- The growth of children's semantic and phonological networks: insight from 10 languages
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Abstract

Children tend to produce words earlier when they are connected to a variety of other words 15 along the phonological and semantic dimensions. Though these semantic and phonological 16 connectivity effects have been extensively documented, little is known about their underlying 17 developmental mechanism. One possibility is that learning is driven by lexical network 18 growth where highly connected words in the child's early lexicon enable learning of similar 19 words. Another possibility is that learning is driven by highly connected words in the 20 external learning environment, instead of highly connected words in the early internal 21 lexicon. The present study tests both scenarios systematically in both the phonological and 22 semantic domains across 10 languages. We show that phonological and semantic connectivity 23 in the learning environment drives growth in both production- and comprehension-based vocabularies, even controlling for word frequency and length. This pattern of findings 25 suggests a word learning process where children harness their statistical learning abilities to detect and learn highly connected words in the learning environment. 27

Keywords: Word learning; semantic network; phonological network; network growth; cross-linguistic analysis.

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Introduction

What factors shape vocabulary learning over the course of early childhood? To
investigate this question, scientists have adopted multiple research strategies, from
conducting controlled laboratory experiments (e.g. Markman, 1990) to analyzing dense
corpora capturing language learning in context (e.g., Roy, Frank, DeCamp, Miller, & Roy,
2015). One prominent strategy consists in documenting the timeline of words' acquisition
and studying the properties that make words easy or hard to learn (e.g., Goodman, Dale, &
Li, 2008; Huttenlocher, Haight, Bryk, Seltzer, & Lyons, 1991). For example, Goodman et al.
(2008) found that, within a lexical category (e.g., nouns), higher parental frequency is
associated with earlier learning. Researchers have studied the role of several other factors
such as word length and the mean length of utterances in which the word occurs (e.g.,
Braginsky, Yurovsky, Marchman, & Frank, 2019; Swingley & Humphrey, 2018).

Besides word-level properties, the structure of the lexicon (that is, how words relate to
one another) is also linked to the Age of Acquisition (AoA) of words. The lexical structure
can be characterized in terms of a network where each node represents a word in the
vocabulary, and each link between two nodes represents a relationship between the
corresponding pair of words (e.g., Collins & Loftus, 1975; Luce & Pisoni, 1998). Previous
studies have investigated early vocabulary structure by constructing networks using a variety
of word-word relations including shared semantic features (McRae, Cree, Seidenberg, &
McNorgan, 2005), target-cue relationships in free association norms (Nelson, McEvoy, &
Schreiber, 1998), co-occurrence in child-directed speech (MacWhinney, 2014), and
phonological relatedness (Vitevitch, 2008). These studies have generally found that children
tend to produce words that have higher neighborhood density (i.e., high connectivity in the
network) earlier, both at the phonological and the semantic level (Carlson, Sonderegger, &
Bane, 2014; Hills, Maouene, Riordan, & Smith, 2010; Hills, Maouene, Maouene, Sheya, &

56 Smith, 2009; Stella, Beckage, & Brede, 2017; Storkel, 2009).

While most studies have focused on the static properties of the lexical network, a few have investigated the underlying developmental process. In particular, Steyvers & Tenenbaum (2005) suggested that the observed effects of connectivity are the consequence of how the lexical network gets constructed in the child's mind. According to this explanation, known as Preferential Attachment, highly connected words in the child's lexicon tend to "attract" more words over time, in a rich-get-richer scenario (Barabasi & Albert, 1999). In other words, what predicts learning is the internal connectivity in the child's early lexicon. In contrast, Hills et al. (2009) suggested that what biases the learning is not the connectivity in the child's internal lexicon but, rather, external connectivity in the learning environment. They called this alternative explanation Preferential Acquisition. For clarity of reading, we will call preferential attachment the Internally-driven mechanism (INT), and preferential acquisition the Externally-driven mechanism (EXT). Figure 1 shows an illustration of both growth scenarios with the same simplified network.

These two proposals represent two divergent ideas about the role of lexical networks in acquisition. On the INT proposal, learning is driven by known words with high connectivity to other known words (Figure 1, left). Thus, the network structure is a causal factor in word learning, that is, children rely on the organization of their past knowledge to determine future learning (Altvater-Mackensen & Mani, 2013; Borovsky, Ellis, Evans, & Elman, 2016; Chi & Koeske, 1983; Storkel, 2009). In contrast, on the EXT approach, learning is driven by the connectivity of words that are not known yet (Figure 1, right). Thus, the relevant network structure is not internally represented by children, and the observed connectivity effect might be an epiphenomenon of some properties of the linguistic input. For example, highly connected concrete nouns in the input could be more easily learned because of their contextual diversity, allowing for easier meaning disambiguation (McMurray, Horst, & Samuelson, 2012; Smith & Yu, 2008; Yurovsky & Frank, 2015). Another reason could be

- that these words are emphasized by the caregivers in their child-directed speech (Clark, 2007;
- Hoff & Naigles, 2002; Huttenlocher et al., 1991).

