Learning to program with F#

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Chapter 1

Preface

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¹Something about why this book is written, the course, and personal notes.

Chapter 2

Introduction

Programming is the act of solving a problem by writing a program to be executed on a computer. A general method for solving problems was given by George Pólya [5] and adapted to programming is:

Understand the problem: To solve any problem it is crucial that the problem formulation is understood, and questions like: What is to be solved? Do you understand everything in the problem description. Is all information for finding the solution available or is something missing?

Design a plan: Good designs means that programs are faster to program easier to debug and maintain. So before you start typing a program consider things like: What are the requirements and constraints for the program? Which components should the program have? How are these components to work together? Designing often involves drawing a diagram of the program, and writing pseudo-code on paper.

Implement the plan: Implementation is the act of transforming a program design into a code. A crucial part of any implementation is choosing which programming language to use. Also, the solution to many problems will have a number of implementations which vary in how much code they require, to which degree they rely on external libraries, which programming style the are best suited for, what machine resources they require, and what their running times are. With a good design, then the coding is usually easy, since the design will have uncovered the major issues and found solutions for these, but sometimes implementation reveals new problems, which requires rethinking the design. Most implementations also include writing documentation of the code.

Reflect on the result: A crucial part in any programming task is ensuring that the program solves the problem sufficiently. E.g., what are the program's bugs, is the documentation of the code sufficient and relevant for its intended use. Is the code easily maintainable and extendable by other programmers. Are there any general lessons to be learned from or general code developed by the programming experience, which may be used for future programming sessions?

Programming is a very complicated process, and the steps in Pólya's list are almost always to be performed, but the order of the steps and the number of times each step is performed varies. ¹ This book focusses on 3 fundamentally different approaches to programming:

Imperative programming, which is a type of programming that statements to change the program's state. Imperative programming emphasises how a program shall accomplish a solution and less on what the solution is. A cooking recipes is an example of the spirit of imperative programming. Almost all computer hardware is designed to execute low-level programs written in imperative style. The first major language was FORTRAN [2] which emphasized imperative style of programming.

· Imperative programming

· Declarative programming

¹Should we mention core activities: Requirements, Design, Construction, Testing, Debugging, Deployment, Maintenance?

 $[\]cdot$ statements

 $[\]cdot$ state

- Declarative programming, which emphasises what a program shall accomplish but not how. We will consider Functional programming as a type of declarative programming. A type of programming which evaluates functions and avoids state changes. The program consists of expressions instead of statements. As a consequence, the output of functions only depends on its arguments. Functional programming has its roots in lambda calculus [1], and the first language emphasizing functional programming was Lisp [3].
- Structured programming, , which emphasises organisation of code in units with well defined interfaces and isolation of internal states and code from other parts of the program. We will focus on Object-oriented programming is the example of structured programming. is a type of programming, where the states and programs are structured into *objects*. A typical object-oriented design takes a problem formulation and identifies key nouns as potential objects and verbs as potential actions to be take on objects. The first object-oriented programming language was Simula 67 developed by Dahl and Nygaard at the Norwegian Computing Center in Oslo.

Most programs follows a single programming paradigm as, e.g., one of the above, but are a mix. Nevertheless, this book will treat each paradigm separately to emphasize their advantages and disadvantages.

This book uses F# also known as Fsharp, which is a functional first programming language that also supports imperative and object oriented programming. It was originally developed for Microsoft's .Net platform, but is available as open source for many operating systems through Mono. As an introduction to programming, F# is a young programming language still under development, with syntax that at times is a bit complex, but it offers a number of advantages:

Interactive and compile mode F# has an interactive and a compile mode of operation.

Indentation for scope F# uses indentation to indicate scope.

Strongly typed F# is strongly typed, reducing the number of run-time errors.

Multi-platform F# is available on Linux, Mac OS X, Android, iOS, Windows, GPUs, and browsers via the Mono platform.

Free to use and open source F# is supported by the Fsharp foundation (http://fsharp.org) and sponsored by Microsoft.

Assemblies F# programs interface easily with other .Net and Mono programs through the language-independent, platform-independent bytecode called Common Intermediate Language (CIL).

Modern computing F# supports all aspects of modern computing including Graphical User Interfaces, Web programming, Information rich programming, Parallel algorithms, . . .

Integrated development environments (IDE) F# is supported by major IDEs such as Visual Studio (https://www.visualstudio.com) and Xamarin Studio (https://www.xamarin.com).

Learning to program requires mastering a programming language, however most programming languages contains details that are rarely used or used in contexts far from a specific programming topic. Hence, this book takes the approach to start with an introduction to the most basic concepts of F# in Part I, followed by the 3 programming paradigms in Part II–IV while gradually expanding the introduction of F# syntax and semantics. In Part V are a number of general topics given for reference. The disadvantage of this approach is that no single part contains a reference guide to F# and F# topics are revisited and expanded across the book. For further reading please consult http://fsharp.org.

- · Functional programming
- \cdot functions
- · expressions
- · Structured programming
- · Objectorientered programming · objects

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Part I

F# basics

Chapter 3

Executing F# code

3.1 Source code

F# is a functional first programming language that also supports imperative and object oriented programming. It also has strong support for parallel programming and information rich programs. It was originally developed for Microsoft's .Net platform, but is available as open source for many operating systems through Mono. In this text we consider F# 4.0 and its Mono implementation, which is different from .Net mainly in terms of the number of libraries accessible. The complete language specification is described in http://fsharp.org/specs/language-spec/4.0/FSharpSpec-4.0-latest.pdf.

F# has 2 modes of execution, interactive and compiled. Interactive mode is well suited for small experiments or back-of-an-envelope calculations, but not for programming in general. In Mono, the interactive system is started by calling fsharpi from the console, while compilation is performed with fshparc and execution of the compiled code is performed using the mono command. The various forms of fsharp programs are identified by suffixes:

.fs An implementation file

.fsi A signature file

.fsx A script file

.fsscript Same as .fsx

.exe An executable file

The implementation, signature, and script files are all typically compiled to produce an executable file, but syntactical correct code can also be entered into the interactive system, in which case these are called script-fragments. The implementation and signature files are special kinds of script files used for building modules.

- \cdot interactive · compiled
- \cdot console
- \cdot implementation file
- · signature file
- · script file

 \cdot modules

· executable file

· script-fragments

3.2Executing programs

Programs may either be executed by the interpreter or by compiling and executing the compiled code. In Mono the interpreter is called fsharpi and can be used in 2 ways: interactively, where a user enters 1 or more script-fragments separated by the ";;" token, or to execute a script file treated as a single script-fragment. To illustrate the difference, consider the following program, which declares a value a to be the decimal value 3.0 and finally print it to the console:

```
let a = 3.0
printfn "%g" a
```

An interactive session is obtained by starting the console, typing the fsharpi command, typing the lines of the program, and ending the script-fragment with the ";;" token:

```
$ fsharpi
F# Interactive for F# 4.0 (Open Source Edition)
Freely distributed under the Apache 2.0 Open Source License

For help type #help;;
> let a = 3.0
- printfn "%g" a;;
3

val a : float = 3.0
val it : unit = ()
> #quit;;
```

The interpreter is stopped by pressing ctrl-d or typing "#quit;;". Conversely, executing the file with the interpreter as follows,

```
$ fsharpi gettingStartedStump.fsx
```

Finally, compiling and executing the code is performed as,

```
$ fsharpc gettingStartedStump.fsx
F# Compiler for F# 4.0 (Open Source Edition)
Freely distributed under the Apache 2.0 Open Source License
$ mono gettingStartedStump.exe
3
```

Both the interpreter and the compiler translates the source code into a format, which can be executed by the computer. While the compiler performs this translation once and stores the result in the executable file, the interpreter translates the code every time the code is executed. Thus, to run the program again with the interpreter, then it must be retranslated as "\$fsharpi gettingStartedStump.fsx", but since the program has been compiled, then the compile-execute only needs the be re-executed "\$ mono gettingStartedStump.exe". On a Macbook Pro, with a 2.9 Ghz Intel Core i5, the time the various stages takes for this script are.

Command	Time
fsharpi gettingStartedStump.fsx	1.88s
fsharpc gettingStartedStump.fsx	1.90s
mono randomTextOrderO.exe	0.05s

I.e., executing the script with fsharpi is slightly faster than by first compiling it with fsharpc and then executing the result with mono, 1.88s < 0.05s + 1.90s, if the script were to be executed only once, but every future execution of the script using the compiled version requires only the use of mono, which is much faster than fsharpi, $1.88s \gg 0.05s$.

The interactive session results in extra output on the *type inference* performed, which is very useful for *debugging* and development of code-fragments, but both executing programs with the interpreted directly from a file and compiling and executing the program is much preferred for programming complete programs, since the starting state is well defined, and since this better supports *unit-testing* a method for debugging programs.

[·] type inference

[·] debugging

 $[\]cdot$ unit-testing

¹Remember to add something about the it value in interactive mode.

Chapter 4

> let a = 357;;

Quick-start guide

Programming is the art of solving problems by writing a program to be executed by a computer. For example, to solve the following problem,

What is the sum of 357 and 864?

we have written the following program in F#,

```
let a = 357
let b = 864
let c = a + b
printfn "%A" c
```

```
1221
```

Listing 4.1: quickStartSum.fsx - A script to add 2 numbers and print the result to the console.

In box the above, we see our program was saved as a script in a file called quickStartSum.fsx, and in the console we executed the program by typing the command fsharpi quickStartSum.fsx. The result is then printed in the console to be 1221.

To solve the program we made program consisting of several lines, where each line was a *statement*. The first statement let a = 357 used the let keyword to bind the value 357 to the name a. Likewise, we bound the value 864 to the name b, but to the name c we bound the result of evaluating the expression a + b. That is, first the value a + b was calculated by substituting the names of a and b with their values to give the expression, 357 + 864, then this expression was evaluated by adding the values to give, 1221, and this value was finally bound to the name c. The last line printed the value of c to the console followed by a newline (LF possibly preceded by CR, see Appendix B.1) with the printfn function. Here printfn is a function of 2 arguments: "%A" and c. Notice, that in contrast to many other languages, F# does not use parentheses to frame the list of arguments, nor does it use commas to separate them. In general, the printfn function always has 1 or more arguments, and the first is a format string. A string is a sequence of characters starting and ending with double quotation marks. E.g., let s = "this is a string of characters" binds the string "this is..." to the name s. For the printfn function, the format string may be any string, but if it contains format character sequences, such as %A, then the values following the format string are substituted. The format string must match the value type, that is, here c is of type integer, whereas the format string %A matches any type.

Types are a central concept in F#. In the script 4.1 we bound values of types int and string to names. The values were not declared to have these types, instead the types were inferred by F#. Had we typed these statements line by line in an interactive session, then we would have seen the inferred types:

```
\cdot statement
```

· format string

 \cdot string

·type

 \cdot type declaration

· type inference

[·]let

[·] keyword · binding

 $[\]cdot$ expression

```
val a : int = 357

> let b = 864;;

val b : int = 864

> let c = a + b;;

val c : int = 1221

> printfn "%A" c;;
1221
val it : unit = ()
```

Listing 4.2: fsharpi, Inferred types are given as part of the response from the interpreter.

The an interactive session displays the type using the *val* keyword. Since the value is also responded, then the last printfn statement is superfluous. However, it is ill advised to design programs to be run in an interactive session, since the scripts needs to be manually copied every time it is to be run, and since the starting state may be unclear.

· val Advice

Were we to solve a slightly different problem,

What is the sum of 357.6 and 863.4?

then we would have to use floating point arithmetic instead of integers, and the program would look like,

```
let a = 357.6
let b = 863.4
let c = a + b
printfn "%A" c
```

```
1221.0
```

Listing 4.3: quickStartSumFloat.fsx - Floating point types and arithmetic.

On the surface, this could appear as an almost negligible change, but the set of integers and the set of real numbers (floats) require quite different representations, in order to be effective on a computer, and as a consequence, the implementation of their operations such as addition are very different. Thus, although the response is an integer, it has type float, which is indicated by 1221.0 which is not the same as 1221. F# is very picky about types, and generally does not allow types to be mixed. E.g., in an interactive session,

Listing 4.4: fsharpi, Mixing types is often not allowed.

we see that binding a name to a number without a decimal point is inferred to be integer, while when binding to a number with a decimal point, then the type is inferred to be a float, and when trying to add values of integer and floating point, then we get an error.

F# is a functional first programming language, and one implication is that names have a *lexical scope*. A scope is an area in a program, where a binding is valid, and lexical scope means that when a binding is used, then its value is substituted at the place of binding regardless of whether its value is rebound later in the text. Further, at the outer most level, rebinding is not allowed. If attempted, then F# will return an error as, e.g., 1

· lexical scope

```
let a = 357
let a = 864
```

```
/Users/sporring/repositories/fsharpNotes/src/quickStartRebindError.fsx(2,5):
error FS0037: Duplicate definition of value 'a'
```

Listing 4.5: quickStartRebindError.fsx - A name cannot be rebound.

However, if the same was performed in an interactive session,

```
> let a = 357;;
val a : int = 357
> let a = 864;;
val a : int = 864
```

Listing 4.6: fsharpi, Names may be reused when separated by the token;;.

then apparently rebinding is valid. The difference is that the ;; token defines a new nested scope.² A token is a letter or a word, which the F# considers as an atomic unit. Scopes can be nested, and in F# a binding may reuse names in a nested scope, in which case the previous value is overshadowed. I.e., attempting the same without ;; between the two let statements results in an error, e.g.,

```
· token
· scope
· nested scope
· overshadow
```

·;;

```
> let a = 357
- let a = 864;;
let a = 864;;
----^
/Users/sporring/repositories/fsharpNotes/src/stdin(3,5): error FS0037:
    Duplicate definition of value 'a'
```

Listing 4.7: fsharpi, Inside a block, names may not be reused.

Scopes can be visualized as nested squares as shown in Figure 4.1.

In F# functions are also values, and defining a function sum as part of the solution to the above \cdot function program gives,

```
let sum x y = x + y
let c = sum 357 864
printfn "%A" c
```

1221

Listing 4.8: quickStartSumFct.fsx - A script to add 2 numbers using a user defined function.

¹When command is omitted, then error messages have unwanted blank lines.

²Language change: Spec 4.0 p. 15.1 talks about blocks instead of scopes.

```
let a = 357
let a = 864;;
(a) Invalid let a = 357;;
let a = 864;;
(b) Valid
```

Figure 4.1: Binding of the the same name in the same scope is invalid in F# 2, but valid in a different scopes. In (a) the two bindings are in the same scope, which is invalid, while in (b) the bindings are in separate scopes by the extra ;; token, which is valid.

Entering the function into an interactive session will illustrate the inferred type, the function sum has: val sum: x:int * y:int -> int, by which is meant that sum is a mapping from the set product of integers with integers into integers. Type inference in F# may cause problems, since the type of a function is inferred in the context, in which it is defined. E.g., in an interactive session, defining the sum in one scope on a single line will default the types to integers, F#'s favorite type, which will give an error, if it in a nested scope is to be used for floats,

```
> let sum x y = x + y
- let c = sum 357.6 863.4;;

val sum : x:float -> y:float -> float
val c : float = 1221.0
```

Listing 4.9: fsharpi, Types are inferred in blocks, and F# tends to prefer integers.

A remedy is to either define the function in the same scope as its use,

```
> let sum x y = x + y
- let c = sum 357.6 863.4;;

val sum : x:float -> y:float -> float
val c : float = 1221.0
```

Listing 4.10: fsharpi, Defining a function together with its use, makes F# infer the appropriate types.

In this chapter, we have scratched the surface of learning how to program by concentrating on a number of key programming concepts and how they are expressed in the F# language. In the following chapters, we will expand the description of F# with features used in all programming approaches.

Chapter 5

Using F# as a calculator

5.1 Literals and basic types

All programs rely on processing of data, and an essential property of data is its type. A literal is a fixed value such as "3", and if we type the number 3 in an interactive session at the input prompt, then F# responds as follows,

 \cdot type \cdot literal

```
> 3;;
val it : int = 3
```

Listing 5.1: fsharpi, Typing the number 3.

What this means is that F# has inferred the type to be *int* and bound it to the identifier *it*. Rumor has it, that the identifier *it* is an abbreviation for 'irrelevant'. For more on binding and identifiers see Chapter 6. Types matter, since the operations that can be performed on integers are quite different from those that can be performed on, e.g., strings. I.e.,

·int ·it

```
> 3;;
val it : int = 3
> 3.0;;
val it : float = 3.0
> '3';;
val it : char = '3'
> "3";;
val it : string = "3"
```

Listing 5.2: fsharpi, Many representations of the number 3 but using different types.

Each literal represent the number 3, but their types are different, and hence they are quite different values. The types int for integer numbers, float for floating point numbers, char for characters, and string for strings of characters are the most common types of literals. A table of all $basic\ types$ predefined in F# is given in Table 5.1. Besides these built-in types, F# is designed such that it is easy to define new types.

Humans like to use the decimal number system for representing numbers. Decimal numbers are base 10 means that for a number consisting of a sequence of digits separated by a decimal point, where each digit can have values $d \in \{0, 1, 2, ..., 9\}$, and the value, which each digit represents is proportional to its position. The part befor the decimal point is called the whole part and the part after is called the fractional part of the number. The whole part without a decimal point and a fractional part is called an integer number. As an example 35.7 is a decimal number, whose value is $3 \cdot 10^1 + 5 \cdot 10^0 + 7 \cdot 10^{-1}$. In F# a decimal number is called a floating point number and in this text we use Extended Backus-Naur Form (EBNF) to describe the grammar of F#, the decimal number just described is given as,

```
dDigit = "0" | "1" | "2" | "3" | "4" | "5" | "6" | "7" | "8" | "9" dInt = dDigit {dDigit}
```

- \cdot float
- \cdot char
- \cdot string
- · basic types
- \cdot decimal number
 - · base
- · decimal point
 - $\cdot \operatorname{digit}$
- · whole part
- · fractional part
- · integer number
- · floating point number
- · Extended Backus-Naur Form
- \cdot EBNF

Metatype	Type name	Description
Boolean	bool	Boolean values true or false
Integer	int	Integer values from -2,147,483,648 to 2,147,483,647
_	byte	Integer values from 0 to 255
	sbyte	Integer values from -128 to 127
	int8	Synonymous with byte
	uint8	Synonymous with sbyte
	int16	Integer values from -32768 to 32767
	uint16	Integer values from 0 to 65535
	int32	Synonymous with int
	uint32	Integer values from 0 to $4,294,967,295$
	int64	Integer values from $-9,223,372,036,854,775,808$ to
		9,223,372,036,854,775,807
	uint64	Integer values from 0 to 18,446,744,073,709,551,615
	nativeint	A native pointer as a signed integer
	unativeint	A native pointer as an unsigned integer
Real float		64-bit IEEE 754 floating point value from $-\infty$ to ∞
double		Synonymous with float
	single	A 32-bit floating point type
	float32	Synonymous with single
	decimal	A floating point data type that has at least 28 significant digits
Character	char	Unicode character
	\mathbf{string}	Unicode sequence of characters
None	None unit No value denoted	
Object	obj	An object
Exception	exn	An exception

Table 5.1: List of basic types. The most commonly used types are highlighted in bold. For at description of integer see Appendix A.1, for floating point numbers see Appendix A.2, for ASCII and Unicode characters see Appendix B, for objects see Chapter 18, and for exceptions see Chapter 9.

```
dFloat = dInt "." {dDigit}
```

meaning that a dDigit is either "0" or "1" or ... or "9", an dInt is 1 or more dDigit, and a dFloat is 1 or more digits, a dot and 0 or more digits. There is no space between the digits and between digits and the dot. So 3, 049 are examples of integers, 34.89 3. are examples of floats, while .5 is neither. Floating point numbers may alternatively be given using *scientific notation*, such as 3.5e-4 and 4e2, which means the number $3.5 \cdot 10^{-4} = 0.00035$ and $4 \cdot 10^2 = 400$. To describe this in EBNF we write

 \cdot scientific notation

· bit

· binary number

· octal number

 \cdot hexadecimal

number

```
sFloat = (dInt | dFloat) ("e" | "E" ) ["+" | "-"] dInt float = dFloat | sFloat
```

Note that the number before the token e may be an dInt or a dFloat, but the exponent value must be an dInt.

The basic unit of information in almost all computers is the binary digit or bit for short. A binary number consists of a sequence of binary digits separated by a decimal point, where each digit can have values $b \in \{0,1\}$, and the base is 2. E.g., the binary number $101.01_2 = 1 \cdot 2^2 + 0 \cdot 2^1 + 1 \cdot 2^0 + 0 \cdot 2^{-1} + 1 \cdot 2^1 = 5.25$. Binary numbers are closely related to octal and hexadecimal numbers, where octals uses 8 as basis and can be written in binary using 3 bits, while hexadecimal numbers uses 16 as basis and can be written in binary using 4 bits. Octals and hexadecimals thus conveniently serve as shorthand for the much longer binary representation. F# has a syntax for writing integers on binary, octal, decimal, and hexadecimal numbers as,

```
cimal,
```

For example 367 is an dInt, Ob101101111, Oo557, and Ox16f is a bitInt, octInt, and hexInt, i.e., a binary, an octal, and a hexadecimal number, they are examples of an xInt and representations of the same number 367. In contrast, Ob12 and ff are neither an dInt nor an xInt.

