Word Learning as Network Growth: A Cross-linguistic Analysis

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Abstract

Children tend to produce words earlier when they are connected to a variety of other words 15 along the phonological and semantic dimensions. Though this connectivity effect has been 16 extensively documented, little is known about the underlying developmental mechanism. 17 One view suggests that learning is primarily predicted by a network growth model where 18 highly connected words in the child's early lexicon enable learning of similar words. Another 19 view suggests that learning is driven by highly connected words in the external learning 20 environment, instead of highly connected words in the early internal lexicon. The present 21 study tests both scenarios systematically in both the phonological and semantic domains 22 across 10 languages. We show that external connectivity in the learning environment drives 23 growth in both production- and comprehension-based vocabularies, even controlling for word frequency and length. This pattern of findings suggests a word learning mechanism where 25 children harness their statistical learning abilities to detect and learn highly connected words in the learning environment.

Keywords: Language understanding; audio-visual processing; word learning; speech perception; computational modeling.

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Introduction

What factors shape vocabulary learning over the course of early childhood? To 32 investigate this question, scientists have adopted multiple research strategies, from 33 conducting controlled laboratory experiments (e.g. Markman, 1990) to analyzing dense corpora capturing language learning in context (e.g., B. C. Roy, Frank, DeCamp, Miller, & Roy, 2015). One strategy consists in documenting the timeline of words' acquisition, and studying the properties that make words easy or hard to learn. For example, within a lexical 37 category, words that are more frequent in child-directed speech are acquired earlier (J. C. Goodman, Dale, & Li, 2008). Other factors include word length and the mean length of 39 utterances in which the word occurs (e.g., Braginsky, Yurovsky, Marchman, & Frank, 2016; 40 Swingley & Humphrey, 2018). 41 Besides these word-level properties, the structure of the lexicon (that is, how words 42 relate to one another) also predicts the Age of Acquisition (AoA) of words. The lexical structure can be characterized in terms of a network where each node represents a word in the vocabulary, and each link between two nodes represents a relationship between the corresponding pair of words (e.g., Collins & Loftus, 1975). Previous studies have investigated early vocabulary structure by constructing networks using a variety of word-word relations including shared semantic features (McRae, Cree, Seidenberg, & McNorgan, 2005), target-cue relationships in free association norms (Nelson, McEvoy, & Schreiber, 1998), co-occurrence in child directed speech (MacWhinney, 2014), and phonological relatedness Vitevitch, 2008). These studies have generally found that children tend to produce words that have higher neighborhood density (i.e., high connectivity in the network) earlier, both at the phonological and the semantic level (Carlson, Sonderegger, & Bane, 2014; Hills, Maouene, Riordan, & Smith, 2010; Hills, Maouene, Maouene, Sheya, & Smith, 2009; Stella, Beckage, & Brede, 2017; Storkel, 2009). While most studies have focused on the static properties of the lexical network, a few

have investigated the underlying developmental process. In particular, Steyvers and
Tenenbaum (2005) suggested that the observed effects of connectivity are the consequence of
how the lexical network gets constructed in the child's mind. According to this explanation,
known as Preferential Attachment, highly connected words in the child's lexicon tend to
"attract" more words over time, in a rich-get-richer scenario (Barabasi & Albert, 1999). In
other words, what predicts word learning is the *internal* connectivity in the child's early
lexicon. In contrast, Hills et al. (2009) suggested that what biases the learning is not the
connectivity in the child's internal lexicon but, rather, *external* connectivity in the learning
environment. They called this alternative explanation Preferential Acquisition. For clarity of
reading, we will call preferential attachment the Internally-driven mechanism (INT), and
preferential acquisition the Externally-driven mechanism (EXT). Figure 1 shows an
illustration of both growth scenarios with the same simplified network.

These two proposals represent two divergent ideas about the role of lexical networks in 69 acquisition. On the INT proposal, learning is driven by known words with high connectivity 70 to other known words (Figure 1, left). Thus, the network structure is a causal factor in early 71 word learning, that is, children rely on the organization of their past knowledge to determine 72 future learning. For example, having a rich and organized knowledge about the domain of dinosaurs would facilitate the acquisition of new dinosaur-related words (Chi & Koeske, 1983). In contrast, on the EXT approach, learning is driven by the connectivity of words that are not known yet (Figure 1, right). Thus, the relevant network structure is not internally represented by children, and the observed connectivity effect might be an epiphenomenon of 77 some properties of the linguistic input. For example, highly connected words in the input 78 could be more easily learned because of their contextual diversity (e.g., Smith & Yu, 2008) or because caregivers emphasize such words in child-directed speech (MacWhinney, 2014).