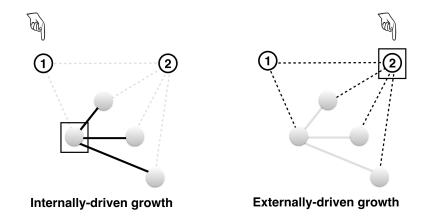


Figure 1. Illustration of the two growth scenarios. Filled grey circles represent known words (Internal) at a certain point in time. The empty, numbered circles represent words that have not yet been learned (External) and which are candidates to enter the lexicon next. The identity of the word that is going to be learned depends on the growth scenario. Here the squares indicate the node that drives growth in each scenario, and the hand pointer indicates which word is likely to be learned. For INT, the utility of a candidate external node is the average degree (i.e., number of links) of the internal nodes that it would attach to. In this simplified example, candidate node 1 would connect to an internal node with 3 connections; thus we have  $u_{INT}(node_1) = 3$ . As for candidate node 2, it would connect to internal nodes that have only one connection each, making an average of 1, i.e.,  $u_{INT}(node_2) = 1$ . According to INT, node 1 is more likely to enter the lexicon. For EXT, the utility of a candidate node is its degree in the entire network. In our example, candidate node 1 has 2 connections in total, whereas candidate node 2 has 5 connections. So we have  $u_{EXT}(node_1) = 2$  and  $u_{EXT}(node_2) = 5$ . Thus, according to EXT, node 2 is more likely to enter the lexicon next. This figure is based on an example from Hills et al. (2009).

Hills et al. (2009) investigated the growth of lexico-semantic networks in toddlers and found that growth did not proceed according to INT as was originally hypothesized by

Steyvers & Tenenbaum (2005), but rather according to EXT.<sup>1</sup> This is an important finding
because it suggests that learning in the early stages is mostly driven by properties of the
external input, regardless of how past knowledge is organized. However, this work explored
the INT/EXT growth in a special case: networks that were based on 1) semantic
associations, 2) production-based vocabularies, and 3) data from English-learning children,
only. The extent to which this result depends on the domain (e.g., semantic vs. phonological
connectivity), the vocabulary measure (production vs. comprehension) and culture/language
is thus an open area for investigation (Hills & Siew, 2018). In this work, we test the
generality of prior findings along these three dimensions.

First, we study the phonological network in addition to the semantic network. These 95 two networks represent different ways the mental lexicon is structured (Beckage & Colunga, 96 2016). In particular, words that are neighbors in the semantic network (e.g., cat, dog) are 97 not necessarily neighbors in the phonological network and vice versa. Does the phonological network also predict word learning? Previous work has found an effect of words' connectivity in the phonological network on their age of learning (Carlson et al., 2014; Stella et al., 2017; Storkel, 2009). In other words, words learned earlier in life tend to sound similar to many other words than a word learned later in life. However, this finding is a priori compatible 102 with both INT and EXT, and previous studies did not explicitly compare these two mechanisms. Here, we investigate whether phonological networks, like semantic networks, 104 grow through EXT, or if they rather grow via INT (Figure 1). 105

Second, we study vocabularies measured using both comprehension and production.

Previous studies have found differences between these vocabularies in terms of their content

<sup>&</sup>lt;sup>1</sup> Besides INT and EXT, the authors tested a third mechanism (called the lure of associates) which resembles EXT in that it is driven by the connectivity of external nodes, except that this connectivity is computed with respect to words that are known. However, EXT is the externally-driven scenario that best predicted the data in this previous work.

and rate of acquisition (Bates, Dale, & Thal, 1995; Benedict, 1979; Fenson et al., 1994). 108 These differences may reflect the fact that comprehension and production do not share the 109 same constraints. For instance, whereas comprehension depends on the ease with which 110 words are stored and accessed, production depends, additionally, on the ease with which 111 words are articulated, e.g., shorter words are produced earlier (Braginsky et al., 2019). By 112 investigating comprehension-based vocabularies, we assess the extent to which the network 113 growth mechanism captures general learning patterns beyond the specific constraints of 114 production. 115

Finally, we use developmental data in 10 languages. Lexical networks can show more or 116 less cross-linguistic variability along both the semantic and phonological domains (Arbesman, Strogatz, & Vitevitch, 2010; Lupyan & Lewis, 2017; Youn et al., 2016). Besides, cultures 118 might differ in the way caregivers talk to children (Cristia, Dupoux, Gurven, & Stieglitz, 119 2017; Kuhl et al., 1997), and this difference in the input could influence the way in which the 120 children's networks grow. Thus, cross-linguistic comparison is crucial to test the extent to 121 which growth mechanisms are equally engaged across a wider variety of cultures compared 122 with the extent to which the growth mechanisms are specific to patterns of learning that 123 emerge due to the particulars of a given language or culture (Bates & MacWhinney, 1987; 124 Slobin, 2014). 125

We adopted the following research strategy. We used parent reports on the

MacArthur-Bates Communicative Development Inventory and its cross-linguistic adaptations

(Fenson et al., 1994; Frank, Braginsky, Yurovsky, & Marchman, 2017). We studied the

timeline of word learning using the normative age of acquisition (i.e., the age at which at

least 50% of children know a given word). Our choice of studying the normative learning

trajectory rather than the individual trajectories was motivated by the nature of the dataset

used—which is primarily based on cross-sectional studies. Children may vary in their

individual learning trajectories, but the aggregate data provide highly robust measures of the

average learning patterns (Fenson et al., 1994). The use of such measures has lead to important insights on the mechanisms of word learning (Goodman et al., 2008; Hills et al., 2010, 2009; Stella et al., 2017; Storkel, 2009).

The paper is organized as follows. First, we describe the datasets we used and explain
how we constructed the networks. Second, we analyze static properties of words'
connectivity in these networks (correlation with age of acquisition and shape of the
distribution), and we explain how these properties inform hypotheses about network growth.
Next, we fit the two hypothesized growth mechanisms to the data. We investigate the extent
to which the results obtained in Hills et al. (2009) generalize to phonological networks and
comprehension-based vocabularies, and whether this generalization holds cross-linguistically.