A character is a Unicode code point, and character literals are enclosed in single quotation marks, see Appendix B.3 for a description of code points.¹ The EBNF for characters is,

```
escapeCodePoint =
   "\u" xDigit xDig
```

where codePoint is a UTF8 encoding of a char. The escape characters escapeChar are special sequences that are interpreted as a single code point shown in Table 5.2. The trigraph \DDD uses decimal specification for the first 256 code points, and the hexadecimal escape codes \uXXXX, \UXXXXXXXX allow for the full specification of any code point. Examples of a char are 'a', '_-', '\n', and '\065'. A string is a sequence of characters enclosed in double quotation marks,²

· string

·character

· Unicode · code point

¹Spec-4.0 p.28: char-char is missing option unicodegraph-long

²Spec-4.0 p. 28-29: simple-string-char is undefined, string-elem is unused.

Character	Escape sequence	Description
BS	\b	Backspace
LF	\n	Line feed
CR	\r	Carriage return
HT	\t	Horizontal tabulation
\	\\	Backslash
"	\"	Quotation mark
,	\'	Apostrophe
BEL	\a	Bell
FF	\f	Form feed
VT	\v	Vertical tabulation
	\uXXXX,\UXXXXXXX,\DDD	Unicode character

Table 5.2: Escape characters. For the unicode characters 'X' are hexadecimal digits, while for tricode characters 'D' is a decimal character.

```
stringChar = char - '"'
simpleString = '"' { stringChar } '"'
```

Examples are "a", "this is a string", and "-&#\@". Newlines and following whitespaces,

```
newline = [CR] LF (* carriage return and line feed *)
whitespace = {SP} (* space *)
```

· newline

are taken literally, but may be ignored by a preceding \character. Further examples of strings are,

```
> "abcde";;
val it : string = "abcde"
> "abc
- de";;
val it : string = "abc
    de"
> "abc\
- de";;
val it : string = "abcde"
> "abc\nde";;
val it : string = "abc
de"
```

Listing 5.3: fsharpi, Examples of string literals.

The response is shown in double quotation marks, which are not part of the string.

F# supports literal types, where the type of a literal is indicated as a prefix og suffix as shown in the - literal type Table 5.3. Examples are,

```
> 3;;
val it : int = 3
> 4u;;
val it : uint32 = 4u
> 5.6;;
val it : float = 5.6
> 7.9f;;
val it : float32 = 7.9000001f
> 'A';;
val it : char = 'A'
> 'B'B;;
val it : byte = 66uy
> "ABC";;
```

type	EBNF	Examples
int, int32	(dInt xInt)["l"]	3
uint32	(dInt xInt)("u" "ul")	3u
byte, uint8	((dInt xInt)"uy") (char "B")	3uy
byte[]	["@"] string "B"	"abc"B and "@http:\\"B
sbyte, int8	(dInt xInt)"y"	3у
int16	(dInt xInt)"s"	3s
uint16	(dInt xInt)"us"	3us
int64	(dInt xInt)"L"	3L
uint64	(dInt xInt)("UL" "uL")	3UL and 3uL
bignum*	dInt "I"	3I
nativeint	(dInt xInt)"n"	3n
unativeint	(dInt xInt)"un"	3un
float, double	float (xInt "LF")	3.0
single, float32	(float ("F" "f")) (xInt "lf")	3.0f
decimal	(float dInt)("M" "m")	3.0m and 3m
string	simpleString	"a \"quote\".\n"
	'@"'{(char - ('"' '\"')) '""'} '"'	@"a ""quote"".\n"
	'""'{char} '""'(*no '"""' substring*)	"""a "quote".\n"""

Table 5.3: List of literal type. No spacing is allowed between the literal and the prefix or suffix. [] notation is for lists, see Chapter 8. *bignum is not a basic type and does not yet have an implementation for dInt ("Q" | "R" | "Z" | "N" | "G") in Mono.

```
val it : string = "ABC"
```

Listing 5.4: fsharpi, Named and implied literals.

Strings literals may be *verbatim* by the @-notation or triple double quotation marks, meaning that the escape sequences are not converted to their code point., e.g.,

 \cdot verbatim

```
> @"abc\nde";;
val it : string = "abc\nde"
```

Listing 5.5: fsharpi, Examples of a string literal.

For strings containing double quotation marks, verbatim literals has 2 possible notations, either use the @-notation and escaping double quotation marks with an extra double quotation mark, or use triple double quotation marks. The triple double quotation marks notation may not contain substrings that are triple double quotation marks, and thus @-notation is preferred.

Advice

Many basic types are compatible and the type of a literal may be changed by type casting. E.g.,

· type casting

```
> float 3;;
val it : float = 3.0
```

Listing 5.6: fsharpi, Casting an integer to a floating point number.

which is a float, since when float is given an argument, then it acts as a function rather than a type, and for the integer 3 it returns the floating point number 3.0. For more on functions see Chapter ??. Boolean values are often treated as the integer values 0 and 1, but no short-hand function names exists for their conversions. Instead use,

```
> System.Convert.ToBoolean 1;;
val it : bool = true
> System.Convert.ToBoolean 0;;
val it : bool = false
> System.Convert.ToInt32 true;;
val it : int = 1
```

```
> System.Convert.ToInt32 false;;
val it : int = 0
```

Listing 5.7: fsharpi, Casting booleans.

Here System.Convert.ToBoolean is the identifier of a function ToBoolean, which is a *member* of the *class* Convert that is included in the *namespace* System. Namespaces, classes, and members are all part of Structured programming to be discussed in Part IV.

 \cdot member

 \cdot class

 \cdot namespace

Type casting is often a destructive operation, e.g., type casting a float to int removes the fractional part without rounding,

```
> int 357.6;;
val it : int = 357
```

Listing 5.8: fsharpi, Fractional part is removed by downcasting.

Here we type casted to a lesser type, in the sense that integers is a subset of floating point numbers, and this is called *downcasting*. The opposite is called *upcasting* and is often non-destructive, as Listing 5.6 showed, where an integer was casted to a float while retaining its value. As a side note, *rounding* a number y.x, where y is the *whole part* and x is the *fractional part*, is the operation of mapping numbers in the interval $y.x \in [y.0, y.5)$ to y and $y.x \in [y.5, y+1)$ to y+1. This can be performed by downcasting as follows,

```
· downcasting
```

- \cdot upcasting
- \cdot rounding
- · whole part
- \cdot fractional part

```
> int (357.6 + 0.5);;
val it : int = 358
```

Listing 5.9: fsharpi, Fractional part is removed by downcasting.

since if $y.x \in [y.0, y.5)$, then $y.x + 0.5 \in [y.5, y + 1)$, from which downcasting removes the fractional part resulting in y. And if $y.x \in [y.5, y + 1)$, then $y.x + 0.5 \in [y + 1, y + 1.5)$, from which downcasting removes the fractional part resulting in y + 1. Hence, the result is rounding.

5.2 Operators on basic types

Listing 5.9 is an example of an arithmetic *expression* using an *infix operator*. Expressions is the basic building block of all F# programs, and its grammar has many possible options. The grammar for expressions are defined recursively, and some of it is given by, ³

- \cdot expression
- · infix operator

```
bool = "true" | "false"
const = byte | sbyte | uint8 | int8 | int16 | uint16 | int | int32 | uint32 |
   int64 | uint64 | bignum | naviteint | unativeint | float | double | single |
   float32 | decimal | char | string | byte [] | bool | "()"
slice-range =
 expr (* single index *)
    expr ".." (* from index to end *)
   ".." expr (* from start to index *)
  | expr ".." expr (* from one index to another *)
   "*" (* from start to end *)
expr =
 const (* constant value *)
  | "(" expr ")" (* block expression *)
  | expr operator expr (* infix operation *)
  | operator expr (* prefix operation *)
  | expr expr (* function application *)
  | expr ".[" slice-range "]" (* slice lookup *)
```

Listing 5.10: expressionArithmetic

³Spec-4.0 Section 4.3: const is missing uint8, int8 nativeint, unativeint.

Operator	op1	op2	Expression	Result	Description
op1 + op2	ints	ints	5 + 2	7	Addition
	floats	floats	5.0 + 2.0	7.0	
	chars	chars	'a' + 'b'	'\195'	Addition of codes
	strings	strings	"ab" + "cd"	"abcd"	Concatenation
op1 - op2	ints	ints	5 - 2	3	Subtraction
	floats	floats	5.0 - 2.0	3.0	
op1 * op2	ints	ints	5 * 2	10	Multiplication
	floats	floats	5.0 * 2.0	10.0	
op1 / op2	ints	ints	5 / 2	2	Integer division
	floats	floats	5.0 / 2.0	2.5	Division
op1 % op2	ints	ints	5 % 2	1	Remainder
	floats	floats	5.0 % 2.0	1.0	
op1 ** op2	floats	floats	5.0 ** 2.0	25.0	Exponentiation
op1 && op2	bool	bool	true && false	false	boolean and
op1 op2	bool	bool	true false	false	boolean or
op1 &&& op2	ints	ints	0b1010 &&& 0b1100	0b1000	bitwise bool and
op1 op2	ints	ints	0b1010 0b1100	0b1110	bitwise boolean or
op1 ^^^ op2	ints	ints	0b1010 ^^^ 0b1101	0b0111	bitwise boolean exclu-
					sive or
op1 <<< op2	ints	ints	0b00001100uy <<< 2	0b00110000uy	bitwise shift left
op1 >>> op2	ints	ints	0b00001100uy >>> 2	0b00000011uy	bitwise and
+op1	ints		+3	3	identity
	floats		+3.0	3.0	
-op1	ints		-3	-3	negation
	floats		-3.0	-3.0	
not op1	bool		not true	false	boolean negation
~~~op1	ints		~~~0b00001100uy	0b11110011uy	bitwise boolean nega-
					tion

Table 5.4: Arithmetic operators on basic types. Ints, floats, chars, and strings means all built-in integer types etc.. Note that for the bitwise operations, digits 0 and 1 are taken to be true and false.

Recursion means that a rule or a function is used by the rule or function itself in its definition. See Part III for more on recursion. Infix notation means that the *operator* op appears between the two *operands*, and since there are 2 operands, it is a *binary operator*. As the grammar shows, the operands themselves can be expressions. Examples are 3+4 and 4+5+6. Some operators only takes one operand, e.g., -3, where - here is used to negate a postive integer. Since the operator appears before the operand it is a *prefix operator*, and since it only takes one argument it is also a *unary operator*. Finally, some expressions are function names, which can be applied to expressions. F# supports a range of arithmetic infix and prefix operators on its built-in types shown in Table 5.4 and 5.5 and a range of mathematical functions shown in Table 5.6. Arithmetic on various types will be discussed in detail in the following sections.  4 

If parentheses are omitted in Listing 5.9, then F# will interpret the expression as (int 357.6)+0.5, which is erroneous, since addition of an integer with a float is undefined. This is an example of precedence, i.e., function evaluation takes precedence over addition meaning that it is performed before addition. Consider the arithmetic expression, whose result is bound to a by

```
> 3 + 4 * 5;;
val it : int = 23
```

Listing 5.11: fsharpi, A simple arithmetic expression.

 $\cdot$  operator

⁴minor comment on indexing and slice-ranges.

 $[\]cdot$  operands

[·] binary operator

[·] prefix operator

[·] unary operator

Operator	op1	op2	Expression	Result	Description
op1 < op2	bool	bool	true < false	false	Less than
	ints	ints	5 < 2	false	
	floats	floats	5.0 < 2.0	false	
	chars	chars	'a' < 'b'	true	
	strings	strings	"ab" < "cd"	true	
op1 > op2	bool	bool	true > false	true	Greater than
	ints	ints	5 > 2	true	
	floats	floats	5.0 > 2.0	true	
	chars	chars	'a' > 'b'	false	
	strings	strings	"ab" > "cd"	false	
op1 = op2	bool	bool	true = false	false	Equal
	ints	ints	5 = 2	false	
	floats	floats	5.0 = 2.0	false	
	chars	chars	'a' = 'b'	false	
	strings	strings	"ab" = "cd"	false	
op1 <= op2	bool	bool	true <= false	false	Less than or equal
	ints	ints	5 <= 2	false	
	floats	floats	5.0 <= 2.0	false	
	chars	chars	'a' <= 'b'	true	
	strings	strings	"ab" <= "cd"	true	
op1 >= op2	bool	bool	true >= false	true	Greater than or equal
	ints	ints	5 >= 2	true	
	floats	floats	5.0 >= 2.0	true	
	chars	chars	'a' >= 'b'	false	
	strings	strings	"ab" >= "cd"	false	
op1 <> op2	bool	bool	true <> false	true	Not Equal
	ints	ints	5 <> 2	true	
	floats	floats	5.0 <> 2.0	true	
	chars	chars	'a' <> 'b'	true	
	strings	strings	"ab" <> "cd"	true	

Table 5.5: Comparison operators on basic types. Ints, floats, chars, and strings means all built-in integer types etc..

Type	Function name	Example	Result	Description
Ints and floats	abs	abs -3	3	Absolute value
Floats	acos	acos 0.8	0.6435011088	Inverse cosine
Floats	asin	asin 0.8	0.927295218	Inverse sinus
Floats	atan	atan 0.8	0.6747409422	Inverse tangent
Floats	atan2	atan2 0.8 2.3	0.3347368373	Inverse tangentvariant
Floats	ceil	ceil 0.8	1.0	Ceiling
Floats	cos	cos 0.8	0.6967067093	Cosine
Floats	cosh	cosh 0.8	1.337434946	Hyperbolic cosine
Floats	exp	exp 0.8	2.225540928	Natural exponent
Floats	floor	floor 0.8	0.0	Floor
Floats	log	log 0.8	-0.2231435513	Natural logarithm
Floats	log10	log10 0.8	-0.09691001301	Base-10 logarithm
Ints, floats,	max	max 3.0 4.0	4.0	Maximum
chars, and strings				
Ints, floats,	min	min 3.0 4.0	3.0	Minimum
chars, and strings				_
Ints	pown	pown 3 2	9	Integer exponent
Floats	round	round 0.8	1.0	Rounding
Ints and floats	sign	sign -3	-1	Sign
Floats	sin	sin 0.8	0.7173560909	Sinus
Floats	sinh	sinh 0.8	0.8881059822	Hyperbolic sinus
Floats	sqrt	sqrt 0.8	0.894427191	Square root
Floats	tan	tan 0.8	1.029638557	Tangent
Floats	tanh	tanh 0.8	0.6640367703	Hyperbolic tangent

Table 5.6: Predefined functions for arithmetic operations

Operator	Associativity	Description
+op, -op,	Left	Unary identity, negation, and bitwise negation operator
~~~op		
f x	Left	Function application
op ** op	Right	Exponent
op * op,	Left	Multiplication, division and remainder
op / op,		
ор % ор		
op + op,	Left	Addition and subtraction binary operators
op - op		
op ^^^ op	Right	bitwise exclusive or
op < op,	Left	Comparison operators, bitwise shift, and bitwise 'and' and 'or'.
op <= op,		
op > op,		
op >= op,		
op = op,		
op <> op,		
op <<< op,		
op >>> op,		
op &&& op,		
op III op,		
&&	Left	Boolean and
11	Left	Boolean or

Table 5.7: Some common operators, their precedence, and their associativity. Rows are ordered from highest to lowest precedences, such that op * op has higher precedence than op + op. Operators in the same row has same precedence. Full table is given in Table D.1.

Here, the addition and multiplication functions are shown in *infix notation* with the *operator* tokens + and *. To arrive at the resulting value 23, F# has to decide in which order to perform the calculation. There are 2 possible orders, 3 + (4 * 5) or (3 + 4) * 5, which gives different results. For integer arithmetic, the correct order is of course to multiply before addition, and we say that multiplication takes *precedence* over addition. Every atomic operation that F# can perform is ordered in terms of its precedences, and for some common built-in operators shown in Table 5.7, the precedence is shown by the order they are given in the table. Associativity implies the order in which calculations are performed for operators of same precedence. For some operators and type combinations association matters little, e.g., multiplication associates to the left and exponentiation associates to the right, e.g., in⁵

```
\begin{array}{l} \cdot \text{ infix notation} \\ \cdot \text{ operator} \end{array}
```

· precedence

 \cdot boolean or

```
· boolean and
```

```
> 3.0*4.0*5.0;;
val it : float = 60.0
> (3.0*4.0)*5.0;;
val it : float = 60.0
> 3.0*(4.0*5.0);;
val it : float = 60.0
> 4.0 ** 3.0 ** 2.0;;
val it : float = 262144.0
> (4.0 ** 3.0) ** 2.0;;
val it : float = 4096.0
> 4.0 ** (3.0 ** 2.0);;
val it : float = 262144.0
```

Listing 5.12: fsharpi, Precedences rules define implicite parentheses.

 $^{^5}$ Spec-4.0, Table 18.2.1 appears to be missing boolean 'and' and 'or' operations. Section 4.4 seems to be missing &&& and ||| bitwise operators.

a	b	$a \cdot b$	a+b	\bar{a}
0	0	0	0	1
0	1	0	1	1
1	0	0	1	0
1	1	1	1	0

Table 5.8: Truth table for boolean 'and', 'or', and 'not' operators. Value 0 is false and 1 is true.

the expression for 3.0 * 4.0 * 5.0 associates to the left, and thus is interpreted as (3.0 * 4.0)* 5.0, but gives the same results as 3.0 * (4.0 * 5.0), since association does not matter for multiplication of numbers. However, the expression for 4.0 ** 3.0 ** 2.0 associates to the right, and thus is interpreted as 4.0 ** (3.0 ** 2.0), which is quite different from (4.0 ** 3.0)** 2.0. Whenever in doubt of association or any other basic semantic rules, it is a good idea to use parentheses as here. It is also a good idea to test your understanding of the syntax and semantic rules by simplest possible scripts, as shown here as well.

Advice

5.3 Boolean arithmetic

Boolean arithmetic is the basis of almost all computers and particularly important for controlling program flow, which will be discussed in Chapter 7. Boolean values are one of 2 possible values, true or false, which is also sometimes written as 1 and 0. Two basic operations on boolean values are 'and' often also written as multiplication, and 'or' often written as addition, and 'not' often written as a bar above the value. All possible combination of input on these values can be written on tabular form, known as a truth table, shown in Table 5.8. That is, the multiplication and addition are good mnemonics for remembering the result of the 'and' and 'or' operators. In F# the values true and false are used, and the operators && for 'and', || for 'or', and the function not for 'not', such that the above table is reproduced by,

 \cdot and \cdot or

 \cdot not

· truth table

```
> printfn "a b a*b a+b not a"
- printfn "%A %A %A %A %A %A"
- false false (false && false) (false || false) (not false)
- printfn "%A %A %A %A %A"
- false true (false && true) (false || true) (not false)
- printfn "%A %A %A %A %A"
- true false (true && false) (true || false) (not true)
- printfn "%A %A %A %A %A"
- true true (true && true) (true || true) (not true);;
a b a*b a+b not a
false false false false true
false true false true true
true false false true false
true true true true false
```

Listing 5.13: fsharpi, Boolean operators and truth tables.

Spacing produced using the **printfn** function is not elegant. In Section 6.4 we will discuss better options for producing more beautiful output. Notice, that the arguments for **printfn** was given on the next line. Here it is important to use *indentation* to indicate continuation of the line. See Section ?? for more.

 \cdot indentation

5.4 Integer arithmetic

The set of integers is infinitely large, but since all computers have limited resources, it is not possible to represent it in their entirety. The various integer types listed in Table 5.1 are finite subset reduced by limiting their ranges. Although bignum is theoretically unlimited, the biggest number representable is still limited by computer memory. An in-depth description of integer implementation can be found in Appendix A. The type int is the most common type.

Table 5.4, 5.5, and 5.6 gives examples operators and functions pre-defined for integer types. Notice that fewer functions are available for integers than for floating point numbers. For most addition, subtraction, multiplication, and negation the result straight forward. However, performing arithmetic operations on integers requires extra care, since the result since they may cause overflow, underflow, e.g., the range of the integer type sbyte is [-128...127], which causes problems in the following example,

 \cdot overflow \cdot underflow

```
> 100y;;
val it : sbyte = 100y
> 30y;;
val it : sbyte = 30y
> 100y + 30y;;
val it : sbyte = -126y
```

Listing 5.14: fsharpi, Adding integers may cause overflow.

Here 100 + 30 = 130, which is larger than the biggest sbyte, and the result is an overflow. Similarly, we get an underflow, when the arithmetic result falls below the smallest value storable in an sbyte,

```
> -100y - 30y;;
val it : sbyte = 126y
```

Listing 5.15: fsharpi, Subtracting integers may cause underflow.

I.e., we were expecting a negative number, but got a postive number instead.

The overflow error in Listing 5.14 can be understood in terms of the binary representation of integers: In binary, $130 = 10000010_2$, and this binary pattern is interpreted differently as byte and sbyte,

```
> 0b10000010uy;;
val it : byte = 130uy
> 0b10000010y;;
val it : sbyte = -126y
```

Listing 5.16: fsharpi, The left most bit is interpreted differently for signed and unsigned integers, which gives rise to potential overflow errors.

That is, for signed bytes, the left-most bit is used to represent the sign, and since the addition of $100 = 01100100_2$ and $30 = 00011110_b$ is $130 = 10000010_2$ causes the left-most bit to be used, then this is wrongly interpreted as a negative number, when stored in an sbyte. Similar arguments can be made explaining underflows.

The division and remainder operators *integer division*, which discards the fractional part after division, and the *remainder* operator calculates the remainder after integer division, e.g.,

 \cdot integer division

· remainder

```
> 7 / 3;;
val it : int = 2
> 7 % 3;;
val it : int = 1
```

Listing 5.17: fsharpi, Integer division and remainder operators.

Together integer division and remainder is a lossless representation of the original number as,

```
> (7 / 3) * 3;;
val it : int = 6
```

a	b	a xor b
0	0	0
0	1	1
1	0	1
0	1	0

Table 5.9: Boolean exclusive or truth table.

```
> (7 / 3) * 3 + (7 % 3);;
val it : int = 7
```

Listing 5.18: fsharpi, Integer division and remainder is a lossless representation of an integer, compare with Listing 5.17.

