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Learning to Program with F#

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Preface

This book has been written as an introduction to programming for novice programmers. It is used in the first programming course at the University of Copenhagen's bachelor in computer science program. It has been typeset in LaTeX, and all programs have been developed and tested in Mono version 6.0.0.327.

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Chapter 1

Introduction

Programming is a creative process in which exciting problems may be solved and new tools and applications may be created. With programming skills, you can create highlevel applications to run on a mobile device that interact with other users, databases, and artificial intelligence; you may create programs that run on supercomputers for simulating weather systems on alien planets or social phenomena in the internet economy; and you may create programs that run on small custom-made hardware for controlling your home appliances.

1.1 How to Learn to Solve Problems by Programming

In order to learn how to program, there are a couple of steps that are useful:

- 1. Choose a programming language: A programming language, such as F#, is a vocabulary and a set of grammatical rules for instructing a computer to perform a certain task. It is possible to program without a concrete language, but your ideas and thoughts must still be expressed in some fairly rigorous way. Theoretical computer scientists typically do not rely on computers nor programming languages but uses mathematics to prove properties of algorithms. However, most computer scientists program using a computer, and with a real language you have the added benefit of checking your algorithm, and hence your thoughts, rigorously on a real computer. This book teaches a subset of F#. The purpose is not to be a reference guide to this language but to use it as a vessel to teach you, the reader, how to convert your ideas into programs.
- 2. Learn the language: A computer language is a structure for thought, and it influences which thoughts you choose to express as a program, and how you

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choose to do it. Any conversion requires you to acquire a sufficient level of fluency in order for you to be able to make programs. You do not need to be a master in F# nor to know every corner of the language, and you will expand your knowledge as you expose yourself to solving problems in the language, but you must invest an initial amount of time and energy in order to learn the basics of the language. This book aims at getting you started quickly, which is why we intentionally teach just a small subset of F#. On the internet and through other works you will be able to learn much more.

- 3. Practice: In order to be a good programmer, the most essential step is: practice, practice, practice! It has been estimated that to master anything, then you have to have spent at least 10000 hours practicing, so get started logging hours! It of course matters, how you practice. This book teaches a number of different programming themes. The point is that programming is thinking, and the scaffold you use shapes your thoughts. It is therefore important to recognize this scaffold and to have the ability to choose one which suits your ideas and your goals best. The best way to expand your abilities is to sharpen your present abilities, push yourself into new territory, and try something new. Do not be afraid to make errors or be frustrated at first. These are the experiences that make you grow.
- 4. Solve real problems: I have found that using my programming skills in real situations with customers demanding specific solutions, has forced me to put the programming tools and techniques that I use into perspective. Sometimes a task requires a cheap and fast solution, other times customers want a long-perspective solution with bug fixes, upgrades, and new features. Practicing solving real problems helps you strike a balance between the two when programming. It also allows makes you a more practical programmer, by allowing you to recognize its applications in your everyday experiences. Regardless, real problems create real programmers.

1.2 How to Solve Problems

Programming is the act of solving a problem by writing a program to be executed on a computer. A general method for solving problems, given by George Pólya [9] and adapted to programming, is:

Understand the problem: To solve any problem it is crucial that the problem formulation is understood. What is to be solved? Do you understand everything in the description of the problem? Is all information for finding the solution available or is something missing?

Design a plan: Good designs lead to programs are faster to implement, easier to find errors in, and easier to update in the future. Before you start typing a program consider things like: What are the requirements and constraints for the program? Which components should the program have? How are these components supposed to work together? Designing often involves drawing a diagram of the program and writing program sketches on paper.

Implement the plan: Implementation is the act of transforming a program design into code. A crucial part of any implementation is choosing which programming language to use. Furthermore, the solution to many problems will have a number of implementations which vary in how much code they require, to which degree they rely on external libraries, which programming style they are best suited for, what machine resources they require, and how long time they take to run on a computer. With a good design, the coding is usually easy, since the design will have uncovered the major issues and found solutions for these, but sometimes implementation reveals new problems, which require rethinking the design. Most often the implementation step also require a careful documentation of key aspects of the code, e.g., a user manual for the user, and internal notes for fellow programmers that are to maintain and update the code in the future.

Reflect on the result: A crucial part of any programming task is ensuring that the program solves the problem sufficiently. Ask yourself questions such as: What are the program's errors, is the documentation of the code sufficient and relevant for its intended use? Is the code easily maintainable and extendable by other programmers? Which parts of your method would you avoid or replicate in future programming sessions? Can you reuse some of the code you developed in other programs?

Programming is a very complicated process, and Pólya's list is a useful guide but not a fail-safe approach. Always approach problem-solving with an open mind.

1.3 Approaches to Programming

This book focuses on several fundamentally different approaches to programming:

Declarative programming emphasizes what a program shall accomplish but not how. We will consider Functional programming as an example of declarative programming. A functional programming language evaluates functions and avoids state changes. The program consists of expressions instead of statements. As an example, the function $f(x) = x^2$ takes a number x, evaluates the expression x^2 , and returns the resulting number. Everything about the function may be

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characterized by the relation between the input and output values. Functional programming has its roots in lambda calculus [1]. The first language emphasizing functional programming was Lisp [7].

Imperative programming emphasizes *how a program shall accomplish a solution* and focusses less on *what the solution is*. A cooking recipe is an example of the spirit of imperative programming, where the recipe emphasizes what should be done in each step rather than describing the result. For example, a recipe for bread might tell you to first mix yeast and water, then add flour, etc. In imperative programming what should be done are called *statements* and in the recipe analogy, the steps are the statements. Statements influence the computer's *states*, in the same way that adding flour changes the state of our dough. Almost all computer hardware is designed to execute low-level programs written in imperative style. Imperative programming builds on the Turing machine [10]. As a historical note, the first major language was FORTRAN [6] which emphasized an imperative style of programming.

Structured programming emphasizes organization of programs in units of code and data. For example, a traffic light may consist of a state (red, yellow, green), and code for updating the state, i.e., switching from one color to the next. We will focus on Object-oriented programming as the example of structured programming. *Object-oriented programming* is a type of programming, where the code and data are structured into *objects*. E.g., a traffic light may be an object in a traffic-routing program. The first object-oriented programming language was Simula 67 developed by Dahl and Nygaard at the Norwegian Computing Center in Oslo [2].

Event-driven programming, which is often used when dynamically interacting with the real world. This is useful, for example, when programming graphical user interfaces, where programs will often need to react to a user clicking on the mouse or to text arriving from a web-server to be displayed on the screen. Event-driven programs are often programmed using *call-back functions*, which are small programs that are ready to run when events occur.

Most programs do not follow a single programming paradigm as, e.g., one of the above, but are a mix. Nevertheless, this book will treat each paradigm separately to emphasize its advantages and disadvantages.

1.4 Why Use F#

This book uses F#, also known as Fsharp, which is a functional first programming language, meaning that it is designed as a functional programming language that also

5 1.4 Why Use F#

supports imperative and object-oriented programming. It was originally developed for Microsoft's .Net platform but is available as open source for many operating systems through Mono. As an introduction to programming, F# is a young programming language still under development, with syntax that at times is a bit complex. Still, it offers a number of advantages:

- Interactive and compile mode: F# has an interactive and a compile mode of operation. In interactive mode you can write code that is executed immediately in a manner similar to working with a calculator, while in compile mode you combine many lines of code possibly in many files into a single application, which is easier to distribute to people who are not F# experts and is faster to execute.
- Indentation for scope: F# uses indentation to indicate scope. Some lines of code belong together and should be executed in a certain order and may share data. Indentation helps in specifying this relationship.
- Strongly typed: F# is strongly typed, reducing the number of runtime errors. That is, F# is picky, and will not allow the programmer to mix up types such as numbers and text. This is a great advantage for large programs.
- Multi-platform: F# is available on Linux, Mac OS X, Android, iOS, Windows, GPUs, and browsers both via the public domain Mono platform and Microsoft's open source .Net system.
- Free to use and open source: F# is supported by the Fsharp foundation (http://fsharp.org) and sponsored by Microsoft.
- Assemblies: F# is designed to be able to easily communicate with other .Net and Mono programs through the language-independent, platform-independent byte-code called Common Intermediate Language (CIL) organized as assemblies. Thus, if you find that certain parts of a program are easy to express in F# and others in C++, then you will be able to combine these parts later into a single program.
- Modern computing: F# supports all aspects of modern computing including Graphical User Interfaces, Web programming, Information rich programming, Parallel algorithms, . . .
- Integrated development environments (IDE): F# is supported by IDEs such as Visual Studio (https://www.visualstudio.com) and Xamarin Studio (https://www.xamarin.com).

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1.5 How to Read This Book

Learning to program requires mastering a programming language, however, most programming languages contain details that are rarely used or used in contexts far from a specific programming topic. Hence, this book only includes a subset of F# but focuses on language structures necessary to understand several common programming paradigms: Imperative programming mainly covered in Chapters 4 to 9, functional programming mainly covered in Chapters 7 to 8, object-oriented programming in Chapters 23 and 25, and event-driven programming in Chapter 15. A number of general topics are given in the appendix for reference. For further reading please consult http://fsharp.org.

Chapter 2

Solving problems by writing a program

Abstract tada - In this chapter, you will find a quick introduction to several essential programming constructs with several examples that you can try on your computer using the dotnet command in your console. All constructs will be discussed in further detail in the following chapters. In this chapter, you will get a peek at:

- How to execute an F# program
- How to perform simple arithmetic using F#
- What types are and why they are important
- How to write to and obtain written input from the user
- How to perform conditional execution of code
- How to define functions
- · How to repeat code without having to rewrite them
- How to add textual comments to help yourself and other programmers understand your programs.

Programming is the art of solving problems by writing a program to be executed by a computer. For example, to solve the following problem,

Problem 2.1

What is the sum of 357 and 864?

we have written the program shown in Listing 2.1. In this book, we will show many programs, and for most, we will also show the result of executing the programs on a computer. Listing 2.1 shows both our program and how this program is executed

Listing 2.1 quickStartSum.fsx: A script to add 2 numbers and print the result to the console. 1 let a = 357 2 let b = 864 3 let c = a + b 4 do printfn "%A" c

on a computer. In the listing, we see our program was saved as a script in a file called quickStartSum.fsx, and in the console (also known as the terminal and the command-line) we executed the program by typing the command dotnet fsi quickStartSum.fsx. The result is then printed by the computer to the console as 1221. The colors are not part of the program but have been added to make it easier for us to identify different syntactical elements of the program.

The program consists of several lines. Our listing shows line numbers to the left. These are not part of the program but added for ease of discussion, since the order in which the lines appear the program matters. In this program, each line contains *expressions*, and this program has let-, do-expressions, and an addition. let-expressions defines aliases, and do-expressions defines computations. let and do are examples of *keywords*, and "+" is an example of an *operator*. Keywords, operators, and other sequences of characters, which F# recognizes are jointly called *lexemes*.

Reading the program from line 1, the first expression we encounter is let a = 357. This is known as a *let-binding* in F# and defines the equivalence between the name a and the value 357. F# does not accept a keyword as a name in a let-bindings. The consequence of this line is that in later lines there is no difference between writing the name a and the value 357. Similarly in line 2 the value 864 is bound to the name b. In contrast, line 3 contains an addition and a let-expression. It is at times useful to simulate the execution the computer does in a step-by-step manner by replacement:

```
let c = a + b \implies let c = 357 + 864 \implies let c = 1221
```

Thus, since the expression on the right-hand side of the equal sign is evaluated, the result of line 3 is that the name c is bound to the value 1221.

Line 4 has a do-expression is also called a *do-binding* or a *statements*. In this dobinding, the *printfn function* printfn is called with 2 arguments, "%A"and c. All functions return values, and printfn the value 'nothing', which is denoted "()". This function is very commonly used but also very special since it can take any number of arguments and produces output to the console. We say that "the output is printed to the screen". The first argument is called the *formatting string* and

describes, what should be printed and how the remaining arguments if any, should be formatted. In this case, the value c is printed as an integer followed by a newline. Notice that in contrast to many other languages, F# does not use parentheses to frame the list of function arguments, nor does it use commas to separate them.

2.1 Executing F# programs on a computer

The main purpose of writing programs is to make computers execute or run them. F# has two modes of execution, *interactive* and *compiled*. Interactive mode allows the user to interact with F# as a dialogue: The user writes statements, and F# responds immediately. If a program has been saved as a file as in Listing 2.1 we do not need to rewrite the complete program every time we wish to execute it but can give the file as input to the F#'s interactive mode as demonstrated in Listing 2.1. Interactive mode is well suited for small experiments or back-of-an-envelope calculations, but not for programming in general, since each line is interpreted anew every time the program is run. In contrast, in compile mode, dotnet interprets the content of a source file once, and writes the result to disk, such that every when the user wishes to run the program, the interpretation step is not performed. For large programs, this can save considerable time. In the first chapters of this book, we will use interactive mode, and compile mode will be discussed in further detail in Chapter 17.

An interactive session is obtained by starting the console, typing the fsharpi command, typing the lines of the program, and ending the script-fragment with ";;". The dialogue in Listing 2.2 demonstrates the workflow. What the user types has been highlighted by a box

```
Listing 2.2: An interactive session.

1 $ dotnet fsi
2
3 Microsoft (R) F# Interactive version 12.0.0.0 for F# 6.0
4 Copyright (c) Microsoft Corporation. All Rights Reserved.
5
6 For help type #help;;
7
8 > let a = 3.0
9 - do printfn "%A" a;;
10 3.0
11 val a : float = 3.0
12 val it : unit = ()
13
14 > #quit;;
```

We see that after typing fsharpi, the program starts by stating details about itself. Then F# writes > indicating that it is ready to receive commands. The user types let a = 3.0 and presses enter, to which the interpreter responds with -. This indicates that the line has been received, that the script fragment is not yet completed, and that it is ready to receive more input. When the user types do printfn "%A" a;; followed by enter, then by ";;" the interpreter knows that the script-fragment is completed, it interprets the script-fragment, responds with 3.0 and some extra information about the entered code, and with > to indicate that it is ready for more script-fragments. The interpreter is stopped when the user types #quit;;. It is also possible to stop the interpreter by typing ctrl-d.

The interactive session results in extra output on the *type inference* performed. In Listing 2.2, F# states that the name a has *type* float and the value 3.0. Likewise, the do statement F# refers to by the name it, and it has the type unit and value "()". Types are very important to F# since they define how different program pieces fit together like lego bricks. They are a key ingredient for finding errors in programs, also known as *debugging*, and much of the rest of this book is concerned with types.

Instead of running fsharpi interactively, we can write the script-fragment from Listing 2.2 into a file, here called gettingStartedStump.fsx. This file can be interpreted directly by dotnet fsi as shown in Listing 2.3.

```
Listing 2.3: Using the interpreter to execute a script.

| $ (dotnet fsi gettingStartedStump.fsx) | 3.0
```

Notice that in the file, ";;" is optional. In comparison to Listing 2.2, we see that the interpreter executes the code and prints the result on screen without the extra type information.

Files are important when programming, and F# and the console interprets files differently by the filename's suffix. A filename's suffix is the sequence of letters after the period in the filename. Generally, there are two types of files: *source code* and compiled programs. Until Chapter 17, we will concentrate on script files, which are source code, written in human-readable form using an editor, and has .fsx or .fsscript as suffix. In Table 2.1 is a complete list of possible suffixes used by F#.

| Suffix | Human readable | Description |
|-----------|----------------|--|
| .fs | Yes | An implementation file, e.g., myModule.fs |
| .fsi | Yes | A signature file, e.g., myModule.fsi |
| .fsx | Yes | A script file, e.g., gettingStartedStump.fsx |
| .fsscript | Yes | Same as .fsx, e.g., gettingStartedStump.fsscript |
| .dll | No | A library file, e.g., myModule.dll |
| .exe | No | A stand-alone <i>executable file</i> , e.g., gettingStartedStump.exe |

Table 2.1 Suffixes used, when programming F#.

2.2 Values have types and types reduce the risk of programming errors

Types are a central concept in F#. In the script 2.1 we bound values of integer type to names. There are several different integer types in F#, here we used the one called |int|. The values were not *declared* to have these types, instead the types were *inferred* by F#. Typing these bindings line by line in an interactive session, we see the inferred types as shown in Listing 2.4. The interactive session displays the type using the

Listing 2.4: Inferred types are given as part of the response from the interpreter.

1 > let a = 357;;
2 val a : int = 357
3
4 > let b = 864;;
5 val b : int = 864
6
7 > let c = a + b;;
8 val c : int = 1221
9
10 > do printfn "%A" c;;
11 1221
12 val it : unit = ()

val keyword followed by the name used in the binding, its type, and its value. Since the value is also returned, the last printfn statement is superfluous. Notice that printfn is automatically bound to the name it of type unit and value "()". F# insists on binding all statements to values, and in lack of an explicit name, it will use it. Rumor has it that it is an abbreviation for "irrelevant".

In mathematics, types are also an important concept. For example, a number may belong to the set of natural \mathbb{N} , integer \mathbb{Z} , or real numbers, where all 3 sets are infinitely large and $\mathbb{N} \subset \mathbb{Z} \subset \mathbb{R}$ as illustrated in Figure 2.1. For many problems,

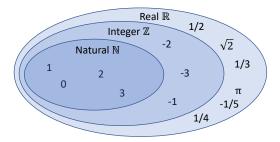


Fig. 2.1 In mathematics, the sets of natural, integer, and real numbers are each infinitely large, and real contains integers which in turn contains the set of natural numbers.

working with infinite sets is impractical, and instead, a lot of work in the early days

of the computer's history was spent on designing finite sets of numbers, which have many of the properties of their mathematical equivalent, but which also are efficient for performing calculations on a computer. For example, the set of integers in F# is called int and is the set [-2 147 483 648 . . . 2 147 483 647]. The most commonly used type to represent numbers with properties similar to reals is called float and is a clever selection of 2^{64} rational numbers. Since the computer representation of, e.g., int and float differ substantially, algorithms used to perform arithmetic also differ, and this limits how such types can be mixed.

Consider a slight modification of Problem 2.1 to the domain of reals,

```
Problem 2.2
What is the sum of 357.6 and 863.4?
```

To solve this problem on a computer we can use the float type, in which case the program would look like Listing 2.5. On the surface, this could appear as a negligi-

```
Listing 2.5 quickStartSumFloat.fsx:
Floating point types and arithmetic.

1 let a = 357.6
2 let b = 863.4
3 let c = a + b
4 do printfn "%A" c

1 $ dotnet fsi quickStartSumFloat.fsx
2 1221.0
```

ble change, but the set of integers and the set of real numbers (floats) require quite different representations to be effective on a computer, and as a consequence, the implementation of their operations, such as addition, are very different. Thus, although the response is an integer, it has type |float| which is indicated by 1221.0 and which is not the same as 1221. F# is very picky about types, and generally does not allow types to be mixed, as demonstrated in the interactive session in Listing 2.6. We see that binding a name to a number without a decimal point is inferred to be an integer, while when binding to a number with a decimal point the type is inferred to be a float, and that our attempt of adding an integer and floating point value gives an error. The error message contains much information. First, it states that the error is in stdin(4,13), which means that the error was found on standard-input at line 4 and column 13. Since the program was executed using fsharpi quickStartSumFloat.fsx, here standard input means the file quickStartSumFloat.fsx shown in Listing 2.5. The corresponding line and column are also shown in Listing 2.6. After the file, line, and column number, F# informs us of the error number and a description of the error. Error numbers are an underdeveloped feature in Mono and should be ignored. However, the verbal description often contains useful information for debugging. In the example we are informed that there is a type mismatch in the expression, i.e., since a is an integer, F# expected b to be one too. Debugging is the process of solving

Listing 2.6: Mixing types is often not allowed. 1 > let a = 357;; 2 val a : int = 357 3 4 > let b = 863.4;; 5 val b : float = 863.4 6 7 > let c = a + b;; 8 9 let c = a + b;; 10 ------^ 11 12 stdin(4,13): error FS0001: The type 'float' does not match the type 'int'

errors in programs, and here we can solve the error by either making a into a float or b into an int. The right solution depends on the application.

2.3 Organizing often used code in functions

printfn is an example of a built-in function, and very often we wish to define our own. For example, in longer programs, some code needs to be used in several places and defining functions to *encapsulate* such code can be a great advantage for reducing the length of code, debugging, and writing code, which is easier to understand by other programmers. A function is defined using a let-binding. For example, to define a function, which takes two integers as input and returns their sum, we write

```
Listing 2.7: Defining the function sum

1 let sum x y = x + y
```

What this means is that we bind the name sum as a function, which takes two arguments and adds them. Further, in the function, the arguments are locally referred to by the names x and y. Indentation determines which lines should be evaluated when the function is called, and in this case, there is only one. The value of the last expression evaluated in a function is its return value. Here there is only one expression x+y, and thus, this function returns the value of the addition. This program does not do anything, since the function is neither called nor is its output used. However, we can modify Listing 2.1 to include it as shown in Listing 2.8. The output is the same for the two programs, and the computation performed is almost the same. A step-by-step manner by replacement of the computation performed in line 3 is

The main difference is that with the function sum we have an independent unit, which can be reused elsewhere in the code.

let $c = 357 + 864 \implies let c = 1221$

2.4 Asking the user for input

let c = sum 357 864

The printfn function allows us to write to the screen, which is useful, but sometimes we wish to start a dialogue with the user. One way to get user input is to ask the user to type something on the keyboard. Technically, input from the keyboard is called an stdin stream. This terminology is intended to remind us of characters streaming from the keyboard like the flow of water in a stream. Computer streams are different than water streams in that characters (or other items) only flow, when we ask for them. F# provides many libraries of prebuilt functions, and here we will use the System.Console.ReadLine function. The "."-lexeme is read as ReadLine is a function which lies in Console which in turn lies in System. In the function documentation, we can read that System. Console. ReadLine takes a unit value as an argument and returns the string the user typed. A string is a built-in type as integers and floats, and while values of the later types contain numbers, strings contain a sequence of characters. The program will not advance until the user presses the newline. An example of a program that multiplies two floating point numbers supplied by a user is given in Listing 2.9, In this program, we find a user dialogue, and we have designed it such that we assume that the user is unfamiliar with the inner workings of our program, and therefore helps the user understand the purpose of the input and the expected result. This is good programming practice. Here, we will not discuss the program line-to-line, but it is advised to the novice programmer to match what is printed on the screen and from where in the code, the output comes from. However, let us focus on line 4 and 4, which introduce two new programming constructs. In each of these lines, 3 things happen: First the System.Console.ReadLine function is called with the "()" value as argument. This

Listing 2.9 quickStartSumInput.fsx:

Asking the user to input two decimal numbers to be added. The user entered 12.3, pressed the return button, 14, and pressed return again.

```
let sum x y = x + y
printfn "Adding a and b"
printf "Enter a: "
let a = float (System.Console.ReadLine ())
printf "Enter b: "
let b = float (System.Console.ReadLine ())
let c = sum a b
do printfn "%A" c

$\frac{1}{2}$ dotnet fsi quickStartSumInput.fsx
Adding a and b
Enter a: 12.3
Enter b: 14
26.3
```

reads all the characters, the user types, up until the user presses the return key. The return value is a string of characters such as "14". This value is different from the number 14, and hence, to later be able to perform float-addition, we *cast* the string value to float, meaning that we call the function float to convert the string-value to the corresponding float value. Finally, the result is bound to the names a and b respectively. Note that even though in the example execution the user first inputs both a decimal number and an integer, both string representations of these are cast to floats, which is why the addition does not give a type error.