Hills et al. (2009) investigated the growth of lexico-semantic networks in toddlers and found that growth did not proceed according to INT as was originally hypothesised by

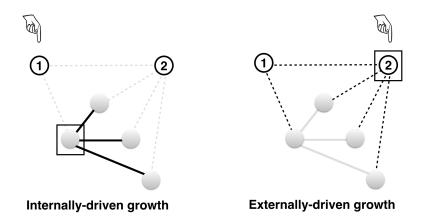


Figure 1. Illustration of the two growth scenarios. Filled grey circles represent known words (Internal) at a certain point in time. The empty, numbered circles represent words that have not yet been learned (External) and which are candidates to enter the lexicon next. The identity of the word that is going to be learned depends on the growth scenario. Here the squares indicate the node that drives growth in each scenario and the hand pointer indicates which word is likely to be learned. For INT, the utility of a candidate, external node is the average degree (i.e., number of links) of the internal nodes that it would attach to. Thus, according to INT, node 1 is more likely to enter the lexicon. For EXT, the utility of a candidate node is its degree in the entire network. According to EXT, node 2 is more likely to enter the lexicon next.

- Steyvers and Tenenbaum (2005), but rather according to EXT. This is a profound finding
- because it suggests that learning in the early stages is mostly driven by properties of the
- external input, regardless of how past knowledge is organized. However, this work has been
- done in the special case of networks that are based on 1) semantic associations, 2)
- production-based vocabularies, and 3) data from English-learning children, only. The extent
- to which this result depends on the domain (e.g., semantic vs. phonological connectivity),

¹Besides INT and EXT, the authors tested a third mechanism (called the lure of associates) which resembles EXT in that it is driven by the connectivity of external nodes, except that this connectivity is computed with respect to words that are known. However, EXT is the externally-driven scenario that best predicted the data in this previous work.

the vocabulary measure (production vs. comprehension) and culture/language is still unclear.
In this work, we test the generality of the finding along these three dimensions.

First, we study the phonological network in addition to the semantic network. These 91 two networks represent different ways the mental lexicon is structured (Beckage & Colunga, 2016). In particular, words that are neighbors in the semantic network (e.g., "cat", "dog") 93 are not necessarily neighbors in the phonological network, and vice versa. Does the phonological network also predict word learning? Previous work did find an effect of words' connectivity in the phonological network on their age of learning (Carlson et al., 2014; Stella et al., 2017; Storkel, 2009). In other words, words learned earlier in life tend to sound similar 97 to many other words than a word learned later in life. However, this finding is a priori compatible with both INT and EXT, and previous studies did not explicitly compare these two mechanisms. Here, we investigate whether phonological networks, like semantic 100 networks, grow through EXT, or if they rather grow via INT (Figure 1). 101

Second, we study vocabularies measured using both comprehension and production. 102 Previous studies have found differences between these vocabularies in terms of their content 103 and rate of acquisition (Benedict, 1979; Fenson et al., 1994). These differences may reflect 104 the fact that comprehension and production do not share the same constraints. For instance, 105 whereas comprehension depends on the ease with which words are stored and accessed, 106 production depends, additionally, on the ease with which words are articulated, e.g., shorter words are produced earlier (Braginsky et al., 2016). By investigating comprehension-based vocabularies, we assess the extent to which the network growth mechanism captures general 109 learning patterns beyond the specific constraints of production. 110

Finally, we use developmental data in 10 languages. Lexical networks can show more or less cross-linguistic variability along both the semantic and phonological domains (Arbesman, Strogatz, & Vitevitch, 2010; Youn et al., 2016). Besides, cultures might differ in the way caregivers talk to children (Cristia, Dupoux, Gurven, & Stieglitz, 2017; Kuhl et al., 1997), and this difference in the input could influence the way in which the children's networks

grow. Thus, cross-linguistic comparison is crucial to test what growth mechanism is
cognitively universal and is used by all children, and what mechanism is specific to some
patterns of learning that emerge due to the particulars of a given language or culture (Bates
MacWhinney, 1987; Slobin, 2014).

