

**Problem 5:**

**Proposition:** For any  $n \in \mathbb{Z}$ , at least one of the integers  $n + 1$ ,  $n + 2$ , or  $n + 4$  is divisible by 3.

**Proof:** Let  $n = 3$ . Then we see that  $3 + 1 = 4$ ,  $3 + 2 = 5$ , and  $3 + 4 = 7$ . None of these are multiples of 3 which shows our initial claim to be false. □