

# Request that you should not refuse

- PLEASE SWITCH OFF AND PUT AWAY YOUR CELL PHONES
- LAPTOPS OK IF WORK IS ACADEMIC
- REMOVE BAGS AND OTHER MATERIALS THAT CAN CAUSE DISTRACTION
- STOP HAVING SIDE CONVERSATIONS
- PARTICIPATE IN CLASS

# Class 11

## Creating a literature

Supply of Labor: Lagrangian Set up, Reservation Wage,  
Leisure Demand Function, Labor Supply Function &  
Labor Elasticity

Returns to Education

- Read for Wednesday's Class (Class 12)

**Work on selecting a Literature for final project**

Look at Vive Le Revolution

For upcoming Weekend

Vive Le Revolution & Bertrand and Mullianathan  
Paper

- RULES FOR LITERATURE
- Microeconomics Topics
- Theoretically Rigorous
- Empirically uses identification strategies such as FE, IV, DID, RD etc.
- Main article: Cannot be a survey article or a paper discussed in this or any other classes
- Main Article: Written in last 10-15 years in a ranked economic journal
- Submit on May 17<sup>th</sup> Wed 2017 in class

## EXAMPLE

**Student Name:** \_\_\_\_\_

**Main Article:** Network Effects and Welfare Cultures” By: Marianne Bertrand, Erzo F.P. Wittmer, Sendhil Mullianathan *The Quarterly Journal of Economics*, August 2000

**Auxiliary Article 1)** “Participation in Heterogeneous Communities” By: Alberto Alesina and Eliana Ferrara, *Quarterly Journal of Economics*, Oxford University Press, 2000

**Auxiliary Article 2)** “Networks in the Modern Economy: Mexican Migrants in the U.S. Labor Market” By: Kaivan Munshi, *Quarterly Journal of Economics*, Oxford University Press, 2003

**Auxiliary Article 3)** “The Role of Information and Social Interactions in Retirement Plan Decisions: Evidence from a Randomized Experiment” By: Esther Duflo and Emmanuel Saez, *Quarterly Journal of Economics*, Oxford University Press, 2003

