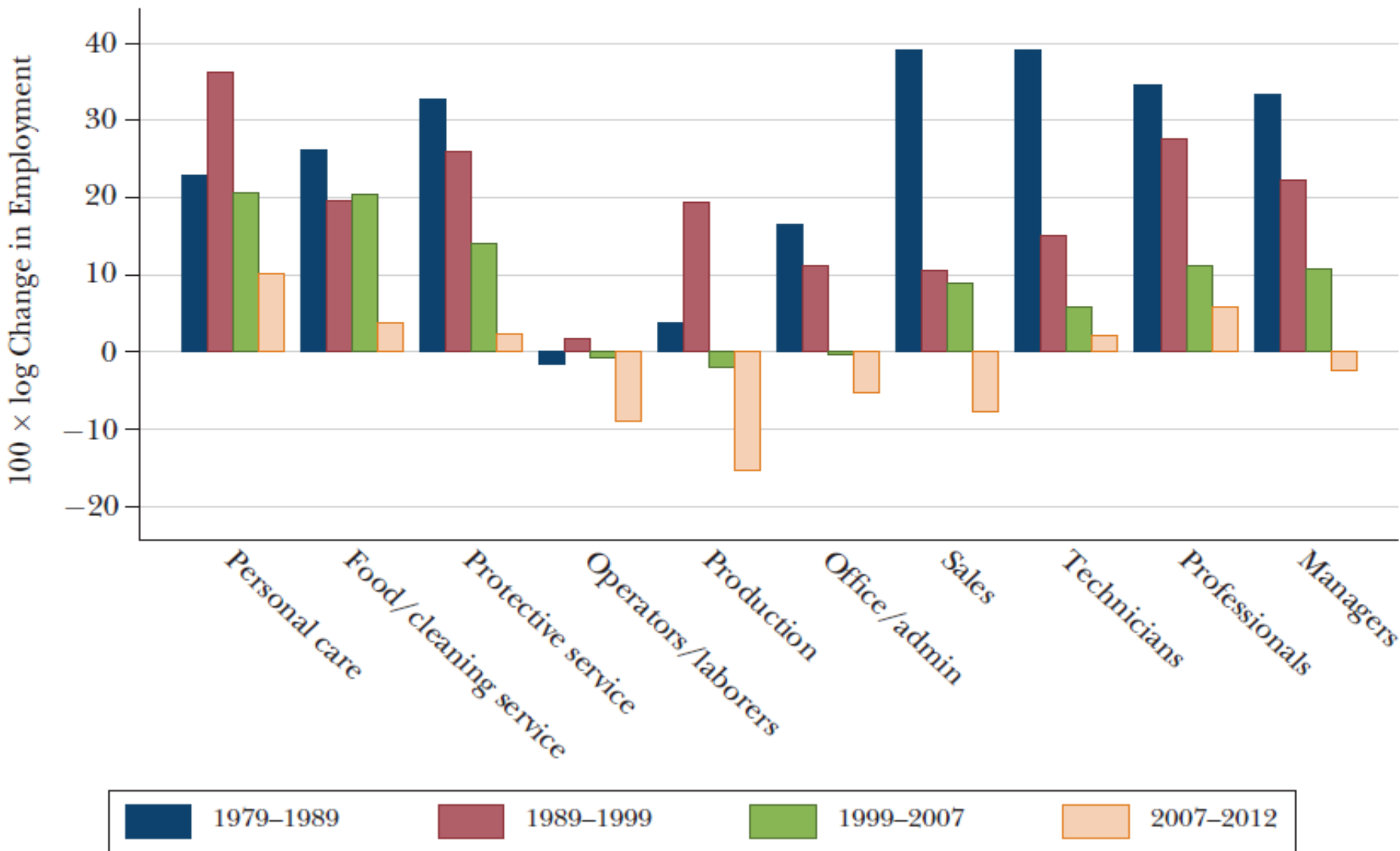
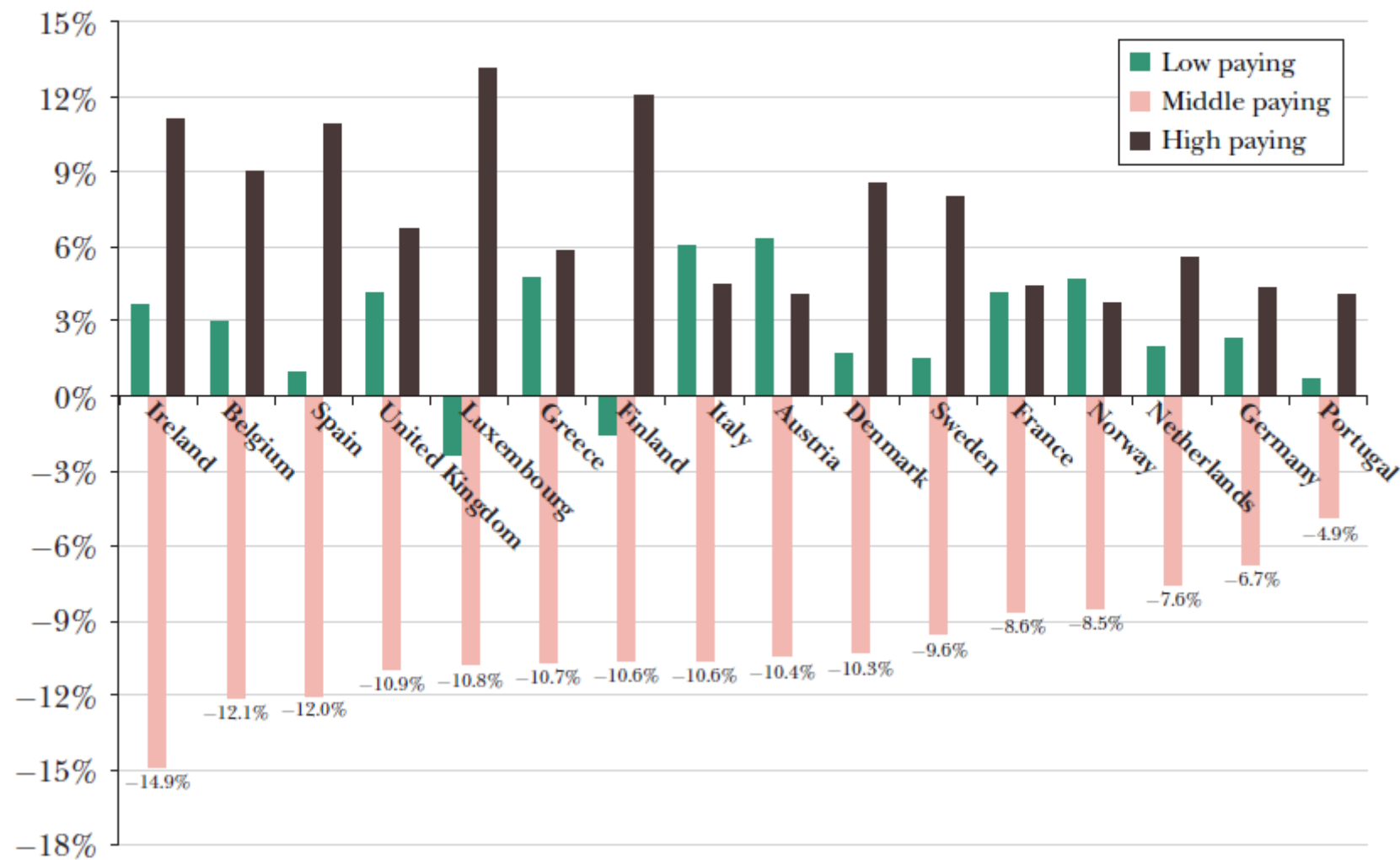


