PSTAT100 Lab4 Solutions

Lab 4: Smoothing

Introduction

So far, you've encountered a number of visualization techniques for displaying tidy data. In those visualizations, all graphic elements represent the values of a dataset—they are visual displays of actual data.

In general, **smoothing means evening out**. Visualizations of actual data are often irregular—points are distributed widely in scatterplots, line plots are jagged, and bars can be discontinuous. When we look at such visuals, we tend to attempt to look past these irregularities in order to discern patterns. For example, we may want to identify the **overall shape** of a histogram or the general trend in a scatterplot. Smoothing techniques allow us to **even out irregularities in graphical displays of actual data**, helping the eye detect underlying patterns.

For our purposes, smoothing consists of drawing a **line or curve** on top of an existing statistical graphic. From a technical point of view, this amounts to **adding derived geometric objects** to a graphic that have fewer irregularities than the displays of actual data.

In this lab, you'll learn some basic **smoothing techniques**:

- Kernel density estimation for histogram smoothing
- LOESS smoothing for scatterplots
- Linear smoothing via regression

We will implement these techniques using the **ggplot2** package in R.

Sections of the lab:

- 0. Introduction to ggplot2 smoothing functions
- 1. Histogram smoothing: Kernel density estimation
- 2. Scatterplot smoothing: LOESS and linear regression smoothing
- 3. Creating polished visualizations

Goals:

- Get familiar with **ggplot2** for creating smooth visualizations.
- Construct handmade histograms using density estimation.
- Implement kernel density estimation using geom_density().
- Implement LOESS smoothing using geom_smooth(method = "loess").
- Implement linear regression smoothing using geom_smooth(method = "lm").

Dataset:

We'll use the same data as last week to stick to a familiar example:

```
## ensure that the .csv file is saved in the same folder as this .qmd file
data <- read.csv("lab4-data.csv")
head(data)</pre>
```

	Country.Name Ye	ear Life	e.Expectancy	Male	.Life.Expectan	су	Female.Life.Expectancy
1	Afghanistan 20	019	63.2		63	.3	63.2
2	Afghanistan 20	015	61.7		61	.0	62.3
3	Afghanistan 20	010	59.9		59	.6	60.3
4	Albania 20	019	78.0		76	.3	79.9
5	Albania 20	015	77.8		76	. 1	79.7
6	Albania 20	010	76.2		74	.2	78.3
	<pre>GDP.per.capita</pre>	region	sub.reg	gion	Population		
1	507.1034	Asia	Southern A	Asia	38041754		
2	578.4664	Asia	Southern A	Asia	34413603		
3	543.3030	Asia	Southern A	Asia	29185507		
4	5353.2449	Europe	Southern Eur	rope	2854191		
5	3952.8012	Europe	Southern Eur	rope	2880703		
6	4094.3503	Europe	Southern Eur	rope	2913021		

str(data)

```
'data.frame':
               620 obs. of 9 variables:
$ Country.Name
                              "Afghanistan" "Afghanistan" "Afghanistan" "Albania" ...
                        : chr
$ Year
                              2019 2015 2010 2019 2015 2010 2000 2019 2015 2010 ...
                        : int
$ Life.Expectancy
                        : num 63.2 61.7 59.9 78 77.8 76.2 73.5 77.1 76.5 75.9 ...
$ Male.Life.Expectancy : num 63.3 61 59.6 76.3 76.1 74.2 70.7 76.2 75.6 75 ...
$ Female.Life.Expectancy: num 63.2 62.3 60.3 79.9 79.7 78.3 76.9 78.1 77.5 76.8 ...
$ GDP.per.capita
                        : num 507 578 543 5353 3953 ...
$ region
                        : chr "Asia" "Asia" "Europe" ...
$ sub.region
                        : chr "Southern Asia" "Southern Asia" "Southern Eu
$ Population
                        : num 38041754 34413603 29185507 2854191 2880703 ...
```

Data Transformations in ggplot2

In ggplot2, data transformations such as filtering, binning, and smoothing can be performed before or within the plotting commands. These transformations help in pre-processing the dataset and making visualizations clearer.

In this section, we will focus on:

- Filtering data for visualization.
- Creating histograms with binned data.
- Using functions in ggplot2 library to streamline transformations.

