Research highlights

We provided a computational model of the development of word-pair learning skills.

The model characterizes this development in terms of a continuous process operating over similar representations across the lifespan.

We used the model to derive novel predictions extending the work of Stager and Werker (1997) and we successfully tested these predictions with both children and adults.

9 Abstract

"Cognitive development is often characterized in terms of discontinuities, but these 10 discontinuities can sometimes be apparent rather than actual and can arise from continuous 11 developmental change. To explore this idea, we use as a case study the finding by Stager and 12 Werker (1997) that children's early ability to distinguish similar sounds does not automatically translate into word learning skills. Early explanations proposed that children may not be able to encode subtle phonetic contrasts when learning novel word meanings, 15 thus suggesting a discontinuous/stage-like pattern of development. However, later work has 16 revealed (e.g., through using more precise testing methods) that children do encode such 17 contrasts, thus favoring a continuous pattern of development. Here we propose a 18 probabilistic model that represents word knowledge in a graded fashion and characterizes 19 developmental change as improvement in the precision of this graded knowledge. Our model 20 explained previous findings in the literature and provided a new prediction — the referents' 21 visual similarity modulates word learning accuracy. The models' predictions were 22 corroborated by human data we collected from both preschool children and adults. The 23 broader impact of this work is to show that computational models, such as ours, can help us explore the extent to which episodes of cognitive development that are typically thought of 25 as discontinuities may emerge from simpler, continuous mechanisms."

Keywords: word learning, cognitive development, computational modeling

27

Continuous developmental change explains discontinuities in word learning

29 Introduction

28

Cognitive development is often characterized in terms of a succession of discontinuous stages. In Piaget's initial conception, these stages cross-cut different aspects of cognition (Piaget, 1954); in more modern conceptions, distinct domains are often thought to progress on their own timeline (e.g., Carey, Zaitchik, & Bascandziev, 2015). Although intuitively appealing, this sort of stage theory can be challenging to integrate with theories of learning, which typically posit that knowledge and skills improve incrementally with experience.

Indeed, one of the central challenges of cognitive development has been to explain transitions between stages which appear to be qualitatively different (Carey, 2009).

Nevertheless, at least in some cases, development may only appear to be stage-like. Some discontinuities may be related to how we measure a specific skill. Other discontinuities may emerge due to statistical thresholding (e.g., an experimental p-value of p < .05 for one age group but not another) which can create a spurious dichotomy between success and failure in observing a given behavior. In such cases, positing discontinuous stages is unnecessary. Instead, a continuous model — involving similar representations across the lifespan — may provide a simpler and more transparent account of development (cf. McMurray, 2007; Shultz, Schmidt, Buckingham, & Mareschal, 1995).

To explore this point computationally, we use a case study from word learning
literature. Stager and Werker (1997) first showed that children's early ability to distinguish
similar sounds does not automatically translate into word learning skills. The authors
measured word learning using an audio-visual habituation Switch task. First, infants are
familiarized with two word-object pairings (e.g., label 1 with object 1 and label 2 with object
2). Second, they are tested using two types of trials. The control "same" trial consists of a
correct pairing (e.g., label 1 with object 1) and the "switch" trial consists of a wrong pairing

(e.g., label 1 with object 2). If babies have correctly learned the association during the
habituation, they are supposed to be surprised by the "switch" trial and not by the "same"
trial. The former should thus result in a greater looking time compared to the latter
(Werker, Cohen, Lloyd, Casasola, & Stager, 1998).

Though infants around 14-month old can distinguish perceptually similar sound pairs such as "dih" and "bih", they appear to fail in mapping this pair to two different objects in the switch task. This failure was initially taken as evidence that 14-month olds do not encode subtle sounds during meaning learning (Pater, Stager, & Werker, 2004; Stager & Werker, 1997). This interpretation suggested a discontinuous/stage-like pattern of development whereby younger children fail to encode the contrastive phonetic detail, whereas older children, around 17 months, typically do (Werker, Fennell, Corcoran, & Stager, 2002).

The initial discontinuous interpretation has been challenged by subsequent work. For instance, Yoshida, Fennell, Swingley, and Werker (2009) investigated whether failure in the Switch task reflects a lack of sound encoding during habituation, or whether it is only due to the nature of the testing method which does not allow learning below a certain threshold to be detected. They used the same habituation procedure as Stager and Werker (1997), but instead of comparing the looking times in "same" and "switch" trials, they tested infants using a two-alternative choice task comparing fixations to target and distractor objects (Fernald, Perfors, & Marchman, 2006; Golinkoff, Hirsh-Pasek, Cauley, & Gordon, 1987).

Using this testing method, researchers found evidence for learning even in 14-month olds.

Another challenge to the discontinuous account of development came from adult studies. If the mismatch between sound discrimination and word learning is only a stage in early infancy, then this mismatch should disappear by adulthood. Nonetheless, even adults show patterns of learning that mirror those shown by 14-month-olds when the sound contrasts are more challenging (Pajak, Creel, & Levy, 2016; White, Yee, Blumstein, & Morgan, 2013).

Some researchers (Pajak et al., 2016; Swingley, 2007; Yoshida et al., 2009) proposed
that word knowledge may not be encoded in a binary fashion, i.e., it is not the case that
children either succeed or fail in encoding minimal contrast when learning the meanings.
Rather, they may be encoding this knowledge in a graded fashion (see Munakata (2001) for
an detailed discussion of a similar view). Thus, development does not so much involve a
qualitative shift (i.e., a sudden emergence of an ability that did not exist before) as much as
it consists in the continuous refinement of initially noisy knowledge.