We test the growth scenarios using parent reports of children vocabularies and their

normative age of acquisition (Fenson et al., 1994). Children may vary in their individual 121 learning trajectories, but the aggregate data leads to an average learning pattern which is 122 highly consistent. It is this normative trajectory that we model in the current study, 123 following in this regard the steps of previous research using similar datasets (Braginsky et al., 2016; J. C. Goodman et al., 2008; Hills et al., 2010, 2009; Stella et al., 2017; Storkel, 2009) The paper is organized as follows. First, we describe the datasets we used and explain 126 how we constructed the networks. Second, we analyze static properties of words' connectivity 127 in these networks (correlation with age of acquisition and shape of the distribution) and we 128 explain how these properties infom hypotheses about network growth. Next, we explicitly fit 129 the two hypothesized growth mechanisms to the data. We investigate the extent to which 130 the results obtained in Hills et al. (2009) generalize to phonological networks and 131 comprehension-based vocabularies, and whether this generalization holds cross-linguistically. 132

Networks Networks

134 Data

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We used data from Wordbank (Frank, Braginsky, Yurovsky, & Marchman, 2017), an open repository aggregating cross-linguistic language developmental data of the MacArthur-Bates Communicative Development Inventory (CDI), a parent report vocabulary checklist. Parent report is a reliable and valid measure of children's vocabulary that allows for the cost-effective collection of datasets large enough to test network-based models of acquisition (Fenson et al., 1994). When filling out a CDI form, caregivers are either invited to indicate whether their child "understands" (comprehension) or "understands and says"

(production) each of about 400-700 words. For younger children (e.g., 8 to 18 months in the English data), both comprehension and production are queried, whereas for older children (16 to 36 months) only production is queried. Due to these limitations, we use data from younger children to test comprehension and data from older children to test production. Following previous studies (Hills et al., 2009; Storkel, 2009), we restrict our analysis to the category of nouns.². Table 1 gives an overview of the data we used.

48 Age of acquisition

For each word in the CDI data, we compute the proportion of children who understand or produce the word at each month. Then we fit a logistic curve to these proportions and determined when the curve crosses 0.5, i.e., the age at which at least 50% of children know the word. We take this point in time to be each word's age of acquisition (Braginsky et al., 2016; J. C. Goodman et al., 2008).

$_{54}$ Semantic networks

We constructed semantic networks for English data following the procedure outlined in 155 Hills et al. (2009), as follows. We used as an index of semantic relatedness the Florida Free 156 Association Norms (Nelson et al., 1998). This dataset was collected by giving adult 157 participants a word (the cue), and asking them to write the first word that comes to mind 158 (the target). For example, when given the word "ball", they might answer with the word 159 "game". A pair of nodes were connected by a directed link from the cue to the target if there 160 was a cue-target relationship between these nodes in the association norms. The connectivity 161 of a given node was characterized by its *indegree*: the number of links for which the word 162 was the target.³ To model growth from month to month, we constructed a different network 163

²This choice was also forced by the fact that the great majority of association data produced by adults–and which we used to build semantic networks–were nouns.

³This choice was based the prior work by @hills2009 stating that analyses with both outdegrees (sum of the links where the word is the cue in a cue-target pair) and total degree (outdegree plus indegree) led to

Table 1
Statistics for the dataset we used.

	Comprehension		Production		
Language	Nouns	Ages	Nouns	Ages	
Croatian	209	8-16	312	16-30	
Danish	200	8-20	316	16-36	
English	209	8-18	312	16-30	
French	197	8-16	307	16-30	
Italian	209	7-24	312	18-36	
Norwegian	193	8-20	316	16-36	
Russian	207	8-18	314	18-36	
Spanish	208	8-18	312	16-30	
Swedish	205	8-16	339	16-28	
Turkish	180	8-16	297	16-36	

at each month, based on the words that have been acquired by that month.

Since the free association norms are available only in English, we used the 165 hand-checked translation equivalents available in Wordbank, which allowed us to use the 166 English association norms across 10 languages. Using the same association data across 167 languages does not necessarily lead to similar networks. Indeed, though this approximation 168 assumes that the semantic similarity measure is universal—which is a reasonable 169 approximation (e.g., Youn et al., 2016), the set of words acquired by children as well as the 170 timeline of this acquisition can still vary from language to language leading to possibility 171 different learning strategies. 172

results weaker than those calculated for indegree.

73 Phonological networks

To construct phonological networks we first mapped the orthographic transcription of
words to their International Phonetic Alphabet (IPA) transcriptions in each language, using
the open source text-to-speech software **Espeak.** We used the Levenshtein distance (also
known as edit distance) as a measure of phonological relatedness between two nodes. The
measure counts the minimum number of operations (insertions, deletions, substitutions)
required to change one string into another.