2.5 Conditionally execute code

Often problem requires code evaluated based on conditions, which only can be decided at *runtime*, i.e., at the time, when the program is run. Consider a slight modification of our problem as

Problem 2.3

Ask for two float values from the user, a and b, and print the result of the division a/b.

To solve this problem, we must decide what to do, if the user inputs b=0, since division by zero is ill-defined. This is an example of a user input error, and later, we will investigate many different methods for handling such errors, but here, we will simply write an error message to the user, if the desired division is ill-defined. Thus, we need to decide at *runtime*, whether to divide a and b or to write an error

message. For this we will use the if-then-else expression. In this program, the

Listing 2.10 quickStartDivisionInput.fsx: Conditionally divide two user-given values. The first time the program is executed, the user enters 3 and 4, and the second time the user inputs 3 and let div x y = x / yprintfn "Dividing a by b" printf "Enter a: " let a = float (System.Console.ReadLine ()) printf "Enter b: " let b = float (System.Console.ReadLine ()) if b = 0 then do printfn "Input error: Cannot divide by zero" let c = div a b do printfn "%A" c \$ dotnet fsi quickStartDivisionInput.fsx Dividing a by b Enter a: 3 Enter b: 4 0.75 \$ dotnet fsi quickStartDivisionInput.fsx Dividing a by b Enter a: 3 Enter b: 0 Input error: Cannot divide by zero

if-then-else expression covers line 7 to 11, and when the computer executes these lines, it first evaluates the condition b = 0. In contrast to let-bindings, the "="-sign does not define the equivalence of a name and a value but tests if the equivalence holds. The result is a true or false value. The set {true, false} is called the boolean set and is written as bool in F#. If the condition evaluates to true, then the code following the then-keyword is executed, and otherwise, the code following the else-keyword is executed. The code belonging to the then- and the else-keywords respectively are called branches, and which lines belongs to each branch is determined by indentation. Hence, in this example, there is one line in the then-branch and two lines in the else-branch. Assuming that the user enters the value 0, then the step-by-step simplification of if-then-else expression is,

```
if b = 0 ...

→ if true ...

→ do printfn "Input error: Cannot divide by zero"
```

2.6 Repeatedly execute code

Often code needs to be evaluated many times or looped. For example, in Problem 2.3 we could repeat the question as many times as needed until the user inputs a non-zero value for *b*. This is called a loop, and there are several programming constructions for this purpose.

Let us first consider recursion. A recursive function is one, which calls itself, e.g., $f(f(f(\ldots(x))))$ is an example of a function f which calls itself many times, possibly infinitely many. In the latter case, we say that the recursion has entered an infinite loop, and we will experience that either the program runs forever or that the execution stops due to a memory error. If we had infinite memory. To avoid this, recursive functions must always have a stopping criterion. Thus, we can design a function for asking the user for a non-zero input value as shown in Listing 2.11. The function readNonZeroValue takes no input denoted by "()", and repeatedly

```
Listing 2.11 quickStartRecursiveInput.fsx:
Recursively call ReadLine until a non-zero value is entered.
let rec readNonZeroValue () =
     let a = float (System.Console.ReadLine ())
     if a <> 0 then
     else
       printfn "Error: zero value entered. Try again"
       readNonZeroValue ()
printfn "Please enter a non-zero value"
let b = readNonZeroValue ()
printfn "You typed: %A" b
$ dotnet fsi quickStartRecursiveInput.fsx
Please enter a non-zero value
Error: zero value entered. Try again
3
You typed: 3.0
```

calls itself until the $a \neq 0$ condition is met. It is recursive since its body contains a call to itself. For technical reasons, F# requires recursive functions to be declared by the rec-keyword as demonstrated. The function has been designed to stop if $a \neq 0$, and in F#, this is tested with the "<>" operator. Thus, if the stopping condition is satisfied, then the then-branch is executed, which does not call itself, and thus the recursion goes no deeper. If the condition is not met, then the else-branch is executed, and the function is eventually called anew. The example execution of the program demonstrates this for the case that the user first inputs the value 0 and then the value 3.

As an alternative to recursive functions, loops may also be implemented using the *while*-expression. In Listing 2.11 is an example of a solution where the recursive loop has been replaced with *while*-loop. As for other constructs, the lines to be

```
Listing 2.12 quickStartWhileInput.fsx:
Replacing recursion in Listing 2.11 with a -loop.

let readNonZeroValueAlt () =
let mutable a = float (System.Console.ReadLine ())
while a = 0 do
printfn "Error: zero value entered. Try again"
a <- float (System.Console.ReadLine ())
a
printfn "Please enter a non-zero value"
let b = readNonZeroValueAlt ()
printfn "You typed: %A" b

standard definition of the printfn and the
```

repeated are indicated by indentation, in this case, lines 4 to 5, and in the end, the result of the readNonZeroValueAlt function is the last expression evaluated, which is the trivial expression a in line 6. In comparison with the recursive version of the program, the while-loop has a continuation conditions (line 3), i.e., the content of the loop is repeated as long as a = 0 evaluates to true. Another difference is that in Listing 2.11 we could simplify our program to only using let valuebindings, here we need a new concept: variables also known as a mutable value. Mutable values allow us to update the value associated with a given name. Thus, the value associated with a name of mutable type depends on when it is accessed. This construction makes programs much more complicated and error-prone, and their use should be minimized. The syntax of mutable values is that first it should be defined with the mutable-keyword as shown in line 2, and when its value is to be updated then the "<-"-notation must be used as demonstrated in line 5. Note that the execution of the two programs Listing 2.11 and Listing 2.12, gives identical output, when presented with identical input. Hence, they solve the same problem by two quite different means. This is a common property of solutions to problems as a program: Often several different solutions exist, which are identical on the surface, but where the quality of the solution depends on how quality is defined and which programming constructions have been used. Here, the main difference is that the recursive solution avoids the use of mutable values, which turns out to be better for proving the correctness of programs and for adapting programs to super-computer architectures. However, recursive solutions may be very memory intensive, if the recursive call is anywhere but the last line of the function.

2.7 Programming as a form of communication

When programming it is important to consider the time dimension of a program. Some usually very small programs are only used for a short while, e.g., to test a programming construction or an idea to a solution. Others small as well as large may be used again and again over a long period, and possibly given to other programmers to use, maintain, and extend. In this case, programming is an act of communication, where what is being communicated is the solution to a problem as well as the thoughts behind the chosen solution. Common experiences among programmers are that it is difficult to fully understand the thoughts behind a program written by a fellow programmer from its source code alone, and for code written perhaps just weeks earlier by the same programmer, said programmer can find it difficult to remember the reasons for specific programming choices. To support this communication, programmers use code-*comments*. As a general concept, this is also called in-code documentation. Documentation may also be an accompanying manual or report. Documentation serves several purposes:

- 1. Communicate what the code should be doing, e.g., describe functions in terms of their input-output relation.
- 2. Highlight big insights essential for the code.
- 3. Highlight possible conflicts and/or areas where the code could be changed later.

F# has two different syntaxes for comments. A block comment is everything bracketed by (* *), and a line comment, which is everything between "//" and the end of the line. For example, adding comments to Listing 2.11 could look like Listing 2.13 Comments are ignored by the computer and serve solely as programmer-to-programmer communication, there are no or few rules for specifying, what is good and bad documentation of a program. The essential point is that coding is a journey in problem-solving, and proper documentation is an aid in understanding the solution and the journey that lead to it.

2.8 Key concepts and terms in this chapter

F# has two modes of operation: Interactive and compile mode. The first chapters
of this book will focus on the interactive mode.

Listing 2.13 quickStartRecursiveInputComments.fsx: Adding comments to Listing 2.11.

```
Demonstration of recursion for keyboard input.
   Author: Jon Sporring
   Date: 2022/7/28
*)
// Description: Repeatedly ask the user for a non-zero number
     until a non-zero value is entered.
// Arguments: None
// Result: the non-zero value entered
let rec readNonZeroValue () =
    // Note that the value of a is different for every
    // recursive call.
    let a = float (System.Console.ReadLine ())
    if a <> 0 then
      a
    else
      printfn "Error: zero value entered. Try again"
      readNonZeroValue ()
printfn "Please enter a non-zero value"
let b = readNonZeroValue ()
printfn "You typed: %A" b
```

- F# is accessed through the **console/terminal/command-line**, which is another program, in which text commands can be given such as starting the dotnet program in interactive mode.
- Programs are written in a human-readable form called the **source-code**.
- Source code consists of several syntactical elements such as **operators** such as "*" and "<-", **keywords** such as "let" and "while", **values** such as 1.2 and the string "hello world", and **user-defined names** such as "a" and "str". All words, which F# recognizes are called **lexemes**.
- A program consists of a sequence of expressions, which comes in two types:
 let and do.
- Values have **types** such as **int**, **float**, **string**, and **bool**. When performing calculations, the type defines which calculations can be done.
- Finding errors in programs is called **debugging**, and **unit-testing** is a form of debugging.
- **Functions** are a type of value and defined using a let-binding. They are used to encapsulate code to make the code easier to read and understand and to make code reusable.

- The **conditional if-then-else** expression is used to control what code is to be executed at **runtime**
- **Recursion** and **while**-loops are programming structure to execute the same code several times.
- **Mutable values** are in contrast to **immutable values** may change value over time, and makes programmer harder to understand.
- **Comments** are **in-code documentation** and are ignored by the computer but serve as an important tool for communication between programmers.

Chapter 3

Using F# as a Calculator

Abstract tada - Introductory text about the objectivs of this chapter

• ...

In this chapter, we will exclusively use the interactive mode to illustrate basic types and operations in F#.

3.1 Literals and Basic Types

All programs rely on processing of data, and an essential property of data is its *type*. A *literal* is a fixed value like the number 3, and if we type the number 3 in an interactive session at the input prompt, then F# responds as shown in Listing 3.1. What this means is that F# has inferred the type to be *int* and bound it to the

```
Listing 3.1: Typing the number 3.

1 > 3;;
2 val it : int = 3
```

identifier it. For more on binding and identifiers see Chapter 4. Types matter, since the operations that can be performed on integers, are quite different from those that can be performed on, e.g., strings. Therefore, the number 3 has many different representations as shown in Listing 3.2. Each literal represents the number 3, but their types are different, and hence they are quite different values. The types int for integer numbers, float for floating point numbers, bool for Boolean values, char for characters, and string for strings of characters are the most common types of literals. A table of all basic types predefined in F# is given in Table 3.1. In addition

Listing 3.2: Many representations of the number 3 but using different types. 1 > 3;; 2 val it : int = 3 4 > 3.0;; 5 val it : float = 3.0 6 7 > '3';; 8 val it : char = '3' 9 10 > "3";; 11 val it : string = "3"

| Metatype | Type name | Description |
|-----------|-------------|--|
| Boolean | bool | Boolean values true or false |
| Integer | <u>int</u> | Integer values from -2,147,483,648 to 2,147,483,647 |
| | byte | Integer values from 0 to 255 |
| | sbyte | Integer values from -128 to 127 |
| | int8 | Synonymous with sbyte |
| | uint8 | Synonymous with byte |
| | int16 | Integer values from -32768 to 32767 |
| | uint16 | Integer values from 0 to 65535 |
| | int32 | Synonymous with int |
| | uint32 | Integer values from 0 to 4,294,967,295 |
| | int64 | Integer values from -9,223,372,036,854,775,808 to |
| | | 9,223,372,036,854,775,807 |
| | uint64 | Integer values from 0 to 18,446,744,073,709,551,615 |
| Real | float | 64-bit IEEE 754 floating point value from $-\infty$ to ∞ |
| | double | Synonymous with float |
| | single | A 32-bit floating point type |
| | float32 | Synonymous with single |
| | decimal | A floating point data type that has at least 28 significant digits |
| Character | char | Unicode character |
| | string | Unicode sequence of characters |
| None | <u>unit</u> | The value () |
| Object | obj | An object |
| Exception | exn | An exception |

Table 3.1 List of some of the basic types. The most commonly used types are underlined. For a description of integer see Appendix B.1, for floating point numbers see Appendix B.2, for ASCII and Unicode characters see Appendix C, for objects see Chapter 23, and for exceptions see Chapter 13.

to these built-in types, F# is designed such that it is easy to define new types.

Humans like to use the *decimal number* system for representing numbers. Decimal numbers are *base* 10, which means that a value is represented as two sequences of decimal digits separated by a *decimal point*, where each *digit d* has a position and a value $d \in \{0, 1, 2, ..., 9\}$. The part before the decimal point is called the *whole part* and the part after is called the *fractional part* of the number. An *integer* is a number with only a whole part and neither a decimal point nor a fractional part. As an example 35.7 is a decimal number, whose value is $3 \cdot 10^1 + 5 \cdot 10^0 + 7 \cdot 10^{-1}$, and

128 is an integer, whose value is $1 \cdot 10^2 + 2 \cdot 10^1 + 8 \cdot 10^0$. In F#, a decimal number is called a *floating point number*. Floating point numbers may alternatively be given using *scientific notation*, such as 3.5e-4 and 4e2, where the e-notation is translated to a value as $3.5e-4 = 3.5 \cdot 10^{-4} = 0.00035$, and $4e2 = 4 \cdot 10^2 = 400$.

The basic unit of information in almost all computers is the binary digit or *bit* for short. Internally, programs and data are all represented as bits, hence F# has a strong support for binary numbers. A *binary number* consists of a sequence of binary digits separated by a decimal point, where each digit can have values $b \in \{0, 1\}$, and the base is 2. E.g., the binary number $101.01_2 = 1 \cdot 2^2 + 0 \cdot 2^1 + 1 \cdot 2^0 + 0 \cdot 2^{-1} + 1 \cdot 2^{-2} = 5.25$. Subscripts are often used to indicate the base of a number, e.g., 101.01_2 and 101.01_{10} are different numbers. Since base 10 is so common, the subscript for base 10 numbers is often omitted.

Binary numbers are closely related to *octal* and *hexadecimal numbers*. Octals uses 8 as basis and hexadecimals use 16 as basis. Each octal digit can be represented by exactly three bits, and each hexadecimal digit can represented by exactly four bits. The hexadecimal digits use 0-9 to represent the values 0-9 and a-f in lower or alternatively upper case to represent the values 10-15. Thus, Octals and hexadecimals conveniently serve as shorthand for the much longer binary representation. As examples, the octal number 37_8 is $3 \cdot 8^1 + 7 \cdot 8^0 = 31$, and the hexadecimal number f_{316} is $15 \cdot 16^1 + 3 \cdot 16^0 = 243$.

To denote integers in bases different than 10, F# uses the prefix '0b' for binary, '0o' for octal, and '0x' for hexadecimal numbers. For example, the value 367₁₀ may be written as an integer 367, as a binary number 0b101101111, as a octal number 0o557, and as a hexadecimal number 0x16f. In F#, the character sequences 0b12 and ff are not recognized as numbers.

A *character* is a *Unicode code point*, and character literals are enclosed in single quotation marks. Appendix C.3 contains more details on code points. The character type in F# is denoted *char*. Examples of characters are 'a', 'D', '3', and examples of non-characters are '23' and 'abc'. Some characters, such as the tabulation character, do not have a visual representation. These can still be represented as a character using *escape sequences*. A character escape sequence starts with "\" followed by letter for simple escapes such as \t for tabulation and \n for newline. Escape sequences can also be a numerical representation of a code point, and three versions exist: The trigraph \DDD, where D is a decimal digit, is used to specify the first 256 code points, the hexadecimal escape codes \uXXXX, where X is a hexadecimal digit, is used to specify the first 65536 code points, and \UXXXXXXXX is used to specify any of the approximately 4.3 · 10⁹ possible code points. All escape sequences are shown in Table 3.2. Examples of char representations of the letter 'a' are: 'a', '\097', '\u00061', '\u000000061'.

A *string* is a sequence of characters enclosed in double quotation marks. Examples are "a", "this is a string", and "-&#\@". Note that the string "a" and the

| Character | Escape sequence | Description |
|-----------|-----------------|--|
| BS | \b | Backspace |
| LF | \n | Line feed |
| CR | \r | Carriage return |
| HT | \t | Horizontal tabulation |
| \ | // | Backslash |
| " | \" | Quotation mark |
| , | \' | Apostrophe |
| BEL | \a | Bell |
| FF | \f | Form feed |
| VT | \v | Vertical tabulation |
| | ∖uXXXX, | Unicode character ('X' is any hexadecimal digit, and 'D' |
| | \UXXXXXXX, | is any decimal digit) |
| | \DDD | |

Table 3.2 Escape characters. The escapecode \DDD is sometimes called a tricode.

character 'a' are not the same. Some strings are so common that they are given special names: One or more spaces " " is called *whitespace*, and both "\n" and "\r\n" are called *newline*. The escape-character "\" may be used to break a line in two. This and other examples are shown in Listing 3.3. Note that the response from

fsharpi is shown in double quotation marks, but this is not part of the string.

F# supports *literal types*, where the type of a literal is indicated as a prefix or suffix as shown in Table 3.3.

The literal type is closely connected to how the values are represented internally. For example, a value of type int32 use 32 bits and can be both positive and negative, while a uint32 value also use 32 bits, but is unsigned. A byte is an 8-bit number, and sbyte is a signed 8-bit number. Values of type float use 64 bits, while float32 only uses 32 bits. The number of bits used to represent numbers directly relates to the range and precession these types can represent. This is summarized in Table 3.1 and discussed in more detail in Appendix B. String literals may be *verbatim* by the @-

| Туре | syntax | Examples | Value |
|-----------------|------------------------------|------------------|------------------------------|
| int, int32 | <int xint="" =""></int> | 3, 0x3 | 3 |
| | <int xint="" ="">l</int> | 31, 0x31 | |
| uint32 | <int xint="" ="">u</int> | 3u | 3 |
| | <int xint="" ="">ul</int> | 3ul | |
| byte, uint8 | <int xint="" ="">uy</int> | 97uy | 97 |
| | ' <char>'B</char> | 'a'B | |
| byte[] | " <string>"B</string> | "a\n"B | [97uy; 10uy] |
| | @" <string>"B</string> | @"a\n"B | [97uy; 92uy; 110uy] |
| sbyte, int8 | <int xint="" ="">y</int> | 3y | 3 |
| int16 | <int xint="" ="">s</int> | 3s | 3 |
| uint16 | <int xint="" ="">us</int> | 3us | 3 |
| int64 | <int xint="" ="">L</int> | 3L | 3 |
| uint64 | <int xint="" ="">UL</int> | 3UL | 3 |
| | <int xint="" ="">uL</int> | 3uL | |
| float, double | <float></float> | 3.0 | 3.0 |
| | <xint>LF</xint> | 0x013LF | 9.387247271e-323 |
| single, float32 | <float>F</float> | 3.0F | 3.0 |
| | <float>f</float> | 3.0f | 3.0 |
| | <xint>lf</xint> | 0x0131f | 4.4701421e-43f |
| decimal | <float int="" ="">M</float> | 3.0M, 3M | 3.0 |
| | <float int="" ="">m</float> | 3.0m, 3m | |
| string | " <string>"</string> | "\"quote\".\n" | "quote". <newline></newline> |
| | @" <string>"</string> | @"""quote"".\n" | "quote".\n. |
| | """ <string>"""</string> | """"quote".\n""" | "quote".\n |

Table 3.3 List of literal types. The syntax notation <> means that the programmer replaces the brackets and content with a value of the appropriate form. The <xint> is one of the integers on hexadecimal, octal, or binary forms such as 0x17, 0o21, and 0b10001. The [| |] brackets means that the value is an array, see Section 20.3 for details.

notation or triple double quotation marks, meaning that the escape sequences are not converted to their code point. The two types of string verbatim treat quotation marks differently, as illustrated in the table. Further examples are shown in Listing 3.4.

Many basic types are compatible, and the type of a literal may be changed by typecasting. An example of casting to a float is shown in Listing 3.5. When float is given an argument, then it acts as a function rather than a type, and for the integer 3 it returns the floating point number 3.0. For more on functions see Chapter 4. Boolean values are often treated as the integer values 0 and 1, but no short-hand function names exist for their conversions. Instead, use functions from the System.Convert family of functions, as demonstrated in Listing 3.6. Here System.Convert.ToBoolean is the identifier of a function ToBoolean, which is a member of the class Convert that is included in the namespace System. Namespaces, classes, and members will be discussed in Chapter 18.

