Word Learning as Network Growth: A Cross-linguistic Analysis

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Abstract

Children tend to produce words earlier when they are connected to a variety of other words 15 along both the phonological and semantic dimensions. Though this connectivity effect has 16 been extensively documented, little is known about the underlying developmental 17 mechanism. One view suggests that learning is primarily driven by a network growth model 18 where highly connected words in the child's early lexicon attract similar words. Another 19 view suggests that learning is driven by highly connected words in the external learning 20 environment, instead of highly connected words in the early internal lexicon. The present 21 study tests both scenarios systematically in both the phonological and semantic domains 22 across 10 languages. We show that external connectivity in the learning environment drives 23 growth in both production- and comprehension-based vocabularies, even controlling for word frequency and length. This pattern of findings suggests a word learning mechanism where 25 children harness their statistical learning abilities to detect and learn highly connected words in the learning environment.

Keywords: Language understanding; audio-visual processing; word learning; speech perception; computational modeling.

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Introduction

What factors shape vocabulary learning over the course of early childhood? To 32 investigate this question, scientists have adopted multiple research strategies, from 33 conducting controlled laboratory experiments (e.g. Markman, 1990) to analyzing dense corpora capturing language learning in context (e.g., B. C. Roy, Frank, DeCamp, Miller, & Roy, 2015). One strategy consists in documenting the timeline of words' acquisition, and studying the properties that make words easy or hard to learn. For example, within a lexical 37 category, words that are more frequent in child-directed speech are acquired earlier (J. C. Goodman, Dale, & Li, 2008). Other factors include word length and the mean length of 39 utterances in which the word occurs (e.g., Braginsky, Yurovsky, Marchman, & Frank, 2016; 40 Swingley & Humphrey, 2018). 41 Besides these word-level properties, the structure of the lexicon (that is, how words 42 relate to one another) also predicts the Age of Acquisition (AoA) of words. The lexical structure can be characterized in terms of a network where each node represents a word in the vocabulary, and each link between two nodes represents a relationship between the corresponding pair of words (e.g., Collins & Loftus, 1975). Previous studies have investigated early vocabulary structure by constructing networks using a variety of word-word relations including shared semantic features (McRae, Cree, Seidenberg, & McNorgan, 2005), target-cue relationships in free association norms (Nelson, McEvoy, & Schreiber, 1998), co-occurrence in child directed speech (MacWhinney, 2014), and phonological relatedness Vitevitch, 2008). These studies have generally found that children tend to produce words that have higher neighborhood density (i.e., high connectivity in the network) earlier, both at the phonological and the semantic level (Carlson, Sonderegger, & Bane, 2014; Hills, Maouene, Riordan, & Smith, 2010; Hills, Maouene, Maouene, Sheya, & Smith, 2009; Stella, Beckage, & Brede, 2017; Storkel, 2009). While most studies have focused on the static properties of the lexical network, a few

have investigated the underlying developmental process. In particular, Steyvers and
Tenenbaum (2005) suggested that the observed effects of connectivity are the consequence of
how the lexical network gets constructed in the child's mind. According to this explanation,
known as Preferential Attachment, highly connected words in the child's lexicon tend to
"attract" more words over time, in a rich-get-richer scenario (Barabasi & Albert, 1999). In
other words, what predicts word learning is the *internal* connectivity in the child's early
lexicon. In contrast, Hills et al. (2009) suggested that what biases the learning is not the
connectivity in the child's internal lexicon but, rather, *external* connectivity in the learning
environment. They called this alternative explanation Preferential Acquisition. For clarity of
reading, we will call preferential attachment the Internally-driven mechanism (INT), and
preferential acquisition the Externally-driven mechanism (EXT). Figure 1 shows an
illustration of both growth scenarios with the same simplified network.

These two proposals represent two divergent ideas about the role of lexical networks in 69 acquisition. On the INT proposal, learning is driven by known words with high connectivity 70 to other known words (Figure 1, left). Thus, the network structure is a causal factor in early 71 word learning, that is, children rely on the organization of their past knowledge to determine 72 future learning. For example, having a rich and organized knowledge about the domain of dinosaurs would facilitate the acquisition of new dinosaur-related words (Chi & Koeske, 1983). In contrast, on the EXT approach, learning is driven by the connectivity of words that are not known yet (Figure 1, right). Thus, the relevant network structure is not internally represented by children, and the observed connectivity effect might be an epiphenomenon of 77 some properties of the linguistic input. For example, highly connected words in the input 78 could be more easily learned because of their contextual diversity (e.g., Smith & Yu, 2008) or because caregivers emphasize such words in child-directed speech (MacWhinney, 2014).