Figure 3

## Change in Occupational Employment Shares in Low, Middle, and High-Wage Occupations in 16 EU Countries, 1993–2010



## Changes in Mean Wages by Occupational Skill Percentile among Full-Time, Full-Year (FTFY) Workers, 1979–2012

*(the y-axis plots 100 times log changes in employment, which is nearly equivalent to percentage points for small changes)*

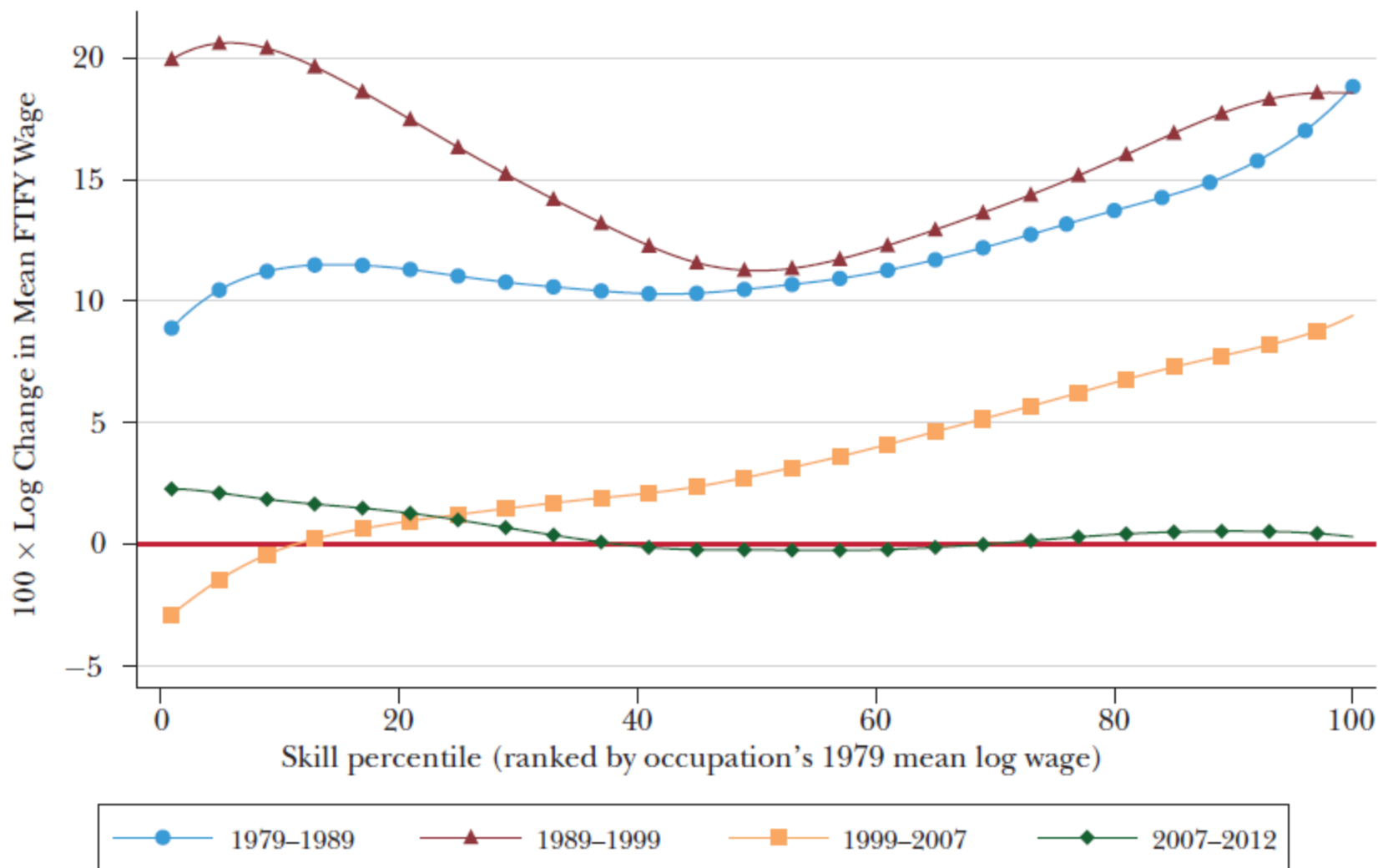
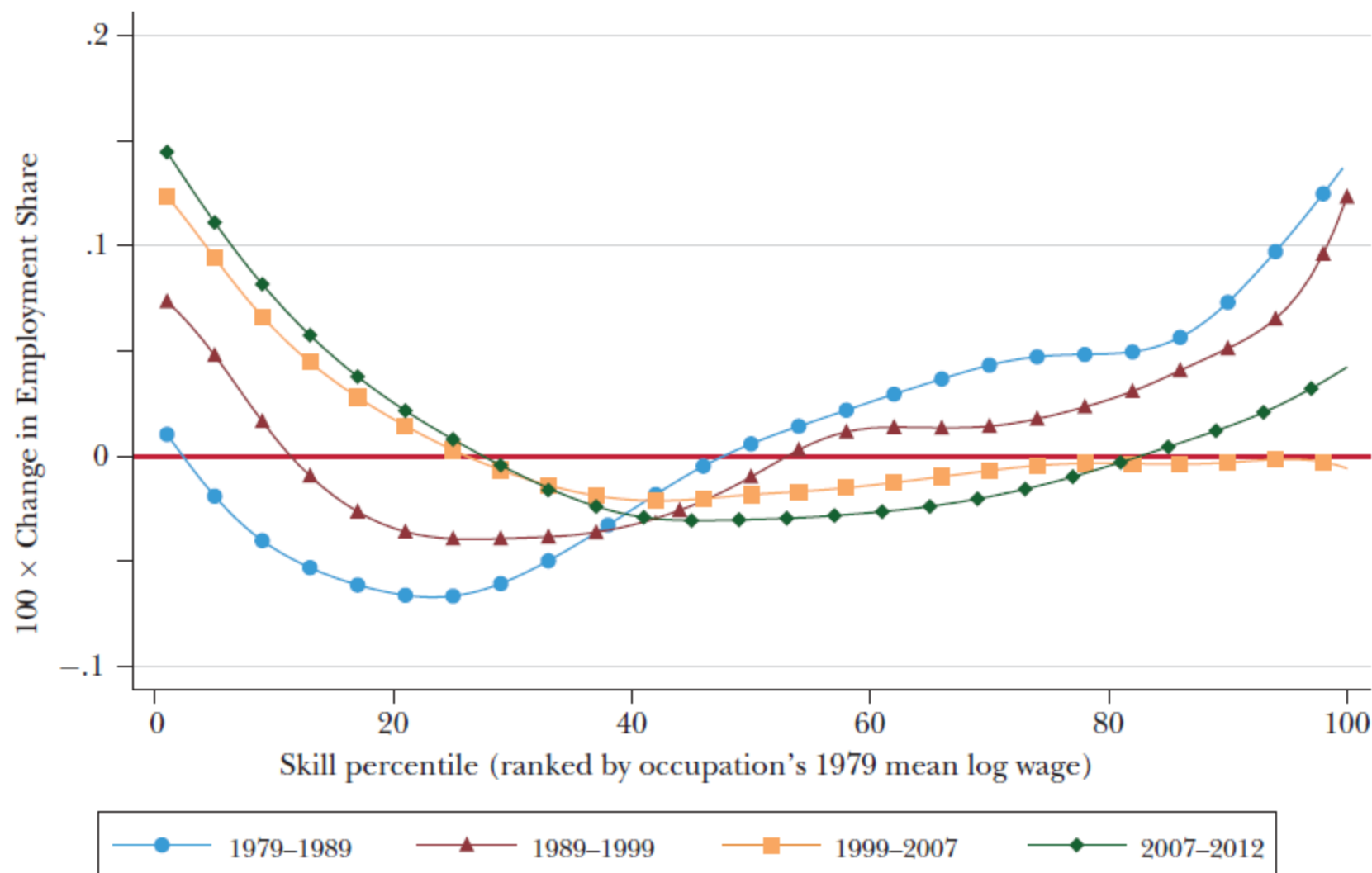