Networks Networks

#### 145 Data

We used data from Wordbank (Frank et al., 2017), an open repository aggregating 146 cross-linguistic language developmental data of the MacArthur-Bates Communicative 147 Development Inventory (CDI), a parent report vocabulary checklist. Parent report is a 148 reliable and valid measure of children's vocabulary that allows for the cost-effective collection 149 of datasets large enough to test network-based models of acquisition (Fenson et al., 1994). 150 When filling out a CDI form, caregivers are either invited to indicate whether their child 151 "understands" (comprehension) or "understands and says" (production) each of about 152 400-700 words. For younger children (e.g., 8 to 18 months in the English data), both 153 comprehension and production are queried, whereas for older children (16 to 36 months) only production is queried. Due to these limitations, we use data from younger children to test comprehension and data from older children to test production. In addition, following 156 previous studies (Hills et al., 2009; Storkel, 2009), we restricted our analysis to the category 157 of nouns due to the fact that nouns predominate the early expressive and receptive lexicons 158 (Bates et al., 1995). Their larger sample size (compared, for example, to verbs or adjectives) 159

is more suited to the network-based analysis of development. Table 1 gives an overview of the data we used.

# 162 Age of acquisition

For each word in the CDI data, we compute the proportion of children who understand or produce the word at each month. Then we fit a logistic curve to these proportions and determined when the curve crosses 0.5, i.e., the age at which at least 50% of children know the word. We take this point in time to be each word's age of acquisition (Braginsky et al., 2019; Goodman et al., 2008).

Table 1
Statistics for the dataset we used. The ages are in months.

|           | Comprehension |      |       | Production |       |       |
|-----------|---------------|------|-------|------------|-------|-------|
| Language  | Nouns         | Ages | N     | Nouns      | Ages  | N     |
| Croatian  | 209           | 8-16 | 250   | 312        | 16-30 | 377   |
| Danish    | 200           | 8-20 | 2,398 | 316        | 16-36 | 3,714 |
| English   | 209           | 8-18 | 2,435 | 312        | 16-30 | 5,520 |
| French    | 197           | 8-16 | 537   | 307        | 16-30 | 827   |
| Italian   | 209           | 7-24 | 648   | 312        | 18-36 | 752   |
| Norwegian | 193           | 8-20 | 2,922 | 316        | 16-36 | 9,303 |
| Russian   | 207           | 8-18 | 768   | 314        | 18-36 | 1,037 |
| Spanish   | 208           | 8-18 | 788   | 312        | 16-30 | 1,146 |
| Swedish   | 205           | 8-16 | 467   | 339        | 16-28 | 900   |
| Turkish   | 180           | 8-16 | 1,115 | 297        | 16-36 | 2,422 |

### 168 Semantic networks

We constructed semantic networks for English data following the procedure outlined in 169 Hills et al. (2009), as follows. We used as an index of semantic relatedness the Florida Free 170 Association Norms (Nelson et al., 1998). This dataset was collected by giving adult 171 participants a word (the cue), and asking them to write the first word that comes to mind 172 (the target). For example, when given the word "ball," they might answer with the word 173 game." A pair of nodes were connected by a directed link from the cue to the target if there 174 was a cue-target relationship between these nodes in the association norms. The connectivity 175 of a given node was characterized by its *indegree*: the number of links for which the word 176 was the target.<sup>2</sup> To model growth from month to month, we constructed a different network 177 at each month, based on the nouns that have been acquired by that month. 178

Since the free association norms are available only in English, we used the 179 hand-checked translation equivalents available in Wordbank, which allowed us to use the 180 English association norms across 10 languages. Semantic associations are not necessarily 181 shared across languages, but we use this technique as a reasonable first approximation. In 182 support of this approximation, Youn et al. (2016) showed that semantic networks across 183 languages share substantial similarities. The fact that semantic associations are assumed to 184 be shared across languages does not mean that the semantic networks will necessarily grow 185 in a similar fashion. For instance, the set of words acquired by children as well as the order 186 of word acquisition can vary from language to language leading to possibly different learning 187 strategies. 188

<sup>&</sup>lt;sup>2</sup> This choice was based on prior work by Hills et al. (2009) stating that analyses with both outdegrees (sum of the links where the word is the cue in a cue-target pair) and total degree (outdegree plus indegree) led to results weaker than those calculated with indegree.

### Phonological networks

To construct phonological networks we first mapped the orthographic transcription of 190 words to their International Phonetic Alphabet (IPA) transcriptions in each language, using 191 the open-source text-to-speech software **Espeak**. This software provides the correct IPA 192 transcription if the word is found in a spelling-to-phonemes dictionary, otherwise it uses 193 language-specific pronunciation rules to generate an approximate phonetic transcription. We 194 used the Levenshtein distance (also known as edit distance) as a measure of phonological 195 relatedness between two nodes. The measure counts the minimum number of operations 196 (insertions, deletions, substitutions) required to change one string into another. 197

In previous studies, two nodes were linked if they had an edit distance of 1 (Carlson et 198 al., 2014; Stella et al., 2017; Storkel, 2009). However, these studies reported a contribution of 199 phonological connectivity to noun learning when networks were built using a dense adult 200 vocabulary. Since the focus of the current study is on the mechanism of growth, the 201 networks are based on children's early vocabulary. The latter, however, contains very few 202 noun pairs with an edit distance of 1. To better represent the similarity space in the 203 phonological domain, we increased the threshold from 1 to 2, that is, two nodes were related 204 if their edit distance was equal to 1 or 2.3 The connectivity of a given node was 205 characterized with its degree: the number of links it shares with other words. 206

<sup>&</sup>lt;sup>3</sup> In Appendix A, we show the main results for phonological networks based on an edit distance of 1. We also show the results for phonological networks where the edges between pairs of words were weighted by a normalized edit distance. We did not consider the case of a threshold larger than 2 since many short pairs appear phonologically unrelated when the edit distance is 3 or more (e.g., "cat"/"dog").