Hills et al. (2009) investigated the growth of lexico-semantic networks in toddlers and found that growth did not proceed according to INT as was originally hypothesised by

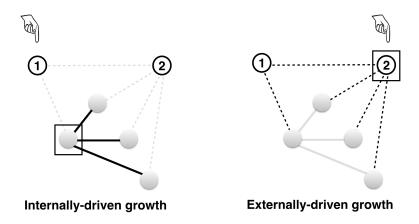


Figure 1. Illustration of the two growth scenarios. Filled grey circles represent known words (Internal) at a certain point in time. The empty, numbered circles represent words that have not yet been learned (External) and which are candidates to enter the lexicon next. The identity of the word that is going to be learned depends on the growth scenario. Here the squares indicate the node that drives growth in each scenario and the hand pointer indicates which word is likely to be learned. For INT, the utility of a candidate, external node is the average degree (i.e., number of links) of the internal nodes that it would attach to. Thus, according to INT, the node 1 is more likely to enter the lexicon. For EXT, the utility of a candidate node is its degree in the entire network. According to EXT, the node 2 is more likely to enter the lexicon next.

- Steyvers and Tenenbaum (2005), but rather according to EXT. This is a profound finding
- because it suggests that learning in the early stages is mostly driven by properties of the
- external input, regardless of how past knowledge is organized. However, this work has been
- done in the special case of networks that are based on 1) semantic associations, 2)
- production-based vocabularies, and 3) data from English-learning children, only. The extent
- to which this result depends on the domain (e.g., semantic vs. phonological connectivity),

<sup>&</sup>lt;sup>1</sup>Besides INT and EXT, the authors tested a third mechanism (called the lure of associates) which resembles EXT in that it is driven by the connectivity of external nodes, except that this connectivity is computed with respect to words that are known. However, EXT is the externally-driven scenario that best predicted the data in this previous work.

the vocabulary measure (production vs. comprehension) and culture/language is still unclear.
In this work, we test the generality of the finding along these three dimensions.

First, we study the phonological network in addition to the semantic network. These 91 two networks represent different ways the mental lexicon is structured (Beckage & Colunga, 2016). In particular, words that are neighbors in the semantic network (e.g., "cat", "dog") 93 are not necessarily neighbors in the phonological network, and vice versa. Does the phonological network also predict word learning? Previous work did find an effect of words' connectivity in the phonological network on their age of learning (Carlson et al., 2014; Stella et al., 2017; Storkel, 2009). In other words, words learned earlier in life tend to sound similar 97 to many other words than a word learned later in life. However, this finding is a priori compatible with both INT and EXT, and previous studies did not explicitly compare these two mechanisms. Here, we investigate whether phonological networks, like semantic 100 networks, grow through EXT, or if they rather grow via INT (Figure 1). 101

Second, we study vocabularies measured using both comprehension and production. 102 Previous studies have found differences between these vocabularies in terms of their content 103 and rate of acquisition (Benedict, 1979; Fenson et al., 1994). These differences may reflect 104 the fact that comprehension and production do not share the same constraints. For instance, 105 whereas comprehension depends on the ease with which words are stored and accessed, 106 production depends, additionally, on the ease with which words are articulated, e.g., shorter words are produced earlier (Braginsky et al., 2016). By investigating comprehension-based vocabularies, we assess the extent to which the network growth mechanism captures general 109 learning patterns beyond the specific constraints of production. 110

Finally, we use developmental data in 10 languages. Lexical networks can show more or less cross-linguistic variability along both the semantic and phonological domains (Arbesman, Strogatz, & Vitevitch, 2010; Youn et al., 2016). Besides, cultures might differ in the way caregivers talk to children (Cristia, Dupoux, Gurven, & Stieglitz, 2017; Kuhl et al., 1997), and this difference in the input could influence the way in which the children's networks

grow. Thus, Cross-linguistic comparison is crucial to test what growth mechanism is
cognitively universal and is used by all children, and what mechanism is specific to some
patterns of learning that emerge due to the particulars of a given language or culture (Bates
MacWhinney, 1987; Slobin, 2014).