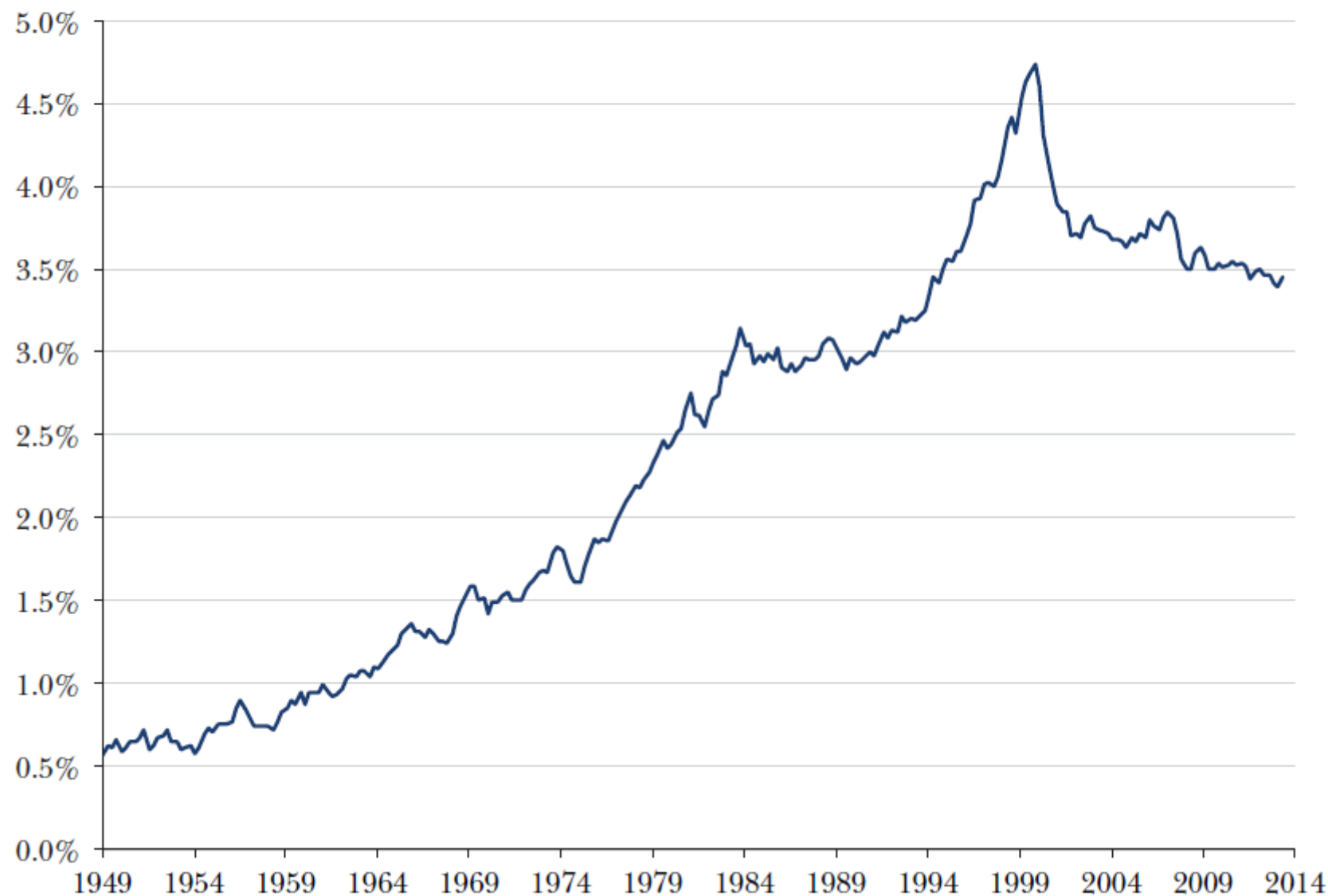
Figure 5

# Smoothed Employment Changes by Occupational Skill Percentile, 1979–2012



*Figure 6*

**Private Fixed Investment in Information Processing Equipment and Software as a Percentage of Gross Domestic Product, 1949–2014**