Filtering Data

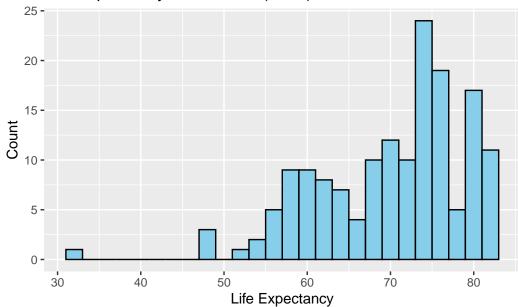
Last week, you saw how to create histograms. As a refresher, to make a histogram of life expectancies across the globe in **2010**, we can **filter** the dataset and then plot it using the following commands:

```
# Load necessary library
library(ggplot2)
library(dplyr) # For data manipulation

# Filter data for the year 2010
data2010 <- data %>% filter(Year == 2010)
```

```
# Plot histogram of Life Expectancy in 2010
ggplot(data2010, aes(x = Life.Expectancy)) +
  geom_histogram(binwidth = 2, fill = "skyblue", color = "black") +
  labs(title = "Life Expectancy Distribution (2010)",
        x = "Life Expectancy",
        y = "Count")
```

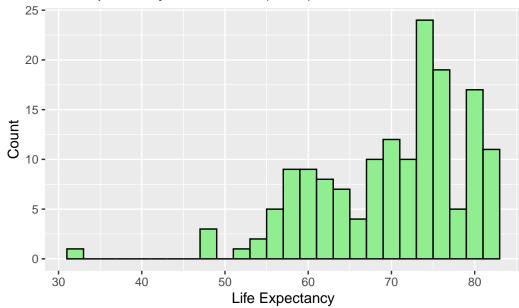
Life Expectancy Distribution (2010)



Alternatively, we can filter within the ggplot command to avoid creating an intermediate dataset:

```
# Filtering within the plotting command
ggplot(data %>% filter(Year == 2010), aes(x = Life.Expectancy)) +
  geom_histogram(binwidth = 2, fill = "lightgreen", color = "black") +
  labs(title = "Life Expectancy Distribution (2010)",
        x = "Life Expectancy",
        y = "Count")
```

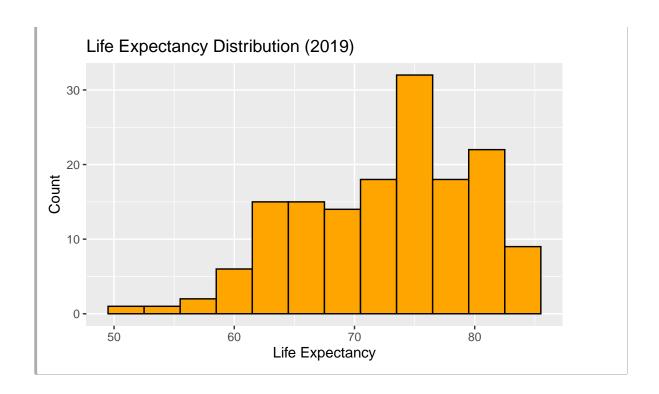




Question 1:

Construct a histogram of life expectancies across the globe in 2019 by filtering the dataset within the ggplot() function. Use a bin size of 3 years instead of 2.

```
ggplot(data %>% filter(Year == 2019), aes(x = Life.Expectancy)) +
  geom_histogram(binwidth = 3, fill = "orange", color = "black") +
  labs(title = "Life Expectancy Distribution (2019)",
        x = "Life Expectancy",
        y = "Count")
```



Counting of Observations in Each Bin

In ggplot2, the process of counting how many observations fall into each bin is handled automatically when creating histograms. This aggregation step reduces the number of values by summarizing raw data into bins.

Instead of manually computing bin counts, we can **extract the aggregated bin data** directly from ggplot2 using ggplot_build().

Extracting Binned Data with ggplot_build()

The codes below give us a dataframe containing the **bin midpoints** (x) and **counts** (count), which we can use for further analysis.

```
# Filter data for the year 2010
data2010 <- data %>% filter(Year == 2010)

# Create histogram using stat_bin()
p <- ggplot(data2010, aes(x = Life.Expectancy)) +</pre>
```

```
stat_bin(binwidth = 2, aes(y = ..count..))

# Extract binned data
binned_data <- ggplot_build(p)$data[[1]]

# Display extracted bin counts
head(binned_data[,c("x","count")])</pre>
```

```
x count
1 32 1
2 34 0
3 36 0
4 38 0
5 40 0
6 42 0
```

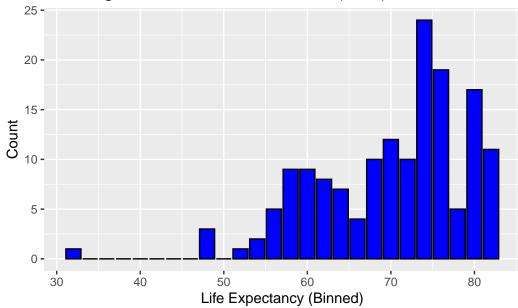
```
tail(binned_data[,c("x","count")])
```

```
x count
21 72 10
22 74 24
23 76 19
24 78 5
25 80 17
26 82 11
```

Plot the Extracted Aggregated Data

Now that we have extracted the bin counts from ggplot_build(), we can plot the manually aggregated data using geom_bar().





