Thesis Proposal

Predictive Modeling with Imbalanced Data

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Introduction

The misuse of opioids

- start with opioid problem
- how much increase in opioid use
- how need to identify patients at increased risk is immediate
- this presents a statistical problem in classifying patients when identifying a rare outcome
- cite some other issues in health with rare outcomes and what people have done
- give fair bit of background (stats in medical, etc) find where people try to predict rare outcomes
- hopefully no ones done exactly what we've done
- no one's explored the tradeoffs of cut-points and sampling, what we've sought to do in order to achieve best prediction
- last paragraph, we sought to identity patients at risk for COT at a safety hospital at Denver, predictive performance, few sentences on what we're doing and what methods and dataset

Predictive modeling with imbalanced data has been found to have report low sensitivity (reference?). To combat this issue of overlooking many true positives,

Methods

Data

To illustrate this issue, we are using electronic health record data from Denver Health from the years 2008 to 2014 of patients for patients with chronic opioid therapy (COT). This is an urban, safety-net hospital. Five percent of the 27,705 patients were reported with the outcome, which was defined as receipt of \geq 90-day supply of opioids with < 30-day gap in supply over a 180-day period or receipt of \geq 10 opioid prescriptions over one year. The data also contained demographic information on the patient including age, race, gender, history of chronic pain, and length of hospital stay.

Statistical Methods

The analysis was done in RStudio version 1.1.383. We used a roughly 2/3rd temporal split of the data to create training and testing datasets, where years 2008-2011 were used to train (65%), and 2012-2014 were used to test (35%).

The model used for this analysis was cross validated lasso regression. This was chosen as it has been found to perform better predictor selection than stepwise selection (reference on this?), and as we were not interested in having interpretable coefficients.

The predictors were first narrowed from 50 to 35 based on clinical relevance.

We first evaluated the prediction performance of the dataset without sampling to see the effects of the imbalanced data on the accuracy, sensitivity, and specificity. This was to serve as a baseline to compare with the techniques available to mitigate the issue of poor sensitivity. The predicted probability cut-point used here was rounding at the standard 0.5 that would be appropriate in balanced datasets.

The first approach used to improve performance was to choose a more informed probability cut-point for the data. This was done using the Youden Index, which finds the maximum of the receiver operating characteristic (ROC) curve (reference here!) with the pROC package.

The second approach was through sampling the dataset. Three types of sampling methods were compared—down sampling, up sampling, and Synthetic Minority Over-sampling Technique (SMOTE). Down sampling takes a random sample from the majority class, in this case those who are not classified as having chronic opioid therapy, in order to match the size of the minority class (reference?). Up sampling does the reverse to take random samples of the minority class in order to match the majority (reference?). SMOTE combines sampling both from the majority and minority, but instead of taking identical copies of the minority it creates synthetic observations using nearest neighbors (reference). For each of the three sampling techniques, the standard 0.5 probability cut-point was used, and the cut-point was optimized using the Youden Index for comparison.

Results

As expected, without using an optimized cut-point or sampling technique, the sensitivity of the model was extremely poor at 8%, with high specificity and accuracy (99% and 96%). Simply choosing a more informed probability cut-point to 0.043 instead of 0.5 improved the sensitivity to 85% and brought the specificity down to 73%. This cut-point is intuitive as the outcome is present at 5% in the dataset, which would be consistent with a 0.5 cutoff in a evenly split dataset. The up and down sampled datasets both showed the same improved sensitivity with probability cut-points at about 0.4, also with close specificities of 74 and 73%. SMOTE on the other hand, resulted in 74% sensitivity and 84% specificity. However, there were improvements in accuracy for SMOTE at 86% as compared to the other three approaches, which had accuracies at 86-87%.

There was no change to the negative predicted value across the approaches, and a decrease in positive predicted value. In terms of the ROC analysis, the area under of the curve for each approach was about the same at 86-87%. See Table 2 for full results for the cut-point, sensitivity, specificity, accuracy, negative predicted value, positive predicted value, and area under the curve.

Discussion

sampling gives a case control in your data and I think should give fewer variables—checked, does not. there are more vars for the sampling cases (by 2 or 3)*

trade offs to discuss with physician, at what point do the sens, spec need to be

Across the different samples, we saw similar improvements for sensitivity.