Many different computational formalisms can represent graded knowledge. Here we use probabilistic models, a formalism that allows both easy examination of internal representations and quantification of the robustness of these representations. Word knowledge can be characterized with a probability distribution over sound instances organized in a similarity space. The probability is highest at the most typical sound instance. It decreases as the instance becomes less typical. The precision of word knowledge can be characterized by whether it tolerates slightly atypical pronunciations. This tolerance is captured formally by the variance of the probability distribution: larger variance indicates higher tolerance and lower precision, whereas smaller variance indicates lower tolerance and higher precision (for an illustration, see Figure 1 top and right panels).

This general framework — in which the precision of word knowledge is characterized with the variance of a probability distribution — can already provide an intuitive way of thinking about several findings. In particular, unlike the binary view, the probabilistic view allows for the possibility of word knowledge being both successful and noisy. This new understanding can provide an account for the fact that children show evidence of learning in some testing condition (e.g., Yoshida et al., 2009) but not in others (e.g., Stager & Werker, 1997) — depending on the precision of the measurement.

In a word-pair learning paradigm, children are supposed to associate one label, e.g., "bih", with object 1 and a second label, e.g., "dih", with object 2. Infants may succeed in

learning both associations. Nevertheless, the variance with which the pair of words are
encoded can still be large, causing their probability distributions to overlap (Figure 1, top).
The way this (noisy) knowledge is probed can lead to different results.

In the Switch task (Stager & Werker, 1997), children are understood to succeed if they 108 reject a wrong association (e.g., "bih" with object 2). However, a large overlap between "bih" 109 and "dih" means that "bih" is itself a plausible mispronunciation of "dih". The wrong 110 association may not be rejected by children because the speaker could have said "bih" but 111 meant "dih". In the two-alternative choice task (Yoshida et al., 2009), children do not have 112 to reject the wrong association; they only need to show a preference, albeit small, for the 113 correct one. Thus, unlike the Switch, this testing method allows us to see subtle evidence of 114 learning even with a large overlap. For example, given the label "bih", children are supposed 115 to pick which object is a better match to this label. Though it is possible that the speaker 116 said "bih" and meant "dih", it is more likely that the speaker both said and meant "bih" — 117 this higher probability leads to a preference for the correct object. 118

In addition to explaining the difference in behavior across the Switch and the 119 preferential looking tasks, the probabilistic account explains difference in behavior within the 120 same task. In particular, when the labels are quite distinct in the perceptual space ("lif" vs. 121 "neem"), the probabilistic distributions do not overlap as much as in the case of 122 similar-sounding words (Figure 1, left). This fact means that the learners will have less 123 tolerance for the wrong association, leading to a successful rejection in the Switch task (as was reported by Stager and Werker (1997) and subsequent studies using the same paradigm). 125 Further, distinctiveness can be enhanced even for minimally different sounds when other cues highlight their difference (Dautriche, Swingley, & Christophe, 2015; Rost & McMurray, 2009, 127 2010; Thiessen, 2007; Yeung & Werker, 2009). 128

In this framework, developmental change can be understood as an increase in the precision (i.e., a decrease in the variance) of the probabilistic knowledge, leading to a lower

overlap between the distributions of similar-sounding words (Figure 1, right). Importantly, a more precise representation still has a non-zero variance. Thus, learning difficulties can still be induced with challenging stimuli or in cognitively demanding situations as was demonstrated in adults studies (Pajak et al., 2016; White et al., 2013).

35 The current study

The probabilistic account has been put forward to explain patterns of learning and development at the qualitative level. However, it is crucial to have a precise computational 137 instantiation of this account which would help us 1) test this theoretical hypothesis more 138 directly and 2) identify the particular parameters that are the locus of developmental change. 139 One previous study attempted to provide such a computational instantiation (Hofer & Levy, 140 2017). However, this previous work was designed with the goal of reproducing the results of 141 a specific study (Pajak et al., 2016) which focused on explaining the mismatch between 142 speech perception and word learning in adults rather than on exploring the mechanism of 143 development.

The present work proposes a model of word-pair learning based on the probabilistic 145 account. We tested the ability of this model to both explain various findings in previous 146 experiments in both children and adults (e.g., the fact that similar words are harder to learn 147 than different words) and to predict new learning patterns that have not been tested before. 148 In particular, we test the prediction that referent similarity (i.e., the confusability of pictures referred to by novel words) should play an identical computational role to word form similarity in predicting recognition difficulty. Although this prediction is intuitive, to our 151 knowledge, it has never been tested. Finally, we explore the extent to which the probabilistic 152 account allows us to understand development in terms of as a continuous refinement in 153 similar representations across the lifespan.

The paper is organized as follows. First, we introduce the model and we explain how it allows us to characterize behavior in a word-pair-learning paradigm. Then we explore the predictions of the model through simulating its behavior across different parameter settings. Next, we quantify the extent to which the model's predictions account for human data we collected from both preschool children and adults. Finally, we discuss the results in the light of existing accounts of word development.

Model Model

52 Probabilistic structure

163

164

165

166

167

168

Our model consists of a set of variables describing the general process of spoken word recognition in a referential situation. These variables are related in a way that reflects the simple generative scenario represented graphically in Figure 2. When a speaker utters a sound in the presence of an object, the observer assumes that the object o activated the concept C in the speaker's mind. The concept prompted the corresponding label L. Finally, the label was physically instantiated by the sound s.

