Word Learning as Network Growth: A Cross-linguistic Analysis

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14 Abstract

Children tend to produce words earlier when they are connected to a variety of other words 15 along both the phonological and semantic dimensions. Though this connectivity effect has 16 been extensively documented, little is known about the underlying developmental 17 mechanism. One view suggests that learning is primarily driven by a network growth model 18 where highly connected words in the child's early lexicon attract similar words. Another 19 view suggests that learning is driven by highly connected words in the external learning 20 environment instead of highly connected words in the early internal lexicon. The present 21 study tests both scenarios systematically in both the phonological and semantic domains, 22 and across 8 languages. We show that external connectivity in the learning environment 23 drives growth in both the semantic and the phonological networks, and that this pattern is consistent cross-linguistically. The findings suggest a word learning mechanism where 25 children harness their statistical learning abilities to (indirectly) detect and learn highly connected words in the learning environment. Keywords: Language understanding; audio-visual processing; word learning; speech

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Introduction

What factors shape vocabulary learning over the course of early childhood? To 32 investigate this question, scientists have adopted multiple research strategies, from 33 conducting controlled laboratory experiments (e.g. Markman, 1990) to analyzing dense corpora capturing language learning in context (e.g., B. C. Roy, Frank, DeCamp, Miller, & Roy, 2015). One strategy consists in documenting the timeline of words' acquisition, and studying the properties that make words easy or hard to learn. For example, within a lexical category, words that are more frequent in child-directed speech are acquired earlier (J. C. Goodman, Dale, & Li, 2008). Other factors include word length, the mean length of 39 utterances in which the word occurs, and concreteness (see Braginsky, Yurovsky, Marchman, & Frank, 2016). Besides these word-level properties, the lexical structure (that is, how words relate to 42 each other) also influences the age of acquisition of words. The lexical structure is best characterized in terms of a network where each node represents a word in the vocabulary, and each link between two nodes represents a relationship between the corresponding pair of words. Previous studies have investigated early vocabulary structure by constructing networks using a variety of word-word relations including shared semantic features, target-cue relationships in free association norms, co-occurrence in child directed speech, and phonological similarity. These studies have found that children tend to produce words that have higher neighborhood density (i.e., high connectivity in the network) earlier, both at the phonological and the semantic level (Engelthaler & Hills, 2017; Hills, Maouene, Riordan, & Smith, 2010; Hills, Maouene, Maouene, Sheya, & Smith, 2009; Stella, Beckage, & Brede, 2017; Storkel, 2009). While most studies have focused on the static properties of the lexical network, a few have investigated the underlying developmental process. In particular, Steyvers and Tenenbaum (2005) suggested that the observed effects of connectivity are the consequence of

how the lexical network gets constructed in the child's mind. According to this explanation, known as Preferential Attachment (PAT), highly connected words in the child's lexicon tend to "attract" more words over time, in a rich-get-richer scenario (Barabasi & Albert, 1999). 59 In other words, what predicts word learning is the *internal* connectivity in the child's early 60 lexicon. In contrast, Hills et al. (2009) suggested that what biases the learning is not the 61 connectivity in the child's internal lexicon but, rather, external connectivity in the learning 62 environment. They called this alternative explanation Preferential Acquisition (PAC). Figure 1 shows an illustration of both growth scenarios with the same simplified network. These two proposals represent two divergent ideas about the role of lexical networks in acquisition. On the PAT proposal, network structure is a causal factor in early word learning; in contrast, on the PAC approach, network structure is not internally represented and, therefore, might be an epiphenomenon of the statistics of the linguistic input. Studies that investigate lexical network growth have focused on semantic networks 69 using English data (Hills et al., 2010, 2009; Steyvers & Tenenbaum, 2005). The novelty of 70 the current study is threefold: First, it investigates whether phonological networks, like 71 semantic networks, grow by PAC, or if they rather grow by PAT. Second, it provides a 72 systematic comparison of both network growth scenarios in the phonological and the 73 semantic domains and assesses their relative contribution to the learning process. Third, it tests the generality of the findings across eight languages.