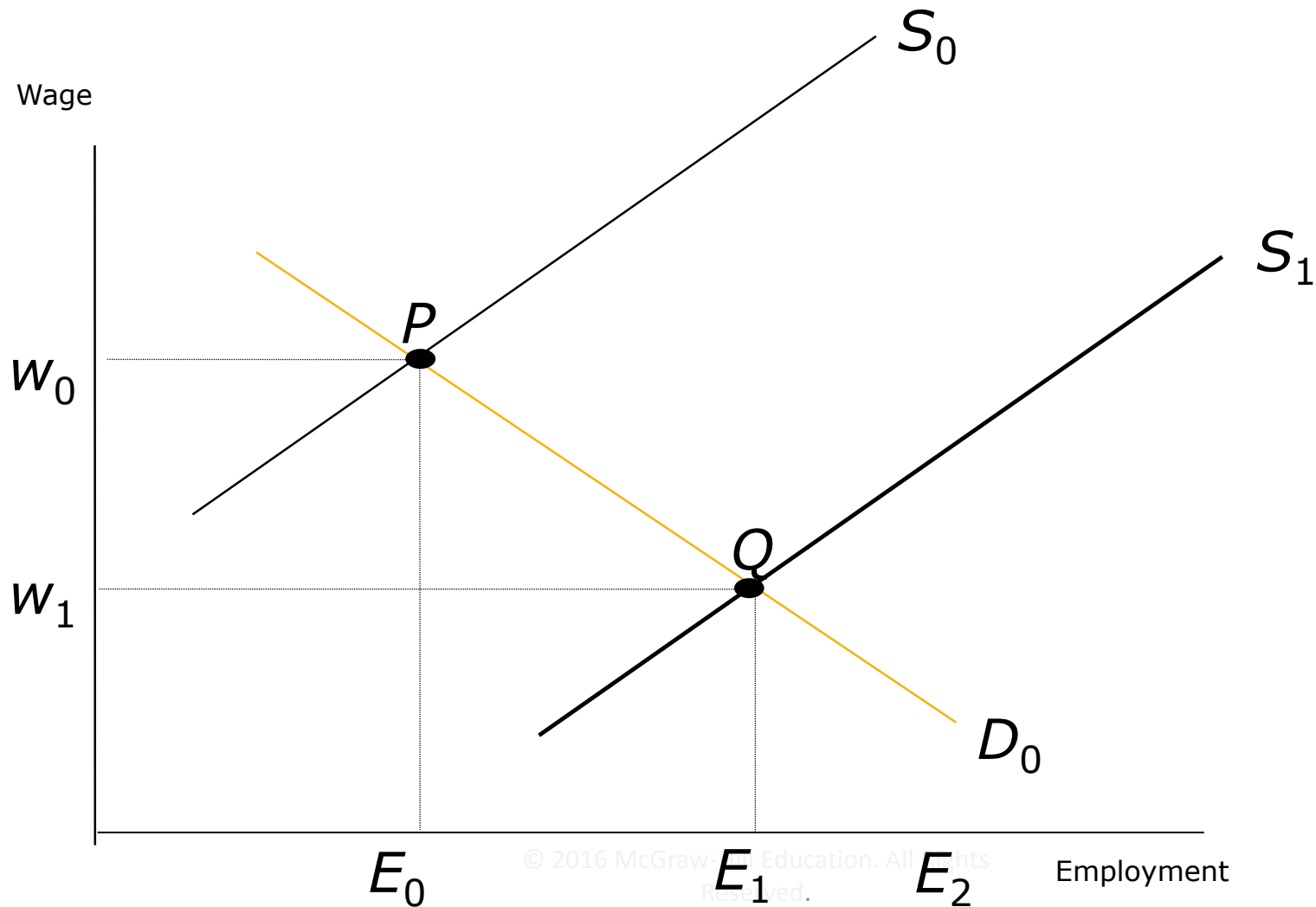
<https://www.youtube.com/watch?v=7Pq-S557XQU>

Humans need not apply (15 mins) –  
You Tube

<https://www.nytimes.com/2017/02/23/magazine/universal-income-global-inequality.html? r=0>