Typecasting is often a destructive operation, e.g., typecasting a float to int removes the fractional part without rounding as shown in Listing 3.7. Here we typecasted to a lesser type, in the sense that the set of integers is a subset of floating point numbers, and this is called *downcasting*. The opposite is called *upcasting* and is often non-destructive, as Listing 3.5 showed. Since floating point numbers are a superset of

Listing 3.4: Named and implied literals. val it : int = 3> 4u;; val it : uint32 = 4u> 5.6;; val it : float = 5.6> 7.9f;; val it : float32 = 7.9000001f> 'A';; val it : char = 'A' > 'B'B;; val it : byte = 66uy > "ABC";; val it : string = "ABC" > @"abc\nde";; val it : string = "abc\nde"

```
Listing 3.5: Casting an integer to a floating point number.

1 > float 3;;
2 val it : float = 3.0
```

```
Listing 3.6: Casting booleans.

1 > System.Convert.ToBoolean 1;;
2 val it : bool = true

3 
4 > System.Convert.ToBoolean 0;;
5 val it : bool = false

6 
7 > System.Convert.ToInt32 true;;
8 val it : int = 1

9 
10 > System.Convert.ToInt32 false;;
11 val it : int = 0
```

integers, the value is retained. As a side note, *rounding* a number y.x, where y is the *whole part* and x is the *fractional part*, is the operation of mapping numbers in the interval $y.x \in [y.0, y.5)$ to y, and those in $y.x \in [y.5, y+1)$ to y+1. This can

```
Listing 3.7: Fractional part is removed by downcasting.

| > int 357.6;;
| val it : int = 357
```

be performed by downcasting, as shown in Listing 3.8. I.e., 357.6 + 0.5 = 358.1

```
Listing 3.8: Rounding by modified downcasting.

1 > int (357.6 + 0.5);;
2 val it : int = 358
```

and removing the fractional part by downcasting results in 358, which is the correct answer.

3.2 Operators on Basic Types

Expressions are the basic building block of all F# programs, and this section will discuss operator expressions on basic types. A typical calculation, such used in Listing 3.8, is

$$\underbrace{357.6}_{\text{operand}} \quad \underbrace{+}_{\text{operand}} \quad \underbrace{0.5}_{\text{operand}}$$
 (3.1)

is an example of an arithmetic *expression*, and the above expression consists of two *operands* and an *operator*. Since this operator takes two operands, it is called a *binary operator*. The expression is written using *infix notation*, since the operands appear on each side of the operator.

In order to discuss general programming structures, we will use a simplified language to describe valid syntactical structures. In this simplified language, the syntax of basic binary operators is shown in the following.

```
Listing 3.9: Syntax for a binary expression.

| <expr><op><expr>
```

Here <expr> is any expression supplied by the programmer, and <op> is a binary infix operator. F# supports a range of arithmetic binary infix operators on its built-in types, such as addition, subtraction, multiplication, division, and exponentiation, using the "+", "-", "*", "/", "**" lexemes, respectively. Not all operators are defined for all types, e.g., addition is defined for integer and float types as well as for characters and strings, but multiplication is only defined for integer and floating-point types. A complete list of built-in operators on basic types is shown in Table 3.4 and 3.5, and a range of mathematical functions is shown in Table 3.6. Note that expressions can themselves be arguments to expressions, and thus, 4+5+6 is also a legal statement. Technically, F# interprets the expression as (4+5)+6 meaning that first 4+5 is evaluated according the <expr> <op> <expr> syntax. Then the result replaces the parenthesis to yield 9+6, which, once again, is evaluated according to the <expr> <op> <expr> syntax to give 15. This is called recursion, which is the

| Operator | bool | ints | floats | char | string | Example | Result | Description |
|----------|----------|--------------|--------|------|--------|-----------------|--------------|------------------------------|
| + | | / | ✓ | ✓ | ✓ | 5 + 2 | 7 | Addition |
| - | | ✓ | ✓ | | | 5.0 - 2.0 | 3.0 | Subtraction |
| * | | \checkmark | ✓ | | | 5 * 2 | 10 | Multiplication |
| / | | \checkmark | ✓ | | | 5.0 / 2.0 | 2.5 | Division |
| % | | \checkmark | ✓ | | | 5 % 2 | 1 | Remainder |
| ** | | | ✓ | | | 5.0 ** 2.0 | 25.0 | Exponentiation |
| + | | \checkmark | ✓ | | | +3 | 3 | identity |
| - | | \checkmark | ✓ | | | -3.0 | -3.0 | negation |
| && | ✓ | | | | | true && false | false | boolean and |
| | / | | | | | true false | true | boolean or |
| not | ✓ | | | | | not true | false | boolean negation |
| &&& | | \checkmark | | | | 0b101 &&& 0b110 | 0b100 | bitwise boolean and |
| | | \checkmark | | | | 0b101 0b110 | 0b111 | bitwise boolean or |
| ^ ^ ^ | | \checkmark | | | | 0b101 ^^^ 0b110 | 0b011 | bitwise boolean exclusive or |
| <<< | | √ | | | | 0b110uy <<< 2 | 0b11000uy | bitwise left shift |
| >>> | | \checkmark | | | | 0b110uy >>> 2 | 0b1uy | bitwise right shift |
| ~~~ | | ✓ | | | | ~~~0b110uy | 0b11111001uy | bitwise boolean negation |

Table 3.4 Arithmetic operators on basic types. Ints and floats means all built-in integer and float types. Note that for the bitwise operations, digits 0 and 1 are taken to be true and false.

| Operator | bool | ints | floats | char | string | Example | Result | Description |
|----------|----------|--------------|--------------|--------------|--------------|--------------|--------|-----------------------|
| < | √ | ✓ | ✓ | \checkmark | ✓ | true < false | false | Less than |
| > | ✓ | \checkmark | \checkmark | \checkmark | \checkmark | 5 > 2 | true | Greater than |
| = | ✓ | ✓ | ✓ | \checkmark | \checkmark | 5.0 = 2.0 | false | Equal |
| <= | ✓ | \checkmark | ✓ | \checkmark | \checkmark | 'a' <= 'b' | true | Less than or equal |
| >= | ✓ | \checkmark | ✓ | \checkmark | \checkmark | "ab" >= "cd" | false | Greater than or equal |
| <> | ✓ | ✓ | ✓ | \checkmark | ✓ | 5 <> 2 | true | Not equal |

Table 3.5 Comparison operators on basic types. Types cannot be mixed, e.g., 3<'a' is a syntax error.

name for a type of rule or function that uses itself in its definition. See Chapter 7 for more on recursive functions.

Unary operators take only one argument and have the syntax:

```
Listing 3.10: A unary expressions.
```

An example of a unary operator is -3, where - here is used to negate a positive integer. Since the operator appears before the operand, it is a *prefix operator*.

The concept of *precedence* is an important concept in arithmetic expressions. If parentheses are omitted in Listing 3.8, then F# will interpret the expression as (int 357.6) + 0.5, which is erroneous since the addition of an integer with a

| Operator | bool | ints | floats | nar | string | | | |
|----------|------|--------------|--------------|-----|----------|---------------|---------|------------------------|
| _ 0 | ã | ÷Ξ | Ψ̈́ | ਹ | Š | Example | Result | Description |
| abs | | > | \checkmark | | | abs -3 | 3 | Absolute value |
| acos | | | \checkmark | | | acos 0.8 | 0.644 | Inverse cosine |
| asin | | | \checkmark | | | asin 0.8 | 0.927 | Inverse sinus |
| atan | | | ✓ | | | atan 0.8 | 0.675 | Inverse tangent |
| atan2 | | | ✓ | | | atan2 0.8 2.3 | 0.335 | Inverse tangentvariant |
| ceil | | | √ | | | ceil 0.8 | 1.0 | Ceiling |
| cos | | | ✓ | | | cos 0.8 | 0.697 | Cosine |
| exp | | | ✓ | | | exp 0.8 | 2.23 | Natural exponent |
| floor | | | \checkmark | | | floor 0.8 | 0.0 | Floor |
| log | | | √ | | | log 0.8 | -0.223 | Natural logarithm |
| log10 | | | √ | | | log10 0.8 | -0.0969 | Base-10 logarithm |
| max | | \checkmark | √ | ✓ | √ | max 3.0 4.0 | 4.0 | Maximum |
| min | | \checkmark | √ | ✓ | √ | min 3.0 4.0 | 3.0 | Minimum |
| pown | | \checkmark | | | | pown 3 2 | 9 | Integer exponent |
| round | | | √ | | | round 0.8 | 1.0 | Rounding |
| sign | | \checkmark | ✓ | | | sign -3 | -1 | Sign |
| sin | | | ✓ | | | sin 0.8 | 0.717 | Sinus |
| sqrt | | | √ | | | sqrt 0.8 | 0.894 | Square root |
| tan | | | \checkmark | | | tan 0.8 | 1.03 | Tangent |

Table 3.6 Predefined functions for arithmetic operations.

float is undefined. This is an example of precedence, i.e., function evaluation takes precedence over addition which means that function evaluation is performed first and addition second. Consider the arithmetic expression shown in Listing 3.11. Here, the

```
Listing 3.11: A simple arithmetic expression.

1 > 3 + 4 * 5;;
2 val it : int = 23
```

addition and multiplication functions are shown in infix notation with the *operator* lexemes "+" and "*". To arrive at the resulting value 23, F# has to decide in which order to perform the calculation. There are 2 possible orders, 3 + (4 * 5) and (3 + 4) * 5 that gives different results. For integer arithmetic, the correct order is, of course, multiplication before addition, and we say that multiplication takes *precedence* over addition. Every atomic operation that F# can perform is ordered in terms of its precedence, and for some common built-in operators shown in Table 3.7, the precedence is shown by the order they are given in the table.

Associativity describes the order in which calculations are performed for binary operators of the same precedence. Some operator's associativity are given in Table 3.7. In the table we see that "*" is left associative, which means that 3.0 * 4.0 * 5.0 is evaluated as (3.0 * 4.0) * 5.0. Conversely, ** is right associative, so 4.0**3.0**2.0 is evaluated as 4.0**(3.0**2.0). For some operators, like multiplication, association matters little, e.g., 4*3*2=4*(3*2)=(4*3)*2, and for other operators, like exponentiation, association makes a huge difference, e.g.,

| Operator | Associativity | Description |
|---|---------------|--|
| + <expr></expr> | Left | Unary identity, negation, and bitwise negation operators |
| - <expr></expr> | | |
| ~~ <expr></expr> | | |
| f <expr></expr> | Left | Function application |
| <expr> ** <expr></expr></expr> | Right | Exponentiation |
| <expr> * <expr></expr></expr> | Left | Multiplication, division and remainder |
| <expr> / <expr></expr></expr> | | |
| <expr> % <expr></expr></expr> | | |
| <expr> + <expr></expr></expr> | Left | Addition and subtraction binary operators |
| <expr> - <expr></expr></expr> | | |
| <expr> ^^^ <expr></expr></expr> | Right | Bitwise exclusive or |
| <expr> < <expr></expr></expr> | Left | Comparison operators, bitwise shift, and bitwise 'and' |
| <expr> <= <expr></expr></expr> | | and 'or'. |
| <expr> > <expr></expr></expr> | | |
| <expr> >= <expr></expr></expr> | | |
| <expr> = <expr></expr></expr> | | |
| <expr> <> <expr></expr></expr> | | |
| <expr> <<< <expr></expr></expr> | | |
| <expr> >>> <expr></expr></expr> | | |
| <expr> &&& <expr></expr></expr> | | |
| <expr> <expr></expr></expr> | | |
| <expr> && <expr></expr></expr> | Left | Boolean and |
| <expr> <expr></expr></expr> | Left | Boolean or |

Table 3.7 Some common operators, their precedence, and their associativity. Rows are ordered from highest to lowest precedences, such that <*expr*> * <*expr*> has higher precedence than <*expr*> + <*expr*>. Operators in the same row have the same precedence.

 \star 4^(3²) \neq (4³)². Examples of this is shown in Listing 3.12. Whenever in doubt of

association or any other basic semantic rules, it is a good idea to use parentheses. It is also a good idea to test your understanding of the syntax and semantic rules by making a simple script.

3.3 Boolean Arithmetic

Boolean arithmetic is the basis of almost all computers and particularly important for controlling program flow, which will be discussed in Chapter 21. Boolean values are one of 2 possible values, true or false, which is also sometimes written as 1 and 0. Basic operations on Boolean values are 'and', 'or', and 'not', which in F# are written respectively as the binary operators &&, ||, and the function not. Since the domain of Boolean values is so small, all possible combination of input on these values can be written on the tabular form, known as a *truth table*, and the truth tables for the basic Boolean operators and functions are shown in Table 3.8. A good mnemonic

| a | b | a && b | a b | not a |
|-------|-------|--------|--------|-------|
| false | false | false | false | true |
| false | true | false | true | true |
| true | false | false | true | false |
| true | true | true | true | false |

Table 3.8 Truth table for boolean 'and', 'or', and 'not' operators. Value 0 is false and 1 is true.

for remembering the result of the 'and' and 'or' operators is to use 1 for true, 0 for false, multiplication for the Boolean 'and' operator, and addition for the Boolean 'or' operator, e.g., true and false in this mnemonic translates to $1 \cdot 0 = 0$, and the result translates back to the Boolean value false. In F#, the truth table for the basic Boolean operators can be produced by a program, as shown in Listing 3.13. Here, we used

```
Listing 3.13: Boolean operators and truth tables.
> printfn "a b a*b a+b not a"
  printfn "%A %A %A %A %A'
    false false (false && false) (false || false) (not false)
  printfn "%A %A %A %A %A'
    false true (false && true) (false || true) (not false)
  printfn "%A %A %A %A %A"
    true false (true && false) (true || false) (not true)
  printfn "%A %A %A %A %A"
     true true (true && true) (true || true) (not true);;
a b a*b a+b not a
false false false true
false true false true true
true false false true false
true true true false
val it : unit = ()
```

the printfn function to present the results of many expressions on something that resembles a tabular form. The spacing produced using the printfn function is not elegant, and in ?? we will discuss better options for producing more beautiful output. Notice that the arguments for printfn was given on the next line with indentation. The indentation is an important part of telling F# which part of what you write belong together. This is an example of the so-called lightweight syntax. Generally,

F# ignores newlines and whitespaces except when using the lightweight syntax. The difference between verbose and lightweight syntax is discussed in Chapter 4.

3.4 Integer Arithmetic

The set of integers is infinitely large, but since all computers have limited resources, it is not possible to represent it in its entirety. The various integer types listed in Table 3.1 are finite subsets reduced by limiting their ranges. An in-depth description of integer implementation can be found in Appendix B. The type int is the most common type.

Table 3.4–3.6 give examples of operators and functions pre-defined for integer types. Notice that fewer functions are available for integers than for floating point numbers. For most addition, subtraction, multiplication, and negation, the result is straightforward. However, performing arithmetic operations on integers requires extra care, since the result may cause *overflow* and *underflow*. For example, an sbyte is specified using the "y"-literal and can hold values [-128...127]. This causes problems in the example in Listing 3.14. Here 100+30=130, which is larger than the biggest

```
Listing 3.14: Adding integers may cause overflow.

1 > 100y;;
2 val it : sbyte = 100y
3 
4 > 30y;;
5 val it : sbyte = 30y
6 
7 > 100y + 30y;;
8 val it : sbyte = -126y
```

sbyte, and the result is an overflow. Similarly, we get an underflow, when the arithmetic result falls below the smallest value storable in an sbyte, as demonstrated in Listing 3.15. I.e., we were expecting a negative number but got a positive number

```
Listing 3.15: Subtracting integers may cause underflow.

1 > -100y - 30y;;
2 val it : sbyte = 126y
```

instead.

The overflow error in Listing 3.14 can be understood in terms of the binary representation of integers: In binary, $130 = 10000010_2$, and this binary pattern is interpreted differently as byte and sbyte, see Listing 3.16. That is, for signed bytes, the leftmost bit is used to represent the sign, and since the addition of $100 = 01100100_2$ and $30 = 00011110_b$ is $130 = 10000010_2$, which causes the left-most bit to be used,

Listing 3.16: The leftmost bit is interpreted differently for signed and unsigned integers, which gives rise to potential overflow errors.

```
1 > 0b10000010uy;;
2 val it : byte = 130uy
3
4 > 0b10000010y;;
5 val it : sbyte = -126y
```

this is wrongly interpreted as a negative number when stored in an sbyte. Similar arguments can be made explaining underflows.

The operator discards the fractional part after division, and the *integer remainder* operator calculates the remainder after integer division, as demonstrated in Listing 3.17. Together, the integer division and remainder can form a lossless representation of

Listing 3.17: Integer division and remainder operators.

```
1 > 7 / 3;;

2 val it : int = 2

3 

4 > 7 % 3;;

5 val it : int = 1
```

the original number, see Listing 3.18. Here we see that integer division of 7 by 3

Listing 3.18: Integer division and remainder is a lossless representation of an integer, compare with Listing 3.17.

```
1 > (7 / 3) * 3;;

2 val it : int = 6

3

4 > (7 / 3) * 3 + (7 % 3);;

5 val it : int = 7
```

followed by multiplication by 3 is less than 7, and that the difference is 7 % 3.

Notice that neither overflow nor underflow error gave rise to an error message, which is why such bugs are difficult to find. Dividing any non-zero number by 0 is infinite, which is also outside the domain of any of the integer types, but in this case, F# casts an *exception*, as shown in Listing 3.19. The output looks daunting at first sight, but the first and last lines of the error message are the most important parts, which tell us what exception was cast and why the program stopped. The middle contains technical details concerning which part of the program caused the error and can be ignored for the time being. Exceptions are a type of *runtime error*, and are discussed in Chapter 13

Integer exponentiation is not defined as an operator but is available as the built-in function pown. This function is demonstrated in Listing 3.20 for calculating 2^5 .


```
Listing 3.20: Integer exponent function.

1 > pown 2 5;;
2 val it : int = 32
```

For binary arithmetic on integers, the following operators are available: <leftExpr> <<< <ri>deftExpr>, which shifts the bit pattern of <leftExpr> <rightExpr> positions to the left while inserting 0's to right; <leftExpr> >>> <rightExpr>, which shifts the bit pattern of <leftExpr> <rightExpr> positions to the right while inserting 0's to left; ~~~ <expr> returns a new integer, where all 0 bits are changed to 1 bits and vice-versa; <expr> && <expr> returns the result of taking the Boolean 'and' operator position-wise; <expr> ||| <expr> returns the result of taking the Boolean 'or' operator position-wise; and <expr> ^^^ <expr> returns the result of the Boolean 'xor' operator defined by the truth table in Table 3.9.

| a | b | a ^^^ b |
|-------|-------|---------|
| false | false | false |
| false | true | true |
| true | false | true |
| true | true | false |

Table 3.9 Boolean exclusive or truth table.

3.5 Floating Point Arithmetic

Like integers, the set of reals is also infinitely large, hence, floating point types are finite subsets reduced by sampling the space of reals. An in-depth description of floating point implementations can be found in Appendix B. The type float is the most common type.

Table 3.4–3.6 give examples of operators and functions pre-defined for floating point types. Note that the remainder operator for floats calculates the remainder after division and discards the fractional part, see Listing 3.21. The remainder for

Listing 3.21: Floating point division and remainder operators. 1 > 7.0 / 2.5;; 2 val it : float = 2.8 3 > 7.0 % 2.5;; 5 val it : float = 2.0

floating point numbers can be fractional, but division, discarding fractional part, and the remainder is still a lossless representation of the original number, as demonstrated in Listing 3.22.

Listing 3.22: Floating point division, downcasting, and remainder is a lossless representation of a number.

```
1 > float (int (7.0 / 2.5));;
2 val it : float = 2.0
3
4 > (float (int (7.0 / 2.5))) * 2.5;;
5 val it : float = 5.0
6
7 > (float (int (7.0 / 2.5))) * 2.5 + 7.0 % 2.5;;
8 val it : float = 7.0
```

Arithmetic using float will not cause over- and underflow problems, since the IEEE 754 standard includes the special numbers $\pm \infty$ and NaN. As shown in Listing 3.23, no exception is thrown. However, the float type has limited precision, since there

Listing 3.23: Floating point numbers include infinity and Not-a-Number.

```
1 > 1.0/0.0;;
2 val it : float = infinity
3
4 > 0.0/0.0;;
5 val it : float = nan
```

is only a finite number of numbers that can be stored in a float. E.g., addition and subtraction can give surprising results, as demonstrated in Listing 3.24. That is,

Listing 3.24: Floating point arithmetic has finite precision.

```
1 > 357.8 + 0.1 - 357.9;;
2 val it : float = 5.684341886e-14
```

addition and subtraction associates to the left, hence the expression is interpreted as (357.8 + 0.1) - 357.9 and we see that we do not get the expected 0. The reason is that the calculation is done stepwise, and in the process, the numbers are represented using the imprecise floating point standard. Thus, 357.8 + 0.1 is

represented as a number close to but not identical to what 357.9 is represented as, and thus, when subtracting these two representations, we get a very small nonzero number. Such errors tend to accumulate, and comparing the result of expressions of

* floating point values should, therefore, be treated with care. Thus, equivalence of two floating point expressions should only be considered up to sufficient precision, e.g., comparing 357.8 + 0.1 and 357.9 up to 1e-10 precision should be tested as, abs ((357.8 + 0.1) - 357.9) < 1e-10.

3.6 Char and String Arithmetic

Addition is the only operator defined for characters. Nevertheless, character arithmetic is often done by casting to an integer. A typical example is the conversion of character case, e.g., to convert the lowercase character 'z' to uppercase. Here, we use the *ASCIIbetical order*, add the difference between any Basic Latin Block letters in upper- and lowercase as integers, and cast back to char, see Listing 3.25. I.e., the

```
Listing 3.25: Converting case by casting and integer arithmetic.

| > char (int 'z' - int 'a' + int 'A');;
| val it : char = 'Z' |
```

code point difference between upper and lower case for any alphabetical character 'a' to 'z' is constant, hence we can change case by adding or subtracting the difference between any corresponding character. Unfortunately, this does not generalize to characters from other languages.

A large collection of operators and functions exist for string. The simplest is concatenation using the "+" operator, as demonstrated in Listing 3.26. Characters

```
Listing 3.26: Example of string concatenation.

| 'hello' + " " + "world";;
| val it : string = "hello world"
```

and strings cannot be concatenated, which is why the above example used the string of a space " "instead of the space character ' '. The characters of a string may be indexed as using the . [] notation. This is demonstrated in Listing 3.27. Notice that the first character has index 0, and to get the last character in a string, we use the string's length property. This is done as shown in Listing 3.28. Since index counting starts at 0, and since the string length is 7, the index of the last character is 6. There is a long list of built-in functions in System.String for working with strings, some of which will be discussed in Section 3.8.