Question 2:

Modify the code above to **extract** the binned data (counts of observations and midpoints for each bin) and **plot** the aggregated data (using **geom_bar()**) for **2015**, using a **bin size of 3 years**.

```
data2019 <- data %>% filter(Year == 2019)

p_2019 <- ggplot(data2019, aes(x = Life.Expectancy)) +
    stat_bin(binwidth = 3, aes(y = ...count..))

binned_data_2019 <- ggplot_build(p_2019)$data[[1]]

# Display extracted bin counts
head(binned_data_2019[,c("x","count")])

    x count
1 51     1
2 54     1
3 57     2</pre>
```

```
4 60
         6
5 63
        15
6 66
        15
tail(binned_data_2019[,c("x","count")])
    x count
7
   69
         14
  72
         18
9
  75
         32
10 78
         18
         22
11 81
          9
12 84
ggplot(binned_data_2019, aes(x = x, y = count)) +
  geom_bar(stat = "identity", fill = "orange", color = "black") +
  labs(title = "Counting of Observations in Each Bin (2019)",
       x = "Life Expectancy (Binned)",
       y = "Count")
     Counting of Observations in Each Bin (2019)
  30 -
  20 -
Count
  10-
                        60
                                         70
        50
                                                         80
                          Life Expectancy (Binned)
```

Converting Count Scale to Density Scale in ggplot2

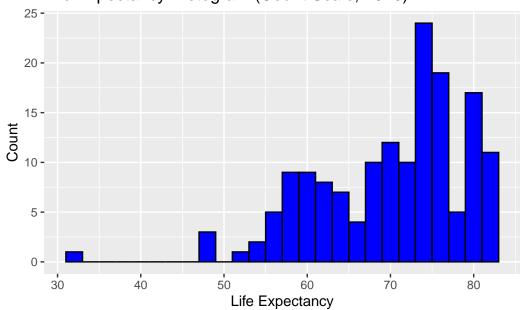
By default, histograms in ggplot2 are displayed using the **count scale**, where the y-axis represents **the number of observations in each bin**.

However, we can also display histograms using the **density scale**, where the y-axis represents **proportions of the total bar area**. This ensures that the total area under the histogram **sums to 1**, making it easier to compare distributions across different datasets or sample sizes.

Histogram on Count Scale

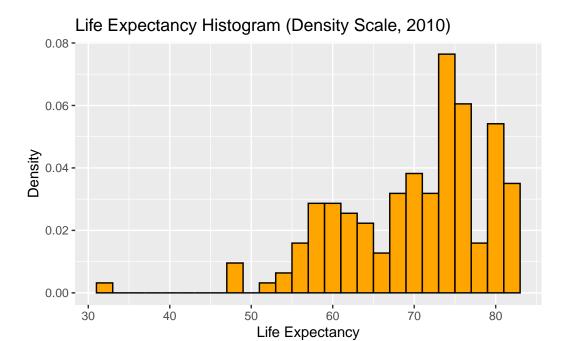
First, let's plot a **regular** histogram where the y-axis represents the **count** of observations per bin.





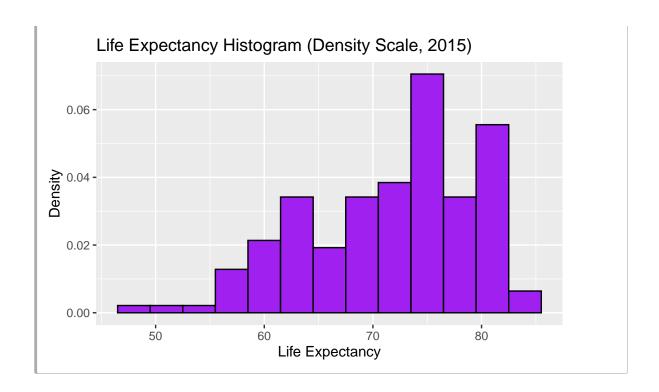
Histogram on Density Scale

To switch to the density scale, we simply replace aes(y = ..count..) with aes(y = ..density..) in $geom_histogram()$. This automatically normalizes the histogram, ensuring that the total area sums to 1.



Question 3: Convert to Density Scale for 2015

Modify the code above to convert the histogram for the year **2015** to the **density scale**, using a **bin size of 3 years**.



Density Estimation in ggplot2

Now that we have explored different transformations, we can apply a **smoothing technique** known as **kernel density estimation**.

Histograms show the **empirical density** by displaying the distribution of values in the sample. A **kernel density estimate** is simply a **smoothed version of the empirical density**. It approximates the **distribution of population values** that the sample comes from.

Why Use Kernel Density Estimation?

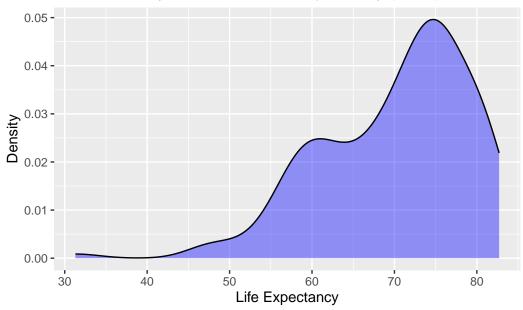
- Helps **visualize** the distribution shape more clearly.
- Allows identification of **multiple peaks** (multi-modality).
- Smooths out irregularities in histograms

Instead of manually computing kernel density estimates, we can use the **built-in** geom_density() function in ggplot2.