And we see that integer division of 7 by 3 followed by multiplication by 3 is less that 7, and the difference is 7 % 3.

Notice that neither overflow nor underflow error gave rise to an error message, which is why such bugs are difficult to find. Dividing any non-zero number with 0 is infinite, which is also outside the domain of any of the integer types, but in this case, F# casts an *exception*,

 \cdot exception

Listing 5.19: fsharpi, Integer division by zero causes an exception run-time error.

The output looks daunting at first sight, but the first and last line of the error message are the most important parts, which tells us what exception was cast and why the program stopped. The middle are technical details concerning which part of the program caused this, and can be ignored for the time being. Exceptions are a type of *run-time error*, and are treated in Chapter 9

Integer exponentiation is not defined as an operator, but this is available the built-in function pown, e.g.,

```
\cdot run-time error
```

```
> pown 2 5;;
val it : int = 32
```

Listing 5.20: fsharpi, Integer exponent function.

which is equal to 2^5 .

For binary arithmetic on integers, the following operators are available: op1 <<< op2, which shifts the bit pattern of op1 op2 positions to the left insert 0's to right; op1 >>> op2, which shifts the bit pattern of op1 op2 positions to the right insert 0's to left; op1 &&& op2, Bitwise 'and', returns the result of taking the boolean 'and' operator position-wise; op | | | op, Bitwise 'or', as 'and' but using the boolean 'or' operator; and op1 ~~~ op1, Bitwise xor, which is returns the result of the boolean 'xor' operator defined by the truth table in Table 5.9.

 $\cdot xor$

· exclusive or

5.5 Floating point arithmetic

The set of reals is infinitely large, and since all computers have limited resources, it is not possible to represent it in their entirety. The various floating point types listed in Table 5.1 are finite subset

reduced by sampling the space of reals. An in-depth description of floating point implementations can be found in Appendix A. The type float is the most common type.

Table 5.4, 5.5, and 5.6 gives examples operators and functions pre-defined for floating point types. For most addition, subtraction, multiplication, divisions, and negation the result straight forward.

The remainder operator for floats calculates the remainder after division and discarding the fractional part,

```
> 7.0 / 2.5;;

val it : float = 2.8

> 7.0 % 2.5;;

val it : float = 2.0
```

Listing 5.21: fsharpi, Floating point division and remainder operators.

The remainder for floating point numbers can be fractional, but division, discarding fractional part, and remainder is still a lossless representation of the original number as,

```
> float (int (7.0 / 2.5));;
val it : float = 2.0
> (float (int (7.0 / 2.5))) * 2.5;;
val it : float = 5.0
> (float (int (7.0 / 2.5))) * 2.5 + 7.0 % 2.5;;
val it : float = 7.0
```

Listing 5.22: fsharpi, Floating point division, truncation, and remainder is a lossless representation of a number.

Arithmetic using float will not cause over- and underflow problems, since the IEEE 754 standard includes the special numbers $\pm \infty$ and NaN. E.g.,

```
> 1.0/0.0;;
val it : float = infinity
> 0.0/0.0;;
val it : float = nan
```

Listing 5.23: fsharpi, Floating point numbers include infinity and Not-a-Number.

However, the float type has limite precision, since there is only a finite number of numbers that can be stored in a float. E.g.,

```
> 357.8 + 0.1 - 357.9;;
val it : float = 5.684341886e-14
```

Listing 5.24: fsharpi, Floating point arithmetic has finite precision.

That is, addition and subtraction associates to the left, hence the expression is interpreted as (357.8 + 0.1) – 357.9, and we see that we do not get the expected 0, since only a limited number of floating point values are available, and the numbers 357.8 + 0.1 and 357.9 do not result in the same floating point representation. Such errors tend to accumulate and comparing the result of expressions of floating point values should therefore be treated with care. Thus, equivalence of two floating point expressions should only be considered up to sufficient precision, e.g., comparing 357.8 + 0.1 and 357.9 up to 1e-10 precision should be tested as, abs ((357.8 + 0.1) - 357.9) < 1e-10.

Advice

5.6 Char and string arithmetic

Addition is the only operator defined for characters, nevertheless, character arithmetic is often done by casting to integer. A typical example is conversion of case, e.g., to convert the lowercase character 'z' to uppercase, we use the *ASCIIbetical order* and add the difference between any Basic Latin Block letters in upper- and lowercase as integers and cast back to char, e.g.,

 \cdot ASCIIbetical order

```
> char (int 'z' - int 'a' + int 'A');;
val it : char = 'Z'
```

Listing 5.25: fsharpi, Converting case by casting and integer arithmetic.

I.e., the code point difference between upper and lower case for any alphabetical character 'a' to 'z' is constant, hence we can change case by adding or subtracting the difference between any corresponding character. Unfortunately, this does not generalize to characters from other languages.

A large collection of operators and functions exist for string. The most simple is concatenation using, e.g.,

```
> "hello" + " " + "world";;
val it : string = "hello world"
```

Listing 5.26: fsharpi, Example of string concatenation.

Characters and strings cannot be concatenated, which is why the above example used the string of a space " " instead of the space character ' '. The characters of a string may be indexed as using the . [] notation,

```
> "abcdefg".[0];;
val it : char = 'a'
> "abcdefg".[3];;
val it : char = 'd'
> "abcdefg".[3..];;
val it : string = "defg"
> "abcdefg".[..3];;
val it : string = "abcd"
> "abcdefg".[1..3];;
val it : string = "bcd"
> "abcdefg".[*];;
val it : string = "abcdefg"
```

Listing 5.27: fsharpi, String indexing using square brackets.

Notice, that the first character has index 0, and to get the last character in a string, we use the string's length property as,

```
> "abcdefg".Length;;
val it : int = 7
> "abcdefg".[7-1];;
val it : char = 'g'
```

Listing 5.28: fsharpi, String length attribute and string indexing.

Notice, since index counting starts at 0, and the string length is 7, then the index of the last character is 6. An alternative notation for indexing is to use the property Char, and in the example ''abcdefg''. [3] is the same as a.Char 3. The is a long list of built-in functions in System.String for working with strings, some of which will be discussed in Chapter 13.1.

The dot notation is an example of Structured programming, where technically speaking, the string "abcdefg" is an immutable object of class string, and [] is an object method and Length is a property. For more on object, classes, and methods see Chapter 18.

 \cdot dot notation

- \cdot object
- \cdot class

· . []

 \cdot method

Chapter 6

Constants, functions, and variables

In the previous chapter, we saw how to use F# as a calculator working with literals, operators and built-in functions. To save time and make programs easier to read and debug, it is useful to bind expressions to identifiers either as new constants, functions or operators. For example, to solve for x, when

$$ax^2 + bx + c = 0 (6.1)$$

we use the quadratic formula from elementary algebra,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a},\tag{6.2}$$

and write a small program that defines functions calculating relevant values for any set of coefficients,

```
let determinant a b c = b ** 2.0 - 2.0 * a * c
let positiveSolution a b c = (-b + sqrt (determinant a b c)) / (2.0 * a)
let negativeSolution a b c = (-b - sqrt (determinant a b c)) / (2.0 * a)

let a = 1.0
let b = 0.0
let c = -1.0
let d = determinant a b c
let xp = positiveSolution a b c
let xn = negativeSolution a b c
printfn "%A * x ** 2.0 + %A * x + %A" a b c
printfn " has determinant %A and solutions %A and %A" d xn xp
```

```
1.0 * x ** 2.0 + 0.0 * x + -1.0
has determinant 2.0 and solutions -0.7071067812 and 0.7071067812
```

Listing 6.1: identifiers Example. fsx - Finding roots for quadratic equations using function name binding.

Here 3 functions are defined as determinant, postiveSolution, and negativeSolution are defined, and applied to 3 values named a, b, and c, and the results are named d, xn, and xp. These names are examples of identifiers, and with these, we may reuse the quadratic formulas and calculated values later, while avoiding possible typing mistakes and reducing amount of code, which needs to be debugged. Before we begin a deeper discussion note that F# has adheres to two different syntax, regular and lightweight. In the regular syntax, newlines and whitespaces are generally ignored, while in lightweight syntax, certain keywords and tokens may be replaced by specific use of newlines and whitespaces. Lightweight syntax is the most common, but the syntaxes may be mixed, and we will highlight the options, when relevant.

· lightweight syntax

The use of identifiers is central in programming. For F# not to be confused by built-in functionality, identifiers must follow a specific grammar: An identifier must start with a letter, but can be followed by zero or more of letters, digits, and a range of special characters. An identifier must not be a keyword

abstract, and, as, assert, base, begin, class, default, delegate, do, done, downcast, downto, elif, else, end, exception, extern, false, finally, for, fun, function, global, if, in, inherit, inline, interface, internal, lazy, let, match, member, module, mutable, namespace, new, null, of, open, or, override, private, public, rec, return, sig, static, struct, then, to, true, try, type, upcast, use, val, void, when, while, with, and yield.

Figure 6.1: List of keywords in F#.

atomic, break, checked, component, const, constraint, constructor, continue, eager, fixed, fori, functor, include, measure, method, mixin, object, parallel, params, process, protected, pure, recursive, sealed, tailcall, trait, virtual, and volatile.

Figure 6.2: List of reserved keywords for possible future use in F#.

or a reserved-keyword listed in Figure 6.1 and 6.2. For characters in the Basic Latin Block, i.e., the first 128 code points alias ASCII characters, an ident is,

```
dDigit = "0" | "1" | "2" | "3" | "4" | "5" | "6" | "7" | "8" | "9"
letter = "A" | "B" | ... | "Z" | "a" | "b" | ... | "z"
specialChar = "_"
ident = (letter | "_") {letter | dDigit | specialChar}
```

Thus, examples of identifiers are a, the Character 9, Next_Word, _tok. The for the full definition, letter = Lu | Ll | Lt | Lm | Lo | Nl and special Char = Pc | Mn | Mc | Cf, which referes to the Unicode general categories described in Appendix B.3, and there are currently 19.345 possible Unicode code points in the letter category and 2.245 possible Unicode code points in the special Char category. Binding expressions to identifiers is done with the keyword let, using the following simplified syntax:

```
arg = ident | "(" ident ":" type ")"
argList = arg | arg argList
identOrOp = ident | ( operatorName )
valueDefn = ["mutable "] ident [":" type] "=" expr
functionDefn = ident—or—op argList [":" type] "=" expr "
expr = ...
    | "let " valueDefn " in " expr (* binding a value or variable *)
    | "let " functionDefn " in " expr (* binding a function or operator *)
    | "fun " argList "—>" expr (* a function as value *)
    | expr ":" type (* type annotation *)
    | "begin " expr " end" (* alternative block expression *)
    | expr; expr (* sequence of expression *)
    | ...
```

which will be discussed in the following.¹

6.1 Values

Binding identifiers to literals or expressions that are evaluated to be values is called value binding, and examples are let a = 3.0 and let b = cos 0.9. On EBNF the simplified syntax,

```
valueDefn = ["mutable "] ident [":" type] "=" expr
expr = ...
| "let " valueDefn " in " expr
| ...
```

I.e., the *let* keyword dictates that the identifier ident is an alias of the expression expr. The type may be specified with the : token to type type. The binding may be mutable as indicated by the

let

· :

¹Spec-4.0 Section 6.6, function-or-value-defns, 1. makes little sense to have values definitions recursive,

keyword mutable, which will be discussed in Section 6.5, and the binding holds lexically for the last expression as indicated by the in keyword.² For example, letting the identifier p be bound to the value 2.0 and using it in an expression is done as follows,

mutablelexicallyin

```
let p = 2.0 in printfn "%A" (p ** 3.0)
```

```
8.0
```

Listing 6.2: letValue.fsx - The identifier p is used in the expression following the in keyword.

In the interactive mode used in the example above, we see that F# infers the type... F# will ignore most newlines between tokens, i.e., the above is equivalent to writing,

```
let p = 2.0 in
printfn "%A" (3.0 ** p)
```

```
9.0
```

Listing 6.3: letValueLF.fsx - Newlines after in make the program easier to read.

F# also allows for an alternative notation called *lightweight syntax*, where e.g., the in keyword is replaced with a newline, and the expression starts on the next line at the same column as let starts in, i.e., the above is equivalent to

 \cdot lightweight syntax

```
let p = 2.0
printfn "%A" (3.0 ** p)
```

```
9.0
```

Listing 6.4: letValueLightWeight.fsx - Lightweight syntax does not require the in keyword, but expression must be aligned with the let keyword.

The same expression in interactive mode will also respond the inferred types, e.g.,

```
> let p = 2.0
- printfn "%A" (3.0 ** p);;
9.0

val p : float = 2.0
val it : unit = ()
```

Listing 6.5: fsharpi, Interactive mode also responds inferred types.

By the val keyword in the line val p: float = 2.0 we see that p is inferred to be of type float and bound to the value 2.0. The inference is based on the type of the right-hand-side, which is of type float. Identifiers may be defined to have a type using the: token, but the types on the left-hand-side and right-hand-side of the = token must be identical. I.e., mixing types gives an error,

```
let p : float = 3
printfn "%A" (3.0 ** p)
```

```
/Users/sporring/repositories/fsharpNotes/src/letValueTypeError.fsx(1,17):
error FS0001: This expression was expected to have type
float
but here has type
```

and 2. possible Mono deviation from specification: let rec functionDefn and functionDefn requires newline before and.

²https://coders-corner.net/2013/11/12/lexical-scope-vs-dynamic-scope/

```
int
```

Listing 6.6: letValueTypeError.fsx - Binding error due to type mismatch.

Here, the left-hand-side is defined to be an identifier of type float, while the right-hand-side is a literal of type integer.

An expression can be a sequence of expressions separated by the token; e.g.,

```
let p = 2.0 in printfn "%A" p; printfn "%A" (3.0 ** p)
```

```
2.0
9.0
```

Listing 6.7: letValueSequence.fsx - A value binding for a sequence of expressions.

The lightweight syntax automatically inserts the ; token at newlines, hence using the lightweight syntax the above is the same as,

```
let p = 2.0
printfn "%A" p
printfn "%A" (3.0 ** p)
```

```
2.0
9.0
```

Listing 6.8: letValueSequenceLightWeight.fsx - A value binding for a sequence using lightweight syntax.

A key concept of programming is scope. In F#, the scope of a value binding is lexically meaning that the binding is constant from the let statement defining it, until it is redefined, e.g.,

 \cdot scope

```
let p = 3 in let p = 4 in printfn " %A" p;
```

4

Listing 6.9: letValueScopeLower.fsx - Redefining identifiers is allowed in lower scopes.

Scopes are given levels, and scopes may be nested, where the nested scope has a level one lower than its parent. F# distinguishes between the top and lower levels, and at the top level in the lightweight syntax, redefining values is not allowed, e.g.,

```
let p = 3
let p = 4
printfn "%A" p;
```

```
/Users/sporring/repositories/fsharpNotes/src/letValueScopeLowerError.fsx(2,5):
error FS0037: Duplicate definition of value 'p'
```

Listing 6.10: letValueScopeLowerError.fsx - Redefining identifiers is not allowed in lightweight syntax at top level.

But using begin and end keywords, we create a block which acts as a nested scope, and then redefining is allowed, e.g.,

blocknested scope

```
begin
  let p = 3
  let p = 4
  printfn "%A" p
end
```

```
4
```

Listing 6.11: letValueScopeBlockAlternative2.fsx - A block has lower scope level, and rebinding is allowed.

It is said that the second binding *overshadows* the first. Alternatively we may use parentheses to create a block, e.g.,

 \cdot overshadows

```
(
  let p = 3
  let p = 4
  printfn "%A" p
)
```

```
4
```

Listing 6.12: letValueScopeBlockAlternative3.fsx - A block may be created using parentheses.

In both cases we used indentation, which is good practice, but not required here. Lowering level is a natural part of function definitions to be discussed in Section 6.3 and flow control structures to be discussed in Chapter 7.

Defining blocks is useful for controlling the extend of a lexical scope of bindings. For example, adding a second printfn statement,

```
let p = 3 in let p = 4 in printfn "%A" p; printfn "%A" p
```

```
4 4
```

Listing 6.13: letValueScopeBlockProblem.fsx - Overshadowing hides the first binding.

will print the value 4 last bound to the identifier p, since token; associates to the right, i.e., the above is interpreted as let p = 3 in let p = 4 in (printfn "%A"p; printfn "%A"p). Instead we may create a block as.³

```
let p = 3 in (let p = 4 in printfn " %A" p); printfn " %A" p;
```

```
4
3
```

Listing 6.14: letValueScopeBlock.fsx - Blocks allow for the return to the previous scope.

Here the lexical scope of let p=4 in ... is for the nested scope, which ends at), returning to the lexical scope of let p=3 in Alternatively, the begin and end keywords could equally have been used.

6.2 Non-recursive functions

A function is a mapping between an input and output domain. A key advantage of using functions, when programming, is that they *encapsulate code* into smaller units, that are easier to debug and may be reused. F# is a functional first programming language, and offers a number of alternative methods for specifying parameters, which will be discussed in this section. Binding identifiers to functions follows a syntax similar to value binding,

 $\begin{array}{c} \cdot \ encapsulate \\ code \end{array}$

³spacing in lstinline mode after double quotation mark is weird.

⁴Remember to say something about interactive scripts and the ;; token and scope

Functions may also be recursive, which will be discussed in Chapter 7. An example in interactive mode is,

```
> let sum (x : float) (y : float) : float = x + y in
- let c = sum 357.6 863.4 in
- printfn "%A" c;;
1221.0

val sum : x:float -> y:float -> float
val c : float = 1221.0
val it : unit = ()
```

Listing 6.15: fsharpi, An example of a binding of an identifier and a function.

and we see that the function is interpreted to have the type val sum: x:float -> y:float -> float. The -> token means a mapping between sets, in this case floats. The function is also a higher order function, to be discussed in detail below, and here it suffices to think of sum as a function that takes 2 floats as argument and returns a float.

Not all types need to be declared, just sufficient for F# to be able to infer the types for the full statement. In the example, one sufficient specification is, and we could just have specified the type of the result,

```
let sum x y : float = x + y
```

Listing 6.16: All types need most often not be specified.

or even just one of the arguments,

```
let sum (x : float) y = x + y
```

Listing 6.17: Just one type is often enough for F# to infer the rest.

In both cases, since the + operator is only defined for operands of the same type, then when the type of either the result, any or both operands are declared, then the type of the remaining follows directly. As for values, lightweight syntax automatically inserts the keyword in and the token;

 $\begin{array}{c} \cdot \ operator \\ \cdot \ operand \end{array}$

```
let sum x y : float = x + y
let c = sum 357.6 863.4
printfn "%A" c
```

```
1221.0
```

Listing 6.18: letFunctionLightWeight.fsx - Lightweight syntax for function definitions.

Arguments need not always be inferred to types, but may be of generic type, which F# prefers, when $type\ safety$ is ensured, e.g.,

· type safety

```
> let second x y = y
- let a = second 3 5
- printfn "%A" a
- let b = second "horse" 5.0
- printfn "%A" b;;
```

```
val second : x:'a -> y:'b -> 'b
val a : int = 5
val b : float = 5.0
val it : unit = ()
```

Listing 6.19: fsharpi, Typesafety implies that a function will work for any type, and hence it is generic.

Here the function **second** does not use the first argument, x which is any type called 'a, and the type of the second element, y, is also any type an not necessarily the same as x, so it is called 'b. Finally the result is the same type as y, whatever it is. This is an example of a *generic function*.

A function may contain a sequence of expressions, but must return a value. E.g., the quadratic formula may written as,

 \cdot generic function

```
let solution a b c sgn =
  let determinant a b c =
    b ** 2.0 - 2.0 * a * c
  let d = determinant a b c
  (-b + sgn * sqrt d) / (2.0 * a)

let a = 1.0
  let b = 0.0
  let c = -1.0
  let xp = solution a b c +1.0
  let xn = solution a b c -1.0
  printfn "%A * x ** 2.0 + %A * x + %A" a b c
  printfn " has solutions %A and %A" xn xp
```

```
1.0 * x ** 2.0 + 0.0 * x + -1.0
has solutions -0.7071067812 and 0.7071067812
```

Listing 6.20: identifiers Example Advance. fsx - A function may contain sequences of expressions.

Here we used the lightweight syntax, where the = identifies the start of a nested scope, and F# identifies the scope by indentation. The amount of space used for indentation is does not matter, but all lines following the first must use the same. The scope ends before the first line with the previous indentation or none. Notice how the last expression is not bound to an identifier, but is the result of the function, i.e., in contrast to many other languages, F# does not have an explicit keyword for returning values. Note also that since the function determinant is defined in the nested scope of solution, then determinant cannot be called outside solution, since the scope ends before let a = 1.0.

Lexical scope and function definitions can be a cause of confusion as the following example shows,

· lexical scope

```
let testScope x =
  let a = 3.0
  let f z = a * x
  let a = 4.0
  f x
printfn "%A" (testScope 2.0)
```

```
6.0
```

Listing 6.21: lexical ScopeNFunction.fsx - Lexical scope means that f(z) = 3x and not 4x at the time of calling.

Here the value binding for a is redefined, after it has been used to define a helper function f. So which value of a is used when we later apply f to an argument? To resolve the confusion, remember that value binding is lexically defined, i.e., the binding let f z = a * x uses the value of a, it has by the ordering of the lines in the script, not dynamically by when f was called. Hence, think of lexical scope

Advice

as substitution of an identifier with its value or function immediately at the place of definition. I.e., since a and 3.0 are synonymous in the first lines of the program, then the function f is really defined as, let f z = 3.0 * x.