A similar probabilistic structure was used by Lewis and Frank (2013) to model concept learning, and by Hofer and Levy (2017) to model spoken word learning. However, the first study assumed that the sounds are heard unambiguously, and the second assumed the concepts are observed unambiguously. In our model, we assume that both labels and concepts are observed with a certain amount of perceptual noise, which we assume, for simplicity, is captured by a normal distribution:

$$p(o|C) \sim \mathcal{N}(\mu_C, \sigma_C^2)$$
 (1)

and and

$$p(s|L) \sim \mathcal{N}(\mu_L, \sigma_L^2)$$
 (2)

Finally, we assume there to be one-to-one mappings between concepts and labels and that observers have successfully learned these mappings during the exposure phase:

$$P(L_i|C_j) = \begin{cases} 1 & \text{if } i = j\\ 0 & \text{otherwise} \end{cases}$$
 (3)

178 Inference

In our canonical inference case, the learner hears a sound s and has to decide which object o provides an optimal match to this sound (see Figure 3). To this end, they must compute the probability P(o|s) for all possible objects. This probability can be computed by summing over all possible concepts and labels:

$$P(o|s) = \sum_{CL} P(o, C, L|s)$$
(4)

Using the fact that $P(o, C, L|s) = \frac{P(o, C, L, s)}{P(s)}$ and that P(s) does not depend on o, we arrive at the equation:

$$P(o|s) \propto \sum_{C,L} P(o,C,L,s)$$
 (5)

The joint probability P(o, C, L, s) is obtained by factoring the graphical model in Figure 2:

$$P(o, C, L, s) = P(s|L)P(L|C)P(C|o)P(o)$$

Using Bayes' rule, we can rewrite P(C|o) in terms of P(o|C):

$$P(C|o) = \frac{P(o|C)P(C)}{P(o)}$$

By subtituting this term in the expression of the joint distribution P(o, C, L, S) we obtain:

$$P(o, C, L, s) = P(s|L)P(L|C)P(o|C)P(C)$$

Finally, assuming that the concepts' prior probability P(C) is uniformly distributed,¹ we obtain the following expression, where all conditional dependencies are now well defined:

$$P(o|s) \propto \sum_{C,L} P(s|L)P(L|C)P(o|C) \tag{6}$$

192 Task and model predictions

each naming situation in our experiment.

187

We use the model to predict word learning in a task similar to the one introduced by

Stager and Werker (1997). We used a modified version of the task where the testing method

consists in a two-alternative forced-choice (Yoshida et al., 2009). In this task, participants

are first exposed to two different word-object pairings (e.g., "lif" - object 1, "neem" - object

2). The word-object associations are introduced sequentially. After this exposure phase,

participants perform a series of test trials. In each of these trials, one of the two sounds is

11This is a reasonable assumption in our particular case given the similarity of the concept pairs used in

uttered (e.g., "lif") and participants choose the corresponding object from the two alternatives. An overview of the task is shown in Figure 3.

Model 1. From the general expression 6, we derive three exact analytical solutions 201 instantiating different learning assumptions. Recall from expressions 1 and 2 that P(o|C)202 and P(s|L) have parameters σ_C and σ_L , respectively, that control perceptual uncertainty. 203 The first solution is derived by assuming that the labels are recovered from sounds with a 204 certain level of uncertainty $\sigma_L > 0$, but that concepts are unambiguously recovered from the 205 observed objects, i.e., $\sigma_C \to 0$. This assumption has been made — whether implicitly or 206 explicitly — by most previous work in this line of research. For example, in Stager and 207 Werker (1997), the objects were quite dissimilar. Thus, the assumption that they were easily 208 discriminated by infants seems relatively well justified. One important implication of this 209 assumption is that only the similarity of word sounds modulates success in word learning, 210 not the similarity of the referents (as long as these referents are differentiated perceptually). 211 This assumption yields the following probability function: 212

$$P(o_T|s) = \frac{1}{1 + e^{-\frac{\Delta s^2}{2\sigma_L^2}}}$$
 (7)

where $\Delta s = s_2 - s_1$.

213

Model 2. The second solution is derived by making the more general assumption that both the labels and the concepts are recovered with noise from the sounds and objects. We first introduce the simplifying assumption that the label-related uncertainty σ_L and the concept-related uncertainty σ_C are of a similar magnitude, i.e., $\sigma_C \approx \sigma_L = \sigma$. This assumption makes the prediction that the sound similarity and the object similarity impact word learning accuracy in exactly the same way. Furthermore, it allows us to study the behavior of the model with only one free parameter, an important consideration given the small number of datapoints available from any given infant experiment.

229

230

231

232

233

234

235

236

237

$$P(o_T|s) = \frac{1 + e^{-\frac{\Delta s^2 + \Delta o^2}{2\sigma^2}}}{1 + e^{-\frac{\Delta s^2 + \Delta o^2}{2\sigma^2}} + e^{-\frac{\Delta s^2}{2\sigma^2}} + e^{-\frac{\Delta o^2}{2\sigma^2}}}$$
(8)

Model 3. We finally derive the third (and most general) solution which allows labeland concept-related uncertainties to vary independently.

$$P(o_T|s) = \frac{1 + e^{-(\frac{\Delta s^2}{2\sigma_L^2} + \frac{\Delta o^2}{2\sigma_C^2})}}{1 + e^{-(\frac{\Delta s^2}{2\sigma_L^2} + \frac{\Delta o^2}{2\sigma_C^2})} + e^{-\frac{\Delta s^2}{2\sigma_L^2}} + e^{-\frac{\Delta o^2}{2\sigma_C^2}}}$$
(9)

In order to understand the predictions of the models (especially the more general ones, i.e., Model 2 and 3), Figure 4 show simulations of the accuracy $P(o_T|s)$ as a function of the distinctiveness parameters (Δs and Δo) and the uncertainty parameters σ_L and σ_C .