We test the growth scenarios using parent reports of children vocabularies and their 120 normative age of acquisition (Fenson et al., 1994). Children may vary in their individual 121 learning trajectories, but the aggregate data leads to an average learning pattern which is 122 highly consistent. It is this normative trajectory that we model in the current study, 123 following in this regard the steps of previous research using similar datasets (Braginsky et al., 2016; J. C. Goodman et al., 2008; Hills et al., 2010, 2009; Stella et al., 2017; Storkel, 2009) The paper is organized as follows. First, we describe the datasets we used and explain 126 how we constructed the networks. Second, we analyze static properties of words' connectivity 127 in these networks (correlation with age of acquisition and shape of the distribution) and we 128 explain how these properties infom hypotheses about network growth. Next, we explicitly fit 129 the two hypothesized growth mechanisms to the data. We investigate the extent to which 130 the results obtained in Hills et al. (2009) generalize to phonological networks and 131 comprehension-based vocabularies, and whether this generalization holds cross-linguistically. 132

Networks Networks

#### 134 Data

We used data from Wordbank (Frank, Braginsky, Yurovsky, & Marchman, 2017), an open repository aggregating cross-linguistic language developmental data of the MacArthur-Bates Communicative Development Inventory (CDI), a parent report vocabulary checklist. Parent report is a reliable and valid measure of children's vocabulary that allows for the cost-effective collection of datasets large enough to test network-based models of acquisition (Fenson et al., 1994). When filling out a CDI form, caregivers are either invited to indicate whether their child "understands" (comprehension) or "understands and says"

(production) each of about 400-700 words. For younger children (e.g., 8 to 18 months in the English data), both comprehension and production are queried, whereas for older children (16 to 36 months) only production is queried. Due to these limitations, we use data from younger children to test comprehension and data from older children to test production. Following previous studies (Hills et al., 2009; Storkel, 2009), we restrict our analysis to nouns. Table 1 gives an overview of the data we used.

## $^{148}$ Age of acquisition

For each word in the CDI data, we compute the proportion of children who understand or produce the word at each month. Then we fit a logistic curve to these proportions and determined when the curve crosses 0.5, i.e., the age at which at least 50% of children know the word. We take this point in time to be each word's age of acquisition (Braginsky et al., 2016; J. C. Goodman et al., 2008).

### 154 Semantic networks

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We constructed semantic networks for English data following the procedure outlined in 155 Hills et al. (2009), as follows. We used as an index of semantic relatedness the Florida Free 156 Association Norms (Nelson et al., 1998). This dataset was collected by giving adult 157 participants a word (the cue), and asking them to write the first word that comes to mind 158 (the target). For example, when given the word "ball", they might answer with the word 159 "game". A pair of nodes were connected by a directed link from the cue to the target if there 160 was a cue-target relationship between these nodes in the association norms. The connectivity 161 of a given node was characterized by its *indegree*: the number of links for which the word was the target. To model growth from month to month, we constructed a different network at each month, based on the words that have been acquired by that month. 164 Since the free association norms are available only in English, we used the 165 hand-checked translation equivalents available in Wordbank, which allowed us to use the 166

English association norms across 10 languages. Using the same association data across

Table 1
Statistics for the dataset we used.

	Comprehension		Production		
Language	Nouns	Ages	Nouns	Ages	
Croatian	209	8-16	312	16-30	
Danish	200	8-20	316	16-36	
English	209	8-18	312	16-30	
French	197	8-16	307	16-30	
Italian	209	7-24	312	18-36	
Norwegian	193	8-20	316	16-36	
Russian	207	8-18	314	18-36	
Spanish	208	8-18	312	16-30	
Swedish	205	8-16	339	16-28	
Turkish	180	8-16	297	16-36	

languages does not necessarily lead to similar networks. Indeed, though this approximation assumes that the semantic similarity measure is universal—which is a reasonable approximation (e.g., Youn et al., 2016), the set of words acquired by children as well as the timeline of this acquisition can still vary from language to language leading to possibility different learning strategies.

### Phonological networks

To construct phonological networks we first mapped the orthographic transcription of
words to their International Phonetic Alphabet (IPA) transcriptions in each language, using
the open source text-to-speech software Espeak. We used the Levenshtein distance (also
known as edit distance) as a measure of phonological relatedness between two nodes. The
measure counts the minimum number of operations (insertions, deletions, substitutions)

179 required to change one string into another.

In previous studies, two nodes were linked if they had an edit distance of 1 (Carlson et al., 2014; Stella et al., 2017; Storkel, 2009). However, these studies reported a contribution of phonological connectivity to word learning when networks were built using a rich adult vocabulary. Since the focus of the current study is on the mechanism of growth, the networks should be based on the children's early vocabulary. The latter, nevertheless, contains very few word pairs with an edit distance of 1. Thus, we increased the threshold from 1 to 2, that is, two nodes were related if their edit distance was equal to 1 or 2.2 The connectivity of a given node was characterized with its degree: the number of links it shares with other words.