76 Networks

#### 77 Data

We used data from Wordbank (Frank, Braginsky, Yurovsky, & Marchman, 2017), an open repository aggregating cross-linguistic language developmental data of the MacArthur-Bates Communicative Development Inventory (CDI), a parent report vocabulary checklist. Parent report is a reliable and valid measure of children's vocabulary that allows for the cost-effective collection of datasets large enough to test network-based models of

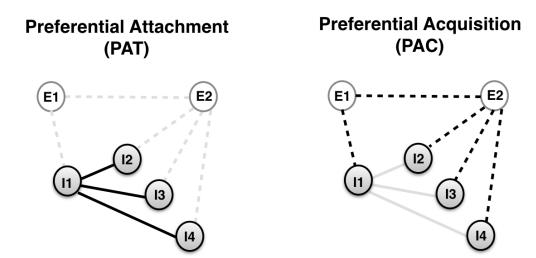


Figure 1. Illustration of the growth scenarios. Filled circles (I1-I4) represent known words (internal), and empty circles (E1 and E2) represent words that have not been learned yet (external). Black lines represent links that are relevant in each growth scenario, and gray lines represent links that are irrelevant. For PAT, the utility of a candidate, external node is the average degree (i.e., number of links) of the internal nodes that it would attach to. Thus, according to PAT, the node E1 is more likely to enter the lexicon first. For PAC, the utility of a candidate node is its degree in the entire network. According to PAC, the node E2 is more likely to enter the lexicon first.

- acquisition (Fenson et al., 1994). We used the *Words and Sentences* version of the CDI
  which contains the productive vocabulary of toddlers (age varied between 16 to 36 months).
  Following previous studies (Hills et al., 2009; Storkel, 2009), we restricted our analysis to
  nouns. We defined the age of acquisition of a given word by the month at which this word
  was produced by at least 50% of children (J. C. Goodman et al., 2008), and we excluded
  nouns that have not been learned (according to this criterion) by the last month for which
  we have CDI data.
- We obtained these nouns in eight languages: Croatian, Danish, English, Italian,
  Norwegian, Russian, Spanish, and Turkish. We used the subset of nouns that had entries in

- the Florida Association Norms (see below). Since these norms are available only in English,
- <sup>93</sup> we used the hand-checked translation equivalents provided by Braginsky et al. (2016),
- <sup>94</sup> allowing us to use the English association norms across languages. Table 1 gives an overview
- of the data used. Translation equivalents were originally constructed for a subset of words
- of appearing on the toddler CDI form, and so not all words are currently available. Note,
- however, that all languages have at least 60% of nouns translated.

	language	total	translated	normed
1	Croatian	253	177	170
2	Danish	295	198	187
3	English	296	296	274
4	Italian	311	203	194
5	Norwegian	305	193	186
6	Russian	311	311	285
7	Spanish	240	173	163
8	Turkish	293	175	164

Table 1

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Total number of nouns produced by toddlers in the CDI (left). We included in our study the subset of these nouns that had available English translations (middle). The final set consisted of nouns that had both available translations as well entries in the Free Association Norms (right).

#### Semantic networks

We constructed semantic networks following the procedure outlined in Hills et al. (2009). We used as an index of semantic relatedness the Florida Free Association Norms (Nelson, McEvoy, & Schreiber, 1998). This dataset was collected by giving adult participants a word (the cue), and asking them to write the first word that comes to mind (the target). For example, when given the word "ball", they might answer with the word "game". A pair

of nodes were connected by a directed link from the cue to the target if there was a cue-target relationship between these nodes in the association norms. The connectivity of a given node was characterized by its *indegree*: the number of links for which the word was the target. To model growth from month to month, we constructed a different network at each month, based on the words that have been acquired by that month.

# 109 Phonological networks

We generated approximate International Phonetic Alphabet (IPA) transcriptions from
the orthographic transcription, across languages, using the open source text-to-speech
software Espeak. We used the Levenshtein distance (also known as edit distance) as a
measure of phonological relatedness between two nodes. The measure counts the minimum
number of operations (insertions, deletions, substitutions) required to change one string into
another.

In previous studies, two nodes were linked if they had an edit distance of 1 (e.g., 116 Storkel, 2009). However, in these previous studies the network was built using an adult 117 vocabulary. In the current study, however, network growth models are based on the 118 children's early vocabulary which contains very few word pairs with an edit distance of 1. 119 When using this threshold, the resulting networks were too sparse and uninformative. Thus, 120 we increased the threshold from 1 to 2, that is, two nodes were related if their edit distance 121 was equal to 1 or 2. The connectivity of a given node was characterized with its degree: the 122 number of links it shares with other words. 123