Conclusions

Both sampling and optimizing probability cutpoints, alone and combined, improved the predicted sensitivity drastically. There was not a distinguishable difference between over and under sampling for either approach, while the SMOTE algorithm appeared to give lower sensitivity than the other two sampling techniques. In addition, using the Youden index resulted in very similiar results as to when the Youden index was used in conjuction with sampling. This may suggest that using both sampling and an informed cut-point at the same time is not necessary, since equivalent predictive performance is seen with the Youden index alone.

Moreover, the decision as to what approach to use is largely influenced by the circumstances of the problem. In some cases it may be more important to have a higher sensitivity than specificy, or vice versa. It may come down to the clinician's decision to have a threshold of sensitivity that is needed. As it can be a case by case choice with many tradeoffs, no one method is recommended above the others.

To expland upon this analysis, we plan to implement a simulation that explores predictive performance of these models at different rarities for the outcome. This is to get a better idea of how they perform in other cirmunstances as well as see when these techniques are no longer needed because the imbalance does not affect model performance. We also plan to implement bootstrap aggregating, also known as bagging. This model averaging approach will hopefully improve the stability and accuracy of our models. Lastly, other sampling or optimzed probability cut-point techniques that are found to be promising may be incorporated into the analysis.

| Data | Threshold | Tab. Specificity | <u>le 1: Result</u> Sensitivity | $\frac{\mathrm{S}}{\mathrm{NPV}}$ | PPV | Accuracy | AUC | Covariates |
|------------------|-----------|------------------|------------------------------------|-----------------------------------|-----|----------|-----|------------|
| Unsampled 0.5 | 0.5 | 99 | 8 | 96 | 35 | 96 | 86 | 31 |
| Unsampled | 0.043 | 73 | 85 | 99 | 12 | 73 | 86 | 31 |
| Down sampled 0.5 | 0.5 | 81 | 75 | 99 | 15 | 81 | 86 | 34 |
| Down sampled | 0.401 | 73 | 85 | 99 | 12 | 74 | 86 | 34 |
| Up sampled 0.5 | 0.5 | 82 | 75 | 99 | 15 | 82 | 87 | 34 |
| Up sampled | 0.399 | 74 | 85 | 99 | 12 | 74 | 87 | 34 |
| SMOTE 0.5 | 0.5 | 86 | 71 | 99 | 17 | 85 | 86 | 33 |
| SMOTE | 0.472 | 84 | 74 | 99 | 17 | 84 | 86 | 33 |

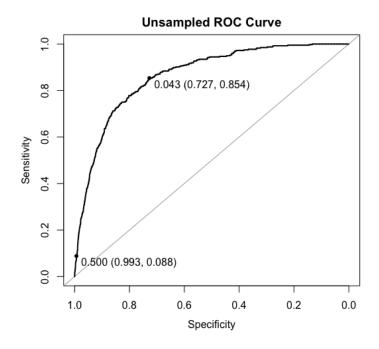


Figure 1: ROC for Unsampled Data: Younden and $0.5~\mathrm{cutoffs}$

References

 $\operatorname{ROC},$ Youden, SMOTE, LASSO, cross-validation Chronic Opioid Therapy, up-sampling, down-sampling

A Statistical Model for Prediction of Future Chronic Opioid Use among Hospitalized Patients