In previous studies, two nodes were linked if they had an edit distance of 1 (Carlson et 180 al., 2014; Stella et al., 2017; Storkel, 2009). However, these studies reported a contribution of 181 phonological connectivity to word learning when networks were built using a rich adult 182 vocabulary. Since the focus of the current study is on the mechanism of growth, the 183 networks should be based on children's early vocabulary. The latter, however, contains very 184 few word pairs with an edit distance of 1. Thus, we increased the threshold from 1 to 2, that 185 is, two nodes were related if their edit distance was equal to 1 or 2.4 The connectivity of a 186 given node was characterized with its degree: the number of links it shares with other words. 187

188 Analysis

Static properties of the global network

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phonologically related.

 used this end-state network as a proxy for the external connectivity in the learning
environment. Below we analyze properties of this global networks that may a priori hint at
an INT- or EXT-like growth. In order to compare various predictors on the same data, we
restrict the analysis to the subset of nouns for which we had both semantic and phonological
information in each language.

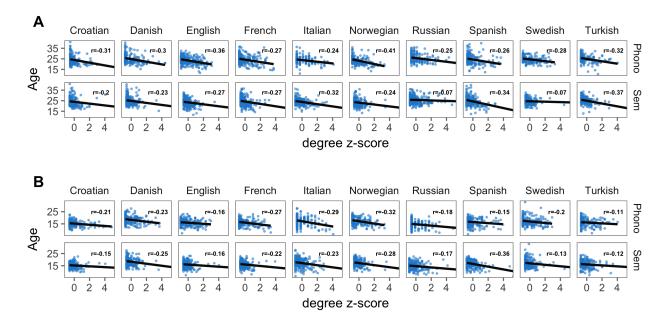


Figure 2. Age of production (A) and comprehension (B) in the global network as predicted by the degree (i.e., connectivity) in this network. Results are shown in each language for phonological and semantic networks. Each point is a word, with lines indicating linear model fits, and numbers indicating the Pearson correlation coefficients.

Connectivity predicts the age of acquisition. Connectivity in the global
network is directly related to EXT as it represents the explicit criterion this growth scenario
uses to determine what words should be learned first (Figure 1). Therefore, a direct
consequence of an EXT-like growth scenario is a correlation between connectivity in the
global network and the age of acquisition. This correlation is also necessary to INT, although
the causality is reversed: higher connectivity in the global network is caused by earlier
learning, not the other way around. Some words end up being highly connected in the global

network precisely because they happen to be acquired earlier and, therefore, have a higher
chance of accumulating more links over time. Thus, the correlation between connectivity in
the end-state network and AoA can result from both EXT and INT. If there is no such
correlation, neither growth scenario can be posited as a possible learning mechanism.

Figure 2 shows how the age of production and comprehension for each word varies as a 211 function of its degree (or indegree for the semantic networks) as well as the correlation values. 212 For ease of visual comparison, the predictor (i.e., the degree) was centered and scaled across 213 languages. The plots show, overall, a negative correlation between the month of acquisition 214 and the degree. In production data, the average correlation across languages was -0.24 215 (SD=0.10) for the semantic networks and -0.30 (SD=0.05) for the phonological networks. In 216 comprehension data, the average correlation was -0.21 (SD=0.08) for the semantic networks and -0.21 (SD=0.07) for the phonological networks. These results indicate that nouns with 218 higher degrees are generally learned earlier, thus replicating previous findings in English (e.g., Storkel 2004, 2009; Hills et al. 2009) and extending these findings to 10 different languages, generally, in both production- and comprehension-based vocabularies.

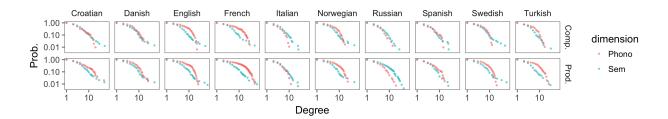


Figure 3. Log-log plot of the cumulative degree distribution function for the global phonological and semantic networks across languages. The figure shows the results for both production and comprehension data. A perfect power-law distribution should appear as a straight line in this graph.