188 Analysis

### 189 Static properties of the global network

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We start by analyzing word connectivity in the global (static) network. We constructed 190 this network using nouns learned by the oldest age for which we have CDI data (e.g., in 191 English this corresponds, in comprehension, to the network by 18 months, and in production, 192 to the network by 30 months). This global network is the end-state towards which both INT 193 and EXT converge by the last month of learning. Moreover, following Hills et al. (2009), we 194 used this end-state network as a proxy for the external connectivity in the learning 195 environment. Below we analyze properties of this global networks that may a priori hint at 196 an INT- or EXT-like growth. In order to compare various predictors on the same data, we 197 restrict the analysis to the subset of nouns for which we had both semantic and phonological 198 information in each language. 199

Connectivity predicts the age of acquisition. Connectivity in the global network is directly related to EXT as it represents the explicit criterion this growth scenario

<sup>&</sup>lt;sup>2</sup>We also considered the case of an edit distance of 1 as well as the continuous measure, i.e., the inverse edit distance without threshold. In both cases, the results were weaker that those obtained with a threshold of 2.

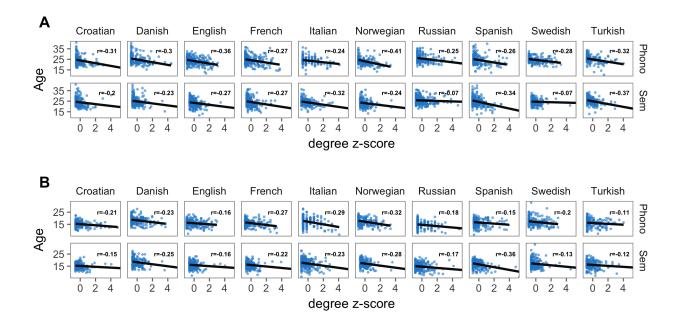


Figure 2. Age of production (A) and comprehension (B) in the global network as predicted by the degree (i.e., connectivity) in this network. Results are shown in each language for phonological and semantic networks. Each point is a word, with lines indicating linear model fits, and numbers indicating the Pearson correlation coefficients.

uses to determine what words should be learned first (Figure 1). Therefore, a direct consequence of an EXT-like growth scenario is a correlation between connectivity in the 203 global network and the age of acquisition. This correlation is also compatible with INT, 204 although the causality is reversed: higher connectivity in the global network is caused by earlier learning, not the other way around. Some words end up being highly connected in the 206 global network precisely because they happen to be acquired earlier and, therefore, have a 207 higher chance of accumulating more links over time. Thus, the correlation between 208 connectivity in the end-state network and AoA is an important blueprint of both EXT and 209 INT. If there is no such correlation, neither growth scenarios can be posited as a possible 210 learning mechanism. 211

Figure 2 shows how the age of production and comprehension for each word varies as a function of its degree (or indegree for the semantic networks) as well as the correlation values.

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For ease of visual comparison, the predictor (i.e., the degree) was centered and scaled across languages. The plots show, overall, a negative correlation between the month of acquisition 215 and the degree. In production data, the average correlation across languages was -0.24 216 (SD=0.10) for the semantic networks and -0.30 (SD=0.05) for the phonological networks. In 217 comprehension data, the average correlation was -0.21 (SD=0.08) for the semantic networks 218 and -0.21 (SD=0.07) for the phonological networks. These results indicate that nouns with 219 higher degrees are generally learned earlier, thus replicating previous findings in English (e.g., 220 Storkel 2004, 2009; Hills et al. 2009) and extending these findings to 10 different languages, 221 generally, in both production- and comprehension-based vocabularies. 222

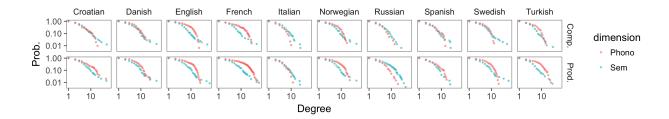


Figure 3. Log-log plot of the cumulative degree distribution function for the global phonological and semantic networks across languages. The figure shows the results for both production and comprehension data. A perfect power-law distribution should appear as a straight line in this graph.

