Submission for the Test Flight Project for Introduction to Mathematical Thinking.

## Problem 10:

**Proposition:** For the collection of intervals  $A_n = [0, \frac{1}{n}]$ , where n = 1, 2, ..., every  $A_{n+1} \subset A_n$  and  $\bigcup_{n=1}^{\infty} A_n = \{0\}$ .

**Proof:** Because  $\frac{1}{n}$  decreases as n increases and cannot be negative, we know that the limit of  $\frac{1}{n}$  goes to 0 as n goes to  $\infty$ . Thus, the limit of the right side of the interval will go to 0 as n goes to  $\infty$ , so the interval will tend to (0,0). And because the interval is closed on both sides, 0 is the only member of that set, so the intersection of all of the intervals  $A_n$  will be  $\{0\}$ .  $\square$