Plot Kernel Density Estimate

To generate a density estimate for life expectancies in 2010, we use geom_density().

Kernel Density Estimate of Life Expectancy (2010)

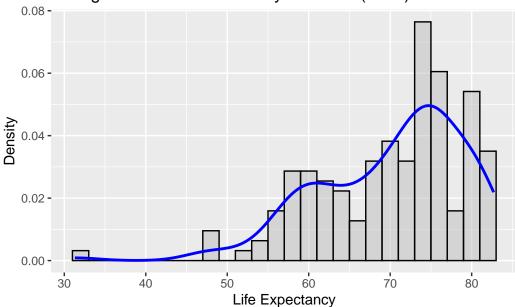


This produces a **smooth curve** representing the estimated probability density of life expectancy values.

Overlay Density Curve on Histogram

We can **overlay** the density estimate on top of the histogram to compare the **empirical** distribution (histogram) and the **smoothed** estimate.

Histogram with Kernel Density Estimate (2010)



Bandwidth Adjustment

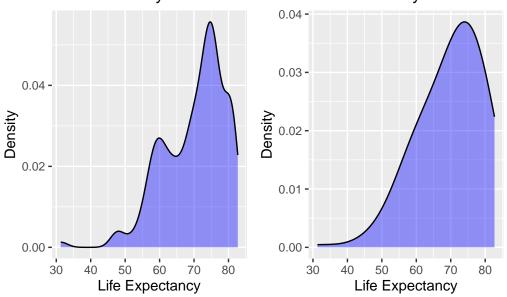
The bandwidth parameter controls the amount of smoothing.

- Larger bandwidth = Smoother curve (less detail)
- Smaller bandwidth = Wigglier curve (More local detail)

We can adjust the bandwidth in geom_density() using the bw argument

```
library(patchwork)
p1<- ggplot(data2010, aes(x = Life.Expectancy)) +
  geom_density(fill = "blue", alpha = 0.4, bw = 2) +
  labs(title = "Kernel Density Estimate with Bw = 2",</pre>
```

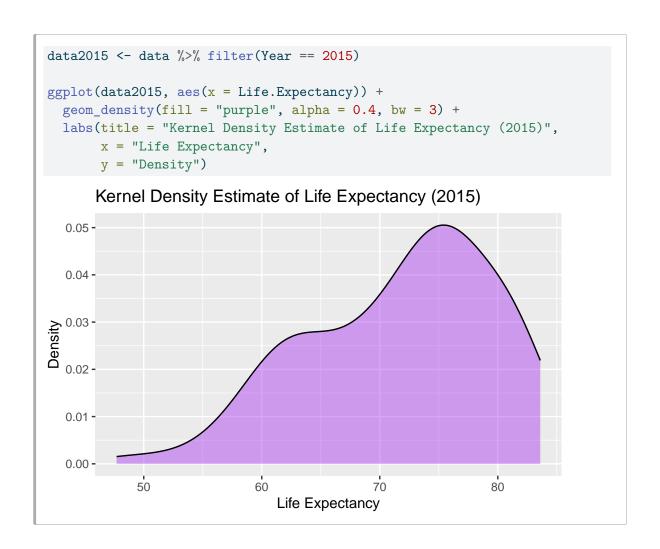
Kernel Density Estimate with Bw ¥@rnel Density Estimate wit



Question 4: Kernel Density Estimation for 2015

Modify the plotting code by decreasing the bandwidth parameter.

Try several values, and then choose one that you feel captures the shape of the distribution well without getting too wiggly.



Comparing Distributions

The visual advantage of a **kernel density estimate** is even more apparent when comparing distributions.

A major task in **exploratory data analysis** is understanding how the distribution of a variable changes over time or across groups. For example, we have already seen that **life expectancy seems to change over time**. We can explore this further by **comparing distributions for different years**.

We can plot **multiple density estimates** on the **same plot** by grouping the data by year.

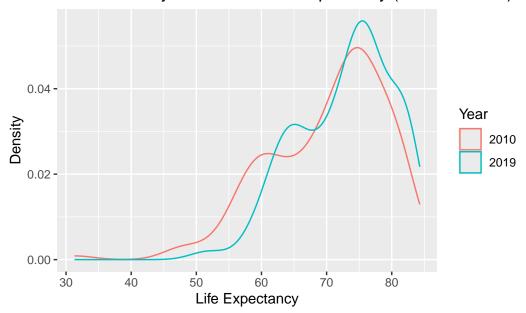
Compare Kernel Density Estimates for Different Years