The *dot notation* is an example of Structured programming, where technically speaking, the string "abcdefg" is an immutable *object* of *class* string, [] is an object

method, and Length is a property. For more on objects, classes, and methods, see Chapter 23.

Strings are compared letter by letter. For two strings to be equal, they must have the same length and all the letters must be identical. E.g., "abs" = "absalon" is false, while "abs" = "abs" is true. The "<>" operator is the boolean negation of the "=" operator, e.g., "abs" <> "absalon" is true, while "abs" <> "abs" is false. For the "<", "<=", ">", and ">=" operators, the strings are ordered alphabetically, such that "abs" < "absalon" && "absalon" < "milk" is true, that is, the "<" operator on two strings is true if the left operand should come before the right when sorting alphabetically. The algorithm for deciding the boolean value of left0p < right0p is as follows: we start by examining the first character, and if left0p. [0] and rightOp. [0] are different, then leftOp < rightOp is equal to leftOp. [0] < rightOp.[0]. E.g., "milk" < "abs" is the same as 'm' < 'a', which is false, since the letter 'm' does not come before the letter 'a' in the alphabet, or more precisely, the codepoint of 'm' is not less than the codepoint of 'a'. If left0p. [0] and rightOp. [0] are equal, then we move on to the next letter and repeat the investigation, e.g., "abe" < "abs" is true, since "ab" = "ab" is true and 'e' < 's' is true. If we reach the end of either of the two strings, then the shorter word is smaller than the longer word, e.g., "abs" < "absalon" is true, while "abs" < "abs" is false. The "<=", ">", and ">=" operators are defined in a similar manner.

3.7 Tuples

Tuples are a direct extension of constants. They are immutable and have neither concatenations nor indexing operations. Tuples are unions of immutable types and have the following syntax:

```
Listing 3.29: Tuples are list of expressions separated by commas.

| <expr>{, <expr>}
```

Tuples are identified by the "," lexeme and often enclosed in parentheses, but that is not required. An example is a triple, also known as a 3-tuple, (2, true, "hello"). In interactive mode, the type of tuples is demonstrated in Listing 3.30. The values

```
Listing 3.30: Tuple types are products of sets.

1 > let tp = (2, true, "hello")
2 - printfn "%A" tp;;
3 (2, true, "hello")
4 val tp : int * bool * string = (2, true, "hello")
5 val it : unit = ()
```

2, true, and "hello" are *members*, and the number of elements of a tuple is its *length*. From the response of F#, we see that the tuple is inferred to have the type int * bool * string. The "*" denotes the Cartesian product between sets. Tuples can be products of any types and follow the lexical scope rules like value and function bindings. Notice also that a tuple may be printed as a single entity by the %A placeholder. In the example we bound tp to the tuple. The opposite is also possible, as demonstrated in Listing 3.31. In this example, a function is defined

```
Listing 3.31: Definition of a tuple.

1 > let deconstructNPrint tp =
2 - let (a, b, c) = tp
3 - printfn "tp = (%A, %A, %A)" a b c
4 -
5 - deconstructNPrint (2, true, "hello")
6 - deconstructNPrint (3.14, "Pi", 'p');
7 tp = (2, true, "hello")
8 tp = (3.14, "Pi", 'p')
9 val deconstructNPrint : 'a * 'b * 'c -> unit
10 val it : unit = ()
```

that takes 1 argument, a 3-tuple. If we wanted a function with 3 arguments, then the function binding should have been let deconstructNPrint a b c = The value binding let (a, b, c) = tp, binds a tuple with 3 named members to a value, thus deconstructing it in terms of its members. This is called pattern matching and will be discussed in further details in Chapter 11. Since we used the \M placeholder in the printfn function, the function can be called with 3-tuples of

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different types. F# informs us that the tuple type is variable by writing 'a * 'b * 'c. The "'" notation means that the type can be decided at run-time, see Section 12.6 for more on variable types.

Pairs or 2-tuples are so common that F# includes two built-in functions, fst and snd, to extract the first and second element of a pair. This is demonstrated in Listing 3.32.

```
Listing 3.32 pair.fsx:

Deconstruction of pairs with the built-in functions fst and snd.

1 let pair = ("first", "second")
2 printfn "fst(pair) = %s, snd(pair) = %s" (fst pair) (snd pair)

1 $ fsharpc --nologo pair.fsx && mono pair.exe
2 fst(pair) = first, snd(pair) = second
```

Tuples of equal lengths can be compared, and the comparison is defined similarly to string comparison. Tuples of equal length are compared element by element. E.g., (1,2) = (1,3) is false, while (1,2) = (1,2) is true. The "<>" operator is the boolean negation of the "=" operator. For the "<", "<=", ">", and ">=" operators, the strings are ordered lexicographically, such that ('a', 'b', 'c') < ('a', 'b', 's') && ('a', 'b', 's') < ('c', 'o', 's') is true, that is, the "<" operator on two tuples is true if and only if the left operand should come before the right when sorting alphabetically. See Listing 3.33 for an example. The algorithm for deciding the boolean value of (a1, a2) < (b1, b2) is as follows: we start by examining the first elements, and if a1 and b1 are different, then the result of (a1, a2) < (b1, b2) is equal to the result of a1 < b1. If a1 and b1 are equal, then we move on to the next letter and repeat the investigation. The "<=", ">", and ">=" operators are defined similarly.

Binding tuples to mutables does not make the tuple mutable. This is demonstrated in Listing 3.34. However, it is possible to define a mutable variable of type tuple such that new tuple values can be assigned to it, as shown in Listing 3.35. Mutable tuples are value types, meaning that binding to new names makes copies, not aliases, as demonstrated in Listing 3.36. The use of tuples shortens code and highlights semantic content at a higher level, e.g., instead of focusing on the elements, tuples focus on their union. While this may look elegant and short there is the risk of *obfuscation*, i.e., writing compact code that is difficult to read, where an unprepared reader of the code may not easily understand the computation nor appreciate its elegance without an accompanying explanation. Hence, always keep an eye out for compact and concise ways to write code, but never at the expense of readability.

Listing 3.33 tupleCompare.fsx: Tuples comparison is similar to string comparison. let lessThan (a, b, c) (d, e, f) = if a <> d then a < d elif b <> e then b < d elif c <> f then c < f else false let printTest x y = printfn "%A < %A is %b" x y (lessThan x y) let a = ('a', 'b', 'c'); let b = ('d', 'e', 'f'); let c = ('a', 'b', 'b'); let d = ('a', 'b', 'd'); printTest a b printTest a c printTest a d s fsharpc --nologo tupleCompare.fsx && mono tupleCompare.exe ('a', 'b', 'c') < ('d', 'e', 'f') is true ('a', 'b', 'c') < ('d', 'e', 'f') is false ('a', 'b', 'c') < ('a', 'b', 'b', 'b') is false ('a', 'b', 'c') < ('a', 'b', 'd') is true

```
Listing 3.34 tupleOfMutables.fsx:

A mutable changes value, but the tuple defined by it does not refer to the new value.

1 let mutable a = 1
1 let mutable b = 2
1 let c = (a, b)
4 printfn "%A, %A, %A" a b c
5 a <- 3
6 printfn "%A, %A, %A" a b c

1 $ fsharpc --nologo tupleOfMutables.fsx && mono tupleOfMutables.exe
2 1, 2, (1, 2)
3 3, 2, (1, 2)
```

3.8 Strings

Strings have been discussed in Chapter 3, the content of which will be briefly revisited here followed by a description of some of the many supporting built-in functions in F# on strings.

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Listing 3.35 mutable Tuple.fsx: A mutable tuple can be assigned a new value. 1 let mutable pair = 1,2 2 printfn "%A" pair 3 pair <- (3,4) 4 printfn "%A" pair 1 \$ fsharpc --nologo mutable Tuple.fsx && mono mutable Tuple.exe 2 (1, 2) 3 (3, 4)

```
Listing 3.36 mutable Tuple Value.fsx:

A mutable tuple is a value type.

let mutable pair = 1,2
let mutable aCopy = pair
pair <- (3,4)
printfn "%A %A" pair aCopy

fsharpc --nologo mutable Tuple Value.fsx && mono mutable Tuple Value.exe
(3, 4) (1, 2)
```

A *string* is a sequence of characters. Each character is represented using UTF-16, see Appendix C for further details on the unicode standard. The type string is an alias for *System.string*. String literals are delimited by double quotation marks "" and inside the delimiters, character escape sequences are allowed (see Table 3.2), which are replaced by the corresponding character code. Examples are "This is a string", "\tTabulated string", "A \"quoted\" string", and "". Strings may span several lines, and new lines inside strings are part of the string unless the line is ended with a backslash. Strings may be *verbatim* by preceding the string with "@", in which case escape sequences are not replaced, but two double quotation marks are an escape sequence which is replaced by a one double quotation mark. Examples of "@"-verbatim strings are:

```
@"This is a string",@"\tNon-tabulated string",@"A ""quoted"" string", and
```

@"".

Alternatively, a verbatim string may be delimited by three double quotation marks. Examples of """"-verbatim strings are:

```
"""This is a string""","""\tNon-tabulated string""","""A "quoted" string""", and"""""".
```

Strings may be indexed using the . [] notation, as demonstrated in Listing 3.27.

3.8.1 String Properties and Methods

Strings have a few properties which are values attached to each string and accessed using the "." notation. The only to be mentioned here is:

```
IndexOf(): str:string -> int.
```

Returns the index of the first occurrence of s or -1, if str does not appear in the string.

```
Listing 3.37: IndexOf()

1 > "Hello World".IndexOf("World");;
2 val it : int = 6
```

Length: int.

Returns the length of the string.

```
Listing 3.38: Length

| > "abcd".Length;;
| val it : int = 4
```

ToLower(): unit -> string.

Returns a copy of the string where each letter has been converted to lower case.

```
Listing 3.39: ToLower()

| > "aBcD".ToLower();;
| val it : string = "abcd"
```

ToUpper(): unit -> string.

Returns a copy of the string where each letter has been converted to upper case.

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```
Listing 3.40: ToUpper()

1 > "aBcD".ToUpper();;

val it : string = "ABCD"
```

Trim(): unit -> string.

Returns a copy of the string where leading and trailing whitespaces have been removed.

```
Listing 3.41: Trim()

1 > " Hello World ".Trim();;
2 val it : string = "Hello World"
```

Split(): unit -> string [].

Splits a string of words separated by spaces into an array of words. See Section 20.3 for more information about arrays.

```
Listing 3.42: Split()

| > "Hello World".Split();;
| val it : string [] = [|"Hello"; "World"|]
```

3.8.2 The String Module

The String module offers many functions for working with strings. Some of the most powerful ones are listed below, and they are all higher-order functions.

String.collect: f:(char -> string) -> str:string -> string.

Creates a new string whose characters are the results of applying f to each of the characters of str and concatenating the resulting strings.

```
Listing 3.43: String.collect

1 > String.collect (fun c -> (string c) + ", ") "abc";;
2 val it : string = "a, b, c, "
```

String.exists: f:(char -> bool) -> str:string -> bool.

Returns true if any character in str evaluates to true when using f.

```
Listing 3.44: String.exists

1 > String.exists (fun c -> c = 'd') "abc";;
2 val it : bool = false
```

String.forall: f:(char -> bool) -> str:string -> bool.

Returns true if all characters in str evalutes to true when using f.

```
Listing 3.45: String.forall

1 > String.forall (fun c -> c < 'd') "abc";;

2 val it : bool = true
```

String.init: n:int -> f:(int -> string) -> string.

Creates a new string with length n and whose characters are the result of applying f to each index of that string.

```
Listing 3.46: String.init

| > String.init 5 (fun i -> (string i) + ", ");;
| val it : string = "0, 1, 2, 3, 4, "
```

String.iter: f:(char -> unit) -> str:string -> unit.
Applies f to each character in str.

```
Listing 3.47: String.iter

1 > String.iter (fun c -> printfn "%c" c) "abc";;
2 a
3 b
4 c
5 val it : unit = ()
```

String.map: f:(char -> char) -> str:string -> string.
Creates a new string whose characters are the results of applying f to each of
the characters of str.

```
Listing 3.48: String.map

1 > let toUpper c = c + char (int 'A' - int 'a')
2 - String.map toUpper "abcd";;
3 val toUpper : c:char -> char
4 val it : string = "ABCD"
```

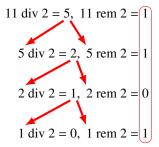
3.9 Programming Intermezzo: Hand Conversion Between Decimal and Binary Numbers

Conversion of integers between decimal and binary form is a key concept one must grasp in order to understand some of the basic properties of calculations on the computer. Converting from binary to decimal is straightforward if using the power-of-two algorithm, i.e., given a sequence of n + 1 binary digits b_i written as

 $b_n b_{n-1} \dots b_0$, and where b_n and b_0 are the most and least significant bits respectively, then the decimal value is calculated as,

$$v = \sum_{i=0}^{n} b_i 2^i \tag{3.2}$$

For example, $10011_2 = 1 + 2 + 16 = 19$. Converting from decimal to binary is a little more complex, but a simple divide-by-two algorithm exists. The key to understanding the divide-by-two algorithm is to realize that dividing a number by two is equivalent to shifting its binary representation one position to the right. E.g., $10 = 1010_2$ and $10/2 = 5 = 101_2$. Odd numbers have $b_0 = 1$, e.g., $11_{10} = 1011_2$ and $11_{10}/2 = 5.5 = 101.1_2$. Hence, if we divide any number by two and get a non-integer number, then its least significant bit was 1. Another way to express this is to say that the least significant bit is the remainder after integer division by two. Sequential application of this idea leads directly to the divide-by-two algorithm. E.g., if we were to convert the number 11_{10} in decimal form to binary form, we would perform the following steps:



Here we used div and rem to signify the integer division and remainder operators. The algorithm stops when the result of integer division is zero. Reading off the remainder from below and up, we find the sequence 1011_2 , which is the binary form of the decimal number 11_{10} . Using the interactive mode, we can perform the same calculation, as shown in Listing 3.49.

Listing 3.49: Converting the number 11_{10} to binary form. > printfn "(%d, %d)" (11 / 2) (11 % 2);; (5, 1) val it: unit = () > printfn "(%d, %d)" (5 / 2) (5 % 2);; (2, 1) val it: unit = () > printfn "(%d, %d)" (2 / 2) (2 % 2);; (1, 0) val it: unit = () > printfn "(%d, %d)" (1 / 2) (1 % 2);; (0, 1) val it: unit = ()

Thus, by reading the second integer-response from printfn from below and up, we again obtain the binary form of 11_{10} to be 1011_2 . For integers with a fractional part, the divide-by-two algorithm may be used on the whole part, while multiply-by-two may be used in a similar manner on the fractional part.

3.10 Key concepts and terms in this chapter

Summary text about the key concepts from this chapter

• ...

Chapter 4

Values, Functions, and Statements

Abstract tada - Introductory text about the objectivs of this chapter

• ...

In this chapter, we will see how we can bind expressions to identifiers either as new constants, functions, or operators, how this saves time when building large programs, and how this makes programs easier to read and debug. As an example, consider the following problem,

Problem 4.1

or given set constants a, b, and c, solve for x in

$$ax^2 + bx + c = 0 (4.1)$$

To solve for x we use the quadratic formula from elementary algebra,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a},\tag{4.2}$$

which gives the general solution for any values of the coefficients. Here, we will assume a positive discriminant, $b^2 - 4ac > 0$. In order to write a program where the code may be reused later, we define a function

discriminant : float -> float -> float -> float

that is, a function that takes 3 arguments, a, b, and c, and calculates the discriminant. Likewise, we will define

positiveSolution : float -> float -> float -> float

and

```
negativeSolution : float -> float -> float -> float
```

that also take the polynomial's coefficients as arguments and calculate the solution corresponding to choosing the positive and negative sign for \pm in the equation. Details on function definition is given in Section 4.2. Our solution thus looks like Listing 4.1. Here, we have further defined names of values a, b, and c which are

```
Listing 4.1 identifiersExample.fsx:
Finding roots for quadratic equations using function name binding.
let discriminant a b c = b ** 2.0 - 4.0 * a * c
let positiveSolution a b c = (-b + sqrt (discriminant a b c))
   /(2.0 * a)
let negativeSolution a b c = (-b - sqrt (discriminant a b c))
    / (2.0 * a)
let a = 1.0
let b = 0.0
 let c = -1.0
let d = discriminant a b c
let xp = positiveSolution a b c
let xn = negativeSolution a b c
do printfn "0 = %A * x ** 2.0 + %A * x + %A" a b c
do printfn " has discriminant %A and solutions %A and %A" d
    xn xp
$ fsharpc --nologo identifiersExample.fsx && mono
   identifiersExample.exe
  = 1.0 * x ** 2.0 + 0.0 * x + -1.0
   has discriminant 4.0 and solutions -1.0 and 1.0
```

used as inputs to our functions, and the results of function application are bound to the names d, xn, and xp. The names of functions and values given here are examples of identifiers, and with these, we may reuse the quadratic formulas and calculated values later, while avoiding possible typing mistakes and reducing the amount of code which needs to be debugged.

The use of identifiers is central in programming. For F#, not to be confused with built-in functionality, identifiers must follow a specific set of rules:

Identifier

- Identifiers are used as names for values, functions, types etc.
- They must start with a Unicode letter or underscore '_', but can be followed by zero or more of letters, digits, and a range of special characters except for

SP, LF, and CR (space, line feed, and carriage return). See Appendix C.3 for more on codepoints that represents letters.

- They can also be a sequence of identifiers separated by a period.
- They cannot be keywords, see Table 4.1.

| Type | Keyword |
|-------------------|--|
| Regular | abstract, and, as, assert, base, begin, class, default, delegate, do, done, downcast, downto, elif, else, end, exception, extern, false, finally, for, fun, function, global, if, in, inherit, inline, interface, internal, lazy, let, match, member, module, mutable, namespace, new, null, of, open, or, override, private, public, rec, return, sig, static, struct, then, to, true, try, type, upcast, use, val, void, when, while, with, and yield. |
| Reserved | atomic, break, checked, component, const, constraint, constructor, continue, eager, fixed, fori, functor, include, measure, method, mixin, object, parallel, params, process, protected, pure, recursive, sealed, tailcall, trait, virtual, and volatile. |
| Symbolic | <pre>let!, use!, do!, yield!, return!, , ->, <-, ., :, (,), [,], [<, >], [,], {,}, ', #, :?>, :?, :>,, ::, :=, ;;, ;, =, _, ?, ??, (*), <@, @>, <@@, and @@>.</pre> |
| Reserved symbolic | ~ and ` |

Table 4.1 Table of (possibly future) keywords and symbolic keywords in F#.

Examples of identifiers are: a, theCharacter9, Next_Word, _tok, and f.sharp.rocks. Since programmers often work in multilingual environment dominated by the English language it is advicable to restrict identifiers to use letters from the English alphabet, numbers, period, and '_'. However, the number of possible identifiers is enormous. The full definition refers to the Unicode general categories described in Appendix C.3, and there are currently 19.345 possible Unicode code points in the letter category and 2.245 possible Unicode code points in the special character category.

Identifiers may be used to carry information about their intended content and use, and careful selection of identifiers can aid programmers to communicate thoughts about the code. Thus, identifiers are often a word or several concatenated words conveying some relevant meaning. For example, in the function definition let discriminant a b c = b ** 2.0 - 4.0 * a * c, the function identifier has been chosen to be discriminant. F# places no special significance to the word 'discriminant', and the program would work exactly the same had the function been called let f a b c = b ** 2.0 - 4.0 * a * c. However, to programmers, the word 'discriminant' informs us of the intended role of the function and thus is much preferred. This is a general principle: **identifier names should be chosen to reflect their semantic value.**. The arguments a, b, and c are short, but adheres to a textbook tradition of elementary algebra. Again, we might as well have used, let discriminant c a b = a ** 2.0 - 4.0 * c * b, which is semantically identical to the original expression, but due to tradition, this would con-

- * fuse most readers of the code. Thus, identifier names should be chosen consistently with the readers' traditions. Finally, identifiers are often concatenations of words, as positiveSolution in Listing 4.1. Concatenations can be difficult to read. Without the capitalization of the second word, we would have had positivesolution. This is readable at most times, but takes longer time to understand in general. Typical solutions are to use a separator, such as positive_solution, lower camel case also known as mixed case as in the example positiveSolution, and upper camel case also known as pascal case as PositiveSolution. In this book, we use lower camel case except where F# requires a capital first letter. Again, the choice does not influence what a program does, only how readable it is to a fellow programmer.
- The important part is that identifier names consisting of concatenated words are often preferred over names with few character, and concatenation should be emphasized, e.g., by camel casing. Choosing the length of identifier names is a balancing act, since when working with large programs, very long identifier names can be tiresome to write, and a common practice is that the length of identifier names is proportional to the complexity of the program. I.e., complex programs use long names, simple programs use short names. What is complex and what is simple is naturally in the eye of the beholder, but when you program, remember that a future reader of the program most likely has not had time to work with the problem as long
- **★** as the programmer, thus **choose identifier names as if you were to explain the meaning of a program to a knowledgeable outsider.**

Another key concept in F# is expressions. An expression can be a mathematical expression, such as 3*5, a function application, such as f3, and many other things. Central in this chapter is the binding of values and functions to identifiers, which is done with the keyword let, e.g., let a = 1.0.

Expressions are the main workhorse of F# and have an enormous variety in how they may be written. We will in this book gradually work through some of the more important facets.

Expressions

- An Expression is a computation such as 3 * 5.
- They can be value bindings between identifiers and expressions that evaluate to a value or a function, see Sections 4.1 and 4.2.
- They can be do-bindings that produce side-effects and whose result are ignored, see Section 4.2
- They can be assignments to variables, see Section 4.1.
- They can be a sequence of expressions separated with the ";" lexeme.
- They can be annotated with a type by using the ":" lexeme.

Before we begin a deeper discussion on bindings, note that F# adheres to two different syntaxes: *verbose* and *lightweight*. In the verbose syntax, newlines and whitespaces are generally ignored, while in lightweight syntax, certain keywords and lexemes may be replaced by newlines and whitespaces. The lightweight syntax is the most common, but the syntaxes may be mixed, and we will highlight the options, when relevant.

4.1 Value Bindings

Binding identifiers to literals, or expressions that are evaluated to be values, is called *value-binding*, and examples are let a = 3.0 and let b = cos 0.9. Value bindings have the following syntax:

```
Listing 4.2: Value binding expression.

| let <valueIdent> = <bodyExpr> [in <expr>]
```

The <code>let</code> keyword binds a value-identifier with an expression. The above notation means that <code><valueIdent></code> is to be replaced with a name and <code><bodyExpr></code> with an expression that evaluates to a value. The following square bracket notation [] means that the enclosed is optional, and <code>F#</code> is able to identify whether or not the optional part is used as signified by the optional presence of the <code>in</code> keyword. If the <code>in</code> keyword is used, then the value-identifier is a local definition in the <code><expr></code> expression, and it is not available in later lines. For lightweight syntax, the <code>in</code> keyword is replaced with a newline, and the binding <code>is</code> available in later lines until the end of the scope it is defined in.

For example, letting the identifier p be bound to the value 2.0 and using it in an expression is done as shown in Listing 4.3. F# will ignore most newlines between lexemes, i.e., the above is equivalent to writing as shown in Listing 4.4. F# also allows for an alternative notation called *lightweight syntax*, where e.g., the in keyword is replaced with a newline, and the expression starts on the next line at the same column as let starts in, i.e., the above is equivalent to Listing 4.5. The same expression in interactive mode will also show with the inferred types, as shown in Listing 4.6. By the val keyword in the line val p: float = 2.0, we see that p is inferred to be of type float and bound to the value 2.0. The inference is based on the type of the right-hand-side which is float. Identifiers may be defined to have a type using the

Listing 4.5 letValueLightWeight.fsx:

Listing 4.3 letValue.fsx: The identifier p is used in the expression following the keyword. 1 let p = 2.0 in do printfn "%A" (3.0 ** p) 1 \$ fsharpc --nologo letValue.fsx && mono letValue.exe 2 9.0

```
Listing 4.4 letValueLF.fsx:

Newlines after make the program easier to read.

let p = 2.0 in
do printfn "%A" (3.0 ** p)

state of the program easier to read.

fsharpc --nologo letValueLF.fsx && mono letValueLF.exe

9.0
```

```
Lightweight syntax does not require the keyword, but the expression must be aligned with the keyword.