# Parametric Reservation Wage, Interior Solution (Equilibrium)

$$U = U(l, c) = l^\alpha \times c^\beta$$

$$MU_l = \frac{\partial U(l, c)}{\partial l} = \alpha l^{\alpha-1} c^\beta$$

$$MU_c = \frac{\partial U(l, c)}{\partial c} = \beta l^\alpha c^{\beta-1}$$

$$|Slope| = |MRS| = \frac{MU_l}{MU_c} = \frac{\alpha c}{\beta l}$$

$$c = \frac{wT + V}{p} + \frac{-w}{p} l$$

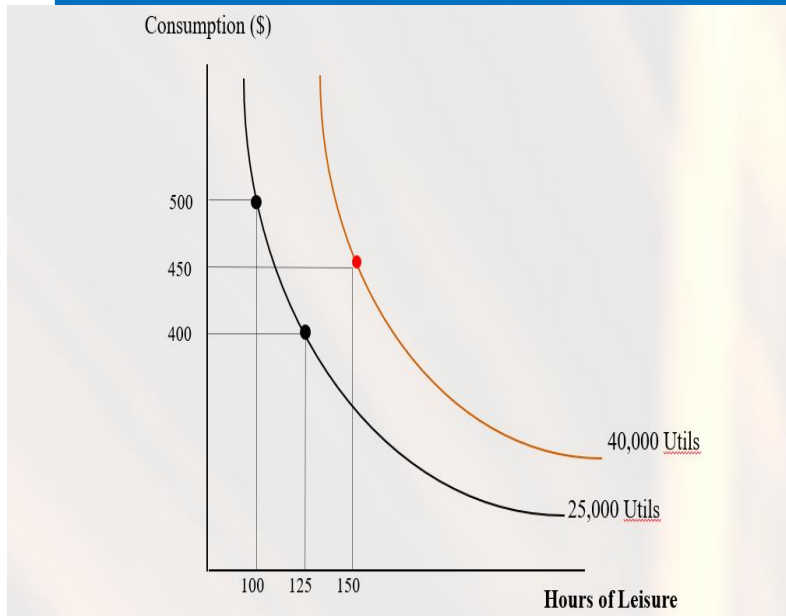
**All Play No Work**

$$VI|_{l=T} = \frac{V}{p}$$

**All Work No Play**

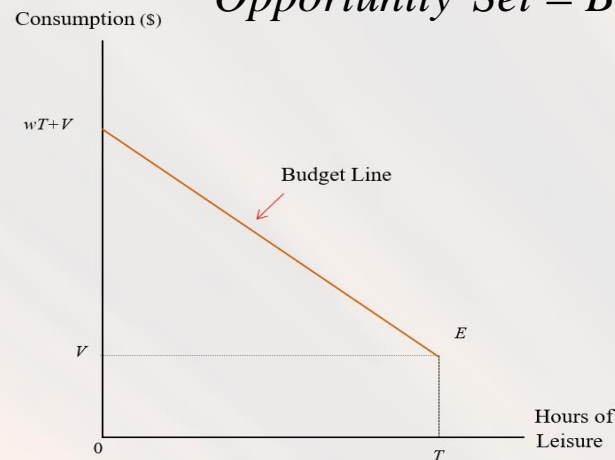
$$VI|_{l=0} = \frac{wT + V}{p}$$

$$|Slope| = |Real\ Wage| = \frac{w}{p}$$



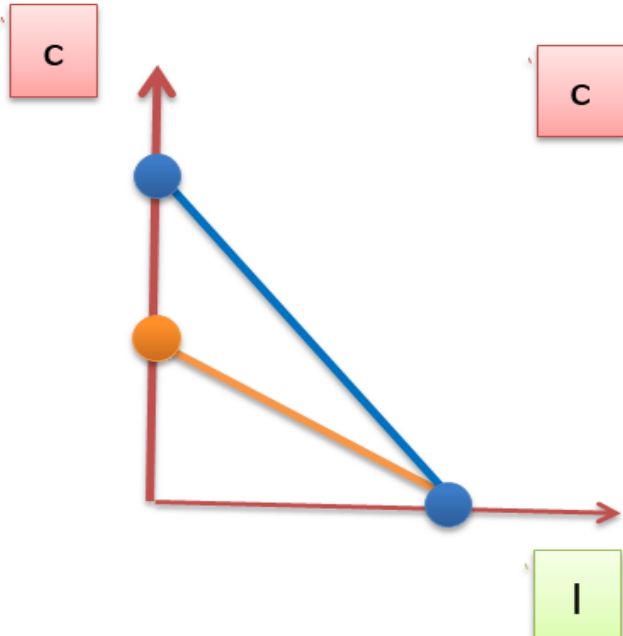
## Graphing the Budget Constraint

*Opportunity Set = Budget Set*

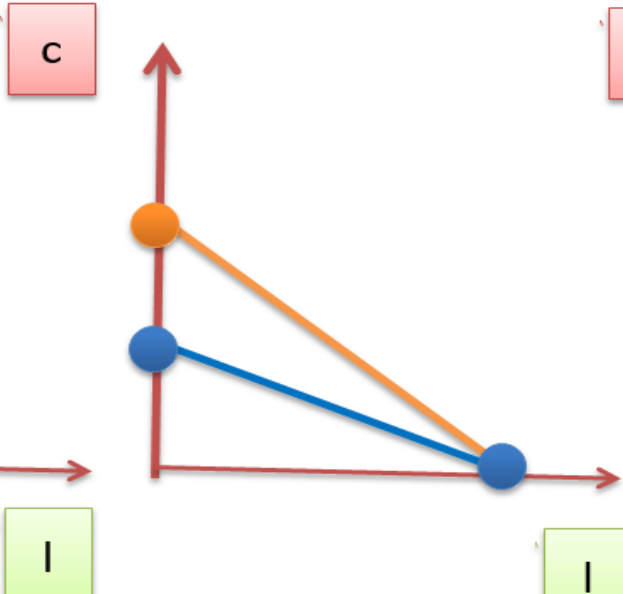


	Baseline/ Benchma rk	Case 1 (increase in w)	Case 2 (Decrease in w)	Case3 (Increase in V)
w	20	40	10	20
p	1	1	1	1
v	0	0	0	100
T	110	110	110	110
<i>Real Wage</i>	20	40	10	20

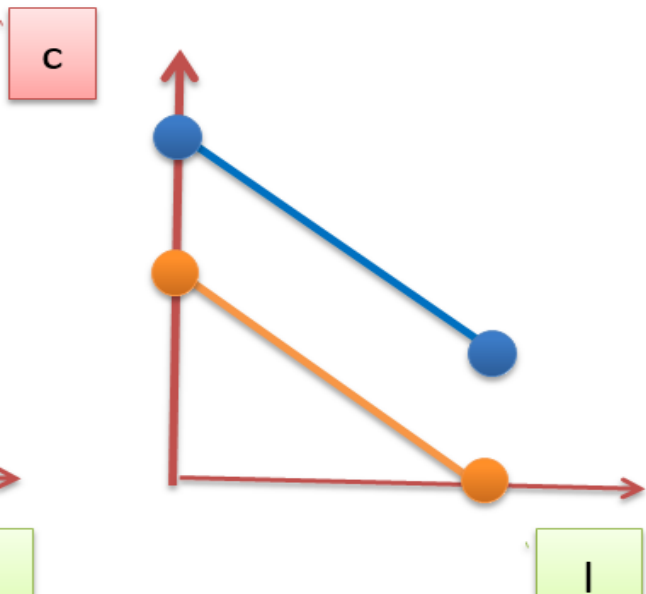
Benchmark & Case 1



Benchmark & Case 2



Benchmark & Case 3



$$RW = |MRS|_{l=T, c=V}$$

## Parametric Reservation Wage, Interior Solution (Equilibrium)

$$RW = \frac{\alpha c}{\beta l} \Big|_{l=T, c=\frac{V}{p}}$$

$$RW = \frac{\alpha V}{\beta p T}$$

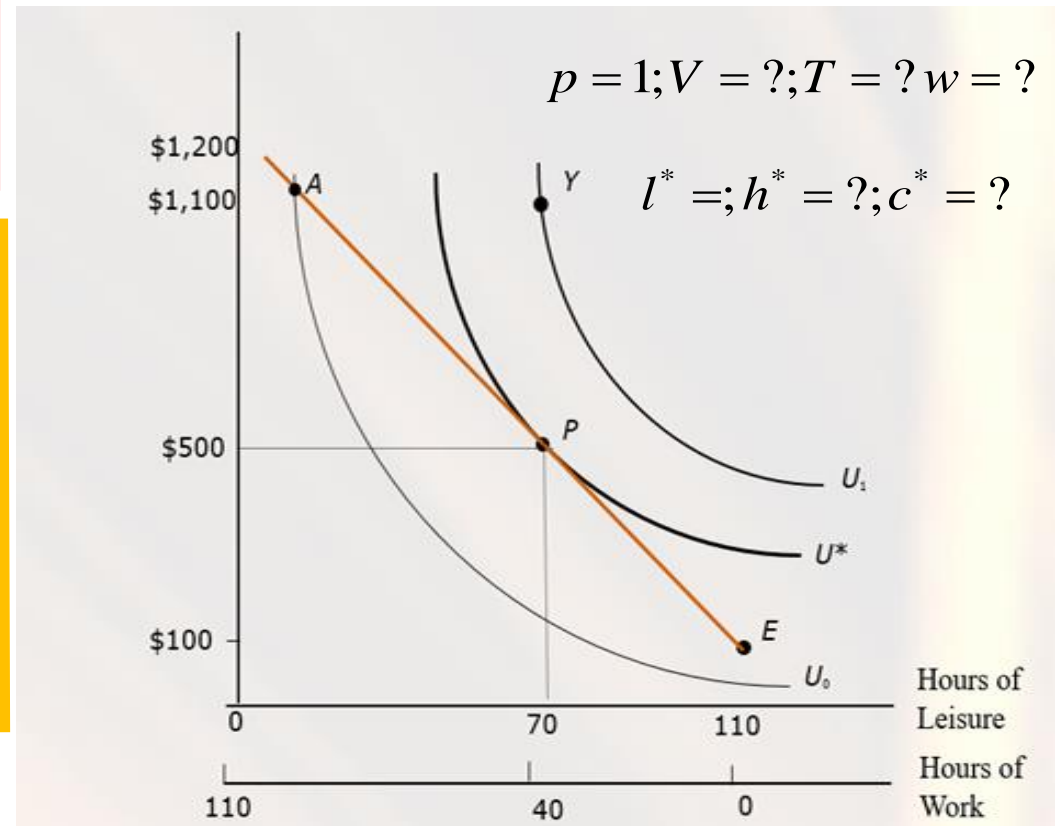
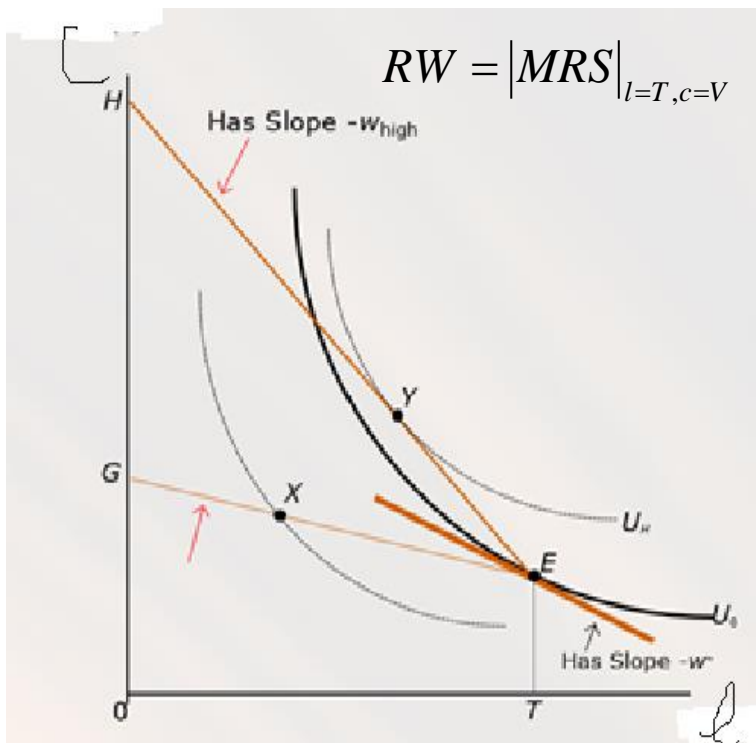
If  $RW < w$  Then  $h^* > 0$