Power-law degree distribution. We also analyzed the global network's degree distribution. The shape of this distribution is particularly relevant to INT as this growth scenario is known to generate networks with a power-law degree distribution, i.e., a distribution of the form $p(k) \propto \frac{1}{k^{\alpha}}$ (Barabasi & Albert, 1999). If the end-state network

displays this property, this fact would suggest, but not prove, an INT-like generative process.

227 If, however, the degree distribution is very different from a power law, this would

significantly weaken the case for INT. The log-log plots are shown in Figure 3. We fit a

power law to each empirical degree distribution following the procedure outlined in Clauset,

Shalizi, and Newman (2009) and using a related R package (poweRlaw, Gillespie, 2015).

Table 2

Results of fitting a power law model to the degree (i.e., connectivity) distribution in each model for production data. Numbers indicate the cut-off degree, the scaling parameter alpha, and the p-value which quantifies the plausibility of the power law hypothesis. If the p-value is close to 1, a power law cannot be rejected as a plausible fit for the data.

	Phono.			Sem.		
Language	cut-off	alpha	p-value	cut-off	alpha	p-value
Croatian	4	2.18	0.123	4	2.55	0.881
Danish	11	4.55	0.858	4	2.38	0.001
English	20	9.14	0.511	5	2.66	0.132
French	20	3.75	0.112	8	2.81	0.133
Italian	9	9.45	0.780	4	2.93	0.608
Norwegian	15	6.28	0.744	5	2.88	0.201
Russian	8	4.20	0.541	24	5.61	0.723
Spanish	13	8.75	0.736	4	2.98	0.460
Swedish	11	4.68	0.103	4	2.49	0.171
Turkish	8	3.26	0.375	4	2.87	0.925

In brief, the analysis consisted in two steps. First, we derived the optimal cut-off, k_{min} , above which the distribution is more likely to follow a power law,⁵ and we estimate the

⁵In natural phenomena, it is often the case that the power law applies only for values above a certain

Table 3

Results of fitting a power law model to the degree distribution in each model for comprehension data. Numbers indicate the cut-off degree, the scaling parameter alpha, and the p-value which quantifies the plausibility of the power law hypothesis. If the p-value is close to 1, a power law cannot be rejected as a plausible fit for the data.

	Phono.			Sem.		
Language	cut-off	alpha	p-value	cut-off	alpha	p-value
Croatian	2	2.06	0.020	5	2.67	0.895
Danish	5	2.98	0.136	4	2.39	0.005
English	13	5.16	0.235	4	2.64	0.765
French	18	5.58	0.336	4	2.63	0.330
Italian	8	10.27	0.909	4	2.88	0.688
Norwegian	13	7.65	0.440	5	2.87	0.433
Russian	5	3.97	0.854	8	3.91	0.952
Spanish	5	3.01	0.085	5	3.11	0.552
Swedish	9	6.75	0.102	5	2.81	0.713
Turkish	9	5.73	0.958	4	3.13	0.887

corresponding scaling parameter α . Second we calculated the goodness-to-fit, which resulted in a p-value quantifying the plausibility of the model. The results are shown in Table 2 for production data, and in Table 3 for comprehension data.

Overall, we could not reject the null hypothesis of a power-law distribution: The

p-value was generally above 0.1 in almost all languages for both production and

comprehension. That said, phonological networks had relatively larger cut-offs than semantic

networks. As was suggested by Arbesman et al. (2010), these "truncated" power-laws in

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phonological networks may reflect the various constraints that exist on word formation in the
phonological domain such as the number of phonemes in the language, the phonotactics (i.e.,
the way sound sequences are arranged in words), and the length of words. Such constraints
may limit the number of words that are phonologically similar, thus leading to distributions
which decay faster than a non-truncated power law.

In sum, the static properties of the end-state network are *a priori* compatible with both INT and EXT. In order to decide between these two developmental scenarios, we need to fit explicit growth models to the data.

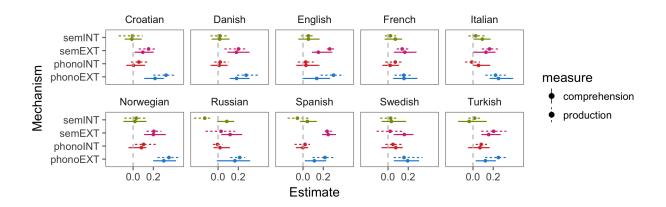


Figure 4. Evaluation of growth scenarios (EXT: externally-driven, INT: internally-driven) for both semantic and phonological networks. Each point represents the mean of the posterior distribution of the growth parameter, with ranges representing 95% credible intervals. Positive values mean that learning proceeds according to the predictions of the growth scenario, whereas negative values mean that learning proceeds in opposition to the predictions of the growth scenario.