1 let p = 2.0
2 do printfn "%A" (3.0 ** p)

1 $ fsharpc --nologo letValueLightWeight.fsx && mono letValueLightWeight.exe
2 9.0
```

```
Listing 4.6: Interactive mode also outputs inferred types.

1 > let p = 2.0
2 - do printfn "%A" (3.0 ** p);;
3 9.0
4 val p : float = 2.0
5 val it : unit = ()
```

":" lexeme, but the types on the left-hand-side and right-hand-side of the "=" lexeme must be identical. Mixing types gives an error, as shown in Listing 4.7. Here, the left-hand-side is defined to be an identifier of type float, while the right-hand-side is a literal of type integer.

An expression can be a sequence of expressions separated by the lexeme ";", see Listing 4.8. The lightweight syntax automatically inserts the ";" lexeme at newlines, hence using the lightweight syntax, the above is the same as shown in Listing 4.9.

A key concept of programming is *scope*. When F# seeks the value bound to a name, it looks left and upward in the program text for its let-binding in the present or higher

Listing 4.7 letValueTypeError.fsx: Binding error due to type mismatch. 1 let p : float = 3 2 do printfn "%A" (3.0 ** p) 1 \$ fsharpc --nologo letValueTypeError.fsx && mono letValueTypeError.exe 2 letValueTypeError.fsx(1,17): error FS0001: This expression was expected to have type 'float' 5 but here has type 'int'

```
Listing 4.8 letValueSequence.fsx:
A value-binding for a sequence of expressions.

1 let p = 2.0 in do printfn "%A" p; do printfn "%A" (3.0 ** p)

1 $ fsharpc --nologo letValueSequence.fsx && mono letValueSequence.exe
2 2.0
3 9.0
```

```
Listing 4.9 letValueSequenceLightWeight.fsx:

A value-binding for a sequence using lightweight syntax.

let p = 2.0
do printfn "%A" p
do printfn "%A" (3.0 ** p)

state="block" fixed by the content of t
```

scopes, see Listing 4.10 for an example. This is called lexical scope. Some special

```
Listing 4.10 letValueScopeLower.fsx:
Redefining identifiers is allowed in lower scopes.

1 let p = 3 in let p = 4 in do printfn " %A" p;

1 $ fsharpc --nologo letValueScopeLower.fsx && mono letValueScopeLower.exe
2 4
```

bindings are mutable, in which case F# uses the *dynamic scope*, that is, the value of a binding is defined by when it is used. This will be discussed in Section 20.1.

Scopes are given levels, and scopes may be nested, where the nested scope has a level one lower than its parent. F# distinguishes between the top and lower levels, and at the top level in the lightweight syntax, redefining values is not allowed, as shown in Listing 4.11. However, using parentheses, we create a *code block*, i.e., a *nested*

Listing 4.11 letValueScopeLowerError.fsx: Redefining identifiers is not allowed in lightweight syntax at top level. 1 let p = 3 2 let p = 4 3 do printfn "%A" p; 1 \$ fsharpc --nologo -a letValueScopeLowerError.fsx 2 letValueScopeLowerError.fsx(2,5): error FS0037: Duplicate definition of value 'p'

scope, and then redefining is allowed, as demonstrated in Listing 4.12. Nevertheless,

```
Listing 4.12 letValueScopeBlockAlternative3.fsx:

A block may be created using parentheses.

1 (
2 let p = 3
3 let p = 4
4 do printfn "%A" p
5 )

1 $ fsharpc --nologo letValueScopeBlockAlternative3.fsx && mono letValueScopeBlockAlternative3.exe
2 4
```

★ avoid reusing names unless it's in a deeper scope.

Inside the block in Listing 4.12 we used indentation, which is good practice, but not required here.

Bindings inside a nested scope are not available outside, as shown in Listing 4.13. Nesting is a natural part of structuring code, e.g., through function definitions to be discussed in Section 4.2 and flow control structures to be discussed in Chapter 21. Blocking code by nesting is a key concept for making robust code that is easy to use by others, without the user necessarily needing to know the details of the inner workings of a block of code.

Listing 4.13 letValueScopeNestedScope.fsx: Bindings inside a scope are not available outside. 1 let p = 3 2 (3 let q = 4 4 do printfn "%A" q 5) 6 do printfn "%A %A" p q 1 \$ fsharpc --nologo -a letValueScopeNestedScope.fsx 2 3 letValueScopeNestedScope.fsx(6,22): error FS0039: The value or constructor 'q' is not defined.

Defining blocks is used for controlling the extent of a lexical scope of bindings. For example, adding a second printfn statement, as in Listing 4.14, will print the value 4, last bound to the identifier p, since F# interprets the above as let p = 3 in let p = 4 in (printfn "%A" p; printfn "%A" p). Had we intended

```
Listing 4.14 letValueScopeBlockProblem.fsx:

Overshadowing hides the first binding.

1 let p = 3 in let p = 4 in do printfn "%A" p; do printfn "%A" p

1 $ fsharpc --nologo letValueScopeBlockProblem.fsx && mono letValueScopeBlockProblem.exe

2 4
3 4
```

to print the two different values of p, then we should have created a block as in Listing 4.15.

```
Listing 4.15 letValueScopeBlock.fsx:

Blocks allow for the return to the previous scope.

1 let p = 3 in (let p = 4 in do printfn "%A" p); do printfn "%A" p;

1 $ fsharpc --nologo letValueScopeBlock.fsx && mono letValueScopeBlock.exe

2 4
3 3
```

4.2 Function Bindings

A function is a mapping between an input and output domain. A key advantage of using functions when programming is that they encapsulate code into smaller units, that are easier to debug and may be reused. F# is a functional first programming language and offers a number of alternative methods for specifying parameters, which will be discussed in this section. Binding identifiers to functions follows a syntax similar to value-binding,

```
Listing 4.16: Function binding expression

| let <funcIdent> <arg> {<arg>} | () = <bodyExpr> [in <expr>]
```

where <type> is a name of an existing type. The argument types are given in parentheses, and the return type is given last.

Functions are a key concept in F#, and in this chapter we will discuss the very basics. Recursive functions will be discussed in Chapter 21 and higher-order functions in Chapter 8.

An example of defining a function and using it in interactive mode is shown in Listing 4.18. Here we see that the function is interpreted to have the type val sum

```
Listing 4.18: An example of a binding of an identifier and a function.

1 > let sum (x : float) (y : float) : float = x + y in

2 - let c = sum 357.6 863.4 in

3 - do printfn "%A" c;;

4 1221.0

5 val sum : x:float -> y:float -> float

6 val c : float = 1221.0

7 val it : unit = ()
```

: x:float -> y:float -> float. The "->" lexeme means a mapping between sets, in this case, floats. The function is also a higher-order function, to be discussed

in detail below, and here it suffices to think of sum as a function that takes 2 floats as argument and returns a float.

Not all types need to be declared, just a sufficient number for F# to be able to infer the types for the full statement. For the example, one is sufficient, and we could just have declare the type of the result, as in Listing 4.19. Or even just one of the

```
Listing 4.19 letFunctionAlterantive.fsx:
Not every type needs to be declared.

1 let sum x y : float = x + y
```

arguments, as in Listing 4.20. In both cases, since the + operator is only defined for

```
Listing 4.20 letFunctionAlterantive2.fsx:

Just one type is often enough for F# to infer the rest.

1 let sum (x : float) y = x + y
```

operands of the same type, declaring the type of either arguments or result implies the type of the remainder. As for values, lightweight syntax automatically inserts the keyword **in** and the lexeme ";", as shown in Listing 4.21.

```
Listing 4.21 letFunctionLightWeight.fsx:
Lightweight syntax for function definitions.

1 let sum x y : float = x + y
2 let c = sum 357.6 863.4
3 do printfn "%A" c

1 $ fsharpc --nologo letFunctionLightWeight.fsx && mono letFunctionLightWeight.exe
2 1221.0
```

Arguments need not always be inferred to types, but may be of the generic type when *type safety* is ensured, as shown in Listing 4.22. Here, the function second does not use the first argument x, which therefore can be of any type, and which F#, therefore, calls 'a. The type of the second element, y, can also be of any type and not necessarily the same as x, so it is called 'b. Finally, the result is the same type as y, whatever it is. This is an example of a *generic function*, since it will work on any type.

A function may contain a sequence of expressions but must return a value. E.g., the quadratic formula may be written as shown in Listing 4.23. Here, we used the lightweight syntax, where the "=" identifies the start of a nested scope, and F# identifies the scope by indentation. The amount of space used for indentation does not matter, but all lines in the same scope must use the same amount. The scope ends before the first line with the previous indentation or none. Notice how the last

Listing 4.22: Type safety implies that a function will work for any type.

```
1 > let second x y = y
2 - let a = second 3 5
3 - do printfn "%A" a
4 - let b = second "horse" 5.0
5 - do printfn "%A" b;;
6 5
7 5.0
8 val second : x:'a -> y:'b -> 'b
9 val a : int = 5
10 val b : float = 5.0
11 val it : unit = ()
```

Listing 4.23 identifiers Example Advance. fsx: A function may contain sequences of expressions.

```
let solution a b c sgn =
  let discriminant a b c =
   b ** 2.0 - 4.0 * a * c
  let d = discriminant a b c
  (-b + sgn * sqrt d) / (2.0 * a)
let a = 1.0
let b = 0.0
let c = -1.0
let xp = solution a b c +1.0
let xn = solution a b c -1.0
do printfn "0 = %A * x ** 2.0 + %A * x + %A" a b c
do printfn " has solutions %A and %A" xn xp
$ fsharpc --nologo identifiersExampleAdvance.fsx && mono
   identifiersExampleAdvance.exe
0 = 1.0 * x ** 2.0 + 0.0 * x + -1.0
  has solutions -1.0 and 1.0
```

expression is not bound to an identifier, but is the result of the function, i.e., in contrast to many other languages, F# does not have an explicit keyword for returning values, but requires a final expression, which will be returned to the caller of the function. Note also that since the function discriminant is defined in the nested scope of solution, and because the scope ends before let a = 1.0, discriminant cannot be called outside solution.

Listing 4.24 lexicalScopeNFunction.fsx: Lexical scope means that f(z) = 3x and not 4x at the time of calling. 1 let testScope x =2 let a = 3.03 let f(z) = 3x and not 4x at the time of calling. 1 let testScope x =2 let a = 4.05 f(x)6 do printfn "%A" (testScope 2.0)

value or function immediately at the place of definition. Since a and 3.0 are synonymous in the first lines of the program, the function f is really defined as let f z = 3.0 * z.

Functions do not need a name, but may be declared as an *anonymous function* using the *fun* keyword and the "->" lexeme, as shown in Listing 4.25. Here, a

```
Listing 4.25 functionDeclarationAnonymous.fsx:
Anonymous functions are functions as values.

1 let first = fun x y -> x
2 do printfn "%d" (first 5 3)

1 $ fsharpc --nologo functionDeclarationAnonymous.fsx && mono functionDeclarationAnonymous.exe
2 5
```

name is bound to an anonymous function which returns the first of two arguments. The difference to let first x y = x is that anonymous functions may be treated as values, meaning that they may be used as arguments to other functions and the new values may be reassigned to their identifiers when mutable, as will be discussed in Section 20.1. A common use of anonymous functions is as arguments to other functions, as demonstrated in Listing 4.26. Note that here apply is given 3 arguments: the function mul and 2 integers. It is not given the result of mul 3 6, since that would not match the definition of apply. Anonymous functions and functions as arguments are powerful concepts, but tend to make programs harder to read, and their use should be limited.

The result of one function is often used as an argument of another. This is function composition, and an example is shown in Listing 4.27. In the example we combine two functions f and g by storing the result of f 2 in a and using that as argument of g. This is the same as g (f 2), and in the later case, the compile creates a temporary value for f 2. Such compositions are so common in F# that a special set

Listing 4.26 functionDeclarationAnonymousAdvanced.fsx:
Anonymous functions are often used as arguments for other functions.

Listing 4.27 functionComposition.fsx: Composing functions using intermediate bindings.

```
let f x = x + 1
let g x = x * x

let a = f 2
let b = g a
let c = g (f 2)
do printfn "a = %A, b = %A, c = %A" a b c

fsharpc --nologo functionComposition.fsx && mono functionComposition.exe
a = 3, b = 9, c = 9
```

of operators has been invented, called the *piping* operators: "/>" and "</". They are used as demonstrated in Listing 4.28. The example shows regular composition,

```
Listing 4.28 functionPiping.fsx:

Composing functions by piping.

1 let f x = x + 1
2 let g x = x * x
3
4 let a = g (f 2)
5 let b = 2 |> f |> g
6 let c = g <| (f <| 2)
7 do printfn "a = %A, b = %A, c = %A" a b c

1 $ fsharpc --nologo functionPiping.fsx && mono functionPiping.exe
2 a = 9, b = 9, c = 9
```

left-to-right, and right-to-left piping. The word piping is a picturial description of data as if it were flowing through pipes, where functions are connection points of pipes distributing data in a network. The three expressions in Listing 4.28 perform the same calculation. The left-to-right piping in line 5 corresponds to the left-to-

A *procedure* is a generalization of the concept of functions, and in contrast to functions, procedures need not return values. This is demonstrated in Listing 4.30. In F#, this is automatically given the unit type as the return value. Procedural

```
Listing 4.30 procedure.fsx:
A procedure is a function that has no return value, and in F# returns "()".

1 let printIt a = printfn "This is '%A'" a
2 do printIt 3
3 do printIt 3.0

1 $ fsharpc --nologo procedure.fsx && mono procedure.exe
2 This is '3'
3 This is '3.0'
```

thinking is useful for *encapsulation* of scripts, but is prone to *side-effects*. For this reason, it is adviced to **prefer functions over procedures.** More on side-effects in \star Section 20.1.

In F#, functions (and procedures) are *first-class citizens*, which means that functions are values: They may be passed as arguments, returned from a function, and bound to a name. For first-class citizens, the name it is bound to does not carry significance to the language, as, e.g., illustrated with the use of anonymous functions. Technically, a function is stored as a *closure*. A closure is a description of the function, its arguments, its expression, and the environment at the time it was created, i.e., the triple (*args*, *exp*, *env*). Consider the listing in Listing 4.31. It defines two functions

mul and applyFactor, where the latter is a higher-order function taking another function as an argument and uses part of the environment to produce its result. The two closures are:

$$mul: (args, exp, env) = ((x, y), (x * y), ())$$
(4.3)

applyFactor:
$$(args, exp, env) = ((x, fct), (body), (factor \rightarrow 2.0))$$
 (4.4)

where lazily write body instead of the whole function's body. The function mul does not use its environment, and everything needed to evaluate its expression are values for its arguments. The function applyFactor also takes two arguments, a function and a value. It uses factor from the environment, thus this is stored in its closure. When mul is given as an argument in Listing 4.31 line 8, then it is its closure which is given to applyFactor, and the closure contains everything that applyFactor requires to use mul. Likewise, if applyFactor is given as argument to yet another function, then its closure includes the relevant part of its environment at the time of definition, factor, such that when applyFactor is applied to two arguments, then its closure contains everything needed to evaluate its expression.

65 4.3 Operators

4.3 Operators

Operators are functions, and in F#, the infix multiplication operator + is equivalent to the function (+), as shown in Listing 4.32. All operators have this option, and you

```
Listing 4.32 addOperatorNFunction.fsx:

Operators have function equivalents.

1 let a = 3.0
2 let b = 4.0
3 let c = a + b
4 let d = (+) a b
5 do printfn "%A plus %A is %A and %A" a b c d

1 $ fsharpc --nologo addOperatorNFunction.fsx && mono addOperatorNFunction.exe
2 3.0 plus 4.0 is 7.0 and 7.0
```

may redefine them and define your own operators, but in F# names of user-defined operators are limited:

- A *unary operator* name can be: "+", "-", "+.", "--.", "%", "&", "&", "~~", "~~", "~~", "~~", "~~", "~~", "~~", ", "apostropheOp. Here apostropheOp is an operator name starting with "!" and followed by one or more of either "!", "%", "&", "*", "+", "-", ".", "/", "<", "=", ">", "@", "^", "|", "~", but apostropheOp cannot be "!=".

The precedence rules and associativity of user-defined operators follow the rules for which they share prefixes with built-in rules, see Table 3.7. For example, .*, +++, and <+ are valid operator names for infix operators, they have precedence as ordered, and their associativities are all left. Using ~ as the first character in the definition of an operator makes the operator unary and will not be part of the name. Examples of definitions and use of operators are, Operators beginning with * must use a space in its definition. For example, without a space (* would be confused with the beginning of a comment (*, see Section 5.2 for more on comments in the code.

Beware, redefining existing operators lexically redefines all future uses of the operators for all types, hence it is not a good idea to redefine operators, but better to

Listing 4.33 operatorDefinitions.fsx: Operators may be (re)defined by their function equivalent. let (.*) x y = x * y + 1 printfn "%A" (3 .* 4) let (+++) x y = x * y + y printfn "%A" (3 +++ 4) let (<+) x y = x < y + 2.0 printfn "%A" (3.0 <+ 4.0) $let (\sim +.) x = x+1$ printfn "%A" (+.1) \$ fsharpc --nologo operatorDefinitions.fsx && mono operatorDefinitions.exe 13 16 true 2

define new ones. In Chapter 23 we will discuss how to define type-specific operators, including prefix operators.

4.4 Do-Bindings

Aside from let-bindings that binds names with values or functions, sometimes we just need to execute code. This is called a *do*-binding or, alternatively, a *statement*. The syntax is as follows:

```
Listing 4.34: Syntax for do-bindings.

[do ]<expr>
```

The expression <expr> must return unit. The keyword do is optional in most cases, but using it emphasizes that the expression is not a function that returns a useful value. Procedures are examples of such expressions, and a very useful family of procedures are the printf family described below. In the remainder of this book, we will refrain from using the do keyword.

4.5 Conditional Expressions

Programs often contain code which should only be executed under certain conditions. This can be expressed with if-expressions, whose syntax is as follows.