$$|MRS| = |Real\ Wage|$$

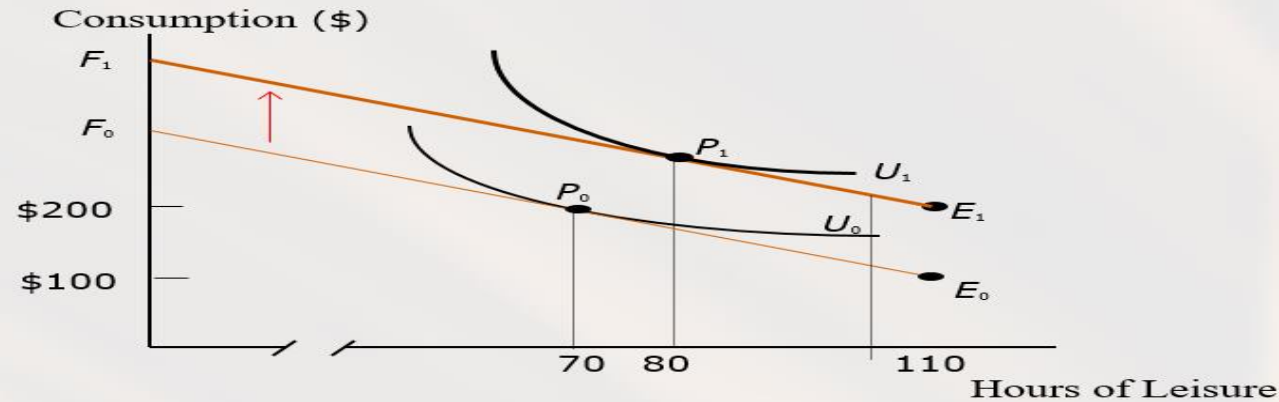
$$\frac{\alpha c}{\beta l} = \frac{w}{p}$$

$$\text{Or, } c^* = \frac{\beta w}{\alpha p} l^* \dots (1)$$

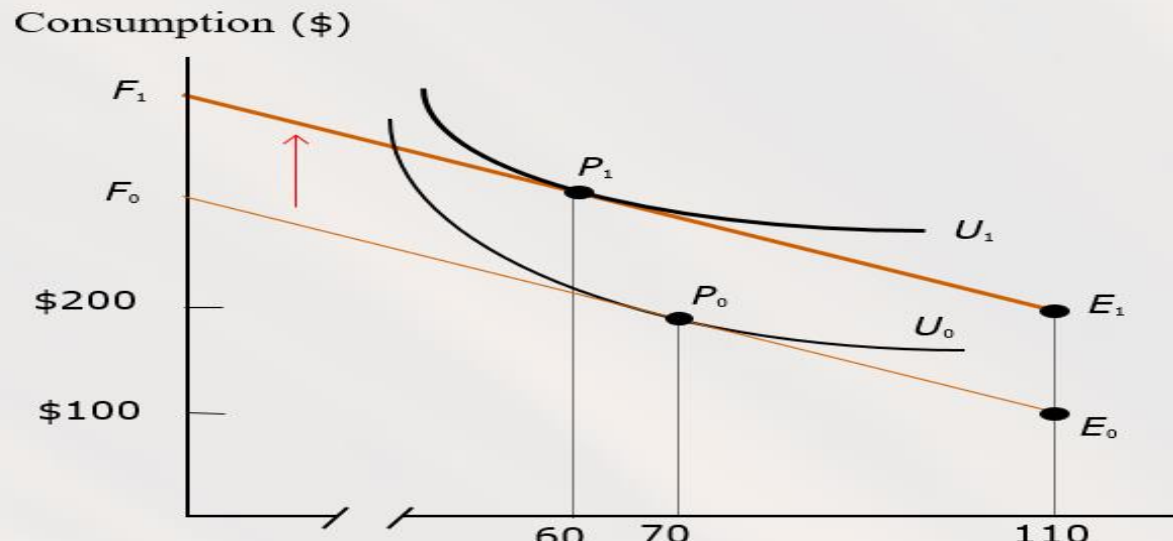
$$c^* = \frac{(wT + V)}{p} - \frac{w}{p} l^* \dots (2)$$