We compare the life expectancy distributions for 2010 and 2019 by grouping by Year in geom_density().

```
# Filter data for 2010 and 2019
data_filtered <- data %>% filter(Year %in% c(2010, 2019))

# Plot density estimates for both years
ggplot(data_filtered, aes(x = Life.Expectancy, color = as.factor(Year))) +
    geom_density() +
    labs(title = "Kernel Density Estimate of Life Expectancy (2010 vs. 2019)",
        x = "Life Expectancy",
        y = "Density",
        color = "Year")
```

Kernel Density Estimate of Life Expectancy (2010 vs. 2019)



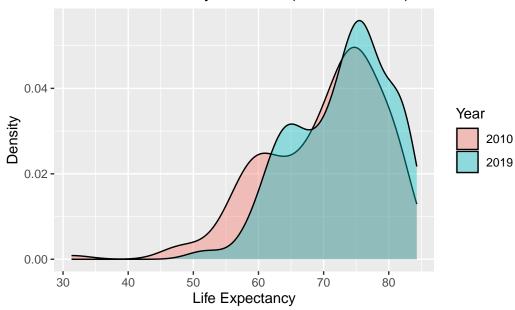
Fill the Area Under the Density Curve

To enhance visibility, we fill the density curves with transparency using fill = Year and alpha for transparency.

```
# Density plot with filled areas
ggplot(data_filtered, aes(x = Life.Expectancy, fill = as.factor(Year))) +
   geom_density(alpha = 0.4) +
```

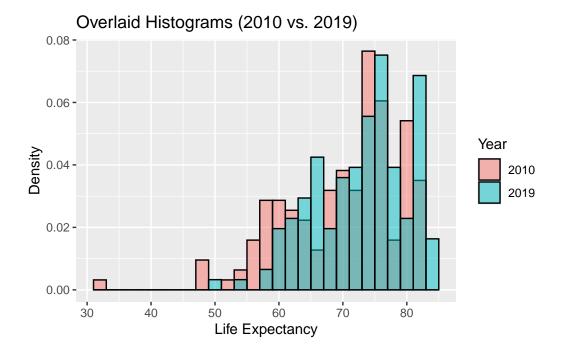
```
labs(title = "Filled Kernel Density Estimate (2010 vs. 2019)",
    x = "Life Expectancy",
    y = "Density",
    fill = "Year")
```

Filled Kernel Density Estimate (2010 vs. 2019)



Comparing with Histograms (Less Effective)

Overlaying **histograms** can sometimes be useful, but they can also be harder to interpret compared to density plots.



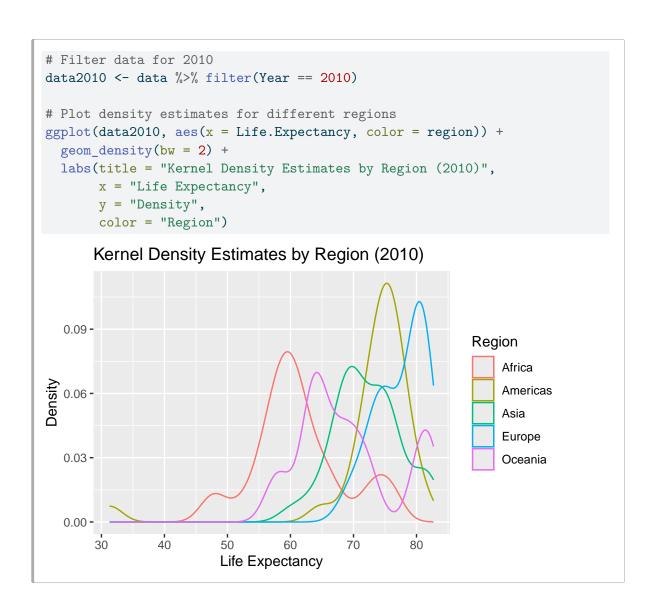
Question 5: Multiple Density Estimates

Follow the example above to construct a plot showing separate density estimates of life expectancy for each region in 2010.

You can choose whether to fill the area beneath the smooth curves or not. Be sure to adjust the bandwidth parameter and select a value that makes sense.

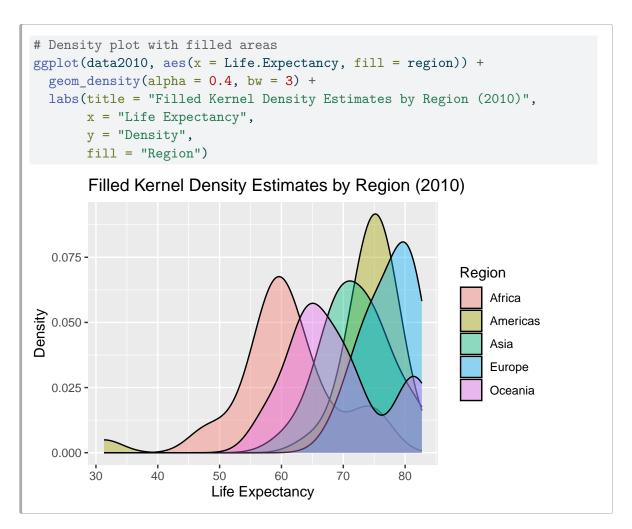
Step 1: Compute Density Estimates for Each Region

We filter the dataset for 2010 and plot separate density curves for each region.