The simulations explain two experimental results from previous studies and make one new prediction:

- 1) For fixed values of Δo and σ , the probability of accurate responses increases as a function of Δs . This pattern accounts for the fact that similar sounds are generally more challenging to learn than different sounds for both children (Stager & Werker, 1997) and adults (Pajak et al., 2016).
- 2) For fixed values of Δs and Δo , accuracy increases when the representational uncertainty σ decreases. This observation provides a simple model for developmental change. Younger children have noisier representations (see Swingley, 2007; Yoshida et al., 2009), which leads to lower word recognition accuracy, especially for similar-sounding words.
- 3) For fixed values of Δs and σ , accuracy increases with the visual distance between the semantic referents Δo . This is a new prediction that our model makes. Previous work studied the effect of several bottom-up and top-down properties in disambiguating

similar sounding words (e.g., Fennell & Waxman, 2010; Rost & McMurray, 2009;
Thiessen, 2007), but to our knowledge, no previous study in the literature tested the
effect of the visual distance between the semantic referents.

Experiment

In this experiment, we tested participants in the word learning task introduced above (Figure 3). More precisely, we explored the predictions related to both distinctiveness and precision. Sound similarity (Δs) and object similarity (Δo) were varied simultaneously in a within-subject design. Two age groups (preschool children and adults) were tested on the same task² to explore whether development can be characterized with the uncertainty parameters, σ_C and σ_L . The experiment, sample size, exclusion criteria, and the model's main predictions were pre-registered.³

$_{252}$ Methods

244

Participants. We report data from N=63 children ages 4-5 years from a nursery school. An additional N=39 children participated but were removed from analyses (using preregistered exclusion criteria) because they were not above chance on the catch trials due to the challenging nature of our procedure (see below). We also report data from N=74 adult participants tested on Amazon Mechanical Turk. An additional N=26 were tested but removed from analyses (again, using preregistered exclusion criteria) because they had low scores on the catch trials or because they were familiar with the non-English sound

²This four-condition within-subject design is relatively novel for preschoolers, but we followed the tablet paradigm (e.g., Frank, Sugarman, Horowitz, Lewis, & Yurovsky, 2016) which allowed us to gather a relatively large number of trials from each child.

³Due to the double-blind review, the link to the osf repository is only provided in the full version addressed to the editor.

stimuli we used in the adult experiment.

Stimuli and similarity rating. The sound stimuli were generated using the

MBROLA Speech Synthesizer (Dutoit, Pagel, Pierret, Bataille, & Van der Vrecken, 1996).

We generated three kinds of nonsense word pairs which varied in their degree of perceptual

similarity to English speakers: 1) different pairs: "lif"/"neem" and "zem"/"doof", 2)

intermediate pairs: "aka"/"ama" and "ada"/"aba", and 3) similar non-English pairs:

"ada"/"adha" (in hindi) and "a\a"a"/"aha" (in arabic).

As for the objects, we used the Dynamic Stimuli javascript library⁴ which allowed us to
generate objects in four different categories: "tree," "bird," "bug," and "fish." These
categories were described to participants as naturally occurring kinds on an alien planet. In
each category, we generated different, intermediate, and similar pairs by manipulating a
continuous property controlling features of the category's shape (e.g., body stretch or head
fatness).

In order to validate and quantify our similarity scales, we ran a separate survey on
Amazon Mechanical Turk where we asked N=20 adults participants to evaluate the
similarity of each sound and object pair on a 7-point scale. Data are shown in Figure 5
where we scaled responses within the range [0,1] for each stimulus group. We used these data
in all models as an empirical measurement of the perceptual distance between the sound
pairs and the object pairs. The use of empirical measurement allows us to eliminate Δs and Δs as free parameters (see Frank and Goodman (2012) and Xu and Tenenbaum (2007) for a
similar strategy).

Design. Each age group saw only two of the three levels of similarity described in
the previous sub-section: different vs. intermediate for the preschoolers, and intermediate vs.
similar for adults. We made this choice in light of pilot studies showing that adults were at

⁴https://github.com/erindb/stimuli

ceiling with different sounds/objects, and children were at chance with the similar sounds/objects. That said, this difference in the level of similarity is accounted for in the model: We used empirical distance measurement to fill in the appropriate values of Δs and Δo for each age group.

To maximize our ability to measure subtle stimulus effects, the experiment was a 2x2 within-subjects factorial design with four conditions: high/low sound similarity crossed with high/low visual object similarity. Besides the four conditions, we also tested participants on a fifth catch condition which was similar in its structure to the other ones but was trivially easy and used only to select participants who were able to follow the instructions and show minimal learning.

Procedure. Preschoolers were tested at the nursery school using a tablet, whereas
adults used their own computers to complete the same experiment online. Participants were
tested in a random sequence of five conditions: the four experimental conditions plus the
catch condition. In each condition, participants saw a first block of four exposure trials
followed by four testing trials, and a second block of two exposure trials (for memory
refreshment) followed by an additional four testing trials. The length of this procedure was
demanding, especially for children, but we adopted a fully within-subjects design based on
pilot testing that indicated that precision of measurement was critical for testing our
experimental predictions.

In the exposure trials, participants saw two objects associated with their corresponding sounds. We presented the first object on the left side of the tablet's screen simultaneously with the corresponding sound. The second sound-object association followed on the other side of the screen after 500ms. For both objects, visual stimuli were present for the duration of the sound clip (about 800ms). In the testing trials, participants saw both objects simultaneously and heard only one sound. They completed the trial by selecting which of the two objects corresponded to the sound. The object-sound pairings were randomized across

participants, as was the order of the conditions (except for the catch condition which was always placed in the middle of the testing sequence). We also randomized the on-screen position (left vs. right) of the two pictures on each testing trial.

313 Results

Experimental results are shown in Figure 6 (solid lines). We first analyzed the results using a mixed-effects logistic regression with sound distance, object distance and age group as fixed effects, and with a maximal random effects structure (allowing us to take into account the full nested structure of our data) (Barr, Levy, Scheepers, & Tily, 2013). We found main effects for all the fixed effects in the regression. For the sound distance, we obtained $\beta = 0.68$ (p < 0.001), replicating previous findings that sound distance modulates success in word learning (e.g., Stager & Werker, 1997).