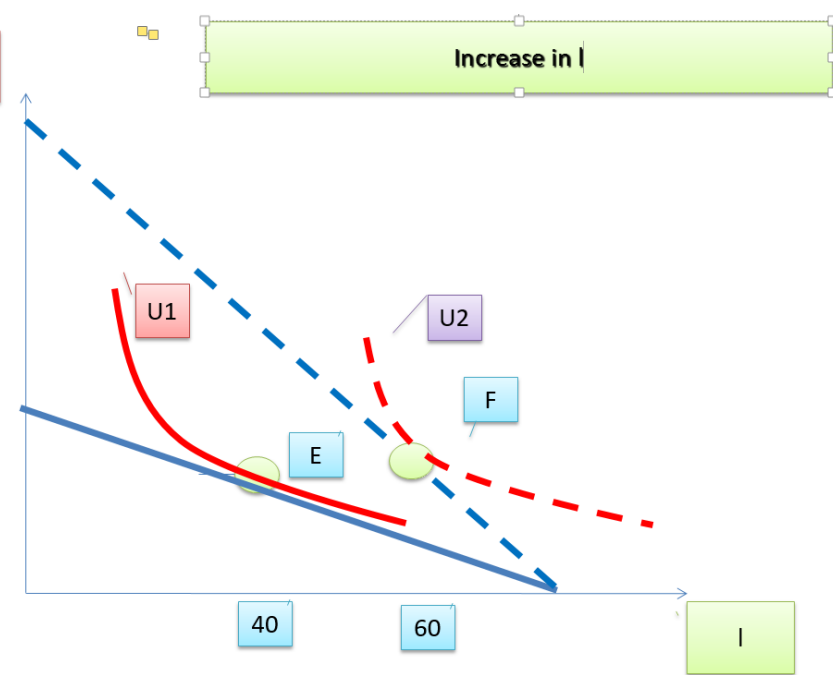
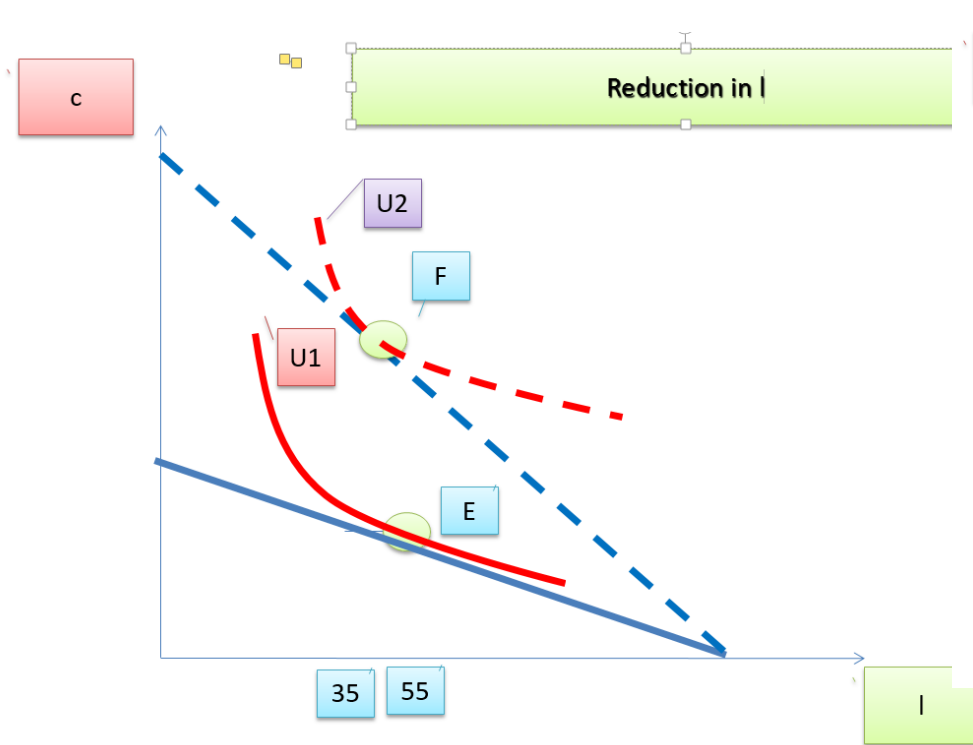
# The Effect of a Change in Nonlabor Income on Hours of Work



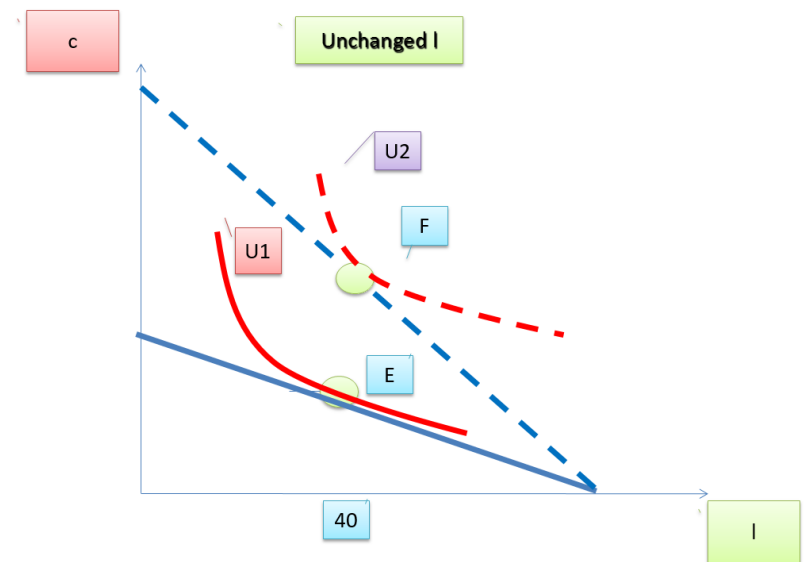
# The Effect of a Change in Nonlabor Income on Hours of Work







**Draw Corresponding Labor Supply Functions in Class**



# Substitution Effect (SE) & Income Effect (IE)

*Substitution Effect From a wage change*

$w \uparrow \rightarrow l \downarrow \rightarrow h \uparrow$ : *Leisure More Expensive*

$w \downarrow \rightarrow l \uparrow \rightarrow h \downarrow$ : *Leisure Less Expensive*

# Clash of SE and IE

$w \uparrow$  *Leisure Normal Good*

*Substitution Effect*  $>$  *Income Effect*  $\rightarrow l \downarrow \rightarrow h \uparrow$

*Substitution Effect*  $=$  *Income Effect*  $\rightarrow l$  *unchanged*  $\rightarrow h$  *unchanged*

*Substitution Effect*  $<$  *Income Effect*  $\rightarrow l \uparrow \rightarrow h \downarrow$

*Income Effect From a wage change*

$w \uparrow \rightarrow l \uparrow \rightarrow h \downarrow$ : *Leisure Normal Good*

$w \downarrow \rightarrow l \downarrow \rightarrow h \uparrow$ : *Leisure Normal Good*

$w \downarrow$  *Leisure Normal Good*

*Substitution Effect*  $>$  *Income Effect*  $\rightarrow l \uparrow \rightarrow h \downarrow$

*Substitution Effect*  $=$  *Income Effect*  $\rightarrow l$  *unchanged*  $\rightarrow h$  *unchanged*

*Substitution Effect*  $<$  *Income Effect*  $\rightarrow l \downarrow \rightarrow h \uparrow$

$$T = h + l$$

$$pc = wh + V$$

$$U = l^\alpha c^\beta$$

$$\frac{\partial U}{\partial l} = \alpha l^{(\alpha-1)} c^\beta = MU_l$$

$$\frac{\partial U}{\partial c} = \beta l^\alpha c^{(\beta-1)} = MU_c$$

$$\Gamma = U + \lambda[w(T - l) + V - pc]$$

$$\left. \begin{aligned} \frac{\partial \Gamma}{\partial l} &= MU_l - \lambda w = 0 \dots (1) \rightarrow pMU_l = \lambda w \\ \frac{\partial \Gamma}{\partial c} &= MU_c - \lambda p = 0 \dots (2) \rightarrow MU_c = \lambda p \end{aligned} \right\} \rightarrow \frac{\alpha c^*}{\beta l^*} = \frac{w}{p} \dots \dots \dots (4)$$

$$\frac{\partial \Gamma}{\partial \lambda} = 0 \Rightarrow w(T - l^*) + V - pc^* = 0 \dots \dots \dots (3)$$