```
Listing 4.35: Conditional expressions.

| if <cond> then <expr> {elif <cond> then <expr>} [else <expr>]
```

The condition <con> is an expression resulting in a Boolean value, and there can be zero or more elif conditions, as indicated by {}. Each expression <expr> is called a *branch*, and all branches must have the same type, such that regardless of which branch is chosen, the type of the result of the conditional expression is the same. Then the expression of the first if-branch, whose condition is true, is evaluate. If all conditions are false then the else-branch is evaluated. If no else expression is present, then "()" will be returned. See Listing 4.36 for a simple example. The

```
Listing 4.36 condition.fsx:

Conditions evaluate their branches depending on the value of the condition.

if true then printfn "hi" else printfn "bye"

if false then printfn "hi" else printfn "bye"

fsharpc --nologo condition.fsx && mono condition.exe

hi
bye
```

lightweight syntax allows for newlines entered everywhere, but indentation must be used to express scope.

To demonstrate conditional expressions, let us write a program which writes the sentence "I have n apple(s)", where the plural 's' is added appropriately for various n's. This is done in Listing 4.37, using the lightweight syntax. The sentence structure and its variants give rise to a more compact solution, since the language to be returned to the user is a variant of "I have/owe no/number apple(s)", i.e., certain conditions determine whether the sentence should use "have" and "owe" and so forth. So, we could instead make decisions on each of these sentence parts, and then built the final sentence from its parts. This is accomplished in the following example: While arguably shorter, this solution is also denser, and most likely more difficult to debug and maintain.

Note that both **elif** and **else** branches are optional, which may cause problems. For example, both

```
let a = if true then 3
```

Listing 4.37 conditionalLightweight.fsx: Using conditional expression to generate different strings. let applesIHave n = if n < -1 then"I owe " + (string -n) + " apples" elif n < 0 then "I owe " + (string -n) + " apple" elif n < 1 then "I have no apples" elif n < 2 then "I have 1 apple" else "I have " + (string n) + " apples" printfn "%A" (applesIHave -3) printfn "%A" (applesIHave -1) printfn "%A" (applesIHave 0) printfn "%A" (applesIHave 1) printfn "%A" (applesIHave 2) printfn "%A" (applesIHave 10) \$ fsharpc --nologo conditionalLightWeight.fsx && mono conditionalLightWeight.exe "I owe 3 apples" "I owe 1 apple" "I have no apples" "I have 1 apple" "I have 2 apples" "I have 10 apples"

and

```
let a = if true then 3 elif false then 4
```

are invalid, since F# is not smart enough to realize that the type of the expression is uniquely determined. Instead, F# looks for the else to ensure all cases have been covered, and that a always will be given a unique value of the same type regardless of the branch taken in the conditional statement. Hence,

```
let a = if true then 3 else 4
```

is the only valid expression of the 3. In practice, F# assumes that the omitted branch returns "()", and thus it is fine to say let a = if true then () and if true then printfn "hej". Nevertheless, it is good practice in F# to always include an else branch.

Listing 4.38 conditionalLightweightAlt.fsx: Using sentence parts to construct the final sentence. let applesIHave n = let haveOrOwe = if n < 0 then "owe" else "have"</pre> let pluralS = if $(n = 0) \mid \mid (abs n) > 1$ then "s" else "" let number = if n = 0 then "no" else (string (abs n)) "I " + haveOrOwe + " " + number + " apple" + pluralS printfn "%A" (applesIHave -3) printfn "%A" (applesIHave -1) printfn "%A" (applesIHave 0) printfn "%A" (applesIHave 1)
printfn "%A" (applesIHave 2)
printfn "%A" (applesIHave 10) \$ fsharpc --nologo conditionalLightWeightAlt.fsx && mono conditionalLightWeightAlt.exe "I owe 3 apples" "I owe 1 apple" "I have no apples" "I have 1 apple" "I have 2 apples" "I have 10 apples"

4.6 Tracing code by hand

The concept of Tracing by hand, will be developed throughout this book. Here we will concentrate in the basics, and as we introduce more complicated programming structures, we will develop the Tracing by hand accordingly. Tracing may seem tedious in the beginning, but in conjunction with strategically placed debugging printfn statements, it is a very valuable tool for debugging.

Consider the program in Listing 19.6. The program calls testScope 2.0, and by running the program, we see that the return-value is 6.0 and not 8.0, as we had expected. Hence, we will use tracing to understand the result.

Tracing a program by hand means that we simulate its execution and, as part of that, keep track of the bindings, assignments closures, scopes, and input and output of the program. To do this, we need to consider the concept of *environments*.

Environments describe bindings available to the program at the present scope and at a particular time and place in the code. There is always an outer environment, called E_0 , and each time we call a function or create a scope, we create a new environment. Only one environment can be active at a time, and it is updated as we simulate the execution of code with new bindings and temporary evaluations of expressions. Once

Listing 4.39 lexicalScopeTracing.fsx: Example of lexical scope and closure environment. 1 let testScope x = 2 let a = 3.0 3 let f z = a * z 4 let a = 4.0 5 f x 6 printfn "%A" (testScope 2.0) 1 \$ fsharpc --nologo lexicalScopeTracing.fsx && mono lexicalScopeTracing.exe 2 6.0

a scope is closed, then its environment is deleted and a return-value is transported to its enclosing environment. In tracing, we note return-values explicitly. Likewise, output from, e.g., printfn is reported with a special notation.

To trace code, we make a table with 4 columns: Step, Line, Environment, and Bindings and evaluations. The Step column enumerates the steps performed. The Line column contains the program-line treated in a step *where* the present environment is updated. The Environment contains the name of the present environment, and Bindings . . . shows *what* in the environment is updated.

The code in Listing 19.6 contains a function definition and a call, hence, the first lines of our table looks like,

```
Step Line Env. Bindings and evaluations

\begin{array}{c|cccc}
\hline
0 & - & E_0 & () \\
1 & 1 & E_0 & testScope = ((x), testScope-body, ()) \\
2 & 6 & E_0 & testScope = ?
\end{array}
```

The elements of the table is to be understood as follows. Step 0 initializes the outer environment. In order for us to remember that the environment is empty, we write the unit value "()". Reading the code from top to bottom, the first nonempty and noncomment line we meet is line 1, hence, in Step 1, we update the environment with the binding of a function to the name testScope. Since functions are values in F#, we note their bindings by their closures: a tuple of argument names, the function-body, and the values lexically available at the place of binding. See Section 4.2 for more information on closures. Following the function-binding, the printfn statement is called in line 6 to print the result testScope 2.0. However, before we can produce any output, we must first evaluate testScope 2.0. Since we do not yet know what this function evaluates to, in Step 2 we simply write the call with a question mark. The call causes the creation of a new environment, and we continue our table as follows,

```
Step Line Env. Bindings and evaluations

3  1  E_1  ((x = 2.0), testScope-body, ())
```

This means that we are going to execute the code in testScope-body. The function was called with 2.0 as argument, causing x = 2.0. Hence, the only binding available at the start of this environment is to the name x. In the testScope-body, we make 3 further bindings and a function call. First to a, then to f, then to another a, which will overshadow the previous binding, and finally we call f. Thus, our table is updated as follows.

Note that by lexical scope, the closure of f includes everything above its binding in E_1 , and therefore we add a = 3.0 and x = 2.0 to the environment element in its closure. This has consequences for the following call to f in line 5, which creates a new environment based on f's closure and the value of its arguments. The value of x in Step 7 is found by looking in the previous steps for the last binding to the name x in E_1 , which occurs in Step 3. Note that the binding to a name x in Step 5 is an internal binding in the closure of f and is irrelevant here. Hence, we continue the table as,

Step Line Env. Bindings and evaluations

8 3
$$E_2$$
 (($z = 2.0$), a * z, ($a = 3.0$, $x = 2.0$))

Executing the body of f, we initially have 3 bindings available: z = 2.0, a = 3.0, and x = 2.0. Thus, to evaluate the expression a * z, we use these bindings and write,

Step Line Env. Bindings and evaluations

9 3
$$E_2$$
 $a*z=6.0$
10 3 E_2 return = 6.0

The 'return'-word is used to remind us that this is the value to replace the question mark with in Step 7. Here we will make a mental note and not physically replace the question mark with the calculated value. If you are ever in doubt which call is connected with which return value, seek upwards in the table from the return statement for the first question mark. Now we delete E_2 and return to the enclosing environment, E_1 . Here the function call was the last expression, hence the return-value from testScope will be equal to the return-value from f, and we write,

Step Line Env. Bindings and evaluations

$$11 \quad 3 \quad E_1 \quad \text{return} = 6.0$$

Similarly, we delete E_1 and return to the question mark in Step 2, which is replaced by the value 6.0. We can now finish the printfn statement and produce the output,

```
Step Line Env. Bindings and evaluations

12 6 E_0 output = "6.0\n"
```

The return-value of a printfn statement is (), and since this line is the last of our program, we return () and end the program:

```
Step Line Env. Bindings and evaluations

\begin{array}{c|cccc}
13 & 6 & E_0 & \text{return} = ()
\end{array}
```

The full table is shown for completeness in Table 19.3. Hence, we conclude that

```
Step Line Env. Bindings and evaluations
0
          E_0 ()
          E_0 testScope = ((x), \text{testScope-body}, ())
1
          E_0 testScope 2.0 = ?
2
     6
3
          E_1 ((x = 2.0), testScope-body, ())
4
     2
          E_1 a = 3.0
5
     3
          E_1 f = ((z), a * z, (a = 3.0, x = 2.0))
6
     4
          E_1 a = 4.0
          E_1 f x = ?
     3
8
          E_2
               ((z = 2.0), a * z, (a = 3.0, x = 2.0))
     3
          E_2 a * z = 6.0
10
     3
          E_2 return = 6.0
     3
11
          E_1 return = 6.0
    6
          E_0 output = "6.0\n"
13
    6
          E_0 return = ()
```

Table 4.2 The complete table produced while tracing the program in Listing 19.6 by hand.

the program outputs the value 6.0, since the function f uses the first binding of a = 3.0, and this is because the binding of f to the expression a * z creates a closure with a lexical scope. Thus, in spite that there is an overshadowing value of a, when f is called, this binding is ignored in the body of f. To correct this, we update the code as shown in Listing 19.7.

4.7 Key concepts and terms in this chapter

Summary text about the key concepts from this chapter

• ...

Listing 4.40 lexicalScopeTracingCorrected.fsx:

Tracing the code in Listing 19.6 by hand produced the table in Table 19.3, and to get the desired output, we correct the code as shown here.

```
let testScope x =
let a = 4.0
let f z = a * z
f x
printfn "%A" (testScope 2.0)

$\f$ fsharpc --nologo lexicalScopeTracingCorrected.fsx && mono lexicalScopeTracingCorrected.exe

8.0
```

Chapter 5

Making programs and documenting them

Abstract tada - Introductory text about the objectivs of this chapter

• ...

5.1 7 step guide to making programs

. . .

5.2 Programming as a commication activity

Documentation is a very important part of writing programs, since it is most unlikely that you will be writing really obvious code. Moreover, what seems obvious at the point of writing may be mystifying months later to the author and to others. Documentation serves several purposes:

- 1. Communicate what the code should be doing.
- 2. Highlight big insights essential for the code.
- 3. Highlight possible conflicts and/or areas where the code could be changed later.

The essential point is that coding is a journey in problem-solving, and proper documentation is an aid in understanding the solution and the journey that lead to it.

Documentation is most often a mixture of in-code documentation and accompanying documents. Here, we will focus on in-code documentation which arguably causes problems in multi-language environments and run the risk of bloating code.

F# has two different syntaxes for comments. Comments can be block comments:

```
Listing 5.1: Block comments.

(*<any text>*)
```

The comment text (<any text>) can be any text and is stilled parsed by F# as keywords and basic types, implying that (* a comment (* in a comment *) *) and (* "*)" *) are valid comments, while (* " *) is invalid.

Alternatively, comments may also be line comments,

```
Listing 5.2: Line comments.

| //<any text>
```

where the comment text ends after the first newline.

The F# compiler has an option for generating *Extensible Markup Language (XML)* files from scripts using the C# documentation comments tags¹. The XML documentation starts with a triple-slash ///, i.e., a lineComment and a slash, which serve as comments for the code construct that follows immediately after. XML consists of tags which always appear in pairs, e.g., the tag "tag" would look like <tag>... </tag>. F# accept any tags, but recommends those listed in Table 5.1. If no tags are used, then it is automatically assumed to be a <summary>. An example of a documented script is shown in Listing 5.3. is:

Mono's fsharpc command may be used to extract the comments into an XML file, as demonstrated in Listing 5.4.

```
Listing 5.4, Converting in-code comments to XML.

$ fsharpc --doc:commentExample.xml commentExample.fsx

F# Compiler for F# 4.0 (Open Source Edition)

Freely distributed under the Apache 2.0 Open Source License
```

This results in an XML file with the content shown in Listing 5.5.

¹ For specification of C# documentations comments see ECMA-334: http://www.ecma-international.org/publications/files/ECMA-ST/Ecma-334.pdf

| Tag | Description | | | |
|--------------------------------------|---|--|--|--|
| <c></c> | Set text in a code-font. | | | |
| <code></code> | Set one or more lines in code-font. | | | |
| <example></example> | Set as an example. | | | |
| <exception></exception> | Describe the exceptions a function can throw. | | | |
| t> | Create a list or table. | | | |
| <para></para> | Set text as a paragraph. | | | |
| <pre><param/></pre> | Describe a parameter for a function or constructor. | | | |
| <pre><paramref></paramref></pre> | Identify that a word is a parameter name. | | | |
| <pre><permission></permission></pre> | Document the accessibility of a member. | | | |
| <remarks></remarks> | Further describe a function. | | | |
| <returns></returns> | Describe the return value of a function. | | | |
| <see></see> | Set as link to other functions. | | | |
| <seealso></seealso> | Generate a See Also entry. | | | |
| <summary></summary> | Main description of a function or value. | | | |
| <typeparam></typeparam> | Describe a type parameter for a generic type or method. | | | |
| <typeparamref></typeparamref> | Identify that a word is a type parameter name. | | | |
| <value></value> | Describe a value. | | | |

Table 5.1 Recommended XML tags for documentation comments, from ECMA-334 3rd Edition, Annex E, Section 2.

```
Listing 5.5, An XML file generated by fsharpc.
<?xml version="1.0" encoding="utf-8"?>
<doc>
<assembly><name>commentExample</name></assembly>
.Double, System.Double, System.Double)">
 <summary>Find x when 0 = ax^2+bx+c.</summary>
 <remarks>Negative discriminants are not checked.</remarks>
 <example>
   The following code:
   <code>
     let a = 1.0
     let b = 0.0
     let c = -1.0
     let xp = (solution a b c +1.0)
     printfn "0 = \%.1fx^2 + \%.1fx + \%.1f => x_+ = \%.1f" a b
   с хр
   </code>
   prints < c>0 = 1.0x^2 + 0.0x + -1.0 => x_+ = 0.7 </c> to
   the console.
 </example>
 <param name="a">Quadratic coefficient.</param>
 <param name="b">Linear coefficient.</param>
 <param name="c">Constant coefficient.</param>
 <param name="sgn">+1 or -1 determines the solution.</param>
 <returns>The solution to x.</returns>
<member name="M:CommentExample.discriminant(System.Double,</pre>
   System.Double,System.Double)">
<summary>
 The discriminant of a quadratic equation with parameters a,
    b, and c
</summary>
</member>
</members>
</doc>
```

Listing 5.3 commentExample.fsx: Code with XML comments. /// The discriminant of a quadratic equation with /// parameters a, b, and c let discriminant a b c = b ** 2.0 - 4.0 * a * c /// <summary>Find x when 0 = ax^2+bx+c.</summary> /// <remarks>Negative discriminants are not checked.</remarks> /// <example> The following code: /// <code> /// let a = 1.0let b = 0.0let c = -1.0111 let xp = (solution a b c +1.0)/// printfn "0=%.1fx^2+%.1fx+%.1f => x_+=%.1f" a b c xp </code> prints $< c>0=1.0x^2+0.0x+-1.0 => x_+=0.7</c>.$ /// /// </example> /// <param name="a">Quadratic coefficient.</param> /// <param name="b">Linear coefficient.</param> /// <param name="c">Constant coefficient.</param> /// <param name="sgn">+1 or -1 determines the solution. /// <returns>The solution to x.</returns> let solution a b c sgn = let d = discriminant a b c (-b + sgn * sqrt d) / (2.0 * a)let a = 1.0let b = 0.0let c = -1.0let xp = (solution a b c +1.0)printfn "0 = $\%.1fx^2 + \%.1fx + \%.1f \Rightarrow x_+ = \%.1f$ " a b c xp

The extracted XML is written in C# type by convention, since F# is part of the Mono and .Net framework that may be used by any of the languages using Assemblies. Besides the XML inserted in the script, the XML has added the <?xml ...> header, <doc>, <assembly>, <members>, and <member> tags. The header and the <doc> tag are standards for XML. The extracted XML is geared towards documenting big libraries of codes and thus highlights the structured programming organisation, see Chapters 18 and 23, and <assembly>, <members>, and <member> are indications for where the functions belong in the hierarchy. As an example, the prefix M: CommentExample. indicates that the method is in the namespace commentExample, which in this case is the name of the file. Furthermore, the function type

```
\begin{tabular}{ll} val & solution : a:float->b:float->c:float->sgn:float->float \\ \end{tabular}
```

is in the XML documentation

M: Comment Example. solution (System. Double, System. Double, System. Double, System. Double),

which is the C# equivalent.

An accompanying program in the Mono suite is mdoc, whose primary use is to perform a syntax analysis of an assembly and generate a scaffold XML structure for an accompanying document. With the -i flag, it is further possible to include the in-code comments as initial descriptions in the XML. The XML may be updated gracefully by mdoc as the code develops, without destroying manually entered documentation in the accompanying documentation. Finally, the XML may be exported to HTML.

The primary use of the mdoc command is to analyze compiled code and generate an empty XML structure with placeholders to describe functions, values, and variables. This structure can be updated and edited as the program develops, and the edited XML files can be exported to *Hyper Text Markup Language* (*HTML*) files and viewed in any browser. Using the console, all of this is accomplished by the procedure shown in Listing 5.6, and the result is shown in Figure 5.1.

```
Listing 5.6, Converting an XML file to HTML.
 $ mdoc update -o commentExample -i commentExample.xml
   commentExample.exe
New Type: CommentExample
Member Added: public static double determinant (double a,
    double b, double c);
Member Added: public static double solution (double a,
    double b, double c, double sgn);
Member Added: public static double a { get; }
Member Added: public static double b { get; }
Member Added: public static double c { get; }
Member Added: public static double xp { get; }
Namespace Directory Created:
New Namespace File:
Members Added: 6, Members Deleted: 0
 $ mdoc export-html -out commentExampleHTML commentExample
 .CommentExample
```

A full description of how to use mdoc is found here².

http://www.mono-project.com/docs/tools+libraries/tools/monodoc/ generating-documentation/

solution Method

Find x when $0 = ax^2+bx+c$.

Syntax

[Microsoft.FSharp.Core.CompilationArgumentCounts(Mono.Cecil.CustomAttributeArgument[])] public static double solution (double a, double b, double c, double sgn)

Parameters

```
Quadratic coefficient.

b
Linear coefficient.

c
Constant coefficient.

sgn
+1 or -1 determines the solution.
```

Returns

The solution to x.

Remarks

Negative discriminants are not checked.

Example

The following code:

```
Example

let a = 1.0
let b = 0.0
let c = -1.0
let xp = (solution a b c +1.0)
printfn "0 = %.1fx^2 + %.1fx + %.1f => x_+ = %.1f" a b c xp

prints 0 = 1.0x^2 + 0.0x + -1.0 => x_+ = 0.7 to the console.
```

Requirements

Namespace:

Assembly: commentExample (in commentExample.dll)
Assembly Versions: 0.0.0.0

Fig. 5.1 Part of the HTML documentation as produced by mdoc and viewed in a browser.

5.3 Key concepts and terms in this chapter

Summary text about the key concepts from this chapter

• ...

Abstract tada - Introductory text about the objectivs of this chapter

• . . .

Chapter 6

Lists

Lists are unions of immutable values of the same type. A list can be expressed as a *sequence expression*,

```
Listing 6.1: The syntax for a list using the sequence expression.

[[<expr>{; <expr>}]]
```

For example, [1; 2; 3] is a list of integers, ["This"; "is"; "a"; "list"] is a list of strings, [(fun $x \rightarrow x$); (fun $x \rightarrow x^*x$)] is a list of functions, and [] is the empty list. Lists may also be given as ranges,

```
Listing 6.2: The syntax for a list using the range expressions.

[<expr> ... <expr> [... <expr>]]
```

where <expr>> in range expressions must be of integers, floats, or characters. Examples are [1 .. 5], [-3.0 .. 2.0], and ['a' .. 'z']. Range expressions may include a step size, thus, [1 .. 2 .. 10] evaluates to [1; 3; 5; 7; 9].

A list type is identified with the *list* keyword, such that a list of integers has the type int list. Like strings, lists may be indexed using the ".[]" notation, the lengths of lists is retrieved using the *Length* property, and we may test whether a list is empty by using the *IsEmpty* property. These features are demonstrated in Listing 6.3. F# implements lists as linked lists, as illustrated in Figure 6.1. As a

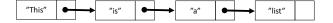


Fig. 6.1 A list is a linked list: Here is illustrated the linked list of ["This"; "is"; "a"; "list"].

consequence, indexing element i has computational complexity O(i). The computational complexity of an operation is a description of how long a computation will take without considering the hardware it is performed on. The notation is sometimes

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Listing 6.3 listIndexing.fsx: Lists are indexed as strings and has a Length property. 1 let printList (lst : int list) : unit = 2 for i = 0 to lst.Length - 1 do 3 printf "%A " lst.[i] 4 printfn "" 5 let lst = [3; 4; 5] 7 printfn "lst = %A, lst.[1] = %A" lst lst.[1] 8 printfn "lst.Length = %A, lst.isEmpty = %A" lst.Length 1 lst.IsEmpty 9 printList lst 1 \$ fsharpc --nologo listIndexing.fsx && mono listIndexing.exe 2 lst = [3; 4; 5], lst.[1] = 4 3 lst.Length = 3, lst.isEmpty = false 4 3 4 5

called Big-O notation or Landau notation. In the present case, the complexity is O(i), which means that the complexity is linear in i and indexing element i+1 takes 1 unit longer than indexing element i when i is very large. The size of the unit is on purpose unspecified and depends on implementation and hardware details. Nevertheless, Big-O notation is a useful tool for reasoning about the efficiency of an operation. F# has access to the list's elements only by traversing the list from its beginning. I.e., to obtain the value of element i, F# starts with element 0, follows the link to element 1 and so on, until element i is reached. To reach element i+1 instead, we would need to follow 1 more link, and assuming that following a single link takes some constant amount of time we find that the computational complexity is O(i).

Compared to arrays, to be discussed below, this is slow, which is why indexing lists should be avoided.

Notice especially that lists are zero-indexed, and thus, the last element in a list 1st is 1st.Length -1. This is a very common source of error! Therefore, indexing in lists using *for*-loops is supported using a special notation with the *in* keyword,

```
Listing 6.4: For-in loop with in expression.

for <ident> in list> do <bodyExpr> [done]
```

In for-in loops, the loop runs through each element of the t>, and assigns it to the identifier <ident>. This is demonstrated in Listing 6.5. Using for-in-expressions remove the risk of off by one indexing errors, and thus for-in is to be

* expressions remove the risk of off-by-one indexing errors, and thus, **for-in is to be preferred over for-to.**

Lists support slicing identically to strings, as demonstrated in Listing 6.6.

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Listing 6.5 listFor.fsx: The - loops are preferred over - loops. 1 let printList (lst : int list) : unit = 2 for elm in lst do 3 printf "%A" elm 4 printfn "" 5 printList [3; 4; 5] 1 \$ fsharpc --nologo listFor.fsx && mono listFor.exe 2 3 4 5

```
Listing 6.6: Examples of list slicing. Compare with Listing 3.27.

| > let lst = ['a' ... 'g'];;
| val lst : char list = ['a'; 'b'; 'c'; 'd'; 'e'; 'f'; 'g']
| > lst.[0];;
| val it : char = 'a'
| > lst.[3];;
| val it : char = 'd'
| | > lst.[3..];
| val it : char list = ['d'; 'e'; 'f'; 'g']
| | | | > lst.[..3];;
| val it : char list = ['a'; 'b'; 'c'; 'd']
| | | > lst.[1..3];;
| val it : char list = ['b'; 'c'; 'd']
| | | | > lst.[*];
| val it : char list = ['a'; 'b'; 'c'; 'd'; 'e'; 'f'; 'g']
```

Lists may be concatenated using either the "@" concatenation operator or the "::" cons operators. The difference is that "@" concatenates two lists of identical types, while "::" concatenates an element and a list of identical types. This is demonstrated in Listing 6.7. Since lists are represented as linked lists, the cons operator

```
Listing 6.7: Examples of list concatenation.