For object distance, we found $\beta = 0.60$ (p < 0.001), and this finding confirms the new prediction of our model, according to which, object distance also modulates success in word learning. Note, in particular, that increasing the visual similarity of the objects makes children succeed in learning the similar-sounding words. Finally, for the age group, we obtained $\beta = 0.59$ (p < 0.001), showing that overall performance improves with age. The full output of the regression model is shown in Table 2.

We next fit the three models obtained through expressions 7, 8, and 9 to the participants' responses in each age group. The predictions of the models are shown 6. The parameter estimates (for σ_L and σ_C) as well as models' goodness to fit (i.e., measured through R^2) are presented in Table 1.

Model 1, which does not take into account ambiguity in recovering concepts from
observed objects, explains only a small part of the variance. In contrast, Model 3, which
does take into account this ambiguity, accounts for all the variance. Interestingly, Model 2

341

which has a single, shared uncertainty parameter for both auditory and visual modalities still explains almost all the variance in human data.

As predicted, the uncertainty parameters were larger for children than they were for adults (Table 1), showing that word knowledge gets more precise with development. Further, the parameter estimates of Model 3 show that this developmental effect is larger for labels (σ_L varies between 0.83 in children and 0.12 in adults) than it is for concepts (σ_C varies between 0.31 in children and 0.17 in adults).

General Discussion

This paper explored the idea that some seemingly stage-like patterns in cognitive 342 development can be characterized in a continuous fashion. We used as a case study the seminal work of Stager and Werker (1997) showing a discrepancy between children's speech 344 perception abilities and their word learning skills. The development of this discrepancy could 345 be understood in terms of a discrete change in word representation. But our model 346 demonstrates that it can also be parsimoniously described as a result of continuous 347 developmental change in the precision of children's graded word knowledge. Our model 348 instantiates the continuous development hypothesis (Pajak et al., 2016; Swingley, 2007; 349 Yoshida et al., 2009). 350

We find in the literature two broad accounts of development in the Switch task: One
that suggests direct development of the sound representation and one that hypothesizes
indirect development of this representation through improvement in general cognitive
resources. On the first account, the sound representation becomes more precise as learners
refine the boundaries of their initially ambiguous phonetic categories and as they gain more
experience with the functional role of these categories (Apfelbaum & McMurray, 2011;
Dietrich, Swingley, & Werker, 2007; Rost & McMurray, 2009, 2010; Yoshida et al., 2009). On

the second account, the precision of sound encoding in the switch task improves as a result of
the maturation of more general resources like the attentional and working memory capacity
(Hofer & Levy, 2017; Stager & Werker, 1997; Werker & Fennell, 2004). Such improvement
allows older children and adults to better encode the sound details while simultaneously
matching these sounds to visual objects. Indeed, one recent meta-analysis of the switch task
concluded that both changing representation precision and better memory/attention play a
role in developmental changes (Tsui, Byers-Heinlein, & Fennell, 2019).

Our model is compatible with both of these accounts. In our work, the probability
distributions do not distinguish between the direct and indirect sources of uncertainty —
both are included. Indeed, part of the measured uncertainty reflects the learner's degrees of
confidence in the phonetic/phonological boundaries (i.e., the direct account) and another
part reflects a possible drop in perceptual acuity due to high cognitive load (i.e., the indirect
account). Note, however, that the model (at least in its current format) is incapable of
answering questions about the development of each of these sources of uncertainty separately
or about their relative contribution to the global uncertainty.

Werker and Curtin (2005) proposed to explain development in the Switch task using 373 their theory called Processing Rich Information from Multidimensional Interactive 374 Representations (or PRIMIR) which attempts to explain various phenomena in early speech 375 perception and word learning within a unified framework. PRIMIR posits that children initially try to attend to various features of the speech signal, regardless of whether or not these features are relevant to the task at hand. For example, when learning the meaning of similar sounds, infants are unsure what detail is most important to identify words (i.e., the 379 phonemes), and will instead activate several aspects of the information simultaneously 380 (including, for example, the gender of the speaker). The lack of selective attention leads to 381 confusion and then to failure in the task. 382

According to PRIMIR, learning similar-sounding words becomes more robust over time

383

as children develop abstract phonemic categories. The latter act as filters, allowing children 384 to attend selectively to the important information. This account is also compatible with our 385 model: Developing phonemic categories allows learners to better determine when a sound 386 contrast signals a change in meaning (i.e., when this contrast straddles two categories as in 387 "bin" vs. "din") and when a sound contrast does not change word meaning (i.e., when it 388 instantiates a variation within the same category). In fact, learning to distinguish contrastive 389 vs. non-contrastive pairs amounts to reducing the overlap between the probability 390 distribution of two neighboring words. 391

While most research has focused on sound representation specifically in analyzing the 392 process of learning similar-sounding words, this work showed that the visual representation 393 of the referent is equally important. Indeed, Model 1 — which assumes that any visually 394 discriminable contrast can be encoded unambiguously as separate referents — failed to 395 explain the data, whereas Model 2 and 3 — which take into account visual ambiguity — 396 succeeded. As a consequence of this assumption, we found that just like word learning is 397 modulated by the phonological similarity of the form, it is also modulated by the visual 398 similarity of the semantic referents. 399

Model 2, which predicts that sound similarity and visual similarity influence word 400 learning accuracy in the same way, explained slightly less variance than Model 3 which 401 predicts that these modalities influence word learning differently. Further, as we stated in 402 the results section, a comparison of the variance estimates across age groups showed that 403 uncertainty reduction in the visual modality was lower compared to that of the auditory modality (Table 1). Perhaps this difference is due to the fact that, in our task, the auditory speech had more sources of noise — that children have to deal with — than the visual input did. The processing of speech involved dealing with both perceptual noise and categorical 407 ambiguity (due to the fact that the phonemic boundaries are still developing). In contrast, 408 the processing of the visual input in our task involved only perceptual noise and no 409

category-related uncertainty. A future direction of research is independent measurement and comparison of these parameters in children.