Power-law degree distribution. We also analyzed the global network's degree 223 distribution. The shape of this distribution is particularly relevant to INT as this growth 224 scenario is known to generate networks with a power-law degree distribution, i.e., a 225 distribution of the form  $p(k) \propto \frac{1}{k^{\alpha}}$  (Barabasi & Albert, 1999). If the end-state network displays this property, this fact would suggest, but not prove, an INT-like generative process. 227 If, however, the degree distribution is very different from a power law, this would significantly weaken the case for INT. The log-log plots are shown in Figure 3. We fit a 229 power law to each empirical degree distribution following the procedure outlined in Clauset, 230 Shalizi, and Newman (2009) and using a related R package (poweRlaw, Gillespie, 2015). 231

Table 2
Results of fitting a power law model to the degree (i.e., connectivity) distribution in each model for production data. Numbers indicate the cut-off degree, the scaling parameter alpha, and the p-value which quantifies the plausibility of the power law hypothesis. If the p-value is close to 1, a power law cannot be rejected as a plausible fit for the data.

	Phono.			Sem.		
Language	cut-off	alpha	p-value	cut-off	alpha	p-value
Croatian	4	2.18	0.123	4	2.55	0.881
Danish	11	4.55	0.858	4	2.38	0.001
English	20	9.14	0.511	5	2.66	0.132
French	20	3.75	0.112	8	2.81	0.133
Italian	9	9.45	0.780	4	2.93	0.608
Norwegian	15	6.28	0.744	5	2.88	0.201
Russian	8	4.20	0.541	24	5.61	0.723
Spanish	13	8.75	0.736	4	2.98	0.460
Swedish	11	4.68	0.103	4	2.49	0.171
Turkish	8	3.26	0.375	4	2.87	0.925

In brief, the analysis consisted in two steps. First, we derived the optimal cut-off,  $k_{min}$ , above which the distribution is more likely to follow a power law,<sup>3</sup> and we estimate the corresponding scaling parameter  $\alpha$ . Second we calculated the goodness-to-fit, which resulted in a p-value quantifying the plausibility of the model. The results are shown in Table 2 for production data, and in Table 3 for comprehension data.

Overall, we could not reject the null hypothesis of a power-law distribution: The *p*-value was generally above 0.1 in almost all languages for both production and

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<sup>&</sup>lt;sup>3</sup>In natural phenomena, it is often the case that the power law applies only for values above a certain minimum.

Table 3
Results of fitting a power law model to the degree distribution in each model for comprehension data. Numbers indicate the cut-off degree, the scaling parameter alpha, and the p-value which quantifies the plausibility of the power law hypothesis. If the p-value is close to 1, a power law cannot be rejected as a plausible fit for the data.

	Phono.			Sem.		
Language	cut-off	alpha	p-value	cut-off	alpha	p-value
Croatian	2	2.06	0.020	5	2.67	0.895
Danish	5	2.98	0.136	4	2.39	0.005
English	13	5.16	0.235	4	2.64	0.765
French	18	5.58	0.336	4	2.63	0.330
Italian	8	10.27	0.909	4	2.88	0.688
Norwegian	13	7.65	0.440	5	2.87	0.433
Russian	5	3.97	0.854	8	3.91	0.952
Spanish	5	3.01	0.085	5	3.11	0.552
Swedish	9	6.75	0.102	5	2.81	0.713
Turkish	9	5.73	0.958	4	3.13	0.887

comprehension. That said, phonological networks had relatively larger cut-offs than semantic
networks. As was suggested by Arbesman et al. (2010), these "truncated" power-laws in
phonological networks —as well as the cross-linguistic variability in the value of the cut-offs—
may reflect the various constraints that exist on word formation such as the number of
phonemes in the language, the phonotactics (i.e., the way sound sequences are arranged in
words), and the length of words. Such constraints may limit the number of words that are
phonologically similar, thus leading to distributions which decay faster than a non-truncated
power law.

In sum, the static properties of the end-state network are *a priori* compatible with both INT and EXT. In order to decide between these two developmental scenarios, we need to fit explicit growth models to the data.

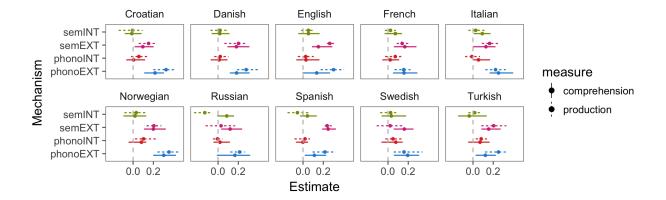


Figure 4. Evaluation of growth scenarios (EXT: externally-driven, INT: internally-driven) for both semantic and phonological networks. Each point represents the mean of the posterior distribution of the growth parameter, with ranges representing 95% credible intervals. Positive values mean that learning proceeds according to the predictions of the growth scenario, whereas negative values mean that learning proceeds in opposition to the predictions of the growth scenario.