Appendix

| | | Chronic Opioid Use | | P- Value |
|---------------------------------------|------------|-----------------------|--------------|-------------|
| | Total | Yes | No | |
| | (N=27,705) | (N=1,457) | (N=26,248) | |
| Gender, n (%) | , | , | , | |
| Female | 12,933 | 652(44.7) | 12,281 | 0.13 |
| | (46.7) | , , | (46.8) | |
| Race, n (%) | | | | |
| Hispanic | 10,798 | 580 (39.8) | 10,218 | 0.01 |
| | (39.0) | | (38.9) | |
| Non-Hispanic White | 10,645 | 555 (38.1) | 10,090 | |
| | (38.4) | , , | (38.4) | |
| African American | 4,842 | 273 (18.7) | 4,569 (17.4) | |
| | (17.5) | , , | | |
| Other or Unknown | 1,420 | 49 (3.4) | 1,371(5.2) | |
| | (5.1) | , | , , , | |
| Age at Index Admission (Years), n (%) | , | | | |
| 15-<35 | 6,017 | 150 (10.3) | 5,867 (22.4) | < 0.000 |
| | (21.7) | , | , , , | |
| 35-<45 | 4,734 | 267 (18.3) | 4,467 (17.0) | |
| | (17.1) | , | , , , | |
| 45-<55 | 6,919 | 506 (34.7) | 6,413 (24.4) | |
| | (25.0) | , | , , , | |
| 55-<65 | 5,880 | 400 (27.5) | 5,480 (20.9) | |
| | (21.2) | , | , , , | |
| 65-<75 | 2,745 | 110 (7.5) | 2,635 (10) | |
| | (9.9) | , | , , , | |
| 75-185 | 1,410 | 24 (1.6) | 1,386 (5.3) | |
| | (5.1) | () | , , , | |
| | , | | | |
| Mean (SD) | 48.1 | 50.2 (11.6) | 48.0 (16.2) | |
| | (16.0) | , | , , | |
| Median (25th, 75th) | 49 (37, | 51 (43, 58) | 49 (36, 59) | |
| , | 59) | , | | |
| Insurance Status, n (%) | , | | | |
| Discount Payment Plan* | 8,499 | 576 (39.5) | 7,923 (30.2) | < 0.000 |
| | (30.7) | , , | | |
| Medicaid | 8,575 | 531 (36.4) | 8,044 (30.6) | |
| | (31.0) | , , | , , | |
| Medicare | 6,260 | 259 (17.8) | 6,001 (22.9) | |
| | (22.6) | ` / | , (') | |

| | | Chronic Opioid Use | | P- Value |
|---|-----------|-----------------------|-----------------|-------------|
| Commercial | 2,402 | 50 (3.4) | 2,352 (9.0) | |
| | (8.7) | , | , , , | |
| Other/Unknown/Self-Pay | 1,969 | 41(2.8) | 1,928 (7.3) | |
| | (7.1) | | | |
| Three Year History of, n (%) | | | | |
| Tobacco Use Disorder | 9,682 | 716 (49.1) | 8,966 (34.2) | < 0.0001 |
| | (34.9) | | | |
| Alcohol Use Disorder | 7,167 | 408 (28.0) | 6,759 (25.8) | 0.06 |
| | (25.9) | | , , | |
| Stimulant Use Disorder | 1,719 | 118 (8.1) | $1,601 \ (6.1)$ | 0.003 |
| | (6.2) | 4.4. (2.0) | 000 (0 1) | 0.40 |
| Opioid Use Disorder | 672 (2.4) | 44 (3.0) | 628 (2.4) | 0.13 |
| Chronic Pain | 14,914 | 1,105 (75.8) | 13,809 | < 0.0001 |
| | (53.8) | , , , | (52.6) | |
| Acute Pain | 10,073 | 611 (41.9) | 9,462 (36.0) | < 0.0001 |
| | (36.4) | , | , , , | |
| | | | | |
| Top 3 Mental Health Disorders, n (%) | | | | |
| Depression | 6,318 | 491 (33.7) | 5,827 (22.2) | < 0.0001 |
| | (22.8) | | | |
| Anxiety Disorder | 3,677 | 265 (18.2) | 3,412 (13.0) | < 0.0001 |
| | (13.3) | | | |
| Bipolar Disorder | 2,362 | 135 (9.3) | 2,227 (8.5) | 0.3 |
| | (8.5) | | | |
| Any Mental Health Disorder n (%) | 9,805 | 634 (43.5) | 9,171 (34.9) | < 0.0001 |
| Tilly Wichtai Health Disorder if (70) | (35.4) | 004 (40.0) | 3,111 (34.3) | <0.0001 |
| | (00.1) | | | |
| Top 3 Chronic Medical Conditions, n | | | | |
| (%) | | | | |
| Hypertension | 11,799 | 773 (53.1) | 11,026 | < 0.0001 |
| | (42.6) | | (42.0) | |
| Respiratory Disease | 7,060 | 444 (30.5) | 6,616 (25.2) | < 0.0001 |
| | (25.5) | | | |
| Diabetes Mellitus | 5,701 | 376 (25.8) | 5,325 (20.3) | < 0.0001 |
| | (20.6) | | | |
| Any Chronic Medical Condition, n (%) | 17,535 | 1,102 (75.6) | 16,433 | < 0.0001 |
| Tiny Ontoine Medical Condition, if (70) | (63.3) | 1,102 (10.0) | (62.6) | <0.0001 |
| Charlson Comorbidity Index from 3 | (00.0) | | (02.0) | |
| Year Diagnosis History | | | | |
| Tour Diagnoon innovy | | | | |