Network growth models

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To test the network growth scenarios, we fit two growth models to the data. We calculated the probability that a word w_i , with a utility value u_i would enter the lexicon at a given month, using a softmax function:

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$$p(w_i) = \frac{e^{\beta u_i}}{\sum_j e^{\beta u_j}} \tag{1}$$

where β is a fitted parameter that captures the magnitude of the relationship between network parameters and growth (analogous to a regression coefficient). A positive value of β means that words with higher utility values u_i are acquired first, and a negative value means that words with lower utility values are acquired first (see Figure 1 for an illustration of how utilities values u_i are defined in each growth scenario). The normalization includes all words that could be learned at that month.

We estimated the parameter β using a Bayesian approach. The inference was performed using the probabilistic programming language WebPPL (N. Goodman & Stuhlmuller, 2014). We defined a uniform prior over β , and at each month, we computed the likelihood function over words that could possibly enter the lexicon at that month, fit to the words that have been learned at that month (using formula 1). Markov Chain Monte Carlo sampling resulted in a posterior distribution over β , which we summarized in Figure 4.

First, the results replicate Hills et al.'s original finding regarding the semantic network in English and the production-based vocabulary, which is that this network grows by EXT, not by INT. Second, our results show that, generally speaking, this finding generalizes to comprehension-based vocabulary, and holds across languages. This generalization was obtained in both the semantic⁶ and phonological domains.

⁶One could imagine that the fact of using English free association norms cross-linguistically would decrease the effect of non-English semantic networks because of possible cultural differences. However, our findings do not support this assumption, rather it supports our initial approximation about the universality of the semantic similarity measure. That said, this apprimation is not perfect; there is evidence that a small part of the variance in free assication data can be explained by phonological similarity (Kachergis, Cox, & Jones, 2011; Matusevych & Stevenson, 2018), thus leading to possibly minor cross-linguistic differences.

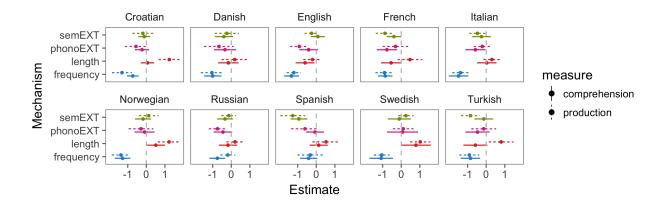


Figure 5. Estimates of the relative contribution of each predictor of AoA in the regression model in each language. Results are shown for both production and comprehension data. Ranges indicate 95% confidence intervals. Positive values indicate a positive relationship (e.g. longer words tend to have a higher AoA), while negative values indicate a negative relationship (e.g. words with higher frequency tend to have a lower AoA).

Comparison to other predictors of age of acquisition

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Above we showed that the way semantic and phonological information is structured in 270 the learning environment contributes to noun learning (via EXT) across languages. However, 271 we know that other factors influence learning as well (e.g., Braginsky et al., 2016). Next we 272 investigated how semantic and phonological connectivity interact with two other factors. 273 The first one is word frequency, a well studied factor shown to predict the age of acquisition 274 in a reliable fashion (e.g. J. C. Goodman et al., 2008). The second factor is word length, which was shown to correlate with phonological connectivity: Shorter words are more likely to have higher connectivity (Pisoni, Nusbaum, Luce, & Slowiaczek, 1985; Vitevitch & 277 Rodríguez, 2005). 278 Since we found INT to be uninformative, we dropped it from this analysis, keeping 279

only EXT. This simplified the model because we no longer needed to fit growth

month-by-month. The latter was a requirement only for INT where the words' utilities

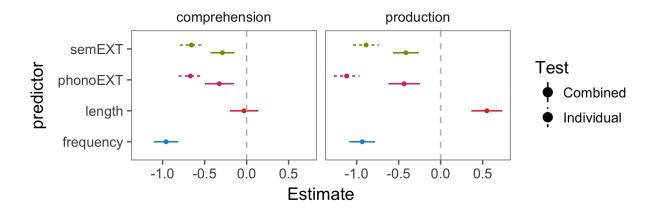


Figure 6. Estimates of the relative contribution of each predictor of AoA in the combined mixed-effects model with language as a random effect. Results are shown for both production and comprehension data. Ranges indicate 95% confidence intervals. Dotted ranges indicate the estimates for the predictor in a separate model that includes only this predictor as a fixed effect.

varied from month to month, depending on how connectivity changed in the growing internal network. A more direct way to assess and compare the contribution of EXT in relation to other word-level factors is through conducting linear regressions, where connectivity in the learning environment, frequency and length predict the age of acquisition.