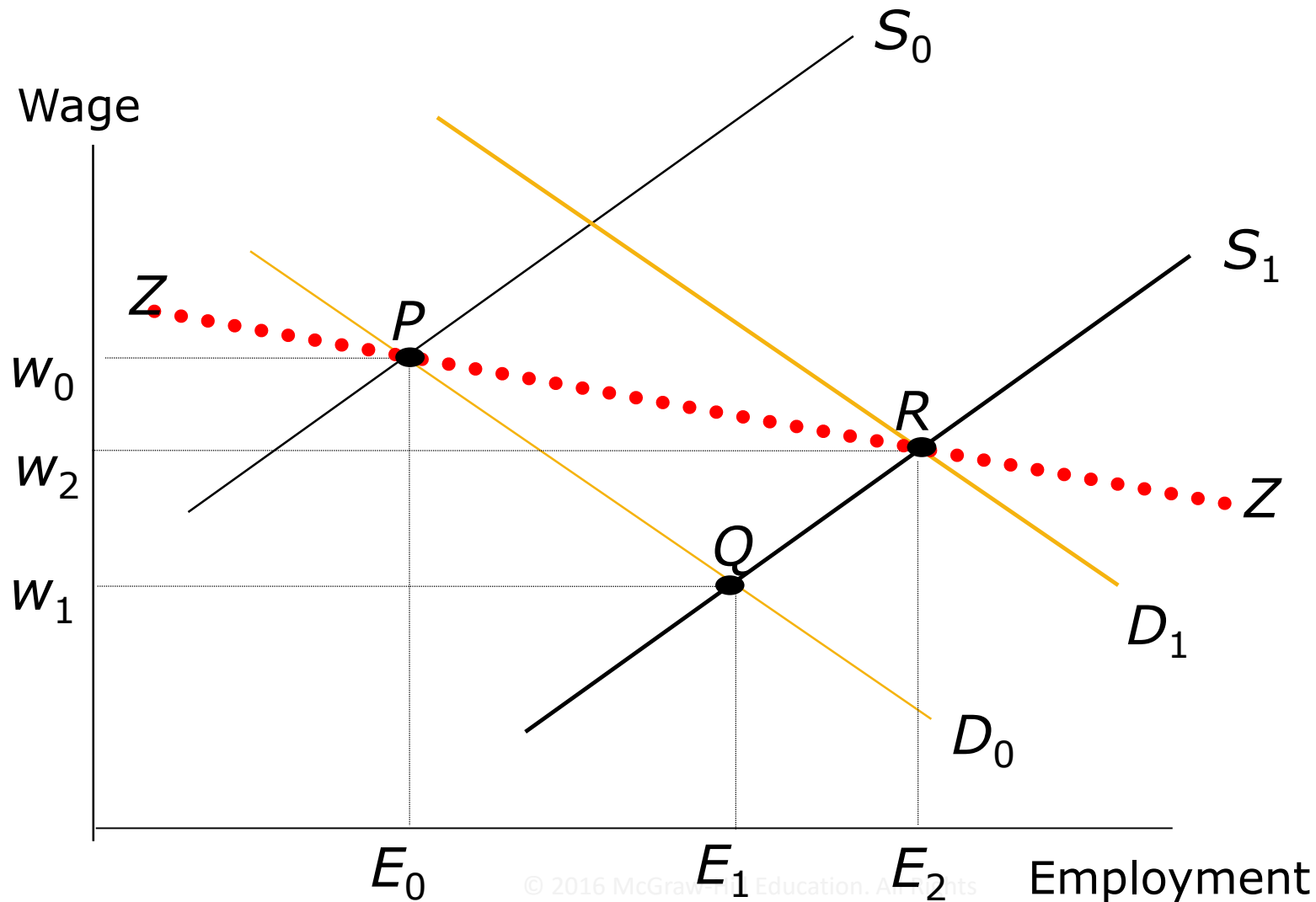
**The future of not working - NYT**

# Estimating Labor Demand for Women





# Empirical Identification of Labor Demand Elasticities



# Women War and Wages

(Acemoglu, Autor and Levy)

# The main variables

- How female labor force participation affects the structure of male and female wages?
- **Dependent Variable ( $y$ ):** Wages of males and females
- **Independent Variable ( $x$ ):** Endogenous Regressor: Labor Force Participation of Women
- **Instrument ( $z$ ):** Exogenous mobilization of men 18-44 in different states of US in 1940

# The IV: Mobilization of men as a predictor for labor participation for women

- only 28 percent of U.S. women over the age of 15 participated in the labor force in 1940
- By 1945 this figure exceeded 34 percent
- Temporary increase in labor supply
- Exogenous b/c the men were selected by draft committees which had different rules in different states

# Challenge I – State Level Factors other than mobilization of men have affected growth in female labor supply : causing weak instrument

- First Stage partial R square; F Stat significant and right sign
- Include more state level characteristics
  - fraction of farmers before the war
  - Racial, educational and occupational structures

## Challenge II – Increase in woman's labor demand because of problems of employability of men: causing simultaneity

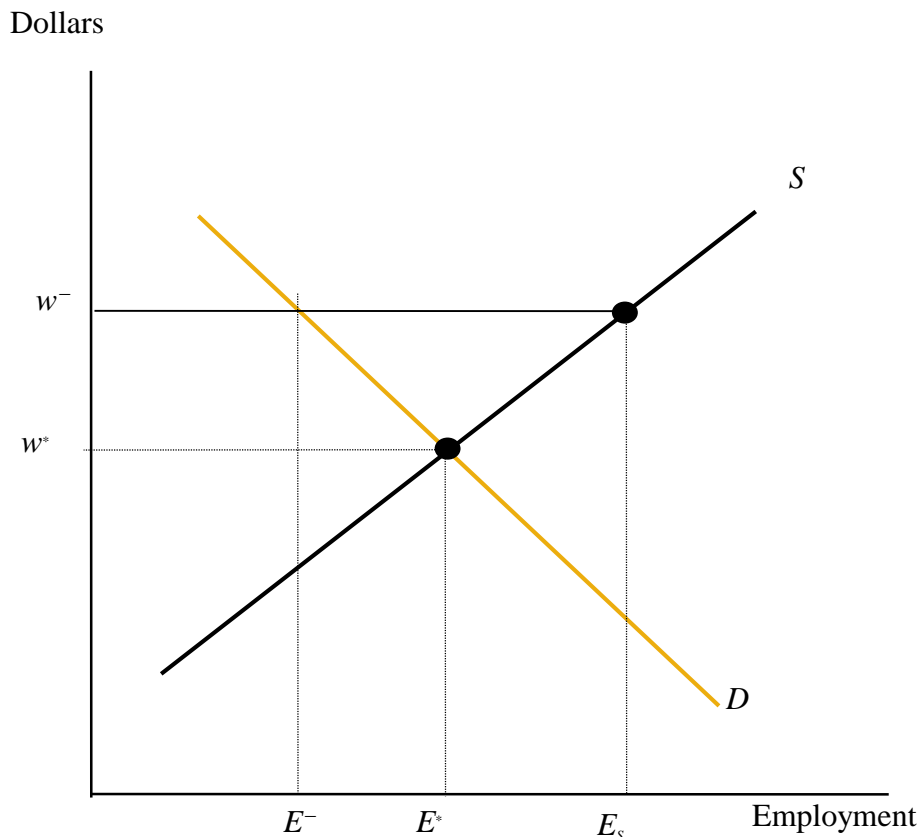
- If greater female participation in 1950 were driven by **demand** rather than supply factors, we would expect **relatively greater wage growth for both women and men in high-mobilization states**
- In reality, both men and women earned relatively **less** in high-mobilization states in 1950 than in 1940

# Results

1. Greater female labor supply reduces female wages. A 10 percent increase in female labor supply relative to male labor supply lowers female wages by 7–8 percent, implying a labor demand elasticity of -1.2 to -1.5.
2. Greater female labor supply also reduces male wages. A 10 percent increase in relative female labor supply typically lowers male earnings by 3–5 percent.