| $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | | | Chronic Opioid Use | | P- Value |
|--|--|-----------|-----------------------|--------------|-------------|
| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | Mean (SD) | 1.9 (2.2) | 2.4 (2.5) | 1.9 (2.2) | < 0.0001 |
| Discharge Diagnoses, n (%) Chronic Pain | , | | , , | ` ' | |
| $\begin{array}{c} \text{Chronic Pain} \\ \text{Cardiovascular System} \\ Patients Who Had Surgical Procedures in the One Year Preceding the Month of the M$ | | (| (, , | | |
| Acute Painf 4,586 255 (17.5) 4,331 (16.5) 0.35 (16.6) Neoplasm | | 8,346 | 729 (50.0) | 7,617 (29.0) | < 0.0001 |
| Neoplasm $\begin{tabular}{ l l l l l l l l l l l l l l l l l l l$ | | (30.1) | , , | | |
| Neoplasm 1,447 | Acute Painŕ | 4,586 | 255 (17.5) | 4,331 (16.5) | 0.32 |
| Top 3 Surgical Procedures During Initial Hospitalization, n (%) Digestive System 3,437 (12.4) Musculoskeletal System 3,037 (11.0) Cardiovascular System 2,312 (8.3) Patients Who Had Surgical Procedure During Index Hospitalization, n (%) Number of Healthcare Encounters in the One Year Preceding the Index Admission, n (%) 2,3280 (84.0) 1,196 (82.1) 2,2084 (84.1) 1,196 (82.1) 2,2084 (84.1) 1,196 (82.1) 2,2084 (84.1) 1,196 (82.1) 2,155 (8.2) 2,155 (8 | | (16.6) | | | |
| Initial Hospitalization, n (%) Digestive System 3,437 225 (15.4) 3,212 (12.2) <0. (12.4) Musculoskeletal System 3,037 258 (17.7) 2,779 (10.6) <0. (11.0) Cardiovascular System 2,312 (8.3) Patients Who Had Surgical Procedure (8.3) Total (9.4) (39.5) (39.1) Number of Healthcare Encounters in the One Year Preceding the Index Admission, n (%) (84.0) (84.1) 1 3,413 197 (13.5) 3,216 (12.3) (12.3) 2+ 1,012 64 (4.4) 948 (3.6) | Veoplasm ¤ | • | 170 (11.7) | 1,277 (4.9) | < 0.0001 |
| Digestive System 3,437 (12.4) 225 (15.4) 3,212 (12.2) <0.00 (12.4) | Op 3 Surgical Procedures During | | | | |
| Musculoskeletal System (12.4) Musculoskeletal System (3.037 (11.0) Cardiovascular System (2.312 (8.3) Patients Who Had Surgical Procedure (8.3) 700 (48.0) 10,256 (39.1) Number of Healthcare Encounters in the One Year Preceding the Index Admission, n (%) 23,280 (84.0) 1,196 (82.1) 22,084 (84.1) 1 3,413 (12.3) 2+ 1,012 64 (4.4) 948 (3.6) | nitial Hospitalization, n (%) | | | | |
| Musculoskeletal System 3,037 (11.0) 258 (17.7) 2,779 (10.6) <0.00 | Digestive System | 3,437 | 225 (15.4) | 3,212 (12.2) | < 0.001 |
| Cardiovascular System (11.0) 2,312 (8.3) Patients Who Had Surgical Procedure During Index Hospitalization, n (%) Number of Healthcare Encounters in the One Year Preceding the Index Admission, n (%) 23,280 (84.0) 1,196 (82.1) 22,084 (84.1) 1 3,413 197 (13.5) 3,216 (12.3) (12.3) 2+ 1,012 64 (4.4) 948 (3.6) | | (12.4) | | | |