Functions do not need a name, but may be declared as an anonymous function using the fun keyword and the -> token,

· anonymous function

```
let first = fun x y -> x
printfn "%d" (first 5 3)
```

```
5
```

Listing 6.22: functionDeclarationAnonymous.fsx - Anonymous functions are functions as values.

Here a name is bound to an anonymous function, which returns the first of two arguments. The difference to $let\ first\ x\ y=x$ is that anonymous functions may be treated as values, meaning that they may be used as arguments to other functions, and new values may be reassigned to their identifiers, when mutable, as will be discussed in Section . A common use of anonymous functions is as as arguments to other functions, e.g.,

```
let apply f x y = f x y
let mul = fun a b -> a * b
printfn "%d" (apply mul 3 6)
```

```
18
```

Listing 6.23: functionDeclarationAnonymousAdvanced.fsx - Anonymous functions are often used as arguments for other functions.

Note that here apply is given 3 arguments, the function mul and 2 integers. It is not given the result of mul 3 6, since that would not match the definition of apply. Anonymous functions and functions as arguments are powerfull concepts, but tend to make programs harder to read, and their use should be limited.

Advice

· currying

Functions may be declared from other functions

```
let mul (x, y) = x*y
let double y = mul (2.0, y)
printfn "%g" (mul (5.0, 3.0))
printfn "%g" (double 3.0)
```

```
15
6
```

Listing 6.24: functionDeclarationTupleCurrying.fsx -

For functions of more than 1 argument, there exists a short notation, which is called *currying* in tribute of Haskell Curry,

```
let mul x y = x*y
let double = mul 2.0
printfn "%g" (mul 5.0 3.0)
printfn "%g" (double 3.0)
```

```
15
6
```

Listing 6.25: functionDeclarationCurrying.fsx -

Here mul 2.0 is a partial specification of the function mul x y, where the first argument is fixed, and hence, double is a function of 1 argument being the second argument of mul. Currying is often used in functional programming, but generally currying should be used carefully, since currying may seriously reduce readability of code.

Advice

A procedure is a generalisation of the concept of functions, and in contrast to functions procedures need not return values,

 \cdot procedure

```
let printIt a = printfn "This is '%A'" a
printIt 3
printIt 3.0
```

```
This is '3'
This is '3.0'
```

Listing 6.26: procedure.fsx - A procedure is a function that has no return value, which in F# implies () as return value.

In F# this is automatically given the unit type as return value. Procedural thinking is useful for encapsulation of scripts, but is prone to side-effects and should be minimized by being replaced by functional thinking. More on side-effects in Section ??. which also does not have a return value. Procedural thinking is useful for encapsulation, but is prone to side-effects and should be minimized by being replaced by functional thinking.

 $\begin{array}{l} \cdot \ encapsulation \\ \cdot \ side-effects \end{array}$

6.3 User-defined operators

Operators are functions, e.g., the infix multiplication operator + is equivalent to the function (+), e.g.,

```
let a = 3.0
let b = 4.0
let c = a + b
let d = (+) a b
printfn "%A plus %A is %A and %A" a b c d
```

```
3.0 plus 4.0 is 7.0 and 7.0
```

Listing 6.27: addOperatorNFunction.fsx -

All operator has this option, and you may redefine them and define your own operators, who has names specified by the following simplified EBNF:

 $^{^{5}}$ comment on dynamic scope and mutable variables.

 $^{^6}$ Remember examples of return of functions, no arguments (), and wildcard patterns as arguments $_$.

```
| "^" {opChar}
| "*" {opChar}
| "/" {opChar}
| "%" {opChar}
| "!=" )
| ":=" | "::" | "$" | "?"
```

Listing 6.28: Grammar for infix and prefix tokens

The precedence rules and associativity of user-defined operators follows the rules for which they share prefixes with built-in rules, see Table ??. E.g., .*, +++, and <+ are valid operator names for infix operators, they have precedence as ordered, and their associativity are all left. Using ~ as the first character in the definition of an operator makes the operator unary and will not be part of the name. Examples of definitions and use of operators are,

```
let (.*) x y = x * y + 1
printfn "%A" (3 .* 4)
let (+++) x y = x * y + y
printfn "%A" (3 +++ 4)
let (<+) x y = x < y + 2.0
printfn "%A" (3.0 <+ 4.0)
let (~+.) x = x+1
printfn "%A" (+.1)</pre>
```

```
13
16
true
2
```

Listing 6.29: operator Definitions. fsx -

Beware, redefining existing operators lexically redefines all future uses of operator for all types, hence it is not a good idea to redefine operators, but better to define new. In Chapter /refchap:oop we will discuss how to define type specific operators including prefix operators.

Advice

Operators beginning with * must use a space in its definition, (* in order for it not to be confused with the beginning of a comment (*. 8

6.4 Printf

A common way to output information to the console is to use one of the family of printf commands. These functions are special, since they take a variable number of arguments, and the number is decided by the first - the format string,

·printf

```
"printf" formatString {ident}
```

where a formatString is a string (simple or verbatim) with placeholders,

```
placeholder = "%%" | ""%" ["0"] ["+"] ["-"] [SP] [dInt] ["." dInt] [
    placeholderType]
placeholderType = "b" | "d" | "i" | "u" | "x" | "X" | "o" | "e" | "E" | "f" | "F"
    | "g" | "G" | "M" | "O" | "A" | "a" | "t"
```

and where the number of arguments after formatString must match the number of placerholders in formatString. The placeholderType is elaborated in Table 6.1. The function printf prints formatString to the console, where all placeholder has been replaced by the value of the corresponding argument formatted as specified. E.g.,

⁷It seems there is a bug in mono: let (+) x = x+1 in printfn "%A" +1;; prints 1 and not 2.

⁸this requires comments to be describe previously!

Placeholder	Type	Description
%b	bool	Replaces with boolean value
%s	string	
%с	char	
%d, %i	basic integer	
%u	basic unsigned integers	
%x	basic integer	formatted as unsigned hexadecimal with lower case letters
%X	basic integer	formatted as unsigned hexadecimal with upper case letters
floating point type %o	basic integer	formatted as unsigned octal integer
%f, %F,	basic floats	formatted on decimal form
%e, %E,	basic floats	formatted on scientific form. Lower case uses "e" while upper case uses "E" in the formatting.
%g, %G,	basic floats	formatted on the short- est of the correspond- ing decimal or scientific form.
%M	decimal	
%0	Objects ToString method	
%A	any built-in types	Formatted as a literal type
%a	Printf.TextWriterFormat ->'a -> ()	
%t	(Printf.TextWriterFormat -> ()	

Table 6.1: Printf placeholder string

```
let pi = 3.1415192
let hello = "hello"
printf "An integer: %d\n" (int pi)
printf "A float %f on decimal form and on %e scientific form, and a char '%c'\
    n" pi pi
printf "A char '%c' and a string \"%s\"\n" hello.[0] hello
printf "Float using width 8 and 1 number after the decimal:\n"
printf " \"%8.1f\" \"%8.1f\"\n" pi -pi
printf " \"%08.1f\" \"%08.1f\"\n" pi -pi
printf " \"% 8.1f\" \"%8.1f\"\n" pi -pi
printf " \"%-8.1f\" \"%-8.1f\"\n" pi -pi
```

```
An integer: 3
A char 'h' and a string "hello"
Float using width 8 and 1 number after the decimal:

" 3.1" " -3.1"

"000003.1" "-00003.1"

" 3.1" " -3.1"

"3.1 " "-3.1 "

" +3.1" " -3.1"

" hello"
"hello"
```

Listing 6.30: printfExample.fsx - Examples of printf and some of its formatting options.

Not all combinations of flags and identifier types are supported, e.g., strings cannot have number of integers after the decimal specified. ⁹ ¹⁰ The placeholder types "%A", "%a", and "%t" are special for F#, examples of their use are,

```
let noArgument writer = printf "I will not print anything"
let customFormatter writer arg = printf "Custom formatter got: \"%A\"" arg
printf "Print examples: %A, %A, %A\n" 3.0m 3uy "a string"
printf "Print function with no arguments: %t\n" noArgument
printf "Print function with 1 argument: %a\n" customFormatter 3.0
```

```
Print examples: 3.0M, 3uy, "a string"

Print function with no arguments: I will not print anything

Print function with 1 argument: Custom formatter got: "3.0"
```

Listing 6.31: printfExampleAdvance.fsx -

The %A is special in that all built-in types including tuples, lists, and arrays to be discussed in Chapter 8 can be printed using this formatting string, but notice that the formatting performed includes the named literal string. The two formatting strings %t and %a are options for user-customizing the formatting, and will not be discussed further.

Beware, formatString is not a string but a Printf.TextWriterFormat, so let str = "hello % s"in printf str "world" will be a type error.

The family of printf is shown in Table 6.2. The function fprintf prints to a stream, e.g., stderr and stdout, of type System.IO.TextWriter. Streams will be discussed in further detail in Chapter ??. The function failwithf is used with exceptions, see Chapter 9 for more details. The function has a number of possible return value types, and for testing the *ignore* function ignores it all, e.g., ignore (failwithf "\%d failed apples"3) 11

·ignore

⁹Mono seems to have a bug, printfn "%.1g" 3.13;; and printfn "%.1f" 3.13;; produces different number of digits.

 $^{^{10}}$ Spec-4.0 %s and %b are missing in Section 3.1.16.

¹¹Mono: bprintf and kprintf are undefined.

Function	Example	Description	
printf	printf "%d apples"3	Prints to the console, i.e., stdout	
printfn		as printf and adds a newline.	
fprintf	fprintf stream "%d apples"3	Prints to a stream, e.g., stderr and stdout	
		, which would be the same as printf and	
		eprintf.	
fprintfn		as fprintf but with added newline.	
eprintf	eprintf "%d apples"3	Print to stderr	
eprintfn		as eprintf but with added newline.	
sprintf	printf "%d apples"3 Return printed string		
failwithf	failwithf "%d failed apples"3	prints to a string and used for raising an excep-	
		tion.	

Table 6.2: The family of printf functions.

6.5 Variables

The mutable in let bindings means that the identifier may be rebound to a new value using the following syntax,

```
expr "<-" expr
```

Mutable data is synonymous with the term variable. A variable is an area in the computers working memory associated with an identifier and a type, and this area may be read from and written to during program execution. For example,

```
· Mutable data
· variable
```

· <-

```
let mutable x = 5
printfn "%d" x
x <- -3
printfn "%d" x</pre>
```

```
5
-3
```

Listing 6.32: mutableAssignReassingShort.fsx - A variable is defined and later reassigned a new value.

Here a area in memory was denoted x, initially assigned the integer value 5, hence the type was inferred to be int. Later, this value of x was replaced with another integer using the <- token. The <- token is used to distinguish the assignment from the comparison operator, i.e., if we by mistake had written,

```
> let mutable a = 0
- a = 3;;

val mutable a : int = 0
val it : bool = false
```

Listing 6.33: fsharpi, Common error - mistaking = and <- tokens for mutable variables. The former is the test operator, while the latter is the assignment expression.

then we instead would have obtained the default assignment of the result of the comparison of the content of a with the integer 3, which is false. However, it's important to note, that when the variable is initially defined, then the '=' operator must be used, while later reassignments must use the <- expression.

Assignment type mismatches will result in an error,

```
let mutable x = 5
printfn "%d" x
x <- -3.0
printfn "%d" x</pre>
```

```
/Users/sporring/repositories/fsharpNotes/src/mutableAssignReassingTypeError.
  fsx(3,6): error FS0001: This expression was expected to have type
  int
but here has type
  float
```

Listing 6.34: mutableAssignReassingTypeError.fsx - Assignment type mismatching causes a compile time error.

I.e., once the type of an identifier has been declared or inferred, then it cannot be changed.

A typical variable is a counter of type integer, and a typical use of counters is to increment them, i.e., erasing a new value to be one more that its previous value. For example,

```
let mutable x = 5 // Declare a variable x and assign the value 5 to it printfn "%d" x x <- x + 1 // Assign a new value -3 to x printfn "%d" x
```

```
5
6
```

 $\textbf{Listing 6.35:} \ \ \text{mutable Assign Increment. fsx-Variable increment is a common use of variables}.$

A function that elegantly implements the incrementation operation may be constructed as,

```
let incr =
  let mutable counter = 0
  fun () ->
    counter <- counter + 1
    counter
printfn "%d" (incr ())
printfn "%d" (incr ())
printfn "%d" (incr ())</pre>
```

```
1
2
3
```

Listing 6.36: mutableAssignIncrementEncapsulation.fsx -

¹² Here the output of incr is an anonymous function, that takes no argument, increments the variable of incr and returns the new value of the counter. This construction is called *encapsulation*, since the variable counter is hidden by the function incr from the user, i.e., the user need not be concerned with how the increment operator is implemented and the variable name used by incr does not clutter the scope where it is used.

 \cdot encapsulation

Variables implement dynamic scope, e.g., in comparison with the lexical scope, where the value of an identifier depends on which line in the program, an identifier is defined, dynamic scope depends on, when it is used. E.g., the script in Listing 6.21 defines a function using lexical scope and returns the number 6.0, however, if a is made mutable, then the behaviour is different:

```
let testScope x =
  let mutable a = 3.0
  let f z = a * x
  a <- 4.0
  f x
printfn "%A" (testScope 2.0)</pre>
```

¹²Explain why this works!

```
8.0
```

Listing 6.37: dynamicScopeNFunction.fsx - Mutual variables implement dynamics scope rules. Compare with Listing 6.21.

Here the respons is 8.0, since the value of a changed befor the function f was called. Variables cannot be returned from functions, that is,

```
let g () =
  let x = 0
  x
printfn "%d" (g ())
```

```
0
```

Listing 6.38: mutableAssignReturnValue.fsx -

declares a function that has no arguments and returns the value 0, while the same for a variable is invalid.

```
let g () =
  let mutual x = 0
  x
printfn "%d" (g ())
```

```
/Users/sporring/repositories/fsharpNotes/src/mutableAssignReturnVariable.fsx (3,3): error FS0039: The value or constructor 'x' is not defined
```

Listing 6.39: mutableAssignReturnVariable.fsx -

There is a workaround for this by using $reference\ cells$ by the build-in function ref and operators! \cdot and :=,

 \cdot reference cells

```
let g () =
  let x = ref 0
  x
let y = g ()
  printfn "%d" !y
y := 3
printfn "%d" !y
```

```
0 3
```

Listing 6.40: mutableAssignReturnRefCell.fsx -

That is, the ref function creates a reference variable, the '!' and the ':=' operators reads and writes its value. Reference cells are in some language called pointers, and their use is strongly discouraged, since they may cause *side-effects*, which is the effect that one function changes the state of another, such as the following example demonstrates,

 \cdot side-effects

```
let updateFactor factor =
  factor := 2

let multiplyWithFactor x =
  let a = ref 1
  updateFactor a
  !a * x

printfn "%d" (multiplyWithFactor 3)
```

6

Listing 6.41: mutableAssignReturnSideEffect.fsx -

In the example, the function updateFactor changes a variable in the scope of multiplyWithFactor, which is prone to errors, since the style of programming does not follow the usual assignment syntax. Better style of programming is,

```
let updateFactor () =
  2

let multiplyWithFactor x =
  let a = ref 1
  a := updateFactor ()
  !a * x

printfn "%d" (multiplyWithFactor 3)
```

```
6
```

Listing 6.42: mutableAssignReturnWithoutSideEffect.fsx -

Here there can be no doubt in multiplyWithFactor that the value of 'a' is changing. Side-effects do have their use, but should in general be avoided at almost all costs, and in general it is advised to refrain from using ref cells.

6.6 In-code documentation

Documentation is a very important part of writing programs, since it is most unlikely, that you will be writing really obvious code. And what seems obvious at the point of writing may be mystifying months later to the author and to others. The documentation serves several purposes:

- 1. Communicate what the code should be doing
- 2. Highlight big insights essential for the code
- 3. Highlight possible conflicts and/or areas, where the code could be changed later

The essential point is that coding is a journey in problem solving, and proper documentation is an aid in understanding the solution and the journey leading to it. Documentation is most often a mixture between in-code documentation and accompanying documents. Here we will focus on in-code documentation, but arguably this does cause problems in multi-language environments, and run the risk of bloating code.

F# has the following simplified syntax for in-code documentation,

```
blockComment = "(*" {codePoint} "*)"
lineComment = "//" {codePoint - newline} newline
```

That is, text framed as a blockComment is still parsed by F# as keywords and basic types implying that (* a comment (* in a comment *)*) and (* "*)" *) are valid comments, while (* " *) is invalid.¹⁴

The F# compiler has an option for generating Extensible Markup Language (XML) files from scripts using the C# documentation comments tags¹⁵. The XML documentation starts with a triple-slash

 $\begin{array}{c} \cdot \, \text{Extensible} \\ \, \text{Markup} \\ \, \text{Language} \end{array}$

 \cdot XML

The AME documentation comments tags. The AME documentation starts with a

¹³Add something about mutable functions

¹⁴lstlisting colors is bad.

 $^{^{15}} For specification of C\#$ documentations comments see ECMA-334 3rd Edition, Annex E, Section 2: http://www.ecma-international.org/publications/files/ECMA-ST/Ecma-334.pdf

Tag	Description
<c></c>	Set text in a code-font.
<code></code>	Set one or more lines in code-font.
<example></example>	Set as an example.
<exception></exception>	Describe the exceptions a function can throw.
t>	Create a list or table.
<para></para>	Set text as a paragraph.
<pre><param/></pre>	Describe a parameter for a function or constructor.
<pre><paramref></paramref></pre>	Identify that a word is a parameter name.
<pre><permission></permission></pre>	Document the accessibility of a member.
<remarks></remarks>	Further describe a function.
<returns></returns>	Describe the return value of a function.
<see></see>	Set as link to other functions.
<seealso></seealso>	Generate a See Also entry.
<summary></summary>	Main description of a function or value.
<typeparam></typeparam>	Describe a type parameter for a generic type or method.
<typeparamref></typeparamref>	Identify that a word is a type parameter name.
<value></value>	Describe a value.

Table 6.3: Recommended XML tags for documentation comments, from ECMA-334 3rd Edition, Annex E, Section 2.

///, i.e., a lineComment and a slash, which serves as comments for the code construct, that follows immediately after. XML consists of tags which always appears in pairs, e.g., the tag "tag" would look like <tag>... </tag>. The F# accept any tags, but recommends those listed in Table 6.3. If no tags are used, then it is automatically assumed to be a <summary>. An example of a documented script is,

```
/// Calculate the determinant of a quadratic equation with parameters a, b,
   and c
let determinant a b c =
 b ** 2.0 - 2.0 * a * c
/// < summary > Find x when 0 = ax^2+bx+c. </summary >
/// <remarks>Negative determinants are not checked.</remarks>
/// <example>
     The following code:
     <code>
111
111
       let a = 1.0
       let b = 0.0
111
       let c = -1.0
///
111
      let xp = (solution a b c +1.0)
111
       printfn "0 = %.1fx^2 + %.1fx + %.1f => x_+ = %.1f" a b c xp
111
     results in \langle c \rangle 0 = 1.0x^2 + 0.0x + -1.0 = x_+ = 0.7 \langle c \rangle printed to the
111
   console.
/// </example>
/// <param name="a">Quadratic coefficient.</param>
/// <param name="b">Linear coefficient.</param>
/// <param name="c">Constant coefficient.</param>
.</param>
/// <returns>The solution to x.</returns>
let solution a b c sgn =
 let d = determinant a b c
 (-b + sgn * sqrt d) / (2.0 * a)
```

```
let a = 1.0
let b = 0.0
let c = -1.0
let xp = (solution a b c +1.0)
printfn "0 = %.1fx^2 + %.1fx + %.1f => x_+ = %.1f" a b c xp
```

```
0 = 1.0x^2 + 0.0x + -1.0 \Rightarrow x_+ = 0.7
```

Listing 6.43: commentExample.fsx - Code with XML comments.

Mono's fsharpc command may be used to extract the comments into an XML file,

```
$ fsharpc --doc:commentExample.xml commentExample.fsx
F# Compiler for F# 4.0 (Open Source Edition)
Freely distributed under the Apache 2.0 Open Source License
```

This results in an XML file with the following content,

```
<?xml version="1.0" encoding="utf-8"?>
<doc>
<assembly><name>commentExample</name></assembly>
<members>
<member name="M:CommentExample.solution(System.Double,System.Double,System.</pre>
   Double, System. Double) ">
<summary>Find x when 0 = ax^2+bx+c.</summary>
<remarks>Negative determinants are not checked.</remarks>
<example>
  The following code:
   <code>
    let a = 1.0
    let b = 0.0
    let c = -1.0
    let xp = (solution a b c +1.0)
    printfn "0 = \%.1fx^2 + \%.1fx + \%.1f => x_+ = \%.1f" a b c xp
  </code>
  results in <c>0 = 1.0x^2 + 0.0x + -1.0 => x_+ = 0.7 </c> printed to the
      console.
</example>
 <param name="a">Quadratic coefficient.</param>
<param name="b">Linear coefficient.</param>
 <param name="c">Constant coefficient.</param>
<param name="sgn">+1 or -1 indicating which solution is to be calculated./
    param>
<returns>The solution to x.</returns>
</member>
<member name="M:CommentExample.determinant(System.Double,System.Double,System.</pre>
   Double)">
<summary>
Calculate the determinant of a quadratic equation with parameters a, b, and c
</summary>
</member>
</members>
</doc>
```

The extracted XML is written in C# type by convention, since F# is part of the Mono and .Net framework that may be used by any of the languages using Assemblies. Besides the XML inserted in the script, the XML has added <?xml ...> header, <doc>, <assembly>, <members>, and <member > tags. The header and the <doc> tag are standards for XML. The extracted XML is geared towards documenting big libraries of codes and thus highlights the structured programming organization, see Part IV, and <assembly>, <members>, and <member> are indications for where the functions belong in the hierarchy. As an example, the prefix M:CommentExample. means that it is a

method in the namespace CommentExample, which in this case is the name of the file. Further, the function type val solution: a:float -> b:float -> c:float -> sgn:float -> float is in the XML documentation M:CommentExample.solution(System.Double,System.Do

An accompanying program in the Mono suite is mdoc, which primary use is to perform a syntax analysis of an assembly and generate a scaffold XML structure for an accompanying document. With the -i flag, it is further possible to include the in-code comments as initial descriptions in the XML. The XML may be updated gracefully by mdoc as the code develops, without destroying manually entered documentation in the accompanying documentation. Finally, the XML may be exported to HTML The primary use of the mdoc command is to analyze compiled code and generate an empty XML structure with placeholders to describe functions, values, and variables. This structure can then be updated and edited as the program develops. The edited XML files can then be exported to Hyper Text Markup Language (HTML) files, which can be viewed in any browser. Using the console, all of this is accomplished by,

The primary use of the mdoc command is to analyze compiled code and generate an empty XML structure with placeholders to describe functions, values, and variables. This structure can then be updated and edited as the program develops. The edited XML files can then be exported to HTML files, which can be viewed in any browser, an example of which is shown in Figure 6.3. A full description of how to use mdoc is found here¹⁶.