Our finding that word learning is mediated by the visual similarity of the semantic 412 objects has implications for theories of lexical development. It suggests that, all things being 413 equal, children may learn, first, words whose semantic referents are visually different as this 414 allows them to minimize semantic ambiguity. It will be interesting for future work to explore 415 whether the results that we obtained using visual similarity generalize to richer, more 416 conceptual features in the semantic space. In addition, it is important to study how 417 laboratory experiment of this sort may explain patterns of word learning in the wild 418 (Engelthaler & Hills, 2017; Fourtassi, Bian, & Frank, 2018; Sizemore, Karuza, Giusti, & 410 Bassett, 2018). 420

There are a few limitations to this work. One is that the model was fit to data from 421 children at a relatively older age (4-5 years old) than what is typically studied in the 422 literature (14-17 month-old). We selected this older age group to optimize the number and 423 precision of the experimental measures (both are crucial to model fitting). Data collection 424 involved presenting participants with several trials across four conditions in a 425 between-subject design. It would have been challenging to obtain such measures with infants. 426 That said, though we used data from older children, we still found clear developmental differences with adults, confirming and extending findings that the ability to distinguish similar-sounding words continues developing well beyond 17 months (Fennell & Byers-Heinlein, 2014; Hazan & Barrett, 2000; Mattock, Polka, Rvachew, & Krehm, 2010).

One limitation of our models is that they only account for bottom-up, similarity-based effects. They do not account for how high-level factors such as social and communicative cues can influence learning. For example, Fennell and Waxman (2010) highlighted the fact that some laboratory tasks such as the one used in Stager and Werker (1997) introduce novel words in isolation (e.g., "neem!") rather than within a naming phrase (e.g., "look at the

neem!"). This fact may prompt children to interpret these novel words in a non-referential way (e.g., an exclamation such as "Wow!").

To conclude, this paper proposes a model that accounts for the development of an important aspect of word learning. Our account suggests that the developmental data can be explained based on a continuous process operating over similar representations across the lifespan, suggesting developmental continuity. We used a case from word learning as an example, but the same idea might apply to other aspects of cognitive development that are typically thought of as stage-like (e.g., acquisition of a theory of mind). Computational models, such as the one proposed here, can help us investigate the extent to which such discontinuities emerge due to genuine qualitative changes and the extent to which they reflect the granularity of the researchers' own measurement tools.

All data and code for these analyses are available at [Due to the doube-blind review, the link to the github repository is only provided in the full version addressed to the editor]

References

447

Apfelbaum, K. S., & McMurray, B. (2011). Using variability to guide dimensional weighting:

Associative mechanisms in early word learning. *Cognitive Science*, 35.

Barr, D., Levy, R., Scheepers, C., & Tily, H. (2013). Random effects structure for
confirmatory hypothesis testing: Keep it maximal. *Journal of Memory and Language*,
68(3).

- ⁴⁵⁴ Carey, S. (2009). The origin of concepts. Oxford University Press.
- ⁴⁵⁵ Carey, S., Zaitchik, D., & Bascandziev, I. (2015). Theories of development: In dialog with

- jean piaget. Developmental Review, 38.
- Dautriche, I., Swingley, D., & Christophe, A. (2015). Learning novel phonological neighbors:

 Syntactic category matters. *Cognition*, 143.
- Dietrich, C., Swingley, D., & Werker, J. (2007). Native language governs interpretation of salient speech sound differences at 18 months. *Proceedings of the National Academy*of Sciences, 104.
- Dutoit, T., Pagel, V., Pierret, N., Bataille, F., & Van der Vrecken, O. (1996). The mbrola project: Towards a set of high quality speech synthesizers free of use for non commercial purposes. In *Proceedings of ICSLP* (Vol. 3). IEEE.
- Engelthaler, T., & Hills, T. T. (2017). Feature biases in early word learning: Network distinctiveness predicts age of acquisition. *Cognitive Science*, 41.
- Fennell, C., & Byers-Heinlein, K. (2014). You sound like mommy: Bilingual and monolingual infants learn words best from speakers typical of their language environments.

 International Journal of Behavioral Development, 38(4).
- Fennell, C., & Waxman, S. (2010). What paradox? Referential cues allow for infant use of phonetic detail in word learning. *Child Development*, 81.
- Fernald, A., Perfors, A., & Marchman, V. A. (2006). Picking up speed in understanding:

 Speech processing efficiency and vocabulary growth across the 2nd year.

 Developmental Psychology, 42.
- Fourtassi, A., Bian, Y., & Frank, M. C. (2018). Word learning as network growth: A

 cross-linguistic analysis. In *Proceedings of the 40th annual meeting of the cognitive*science society.
- Frank, M. C., & Goodman, N. D. (2012). Predicting pragmatic reasoning in language games.