#### 50 Network growth models

To test the network growth scenarios, we fit two growth models to the data. We calculated the probability that a word  $w_i$ , with a utility value  $u_i$  would enter the lexicon at a given month, using a softmax function:

$$p(w_i) = \frac{e^{\beta u_i}}{\sum_j e^{\beta u_j}} \tag{1}$$

where  $\beta$  is a fitted parameter that captures the magnitude of the relationship between network parameters and growth (analogous to a regression coefficient). A positive value of  $\beta$ 

means that words with higher utility values  $u_i$  are acquired first, and a negative value means 256 that words with lower utility values are acquired first (see Figure 1 for an illustration of how 257 utilities values  $u_i$  are defined in each growth scenario). The normalization includes all words 258 that could be learned at that month. 259

We estimated the parameter  $\beta$  using a Bayesian approach. The inference was 260 performed using the probabilistic programming language WebPPL (N. Goodman & 261 Stuhlmuller, 2014). We defined a uniform prior over  $\beta$ , and at each month, we computed the 262 likelihood function over words that could possibly enter the lexicon at that month, fit to the 263 words that have been learned at that month (using formula 1). Markov Chain Monte Carlo sampling resulted in a posterior distribution over  $\beta$ , which we summarized in Figure 4. 265 First, the results replicate Hills et al.'s original finding regarding the semantic network 266 in English and the production-based vocabulary, which is that this network grows by EXT, 267 not by INT. Second, our results show that, generally speaking, this finding generalizes to 268 comprehension-based vocabulary, and holds across languages. This generalization was 269 obtained in both the semantic<sup>4</sup> and phonological domains.

## Comparison to other predictors of age of acquisition

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Above we showed that the way semantic and phonological information is structured in 272 the learning environment contributes to noun learning (via EXT) across languages. However, 273 we know that other factors influence learning as well (e.g., Braginsky et al., 2016). Next we 274 investigated how semantic and phonological connectivity interact with two other factors. 275 The first one is word frequency, a well studied factor shown to predict the age of acquisition 276 in a reliable fashion (e.g. J. C. Goodman et al., 2008). The second factor is word length, 277 which was shown to correlate with phonological connectivity: Shorter words are more likely 278 <sup>4</sup>One could imagine that the fact of using English free association norms cross-linguistically would decrease the effect of non-English semantic networks because of possible cultural differences. However, our findings do not support this assumption, rather it supports our initial approximation about the universality of the semantic similarity measure.

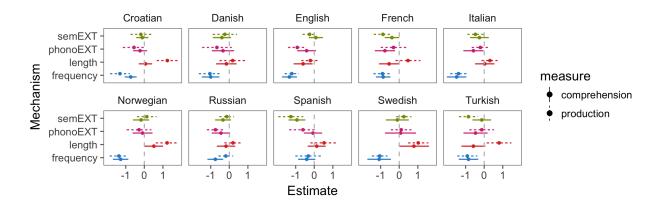


Figure 5. Estimates of the relative contribution of each predictor of AoA in the regression model in each language. Results are shown for both production and comprehension data. Ranges indicate 95% confidence intervals. Positive values indicate a positive relationship (e.g. longer words tend to have a higher AoA), while negative values indicate a negative relationship (e.g. words with higher frequency tend to have a lower AoA).

to have higher connectivity (Pisoni, Nusbaum, Luce, & Slowiaczek, 1985; Vitevitch & Rodríguez, 2005).

Since we found INT to be uninformative, we dropped it from this analysis, keeping
only EXT. This simplified the model because we no longer needed to fit growth
month-by-month. The latter was a requirement only for INT where the words' utilities
varied from month to month, depending on how connectivity changed in the growing internal
network. A more direct way to assess and compare the contribution of EXT in relation to
other word-level factors is through conducting linear regressions, where connectivity in the
learning environment, frequency and length predict the age of acquisition.

For word length, we counted the number of phonemes in our generated IPA transcription. For word frequency, we used the frequency estimates from Braginsky et al. (2016) where unigram counts were derived based on CHILDES corpora in each language (MacWhinney, 2014). For each word, counts included words that shared the same stem (e.g., "cats" counts as "cat"), or words that were synonymous (e.g. "father" counts as "daddy").

