Submission for the Test Flight Project for Introduction to Mathematical Thinking.

Problem 10:

Proposition: For the collection of intervals $A_n = [0, \frac{1}{n}]$, where n = 1, 2, ..., every $A_{n+1} \subset A_n$ and $\bigcup_{n=1}^{\infty} A_n = \{0\}$.

Proof: Because $\frac{1}{n}$ decreases as n increases, we know that the limit of $\frac{1}{n}$ goes to 0 as n goes to ∞ . Thus, the limit of the right side of the interval will go to 0 as n goes to ∞ , so the interval will tend to (0,0). And because the interval is closed on both sides, 0 is the only member of that set, so the intersection of all of the intervals A_n will be $\{0\}$.