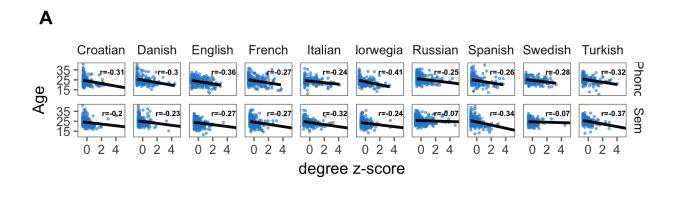
124 Analysis

# Static properties of the global network

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We start by analyzing word connectivity in the global (static) network. We constructed this network using nouns learned by the oldest age for which we have CDI data (e.g., in English this corresponds to the network by 30 months). This global network is the end-state

towards which both PAT and PAC should converge by the last month of learning. Moreover, following Hills et al. (2009), we used this end-state network as a proxy for the external connectivity in the learning environment. Below we analyze properties of this global networks that are relevant to PAC and/or PAT.



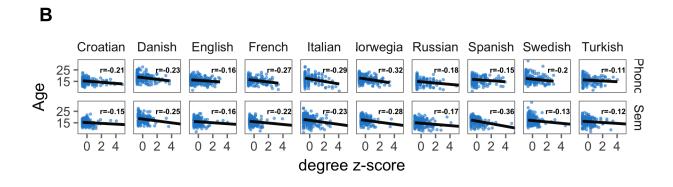


Figure 2. Age of production (A) and comprehension (B) in the global network as predicted by the degree in this network. Results are shown in each language for phonological and semantic networks. Each point is a word, with lines indicating linear model fits.

Connectivity predicts the age of acquisition. Connectivity in the global
network is directly related to PAC as it represents the explicit criterion PAC uses to
determine what words should be learned first (Figure 1). Therefore, a direct consequence of
a PAC-like growth scenario is a correlation between connectivity in the global network and

the age of acquisition.<sup>1</sup> Figure 2 shows how the age of production (A) and comprehension
(B) for each word varies as a function of its degree (or indegree for the semantic network).
For ease of visual comparison, the predictor (i.e., the degree) was centered and scaled across
languages. The plots show, overall, a negative correlation between the month of acquisition
and the degree, indicating that nouns with higher degrees are generally learned earlier.

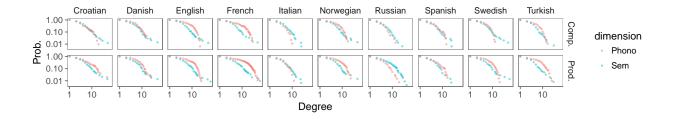


Figure 3. Log-log plot of the cumulative degree distribution function for the global phonological and semantic networks across languages. The figure shows the results for both production and comprehension data. A perfect power-law distribution should appear as a straight line in this graph.

**Power-law degree distribution?** We also analyzed the global network's degree 142 distribution. The shape of this distribution is particularly relevant to PAT as this growth 143 scenario is known to generate networks with a power-law degree distribution (i.e., a 144 distribution of the form  $p(k) \propto \frac{1}{k^{\alpha}}$ , Barabasi & Albert, 1999). If the network displays this 145 property, this fact would suggest a PAT-like generative process. Conversely, if the degree 146 distribution does not follow a power law, this fact would weaken the case for PAT. The 147 log-log plots are shown in Figure 3. We fit a power law to each empirical degree distribution 148 following the procedure outlined in Clauset, Shalizi, and Newman (2009) and using the 149 <sup>1</sup>This correlation is also compatible with PAT, although the causality is reversed. Indeed, from the perspective of this growth scenario, higher connectivity in the global network is caused by earlier learning, not the other way around. Some words end up being highly connected in the global network precisely because they happen to be acquired earlier and, therefore, have a higher chance of accumulating more links over time.

related R package (poweRlaw, Gillespie, 2015). In brief, the analysis consisted in two steps.

First, we derived the optimal cut-off,  $k_{min}$ , above which the distribution is more likely to

follow a power law,<sup>2</sup> and we estimate the corresponding scaling parameter  $\alpha$ . Second we

calculated the goodness-to-fit, which resulted in a p-value quantifying the plausibility of the

model. The results are shown in Appendix 1, table XX. Overall, we could not reject the null

hypothesis of a power-law distribution: the p-value was generally above 0.1.

In sum, the static properties of the global network are a priori compatible with both

In sum, the static properties of the global network are *a priori* compatible with both PAT and PAC. In order to decide between these two developmental scenarios, we need to fit explicit growth models to the data.