- Science, 336 (6084).
- Frank, M. C., Sugarman, E., Horowitz, A. C., Lewis, M., & Yurovsky, D. (2016). Using
 tablets to collect data from young children. *Journal of Cognition and Development*,

 17(1).
- Golinkoff, R. M., Hirsh-Pasek, K., Cauley, K. M., & Gordon, L. (1987). The eyes have it:

 Lexical and syntactic comprehension in a new paradigm. *Journal of Child Language*,

 14.
- Hazan, V., & Barrett, S. (2000). The development of phonemic categorization in children aged 6–12. *Journal of Phonetics*, 28(4).
- Hofer, M., & Levy, R. (2017). Modeling Sources of Uncertainty in Spoken Word Learning. In

 Proceedings of the 39th Annual Meeting of the Cognitive Science Society.
- Lewis, M., & Frank, M. C. (2013). An integrated model of concept learning and
 word-concept mapping. In *Proceedings of the annual meeting of the cognitive science*society (Vol. 35).
- Mattock, K., Polka, L., Rvachew, S., & Krehm, M. (2010). The first steps in word learning
 are easier when the shoes fit: Comparing monolingual and bilingual infants.

 Developmental Science, 13(1).
- McMurray, B. (2007). Defusing the childhood vocabulary explosion. *Science*, 317(5838).
- Munakata, Y. (2001). Graded representations in behavioral dissociations. Trends in
 Cognitive Sciences, 5(7).
- Pajak, B., Creel, S., & Levy, R. (2016). Difficulty in learning similar-sounding words: A developmental stage or a general property of learning? *Journal of Experimental*

- Psychology: Learning, Memory, and Cognition, 42(9).
- Pater, J., Stager, C., & Werker, J. (2004). The perceptual acquisition of phonological contrasts. *Language*, 80.
- Piaget, J. (1954). The construction of reality in the child. New York, NY, US: Basic Books.
- Rost, G., & McMurray, B. (2009). Speaker variability augments phonological processing in early word learning. *Developmental Science*, 12.
- Rost, G., & McMurray, B. (2010). Finding the signal by adding noise: The role of noncontrastive phonetic variability in early word learning. *Infancy*, 15.
- Shultz, T. R., Schmidt, W. C., Buckingham, D., & Mareschal, D. (1995). Modeling cognitive development with a generative connectionist algorithm. In T. J. Simon & G. S.
- Halford (Eds.), Developing cognitive competence: New approaches to process modeling.

 Hillsdale, NJ: Lawrence Erlbaum Associates, Inc.
- Sizemore, A. E., Karuza, E. A., Giusti, C., & Bassett, D. S. (2018). Knowledge gaps in the early growth of semantic feature networks. *Nature Human Behaviour*, 2(9).
- Stager, C., & Werker, J. (1997). Infants listen for more phonetic detail in speech perception
 than in word-learning tasks. *Nature*, 388(6640).
- Swingley, D. (2007). Lexical exposure and word-form encoding in 1.5-year-olds.

 Developmental Psychology, 43(2).
- Thiessen, E. (2007). The effect of distributional information on children's use of phonemic contrasts. *Journal of Memory and Language*, 56.
- Tsui, A. S. M., Byers-Heinlein, K., & Fennell, C. (2019). Associative word learning in

- infancy: A meta-analysis of the switch task. Developmental Psychology, 55.
- Werker, J., & Curtin, S. (2005). PRIMIR: A developmental framework of infant speech processing. Language Learning and Development, 1.
- Werker, J., & Fennell, C. (2004). Listening to sounds versus listening to words: Early steps in word learning. In D. G. Hall & S. Waxman (Eds.), Weaving a lexicon. Cambridge: MIT Press.
- Werker, J., Cohen, L. B., Lloyd, V. L., Casasola, M., & Stager, C. (1998). Acquisition of word-object associations by 14-month-old infants. *Developmental Psychology*, 34.
- Werker, J., Fennell, C., Corcoran, K., & Stager, C. (2002). Infants' ability to learn phonetically similar words: Effects of age and vocabulary size. *Infancy*, 3.
- White, K., Yee, E., Blumstein, S., & Morgan, J. (2013). Adults show less sensitivity to

 phonetic detail in unfamiliar words, too. *Journal of Memory and Language*, 68(4).
- Xu, F., & Tenenbaum, J. B. (2007). Word learning as bayesian inference. *Psychological Review*, 114(2).
- Yeung, H., & Werker, J. (2009). Learning words' sounds before learning how words sound:

 9-month-olds use distinct objects as cues to categorize speech information. *Cognition*,

 113.
- Yoshida, K., Fennell, C., Swingley, D., & Werker, J. (2009). 14-month-olds learn similar-sounding words. *Developmental Science*, 12.

541

Figure captions

- An illustration of the probabilistic/continuous account using simulated Figure 1. 542 data. A word is represented with a distribution over the perceptual space 543 (indicated in red or blue). When the uncertainty of the representation is 544 large relative to the distance between the stimuli (top panel), an instance 545 of the red category (indicated with a star) could also be a plausible 546 instance of the green category, hence the low recognition accuracy score. 547 The accuracy is higher when the stimuli are less similar (left panel), or 548 when the representation are more precise (right panel). 549
- Graphical representation of our model. Circles indicate random variables (shading indicates observed variables). The squares indicate fixed model parameters.
- 553 Figure 3. An overview of the task used in this study.
- The predicted probability of accurate responses in the testing phase as a function of stimuli distinctiveness Δs and Δo and representation precision σ (For simplicity, we use model 2, which assumes that $\sigma = \sigma_C = \sigma_L$).

 Dashed line represents chance.
- Distances for both sound and object pairs from an adult norming study.

 Data represent Likert values normalized to [0,1] interval. Error bars
 represent 95% confidence intervals.
- Figure 6. Accuracy of word recognition as a function of the sound distance, the
 object distance, and the age group (preschool children vs. adults). We
 show both the models' predictions (dashed lines) and the experimental
 results (solid lines, same across the three panels). Error bars represent
 95% confidence intervals.

Table 1

Characteristics and performance of the models used in this study.