$l^*$  will give Leisure Demand Function. Using 3 and 4

$$\left. \begin{aligned} pc^* &= w(T - l^*) + V \\ c^* &= \frac{\beta w}{\alpha p} l^* \end{aligned} \right\} p \frac{\beta w}{\alpha p} l^* = w(T - l^*) + V = wT + V - wl^*$$

$$l^* = \frac{(wT + V)}{w \left(1 + \frac{\beta}{\alpha}\right)} = \frac{T}{\left(1 + \frac{\beta}{\alpha}\right)} + \frac{V}{w \left(1 + \frac{\beta}{\alpha}\right)}$$

$$l^* = \frac{(wT + V)}{w\left(1 + \frac{\beta}{\alpha}\right)} = \frac{T}{\left(1 + \frac{\beta}{\alpha}\right)} + \frac{V}{w\left(1 + \frac{\beta}{\alpha}\right)}$$

$$c^* = \frac{\beta w}{\alpha p} \left[ \left( \frac{T}{1 + \frac{\beta}{\alpha}} \right) + \frac{V}{w\left(1 + \frac{\beta}{\alpha}\right)} \right]$$

$$U^* = l^{*\alpha} c^{*\beta}$$

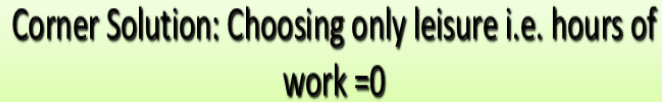
$h^* = T - l^*$  will give Labor Supply Function.

$$h^* = T - l^* = T - \frac{(wT + V)}{w\left(1 + \frac{\beta}{\alpha}\right)} = T - \frac{T}{\left(1 + \frac{\beta}{\alpha}\right)} - \frac{V}{w\left(1 + \frac{\beta}{\alpha}\right)}$$

$$\frac{\partial h^*}{\partial w} = \frac{V}{w^2\left(1 + \frac{\beta}{\alpha}\right)} > 0$$

$$\varepsilon^s = \frac{w}{h^*} \frac{\partial h^*}{\partial w} = \frac{w}{h^*} \times \frac{V}{w^2\left(1 + \frac{\beta}{\alpha}\right)} > 0$$

# Detail



**OR**

$$Or, \frac{MU_l}{w} > \frac{MU_c}{p}$$

# All Play No Work

$$l^* = T_{\dots\dots\dots}(3)$$

$$h^* = T - l^* = 0..(4)$$

$$c^* = V_{\dots\dots\dots\dots\dots\dots}(5)$$

$$U^* = \left(l^*\right)^{\alpha} \times \left(c^*\right)^{\beta}$$

$$U^* = T^\alpha V^\beta ....(6)$$

# Interior solutions with Different Preference Parameters

$$l^* = \frac{(wT + V)}{(1 + \frac{\beta}{\alpha})w} .....(3)$$

$$h^* = T - l^* = T - \frac{(wT + V)}{(1 + \frac{\beta}{\alpha})w}$$

$$h^* = T - \frac{T}{(1 + \frac{\beta}{\alpha})} - \frac{V}{(1 + \frac{\beta}{\alpha})w} ..(4)$$

$$c^* = \frac{(wT + V)}{p} - \frac{w}{p}l^* .....(5)$$

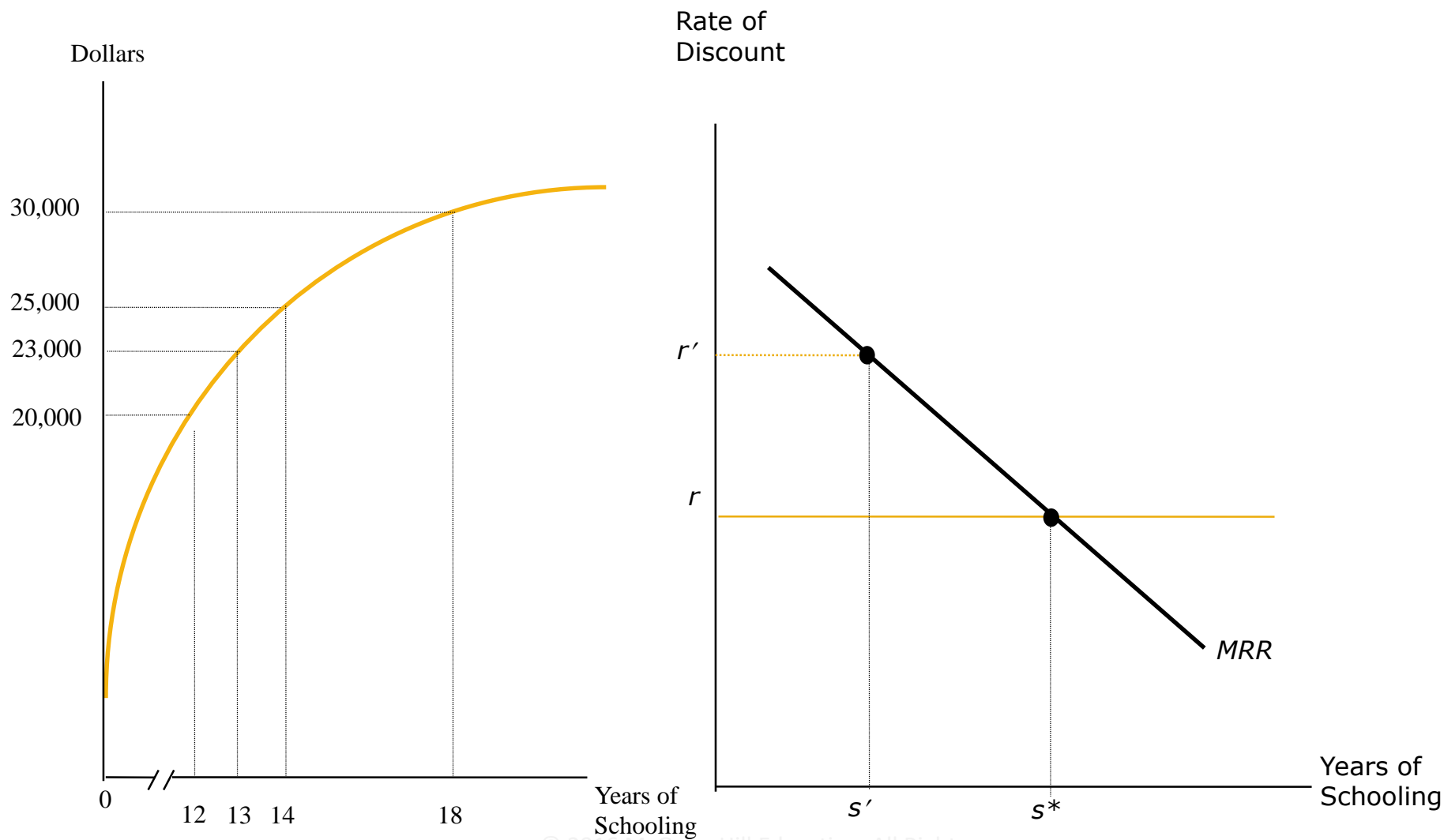
$$U^* = (l^*)^\alpha \times (c^*)^\beta .....(6)$$

	Basel ine	Ca se 1	Cas e 2	Cas e3		Basel ine	Ca se 1	Cas e 2	Cas e3
Alpha	0.5	0.5	0.5	0.5	Alpha	0.5	0.5	0.5	0.5
Beta	0.5	0.5	0.5	0.5	Beta	1	1	1	1
w	20	40	10	20	w	20	40	10	20
p	1	1	1	1	p	1	1	1	1
v	0	0	0	100	v	0	0	0	100
T	110	110	110	110	T	110	110	110	110
l*	?	?	?	?	l*	?	?	?	?
h*	?	?	?	?	h*	?	?	?	?
c*	?	?	?	?	c*	?	?	?	?
U*	?	?	?	?	U*	?	?	?	?