[·] Hyper Text Markup Language

 $[\]cdot \, \mathrm{HTML}$

 $^{^{16}}$ http://www.mono-project.com/docs/tools+libraries/tools/monodoc/generating-documentation/

solution Method

Find x when $0 = ax^2+bx+c$.

Syntax

```
[Microsoft.FSharp.Core.CompilationArgumentCounts(Mono.Cecil.CustomAttributeArgument[])] public static double solution (double a, double b, double c, double sgn)
```

Parameters

- a Quadratic coefficient.

 b Linear coefficient.

 c Constant coefficient.

 sgn +1 or -1 indicating which solution is to be calculated.
- Returns

The solution to x.

Remarks

Negative determinants are not checked.

Example

Requirements

```
Namespace:
Assembly: commentExample (in commentExample.dll)
Assembly Versions: 0.0.0.0
```

Figure 6.3: Part of the HTML documentation as produce by mdoc and viewed in a browser.

Controlling program flow

Non-recursive functions encapsulates code and allows for some control of flow, that is, if there is a piece of code, which we need to to have executed many times, then we can encapsulate it in the body of a function, and then call the function several times. In this chapter, we will look at more general control of flow via loops, conditional execution, and recursion, and therefore we look at further extension of the expr rule,

7.1 For and while loops

Many programming constructs need to be repeated. The most basic example is counting, e.g., from 1 to 10 with a *for*-loop,

 \cdot for

```
> for i = 1 to 10 do
- printf "%d " i
- printfn "";;
1 2 3 4 5 6 7 8 9 10
val it : unit = ()
```

Listing 7.1: fsharpi, Counting from 1 to 10 using a for-loop.

As this interactive script demonstrates, the identifier i takes all the values between 1 and 10, but in spite of its changing state, it is not mutable. Note also that the return value of the for expression is () like the printf functions. The for and while loops follow the syntax,

```
pat = const | ...
expr = ...
```

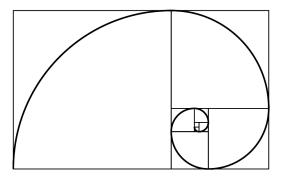


Figure 7.1: The Fibonacci spiral is an approximation of the golden spiral. Each square has side lengths of successive Fibonacci numbers, and the curve in each square is the circular arc with radius of the square it is drawn in. Figure by Dicklyon https://commons.wikimedia.org/w/index.php?curid=3730979

Using lightweight syntax the script block between the **do** and **done** keywords may be replaced by a newline and indentation, e.g.,

· do · done

```
for i = 1 to 10 do
  printf "%d " i
printfn ""
```

```
1 2 3 4 5 6 7 8 9 10
```

Listing 7.2: countLightweight.fsx - Counting from 1 to 10 using a for-loop.

A more complicated example is,

Write a program that prints the n'th Fibonacci number.

The Fibonacci numbers is the series of numbers 1, 1, 2, 3, 5, 8, 13..., where the fib(n) = fib(n-1) + fib(n-2), and they are related to Golden spirals shown in Figure 7.1. We could solve this problem with a for-loop as follows,

```
let fib n =
  let mutable a = 1
  let mutable b = 1
  let mutable f = 0
  for i = 3 to n do
    f <- a + b
    a <- b
    b <- f
  f

printfn "fib(1) = 1"
printfn "fib(2) = 1"
for i = 3 to 10 do
  printfn "fib(%d) = %d" i (fib i)</pre>
```

```
fib(1) = 1

fib(2) = 1

fib(3) = 2

fib(4) = 3

fib(5) = 5

fib(6) = 8

fib(7) = 13

fib(8) = 21

fib(9) = 34

fib(10) = 55
```

Listing 7.3: fibFor.fsx - The n'th Fibonacci number as the sum of the previous 2 numbers, which are sequentially updated from 3 to n.

The basic idea of the solution is that if we are given the (n-1)'th and (n-2)'th numbers, then the n'th number is trivial to compute. And assume that fib(1) and fib(2) are given, then it is trivial to calculate the fib(3). Now we have the first 3 numbers, so we disregard fib(1) and calculate fib(4) from fib(2) and fib(3), and this process continues until we have reached the desired fib(n) For the alternative for-loop, consider the problem,

Write a program that identifies prime factors of a given integer n.

Prime numbers are integers divisible only be 1 and themselves with zero remainder. Let's assume that we already have identified a list of primes from 2 to n, then we could write a program that checks the remainder as follows,

```
let primeFactorCheck n =
  printfn "%d %% i = 0?" n
  for i in [2; 3; 5; 7; 11; 13; 17] do
    printfn "i = %d? %b" i (n%i = 0)
  ()
  primeFactorCheck 10
```

```
10 % i = 0?
i = 2? true
i = 3? false
i = 5? true
i = 7? false
i = 11? false
i = 13? false
i = 17? false
```

Listing 7.4: primeCheck.fsx - Checking whether a given number has remainder zero after division by some low prime numbers.

In this example, the variable **i** runs through the elements of a list, which will be discussed in further detail in Chapter 8.

The *while*-loop is simpler than the for-loop and does not contain a builtin counter structure. Hence, if we are to repeat the count-to-10 program from Listing 7.1 example, it would look somewhat like,

·while

```
let mutable i = 1
while i <= 10 do
    printf "%d " i
    i <- i + 1
printf "\n"</pre>
```

```
1 2 3 4 5 6 7 8 9 10
```

Listing 7.5: countWhile.fsx - Count to 10 with a counter variable.

In this case, the for-loop is to be preferred, since more lines of code typically means more chances of making a mistake. But the while-loop allows for other logical structures. E.g., lets find the biggest Fibonacci number less than 100,

```
let largestFibLeq n =
  let mutable a = 1
  let mutable b = 1
  let mutable f = 0
  while f <= n do
    f <- a + b
    a <- b
    b <- f
  a

printfn "largestFibLeq(1) = 1"
printfn "largestFibLeq(2) = 1"
for i = 3 to 10 do
  printfn "largestFibLeq(%d) = %d" i (largestFibLeq i)</pre>
```

```
largestFibLeq(1) = 1
largestFibLeq(2) = 1
largestFibLeq(3) = 3
largestFibLeq(4) = 3
largestFibLeq(5) = 5
largestFibLeq(6) = 5
largestFibLeq(7) = 5
largestFibLeq(8) = 8
largestFibLeq(9) = 8
largestFibLeq(10) = 8
```

Listing 7.6: fibWhile.fsx - Search for the largest Fibonacci number less than a specified number.

Thus, while-loops are most often used, when the number of iteration cannot easily be decided, when entering the loop.

Both for- and while-loops are often associated with variables, i.e., values that change while looping. If one mistakenly used values and rebinding, then the result would in most cases be of little use, e.g.,

```
let a = 1
for i = 1 to 10 do
  let a = a + 1
  printf "(%d, %d) " a i
printf "\n"
```

```
(2, 1) (2, 2) (2, 3) (2, 4) (2, 5) (2, 6) (2, 7) (2, 8) (2, 9) (2, 10)
```

Listing 7.7: for ScopeError.fsx - Lexical scope error. While rebinding is valid F# syntax, has little effect due to lexical scope.

I.e., the let expression rebinds a every iteration of the loop, but the value on the right-hand-side is taken lexically from above, where a has the value 1, so every time the result is the value 2.

7.2 Conditional expressions

Consider the task,

Write a function that given n writes the sentence, "I have n apple(s)", where the plural 's' is added appropriately.

For this we need to test on n's size, and one option is to use conditional expressions like,

```
let applesIHave n =
   if n < 0 then "I owe " + (string -n) + " apples"
   elif n < 1 then "I have no apples"
   elif n < 2 then "I have 1 apple"
   else "I have " + (string n) + " apples"

printfn "%A" (applesIHave -3)
printfn "%A" (applesIHave -1)
printfn "%A" (applesIHave 0)
printfn "%A" (applesIHave 1)
printfn "%A" (applesIHave 2)
printfn "%A" (applesIHave 10)</pre>
```

Listing 7.8: Using conditional expression to generate different strings.

The grammar for conditional expressions is,

where the expr following if and elif are conditions, i.e., expressions that evaluate to a boolean value. The expr following then and else are called branches, and all branches must have same type. The result of the conditional expression is the first branch, for which its condition was true. The lightweight syntax allows for the visually more simple expression of scope by use of indentation

·if ·elif

·else

 \cdot conditions \cdot then

· branches

```
let applesIHave n =
  if n < 0 then
    "I owe " + (string -n) + " apples"
  elif n < 1 then
    "I have no apples"
  elif n < 2 then
    "I have 1 apple"
  else
    "I have " + (string n) + " apples"</pre>
```

Listing 7.9: Lightweight syntax allows for making blocks of code by indentation in order to make code more for easy to read.

Note that both elif and else branches are optional, which may cause problems, e.g., both let a = if true then 3 and let a = if true then 3 elif false then 4 will be invalid, since F# is not smart enough to realize that the type of the expression is uniquely determined. Instead F# looks for the else to ensure all cases have been covered, and that a always will be given a unique value of the same type regardless of the branches taken in the conditional statement, hence, let a = if true then 3 else 4 is the only valid expression of the 3. However, the omitted branches are assumed to return (), and thus it is fine to say let a = if true then () and if true then printfn "hej"

7.2.1 Programming intermezzo

Using loops and conditional expressions we are now able to solve the following problem

Given an integer on decimal form, write its equivalent value on binary form

To solve this problem, consider odd numbers: They all have the property, that the least significant bit is 1, e.g., $1_2 = 1, 101_2 = 5, 110_2 = 6$, and that division by 2 is equal to right-shifting by 1, e.g., $1_2/2 = 0.1_2 = 0.5, 101_2/2 = 10.1_2 = 2.5, 110_2/2 = 11_2 = 3$. Thus by integer division by 2 and checking the remainder, we may sequentially read off the least significant bit. This leads to the following algorithm,

```
let dec2bin n =
  if n < 0 then
    "Illegal value"
  elif n = 0 then
    "0b0"
  else
    let mutable v = n
    let mutable str = ""
    while v > 0 do
      str <- (string (v % 2)) + str
      v <- v / 2
    "0b"+str
printfn "d \rightarrow s" -1 (dec2bin -1)
printfn "%d -> %s" 0 (dec2bin 0)
printfn "%d -> %s" 1 (dec2bin 1)
printfn "%d -> %s" 2 (dec2bin 2)
printfn "d \rightarrow s" 3 (dec2bin 3)
printfn "%d -> %s" 10 (dec2bin 10)
printfn "%d -> %s" 1023 (dec2bin 1023)
```

```
-1 -> Illegal value
0 -> 0b0
1 -> 0b1
2 -> 0b10
3 -> 0b11
10 -> 0b1010
1023 -> 0b1111111111
```

Listing 7.10: dec2bin.fsx - Using integer division and remainder to convert any positive integer to binary form.

7.3 Pattern matching

Conditional expressions are so common that a short-hand notation called *pattern matching* is available in F#. For the Consider the task,

· pattern matching

Write a function that given n writes the sentence, "I have n apple(s)", where the plural 's' is added appropriately.

For this we need to test on n's size, and one option is to use conditional expressions like,

```
let applesIHave n =
  match n with
  i when i < 0 -> "I owe " + (string -i) + " apples"
  | 0 -> "I have no apples"
  | 1 -> "I have 1 apple"
  | _ -> "I have " + (string n) + " apples"

printfn "%A" (applesIHave -3)
printfn "%A" (applesIHave -1)
printfn "%A" (applesIHave 0)
printfn "%A" (applesIHave 1)
printfn "%A" (applesIHave 2)
printfn "%A" (applesIHave 10)
```

```
"I owe 3 apples"
"I owe 1 apples"
```

```
"I have no apples"
"I have 1 apple"
"I have 2 apples"
"I have 10 apples"
```

Listing 7.11: matchWith.fsx - Using the match-keywordwith programming construct to vary calculation based on the input value.

Here the match-with keywords starts a sequence of conditions separated by the | token, where the default operator is the = comparison operator, but where others can be used with the when. The syntax of match expressions is,

```
match with when
```

```
pat = const | "_" | ...
guard = "when" expr
rule = pat [guard] -> expr
rules = "|" rule | "|" rule rules (* first "|'' is optional' *)
expr = ...
   | "match " expr " with " rules (* match expression *)
   | "function " rules (* matching function expression *)
   | ...
```

As for conditional expressions, the rules are treated sequentially from first to last, and the expression following the first rule with a true condition is the the result of the entire expression. The rules are versatile in their possible expression, e.g., the line | 1 -> "I have no apples" is equivalent to elif n < 1 then "I have no apples", and the \lstinline| _ -> "I have " + (string n) + "apples"!, matches the else "I have "+ (string n)+ "apples", since the _ token is a wildcard pattern matching anything. Finally, the first rule is a guarded rule indicated by the when keyword, i when i < 0 -> "I owe "+ (string -i)+ "apples". It uses the optional disregard of the | token and is equivalent to if n < 0 then "I owe "+ (string -n)+ "apples". Guarded rules can be any rules, and here we used the identifier i meaning let i = n in if i < 0 then ..., i.e., n is renamed. One way to think of guarded expressions is that i when i < 0 is a set, and the condition is on n being part of the set or not.

Using lightweight syntax, the rules may be put on separate lines but must start in the column, where the match starts or greater. Match with can only take one identifier, but this can be tuples for matching with combinations of identifiers, see Chapter 8 for more on tuples. A match expression is general but is most often seen as the initial part of a function definition. This is so common, that F# has a special syntax integrating function definitions and match with expressions using the function keyword,

·function

```
let applesIHave = function
  i when i < 0 -> "I owe " + (string -i) + " apples"
  | 0 -> "I have no apples"
  | 1 -> "I have 1 apple"
  | n -> "I have " + (string n) + " apples"

printfn "%A" (applesIHave -3)
printfn "%A" (applesIHave -1)
printfn "%A" (applesIHave 0)
printfn "%A" (applesIHave 1)
printfn "%A" (applesIHave 1)
printfn "%A" (applesIHave 2)
printfn "%A" (applesIHave 10)
```

```
"I owe 3 apples"
"I owe 1 apples"
"I have no apples"
"I have 1 apple"
"I have 2 apples"
```

¹Spec-4.0 weirdness: Offside rule for match is different for function.

```
"I have 10 apples"
```

Listing 7.12: functionKeyword.fsx - Function definition and match expressions are integrated using the function keyword. Compare with Listing 7.11

Comparing with Listing 7.11 notice that the function definition does not explicitly name an argument but assumes one, following the function follows immediately the rules, and the wildcard pattern $_$ is replaced with an identifier without any guards, which thus matches everything. Replacing the wildcard pattern with a name has the advantage that this name can be used locally in the expression belonging to this rule, i.e., it acts as a let n = 0 on the implicit argument of the function. Implicit arguments makes the code hard to read and, thus the use of function definitions with the keyword function should be avoided.

Advice

7.4 Recursive functions

Recursion is a central concept in F#. A recursive function is a function, which calls itself. From a compiler point of view, this is challenging, since the function is used before the compiler has completed its analysis. However, this there is a technical solution for, and we will just concern ourselves with the logics of using recursion for programming. An example of a recursive function that counts from 1 to 10 similarly to Listing 7.1 is,

· recursive function

```
let rec prt a b =
   if a > b then
      printf "\n"
   else
      printf "%d " a
      prt (a + 1) b
```

```
1 2 3 4 5 6 7 8 9 10
```

Listing 7.13: countRecursive.fsx - Counting to 10 using recursion.

Here the prt calls itself repeatedly, such that the first call is prt 1 10, which calls prt 2 10, and so on until the last call prt 10 10. Calling prt 11 10 would not result in recursive calls, since when a is higher than 10 then the *stopping criterium* is met and a newline is printed. For values of a smaller than or equal b then the recursive branch is executed. Since prt calls itself as the last all but the stopping condition, then this is a *tail-recursive* function. Most compilers achieve high efficiency in terms of speed and memory, so *prefer tail-recursion whenever possible*.

· stopping criterium · tail-recursive Advice

```
functionOrValueDefnList =
  functionOrValueDefn
  | functionOrValueDefn " and " functionOrValueDefnList
  expr = ...
  | "let " rec functionOrValueDefnList (* recursive definition *)
  | ...
```

Using recursion to calculate the Fibonacci number as Listing 7.3.

```
let rec fib n =
  match n with
    i when i < 1 -> 0
    | i when i = 1 -> 1
    | i -> fib (n - 1) + fib (n - 2)

for i = 0 to 10 do
  printfn "fib(%d) = %d" i (fib i)
```

```
fib(0) = 0
fib(1) = 1
fib(2) = 1
fib(3) = 2
fib(4) = 3
fib(5) = 5
fib(6) = 8
fib(7) = 13
fib(8) = 21
fib(9) = 34
fib(10) = 55
```

Listing 7.14: fibRecursive.fsx - The n'th Fibonacci number using recursive.

Here we used the fact that including $\operatorname{fib}(0) = 0$ in the Fibonacci series also produces it using the rule $\operatorname{fib}(n) = \operatorname{fib}(n-2) + \operatorname{fib}(n-1), \ n \geq 0$, which allowed us to define a function that is well defined for the complete set of integers. I.e., a negative argument returns 0. This is a general advice: $make\ functions$ that fails gracefully. The recursive definition allows for recursive value definitions and defining several values and functions in one expression. This is rarely used and will not be discussed further in this text.

Advice

Tuples, Lists, Arrays, and Sequences

F# is tuned to work with lists. However, an elegant alternative is available as

```
let courseGrades =
    ["Introduction to programming", 95;
    "Linear algebra", 80;
    "User Interaction", 85;]

let mutable sum = 0;
let mutable n = 0;
for (title, grade) in courseGrades do
    printfn "Course: %s, Grade: %d" title grade
    sum <- sum + grade;
    n <- n + 1;
let avg = (float sum) / (float n)
printfn "Average grade: %g" avg</pre>
```

```
Course: Introduction to programming, Grade: 95
Course: Linear algebra, Grade: 80
Course: User Interaction, Grade: 85
Average grade: 86.6667
```

Listing 8.1: flowForLists.fsx -

This to be preferred, since we completely can ignore list boundary conditions and hence avoid out of range indexing. For comparison see a recursive implementation of the same,

```
let courseGrades =
    ["Introduction to programming", 95;
    "Linear algebra", 80;
    "User Interaction", 85;]

let rec printAndSum lst =
    match lst with
    | (title, grade)::rest ->
        printfn "Course: %s, Grade: %d" title grade
        let (sum, n) = printAndSum rest
        (sum + grade, n + 1)
        | _ -> (0, 0)

let (sum, n) = printAndSum courseGrades
let avg = (float sum) / (float n)
printfn "Average grade: %g" avg
```

```
Course: Introduction to programming, Grade: 95
Course: Linear algebra, Grade: 80
Course: User Interaction, Grade: 85
Average grade: 86.6667
```

Listing 8.2: flowForListsRecursive.fsx -

Note how this implementation avoids the use of variables in contrast to the previous examples.