207 Analysis

# 208 Static properties of the global network

We start by analyzing word connectivity in the global (static) network. We constructed this network using nouns learned by the oldest age for which we have CDI data (e.g., in English this corresponds, in comprehension, to the network by 18 months, and in production, to the network by 30 months). This global network is the end-state towards which both INT and EXT converge by the last month of learning. Moreover, following Hills et al. (2009), we used this end-state network as a proxy for the external connectivity in the learning environment. Below we analyze properties of these global networks that may a priori hint at an INT- or EXT-like growth.

Connectivity predicts the age of acquisition. Connectivity in the global 217 network is directly related to EXT as it represents the explicit criterion this growth scenario uses to determine what words should be learned first (Figure 1). Therefore, a direct consequence of an EXT-like growth scenario is a correlation between connectivity in the 220 global network and the age of acquisition. This correlation is also necessary to INT, although 221 the causality is reversed: Higher connectivity in the global network is caused by earlier 222 learning, not the other way around. Some words end up being highly connected in the global 223 network precisely because they happen to be acquired earlier and, therefore, have a higher 224 chance of accumulating more links over time. Thus, the correlation between connectivity in 225 the end-state network and AoA can result from both EXT and INT. If there is no such 226 correlation, neither growth scenario can be posited as a possible learning mechanism. 227

Figures 2 and 3 show how the age of acquisition in production and comprehension, respectively, correlates with the degree (or indegree for the semantic networks). For ease of visual comparison, the predictor (i.e., the degree) was centered and scaled. The plots show, overall, a negative correlation between the month of acquisition and the degree. In production data, the average correlation across languages was -0.24 (SD = 0.10) for the

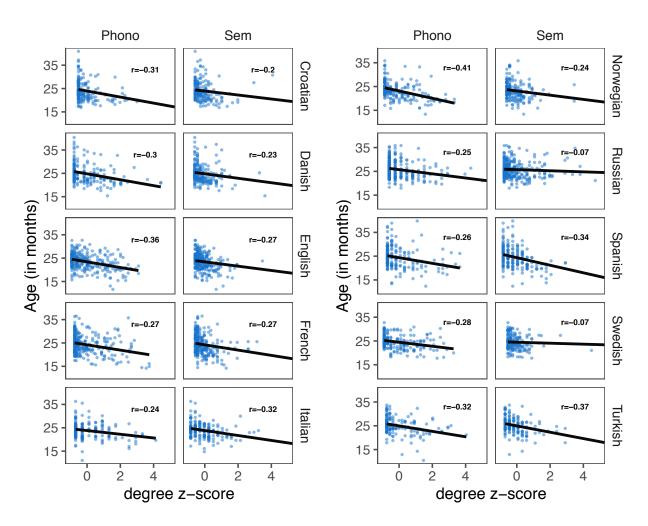


Figure 2. Production data (Age of acquisition) as predicted by the degree (i.e., connectivity) in this network. Results are shown in each language for phonological and semantic networks. Each point is a word, with lines indicating linear model fits, and numbers indicating the Pearson correlation coefficients.

semantic networks and -0.30 (SD = 0.05) for the phonological networks. In comprehension data, the average correlation was -0.21 (SD = 0.08) for the semantic networks and -0.21 (SD = 0.07) for the phonological networks. These results indicate that nouns with higher degrees are generally learned earlier, thus replicating previous findings in English (Hills et al., 2009; Storkel, 2009) and extending these findings to 10 different languages, generally, in both production- and comprehension-based vocabularies.

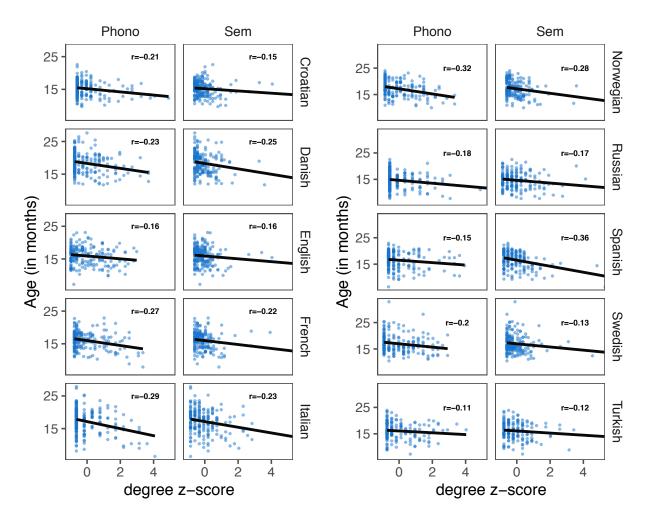


Figure 3. Comprehension data (Age of acquisition) as predicted by the degree (i.e., connectivity) in this network. Results are shown in each language for phonological and semantic networks. Each point is a word, with lines indicating linear model fits, and numbers indicating the Pearson correlation coefficients.