# Policy Question: Returns to Education: Human Capital/ Signaling

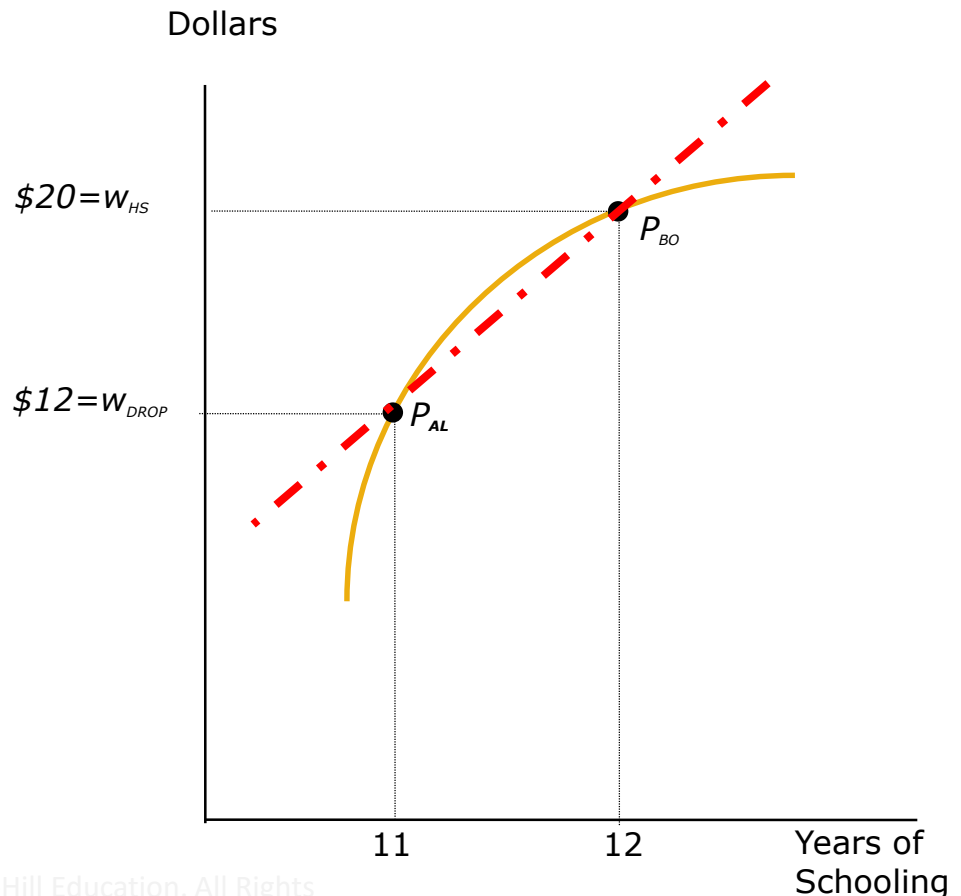
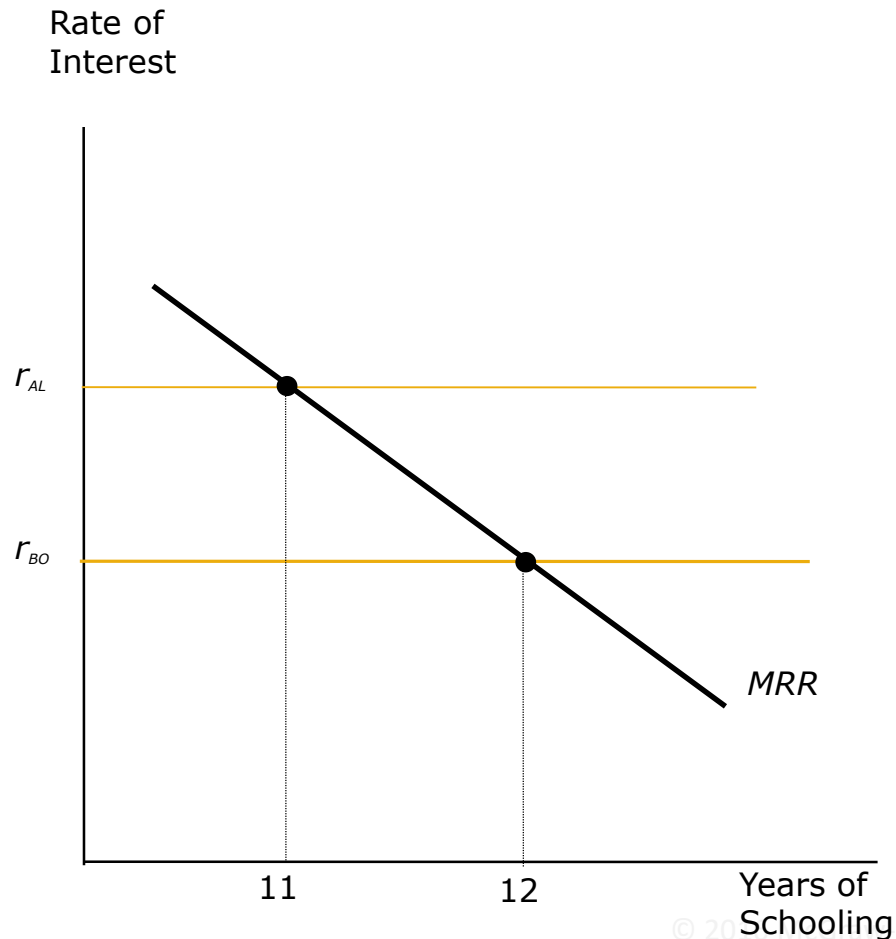
If your years of schooling increases by 1 unit how much does your per hour wage increase?