# 159 Network growth models

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How does each growth scenario predict noun development? To test the network growth scenarios, we fit different growth models to the data. We calculated the probability that a word  $w_i$ , with a growth value  $d_i$  would enter the lexicon at a given month, using a softmax function:

$$p(w_i) = \frac{e^{\beta d_i}}{\sum_j e^{\beta d_j}} \tag{1}$$

where  $\beta$  is a fitted parameter that captures the magnitude of the relationship between network parameters and growth (analogous to a regression coefficient). A positive value of  $\beta$ means that words with higher growth values  $d_i$  are acquired first, and a negative value means that words with lower growth values are acquired first (see Figure 1 for an illustration of how growth values  $d_i$  are defined in each growth scenario). The normalization includes all words that could be learned at that month.

We estimated the parameter  $\beta$  using a Bayesian approach. The inference was performed using the probabilistic programming language WebPPL (N. Goodman &

<sup>&</sup>lt;sup>2</sup>In natural phenomena, it is often the case that the power law applies only for values above a certain minimum.

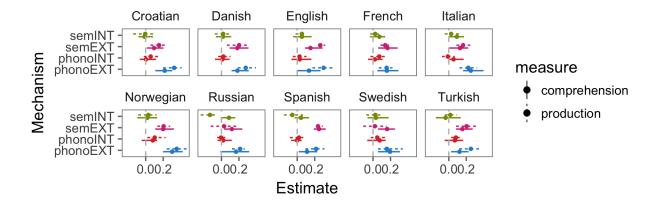
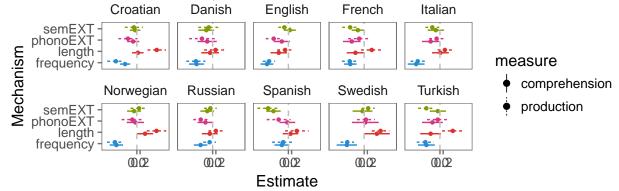


Figure 4. Evaluation of growth scenarios (EXT: externally-driven, INT: internally-driven) for both semantic and phonological networks. Each point represents the mean of the posterior distribution of the growth parameter, with ranges representing 95% credible intervals. Positive values mean that learning proceeds according to the predictions of the growth scenario, whereas negative values mean that learning proceeds in opposition to the predictions of the growth scenario.

Stuhlmuller, 2014). We defined a uniform prior over  $\beta$ , and at each month, we computed the likelihood function over words that could possibly enter the lexicon at that month, fit to the words that have been learned at that month (using formula 1). Markov Chain Monte Carlo sampling resulted in a posterior distribution over  $\beta$ , which we summarized in Figure 4.

For the semantic networks, the results replicate Hills et al.'s finding in English, which is that the semantic network grows by PAC, not by PAT. Moreover, this finding holds in seven of the eight languages we examined.<sup>3</sup> The PAC model also fits better than PAT for phonological networks. We note however that PAT, though weaker, fares better for the phonological networks (where it predicts part of the growth process in some languages such as Croatian, English, Norwegian and Russian) than it does for the semantic networks (where it is rather universally unpredictive).



#### 184 Comparison to other predictors of age of acquisition

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We saw that the way semantic and phonological information is structured in the learning environment (i.e., PAC) contributes to noun learning across languages. However, we know that other factors influence learning as well (e.g., Braginsky et al., 2016). Next we investigated how semantic and phonological connectivity interact with two other factors.

The first one is word frequency, a well studied factor shown to predict the age of acquisition in a reliable fashion (e.g. J. C. Goodman et al., 2008). The second factor is word length, which correlates with phonological connectivity.

Since PAT was uninformative, we dropped it from this analysis, keeping only PAC.

This simplified the model because we no longer needed to fit growth month-by-month.<sup>4</sup> A more direct way to assess and compare the contribution of PAC in relation to other

<sup>&</sup>lt;sup>3</sup>One could imagine that the fact of using English free association norms cross-linguistically would decrease the effect of non-English semantic networks because of possible cultural differences. However, our findings do not support this assumption as the effects were generally similar in magnitude cross-linguistically.

<sup>&</sup>lt;sup>4</sup>This was a requirement only for PAT where the words' utilities varied from month to month, depending on how connectivity changed in the growing internal network.