8.1 Tuples

1

8.2 Lists

8.3 Arrays

8.3.1 1 dimensional arrays

Roughly speaking, arrays are mutable lists, and may be created and indexed in the same manner, e.g.,

```
let A = [| 1; 2; 3; 4; 5 |]
let B = [| 1 .. 5 |]
let C = [| for a in 1 ..5 do yield a |]

let printArray (a : int array) =
  for i = 0 to a.Length - 1 do
    printf "%d " a.[i]
  printArray A
  printArray B
  printArray C
```

```
1 2 3 4 5
1 2 3 4 5
1 2 3 4 5
```

Listing 8.3: arrayCreation.fsx -

Notice that as for lists, arrays are indexed starting with 0, and that in this particular case it was necessary to specify the type of the argument for printArray as an array of integers with the array keyword. The array keyword is synonymous with '[]'. Arrays do not support pattern matching, cannot be resized, but are mutable,

```
let A = [| 1; 2; 3; 4; 5 |]

let printArray (a : int array) =
  for i = 0 to a.Length - 1 do
    printf "%d " a.[i]
  printf "\n"

let square (a : int array) =
  for i = 0 to a.Length - 1 do
    a.[i] <- a.[i] * a.[i]</pre>
```

¹remember fst and snd Spec-4.0 Section 18.2.7

```
printArray A
square A
printArray A
```

```
1 2 3 4 5
1 4 9 16 25
```

Listing 8.4: arrayReassign.fsx -

Notice that in spite the missing mutable keyword, the function square still had the side-effect of squaring alle entries in A. Arrays support *slicing*, that is, indexing an array with a range results in a copy of array with values corresponding to the range, e.g.,

· slicing

```
let A = [| 1; 2; 3; 4; 5 |]
let B = A.[1..3]
let C = A.[..2]
let D = A.[3..]
let E = A.[*]

let printArray (a : int array) =
  for i = 0 to a.Length - 1 do
    printf "%d " a.[i]
  printArray A
printArray A
printArray B
printArray C
printArray D
printArray E
```

```
1 2 3 4 5
2 3 4
1 2 3
4 5
1 2 3 4 5
```

Listing 8.5: arraySlicing.fsx -

As illustrated, the missing start or end index implies from the first or to the last element. There are quite a number of built-in procedures for all arrays some of which we summarize in Table 8.1. Thus, the arrayReassign.fsx program can be written using arrays as,

```
let A = [| 1 .. 5 |]

let printArray (a : int array) =
    Array.iter (fun x -> printf "%d " x) a
    printf "\n"

let square a = a * a

printArray A
let B = Array.map square A
printArray A
printArray B
```

```
1 2 3 4 5
1 2 3 4 5
1 4 9 16 25
```

append	Creates an array that contains the elements of one array followed by the elements of
	another array.
average	Returns the average of the elements in an array.
blit	Reads a range of elements from one array and writes them into another.
choose	Applies a supplied function to each element of an array. Returns an array that contains the results x for each element for which the function returns $\mathrm{Some}(x)$.
collect	Applies the supplied function to each element of an array, concatenates the results, and returns the combined array.
concat	Creates an array that contains the elements of each of the supplied sequence of arrays.
copy	Creates an array that contains the elements of the supplied array.
create	Creates an array whose elements are all initially the supplied value.
empty	Returns an empty array of the given type.
exists	Tests whether any element of an array satisfies the supplied predicate.
fill	Fills a range of elements of an array with the supplied value.
filter	Returns a collection that contains only the elements of the supplied array for which the supplied condition returns true.
find	Returns the first element for which the supplied function returns true. Raises System.Collections.Generic.KeyNotFoundException if no such element exists.
findIndex	Returns the index of the first element in an array that satisfies the supplied condition. Raises System.Collections.Generic.KeyNotFoundException if none of the elements satisfy the condition.
fold	Applies a function to each element of an array, threading an accumulator argument through the computation. If the input function is f and the array elements are i0iN,
	this function computes f ((f s i0)) iN.
foldBack	Applies a function to each element of an array, threading an accumulator argument through the computation. If the input function is f and the array elements are i0iN, this function computes f i0 ((f iN s)).
forall	Tests whether all elements of an array satisfy the supplied condition.
isEmpty	Tests whether an array has any elements.
iter	Applies the supplied function to each element of an array.
init	
length	Returns the length of an array. The System.Array.Length property does the same thing.
map	Creates an array whose elements are the results of applying the supplied function to each of the elements of a supplied array.
mapi	
max	Returns the largest of all elements of an array. Operators.max is used to compare the elements.
min	Returns the smallest of all elements of an array. Operators.min is used to compare the elements.
ofList	Creates an array from the supplied list.
ofSeq	Creates an array from the supplied enumerable object.
partition	Splits an array into two arrays, one containing the elements for which the supplied condition returns true, and the other containing those for which it returns false.
rev	Reverses the order of the elements in a supplied array.
sort	Sorts the elements of an array and returns a new array. Operators.compare is used to
1	compare the elements.
sub	Creates an array that contains the sup <pli>plied subrange, which is specified by starting index and length.</pli>
sum	Returns the sum of the elements in the array.
toList	Converts the supplied array to a list.
toSeq	Views the supplied array as a sequence.
unzip	Splits an array of tuple pairs into a tuple of two arrays.
zeroCreate	Creates an array whose elements are all initially zero.
zip	Combines two arrays into an array of tuples that have two elements. The two arrays must have equal lengths; otherwise, System.ArgumentException is raised.

Listing 8.6: arrayReassignModule.fsx -

and the flowForListsIndex.fsx program can be written using arrays as,

```
let courseGrades =
    ["Introduction to programming", 95;
    "Linear algebra", 80;
    "User Interaction", 85;]

let A = Array.ofList courseGrades
let printCourseNGrade (title, grade) =
    printfn "Course: %s, Grade: %d" title grade
Array.iter printCourseNGrade A
let (titles,grades) = Array.unzip A
let avg = (float (Array.sum grades)) / (float grades.Length)
printfn "Average grade: %g" avg
```

```
Course: Introduction to programming, Grade: 95
Course: Linear algebra, Grade: 80
Course: User Interaction, Grade: 85
Average grade: 86.6667
```

Listing 8.7: flowForListsIndexModule.fsx -

Both cases avoid the use of variables and side-effects which is a big advantage for code safety.

8.3.2 Multidimensional Arrays

Higher dimensional arrays can be created as arrays of arrays (of arrays \dots). These are known as jagged arrays, since there is no inherent control of that all sub-arrays are of similar size. E.g., the following is a jagged array of increasing width,

· jagged arrays

```
let A = [| for n in 1..3 do yield [| 1 .. n |] |]

let printArrayOfArrays (a : int array array) =
  for i = 0 to a.Length - 1 do
    for j = 0 to a.[i].Length - 1 do
        printf "%d " a.[i].[j]
        printf "\n"

printArrayOfArrays A
```

```
1
1 2
1 2 3
```

Listing 8.8: arrayJagged.fsx -

Indexing arrays of arrays is done sequentially, in the sense that in the above example, the number of outer arrays is a.Length, a.[i] is the i'th array, the length of the i'th array is a.[i].Length, and the j'th element of the i'th array is thus a.[i].[j]. Often 2 dimensional square arrays are used, which can be implemented as a jagged array as,

```
let pownArray (a : int array) p =
  for i = 0 to a.Length - 1 do
    a.[i] <- pown a.[i] p
  a</pre>
```

```
let A = [| for n in 1..3 do yield (pownArray [| 1 .. 4 |] n ) |]

let printArrayOfArrays (a : int array array) =
  for i = 0 to a.Length - 1 do
    for j = 0 to a.[i].Length - 1 do
       printf "%2d " a.[i].[j]
    printf "\n"

printArrayOfArrays A
```

```
1 2 3 4
1 4 9 16
1 8 27 64
```

Listing 8.9: arrayJaggedSquare.fsx -

In fact, square arrays of dimensions 2 to 4 are so common that fsharp has built-in modules for their support. In the following describe Array2D. The workings of Array3D and Array4D are very similar. An example of creating the same 2 dimensional array as above but as an Array2D is,

```
let A = Array2D.create 3 4 0
for i = 0 to (Array2D.length1 A) - 1 do
    for j = 0 to (Array2D.length2 A) - 1 do
        A.[i,j] <- pown (j + 1) (i + 1)

let printArray2D (a : int [,]) =
    for i = 0 to (Array2D.length1 a) - 1 do
        for j = 0 to (Array2D.length2 a) - 1 do
        printf "%2d " a.[i, j]
        printf "\n"

printArray2D A</pre>
```

```
1 2 3 4
1 4 9 16
1 8 27 64
```

Listing 8.10: array2D.fsx -

Notice that the indexing uses a slightly different notation '[,]' and the length functions are also slightly different. The statement A.Length would return the total number of elements in the array, in this case 12.

There are a bit few built-in procedures for 2 dimensional array types, some of which are summarized in Table 8.2

8.4 Sequences

²note that A.[1,*] is a Array but A.[1..1,*] is an Array2D.

blit	Reads a range of elements from one array and writes them into another.	
copy	Creates an array that contains the elements of the supplied array.	
create	Creates an array whose elements are all initially the supplied value.	
iter	Applies the supplied function to each element of an array.	
length1	Returns the length of an array in the first dimension.	
length2	Returns the length of an array in the second dimension.	
map	Creates an array whose elements are the results of applying the supplied function to	
	each of the elements of a supplied array.	
mapi		
zeroCreate	Creates an array whose elements are all initially zero.	

 $\label{thm:condition} Table~8.2:~Some~built-in~procedures~in~the~Array2D~module~for~arrays~(from~https://msdn.microsoft.com/en-us/visualfsharpdocs/conceptual/fsharp-core-library-reference)$

Part II Imperative programming

Exceptions

9.1 Exception Handling

Exception handling allows programmers to catch and handle errors whenever an application enters an invalid state.

Remember

- $\bullet\,$ ex
n type Spec-4.0 Chapter 18.1
- $\bullet~{\rm Spec\text{-}}4.0~{\rm Section}~18.2.8$

. . .

Testing programs

. . .

Input/Output

1

Reading and writing to files and the console window.

11.1 Console I/O

. . .

11.2 File I/O

```
let getAFileName () =
  let mutable filename = Unchecked.defaultof<string>
  let mutable fileExists = false
  while not(fileExists) do
    System.Console.Write("Enter Filename: ")
    filename <- System.Console.ReadLine()
    fileExists <- System.IO.File.Exists filename
  filename

let listOfFiles = System.IO.Directory.GetFiles(".")
printfn "Directory contains: %A" listOfFiles
let filename = getAFileName ()
printfn "You typed: %s" filename</pre>
```

```
let rec printFile (reader : System.IO.StreamReader) =
  if not(reader.EndOfStream) then
    let line = reader.ReadLine ()
    printfn "%s" line
    printFile reader

let filename = "readFile.fsx"
let reader = System.IO.File.OpenText filename
printFile reader
```

```
let rec printFile (reader : System.IO.StreamReader) =
  if not(reader.EndOfStream) then
   let line = reader.ReadLine ()
   printfn "%s" line
   printFile reader
```

¹Spec-4.0 Section 18.2.9

```
let filename = "readFile.fsx"
let reader = System.IO.File.OpenText filename
printFile reader
```

Listing 11.1: readFile.fsx -

```
let rec readFile (stream : System.IO.StreamReader) =
  if not(stream.EndOfStream) then
    (stream.ReadLine ()) :: (readFile stream)
  else
    []
let rec writeFile (stream : System.IO.StreamWriter) text =
 match text with
  | (1 : string) :: ls ->
   stream.WriteLine 1
   writeFile stream ls
 | _ -> ()
let reverseString (s : string) =
  System.String(Array.rev (s.ToCharArray()))
let inputStream = System.IO.File.OpenText "reverseFile.fsx"
let text = readFile inputStream
let reverseText = List.map reverseString (List.rev text)
let outputStream = System.IO.File.CreateText "xsf.eliFesrever"
writeFile outputStream reverseText
outputStream.Close ()
printfn "%A" reverseText
```

```
["txeTesrever "A%" nftnirp"; ")( esolC.maertStuptuo";
"txeTesrever maertStuptuo eliFetirw";
""reverseFile.fsx" txeTetaerC.eliF.OI.metsyS = maertStuptuo tel";
")txet ver.tsiL( gnirtSesrever pam.tsiL = txeTesrever tel";
"maertStupni eliFdaer = txet tel";
""xsf.eliFesrever" txeTnepO.eliF.OI.metsyS = maertStupni tel"; "";
")))(yarrArahCoT.s( ver.yarrA(gnirtS.metsyS ";
"= )gnirts : s( gnirtSesrever tel"; ""; ")( >- _ | ";
"sl maerts eliFetirw "; "l eniLetirW.maerts ";
">- sl :: )gnirts : l( | "; "htiw txet hctam ";
"= txet )retirWmaertS.OI.metsyS : maerts( eliFetirw cer tel"; ""; "][ ";
"esle "; ")maerts eliFdaer( :: ))( eniLdaeR.maerts( ";
"neht )maertSfOdnE.maerts(ton fi ";
"= )redaeRmaertS.OI.metsyS : maerts( eliFdaer cer tel"]
```

Listing 11.2: reverseFile.fsx -

Graphical User Interfaces

. . .

The Collection

13.1 System.String

The list of built-in methods accessible with the dot notation is defined in System.String class and is long. Here follows short descriptions of some useful methods:

Compare (String, String) Compares two specified String objects and returns an integer that indicates their relative position in the sort order.

CompareOrdinal(String, String) Compares two specified String objects by evaluating the numeric values of the corresponding Char objects in each string.

CompareOrdinal (String, Int32, String, Int32, Int32) Compares substrings of two specified String objects by evaluating the numeric values of the corresponding Char objects in each substring.

CompareTo(Object) Compares this instance with a specified Object and indicates whether this instance precedes, follows, or appears in the same position in the sort order as the specified Object.

CompareTo(String) Compares this instance with a specified String object and indicates whether this instance precedes, follows, or appears in the same position in the sort order as the specified String.

Concat(Object) Creates the string representation of a specified object.

Concat(Object[]) Concatenates the string representations of the elements in a specified Object array.

Concat(IEnumerable(String)) Concatenates the members of a constructed IEnumerable(T) collection of type String.

Concat(String[]) Concatenates the elements of a specified String array.

Concat(Object, Object) Concatenates the string representations of two specified objects.

Concat (String, String) Concatenates two specified instances of String.

Concat(Object, Object, Object) Concatenates the string representations of three specified objects.

Concat(String, String, String) Concatenates three specified instances of String.

Concat(Object, Object, Object, Object) Concatenates the string representations of four specified objects and any objects specified in an optional variable length parameter list.

Concat(String, String, String, String) Concatenates four specified instances of String.

Concat(T)(IEnumerable(T)) Concatenates the members of an IEnumerable(T) implementation.

- Contains Returns a value indicating whether the specified String object occurs within this string.
- Copy Creates a new instance of String with the same value as a specified String.
- CopyTo Copies a specified number of characters from a specified position in this instance to a specified position in an array of Unicode characters.
- EndsWith(String) Determines whether the end of this string instance matches the specified string.
- EndsWith(String, StringComparison) Determines whether the end of this string instance matches the specified string when compared using the specified comparison option.
- EndsWith(String, Boolean, CultureInfo) Determines whether the end of this string instance matches the specified string when compared using the specified culture.
- Equals (Object) Determines whether this instance and a specified object, which must also be a String object, have the same value. (Overrides Object.Equals(Object).)
- Equals (String) Determines whether this instance and another specified String object have the same value.
- Equals (String, String) Determines whether two specified String objects have the same value.
- Equals (String, StringComparison) Determines whether this string and a specified String object have the same value. A parameter specifies the culture, case, and sort rules used in the comparison.
- Equals (String, String, StringComparison) Determines whether two specified String objects have the same value. A parameter specifies the culture, case, and sort rules used in the comparison.
- Finalize Allows an object to try to free resources and perform other cleanup operations before it is reclaimed by garbage collection. (Inherited from Object.)
- Format(String, Object) Replaces one or more format items in a specified string with the string representation of a specified object.
- Format(String, Object[]) Replaces the format item in a specified string with the string representation of a corresponding object in a specified array.
- Format(IFormatProvider, String, Object[]) Replaces the format item in a specified string with the string representation of a corresponding object in a specified array. A specified parameter supplies culture-specific formatting information.
- Format(String, Object, Object) Replaces the format items in a specified string with the string representation of two specified objects.
- Format(String, Object, Object, Object) Replaces the format items in a specified string with the string representation of three specified objects.
- GetEnumerator Retrieves an object that can iterate through the individual characters in this string.
- GetHashCode Returns the hash code for this string. (Overrides Object.GetHashCode().)
- GetType Gets the Type of the current instance. (Inherited from Object.)
- GetTypeCode Returns the TypeCode for class String.
- IndexOf (Char) Reports the zero-based index of the first occurrence of the specified Unicode character in this string.
- IndexOf (String) Reports the zero-based index of the first occurrence of the specified string in this instance.

- IndexOf (Char, Int32) Reports the zero-based index of the first occurrence of the specified Unicode character in this string. The search starts at a specified character position.
- IndexOf(String, Int32) Reports the zero-based index of the first occurrence of the specified string in this instance. The search starts at a specified character position.
- IndexOf(String, StringComparison) Reports the zero-based index of the first occurrence of the specified string in the current String object. A parameter specifies the type of search to use for the specified string.
- IndexOf (Char, Int32, Int32) Reports the zero-based index of the first occurrence of the specified character in this instance. The search starts at a specified character position and examines a specified number of character positions.
- IndexOf (String, Int32, Int32) Reports the zero-based index of the first occurrence of the specified string in this instance. The search starts at a specified character position and examines a specified number of character positions.
- IndexOf(String, Int32, StringComparison) Reports the zero-based index of the first occurrence of the specified string in the current String object. Parameters specify the starting search position in the current string and the type of search to use for the specified string.
- IndexOf(String, Int32, Int32, StringComparison) Reports the zero-based index of the first occurrence of the specified string in the current String object. Parameters specify the starting search position in the current string, the number of characters in the current string to search, and the type of search to use for the specified string.
- IndexOfAny(Char[]) Reports the zero-based index of the first occurrence in this instance of any character in a specified array of Unicode characters.
- IndexOfAny(Char[], Int32) Reports the zero-based index of the first occurrence in this instance of any character in a specified array of Unicode characters. The search starts at a specified character position.
- IndexOfAny(Char[], Int32, Int32) Reports the zero-based index of the first occurrence in this instance of any character in a specified array of Unicode characters. The search starts at a specified character position and examines a specified number of character positions.
- Insert Returns a new string in which a specified string is inserted at a specified index position in this instance.
- Intern Retrieves the system's reference to the specified String.
- IsInterned Retrieves a reference to a specified String.
- IsNormalized() Indicates whether this string is in Unicode normalization form C.
- IsNormalized(NormalizationForm) Indicates whether this string is in the specified Unicode normalization form.
- IsNullOrEmpty Indicates whether the specified string is a null reference (Nothing in Visual Basic) or an Empty string.
- IsNullOrWhiteSpace Indicates whether a specified string is a null reference (Nothing in Visual Basic), empty, or consists only of whitespace characters.
- Join(String, IEnumerable(String)) Concatenates the members of a constructed IEnumerable(T) collection of type String, using the specified separator between each member.
- Join(String, Object[]) Concatenates the elements of an object array, using the specified separator between each element.

- Join(String, String[]) Concatenates all the elements of a string array, using the specified separator between each element.
- Join(String, String[], Int32, Int32) Concatenates the specified elements of a string array, using the specified separator between each element.
- Join(T)(String, IEnumerable(T)) Concatenates the members of a collection, using the specified separator between each member.
- LastIndexOf (Char) Reports the zero-based index position of the last occurrence of a specified Unicode character within this instance.
- LastIndexOf(String) Reports the zero-based index position of the last occurrence of a specified string within this instance.
- LastIndexOf (Char, Int32) Reports the zero-based index position of the last occurrence of a specified Unicode character within this instance. The search starts at a specified character position.
- LastIndexOf (String, Int32) Reports the zero-based index position of the last occurrence of a specified string within this instance. The search starts at a specified character position.
- LastIndexOf(String, StringComparison) Reports the zero-based index of the last occurrence of a specified string within the current String object. A parameter specifies the type of search to use for the specified string.
- LastIndexOf (Char, Int32, Int32) Reports the zero-based index position of the last occurrence of the specified Unicode character in a substring within this instance. The search starts at a specified character position and examines a specified number of character positions.
- LastIndexOf(String, Int32, Int32) Reports the zero-based index position of the last occurrence of a specified string within this instance. The search starts at a specified character position and examines a specified number of character positions.
- LastIndexOf(String, Int32, StringComparison) Reports the zero-based index of the last occurrence of a specified string within the current String object. Parameters specify the starting search position in the current string, and type of search to use for the specified string.
- LastIndexOf(String, Int32, Int32, StringComparison) Reports the zero-based index position of the last occurrence of a specified string within this instance. Parameters specify the starting search position in the current string, the number of characters in the current string to search, and the type of search to use for the specified string.
- LastIndexOfAny(Char[]) Reports the zero-based index position of the last occurrence in this instance of one or more characters specified in a Unicode array.
- LastIndexOfAny(Char[], Int32) Reports the zero-based index position of the last occurrence in this instance of one or more characters specified in a Unicode array. The search starts at a specified character position.
- LastIndexOfAny(Char[], Int32, Int32) Reports the zero-based index position of the last occurrence in this instance of one or more characters specified in a Unicode array. The search starts at a specified character position and examines a specified number of character positions.
- MemberwiseClone Creates a shallow copy of the current Object. (Inherited from Object.)
- Normalize() Returns a new string whose textual value is the same as this string, but whose binary representation is in Unicode normalization form C.
- Normalize(NormalizationForm) Returns a new string whose textual value is the same as this string, but whose binary representation is in the specified Unicode normalization form.