# The Impact of the Minimum Wage on Employment

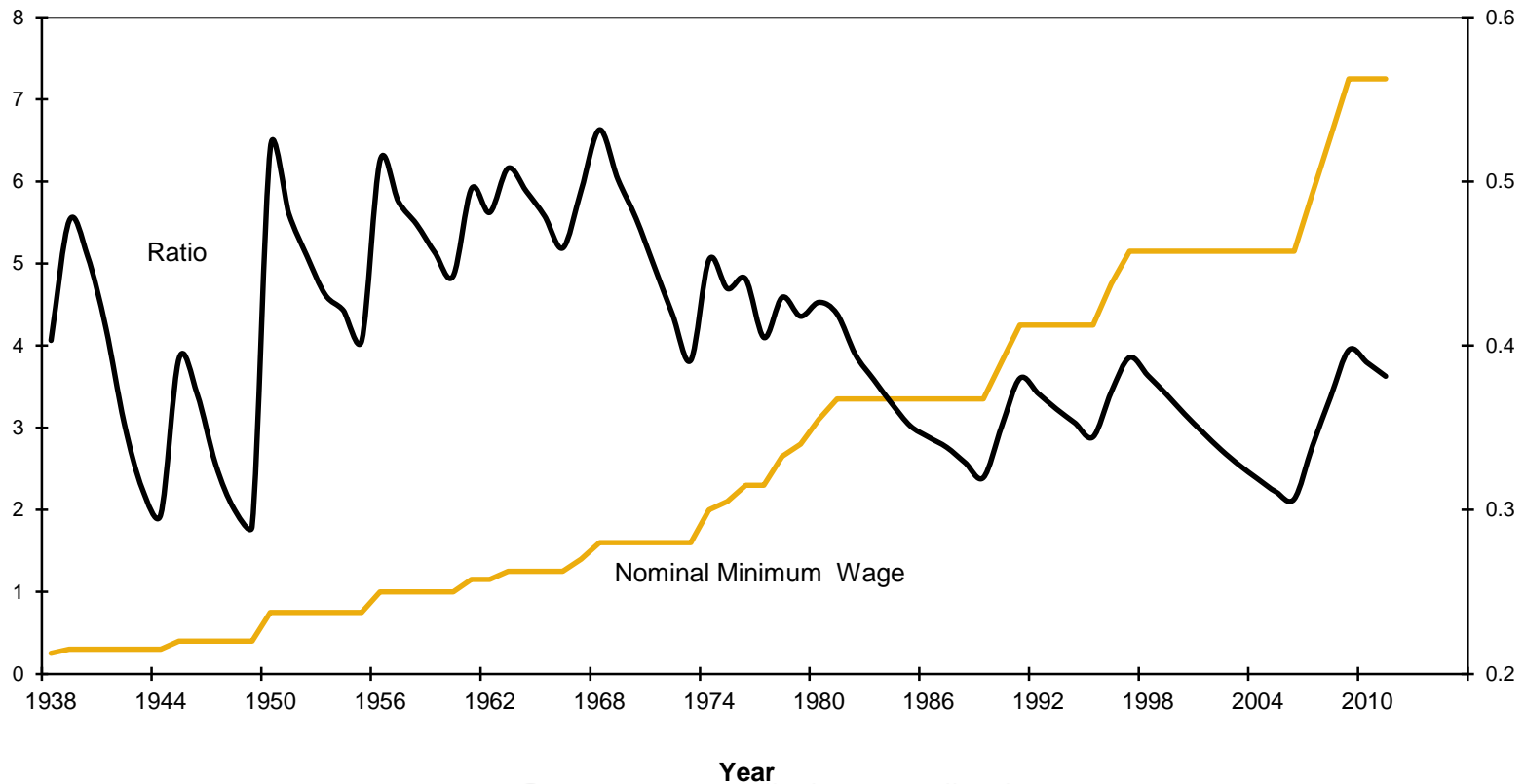
$$\text{Unemployment Rate} = \frac{E_s - \bar{E}}{E_s}$$



A minimum wage set at  $w^-$  results in employers cutting employment from  $E^*$  to  $E^-$ . The higher wage also encourages  $E_s - E^*$  workers to enter the market. Thus, under a minimum wage,  $E_s - E^-$  workers are unemployed.