Step 2: Fill the Area Under the Density Curves

To enhance visibility, we can fill the area under the density curves with transparency using fill = region and alpha.



Note:

Remember to modify the bw parameter in above codes to adjust the smoothness of the density curves.

Question 6: Interpretation

Do the distributions of life expectancies seem to differ by region? If so, what is one difference that you notice? Answer in 1-2 sentences.

YOUR ANSWER:

Yes, the distributions of life expectancies differ by region.

One noticeable difference is that the mode of the distribution of Africa gives the lowest life expectancies, around 50-60 years, while that os Europe has the highest, mostly above

75 years. Additionally, the distribution of life expectancies of Asia displaying more variability. This suggests that life expectancy varies significantly across regions, likely due to differences in healthcare, economic development, and living conditions.

Question 7: Outlier

Notice that **small peak far to the left** in the **Americas** region. That is an **outlier** in life expectancy.

Tasks:

- 1. Identify the country with the lowest life expectancy in the Americas in 2010.
- 2. Check life expectancies for that country across different years.
- 3. Investigate why life expectancy was so low in that country for 2010.

Task 1: Find the Country with the Lowest Life Expectancy

Filter for 2010 and Americas, then find the **country** with the **lowest** life expectancy.

```
# Find the country with the lowest life expectancy in the Americas in 2010
lowest Americas <- data %>%
 filter(Year == 2010, region == "Americas") %>%
 arrange(Life.Expectancy) %>%
 head(1) # Select the lowest value
# Print the outlier row
lowest_Americas
 Country.Name Year Life.Expectancy Male.Life.Expectancy Female.Life.Expectancy
1
         Haiti 2010
                               31.3
                                                                            35.4
                                                      28
 GDP.per.capita
                                               sub.region Population
                   region
1
        1172.099 Americas Latin America and the Caribbean
                                                              9949322
```

Task 2: Examine Life Expectancies for This Country

Now, check life expectancy across all years for the identified outlier country.

YOUR ANSWER:

```
# Get the country name
outlier country name <- lowest Americas $Country.Name
# Filter data for this country across all years
outlier_country <- data %>%
  filter(Country.Name == outlier_country_name)
# Print the life expectancy trend
outlier_country
  Country.Name Year Life.Expectancy Male.Life.Expectancy Female.Life.Expectancy
1
         Haiti 2019
                                64.1
                                                     63.3
                                                                             64.8
2
         Haiti 2015
                                62.6
                                                     62.1
                                                                             63.1
3
         Haiti 2010
                                31.3
                                                     28.0
                                                                             35.4
                                                                             57.2
         Haiti 2000
                                57.0
                                                     57.0
  GDP.per.capita
                                                sub.region Population
                   region
1
        1272.491 Americas Latin America and the Caribbean
                                                             11263077
2
        1389.120 Americas Latin America and the Caribbean
                                                             10695542
        1172.099 Americas Latin America and the Caribbean
3
                                                              9949322
4
         811.534 Americas Latin America and the Caribbean
                                                              8463806
```

Task 3: Interpretation

What happened in 2010?

Can you explain why life expectancy was so low for this country in 2010? Hint: If you're unsure, search for major events in this country in 2010 (e.g., conflicts, disasters, epidemics).

YOUR ANSWER:

The country with the lowest life expectancy in the Americas in 2010 was Haiti. Its life expectancy dropped sharply due to the devastating earthquake in January 2010, which caused a major humanitarian crisis, widespread destruction, and a high death toll.

Scatterplot Smoothing

In this section, you'll explore two techniques for smoothing scatterplots:

- 1. LOESS (Locally Weighted Scatterplot Smoothing) Produces a curved trend line.
- 2. Linear Regression Smoothing Produces a straight-line trend.

Recall that in lab 3, we illustrated a variable transformation to reduce skewness in GDP per capita, That is, we will apply a log transformation to GDP.per.capita.

```
data_mod1 <- data %>%
  mutate(log_GDP_per_capita = log(GDP.per.capita))
```

LOESS or Local Polynomial Regression Fitting

Locally weighted scatterplot smoothing (LOESS) is a flexible technique for visualizing trends in scatterplots. It is conceptually similar to kernel density estimation, but applied to scatterplots instead of distributions.

To illustrate, let's examine the relationship between **GDP** per capita and life expectancy for the year 2010.