- PadLeft(Int32) Returns a new string that right-aligns the characters in this instance by padding them with spaces on the left, for a specified total length.
- PadLeft(Int32, Char) Returns a new string that right-aligns the characters in this instance by padding them on the left with a specified Unicode character, for a specified total length.
- PadRight(Int32) Returns a new string that left-aligns the characters in this string by padding them with spaces on the right, for a specified total length.
- PadRight(Int32, Char) Returns a new string that left-aligns the characters in this string by padding them on the right with a specified Unicode character, for a specified total length.
- Remove(Int32) Returns a new string in which all the characters in the current instance, beginning at a specified position and continuing through the last position, have been deleted.
- Remove(Int32, Int32) Returns a new string in which a specified number of characters in this instance beginning at a specified position have been deleted.
- Replace (Char, Char) Returns a new string in which all occurrences of a specified Unicode character in this instance are replaced with another specified Unicode character.
- Replace(String, String) Returns a new string in which all occurrences of a specified string in the current instance are replaced with another specified string.
- Split(Char[]) Returns a string array that contains the substrings in this instance that are delimited by elements of a specified Unicode character array.
- Split(Char[], Int32) Returns a string array that contains the substrings in this instance that are delimited by elements of a specified Unicode character array. A parameter specifies the maximum number of substrings to return.
- Split(Char[], StringSplitOptions) Returns a string array that contains the substrings in this string that are delimited by elements of a specified Unicode character array. A parameter specifies whether to return empty array elements.
- Split(String[], StringSplitOptions) Returns a string array that contains the substrings in this string that are delimited by elements of a specified string array. A parameter specifies whether to return empty array elements.
- Split(Char[], Int32, StringSplitOptions) Returns a string array that contains the substrings in this string that are delimited by elements of a specified Unicode character array. Parameters specify the maximum number of substrings to return and whether to return empty array elements.
- Split(String[], Int32, StringSplitOptions) Returns a string array that contains the substrings in this string that are delimited by elements of a specified string array. Parameters specify the maximum number of substrings to return and whether to return empty array elements.
- StartsWith(String) Determines whether the beginning of this string instance matches the specified string.
- StartsWith(String, StringComparison) Determines whether the beginning of this string instance matches the specified string when compared using the specified comparison option.
- StartsWith(String, Boolean, CultureInfo) Determines whether the beginning of this string instance matches the specified string when compared using the specified culture.
- Substring(Int32) Retrieves a substring from this instance. The substring starts at a specified character position.
- Substring(Int32, Int32) Retrieves a substring from this instance. The substring starts at a specified character position and has a specified length.

ToCharArray() Copies the characters in this instance to a Unicode character array.

ToCharArray(Int32, Int32) Copies the characters in a specified substring in this instance to a Unicode character array.

ToLower() Returns a copy of this string converted to lowercase.

ToLower(CultureInfo) Returns a copy of this string converted to lowercase, using the casing rules of the specified culture.

ToLowerInvariant Returns a copy of this String object converted to lowercase using the casing rules of the invariant culture.

ToString() Returns this instance of String; no actual conversion is performed. (Overrides Object.ToString().)

ToString(IFormatProvider) Returns this instance of String; no actual conversion is performed.

ToUpper() Returns a copy of this string converted to uppercase.

ToUpper(CultureInfo) Returns a copy of this string converted to uppercase, using the casing rules of the specified culture.

ToUpperInvariant Returns a copy of this String object converted to uppercase using the casing rules of the invariant culture.

Trim() Removes all leading and trailing whitespace characters from the current String object.

Trim(Char[]) Removes all leading and trailing occurrences of a set of characters specified in an array from the current String object.

TrimEnd Removes all trailing occurrences of a set of characters specified in an array from the current String object.

TrimStart Removes all leading occurrences of a set of characters specified in an array from the current String object.

13.2 Mutable Collections

System.Collections.Generic

13.2.1 Mutable lists

List, LinkedList

13.2.2 Stacks

Stack

13.2.3 Queues

Queue

13.2.4 Sets and dictionaries

HashSet, and Dictionary from

Imperative programming

14.1 Introduction

Imperativ programming focusses on how a problem is to be solved as a list of statements and and a set of states, where states may change over time. An example is a baking recipe, e.g.,

- · Imperativ programming
- \cdot statements
- \cdot states

- 1. Mix yeast with water
- 2. Stir in salt, oil, and flour
- 3. Knead until the dough has a smooth surface
- 4. Let the dough rise until it has double size
- 5. Shape dough into a loaf
- 6. Let the loaf rise until double size
- 7. Bake in oven until the bread is golden brown

Each line in this example consists of one or more statements that are to be executed, and while executing them states such as size of the dough, color of the bread changes, and some execution will halt execution until certain conditions of these states are fulfilled, e.g., the bread will not be put into the oven for baking before it has risen sufficiently.

Statements may be grouped into procedures, and structuring imperative programs heavily into procedures is called *Procedural programming*, which is sometimes considered as a separate paradigm from imperative programming. *Object oriented programming* is an extension of imperative programming, where statements and states are grouped into classes and will be treated elsewhere.

Almost all computer hardware is designed for *machine code*, which is a common term used for many low-level computer programming language, and almost all machine langues follow the imperative programming paradigm.

Functional programming may be considered a subset of imperative programming, in the sense that functional programming does not include the concept of a state, or one may think of functional programming as only have one unchanging state. Functional programming has also a bigger focus on what should be solved, by declaring rules but not explicitly listing statements describing how these rules should be combined and executed in order to solve a given problem. Functional programming will be treated elsewhere.

- · Procedural programming
- · Object oriented programming
- \cdot machine code
- · Functional programming

14.2 Generating random texts

14.2.1 0'th order statistics

```
let histToCumulativeProbability hist =
  let appendSum (acc : float array) (elem : int) =
    let sum =
      if acc.Length = 0 then
        float elem
        acc.[acc.Length-1] + (float elem)
    Array.append acc [| sum |]
  let normalizeProbability k v = v/k
  let cumSum = Array.fold appendSum Array.empty<float> hist
  if cumSum.[cumSum.Length - 1] > 0.0 then
    Array.map (normalizeProbability cumSum.[cumSum.Length - 1]) cumSum
  else
    Array.create cumSum.Length (1.0 / (float cumSum.Length))
let lookup (hist : float array) (v : float) =
  Array.findIndex (fun h -> h > v) hist
let countEqual A v =
  Array.fold (fun acc elem -> if elem = v then acc+1 else acc) 0 A
let intToIdx i = i - (int ' ')
let idxToInt i = i + (int ' ')
let legalIndex size idx =
  (0 \le idx) \&\& (idx \le size - 1)
let analyzeFile (reader : System.IO.StreamReader) size pushForward =
  let hist = Array.create size 0
  let mutable c = Unchecked.defaultof <int>
  while not(reader.EndOfStream) do
    c <- pushForward (reader.Read ())</pre>
    if legalIndex size c then
      hist.[c] <- hist.[c] + 1
  hist
let sampleFromCumulativeProbability cumulative noSamples =
 let rnd = System.Random ()
  let rndArray = Array.init noSamples (fun _ -> rnd.NextDouble ())
  Array.map (lookup cumulative) rndArray
let filename = "randomTextOrderO.fsx"
let noSamples = 200
let histSize = 126 - 32 + 1
let reader = System.IO.File.OpenText filename
let hist = analyzeFile reader histSize intToIdx
reader.Close ()
let idxValue = Array.mapi (fun i v -> (idxToInt i, v)) hist
printfn "%A" idxValue
printfn "%d zeros out of %d elements" (countEqual hist 0) hist.Length
let cumulative = histToCumulativeProbability hist
let rndIdx = sampleFromCumulativeProbability cumulative noSamples
let rndInt = Array.map idxToInt rndIdx
let rndChar = Array.map (fun v -> char v) rndInt
```

```
let text = System.String.Concat rndChar // System.String is not the same as
    String !!!
printfn "%A" text
```

```
[|(32, 339); (33, 3); (34, 8); (35, 0); (36, 0); (37, 4); (38, 2); (39, 4);
  (40, 27); (41, 27); (42, 0); (43, 5); (44, 1); (45, 13); (46, 42); (47, 4);
  (48, 11); (49, 9); (50, 3); (51, 1); (52, 0); (53, 0); (54, 1); (55, 0);
  (56, 0); (57, 0); (58, 5); (59, 0); (60, 6); (61, 31); (62, 9); (63, 0);
  (64, 0); (65, 19); (66, 0); (67, 8); (68, 1); (69, 3); (70, 7); (71, 0);
  (72, 0); (73, 14); (74, 0); (75, 0); (76, 7); (77, 0); (78, 1); (79, 5);
  (80, 6); (81, 0); (82, 3); (83, 26); (84, 9); (85, 1); (86, 2); (87, 0);
  (88, 0); (89, 0); (90, 0); (91, 6); (92, 0); (93, 6); (94, 0); (95, 1);
 (96, 0); (97, 100); (98, 14); (99, 41); (100, 50); (101, 143); (102, 29);
 (103, 12); (104, 38); (105, 87); (106, 0); (107, 5); (108, 89); (109, 63);
 (110, 75); (111, 50); (112, 26); (113, 2); (114, 88); (115, 47); (116, 121);
 (117, 55); (118, 18); (119, 3); (120, 21); (121, 31); (122, 12); (123, 0);
  (124, 2); (125, 0); (126, 0)|]
29 zeros out of 95 elements
"ym1e m )i lsauy cat.a o) eNtalmtucalu. haet giitCi1e ifeI mgrE"euubehce tl
   is datcira rattTueep ac(i( Ft ldful0fCl]na o il elatx.atr)p nl=earu1 a.
   \verb"rcVySce" elpid1hhn.an t.ymr.p.maz ahdi1 cT Aeu r:r."
```

Listing 14.1: randomTextOrder0.fsx -

14.2.2 1'th order statistics

```
let histToCumulativeProbability hist =
  let appendSum (acc : float array) (elem : int) =
    let sum =
      if acc.Length = 0 then
        float elem
        acc.[acc.Length-1] + (float elem)
    Array.append acc [| sum |]
  let normalizeProbability k v = v/k
  let cumSum = Array.fold appendSum Array.empty<float> hist
  if cumSum.[cumSum.Length - 1] > 0.0 then
    Array.map (normalizeProbability cumSum.[cumSum.Length - 1]) cumSum
  else
    Array.create cumSum.Length (1.0 / (float cumSum.Length))
let lookup (hist : float array) (v : float) =
  Array.findIndex (fun h -> h > v) hist
let countEqual A v =
 Array.fold (fun acc elem -> if elem = v then acc+1 else acc) 0 A
let intToIdx i = i - (int ' ')
let idxToInt i = i + (int ' ')
let legalIndex size idx =
  (0 \le idx) && (idx \le size - 1)
let analyzeFile (reader : System.IO.StreamReader) size pushForward =
let hist = Array2D.create size size 0
```

```
let mutable c1 = Unchecked.defaultof <int>
  let mutable c2 = Unchecked.defaultof <int>
  let mutable nRead = 0
  while not(reader.EndOfStream) do
    c2 <- pushForward (reader.Read ())</pre>
    if legalIndex size c2 then
      nRead <- nRead + 1
      if nRead >= 2 then
        hist.[c1,c2] \leftarrow hist.[c1,c2] + 1
      c1 <- c2;
  hist
let Array2DToArray (arr : 'T [,]) = arr |> Seq.cast<'T> |> Seq.toArray
let Array2DOfArray (a : 'T []) = Array2D.init 1 a.Length (fun i j -> a.[j])
let hist2DToCumulativeProbability hist =
  let rows = Array2D.length1 hist
  let cols = Array2D.length2 hist
  let cumulative = Array2D.zeroCreate<float> rows cols
  for i = 0 to rows - 1 do
    let histi = Array2D0fArray (histToCumulativeProbability hist.[i,*])
    Array2D.blit histi 0 0 cumulative i 0 1 cols
  cumulative
let marginal (hist : int [,]) =
  let rows = Array2D.length1 hist
  let sum = Array.zeroCreate rows
  for i = 0 to rows - 1 do
    sum.[i] <- Array.sum hist.[i,*]</pre>
let sampleFromCumulativeProbability (cumulative : float [,]) (margCumulative :
    float array) noSamples =
  let rnd = System.Random ()
  let samples = Array.zeroCreate < int > noSamples
  let mutable v = rnd.NextDouble ()
  let mutable i = Unchecked.defaultof <int>
  samples.[0] <- lookup margCumulative v
  for n = 1 to noSamples - 1 do
    v <- rnd.NextDouble ()
    i <- samples.[n - 1]
    samples.[n] <- lookup cumulative.[n, *] v</pre>
  samples
let filename = "randomTextOrder0.fsx"
let noSamples = 200
let histSize = 126 - 32 + 1
let reader = System.IO.File.OpenText filename
let hist = analyzeFile reader histSize intToIdx
reader.Close ()
let idxValue = Array2D.mapi (fun i j v -> (idxToInt i, idxToInt j, v)) hist
printfn "%A" (Array2DToArray idxValue)
printfn "%d zeros out of %d elements" (countEqual (Array2DToArray hist) 0)
   hist.Length
let margHist = marginal hist;
let margCumulative = histToCumulativeProbability margHist
let cumulative = hist2DToCumulativeProbability hist
```

```
(*
let rndIdx = sampleFromCumulativeProbability cumulative margCumulative
    noSamples
let rndInt = Array.map idxToInt rndIdx
let rndChar = Array.map (fun v -> char v) rndInt
let text = System.String.Concat rndChar // System.String is not the same as
    String !!!
printfn "%A" text
*)
```

```
[|(32, 32, 63); (32, 33, 1); (32, 34, 4); (32, 35, 0); (32, 36, 0); (32, 37, 34, 4); (32, 35, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 0); (32, 36, 
     (32, 38, 1); (32, 39, 4); (32, 40, 26); (32, 41, 0); (32, 42, 0); (32, 43,
     (32, 44, 0); (32, 45, 10); (32, 46, 0); (32, 47, 2); (32, 48, 5); (32, 49,
     (32, 50, 1); (32, 51, 1); (32, 52, 0); (32, 53, 0); (32, 54, 0); (32, 55, 0)
     (32, 56, 0); (32, 57, 0); (32, 58, 5); (32, 59, 0); (32, 60, 4); (32, 61,
             29);
     (32, 62, 2); (32, 63, 0); (32, 64, 0); (32, 65, 15); (32, 66, 0); (32, 67,
     (32, 68, 0); (32, 69, 0); (32, 70, 0); (32, 71, 0); (32, 72, 0); (32, 73, 0)
     (32, 74, 0); (32, 75, 0); (32, 76, 0); (32, 77, 0); (32, 78, 0); (32, 79, 0)
     (32, 80, 0); (32, 81, 0); (32, 82, 0); (32, 83, 6); (32, 84, 0); (32, 85, 1)
     (32, 86, 0); (32, 87, 0); (32, 88, 0); (32, 89, 0); (32, 90, 0); (32, 91, 1)
     (32, 92, 0); (32, 93, 0); (32, 94, 0); (32, 95, 1); (32, 96, 0); (32, 97,
            13);
     (32, 98, 0); (32, 99, 15); (32, 100, 1); (32, 101, 8); (32, 102, 6);
     (32, 103, 0); (32, 104, 18); (32, 105, 20); (32, 106, 0); (32, 107, 1);
     (32, 108, 11); (32, 109, 1); (32, 110, 7); (32, 111, 2); (32, 112, 2);
    (32, 113, 0); (32, 114, 12); (32, 115, 10); (32, 116, 7); (32, 117, 0);
    (32, 118, 9); (32, 119, 1); (32, 120, 0); (32, 121, 0); (32, 122, 1);
    (32, 123, 0); (32, 124, 1); (32, 125, 0); (32, 126, 0); (33, 32, 0);
    (33, 33, 2); (33, 34, 0); (33, 35, 0); (33, 36, 0); ...|]
8640 zeros out of 9025 elements
```

Listing 14.2: randomTextOrder1.fsx -

Part III Declarative programming

Types and measures

15.1 Unit of Measure

F# allows for assigning unit of measure to the following types,

· unit of measure

sbyte, int, int16, int32, int64, single, float32, float, and decimal.

by using the syntax,

```
"[<Measure>] type" unit-name [ "=" unit-expr ]
```

and then use "<"unit-name ">" as suffix for literals. In Figure ?? E.g., defining unit of measure 'm' and 's', then we can make calculations like,

```
> [<Measure>] type m
- [<Measure>] type s
- let a = 3<m/s^2>
- let b = a * 10<s>
- let c = 4 * b;;

[<Measure>]
type m
[<Measure>]
type s
val a : int<m/s ^ 2> = 3
val b : int<m/s> = 30
val c : int<m/s> = 120
```

Listing 15.1: fsharpi, floating point and integer numbers may be assigned unit of measures.

However, if we mixup unit of measures under addition, then we get an error,

Listing 15.2: fsharpi, unit of measures adds an extra layer of types for syntax checking at compile time.

Unit of measures allow for *, /, and $^{-1}$ for multiplication, division and exponentiation. Values with units can be casted to *unit-less* values by casting, and back again by multiplication as,

 \cdot unit-less

```
> [<Measure>] type m
- let a = 2<m>
- let b = int a
- let c = b * 1<m>;;

[<Measure>]
type m
val a : int<m> = 2
val b : int = 2
val c : int<m> = 2
```

Listing 15.3: fsharpi, type casting unit of measures.

Compound symbols can be declared as,

```
> [<Measure>] type s
- [<Measure>] type m
- [<Measure>] type kg
- [<Measure>] type N = kg * m / s^2;;

[<Measure>]
type s
[<Measure>]
type m
[<Measure>]
type kg
[<Measure>]
type kg
[<Measure>]
type kg
[<Measure>]
type kg
```

Listing 15.4: fsharpi, aggregated unit of measures.

For fans of the metric system there is the International System of Units, and these are built-in in Microsoft.FSharp.Data.UnitSystems.SI.UnitSymbols and give in Table 15.1. Hence, using the predefined unit of seconds, we may write,

```
> let a = 10.0 < Microsoft.FSharp.Data.UnitSystems.SI.UnitSymbols.s>;;
val a : float < Data.UnitSystems.SI.UnitSymbols.s> = 10.0
```

Listing 15.5: fsharpi, SI unit of measures are built-in.

To make the use of these predefined symbols easier, we can import them into the present scope by the open keyword,

```
> open Microsoft.FSharp.Data.UnitSystems.SI.UnitSymbols;;
> let a = 10.0<s>;;
val a : float<s> = 10.0
```

Listing 15.6: fsharpi, simpler syntax by importing, but beware of namespace pollution.

The open keyword should be used with care, since now all the bindings in Microsoft.FSharp. Data.UnitSystems.SI.UnitSymbols have been imported into the present scope, and since we most likely do not know, which bindings have been used by the programmers of Microsoft.FSharp.Data. UnitSystems.SI.UnitSymbols, we do not know which identifiers to avoid, when using let statements. We have obtained, what is known as namespace pollution. Read more about namespaces in Part IV. Using unit of measures is advisable for calculations involving real-world values, since some semantical errors of arithmetic expressions may be discovered by checking the resulting unit of measure.

 \cdot namespace pollution

·open

¹Spec-4.0: this notation is inconsistent with ** for float exponentiation.

Unit	Description
A	Ampere, unit of electric current.
Bq	Becquerel, unit of radioactivity.
C	Coulomb, unit of electric charge, amount of electricity.
cd	Candela, unit of luminous intensity.
F	Farad, unit of capacitance.
Gy	Gray, unit of an absorbed dose of radiation.
H	Henry, unit of inductance.
Hz	Hertz, unit of frequency.
J	Joule, unit of energy, work, amount of heat.
K	Kelvin, unit of thermodynamic (absolute) temperature.
kat	Katal, unit of catalytic activity.
kg	Kilogram, unit of mass.
lm	Lumen, unit of luminous flux.
lx	Lux, unit of illuminance.
m	Metre, unit of length.
mol	Mole, unit of an amount of a substance.
N	Newton, unit of force.
ohm	Unitnames.o SI unit of electric resistance.
Pa	Pascal, unit of pressure, stress.
s	Second, unit of time.
S	Siemens, unit of electric conductance.
Sv	Sievert, unit of dose equivalent.
T	Tesla, unit of magnetic flux density.
V	Volt, unit of electric potential difference, electromotive force.
W	Watt, unit of power, radiant flux.
Wb	Weber, unit of magnetic flux.

Table 15.1: International System of Units.

Functional programming

Part IV Structured programming

Namespaces and Modules

Things to remember:

- difference between .fs and .fsx Spec-4.0 Chapter 12.1 and 12.3
- signature files and their usefulness

A script file consists of a sequence of module elements

· module elements

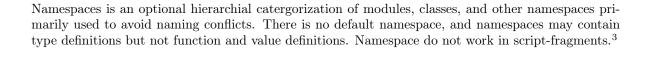
```
script-file = implementation-file
implementation-file =
  namespace-decl-groupList
  | named-module
  | anonynmous-module
namespace-decl-groupList = namespace-decl-group | namespace-decl-group namespace-
    decl-groupList
named-module = "module" long-ident module-elems
anonymous-module = module-elems
module-elems = module-elem | module-elem module-elems
namespace-decl-group = "namespace" long-ident module-elems | "namespace" global
   module-elems
module-elem =
  module-function-or-value-defn type-defns
  | exception-defn
  | module-defn
  | module-abbrev
  | import-decl compiler-directive-decl
```

F# source code units are made up of declarations grouped using namespaces, type definitions, and module definitions. A file may contain multipe namespaces each defining types and modules, these in turn may contain function and value definitions, which in turn contains expressions.

With no leading namespace or module declaration, then F# will immediately insert a module, where the name of the module is the same as the file name with capitalized first letter.²

¹Spec-4.0 Chapter 10.