# Nominal Minimum Wages & Ratio of Minimum wage to Average Manufacturing Wage in the United States , 1938-2011



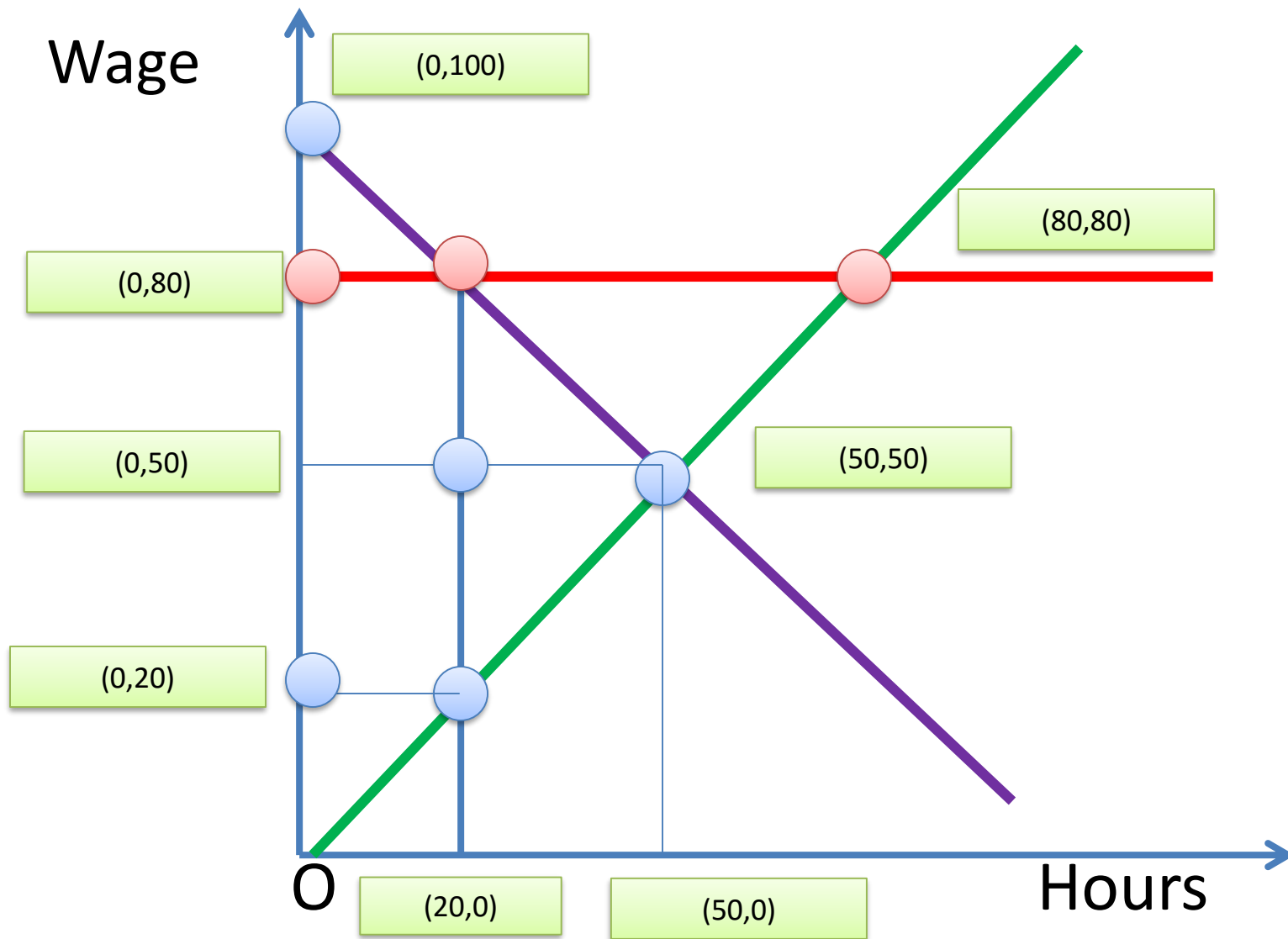
# Solving Two Unknowns from Two Linear Equations

$$w = 100 - h^d \dots(1)$$

$$w = h^s \dots(2)$$

$$\overline{w} = 80$$

- a. Draw DD and SS on Graph
- b. Solve for Equilibrium wage rate and hours
- c. What quantity is demanded and supplied at the wage floor ( $\overline{w}$ ) i.e. find out  $E^d$  and  $E^s$  and  $E^*$
- d. Find the unemployment rate



	Before the Price Floor (Min Wage)	After the Price Floor (Min Wage)	Change
Firm Surplus	$\frac{1}{2} \times 50 \times 50 = 1250$	$(\frac{1}{2} \times 20 \times 20) = 200$	$-(\frac{1}{2} \times 30 \times 30) - (30 \times 20) = -1050$
Worker Surplus	$\frac{1}{2} \times 50 \times 50 = 1250$	$(\frac{1}{2} \times 20 \times 20) + (30 \times 20) + (30 \times 20) = 1400$	$-(\frac{1}{2} \times 30 \times 30) + (30 \times 20) = 150$
Total Surplus (WS+PS)	$1250 + 1250 = 2500$	$200 + 1400 = 1600$	$-1050 + 150 = -900$

Suppose the manufacturing industry in a US city has labor demand and supply curves estimated as

$$w = A - Bh^d \dots (1)$$

$$w = C + Dh^s \dots (2)$$

In the baseline the industry does not have any minimum wage restriction. Suppose a new law is passed where this sector has to pay a wage floor of **Z which is above the baseline equilibrium wage**. Which equation will you modify (equation 1 or equation 2) and how? You might want to draw a graph to know. Find the equilibrium wage and employment in baseline and in the case of new equilibrium.