Power-law degree distribution. We also analyzed the global network's degree distribution. The shape of this distribution is particularly relevant to INT as this growth scenario is known to generate networks with a power-law degree distribution, i.e., a distribution of the form  $p(k) \propto \frac{1}{k^{\alpha}}$  (Barabasi & Albert, 1999). If the end-state network displays this property, this fact would suggest, but not prove, an INT-like generative process. If, however, the degree distribution is very different from a power law, this would significantly weaken the case for INT. The log-log plots are shown in Figure 4. We fit a

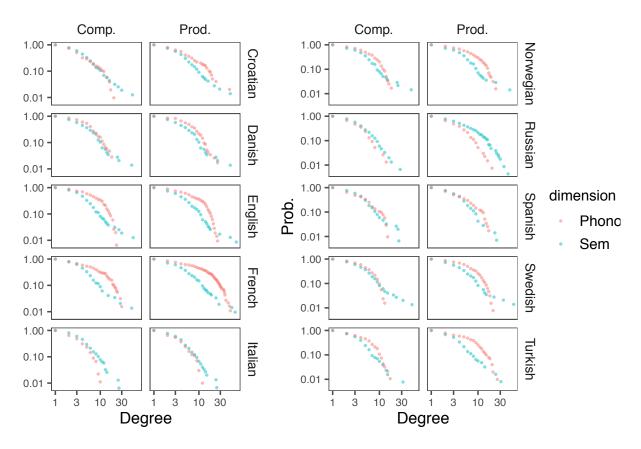


Figure 4. Log-log plot of the cumulative degree distribution function for the global phonological and semantic networks across languages. The figure shows the results for both production and comprehension data. A perfect power-law distribution should appear as a straight line in this graph.

power law to each empirical degree distribution following the procedure outlined in Clauset,
Shalizi, & Newman (2009) and using a related R package (poweRlaw, Gillespie, 2015).

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In brief, the analysis consisted in two steps. First, we derived the optimal cut-off,  $k_{min}$ , above which the distribution is more likely to follow a power-law,<sup>4</sup> and we estimate the corresponding scaling parameter  $\alpha$ . Second, we calculated the goodness-to-fit, which resulted in a p-value quantifying the plausibility of the model. The results are shown in Table 2 for production data, and in Table 3 for comprehension data.

<sup>&</sup>lt;sup>4</sup> In natural phenomena, it is often the case that the power law applies only for values above a certain minimum.

Table 2
Results of fitting a power-law model to the degree (i.e., connectivity) distribution in each model for production data. Numbers indicate the cut-off degree, the scaling parameter alpha, and the p-value which quantifies the plausibility of the power-law hypothesis. If the p-value is close to 1, a power law cannot be rejected as a plausible fit for the data.

|           |         | Sem.  |         |         | Phono. |         |
|-----------|---------|-------|---------|---------|--------|---------|
| Language  | cut-off | alpha | p-value | cut-off | alpha  | p-value |
| Croatian  | 4       | 2.55  | 0.881   | 4       | 2.18   | 0.123   |
| Danish    | 4       | 2.38  | 0.001   | 11      | 4.55   | 0.858   |
| English   | 5       | 2.66  | 0.132   | 20      | 9.14   | 0.511   |
| French    | 8       | 2.81  | 0.133   | 20      | 3.75   | 0.112   |
| Italian   | 4       | 2.93  | 0.608   | 9       | 9.45   | 0.780   |
| Norwegian | 5       | 2.88  | 0.201   | 15      | 6.28   | 0.744   |
| Russian   | 24      | 5.61  | 0.723   | 8       | 4.20   | 0.541   |
| Spanish   | 4       | 2.98  | 0.460   | 13      | 8.75   | 0.736   |
| Swedish   | 4       | 2.49  | 0.171   | 11      | 4.68   | 0.103   |
| Turkish   | 4       | 2.87  | 0.925   | 8       | 3.26   | 0.375   |

Overall, we could not reject the null hypothesis of a power-law distribution: The

p-value was generally above 0.1 in almost all languages for both production and

comprehension. That said, phonological networks had relatively larger cut-offs than semantic

networks. These "truncated" power-laws in phonological networks may be due to the

constraints that exist on word formation in the phonological domain such as the size of the

phonemic inventory, phonotactic rules, and word length. Such constraints may limit the

number of words that are phonologically similar, thus leading to distributions that decay

faster than a non-truncated power law (Arbesman et al., 2010).

Table 3

Results of fitting a power-law model to the degree distribution in each model for comprehension data. Numbers indicate the cut-off degree, the scaling parameter alpha, and the p-value which quantifies the plausibility of the power-law hypothesis. If the p-value is close to 1, a power law cannot be rejected as a plausible fit for the data.

|           |         | Sem.  |         |         | Phono. |         |
|-----------|---------|-------|---------|---------|--------|---------|
| Language  | cut-off | alpha | p-value | cut-off | alpha  | p-value |
| Croatian  | 5       | 2.67  | 0.895   | 2       | 2.06   | 0.020   |
| Danish    | 4       | 2.39  | 0.005   | 5       | 2.98   | 0.136   |
| English   | 4       | 2.64  | 0.765   | 13      | 5.16   | 0.235   |
| French    | 4       | 2.63  | 0.330   | 18      | 5.58   | 0.336   |
| Italian   | 4       | 2.88  | 0.688   | 8       | 10.27  | 0.909   |
| Norwegian | 5       | 2.87  | 0.433   | 13      | 7.65   | 0.440   |
| Russian   | 8       | 3.91  | 0.952   | 5       | 3.97   | 0.854   |
| Spanish   | 5       | 3.11  | 0.552   | 5       | 3.01   | 0.085   |
| Swedish   | 5       | 2.81  | 0.713   | 9       | 6.75   | 0.102   |
| Turkish   | 4       | 3.13  | 0.887   | 9       | 5.73   | 0.958   |

In sum, the static properties of the end-state network are *a priori* compatible with both INT and EXT. In order to decide between these two developmental scenarios, we need to fit explicit growth models to the data.