²https://en.wikibooks.org/wiki/F_Sharp_Programming/Modules_and_Namespaces



 $^{^3 \}mathtt{https://fsharp} for fun and \mathtt{profit.com/posts/organizing-functions/}$

Object-oriented programming

Things to remember:

- upcast and downcast upcast, :>, downcast, :?>
- boxing (box 5):?> int;;, see Spec-4.0 chapter 18.2.6.
- obj type Spec-4.0 chapter 18.1
- \bullet boxing Spec-4.0 Section 18.2.6

$\begin{array}{c} {\rm Part~V} \\ {\rm Appendix} \end{array}$

Appendix A

Number systems on the computer

A.1 Binary numbers

Humans like to use the decimal number system for representing numbers. Decimal numbers are base 10 means that for a number consisting of a sequence of digits separated by a decimal point, where each digit can have values $d \in \{0, 1, 2, \dots, 9\}$ and the weight of each digit is proportional to its place in the sequence of digits w.r.t. the decimal point, i.e., the number $357.6 = 3 \cdot 10^2 + 5 \cdot 10^1 + 7 \cdot 10^0 + 6 \cdot 10^{-1}$ or in general:

- · decimal number
- \cdot base
- · decimal point
- · digit

$$v = \sum_{i=-m}^{n} d_i 10^i \tag{A.1}$$

The basic unit of information in almost all computers is the binary digit or *bit* for short. A *binary* number consists of a sequence of binary digits separated by a decimal point, where each digit can have values $b \in \{0, 1\}$, and the base is 2. The general equation is,

$$\cdot$$
 bit

· binary

$$v = \sum_{i=-m}^{n} b_i 2^i \tag{A.2}$$

and examples are $1011.1_2 = 1 \cdot 2^3 + 0 \cdot 2^2 + 1 \cdot 2^1 + 1 \cdot 2^0 + 1 \cdot 2^{-1} = 11.5$. Notice that we use subscript 2 to denote a binary number, while no subscript is used for decimal numbers. The left-most bit is called the *most significant bit*, and the right-most bit is called the *least significant bit*. Due to typical organization of computer memory, 8 binary digits is called a *byte*, and 32 digits a *word*.

Other number systems are often used, e.g., octal numbers, which are base 8 numbers, where each digit is $o \in \{0, 1, \dots, 7\}$. Octals are useful short-hand for binary, since 3 binary digits maps to the set of octal digits. Likewise, hexadecimal numbers are base 16 with digits $h \in \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, a, b, c, d, e, f\}$, such that $a_{16} = 10$, $b_{16} = 11$ and so on. Hexadecimals are convenient since 4 binary digits map directly to the set of octal digits. Thus $367 = 101101111_2 = 557_8 = 16f_{16}$. A list of the intergers 0–63 is various bases is given in Table A.1.

- · least significant bit
- · byte
- \cdot word
- \cdot octal
- · hexadecimal

A.2 IEEE 754 floating point standard

The set of real numbers also called *reals* includes all fractions and irrational numbers. It is infinite in size both in the sense that there is no largest nor smallest number and between any 2 given numbers there are infinitely many numbers. Reals are widely used for calculation, but since any computer only has finite memory, it is impossible to represent all possible reals. Hence, any computation performed on a computer with reals must rely on approximations. *IEEE 754 double precision floating-point format* (binary64), known as a double, is a standard for representing an approximation of reals using 64 bits. These bits are divided into 3 parts: sign, exponent and fraction,

$$s e_1 e_2 \dots e_{11} m_1 m_2 \dots m_{52}$$

 \cdot reals

· IEEE 754 double precision floating-point format

- · binary64
- \cdot double

Dec	Bin	Oct	Hex	Dec	Bin	Oct	Hex
0	0	0	0	32	100000	40	20
1	1	1	1	33	100001	41	21
2	10	2	2	34	100010	42	22
3	11	3	3	35	100011	43	23
4	100	4	4	36	100100	44	24
5	101	5	5	37	100101	45	25
6	110	6	6	38	100110	46	26
7	111	7	7	39	100111	47	27
8	1000	10	8	40	101000	50	28
9	1001	11	9	41	101001	51	29
10	1010	12	a	42	101010	52	2a
11	1011	13	b	43	101011	53	2b
12	1100	14	c	44	101100	54	2c
13	1101	15	d	45	101101	55	2d
14	1110	16	e	46	101110	56	2e
15	1111	17	f	47	101111	57	2f
16	10000	20	10	48	110000	60	30
17	10001	21	11	49	110001	61	31
18	10010	22	12	50	110010	62	32
19	10011	23	13	51	110011	63	33
20	10100	24	14	52	110100	64	34
21	10101	25	15	53	110101	65	35
22	10110	26	16	54	110110	66	36
23	10111	27	17	55	110111	67	37
24	11000	30	18	56	111000	70	38
25	11001	31	19	57	111001	71	39
26	11010	32	1a	58	111010	72	3a
27	11011	33	1b	59	111011	73	3b
28	11100	34	1c	60	111100	74	3c
29	11101	35	1d	61	111101	75	3d
30	11110	36	1e	62	111110	76	3e
31	11111	37	1f	63	111111	77	3f

Table A.1: A list of the intergers 0–63 in decimal, binary, octal, and hexadecimal.

where s, e_i , and m_j are binary digits. The bits are converted to a number using the equation by first calculating the exponent e and the mantissa m,

$$e = \sum_{i=1}^{11} e_i 2^{11-i},\tag{A.3}$$

$$m = \sum_{j=1}^{52} m_j 2^{-j}.$$
 (A.4)

I.e., the exponent is an integer, where $0 \le e < 2^{11}$, and the mantissa is a rational, where $0 \le m < 1$. For most combinations of e and m the real number v is calculated as,

$$v = (-1)^{s} (1+m) 2^{e-1023}$$
(A.5)

with the exception that

	m = 0	$m \neq 0$
e = 0	$v = (-1)^s 0 \text{ (signed zero)}$	$v = (-1)^s m2^{1-1023}$ (subnormals)
$e = 2^{11} - 1$	$v = (-1)^s \infty$	$v = (-1)^s \text{ NaN (not a number)}$

 \cdot subnormals

 \cdot not a number

 \cdot NaN

where $e = 2^{11} - 1 = 111111111111_2 = 2047$. The largest and smallest number that is not infinity is thus

$$e = 2^{11} - 2 = 2046 \tag{A.6}$$

$$m = \sum_{j=1}^{52} 2^{-j} = 1 - 2^{-52} \simeq 1. \tag{A.7}$$

$$v_{\text{max}} = \pm (2 - 2^{-52}) 2^{1023} \simeq \pm 2^{1024} \simeq \pm 10^{308}$$
 (A.8)

The density of numbers varies in such a way that when e - 1023 = 52, then

$$v = (-1)^{s} \left(1 + \sum_{j=1}^{52} m_j 2^{-j} \right) 2^{52}$$
(A.9)

$$= \pm \left(2^{52} + \sum_{j=1}^{52} m_j 2^{-j} 2^{52}\right) \tag{A.10}$$

$$= \pm \left(2^{52} + \sum_{j=1}^{52} m_j 2^{52-j}\right) \tag{A.11}$$

$$\stackrel{k=52-j}{=} \pm \left(2^{52} + \sum_{k=51}^{0} m_{52-k} 2^k \right) \tag{A.12}$$

which are all integers in the range $2^{52} \le |v| < 2^{53}$. When e - 1023 = 53, then the same calculation gives

$$v \stackrel{k=53-j}{=} \pm \left(2^{53} + \sum_{k=52}^{1} m_{53-k} 2^k\right)$$
 (A.13)

which are every second integer in the range $2^{53} \le |v| < 2^{54}$, and so on for larger e. When e-1023 = 51, then the same calculation gives,

$$v \stackrel{k=51-j}{=} \pm \left(2^{51} + \sum_{k=50}^{-1} m_{51-k} 2^k\right)$$
 (A.14)

which gives a distance between numbers of 1/2 in the range $2^{51} \le |v| < 2^{52}$, and so on for smaller e. Thus we may conclude that the distance between numbers in the interval $2^n \le |v| < 2^{n+1}$ is 2^{n-52} , for $-1022 = 1 - 1023 \le n < 2046 - 1023 = 1023$. For subnormals the distance between numbers are

$$v = (-1)^s \left(\sum_{j=1}^{52} m_j 2^{-j}\right) 2^{-1022}$$
(A.15)

$$= \pm \left(\sum_{j=1}^{52} m_j 2^{-j} 2^{-1022}\right) \tag{A.16}$$

$$= \pm \left(\sum_{j=1}^{52} m_j 2^{-j-1022}\right) \tag{A.17}$$

$$\stackrel{k=-j-1022}{=} \pm \left(\sum_{j=-1023}^{-1074} m_{-k-1022} 2^k \right) \tag{A.18}$$

which gives a distance between numbers of $2^{-1074} \simeq 10^{-323}$ in the range $0 < |v| < 2^{-1022} \simeq 10^{-308}$.

Appendix B

Commonly used character sets

Letters, digits, symbols and space are the core of how we store data, write programs, and comunicate with computers and each others. These symbols are in short called characters, and represents a mapping between numbers, also known as codes, and a pictorial representation of the character. E.g., the ASCII code for the letter 'A' is 65. These mappings are for short called character sets, and due to differences in natural languages and symbols used across the globe, many different character sets are in use. E.g., the English alphabet contains the letters 'a' to 'z', which is shared by many other European languages, but which have other symbols and accents for example, Danish has further the letters 'æ', ' ϕ ', and 'å'. Many non-european languages have completely different symbols, where Chinese character set is probably the most extreme, where some definitions contains 106,230 different characters albeit only 2,600 are included in the official Chinese language test at highest level.

Presently, the most common character set used is Unicode Transformation Format (UTF), whose most popular encoding schemes are 8-bit (UTF-8) and 16-bit (UTF-16). Many other character sets exists, and many of the later builds on the American Standard Code for Information Interchange (ASCII). The ISO-8859 codes were an intermediate set of character sets that are still in use, but which is greatly inferior to UTF. Here we will briefly give an overview of ASCII, ISO-8859-1 (Latin1), and UTF.

B.1 ASCII

The American Standard Code for Information Interchange (ASCII) [4], is a 7 bit code tuned for the letters of the english language, numbers, punctuation symbols, control codes and space, see Tables B.1 and B.2. The first 32 codes are reserved for non-printable control characters to control printers and similar devices or to provide meta-information. The meaning of each control characters is not universally agreed upon.

The code order is known as $ASCIIbetical\ order$, and it is sometimes used to perform arithmetic on codes, e.g., an upper case letter with code c may be converted to lower case by adding 32 to its code. The ASCIIbetical order also has consequence for sorting, i.e., when sorting characters according to their ASCII code, then 'A' comes before 'a', which comes before the symbol ' $\{$ '.

- · American Standard Code for Information Interchange
- \cdot ASCII
- · ASCIIbetical order

B.2 ISO/IEC 8859

The ISO/IEC 8859 report http://www.iso.org/iso/catalogue_detail?csnumber=28245 defines 10 sets of codes specifying up to 191 codes and graphic characters using 8 bits. Set 1 also known as ISO/IEC 8859-1, Latin alphabet No. 1, or *Latin1* covers many European languages and is designed to be compatible with ASCII, such that code for the printable characters in ASCII are the same in ISO 8859-1. In Table B.3 is shown the characters above 7e. Codes 00-1f and 7f-9f are undefined in ISO 8859-1.

· Latin1

x0+0x	00	10	20	30	40	50	60	70
00	NUL	DLE	SP	0	0	P		p
01	SOH	DC1	!	1	A	Q	a	q
02	STX	DC2	"	2	В	R	b	r
03	ETX	DC3	#	3	С	S	С	s
04	EOT	DC4	\$	4	D	Т	d	t
05	ENQ	NAK	%	5	E	U	e	u
06	ACK	SYN	&	6	F	V	f	V
07	BEL	ETB	,	7	G	W	g	W
08	BS	CAN	(8	Н	X	h	X
09	HT	EM)	9	I	Y	i	У
0A	$_{ m LF}$	SUB	*	:	J	Z	j	Z
0B	VT	ESC	+	;	K	[k	{
0C	FF	FS	,	<	L	\	1	
0D	CR	GS	_	=	M]	m	}
0E	SO	RS		>	N	^	n	~
0F	SI	US	/	?	O	_	О	DEL

Table B.1: ASCII

B.3 Unicode

Unicode is a character standard defined by the Unicode Consortium, http://unicode.org as the Unicode Standard. Unicode allows for 1,114,112 different codes. Each code is called a code point, which represents an abstract character. However, not all abstract characters requires a unit of several code points to be specified. Code points are divided into 17 planes each with $2^{16} = 65,536$ code points. Planes are further subdivided into named blocks. The first plane is called the Basic Multilingual plane and it are the first 128 code points is called the Basic Latin block and are identical to ASCII, see Table B.1, and code points 128-255 is called the Latin-1 Supplement block, and are identical to the upper range of ISO 8859-1, see Table B.3. Each code-point has a number of attributes such as the unicode general category. Presently more than 128,000 code points covering 135 modern and historic writing systems, and obtained at http://www.unicode.org/Public/UNIDATA/UnicodeData.txt, which includes the code point, name, and general category.

A unicode code point is an abstraction from the encoding and the graphical representation of a character. A code point is written as "U+" followed by its hexadecimal number, and for the Basic Multilingual plane 4 digits are used, e.g., the code point with the unique name LATIN CAPITAL LETTER A has the unicode code point is "U+0041", and is in this text it is visualized as 'A'. More digits are used for code points of the remaining planes.

The general category is used in grammars to specify valid characters, e.g., in naming identifiers in F#. Some categories and their letters in the first 256 code points are shown in Table B.5.

To store and retrieve code points, they must be encoded and decoded. A common encoding is UTF-8, which encodes code points as 1 to 4 bytes, and which is backward-compatible with ASCII and ISO 8859-1. Hence, in all 3 coding systems the character with code 65 represents the character 'A'. Another popular encoding scheme is UTF-16, which encodes characters as 2 or 4 bytes, but which is not backward-compatible with ASCII or ISO 8859-1. UTF-16 is used internally in many compiles, interpreters and operating systems.

- \cdot Unicode Standard
- · code point
- · blocks
- · Basic Multilingual plane
- · Basic Latin block
- · Latin-1 Supplement block
- · unicode general category

 \cdot UTF-8

· UTF-16

Code	Description
NUL	Null
SOH	Start of heading
STX	Start of text
ETX	End of text
EOT	End of transmission
ENQ	Enquiry
ACK	Acknowledge
BEL	Bell
BS	Backspace
HT	Horizontal tabulation
LF	Line feed
VT	Vertical tabulation
FF	Form feed
CR	Carriage return
SO	Shift out
SI	Shift in
DLE	Data link escape
DC1	Device control one
DC2	Device control two
DC3	Device control three
DC4	Device control four
NAK	Negative acknowledge
SYN	Synchronous idle
ETB	End of transmission block
CAN	Cancel
EM	End of medium
SUB	Substitute
ESC	Escape
FS	File separator
GS	Group separator
RS	Record separator
US	Unit separator
SP	Space
DEL	Delete

Table B.2: ASCII symbols.

x0+0x	80	90	A0	В0	C0	D0	E0	F0
00			NBSP	0	À	Đ	à	ð
01			i	土	Á	Ñ	á	$ ilde{ ext{n}}$
02			¢	2	Â	Ò	â	ò
03			£	3	Ã	Ó	$ ilde{ ext{a}}$	ó
04			¤	,	Ä	Ô	ä	ô
05			¥	μ	Å	Õ	å	õ
06				\P	Æ	Ö	æ	ö
07			§	•	Ç	×	ç	÷
08			•	د	È	Ø	è	Ø
09			©	1	É	Ù	é	ù
0a			<u>a</u>	Ō	Ê	Ú	ê	ú
0b			«	>>	Ë	Û	ë	û
0c			Г	$\frac{1}{4}$	Ì	Ü	ì	ü
0d			SHY	$\frac{\frac{1}{4}}{\frac{1}{2}}$	Í	Ý	í	ý
0e			<u>R</u>	$\frac{3}{4}$	Î	Þ	î	þ
Of			-	į	Ϊ	ſŝ	ï	ÿ

Table B.3: ISO-8859-1 (latin1) non-ASCII part. Note that the codes 7f-9f are undefined.

Code	Description
NBSP	Non-breakable space
SHY	Soft hypen

Table B.4: ISO-8859-1 special symbols.

General	Code points	Name
category		
Lu	U+0041-U+005A, U+00C0-U+00D6,	Upper case letters
	U+00D8-U+00DE	
Ll	U+0061-U+007A, U+00B5,	Lower case letter
	$U+00DF-U+00F6,\ U+00F8-U+00FF$	
$_{ m Lt}$	None	Digraphic letter, with first part uppercase
Lm	None	Modifier letter
Lo	U+00AA, U+00BA	Gender ordinal indicator
Nl	None	Letterlike numeric character
Pc	$\mathrm{U}{+005}\mathrm{F}$	Low line
Mn	None	Nonspacing combining mark
Mc	None	Spacing combining mark
Cf	U+00AD	Soft Hyphen

Table B.5: Some general categories for the first 256 code points.

Appendix C

A brief introduction to Extended Backus-Naur Form

Extended Backus-Naur Form (EBNF) is a language to specify programming languages in. The name is a tribute to John Backus who used it to describe the syntax of ALGOL58 and Peter Nauer for his work on ALGOL 60.

· Extended Backus-Naur Form

An EBNF consists of terminal symbols and production rules. Examples of typical terminal symbol are characters, numbers, punctuation marks, and whitespaces, e.g.,

```
\cdot EBNF
```

- \cdot terminal symbols
- · production rules

```
digit = "0" | "1" | "2" | "3" | "4" | "5" | "6" | "7" | "8" | "9" ;
```

A production rule specifies a method of combining other production rules and terminal symbols, e.g.,

```
number = { digit } ;
```

A proposed standard for EBNF (proposal ISO/IEC 14977, http://www.cl.cam.ac.uk/~mgk25/iso-14977.pdf) is,

'=' definition, e.g.,

```
zero = "0" ;
```

here zero is the terminal symbol 0.

',' concatenation, e.g.,

```
one = "1";
eleven = one, one;
```

here eleven is the terminal symbol 11.

- ';' termination of line
- 'I' alternative options, e.g.,

```
digit = "0" | "1" | "2" | "3" | "4" | "5" | "6" | "7" | "8" | "9" ;
```

here digit is the single character terminal symbol, such as 3.

'[...]' optional, e.g.,

```
zero = "0";
nonZeroDigit = "1" | "2" | "3" | "4" | "5" | "6" | "7" | "8" | "9";
nonZero = [ zero ], nonZeroDigit
```

here nonZero is a non-zero digit possibly preceded by zero, such as 02.

'{ ...}' repetition zero or more times, e.g.,

```
digit = "0" | "1" | "2" | "3" | "4" | "5" | "6" | "7" | "8" | "9";
number = digit, { digit }
```

here number is a word consisting of 1 or more digits, such as 12.

'(...)' grouping, e.g.,

```
digit = "0" | "1" | "2" | "3" | "4" | "5" | "6" | "7" | "8" | "9";
number = digit, { digit }
expression = number, { ( "+" | "-" ), number };
```

here expression is a number or a sum of numbers such as 3 + 5.

" ... " a terminal string, e.g.,

```
string = "abc"';
```

"' ... '" a terminal string, e.g.,

```
string = 'abc';
```

'(* ... *)' a comment (* ... *)

```
(* a binary digit *) digit = "0" | "1" (* from this all numbers may be
  constructed *);
```

Everything inside the comments are not part of the formal definition.

'? ... ?' special sequence, a notation reserved for future extensions of EBNF.

'-' exception, e.g.,

here consonant are all letters except vowels.

The proposal allows for identifies that includes space, but often a reduced form is used, where identifiers are single words, in which case the concatenation symbol , is omitted. Likewise, the termination symbol ; is often replaced with the new-line character, and if long lines must be broken, then indentation is used to signify continuation.

In this relaxed EBNF, the EBNF syntax itself can be expressed in EBNF as,

```
string = character { character }
terminal = "'" string "'" | '"' string '"'
rhs = identifier
    | terminal
    | "[" rhs "]"
    | "(" rhs ")"
    | rhs "|" rhs
    (* | rhs "," rhs *)
rule = identifier "=" rhs (* ";" *)
grammar = rule { rule }
```

Here the comments demonstrate, the relaxed modification.

Appendix D

Language Details

1

¹Somewhere I should possibly talk about Lightweight Syntax, Spec-4.0 Chapter 15.1

Operator	Associativity	Description
ident "<"types ">"	Left	High-precedence type application
ident "("expr ")"	Left	High-predence application
"."	Left	
prefixOp	Left	All prefix operators
"" rule	Left	Pattern matching rule
ident expr,	Left	
"lazy'' expr,		
"assert'' epxr		
"**"opChar	Right	Exponent like
"*"opChar, "/"opChar,	Left	Infix multiplication like
"%"opChar		
"-"opChar, "+"opChar	Left	Infix addition like
":?''	None	
"::''	Right	
"^'' opChar	Right	
"!="opChar, "<"opChar,	Left	Infix addition like
">"opChar, "=",		
" "opChar, "&"opChar,		
"\$"opChar		
":>", ":?>"	Right	
"&", "&&"	Left	Boolean and like
"or", " "	Left	Boolean or like
п, п	None	
":="	Right	
"->"	Right	
"if"	None	
"function", "fun",	None	
"match", "try"		
"let"	None	
"; "	Right	
" "	Left	
"when"	Right	
"as"	Right	

Table D.1: Precedence and associativity of operators. Operators in the same row has same precedence. See Listing 6.28 for the definition of prefixOp

Bibliography

- [1] Alonzo Church. A set of postulates for the foundation of logic. *Annals of Mathematics*, 33(2):346–366, 1932.
- [2] Programming Research Group. Specifications for the ibm mathematical formula translating system, fortran. Technical report, Applied Science Division, International Business Machines Corporation, 1954
- [3] John McCarthy. Recursive functions of symbolic expressions and their computation by machine, part i. *Communications of the ACM*, 3(4):184–195, 1960.
- [4] X3: ASA Sectional Committee on Computers and Information Processing. American standard code for information interchange. Technical Report ASA X3.4-1963, American Standards Association (ASA), 1963. http://worldpowersystems.com/projects/codes/X3.4-1963/.
- [5] George Pólya. How to solve it. Princeton University Press, 1945.

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