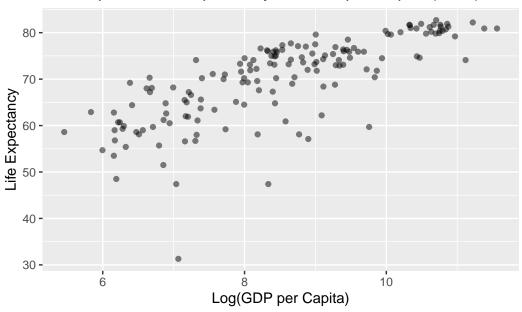
Step 1: Scatterplot of GDP per Capita vs. Life Expectancy

First, we create a basic **scatterplot**.

```
# Filter data for 2010
data_2010 <- data_mod1 %>% filter(Year == 2010)

# Scatterplot
ggplot(data_2010, aes(x = log_GDP_per_capita, y = Life.Expectancy)) +
    geom_point(alpha = 0.5) +
    labs(title = "Scatterplot of Life Expectancy vs. GDP per Capita (2010)",
        x = "Log(GDP per Capita)",
        y = "Life Expectancy")
```

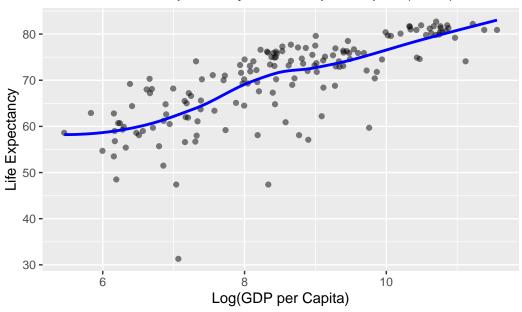
Scatterplot of Life Expectancy vs. GDP per Capita (2010)



Step 2: Add LOESS

To add a LOESS curve, we use geom_smooth(method = "loess").

LOESS of Life Expectancy vs. GDP per Capita (2010)

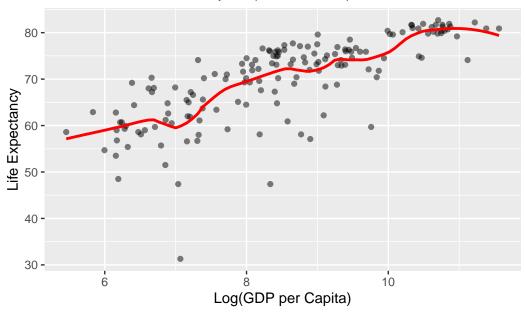


Step 3: Adjusting LOESS Span

The **span parameter** controls the degree of smoothing:

- Larger span \rightarrow Smoother curve (more general trend)
- Smaller span \rightarrow Wigglier curve (more localized trends)

LOESS with Smaller Span (More Detail)

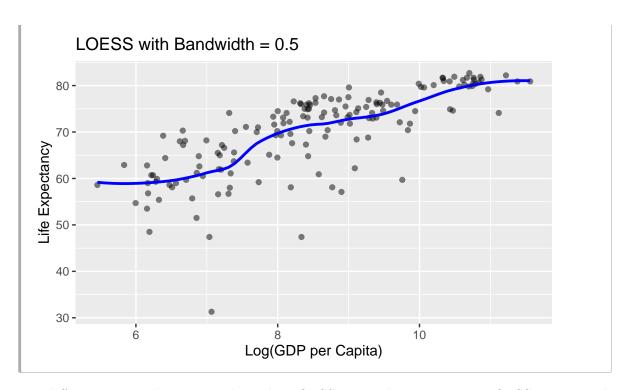


Question 8: LOESS Bandwidth Selection

Tinker with the **bandwidth parameter** (span in ggplot2) to see its effect on the **smoothness** of the LOESS curve.

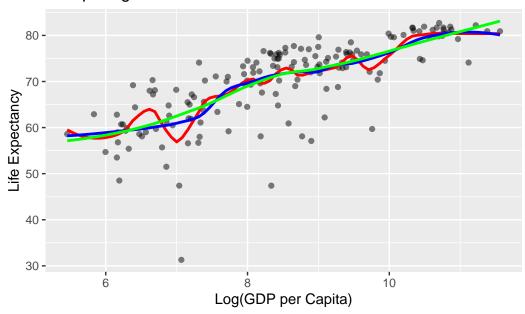
Choose a value that produces a trend line that best represents the data

Modify the span parameter in geom_smooth() to change the smoothness of the LOESS curve.



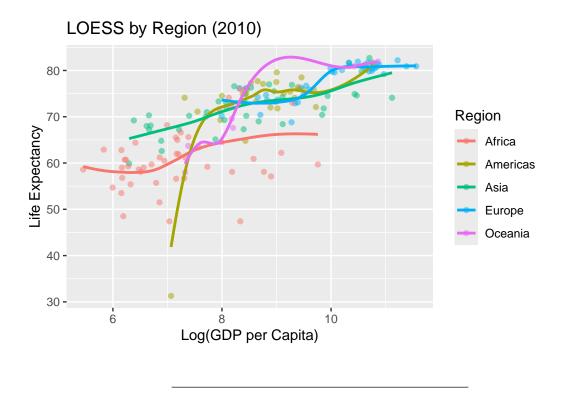
Try different span values to see how the LOESS curve changes. Draw LOESS curves with different span values in the same scatterplot.