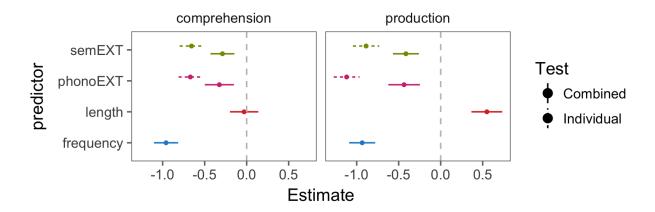


Figure 6. Estimates of the relative contribution of each predictor of AoA in the combined mixed-effects model with language as a random effect. Results are shown for both production and comprehension data. Ranges indicate 95% confidence intervals. Dotted ranges indicate the estimates for the predictor in a separate model that includes only this predictor as a fixed effect.

Although these frequency counts use transcripts from independent sets of children, they are based on large samples, and this allows us to average out possible differences between children and the specificities of their input (see J. C. Goodman et al., 2008).

We conducted two analyses. We fit a linear regression for each language, and we fit a linear mixed-effect model to all the data pooled across languages, with language as a random effect. Figure 5 shows the coefficient estimate for each predictor in each language for production and comprehension data. Figure 6 shows the coefficient estimates for all languages combined (all predictors were centered and scaled).

The findings for the new predictors were as follows. Overall, frequency is the largest and most consistent predictor of age of acquisition in both comprehension and production data and across languages, endorsing results for nouns across a variety of analyses (Braginsky et al., 2016; J. C. Goodman et al., 2008; B. C. Roy et al., 2015). Word length is more predictive for production than comprehension (and this difference is very clear in the

global model), replicating previous work (Braginsky et al., under review). Thus, word length seems to reflect the effects of production's constraints rather than than comprehension's constraints, i.e., longer words are harder to articulate but they may not be significantly more difficult to store and access.

As for the factors of interest, i.e., semantic and phonological connectivity, we found 310 cross-linguistic differences. Connectivity contributes to learning in some languages but not in 311 other. In particular, semantic connectivity does not explain variance in English data beyond 312 that explained by phonological connectivity, frequency and length. This contrasts with the 313 original finding in Hills et al. (2009). However, this might be due to our using a slightly 314 different model (which included word length as a covariate) and a larger dataset. That said, 315 and despite these apparent cross-linguistic differences, both phonological and semantic 316 connectivity are significant predictors in the combined model (Figure 6). 317

318 Discussion

This study provided an analysis of network growth during development. We compared 319 two network growth scenarios described in the pioneering work of Steyvers and Tenenbaum 320 (2005) and Hills et al. (2009). The first scenario, INT (originally called Preferential 321 Attachment), described a rich-get-richer network growth model in which the current 322 structure of the learner's internal network determines future growth; the other, EXT 323 (originally called Preferential Acquisition) described a model in which the external, global 324 environmental network structure determines learners' growth patterns. These two 325 mechanisms represent two fundamentally different accounts of lexical growth: One suggests that future word knowledge is primarily shaped by the children's past knowledge and its organization, whereas the other suggests that learning is shaped, rather, by salient properties in the input regardless of how past knowledge is organized. The present study tested the 329 generality of previous findings (Hills et al., 2010, 2009) by 1) investigating phonological 330 networks together with semantic networks, 2) testing both comprehension- and 331

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production-based vocabularies, and 3) comparing the results across 10 languages.

We found that the original findings reported in Hills et al. (2009) generalize well across 333 all these dimensions. First, just like semantic networks, phonological networks grow via the 334 externally-driven scenario (EXT), not by the internally-driven mechanism (INT). Second, 335 comprehension-based vocabularies grow in a way similar to production-based vocabularies. 336 Finally, the findings were, overall, similar across the 10 languages we tested. Although we 337 find some cross-linguistic variation when semantic and phonological networks were pitted against frequency and length, this variability is to be taken with a grain of salt as it might be exaggerated in our study by the limited and partially-overlapping sample of nouns for each language. In fact, both phonological and semantic connectivity are significant 341 predictors above and beyond frequency and length when data are pooled across languages. 342

These findings corroborate the hypothesis that children start by learning words that have high similarity to a variety of other words in the learning environment, not in the child's available lexicon. This hypothesis implies that children are sensitive to highly connected words although they do not initially have access to the full network, thus raising some important questions: What mechanism allows children to distinguish highly connected words from other words? Besides, why would highly connected words be easier to learn?