| Cardiovascular System 2,312 (8.3) Patients Who Had Surgical Procedure During Index Hospitalization, n (%) Number of Healthcare Encounters in the One Year Preceding the Index Admission, n (%) 2,312 (8.3) 700 (48.0) 10,256 (39.1) Number of Healthcare Encounters in the One Year Preceding the Index Admission, n (%) 23,280 (84.0) (84.1) 1 3,413 197 (13.5) 3,216 (12.3) (12.3) 2+ 1,012 64 (4.4) 948 (3.6) | Ausculoskeletal System | <i>'</i> | 258 (17.7) | 2,779 (10.6) | < 0.0001 |
| Patients Who Had Surgical Procedure 10,956 700 (48.0) 10,256 (39.1) Number of Healthcare Encounters in the One Year Preceding the Index Admission, n (%) 23,280 1,196 (82.1) 22,084 0.03 (84.0) 1 3,413 197 (13.5) 3,216 (12.3) (12.3) 2+ 1,012 64 (4.4) 948 (3.6) | Cardiovascular System | | 157 (10.8) | 2,155 (8.2) | < 0.001 |
| During Index Hospitalization, n (%) (39.5) (39.1) Number of Healthcare Encounters in the One Year Preceding the Index Admission, n (%) (23,280 1,196 (82.1) 22,084 0.03 (84.0) (84.1) 1 3,413 197 (13.5) 3,216 (12.3) (12.3) 2+ 1,012 64 (4.4) 948 (3.6) | , and the second | (8.3) | , , | | |
| During Index Hospitalization, n (%) (39.5) (39.1) Number of Healthcare Encounters in the One Year Preceding the Index Admission, n (%) (23,280 1,196 (82.1) 22,084 0.03 (84.0) (84.1) 1 3,413 197 (13.5) 3,216 (12.3) (12.3) 2+ 1,012 64 (4.4) 948 (3.6) | Patients Who Had Surgical Procedure | 10,956 | 700 (48.0) | 10,256 | < 0.0001 |
| the One Year Preceding the Index Admission, n (%) $\begin{array}{cccccccccccccccccccccccccccccccccccc$ | _ | * | , | | |
| Admission, n (%) 0 23,280 1,196 (82.1) 22,084 0.03 (84.0) (84.1) 1 3,413 197 (13.5) 3,216 (12.3) (12.3) 2+ 1,012 64 (4.4) 948 (3.6) | Number of Healthcare Encounters in | , | | , | |
| 0 23,280 1,196 (82.1) 22,084 0.03 (84.0) (84.1) 1 3,413 197 (13.5) 3,216 (12.3) (12.3) 2+ 1,012 64 (4.4) 948 (3.6) | he One Year Preceding the Index | | | | |
| (84.0) (84.1) 1 3,413 197 (13.5) 3,216 (12.3) (12.3) 2+ 1,012 64 (4.4) 948 (3.6) | Admission, n (%) | | | | |
| 1 3,413 197 (13.5) 3,216 (12.3) (12.3) 2+ 1,012 64 (4.4) 948 (3.6) | ı | 23,280 | 1,196 (82.1) | 22,084 | 0.03 |
| (12.3) 2+ 1,012 64 (4.4) 948 (3.6) | | (84.0) | | , , | |
| 2+ 1,012 64 (4.4) 948 (3.6) | | • | 197 (13.5) | 3,216 (12.3) | |
| | | , | | | |
| (3.7) | + | • | 64 (4.4) | 948 (3.6) | |
| | | (3.7) | | | |
| | (ap) | 0.0 (0.0) | 0.0 (0.7) | 0.2 (0.0) | |
| Mean (SD) $0.2 (0.6) 0.2 (0.7) 0.2 (0.6)$ | , | ` / | \ / | ` / | |
| Median (25th, 75th) $0.0 (0, 0) 0.0 (0, 0) 0.0 (0, 0)$ | , | | | | -0.0001 |
| | | • | 227 (15.6) | 1,379 (5.3) | < 0.0001 |
| (%) (5.8) | , | (5.8) | | | |
| Past Year Receipt of Non-Opioid Analgesics (NSAIDs, neuropathic | | | | | |
| agents, topical capsaicin & lidocaine), | | | | | |
| n (%) | | | | | |
| | . (/0) | 4.875 | 620 (42.6) | 4.255 (16.2) | < 0.0001 |
| (17.6) 	 (12.0) 	 1,255 	 (10.2) 	 < 0. | | • | 0=0 (1=.0) | -, (10.2) | 10.0001 |
| Past Year Number of Opioid | Past Year Number of Opioid | (=) | | | |
| Prescriptions Filled, n (%) | - | | | | |