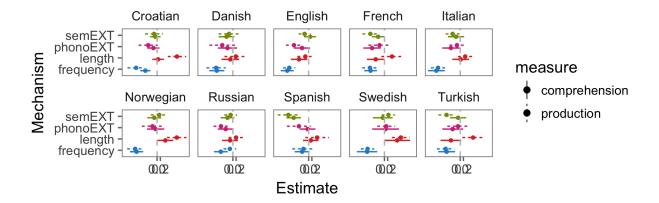


Figure 5. Estimates of the relative contribution of each predictor of AoA in the combined regression model. Results are shown for both production and comprehension data. Ranges indicate 95% confidence intervals. Positive values indicate a positive relationship (e.g. longer words tend to have a higher AoA), while negative values indicate a negative relationship (e.g. words with higher frequency tend to have a lower AoA).

word-level factors is through conducting linear regressions, where connectivity in the learning environment, frequency and length predict the age of acquisition.

We used the frequency estimates from Braginsky et al. (2016) where unigram counts were derived based on CHILDES corpora in each language.<sup>5</sup> For each word, counts included words that shared the same stem (e.g., "cats" counts as "cat"), or words that were synonymous (e.g. "father" counts as "daddy"). For word length, we counted the number of

<sup>&</sup>lt;sup>5</sup>Note that these frequency counts are based on transcripts from independent sets of children and represent a general estimate of environmental frequency across children.

201 phonemes in our generated IPA transcription.

We conducted two analyses. We fit a linear regression for each language, and we fit a 202 linear mixed-effect model to all the data pooled across languages, with language as a random 203 effect. Figure 5 shows the coefficient estimate for each predictor in each language for 204 production and comprehension data. Figure ?? shows the coefficient estimates for all 205 languages combined (all predictors were centered and scaled). The findings were as follows. 206 Overall, frequency is the largest and most consistent predictor of age of acquisition, 207 replicating results for nouns across a variety of analyses (Braginsky et al., 2016; J. C. 208 Goodman et al., 2008; B. C. Roy et al., 2015). Word length predicts learning in some 209 languages such as Croatian and Norwegian, but not in others (including English). It remains, however, a significant predictor in the global model. As for the factors of interest, i.e., 211 semantic and phonological connectivity, we also found cross-linguistic differences. 212 Phonological connectivity contributes to learning in languages such as Croatian, English and 213 Russian, whereas semantic connectivity contributes to learning in Turkish, Spanish and to 214 some extent in Croatian, but not in English.<sup>6</sup> Despite these cross-linguistic differences, both 215 phonological and semantic connectivity are significant predictors in the combined model. 216

Discussion

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The present study provided a comprehensive analysis of how lexical connectivity influences the age of acquisition of nouns in toddlers. We compared two network growth scenarios and assessed their relative contributions across eight languages. One scenario, PAT, described a rich-get-richer network growth model in which the structure of the learner's internal network determines future growth; the other, PAC, described a model in which the  $\overline{\ }^{6}$ Semantic connectivity does not explain variance in English data beyond that explained by phonological

<sup>&</sup>lt;sup>6</sup>Semantic connectivity does not explain variance in English data beyond that explained by phonological connectivity, frequency and length. This contrasts with the original finding in Hills et al. 2009. However, in this previous study, semantic connectivity was not tested in a model that included frequency, length and phonological connectivity as covariates. Another important difference is the number of words tested: Our study uses a larger set of nouns.

external, global environmental network structure determines learners' growth patterns. Our findings largely replicate the results obtained by Hills et al. (2009): Semantic networks grow 224 by preferential acquisition, not by preferential attachment. A novel finding is that 225 phonological networks also grow primarily by preferential acquisition. Moreover, both 226 semantic and phonological connectivity in the learning environment predict growth. These 227 findings generalize well across languages. When pitted against other known predictors of age 228 of acquisition (word frequency and length), the effect of word connectivity shows a 229 cross-linguistic variation, predicting learning in some languages, but not in others. 230 Nevertheless, this cross-linguistic variability is to be taken with a grain of salt as it might be 231 exaggerated in our study by the limited and partially-overlapping sample of nouns for each 232 language. In fact, both phonological and semantic connectivity are significant predictors 233 when data are pooled across languages. 234

Children start by learning words that have high semantic and phonological similarity to a variety of other words in the learning environment, not in the child's available lexicon.

This result suggests that children are sensitive to connectivity even without having first acquired the connected words. How can children indirectly detect highly connected words, and why would such words be more readily learned?

In the semantic case, the networks are based on free association norms. These associations can be (partly) derived from the patterns of word-word co-occurrence (e.g., Griffiths, Steyvers, & Tenenbaum, 2007), i.e., two words are associated if they co-occur in many different contexts. In a network structure, highly connected words would be the words that co-occur with many other words in various contexts. Why would such words be easier to learn? One possibility, suggested by Hills et al. (2010), is that the referents of these words are more easily disambiguated from other potential referents because their presence in multiple contexts provides more cross-situational, disambiguating statistics about their true referents (Smith & Yu, 2008).