For word length, we counted the number of phonemes in our generated IPA 286 transcription. For word frequency, we used the frequency estimates from Braginsky et al. 287 (2016) where unigram counts were derived based on CHILDES corpora in each language 288 (MacWhinney, 2014). For each word, counts included words that shared the same stem (e.g., 289 'cats' counts as "cat"), or words that were synonymous (e.g. "father" counts as "daddy"). 290 Although these frequency counts use transcripts from independent sets of children, they are 291 based on large samples, and this allows us to average out possible differences between 292 children and the specificities of their input (see J. C. Goodman et al., 2008). 293

We conducted two analyses. We fit a linear regression for each language, and we fit a

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linear mixed-effect model to all the data pooled across languages, with language as a random
effect. Figure 5 shows the coefficient estimate for each predictor in each language for
production and comprehension data. Figure 6 shows the coefficient estimates for all
languages combined (all predictors were centered and scaled).

The findings for the new predictors were as follows. Overall, frequency is the largest 299 and most consistent predictor of age of acquisition in both comprehension and production 300 data and across languages, endorsing results for nouns across a variety of analyses 301 (Braginsky et al., 2016; J. C. Goodman et al., 2008; B. C. Roy et al., 2015). Word length is 302 more predictive for production than comprehension (and this difference is very clear in the 303 global model), replicating previous work (Braginsky et al., under review). Thus, word length 304 seems to reflect the effects of production's constraints rather than than comprehension's 305 constraints, i.e., longer words are harder to articulate but they may not be significantly more 306 difficult to store and access. 307

As for the factors of interest, i.e., semantic and phonological connectivity, we found 308 cross-linguistic differences. Connectivity contributes to learning in some languages but not in 309 other. In particular, semantic connectivity does not explain variance in English data beyond 310 that explained by phonological connectivity, frequency and length. This contrasts with the 311 original finding in Hills et al. (2009). However, this might be due to our using a slightly 312 different model (which included word length as a covariate) and a larger dataset. That said, 313 and despite these apparent cross-linguistic differences, both phonological and semantic 314 connectivity are significant predictors in the combined model (Figure 6). 315

316 Discussion

This study provided an analysis of network growth during development. We compared two network growth scenarios described in the pioneering work of Steyvers and Tenenbaum (2005) and Hills et al. (2009). The first scenario, INT (originally called Preferential Attachment), described a rich-get-richer network growth model in which the current

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structure of the learner's internal network determines future growth; the other, EXT (originally called Preferential Acquisition) described a model in which the external, global 322 environmental network structure determines learners' growth patterns. These two 323 mechanisms represent two fundamentally different accounts of lexical growth: One suggests 324 that future word knowledge is primarily shaped by the children's past knowledge and its 325 organization, whereas the other suggests that learning is shaped, rather, by salient properties 326 in the input regardless of how past knowledge is organized. The present study tested the 327 generality of previous findings (Hills et al., 2010, 2009) by 1) investigating phonological 328 networks together with semantic networks, 2) testing both comprehension- and 329 production-based vocabularies, and 3) comparing the results across 10 languages. 330

We found that the original findings reported in Hills et al. (2009) generalize well across all these dimensions. First, just like semantic networks, phonological networks grow via the 332 externally-driven scenario (EXT), not by the internally-driven mechanism (INT). Second, 333 comprehension-based vocabularies grow in a way similar to production-based vocabularies. 334 Finally, the findings were, overall, similar across the 10 languages we tested. Although we find some cross-linguistic variation when semantic and phonological networks were pitted against frequency and length, this variability is to be taken with a grain of salt as it might be exaggerated in our study by the limited and partially-overlapping sample of nouns for each language. In fact, both phonological and semantic connectivity are significant predictors above and beyond frequency and length when data are pooled across languages. 340

These findings corroborate the hypothesis that children start by learning words that 341 have high similarity to a variety of other words in the learning environment, not in the child's available lexicon. This hypothesis implies that children are sensitive to highly 343 connected words although they do not initially have access to the full network, thus raising some important questions: What mechanism allows children to distinguish highly connected 345 words from other words? Besides, why would highly connected words be easier to learn? 346

One possibility is that these patterns emerge from children's use of statistical learning

abilities (Aslin & Newport, 2012; Saffran, Aslin, & Newport, 1996; Smith & Yu, 2008). The
term "statistical learning" has been used in the developmental literature to describes the
process by which one acquires information about their environment through tracking the
frequency distribution of some elements (e.g., words) in different contexts. An important
property of this kind of learning is that it occurs without explicit instructions and through
mere exposure to the input. Previous work in this line of research has documented specific
mechanisms which can explain the patterns found in the current study.