### Network growth models

To test the network growth scenarios, we fit two growth models to the data. We calculated the probability that a word  $w_i$ , with a utility value  $u_i$  would enter the lexicon at a

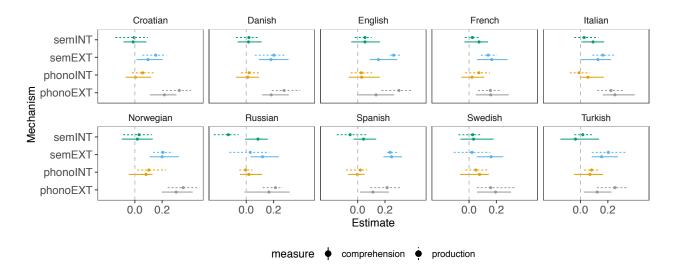


Figure 5. Evaluation of growth scenarios (EXT: externally-driven, INT: internally-driven) for both semantic and phonological networks. Each point represents the mean of the posterior distribution of the growth parameter, with ranges representing 95% credible intervals. Positive values mean that learning proceeds according to the predictions of the growth scenario, whereas negative values mean that learning proceeds in opposition to the predictions of the growth scenario.

267 given month, using a softmax function:

$$p(w_i) = \frac{e^{\beta u_i}}{\sum_j e^{\beta u_j}} \tag{1}$$

where  $\beta$  is a fitted parameter that captures the magnitude of the relationship between network parameters and growth (analogous to a regression coefficient). A positive value of  $\beta$ means that words with higher utility values  $u_i$  are acquired first, and a negative value means that words with lower utility values are acquired first (see Figure 1 for an illustration of how utility values  $u_i$  are defined in each growth scenario). The normalization includes all words that could be learned at that month.

We estimated the parameter  $\beta$  using a Bayesian approach. The inference was performed using the probabilistic programming language WebPPL (Goodman & Stuhlmuller, 2014). We defined a uniform prior over  $\beta$ , and at each month, we computed the likelihood

function over words that could possibly enter the lexicon at that month, fit to the words that have been learned at that month (using Formula 1). Markov Chain Monte Carlo sampling 278 resulted in a posterior distribution over  $\beta$ , which we summarized in Figure 5. The results 279 replicate Hills et al.'s original finding regarding the semantic network in English and the 280 production-based vocabulary, which is that this network grows by EXT, not by INT. 281 Crucially, our results show that, generally speaking, this finding generalizes to 282 comprehension-based vocabulary, and holds across languages. This generalization was 283 obtained in both the semantic<sup>5</sup> and phonological domains. In Appendix B, we show that the 284 semantic and phonological domains provide largely non-redundant information. 285

### 286 Comparison to other predictors of age of acquisition

Above we showed that the way semantic and phonological information is structured in 287 the learning environment contributes to noun learning (via EXT) across languages. However, 288 we know that other factors influence learning as well (e.g., Braginsky et al., 2019). Next, we 289 investigated how semantic and phonological connectivity interact with two other factors. 290 The first one is word frequency, a well-studied factor shown to predict the age of acquisition 291 in a reliable fashion (e.g., Goodman et al., 2008). The second factor is word length, which 292 was shown to correlate with phonological connectivity: Shorter words are more likely to have 293 higher connectivity (Pisoni, Nusbaum, Luce, & Slowiaczek, 1985; Vitevitch & Rodri'guez, 294 2005). 295

Since we found INT to be uninformative, we dropped it from this analysis, keeping

<sup>&</sup>lt;sup>5</sup> One could imagine that the fact of using English free association norms cross-linguistically would decrease the effect of non-English semantic networks because of possible cultural differences. However, our findings do not support this assumption; rather, it supports our initial approximation about the shared nature of the semantic similarity measure. That said, this approximation is not perfect. For example, there is evidence that a small part of the variance in free association data can be explained by phonological similarity (Kachergis, Cox, & Jones, 2011; Matusevych & Stevenson, 2018), thus leading to possibly minor cross-linguistic differences.

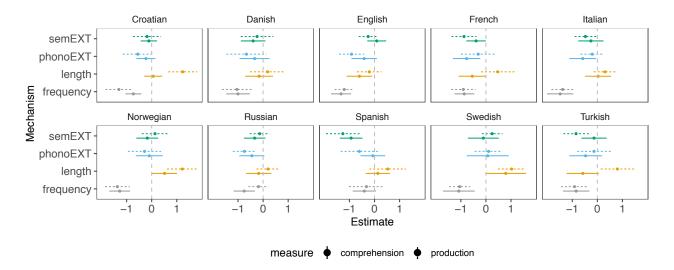


Figure 6. Estimates of the relative contribution of each predictor of AoA in the regression model in each language. Results are shown for both production and comprehension data. Ranges indicate 95% confidence intervals. Positive values indicate a positive relationship (e.g. longer words tend to have a higher AoA), while negative values indicate a negative relationship (e.g. words with higher frequency tend to have a lower AoA).