In the phonological case, connectivity is inherently correlated with phonotactic

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probability (Vitevitch, Luce, Pisoni, & Auer, 1999). That is, highly connected words tend to
be made of frequent sound sequences. Even infants show a sensitivity for high frequency
sound sequences in the ambient language (Jusczyk, Luce, & Charles-Luce, 1994). Moreover,
phonotactic probability facilitates learning and recognition (e.g., Storkel, 2001). In other
words, children's sensitivity to local phonotactic regularities might lead them to learn
higher-probability words more easily. This learning effect, in turn, would lead to an observed
pattern of growth that would appear to follow the PAC growth model even though learners
themselves would only be tracking local statistics.

Finally, while validating previous results using network growth models, our study suggests that these correlational patterns may emerge from the operation of simpler mechanisms in both the semantic and phonological domains. One question for future experimental work is whether such patterns of growth can be produced in controlled behavioral experiments.

All data and code for these analyses are available at https://github.com/afourtassi/networks

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#### Disclosure statement

None of the authors have any financial interest or a conflict of interest regarding this work and this submission.

Appendix 1: Power law model

	Kmin	alpha	pValue	dimension	language
1	4.00	2.55	0.88	Sem	Croatian
2	4.00	2.18	0.12	Phono	Croatian
3	4.00	2.38	0.00	Sem	Danish
4	11.00	4.55	0.86	Phono	Danish
5	5.00	2.66	0.13	Sem	English
6	20.00	9.14	0.51	Phono	English
7	8.00	2.81	0.13	Sem	French
8	20.00	3.75	0.11	Phono	French
9	4.00	2.93	0.61	Sem	Italian
10	9.00	9.45	0.78	Phono	Italian
11	5.00	2.88	0.20	Sem	Norwegian
12	15.00	6.28	0.74	Phono	Norwegian
13	24.00	5.61	0.72	Sem	Russian
14	8.00	4.20	0.54	Phono	Russian
15	4.00	2.98	0.46	Sem	Spanish
16	13.00	8.75	0.74	Phono	Spanish
17	4.00	2.49	0.17	Sem	Swedish
18	11.00	4.68	0.10	Phono	Swedish
19	4.00	2.87	0.93	Sem	Turkish
20	8.00	3.26	0.38	Phono	Turkish

Table 2

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Results of fitting a power law model to the degree distribution in each model for production data. Kmin is the optimal degree cut-off, alpha is the scaling parameter, and pValue is the probability that quantifies the plausibility of the power law hypothesis. If pValue is close to 1, the power law model cannot be rejected as a plausible fit for the data. If, instead, pValue is small (e.g., p < 0.05) then the null hypothesis of a power law model can be rejected.

	Kmin	alpha	pValue	dimension	language
1	5.00	2.67	0.90	Sem	Croatian
2	2.00	2.06	0.02	Phono	Croatian
3	4.00	2.39	0.01	Sem	Danish
4	5.00	2.98	0.14	Phono	Danish
5	4.00	2.64	0.77	Sem	English
6	13.00	5.16	0.23	Phono	English
7	4.00	2.63	0.33	Sem	French
8	18.00	5.58	0.34	Phono	French
9	4.00	2.88	0.69	Sem	Italian
10	8.00	10.27	0.91	Phono	Italian
11	5.00	2.87	0.43	Sem	Norwegian
12	13.00	7.65	0.44	Phono	Norwegian
13	8.00	3.91	0.95	Sem	Russian
14	5.00	3.97	0.85	Phono	Russian
15	5.00	3.11	0.55	Sem	Spanish
16	5.00	3.01	0.09	Phono	Spanish
17	5.00	2.81	0.71	Sem	Swedish
18	9.00	6.75	0.10	Phono	Swedish
19	4.00	3.13	0.89	Sem	Turkish
20	9.00	5.73	0.96	Phono	Turkish

Results of fitting a power law model to the degree distribution in each model for comprehension data. Kmin is the optimal degree cut-off, alpha is the scaling parameter, and pValue is the probability that quantifies the plausibility of the power law hypothesis. If pValue is close to 1, the power law model cannot be rejected as a plausible fit for the data. If, instead,

p Value is small (e.g., p < 0.05) then the null hypothesis of a power law model can be rejected.

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