# Schooling Model: The Wage-Schooling Locus & its slope [Marginal Rate of Return (MRR)]

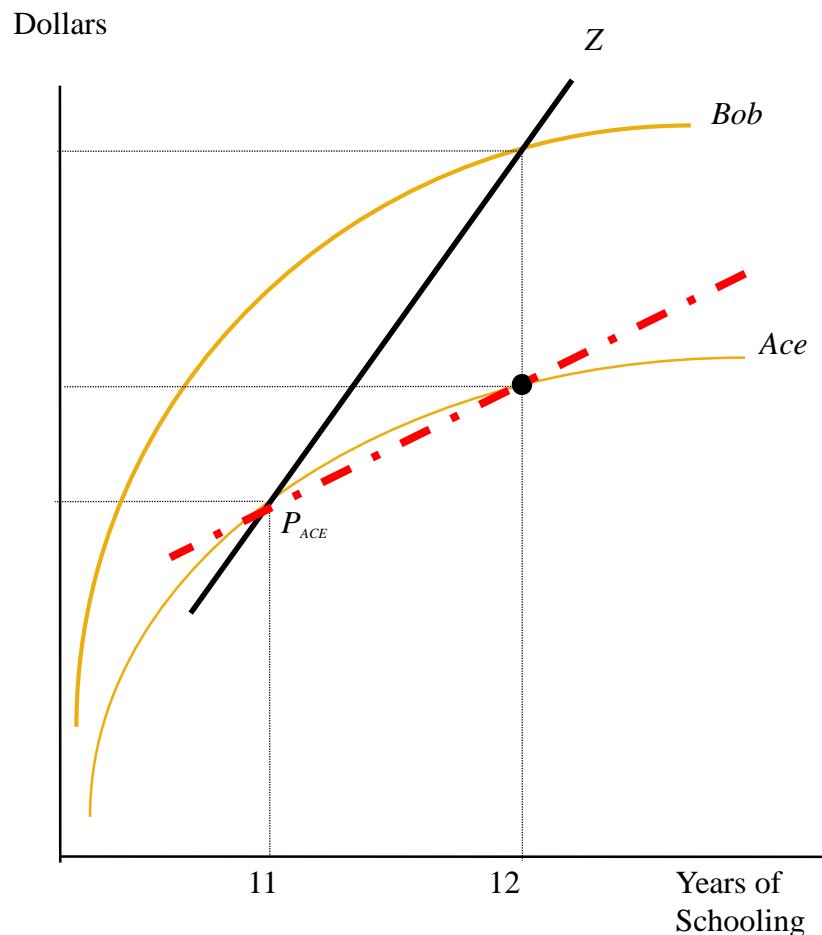
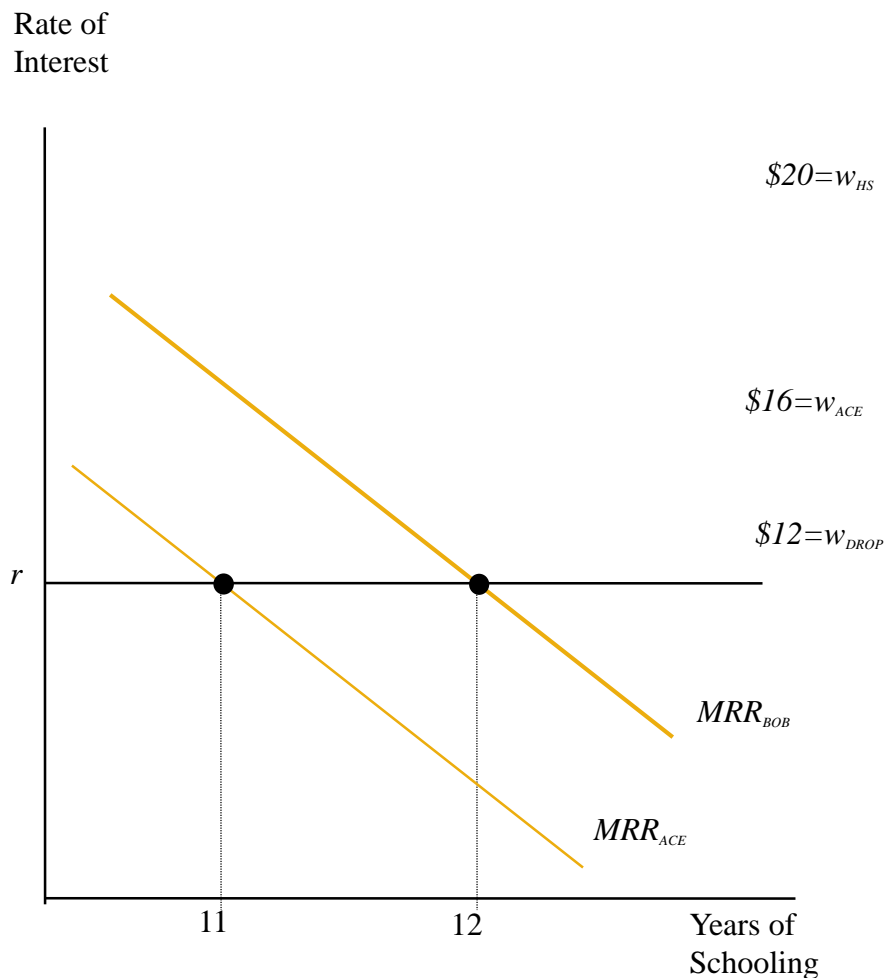




# Schooling and Earnings When Workers Have Different Rates of Discount (what do discount rates depend on?)



# Schooling and Earnings When Workers Have Different Abilities (what is ability?)



# Consequences of Ability Bias

- The extent to which unobserved ability differences exist affects estimates on returns to schooling, since the ability difference may be the true source of the wage differential.
- Suppose high school grads earn \$15,000 more than high school dropouts. Should government fund programs for high school completion? Appears that program may “pay for itself” (erroneous perception)

# Today's Paper: Vive la Re'volution

Table 1  
Descriptive Statistics

Variable	Mean	Standard Deviation
Cohort dummy:		
1946	.128	.33
1947	.140	.35
1948	.145	.35
1949	.148	.35
1950	.145	.35
1951	.145	.35
1952	.148	.35
Education dummy:		
Less than <i>baccalauréat</i>	.718	.45
<i>Baccalauréat</i> only	.096	.29
University diploma ( <i>bac</i> + 2)	.074	.26
University degree	.111	.31
Years of higher education	1.440	2.47
Wage (log)	9.170	.49
Middle-class family background	.246	.43
N	26,371	26,371

SOURCE.—Labor Force Survey 1990, 1993, 1996, and 1999.

NOTE.—Sample is male wage earners born between 1946 and 1952.