1 > ([1] @ [2; 3]);;
2 val it : int list = [1; 2; 3]

4 > ([1; 2] @ [3; 4]);;
5 val it : int list = [1; 2; 3; 4]

6

7 > (1 :: [2; 3]);;
8 val it : int list = [1; 2; 3]
```

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is very efficient and has computational complexity O(1), while concatenation has computational complexity O(n), where n is the length of the first list.

It is possible to make multidimensional lists as lists of lists, as shown in Listing 6.8. The example shows a *ragged multidimensional list*, since each row has a different

number of elements. This is also illustrated in Figure 6.2.

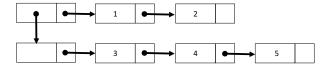


Fig. 6.2 A list is a ragged linked list: Here is illustrated the linked list of [[1;2];[3;4;5]].

The indexing of a particular element is slow due to the linked list implementation of lists, which is why arrays are often preferred for two- and higher-dimensional data structures, see Section 20.3.

6.1 List Properties

Lists support a number of properties, some of which are listed below.

Head: Returns the first element of a list.

```
Listing 6.9: Head

| > [1; 2; 3]. Head;;
| val it : int = 1
```

IsEmpty: Returns true if the list is empty.

```
Listing 6.10: IsEmpty

| > [1; 2; 3].IsEmpty;;
| val it : bool = false
```

Length: Returns the number of elements in the list.

```
Listing 6.11: Length

1 > [1; 2; 3].Length;;
2 val it : int = 3
```

Tail: Returns the list, except for its first element.

```
Listing 6.12: Tail

1 > [1; 2; 3].Tail;;
2 val it : int list = [2; 3]
```

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6.2 The List Module

The built-in List module contains a wealth of functions for lists, some of which are briefly summarized below:

List.collect: f:('T -> 'U list) -> lst:'T list -> 'U list.

Applies f to each element in lst and return a concatenated list of the results.

```
Listing 6.13: List.collect

| > List.collect (fun elm -> [elm; elm; elm]) [1; 2; 3];;
| val it : int list = [1; 1; 1; 2; 2; 2; 3; 3; 3]
```

List.contains: elm:'T -> lst:'T list -> bool.

Returns true or false depending on whether or not elm is contained in lst.

```
Listing 6.14: List.contains
```

List.filter: f:('T -> bool) -> lst:'T list -> 'T list.

Returns a new list with all the elements of lst for which f evaluates to true.

```
Listing 6.15: List.filter

1 > List.filter (fun x -> x % 2 = 1) [0 .. 9];;
2 val it : int list = [1; 3; 5; 7; 9]
```

List.find: f:('T -> bool) -> lst:'T list -> 'T.

Returns the first element of lst for which f is true.

```
Listing 6.16: List.find

| > List.find (fun x -> x % 2 = 1) [0 .. 9];;
| val it : int = 1
```

List.findIndex: f:('T -> bool) -> lst:'T list -> int.

Returns the index of the first element of lst for which f is true.

```
Listing 6.17: List.findIndex

| > List.findIndex (fun x -> x = 'k') ['a' .. 'z'];;
| val it : int = 10
```

List.fold: f:('S -> 'T -> 'S) -> elm:'S -> lst:'T list -> 'S.

Updates an accumulator iteratively by applying f to each element in lst. The initial value of the accumulator is elm. For example, when lst consists of n+1 elements List.fold calculates:

```
f (...(f (f elm lst.[0]) lst.[1]) ...) lst.[n].
```

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```
Listing 6.18: List.fold

1 > let addSquares acc elm = acc + elm*elm

2 - List.fold addSquares 0 [0 .. 9];;

3 val addSquares : acc:int -> elm:int -> int

4 val it : int = 285
```

List.foldBack: f:('T -> 'S -> 'S) -> lst:'T list -> elm:'S -> 'S.

Updates an accumulator iteratively backwards by applying f to each element in lst. The initial value of the accumulator is elm. For exampel, when lst consists of n+1 elements List.foldBack calculates:

f lst.[0] (f lst.[1](...(f lst.[n] elm)...)).

```
Listing 6.19: List.foldBack

| > let addSquares elm acc = acc + elm*elm
| - List.foldBack addSquares [0 .. 9] 0;;
| val addSquares : elm:int -> acc:int -> int
| val it : int = 285
```

List.forall: f:('T -> bool) -> lst:'T list -> bool.

Returns true if all elements in lst are true when f is applied to them.

```
Listing 6.20: List.forall

1 > List.forall (fun x -> x % 2 = 1) [0 .. 9];;
2 val it : bool = false
```

List.head: lst:'T list -> int.

Returns the first element in 1st. An exception is raised if 1st is empty. See Section 13.1 for more on exceptions.

```
Listing 6.21: List.head

1 > List.head [1; -2; 0];;
2 val it : int = 1
```

List.init: $m:int \rightarrow f:(int \rightarrow 'T) \rightarrow 'T list.$

Create a list with m elements and whose value is the result of applying f to the index of the element.

```
Listing 6.22: List.init

1 > List.init 10 (fun i -> i * i);;
2 val it : int list = [0; 1; 4; 9; 16; 25; 36; 49; 64; 81]
```

List.isEmpty: lst:'T list -> bool.
Returns true if lst is empty.

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```
Listing 6.23: List.isEmpty

1 > List.isEmpty [1; 2; 3];;
2 val it : bool = false
```

List.iter: f:('T -> unit) -> lst:'T list -> unit.

Applies f to every element in lst.

```
Listing 6.24: List.iter
```

List.map: f:('T -> 'U) -> lst:'T list -> 'U list.

Returns a list as a concatenation of applying f to every element of 1st.

```
Listing 6.25: List.map

| > List.map (fun x -> x*x) [0 .. 9];;
| val it : int list = [0; 1; 4; 9; 16; 25; 36; 49; 64; 81]
```

List.ofArray: arr:'T [] -> 'T list.

Returns a list whose elements are the same as arr. See Section 20.3 for more on arrays.

```
Listing 6.26: List.ofArray

1 > List.ofArray [|1; 2; 3|];;
2 val it : int list = [1; 2; 3]
```

List.rev: lst:'T list -> 'T list.

Returns a new list with the same elements as in 1st but in reversed order.

```
Listing 6.27: List.rev

1 > List.rev [1; 2; 3];;
2 val it : int list = [3; 2; 1]
```

List.sort: lst:'T list -> 'T list.

Returns a new list with the same elements as in 1st but where the elements are sorted.

```
Listing 6.28: List.sort

| > List.sort [3; 1; 2];;
| val it : int list = [1; 2; 3]
```

List.tail: 'T list -> 'T list.

Returns a new list identical to 1st but without its first element. An Exception is raised if 1st is empty. See Section 13.1 for more on exceptions.

```
Listing 6.29: List.tail

1 > List.tail [1; 2; 3];;
2 val it : int list = [2; 3]

4 > let a = [1; 2; 3] in List.tail a;;
5 val it : int list = [2; 3]
```

List.toArray: lst:'T list -> 'T [].

Returns an array whose elements are the same as 1st. See Section 20.3 for more on arrays.

```
Listing 6.30: List.toArray

1 > List.toArray [1; 2; 3];;
2 val it : int [] = [|1; 2; 3|]
```

List.unzip: lst:('T1 * 'T2) list -> 'T1 list * 'T2 list.

Returns a pair of lists of all the first elements and all the second elements of lst, respectively.

List.zip: lst1:'T1 list -> lst2:'T2 list -> ('T1 * 'T2) list.

Returns a list of pairs, where elements in lst1 and lst2 are iteratively paired.

```
Listing 6.32: List.zip

1 > List.zip [1; 2; 3] ['a'; 'b'; 'c'];;
2 val it : (int * char) list = [(1, 'a'); (2, 'b'); (3, 'c')]
```

6.3 Key concepts and terms in this chapter

Summary text about the key concepts from this chapter

• ...

Abstract tada - Introductory text about the objective of this chapter

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• ...

Chapter 7

Recursion

Recursion is a central concept in F# and is used to control flow in loops without the **for** and **while** constructions. Figure 7.1 illustrates the concept of an infinite loop with recursion.

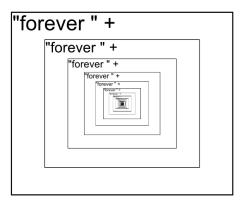


Fig. 7.1 An infinitely long string of "forever forever forever...", conceptually calculated by let rec forever () = "forever " + (forever ()).

7.1 Recursive Functions

A *recursive function* is a function which calls itself, and the syntax for defining recursive functions is an extension of that for regular functions:

```
Listing 7.1: Syntax for defining one or more mutually dependent recursive functions.

| let rec <ident> = <expr> {and <ident> = <expr>} [in] <expr>
```

From a compiler point of view, the **rec** is necessary, since the function is used before the compiler has completed its analysis. If two functions are mutually recursive, then they must be defined jointly using the **and** keyword.

An example of a recursive function that counts from 1 to 10 similarly to Listing 21.5 is given in Listing 7.2. Here the prt function calls itself repeatedly, such that the first

call is prt 1 10, which calls prt 2 10, and so on until the last call prt 11 10. Each time prt is called, new bindings named a and b are made to new values. This is illustrated in Figure 7.2. The old values are no longer accessible, as indicated by subscripts in the figure. E.g., in prt₃, the scope has access to a_3 but not a_2 and a_1 . Thus, in this program, the process is similar to a **for** loop, where the counter is a, and in each loop its value is reduced.

The structure of the function is typical for recursive functions. They very often follow the following pattern.

```
Listing 7.3: Recursive functions consist of a stopping criterium, a stopping expression, and a recursive step.

let rec f a =
lif <stopping condition>
then <stopping step>
else <recursion step>
```

The match – with are also very common conditional structures. In Listing 7.2, a > b is the stopping condition, printfn "\n" is the stopping step, and printfn "\%d " a; prt (a + 1) b is the recursion step.

```
$ fsharpc countRecursive.fsx && mono countRecursive.exe
prt 1 10
    prt_1: a_1 = 1, b_1 = 10
    1 > 10: X
       printf "1 "
       prt 2 10
            prt<sub>2</sub>: a<sub>2</sub>= 2, b<sub>2</sub>= 10
            2 > 10: X
              printf "2 "
              prt 3 10
                   prt_3: a_3 = 3, b_3 = 10
                   3 > 10: X
                    printf "3 "
                     prt 4 10
                         prt 11 10
                             prt<sub>11</sub>: a<sub>11</sub>= 1, b<sub>11</sub>= 10
                             11 > 10 <
                                 printf "\\n"
                              ()
                   ()
            ()
     ()
()
```

Fig. 7.2 Illustration of the recursion used to write the sequence " $123 \dots 10$ " in line 8 in Listing 7.2. Each frame corresponds to a call to prt, where new values overshadow old ones. All calls return unit.

7.2 The Call Stack and Tail Recursion

Fibonacci's sequence of numbers is a recursive sequence of numbers with relations to the Golden ratio and structures in biology. The Fibonacci sequence is the sequence of numbers $1, 1, 2, 3, 5, 8, 13, \ldots$ The sequence starts with 1, 1 and the next number is recursively given as the sum of the two previous ones. A direct implementation of this is given in Listing 21.8. Here we extended the sequence to $0, 1, 1, 2, 3, 5, \ldots$

```
Listing 7.4 fibRecursive.fsx:
The n'th Fibonacci number using recursion.
let rec fib n =
   if n < 1 then
   elif n = 1 then
     1
   else
     fib (n - 1) + fib (n - 2)
for i = 0 to 10 do
   printfn "fib(%d) = %d" i (fib i)
$ fsharpc --nologo fibRecursive.fsx && mono fibRecursive.exe
fib(0) = 0
fib(1) = 1
fib(2) = 1
fib(3) = 2
fib(4) = 3
fib(5) = 5
fib(6) = 8
fib(7) = 13
fib(8) = 21
fib(9) = 34
fib(10) = 55
```

with the starting sequence 0, 1, allowing us to define all fib(n) = 0, n < 1. Thus, our function is defined for all integers, and for the irrelevant negative arguments it fails gracefully by returning 0. This is a general piece of advice: **make functions that fail gracefully.**

A visualization of the calls and the scopes created by fibRecursive is shown in Figure 7.3. The figure illustrates that each recursive step results in two calls to the function, thus creating two new scopes. And it gets worse. Figure 7.4 illustrates the tree of calls for fib 5. Thus, a call to the function fib generates a tree of calls that is five levels deep and has fib(5) number of nodes. In general for the program in Listing 7.4, a call to fib(n) produces a tree with fib(n) $\leq c\alpha^n$ calls to the function for some positive constant c and $\alpha \geq \frac{1+\sqrt{5}}{2} \sim 1.6$. Each call takes time and requires memory, and we have thus created a slow and somewhat memory-intensive function.

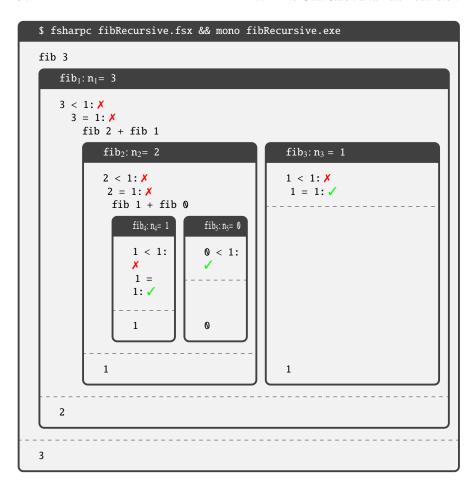


Fig. 7.3 Illustration of the recursion used to write the sequence "1 2 3 ... 10" in line 8 in Listing 7.2. Each frame corresponds to a call to fib, where new values overshadow old ones.

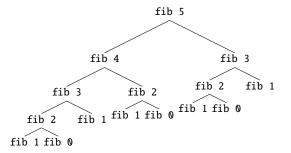


Fig. 7.4 The function calls involved in calling fib 5.

This is a hugely ineffective implementation of calculating entries into Fibonacci's sequence, since many of the calls are identical. E.g., in Figure 7.4, fib 1 is called five times. Before we examine a faster algorithm, we first need to discuss how F# executes function calls.

When a function is called, then memory is dynamically allocated internally for the function on what is known as the *call stack*. Stacks are used for many things in programming, but typically the call stack is considered special, since it is almost always implicitly part of any program execution. Hence, it is often just referred to as *The Stack*. When a function is called, a new *stack frame* is stacked (pushed) on the call stack, including its arguments, local storage such as mutable values, and where execution should return to when the function is finished. When the function finishes, the stack frame is unstacked (popped) and in its stead, the return value of the function is stacked. This return value is then unstacked and used by the caller. After unstacking the return value, the call stack is identical to its state prior to the call. Figure 7.5 shows snapshots of the call stack when calling fib 5 in Listing 7.4. The call first stacks a frame onto the call stack with everything needed to execute the

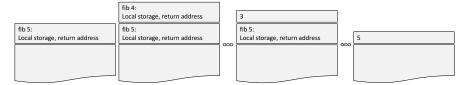


Fig. 7.5 A call to fib 5 in Listing 7.4 starts a sequence of function calls and stack frames on the call stack.

function body plus a reference to where the return to, when the execution is finished. Then the body of fib is executed, which includes calling fib 4 and fib 3 in turn. The call to fib 4 stacks a frame onto the call stack, and its body is executed. Once execution is returned from the call to fib 4, the result of the function is on top of the stack. It is unstacked, saved and the call to fib 3 is treated equally. When the end of fib 5 is reached, its frame is unstacked, and its result is stacked. In this way, the call stack is returned to its original state except for the result of the function, and execution is returned to the point right after the original call to fib 5. Thus, for Listing 7.4 $O(\alpha^n)$, $\alpha = \frac{1+\sqrt{5}}{2}$ stacking operations are performed for a call to fib n. The O(f(n)) is the Landau symbol used to denote the order of a function, such that if g(n) = O(f(n)) then there exists two real numbers M > 0 and a n_0 such that for all $n \ge n_0$, $|g(n)| \le M|f(n)|$. As indicated by the tree in Figure 7.4, the call tree is at most n high, which corresponds to a maximum of n additional stack frames as compared to the starting point.

The implementation of Fibonacci's sequence in Listing 7.4 can be improved to run faster and use less memory. One such algorithm is given in Listing 7.5 Calculating the 45th Fibonacci number a MacBook Pro, with a 2.9 GHz Intel Core i5 using Listing 7.4 takes about 11.2s while using Listing 7.5 is about 224 times faster and only takes 0.050s. The reason is that fib in Listing 7.5 calculates every number in

Listing 7.5 fibRecursiveAlt.fsx: A fast, recursive implementation of Fibonacci's numbers. Compare with Listing 7.4. let fib n = let rec fibPair n pair = if n < 2 then pair else fibPair (n - 1) (snd pair, fst pair + snd pair) if n < 1 then 0 elif n = 1 then 1 else fibPair n (0, 1) |> snd printfn "fib(10) = %d" (fib 10) s fsharpc --nologo fibRecursiveAlt.fsx && mono fibRecursiveAlt.exe fib(10) = 55

the sequence once and only once by processing the list recursively while maintaining the previous two values needed to calculate the next in the sequence. I.e., the function fibPair transforms the pair (a,b) to (b,a+b) such that, e.g., the 4th and 5th pair (3,5) is transformed into the 5th and the 6th pair (5,8) in the sequence. What complicates the algorithm is that besides the transformation, we must keep track of when to stop, which here is done using a counter variable, that is recursively reduced by 1 until our stopping criterium.

Listing 7.5 also uses much less memory than Listing 7.4, since its recursive call is the last expression in the function, and since the return value of two recursive calls to fibPair is the same as the return value of the last. In fact, the return value of any number of recursive calls to fibPair is the return value of the last. This structure is called *tail-recursion*. Compilers can easily optimize the call stack usage for tail recursion, since when in this example fibPair calls itself, then its frame is no longer needed, and may be replaced by the new fibPair with the slight modification, that the return point should be to fib and not the end of the previous fibPair. Once the recursion reaches the stopping criteria, then instead of popping a long list of calls of fibPair frames, then there is only one, and the return value is equal to the return value of the last call and the return point is to fib. Thus, many stack frames in tail recursion are replaced by one. Hence, **prefer tail-recursion whenever possible.**

7.3 Mutually Recursive Functions

Functions that recursively call each other are called *mutually recursive* functions. F# offers the let - rec - and notation for co-defining mutually re-

cursive functions. As an example, consider the function even: int -> bool, which returns true if its argument is even and false otherwise, and the opposite function odd: int -> bool. A mutually recursive implementation of these functions can be developed from the following relations: even 0 = true, odd 0 = false, and for n > 0, even n = odd (n-1), which implies that for n > 0, odd n = even (n-1): Notice that in the lightweight notation the and must

```
Listing 7.6 mutually Recursive.fsx:
Using mutual recursion to implement even and odd functions.
let rec even x =
  if x = 0 then true
   else odd (x - 1)
and odd x =
  if x = 0 then false
   else even (x - 1);
let w = 5;
printfn "%*s %*s %*s" w "i" w "even" w "odd"
for i = 1 to w do
   printfn "%*d %*b %*b" w i w (even i) w (odd i)
$ fsharpc --nologo mutuallyRecursive.fsx && mono
    mutuallyRecursive.exe
    i even
              odd
    1 false true
     2 true false
     3 false true
     4 true false
     5 false true
```

be on the same indentation level as the original let.

Without the and keyword, F# will issue a compile error at the definition of even. However, it is possible to implement mutual recursion by using functions as an argument, e.g., This being said, Listing 7.6 is clearly to be preferred over Listing 7.7.

In the example above, we used the **even** and **odd** function problems to demonstrate mutual recursion. There is, of course, a much simpler solution, which does not use recursion at all: This is to be preferred anytime as the solution to the problem.

Listing 7.7 mutually Recursive Alt.fsx: Mutual recursion without the keyword requires a helper function. let rec evenHelper (notEven: int -> bool) x = if x = 0 then true else notEven (x - 1) let rec odd x = if x = 0 then false else evenHelper odd (x - 1);; let even x = evenHelper odd x let w = 5; printfn "%*s %*s %*s" w "i" w "Even" w "Odd" for i = 1 to w do printfn "%*d %*b %*b" w i w (even i) w (odd i) \$ fsharpc --nologo mutuallyRecursiveAlt.fsx && mono mutuallyRecursiveAlt.exe i Even Odd 1 false true 2 true false 3 false true

```
Listing 7.8 parity.fsx:
A better way to test for parity without recursion.

1 let even x = (x % 2 = 0)
2 let odd x = not (even x)
```

4 true false 5 false true

7.4 Tracing Recursive Programs

Tracing by hand is a very illustrative method for understanding recursive programs. Consider the recursive program in Listing 7.9. The program includes a function for

```
Listing 7.9 gcd.fsx:

The greatest common divisor of 2 integers.