				Children		Adults	
Model	Structure	Param.	\mathbb{R}^2	$\sigma_{ m L}$	$\sigma_{ m C}$	$\sigma_{ m L}$	$\sigma_{ m C}$
model 1	$\sigma_{\rm L}$ only	1	0.27	1	_	0.37	_
model 2	$\sigma_{ m L} = \sigma_{ m C}$	1	0.95	0.6	0.6	0.15	0.15
model 3	$\sigma_{ m L} eq \sigma_{ m C}$	2	1.00	0.83	0.31	0.12	0.17

	Predictor	Estimate	Std.Error	z.value	p.value
1	(Intercept)	1.06	0.21	5.02	< 0.01
2	sound_dist	0.68	0.14	4.72	< 0.01
3	object_dist	0.6	0.15	3.96	< 0.01
4	age	0.59	0.16	3.64	< 0.01
5	$sound_dist*object_dist$	0.36	0.14	2.56	0.01
6	sound_dist*age	0.37	0.13	2.83	< 0.01
7	object_dist*age	0.25	0.13	1.91	0.06
8	sound_dist*object_dist*age	0.19	0.13	1.45	0.15

Table 2

Predictor estimates with standard errors and significance information for a logistic mixed-effects model predicting the accuracy of word learning.

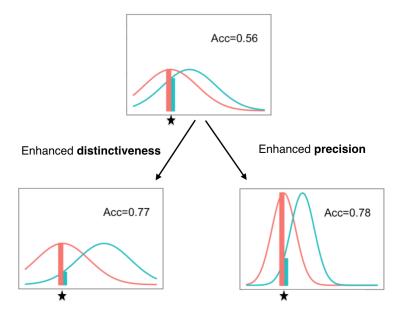


Figure 1. An illustration of the probabilistic/continuous account using simulated data. A word is represented with a distribution over the perceptual space (indicated in red or blue). When the uncertainty of the representation is large relative to the distance between the stimuli (top panel), an instance of the red category (indicated with a star) could also be a plausible instance of the green category, hence the low recognition accuracy score. The accuracy is higher when the stimuli are less similar (left panel), or when the representation are more precise (right panel).

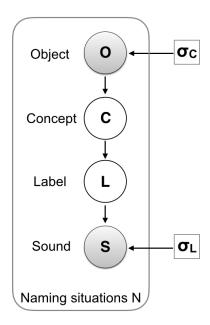


Figure 2. Graphical representation of our model. Circles indicate random variables (shading indicates observed variables). The squares indicate fixed model parameters.

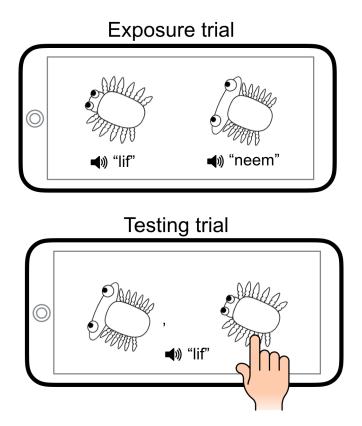


Figure 3. An overview of the task used in this study.

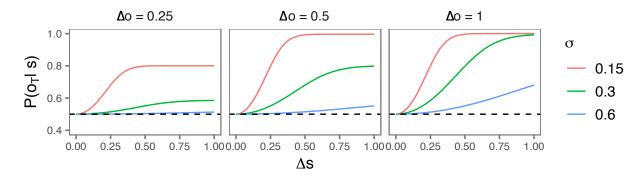


Figure 4. The predicted probability of accurate responses in the testing phase as a function of stimuli distinctiveness Δs and Δo and representation precision σ (For simplicity, we use model 2, which assumes that $\sigma = \sigma_C = \sigma_L$). Dashed line represents chance.

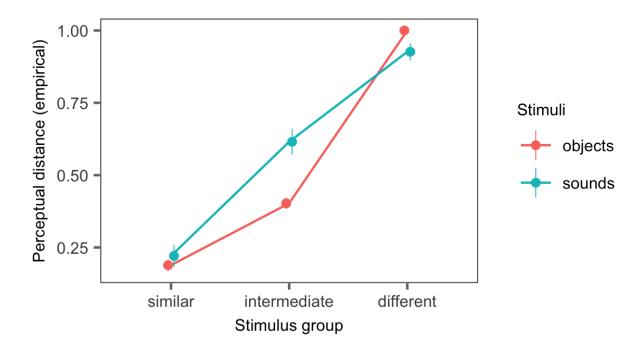


Figure 5. Distances for both sound and object pairs from an adult norming study. Data represent Likert values normalized to [0,1] interval. Error bars represent 95% confidence intervals.

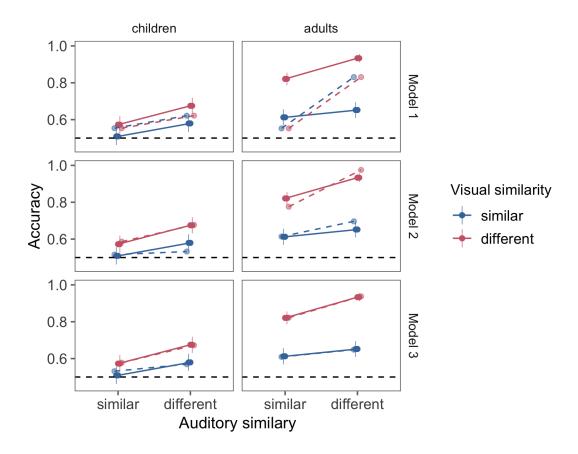


Figure 6. Accuracy of word recognition as a function of the sound distance, the object distance, and the age group (preschool children vs. adults). We show both the models' predictions (dashed lines) and the experimental results (solid lines, same across the three panels). Error bars represent 95% confidence intervals.