| | | Chronic | | P- |
|---------------------------------------|-----------|-------------|--------------|---------|
| | | Opioid Use | | Value |
| 0 | 21,543 | 549 (37.7) | 20,994 | < 0.000 |
| | (77.8) | | (80.0) | |
| 1 | 3,167 | 249(17.1) | 2,918 (11.1) | |
| | (11.7) | | | |
| 2 | 1,331 | 197(13.5) | 1,134(4.3) | |
| | (4.8) | | | |
| 3 | 646 (2.3) | 132(9.1) | 514(2.0) | |
| 9-Apr | 1,018 | 330 (22.6) | 688 (2.6) | |
| - | (3.7) | , | , | |
| Receipt of Opioid at Discharge, n (%) | 8,028 | 817 (56.1) | 7,211 (27.5) | < 0.000 |
| | (29.0) | , | , , , | |
| Milligrams of Morphine Per Hospital | , | | | |
| Day, n (%) | | | | |
| 0 | 9,655 | 189 (13.0) | 9,466 (36.1) | < 0.000 |
| | (34.8) | () | , , , | |
| 0.01 < 10 | 3,320 | 108 (7.4) | 3,212 (12.2) | |
| | (12.0) | | -) () | |
| 10 < 51 | 7,337 | 490 (33.6) | 6,847 (26.1) | |
| | (26.5) | | 0,010 (1011) | |
| 51 < 100 | 4,413 | 371 (25.5) | 4,042 (15.4) | |
| 01 (100 | (15.) | 3.1 (23.3) | 1,012 (1011) | |
| 100+ | 2,980 | 299 (20.5) | 2,681 (10.2) | |
| 100 | (10.8%) | 200 (20.0) | 2,001 (10.2) | |
| | (10.070) | | | |
| Mean (SD) | 37.7 | 64.4 (76.7) | 36.2 (64.4) | |
| Wicker (SD) | (65.4) | 01.1 (10.1) | 00.2 (01.1) | |
| Median (25th, 75th) | 12.5 (0, | 45.5 (14.3, | 10.8 (0, | |
| Wiedian (2001) | 54.7) | 90.2) | 52.2) | |
| Length of Hospital Stay (days) | 01.1) | 30.2) | 02.2) | |
| 1 | 8,449 | 383 (26.3) | 8,066 (30.7) | 0.0003 |
| 1 | (30.0) | 303 (20.3) | 0,000 (30.1) | 0.0003 |
| 2 | 5,655 | 282 (19.4) | 5,373 (20.5) | |
| 2 | (20.4) | 202 (19.4) | 5,575 (20.5) | |
| 5-Mar | 7,801 | 450 (30.9) | 7,351 (28.0) | |
| J-Mai | / | 450 (50.9) | 7,331 (28.0) | |
| <i>C</i> . | (28.2) | 240 (92 5) | T 4TO (00 0) | |
| 6+ | 5,800 | 342 (23.5) | 5,458 (20.8) | |
| | (20.9) | | | |
| Maray (CD) | 47 (0.0) | 40 (77) | 16 (01) | |
| Mean (SD) | 4.7 (9.0) | \ / | 4.6 (9.1) | |
| Median (25th, 75th) | 2(1, 5) | 3(1, 5) | 2(1, 5) | |

| | | Chronic Opioid Use | | P- Value |
|---|----|-----------------------|------------|-------------|
| Number of Subsequent Hospitalizations within 12 Months | | | | < 0.001 |
| post Hospital Discharge | | | | |
| Mean (SD) | NA | 1.48(2.20) | 0.54(1.21) | |
| Median (25th, 75th) | NA | 1 (0,2) | 0 (0,1) | |