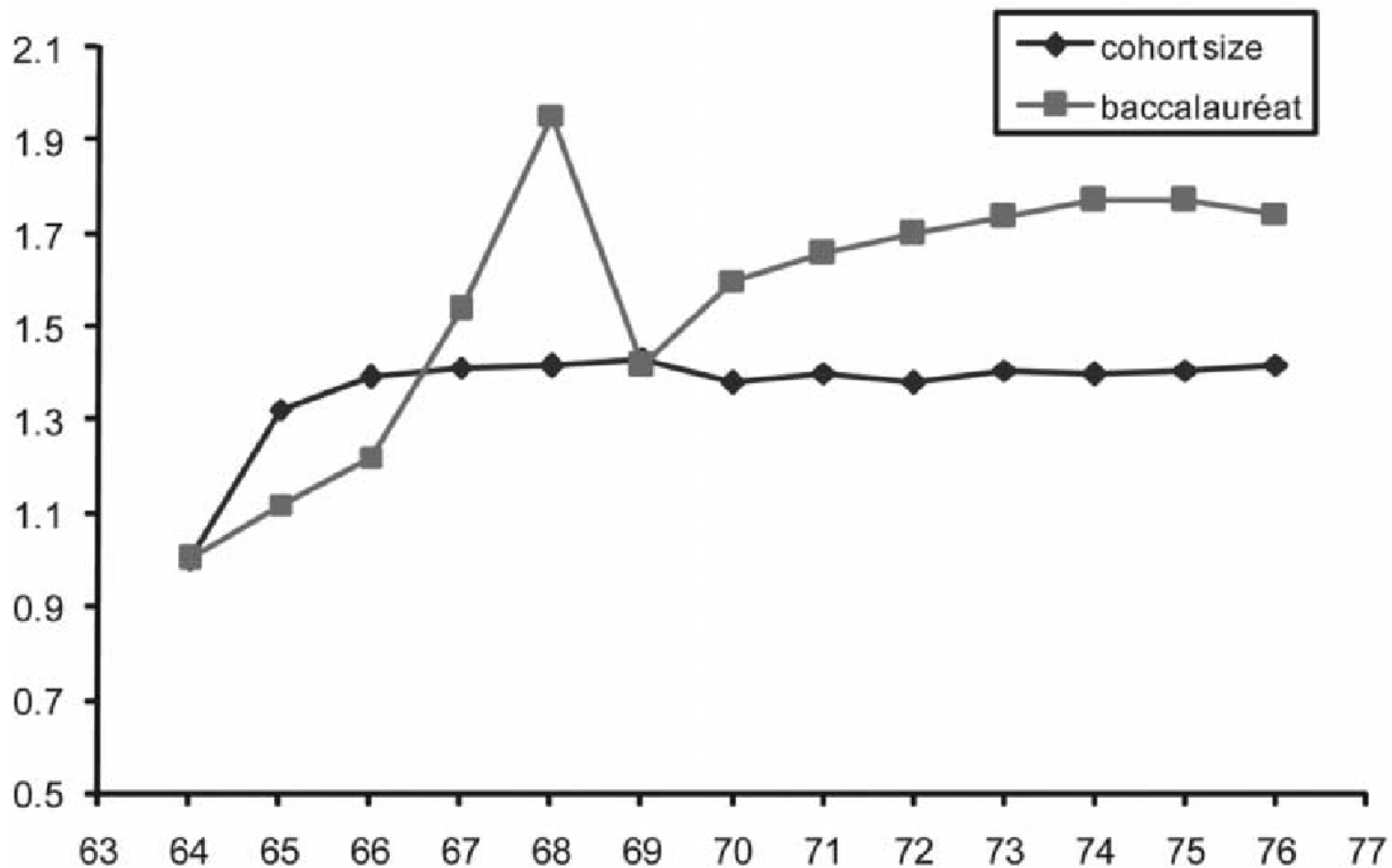


FIG. 1.—Trends in the number of *bacheliers* and in cohort size. The size of the cohort for year  $t$  corresponds to the number of persons born at  $t - 19$  (19 is the median age of candidates). The two series are normalized to one in 1945. Source: French Ministry of Education (number of *bacheliers*) and the French Statistical Office (cohort size).

Table 2

## Distribution of Education across Male Workers, by Year of Birth (%)

	<i>Baccalauréat</i> Only (1)	Greater than <i>Baccalauréat</i>		
		All (2)	Diploma ( <i>Bac</i> + 2) (3)	Degree+ (> <i>Bac</i> + 2) (4)
1946	9.9 (.4)	17.4 (.6)	6.3 (.3)	11.0 (.5)
1947	9.0 (.4)	18.8 (.6)	7.1 (.4)	11.8 (.5)
1948	9.1 (.4)	19.0 (.6)	6.9 (.4)	12.1 (.5)
1949	9.8 (.4)	20.3 (.6)	8.6 (.4)	11.6 (.5)
1950	9.8 (.4)	18.4 (.6)	8.0 (.4)	10.4 (.5)
1951	9.8 (.4)	17.9 (.6)	7.5 (.4)	10.4 (.5)
1952	9.8 (.4)	17.8 (.6)	7.3 (.4)	10.4 (.5)

SOURCE.—Labor Force Survey 1990, 1993, 1996, and 1999.

NOTE.—Sample is male wage earners. Standard deviation is in parentheses.

# IV 1: Birth Cohorts

- 1949 birth cohorts were the treatment cohorts
- In 1968 the affected cohort should be 19 years old (repeating class in secondary education system is pretty common)
- In our analysis we choose 1946 and 1952 as comparison cohorts as they are less likely to be affected by the relaxation of examination standards in 1968

**Table 4**  
**Impact of Birth Cohort on the Education and Labor Market Outcomes of Male Workers**

	<i>Baccalauréat</i> Only (1)	At Least University Diploma ( <i>Bac</i> + 2 or More) (2)	At Least University Degree ( <i>Bac</i> + 3) (3)	Years of Higher Education (4)	Log Wage (5)	<i>Cadre</i> (Up- per-White- Collar Occupation) (6)
1947	−.009 (.006)	.014 (.008)	.008 (.006)	.060 (.050)	.006 (.010)	.001 (.008)
1948	.007 (.006)	.015 (.008)	.012 (.006)	.080 (.050)	.031 (.010)	.008 (.008)
1949	−.001 (.006)	.027 (.008)	.009 (.006)	.150 (.050)	.021 (.010)	.016 (.008)
1950	−.001 (.006)	.008 (.008)	−.002 (.006)	.030 (.050)	.005 (.010)	.000 (.008)
1951	−.005 (.006)	.002 (.008)	−.001 (.006)	.010 (.050)	.003 (.010)	.003 (.008)
Trend	−.000 (.001)	.001 (.008)	−.001 (.001)	.005 (.010)	.010 (.002)	−.005 (.001)
Age	−.000 (.001)	.001 (.008)	.000 (.001)	.004 (.005)	.023 (.001)	.003 (.001)
N	26,370	26,370	26,370	26,370	26,370	26,370

SOURCE.—Labor Force Survey 1990, 1993, 1996, and 1999.

NOTE.—Sample is male wage earners born between 1946 and 1952. Coefficients for the worker's cohort dummy are relative to the comparison cohorts of 1946 and 1952. Standard deviation is in parentheses.