One possibility is that these patterns emerge from children's use of statistical learning abilities (Aslin & Newport, 2012; Saffran, Aslin, & Newport, 1996; Smith & Yu, 2008). The term "statistical learning" has been used in the developmental literature to describes the process by which one acquires information about their environment through tracking the frequency distribution of some elements (e.g., words) in different contexts. An important property of this kind of learning is that it occurs without explicit instructions and through mere exposure to the input. Previous work in the line of research has documented specific mechanisms which can explain the patterns found in the current study.

For example, in the semantic domain, growth according to EXT can be explained by a mechanism similar to cross-situational learning (Pinker, 2013; Smith & Yu, 2008; Yurovsky

& Frank, 2015). According to this mechanism, children track the co-occurrence of concrete 359 nouns with their possible semantic referents. The referent of a word heard in only one 360 naming situation can be ambiguous (e.g., when the word "ball" is heard for the first time in 361 the presence of both a ball and a chair), but hearing the same word in a diversity of 362 semantic contexts allows the learner to narrow down the set of possible word-object 363 mappings. In our case, free association (used to determine semantnic network connectivity) 364 is related to contextual co-occurrence (Fourtassi & Dupoux, 2013; Griffiths, Stevyers, & 365 Tenenbaum, 2007), meaning that highly connected words will tend to occur in a variety of speech and referential contexts. This fact makes such words easier to learn because they 367 have more referential disambiguating cues across learning contexts. Crucially, children can 368 learn these words without knowing the other words with witch they co-occur (hence the 369 similarity with EXT). This possibility is supported by the finding that words' diversity of occurrence in child directed speech predicts their age of learning (Hills et al., 2010). 371

In the phonological case, network growth according to EXT is also compatible with a 372 scenario whereby children are tracking lwo level statistical patterns, e.g., high probability 373 sound sequences. Indeed, connectivity in the phonological network is inherently correlated 374 with phonotactic probability (Vitevitch, Luce, Pisoni, & Auer, 1999). That is, highly connected words tend to be made of frequent sound sequences. Children are sensitive to 376 local phonotactic regularities (Jusczyk, Luce, & Charles-Luce, 1994) and this sensitivity might lead them to learn higher-probability words more easily (Storkel, 2001). This 378 explanation is supported by computational simulations that show how learning general 379 phonotactics patterns create "well-worn paths" which allow the models to represent several 380 distinct but phonologically neighboring words (Dell, Juliano, & Govindjee, 1993; Takac, 381 Knott, & Stokes, 2017). 382

Besides using their own statistical learning skills, children could also benefit from the way their caregivers speak. Perhaps the caregivers put more emphasis on the words that are highly connected in *their* mature lexical network. This emphasis would guide children to

learn first these highly connected words even though children do not have access to the
distribution of words' connectivity in the final network. Investigating this possibility would
require further research on caregiver-child interaction (MacWhinney, 2014; B. C. Roy et al.,
2015), examining what words are introduced over development and the extent to which
children's uptake is influenced by this input (Clark, 2007; Hoff & Naigles, 2002).

This work shares a number of limitations with previous studies using similar research 391 strategy and datasets. Chief among these limitations is the fact that the age of word 392 acquisition is computed using different children at different ages (due to the fact that 393 available CDI data is mainly cross-sectional). Although this measure has proven highly 394 consistent (Fenson et al., 1994), it led us to focus on studying the learning mechanism of the 395 "average" child. Individual trajectories, however, could lead to different netwtok strutures 396 and show different learning patterns. For example, using longitudinal data Beckage, Smith, 397 and Hills (2011) found differences between typical and late talkers in terms of the semantic 398 network structure. Besides, although our study endorses the externally-driven account of 399 network growth, this does not mean individual children never use some variant of INT or 400 some combination of both INT and EXT (Beckage and Colunga, under review). For 401 example, some children develop "islands of expertise", that is, well organized knowledge 402 about a certain topic (e.g., birds or dinosaurs). This prior knowledge enables these children 403 to learn new related words more easily (e.g., Chi & Koeske, 1983).

To conclude, our work validates and generalizes previous results in early network
development. It suggests that the advantage of highly connected words may result, at least
in the early stages of word learning, from the operation of simpler mechanisms in both the
semantic and phonological domains. One question for future experimental work is whether
such correlational patterns of growth can be produced in controlled behavioral experiments.

All data and code for these analyses are available at https://github.com/afourtassi/networks 411

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