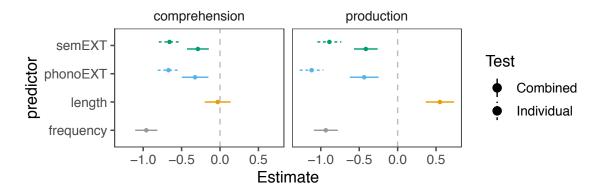


Figure 7. Estimates of the relative contribution of each predictor of AoA in the combined mixed-effects model with language as a random effect. Results are shown for both production and comprehension data. Ranges indicate 95% confidence intervals. Dotted ranges indicate the estimates for the predictor in a separate model that includes only this predictor as a fixed effect.

only EXT. This simplified the model because we no longer needed to fit growth

298 month-by-month. The latter was a requirement only for INT where the words' utilities

varied from month to month, depending on how connectivity changed in the growing internal
network. A more direct way to assess and compare the contribution of EXT in relation to
other word-level factors is through conducting regressions, where connectivity in the learning
environment, frequency, and length predict the age of acquisition.

For word length, we counted the number of phonemes in our generated IPA transcription. For word frequency, we used the frequency estimates from Braginsky et al. (2019) where unigram counts were derived based on CHILDES corpora in each language (MacWhinney, 2014). Although these frequency counts use transcripts from independent sets of children, they are based on large samples, and this allows us to average out possible differences between children and the specificities of their input (see Goodman et al., 2008 for a similar research strategy).

We conducted two analyses. We fit a linear regression for each language, and we fit a linear mixed-effect model to all the data pooled across languages, with language as a random effect. Figure 6 shows the coefficient estimate for each predictor in each language for production and comprehension data. Figure 7 shows the coefficient estimates for all languages combined (all predictors were centered and scaled).

The findings for the new predictors were as follows. Overall, frequency is the largest and most consistent predictor of age of acquisition in both comprehension and production data and across languages, endorsing results for nouns across a variety of analyses (Braginsky et al., 2019; Goodman et al., 2008; Roy et al., 2015). Word length is more predictive for production than comprehension (and this difference is very clear in the global model), replicating previous work (Braginsky et al., 2019). Thus, word length seems to reflect the effects of production's constraints rather than comprehension's constraints, i.e., longer words are harder to articulate but they may not be significantly more difficult to store and access.

As for the factors of interest, i.e., semantic and phonological connectivity, we found

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cross-linguistic differences. Connectivity contributes to learning in some languages but not in
others. In particular, semantic connectivity does not explain variance in English data beyond
that explained by phonological connectivity, frequency, and length. This finding contrasts
with the original finding in Hills et al. (2009). However, this difference might be due to our
using a slightly different model (which included word length as a covariate) and a larger
dataset. That said, and despite these apparent cross-linguistic differences, both phonological
and semantic connectivity are significant predictors in the combined model (Figure 7).

Discussion

This study provided an analysis of network growth during development. We compared 332 two network growth scenarios described in the pioneering work of Steyvers & Tenenbaum 333 (2005) and Hills et al. (2009). The first scenario, INT (originally called Preferential 334 Attachment), described a rich-get-richer network growth model in which the current 335 structure of the learner's internal network determines future growth; the other, EXT 336 (originally called Preferential Acquisition) described a model in which the external, global 337 environmental network structure determines learners' growth patterns. These two 338 mechanisms represent two fundamentally different accounts of lexical growth: One suggests 339 that future word knowledge is primarily shaped by the children's past knowledge and its 340 organization, whereas the other suggests that learning is shaped, rather, by salient properties in the input regardless of how past knowledge is organized. The present study tested the generality of previous findings by 1) investigating phonological networks together with semantic networks, 2) testing both comprehension- and production-based vocabularies, and 3) comparing the results across 10 languages.

We found that the original findings reported in Hills et al. (2009) generalize well across all these dimensions. First, just like semantic networks, phonological networks grow via the externally-driven scenario (EXT), not by the internally-driven mechanism (INT). Second, comprehension-based vocabularies grow in a way similar to production-based vocabularies.

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Finally, the findings were, overall, similar across the 10 languages we tested. Although we
find some cross-linguistic variation when semantic and phonological networks were pitted
against frequency and length, this variability is to be taken with a grain of salt as it might
be exaggerated in our study by several factors such as the limited and partially-overlapping
set of nouns for each language, measurement error due to the sample of acquisition data, the
sample of frequency data, and the translation of association norms. In fact, both
phonological and semantic connectivity are significant predictors above and beyond
frequency and length when data are pooled across languages.

These findings corroborate the hypothesis that children start by learning words that have high similarity to a variety of other words in the learning environment, not in the child's available lexicon. This hypothesis implies that children are sensitive to highly connected words although they do not initially have access to the full network, thus raising some important questions: What mechanism allows children to distinguish highly connected words from other words? Besides, why would highly connected words be easier to learn?

One possibility is that these patterns emerge from children's use of statistical learning abilities (Aslin & Newport, 2012; Saffran, Aslin, & Newport, 1996; Smith & Yu, 2008). The term "statistical learning" has been used in the developmental literature to describes the process by which one acquires information about their environment through tracking the frequency distribution of some elements (e.g., words) in different contexts. An important property of this kind of learning is that it occurs without explicit instructions and through mere exposure to the input. Previous work in this line of research has documented specific mechanisms that can explain the patterns found in the current study.