For example, in the semantic domain, growth according to EXT can be explained by a 355 mechanism similar to cross-situational learning (Pinker, 2013; Smith & Yu, 2008; Yurovsky 356 & Frank, 2015). According to this mechanism, children track the co-occurrence of concrete 357 nouns with their possible semantic referents. The referent of a word heard in only one 358 naming situation can be ambiguous (e.g., when the word "ball" is heard for the first time in 350 the presence of both a ball and a chair), but hearing the same word in a diversity of 360 semantic contexts allows the learner to narrow down the set of possible word-object 361 mappings. In our case, free association (used to determine semantic network connectivity) is 362 related to contextual co-occurrence (Fourtassi & Dupoux, 2013; Griffiths, Steyvers, & 363 Tenenbaum, 2007), meaning that highly connected words will tend to occur in a variety of speech and referential contexts. This fact makes such words easier to learn because they have more referential disambiguating cues across learning contexts. Crucially, children can learn these words without necessarily knowing the meaning of all other words with witch 367 they co-occur (hence the similarity with EXT). This possibility is supported by the finding 368 that words' diversity of occurrence in child directed speech predicts their age of learning (Hills et al., 2010). 370

In the phonological case, network growth according to EXT is also compatible with a scenario whereby children are tracking lwo level statistical patterns, e.g., high probability sound sequences. Indeed, connectivity in the phonological network is inherently correlated with phonotactic probability (Vitevitch, Luce, Pisoni, & Auer, 1999). That is, highly

connected words tend to be made of frequent sound sequences. Children are sensitive to local phonotactic regularities (Jusczyk, Luce, & Charles-Luce, 1994) and this sensitivity might lead them to learn higher-probability words more easily (Storkel, 2001). This explanation is supported by computational simulations that show how learning general phonotactics patterns create "well-worn paths" which allow the models to represent several distinct but phonologically neighboring words (Dell, Juliano, & Govindjee, 1993; Takac, Knott, & Stokes, 2017).

Besides using their own statistical learning skills, children could also benefit from the way their caregivers speak. Perhaps the caregivers put more emphasis on the words that are highly connected in *their* mature lexical network. This emphasis would guide children to learn first these highly connected words even though children do not have access to the distribution of words' connectivity in the final network. Investigating this possibility would require further research on caregiver-child interaction (MacWhinney, 2014; B. C. Roy et al., 2015), examining what words are introduced over development and the extent to which children's uptake is influenced by this input (Clark, 2007; Hoff & Naigles, 2002).

This work shares a number of limitations with previous studies using similar research 390 strategy and datasets. Chief among these limitations is the fact that the age of word 391 acquisition is computed using different children at different ages (due to the fact that 392 available CDI data is mainly cross-sectional). Although this measure has proven highly 393 consistent (Fenson et al., 1994), it led us to focus on studying the learning mechanism of the 394 "average" child. Individual trajectories, however, could lead to different netwtok strutures 395 and show different learning patterns. For example, using longitudinal data Beckage, Smith, and Hills (2011) found differences between typical and late talkers in terms of the semantic network structure. Besides, although our study endorses the externally-driven account of network growth, this does not mean individual children never use some variant of INT or 399 some combination of both INT and EXT (Beckage and Colunga, under review). For 400 example, some children develop "islands of expertise", that is, well organized knowledge 401

about a certain topic (e.g., birds or dinosaurs). This prior knowledge enables these children to learn new related words more easily (e.g., Chi & Koeske, 1983).

To conclude, our work validates and generalizes previous results in early network
development. It suggests that the advantage of highly connected words may result, at least
in the early stages of word learning, from the operation of simpler mechanisms in both the
semantic and phonological domains. One question for future experimental work is whether
such correlational patterns of growth can be produced in controlled behavioral experiments.

All data and code for these analyses are available at

https://github.com/afourtassi/networks

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