Comparing Different LOESS Bandwidths



Groupwise LOESS (Separate Curves by Region)

To compute LOESS trends for each region separately, set group = region.



Regression Smoothing

Later in the course, you will learn about **linear regression**, but here we introduce it as a **visualization technique**.

- Like LOESS, linear regression smooths scatterplot data.
- The key difference: Linear regression produces a straight line, while LOESS allows curvature.

In cases where LOESS curves are almost linear, a regression line may be the cleaner choice.

Step 1: Scatterplot of GDP per Capita vs. Life Expectancy

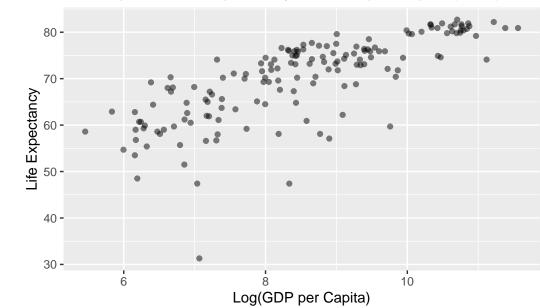
First, we create a basic scatterplot.

```
# Filter data for 2010
data_2010 <- data_mod1 %>% filter(Year == 2010)

# Scatterplot
ggplot(data_2010, aes(x = log_GDP_per_capita, y = Life.Expectancy)) +
```

```
geom_point(alpha = 0.5) +
labs(title = "Scatterplot of Life Expectancy vs. GDP per Capita (2010)",
    x = "Log(GDP per Capita)",
    y = "Life Expectancy")
```

Scatterplot of Life Expectancy vs. GDP per Capita (2010)

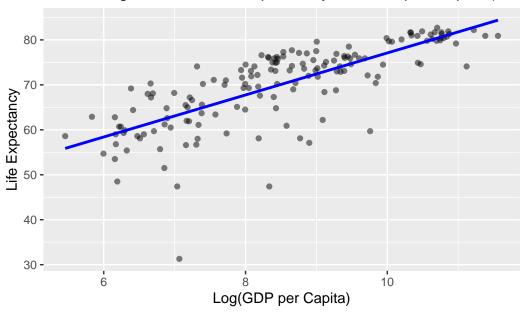


Step 2: Adding a Linear Regression Line

To add a linear regression trend, we use geom_smooth(method = "lm").

```
# Scatterplot with linear regression smoothing
ggplot(data_2010, aes(x = log_GDP_per_capita, y = Life.Expectancy)) +
    geom_point(alpha = 0.5) +
    geom_smooth(method = "lm", color = "blue", se = FALSE) +
    labs(title = "Linear Regression of Life Expectancy vs. GDP per Capita (2010)",
        x = "Log(GDP per Capita)",
        y = "Life Expectancy")
```

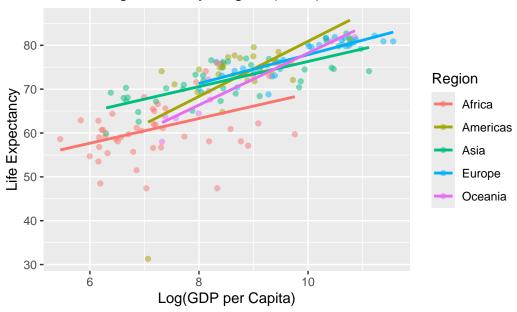
Linear Regression of Life Expectancy vs. GDP per Capita (2010)



Step 3: Groupwise Regression by Region

To compute separate regression lines for each region, we set color = region.

Linear Regression by Region (2010)

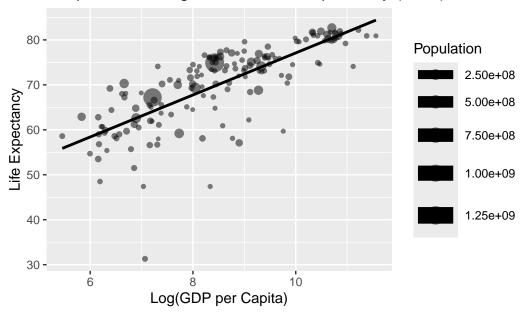


Question 9: Simple Regression Line

Modify the code to construct a scatterplot of life expectancy vs. log GDP per capita (2010)

- The points should be sized by population.
- Remove color grouping by region.
- Overlay a single linear regression line.

Simple Linear Regression of Life Expectancy (2010)



Submission

- 1. Rename and save the notebook.
- 2. Restart the kernel and run all cells. (CAUTION: if your notebook is not saved, you will lose your work.)
- 3. Carefully look through your notebook and verify that all computations execute correctly. You should see **no errors**; if there are any errors, make sure to correct them before you submit the notebook.
- 4. Download the notebook as an .qmd file. This is your backup copy.
- 5. Export the notebook as PDF and upload to Canvas.