For example, in the semantic domain, growth according to EXT could be explained by a mechanism similar to cross-situational learning (McMurray et al., 2012; Smith & Yu, 2008; Yurovsky & Frank, 2015). According to this mechanism, children track the co-occurrence of concrete nouns with their possible semantic referents. The referent of a word heard in only

one naming situation can be ambiguous (e.g., when the word "ball" is heard for the first time 376 in the presence of both a ball and a chair), but hearing the same word in a diversity of 377 semantic contexts allows the learner to narrow down the set of possible word-object 378 mappings. In our case, free association (used to determine semantic network connectivity) is 379 related to contextual co-occurrence (Fourtassi & Dupoux, 2013; Griffiths, Steyvers, & 380 Tenenbaum, 2007), meaning that highly connected words will tend to occur in a variety of 381 speech and referential contexts. This fact makes such words easier to learn because they 382 have more referential disambiguating cues across learning contexts. Crucially, children can 383 learn these words without necessarily knowing the meaning of all other words with which 384 they co-occur (Fourtassi, Dunbar, & Dupoux, 2014), hence the similarity with EXT. This 385 possibility is supported by the finding that words' diversity of occurrence in child-directed 386 speech predicts their age of learning (Hills et al., 2010; Stella et al., 2017).

In the phonological case, network growth according to EXT is also compatible with a 388 scenario whereby children are tracking low-level statistical patterns, e.g., high probability 389 sound sequences. Indeed, connectivity in the phonological network is inherently correlated 390 with phonotactic probability (Vitevitch, Luce, Pisoni, & Auer, 1999). That is, highly 391 connected words tend to be made of frequent sound sequences. Children are sensitive to 392 local phonotactic regularities (Jusczyk, Luce, & Charles-Luce, 1994), and this sensitivity 393 might lead them to learn higher-probability words more easily (Storkel, 2001). This 394 explanation is supported by computational simulations that show how learning general 395 phonotactics patterns create "well-worn paths" which allow the models to represent several 396 distinct but phonologically neighboring words (Dell, Juliano, & Govindjee, 1993; Siew, 2013; 397 Takac, Knott, & Stokes, 2017). More generally, there is a growing interest in investigating 398 precisely how the local patterns acquired through statistical learning may give rise to the 399 global network organization (For a review, see Karuza, Thompson-Schill, & Bassett, 2016).

Besides using their own statistical learning skills, children could also benefit from the

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way their caregivers speak. Perhaps the caregivers put more emphasis on the words that are 402 highly connected in their mature lexical network. This emphasis would guide children to 403 learn first these highly connected words, even though children do not have access to the 404 distribution of words' connectivity in the final network. Investigating this possibility would 405 require further research on caregiver-child interaction (MacWhinney, 2014; Roy et al., 2015), 406 examining what words are introduced over development and the extent to which children's 407 uptake is influenced by this input (Clark, 2007; Hoff & Naigles, 2002; Huttenlocher et al., 408 1991). 400

This study investigated the class of nouns in isolation — following previous studies investigating the early semantic and phonological network (Hills et al., 2009; Storkel, 2009).
We could ask if studying one class separately is a legitimate research strategy. In other words, would word classes (such as nouns, verbs and function words) be acquired relatively differently, or would they interact substantially to the extent that it becomes unreasonable to study each class separately?

There are many observations that support the hypothesis that different word classes 416 have different pathways of learning, making it worthwhile to study each class separately. For 417 instance, different word classes follow different time trajectories: In the early stages of 418 development, nouns tend to be acquired at a higher pace than predicates and function words 419 (Bates et al., 1994). Research has shown that this difference cannot be trivially attributed to 420 differences in the degree to which these classes are present in the input; if anything, verbs 421 and function words are often more frequent in the input than nouns (e.g., Gentner, 1982). Goodman et al. (2008) found an effect of frequency on the age of acquisition within — not 423 across — classes. Further, recent work by Braginsky et al. (2019) tested a large number of predictors, besides frequency, and found that these predictors do not influence the 425 acquisition of word classes in the same way. For example, the acquisition of nouns was found 426 to be most influenced by frequency and concreteness, whereas the acquisition of function 427

words was most influenced by word length.

This work shares a number of limitations with previous studies using similar research 429 strategy and datasets. Chief among these limitations is the fact that the age of word 430 acquisition is computed using different children at different ages (due to the fact that 431 available CDI data is mainly cross-sectional). Such a measure has been shown to be valid 432 and reliable (Fenson et al., 1994), and has allowed researchers to study important aspects of 433 word learning (Braginsky et al., 2019; Goodman et al., 2008; Hills et al., 2009; Stella et al., 434 2017; Storkel, 2009). In our case, the use of cost-effective cross-sectional data has allowed us 435 to leverage large-scale studies across several languages. That said, it is important to 436 remember that this type of data can only inform us about the learning trajectory of the 437 "average" child. Although our study endorses, overall, the externally-driven account of 438 network growth, this does not mean individual children never use some variant of INT or 439 some combination of both INT and EXT (Beckage & Colunga, 2019). To illustrate, some 440 children develop "islands of expertise," that is, well-organized knowledge about a certain 441 topic (e.g., birds or dinosaurs). This prior knowledge enables these children to learn new 442 related words more easily (e.g., Chi & Koeske, 1983).

To conclude, our work validates and generalizes previous results in early network
development. It suggests that the advantage of highly connected words may result, at least
in the early stages of word learning, from the operation of simpler mechanisms in both the
semantic and phonological domains. One question for future experimental work is whether
such correlational patterns of growth can be produced in controlled behavioral experiments.

All data and code for these analyses are available at https://github.com/afourtassi/networks 450

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