1 let rec gcd a b =
2    if a < b then
3        gcd b a
4    elif b > 0 then
5        gcd b (a % b)
6    else
7        a
8
9 let a = 10
10 let b = 15
11 printfn "gcd %d %d = %d" a b (gcd a b)

1 $ fsharpc --nologo gcd.fsx && mono gcd.exe
2 gcd 10 15 = 5
```

calculating the greatest common divisor of 2 integers, and calls this function with the numbers 10 and 15. Following the notation introduced in Section 19.3, we write:

```
        Step Line Env. Bindings and evaluations

        0
        -
        E_0 ()

        1
        1
        E_0 gcd = ((a, b), gcd-body, ())

        2
        9
        E_0 a = 10

        3
        10
        E_0 b = 15
```

In line 11, gdc is called before any output is generated, which initiates a new environment E_1 and executes the code in gcd-body:

In E_1 we have that a < b, which fulfills the first condition in line 2. Hence, we call gdc with switched arguments and once again initiate a new environment,

In E_2 , a < b in line 2 is false, but b > 0 in line 4 is true, hence, we first evaluate a % b, call gcd b (a % b), and then create a new environment,

| Step | Line | Env. | Bindings and evaluations |
|------|------|-------|---------------------------------|
| 8 | 5 | E_2 | a % b = 5 |
| 9 | 5 | E_2 | gcd b (a % b) = ? |
| 10 | 1 | E_3 | ((a = 10, b = 5), gcd-body, ()) |

Again we fall through to line 5, evaluate the remainder operator and initiate a new environment,

| Step | Line | Env. | Bindings and evaluations |
|------|------|-------|---|
| 11 | 5 | E_3 | a % b = 0 |
| 12 | 5 | | gcd b (a % b) = ? |
| 13 | 1 | E_4 | $((a = 5, b = 0), \operatorname{gcd-body}, ())$ |

This time both a < b and b > 0 are false, so we fall through to line 7 and return the value of a from E_4 , which is 5:

Step Line Env. Bindings and evaluations
$$14 \quad 7 \quad E_4 \quad \text{return} = 5$$

We scratch E_4 , return to E_3 , either physically or mentally replace the ?-mark with 5 and continue the evaluation of line 5. Since this is also a branch of the last statement in gdc, we return the previously evaluated value,

Step Line Env. Bindings and evaluations
$$15 \quad 5 \quad E_3 \quad \text{return} = 5$$

Like before, we scratch E_3 , return to E_2 , either physically or mentally replace the ?-mark with 5 and continue the evaluation of line 5. Since this is also a branch of the last statement in gdc, we return the just evaluated value,

Again, we scratch E_2 , return to E_1 , either physically or mentally replace the ?-mark with 5 and continue the evaluation of line 5. Since this is also a branch of the last statement in gdc, we return the just evaluated value,

| Step | Line | Env. | Bindings and evaluations |
|------|------|-------|--------------------------|
| 17 | 3 | E_1 | return = 5 |

Finally, we scratch E_1 , return to E_0 , either physically or mentally replace the ?-mark with 5 and continue the evaluation of line 5:

Note that the output of printfn is a side-effect while its return-value is unit. In any case, since this is the last line in our program, we are done tracing.

7.5 Key concepts and terms in this chapter

Summary text about the key concepts from this chapter

• ...

Chapter 8

Higher-Order Functions

Abstract tada - Introductory text about the objectivs of this chapter

• ...

A higher-order function is a function that takes a function as an argument and/or returns a function. higher-order functions are also sometimes called functionals or functors. F# is a functions-first programming language with strong support for working with functions as values: Functions evaluate as *closures*, see Section 4.2, which can be passed to and from functions as any other value. An example of a higher-order function is List.map which takes a function and a list and produces a list, demonstrated in Listing 8.1. Here List.map applies the function inc to every element of

```
Listing 8.1 higherOrderMap.fsx:
List.map is a higher-order function, since it takes a function as argument.

1 let inc x = x + 1
2 let newList = List.map inc [2; 3; 5]
3 printfn "%A" newList

1 $ fsharpc --nologo higherOrderMap.fsx && mono higherOrderMap.exe
2 [3; 4; 6]
```

the list. higher-order functions are often used together with *anonymous functions*, where the anonymous functions is given as argument. For example, Listing 8.1 may be rewritten using an anonymous function as shown in Listing 8.2. The code may be compacted even further, as shown in Listing 8.3. What was originally three lines in Listing 8.1 including bindings to the names inc and newList has in Listing 8.3 been reduced to a single line with no bindings. All three programs result in the same output and as such are equal. Likewise, running times will be equal. However, they differ in readability for a programmer and ease of bug hunting and future mainte-

Listing 8.2 higherOrderAnonymous.fsx:

An anonymous function is a higher-order function used here as an unnamed argument. Compare with Listing 8.1.

```
let newList = List.map (fun x -> x + 1) [2; 3; 5]
printfn "%A" newList

1 $ fsharpc --nologo higherOrderAnonymous.fsx && mono higherOrderAnonymous.exe
2 [3; 4; 6]
```

```
Listing 8.3 higherOrderAnonymousBrief.fsx:
A compact version of Listing 8.1.

1 printfn "%A" (List.map (fun x -> x + 1) [2; 3; 5])

1 $ fsharpc --nologo higherOrderAnonymousBrief.fsx && mono higherOrderAnonymousBrief.exe

2 [3; 4; 6]
```

nance: Bindings allows us to reuse the code at a later stage, but if there is no reuse, then the additional bindings may result in a cluttered program. Further, for compact programs like Listing 8.3, it is not possible to perform a unit test of the function arguments. Finally, bindings emphasize semantic aspects of the evaluation being performed merely by the names we select, and typically long, meaningful names are to be preferred, within reasonable limits. For example instead of inc one could have used increment_by_one or similar which certainly is semantically meaningful, but many programmers will find that the short is to be preferred in order to reduce the amount of typing to be performed.

Anonymous functions are also useful as return values of functions, as shown in Listing 8.4 Here the inc function produces a customized incrementation function

```
Listing 8.4 higherOrderReturn.fsx:

The procedure inc returns an increment function. Compare with Listing 8.1.

1 let inc n =
2 fun x -> x + n
3 printfn "%A" (List.map (inc 1) [2; 3; 5])

1 $ fsharpc --nologo higherOrderReturn.fsx && mono higherOrderReturn.exe
2 [3; 4; 6]
```

as argument to List.map: It adds a prespecified number to an integer argument. Note that the closure of this customized function is only produced once, when

the arguments for List.map is prepared, and not every time List.map maps the function to the elements of the list. Compare with Listing 8.1.

Piping is another example of a set of higher-order function: (<|), (|>), (<||), (||>), (|||>), (|||>). E.g., the functional equivalent of the right-to-left piping operator takes a value and a function and applies the function to the value, as demonstrated in Listing 8.5. Here the piping operator is used to apply the inc

```
Listing 8.5 higherOrderPiping.fsx:

The functional equivalent of the right-to-left piping operator is a higher-
order function.

1 let inc x = x + 1
2 let aValue = 2
3 let anotherValue = (|>) aValue inc
4 printfn "%d -> %d" aValue anotherValue

1 $ fsharpc --nologo higherOrderPiping.fsx && mono
higherOrderPiping.exe
2 2 -> 3
```

function to aValue. A more elegant way to write this would be aValue |> inc, or even just inc aValue.

8.1 Function Composition

Piping is a useful shorthand for composing functions, where the focus is on the transformation of arguments and results. Using higher-order functions, we can forgo the arguments and compose functions as functions directly. This is done with the ">>" and "<<" operators. An example is given in Listing 8.6. In the example we see that (f >> g) x gives the same result as g(fx), while (f << g) x gives the same result as f(gx). A memo technique for remembering the order of the application, when using the function composition operators, is that (f >> g) x is the same as f(gx), i.e., the result of applying f(gx) to f(gx) to g(gx). However, there is a clear distinction between the piping and composition operators. The type of the piping operator is

```
(|>) : ('a, 'a -> 'b) -> 'b
```

i.e., the piping operator takes a value of type 'a and a function of type 'a -> 'b, applies the function to the value, and produces the value 'b. In contrast, the composition operator has type

Listing 8.6 higherOrderComposition.fsx: Functions defined as compositions of other functions. let f x = x + 1let g x = x * xlet h = f >> g $let k = f \ll g$ printfn "%d" (g (f 2)) printfn "%d" (h 2) printfn "%d" (f (g 2)) printfn "%d" (k 2) \$ fsharpc --nologo higherOrderComposition.fsx && mono higherOrderComposition.exe 9 9 5 5

i.e., it takes two functions of type 'a -> 'b and 'b -> 'c respectively, and produces a new function of type a' -> 'c.

(>>) : ('a -> 'b, 'b -> 'c) -> ('a -> 'c)

8.2 Currying

¹ Haskell Curry (1900–1982) was an American mathematician and logician who also has a programming language named after him: Haskell.

Listing 8.7 higherOrderCurrying.fsx: Currying: defining a function as a partial specification of another. 1 let mul x y = x*y 2 let timesTwo = mul 2.0 3 printfn "%g" (mul 5.0 3.0) 4 printfn "%g" (timesTwo 3.0) 1 \$ fsharpc --nologo higherOrderCurrying.fsx && mono higherOrderCurrying.exe 2 15 3 6

Listing 8.8 higherOrderTuples.fsx:

Partial specification of functions using tuples is less elegant. Compare with Listing 8.7.

```
let mul (x, y) = x*y
let timesTwo y = mul (2.0, y)
printfn "%g" (mul (5.0, 3.0))
printfn "%g" (timesTwo 3.0)

fsharpc --nologo higherOrderTuples.fsx && mono higherOrderTuples.exe

15
6
```

Listing 8.9: Two functions to convert between two and 2-tuple arguments.

```
1 > let curry f x y = f (x,y)
2 - let uncurry f (x,y) = f x y;;
3 val curry : f:('a * 'b -> 'c) -> x:'a -> y:'b -> 'c
4 val uncurry : f:('a -> 'b -> 'c) -> x:'a * y:'b -> 'c
```

Hence, curry mul 2.0 is equal to fun y -> 2.0 * y, since the precedence of function calls is (curry mul) 2.0.

Currying makes elegant programs and is often used in functional programming. Nevertheless, currying may lead to obfuscation, and in general, **currying should be * used with care and be well documented for proper readability of code.**

8.3 Key concepts and terms in this chapter

Summary text about the key concepts from this chapter

• ...

Chapter 9

Collections of Data

Abstract tada - Introductory text about the objectivs of this chapter

• . . .

F# is tuned to work with collections of data, and there are several built-in types of collections with various properties making them useful for different tasks. Examples include strings, lists, and arrays. Strings were discussed in Chapter 3 and will be revisited here in more details.

The data structures discussed below all have operators, properties, methods, and modules to help you write elegant programs using them.

Properties and methods are common object-oriented terms used in conjunction with the discussed functionality. They are synonymous with values and functions and will be discussed in Chapter 23. Properties and methods for a value or variable are called using the *dot notation*, i.e., with the "."-lexeme. For example, "abcdefg".Length is a property and is equal to the length of the string, and "abcdefg".ToUpper() is a method and creates a new string where all characters have been converted to upper case.

The data structures also have accompanying modules with a wealth of functions and where some are mentioned here. Further, the data structures are all implemented as classes offering even further functionality. The modules are optimized for functional programming, see Chapters 7 to 10, while classes are designed to support object-oriented programming, see Chapters 23 to 25.

In the following, a brief overview of many properties, methods, and functions is given by describing their name and type-definition, and by giving a short description and an example of their use. Several definitions are general and works with many different types. To describe this we will use the notation of generic types, see Section 4.2. The name of a generic type starts with the "'" lexeme, such as 'T. The implication of the appearance of a generic type in, e.g., a function's type-definition, is that the function may be used with any real type such as int or char. If the same generic type name is used in several places in the type-definition, then the function must use a real type consistently. For example, The List.fromArray function has type arr:'T [] -> 'T list, meaning that it takes an array of some type and returns a list of the same type.

See the F# Language Reference at https://docs.microsoft.com/en-us/dotnet/fsharp/ for a full description of all available functionality including variants of those included here.

- **9.1 Maps**
- **9.2 Sets**

9.3 Key concepts and terms in this chapter

Summary text about the key concepts from this chapter

• . . .

Chapter 10

The Functional Programming Paradigm

Functional programming is a style of programming which performs computations by evaluating functions. Functional programming avoids mutable values and side-effects. It is declarative in nature, e.g., by the use of value- and function-bindings – let-bindings – and avoids statements – do-bindings. Thus, the result of a function in functional programming depends only on its arguments, and therefore functions have no side-effect and are deterministic, such that repeated call to a function with the same arguments always gives the same result. In functional programming, data and functions are clearly separated, and hence data structures are dum as compared to objects in object-oriented programming paradigm, see Chapter 25. Functional programs clearly separate behavior from data and subscribes to the view that *it is better to have 100 functions operate on one data structure than 10 functions on 10 data structures.* Simplifying the data structure has the advantage that it is much easier to communicate data than functions and procedures between programs and environments. The .Net, mono, and java's virtual machine are all examples of an attempt to rectify this, however, the argument still holds.

The functional programming paradigm can trace its roots to lambda calculus introduced by Alonzo Church in 1936 [1]. Church designed lambda calculus to discuss computability. Some of the forces of the functional programming paradigm are that it is often easier to prove the correctness of code, and since no states are involved, then functional programs are often also much easier to parallelize than other paradigms.

Functional programming has a number of features:

Pure functions

Functional programming is performed with pure functions. A pure function always returns the same value, when given the same arguments, and it has no side-effects. A function in F# is an example of a pure function. Pure functions can be replaced by their result without changing the meaning of the program. This is known as *referential transparency*.

higher-order functions

Functional programming makes use of higher-order functions, where functions may be given as arguments and returned as results of a function application. higher-order functions and *first-class citizenship* are related concepts, where higher-order functions are the mathematical description of functions that operator on functions, while a first-class citizen is the computer science term for functions as values. F# implements higher-order functions.

Recursion

Functional programs use recursion instead of **for**- and **while**-loops. Recursion can make programs ineffective, but compilers are often designed to optimize tail-recursion calls. Common recursive programming structures are often available as optimized higher-order functions such as *iter*, *map*, *reduce*, *fold*, and *foldback*. F# has good support for all of these features.

Immutable states

Functional programs operate on values, not on variables. This implies lexicographical scope in contrast to mutable values, which implies dynamic scope.

Strongly typed

Functional programs are often strongly typed, meaning that types are set no later than at compile-time. F# does have the ability to perform runtime type assertion, but for most parts it relies on explicit type annotations and type inference at compile-time. This means that type errors are caught at compile time instead of at runtime.

Lazy evaluation

Due to referential transparency, values can be computed any time up until the point when it is needed. Hence, they need not be computed at compilation time, which allows for infinite data structures. F# has support for lazy evaluations using the <code>lazy</code>-keyword, sequences using the <code>seq</code>-type, and computation expressions, all of which are advanced topics and not treated in this book.

Immutable states imply that data structures in functional programming are different than in imperative programming. E.g., in F# lists are immutable, so if an element of a list is to be changed, a new list must be created by copying all old values except that which is to be changed. Such an operation is therefore linear in computational complexity. In contrast, arrays are mutable values, and changing a value is done by reference to the value's position and changing the value at that location. This has constant computational complexity. While fast, mutable values give dynamic scope and makes reasoning about the correctness of a program harder, since mutable states do not have referential transparency.

Functional programming may be considered a subset of *imperative programming*, in the sense that functional programming does not include the concept of a state, or one may think of functional programming as only having one unchanging state.

Functional programming also has a bigger focus on declaring rules for *what* should be solved, and not explicitly listing statements describing *how* these rules should be combined and executed in order to solve a given problem. Functional programming is often found to be less error-prone at runtime, making more stable, safer programs that are less open for, e.g., hacking.

10.1 Functional Design

A key to all good programming designs is encapsulating code into modules. For functional programs, the essence is to consider data and functions as transformations of data. I.e., the basic pattern is a piping sequence,

```
x \mid > f \mid > g \mid > h,
```

where \mathbf{x} is the input data and \mathbf{f} , \mathbf{g} , and \mathbf{h} are functions that transform the data. Of course, most long programs include lots of control structure, implying that we would need junctions in the pipe system, however, piping is a useful memo technique.

In functional programming there are some pitfalls that you should avoid:

- Creating large data structures, such as a single record containing all data. Since
 data is immutable, changing a single field in a monstrous record would mean a
 lot of copying in many parts of your program. In such cases, it is better to use a
 range of data structures that express isolated semantic units of your problem.
- Non-tail recursion. Relying on the built-in functions map, fold, etc., is a good start for efficiency.
- Single character identifiers. Since functional programming tends to produce small, well-defined functions, there is a tendency to use single character identifiers, e.g., let f x = In the very small, this can be defended, but the names used as identifiers can be used to increase the readability of code to yourself or to others. Typically, identifiers are long and informative in the outermost scope, while decreasing in size as you move in.
- Few comments. Since functional programming is very concise, there is a tendency for us as programmers to forget to add sufficient comments to the code, since at the time of writing, the meaning may be very clear and well thought through. However, experience shows that this clarity deteriorates fast with time.
- Identifiers that are meaningless clones of each other. Since identifiers cannot be reused except by overshadowing in deeper scopes, there is often a tendency to

have a family of identifiers like a, a2, newA etc. It is better to use names that more clearly state the semantic meaning of the values, or, if only used as temporary storage, to discard them completely in lieu of piping and function composition. However, the lattermost often requires comments describing the transformation being performed.

Thus, a design pattern for functional programs must focus on,

- What input data is to be processed
- How the data is to be transformed

For large programs, the design principle is often similar to other paradigms, which are often visualized graphically as components that take input, interact, and produce results often together with a user. The effect of functional programming is mostly seen in the small, i.e., where a subtask is to be structured functionally.

Chapter 11

Pattern Matching

Abstract tada - Introductory text about the objectivs of this chapter

• ...

Pattern matching is used to transform values and variables into a syntactical structure. The simplest example is value-bindings. The *let*-keyword was introduced in Section 4.1, its extension with pattern matching is given as,

```
Listing 11.1: Syntax for let-expressions with pattern matching.

[[<Literal>]]
2 let [mutable] <pat> [: <returnType>] = <bodyExpr> [in <expr>]
```

A typical use of this is to extract elements of tuples, as demonstrated in Listing 11.2. Here we extract the elements of a pair twice. First by binding to x and y, and second

```
Listing 11.2 letPattern.fsx:

Patterns in expressions may be used to extract elements of tuples.

1 let a = (3,4)
2 let (x,y) = a
3 let (alsoX,_) = a
4 printfn "%A: %d %d %d" a x y alsoX

1 $ fsharpc --nologo letPattern.fsx && mono letPattern.exe
2 (3, 4): 3 4 3
```

by binding to alsoX while using the wildcard pattern to ignore the second element. Thus, again the wildcard pattern in value-bindings is used to underline a disregarded value.

Another common use of patterns is as an alternative to if – then – else expressions, particularly when parsing input for a function. Consider the example in Listing 11.3. In the example, a discriminated union and a function are defined. The function

```
Listing 11.3 switch.fsx:

Using - to print discriminated unions.

1 type Medal = Gold | Silver | Bronze
2 let statement (m : Medal) : string =
3 if m = Gold then "You won"
4 elif m = Silver then "You almost won"
5 else "Maybe you will win next time"
6
7 let m = Silver
8 printfn "%A : %s" m (statement m)

1 $ fsharpc --nologo switch.fsx && mono switch.exe
2 Silver : You almost won
```

converts each case to a supporting statement, using an if-expression. The same can be done with the match - with expression and patterns, as demonstrated in Listing 11.4. Here we used a pattern for the discriminated union cases and a

wildcard pattern as default. The lightweight syntax for match-expressions is,

```
Listing 11.5: Syntax for match-expressions.

| match <inputExpr> with
| [|] <pat> [when <guardExpr>] -> <caseExpr>
| <pat> [when <guardExpr>] -> <caseExpr> ...
```

where <inputExpr> is the *input pattern* to find matches of, <pat> is a pattern to match with, <guardExpr> is an optional guard expression, and <caseExpr> is the resulting expression. Each set starting with <pat> is called a case. In lightweight syntax, the indentation must be equal to or higher than the indentation of match. All cases must return a value of the same type, and F# reports an error when the complete domain of the input pattern is not covered by cases in match-expressions.

Patterns are also used in a version of *for*-loop expressions, and its lightweight syntax is given as,

Typically, <sourceExpr> is a list or an array. An example is given in Listing 11.7. The wildcard pattern is used to disregard the first element in a pair while iterating

```
Listing 11.7 forPattern.fsx:
Patterns may be used in -loops.

1 for (_,y) in [(1,3); (2,1)] do
2 printfn "%d" y

1 $ fsharpc --nologo forPattern.fsx && mono forPattern.exe
2 3
3 1
```

over the complete list. It is good practice to use wildcard patterns to emphasize \star unused values.

The final expression involving patterns to be discussed is the *anonymous functions*. Patterns for anonymous functions have the syntax,

```
Listing 11.8: Syntax for anonymous functions with pattern matching.

| fun <pat> [<pat> ...] -> <bodyExpr>
```

This is an extension of the syntax discussed in Section 4.2. A typical use for patterns in *fun*-expressions is shown in Listing 11.9. Here we use an anonymous function expression and bind it to f. The expression has one argument of any type, which it ignores through the wildcard pattern. Some limitations apply to the patterns allowed in *fun*-expressions. The wildcard pattern in *fun*-expressions are often used for *mockup functions*, where the code requires the said function, but its content has yet to be decided. Thus, mockup functions can be used as loose place-holders while experimenting with program design.

```
Listing 11.9 funPattern.fsx:

Patterns may be used in -expressions.

1 let f = fun _ -> "hello"
2 printfn "%s" (f 3)

1 $ fsharpc --nologo funPattern.fsx && mono funPattern.exe
2 hello
```

Patterns are also used in exceptions to be discussed in Section 13.1, and in conjunction with the **function**-keyword, a keyword we discourage in this book. We will now demonstrate a list of important patterns in F#.

11.1 Wildcard Pattern

A *wildcard pattern* is denoted "_" and matches anything, see e.g., Listing 11.10. In this example, anything matches the wildcard pattern, so all cases are covered and

```
Listing 11.10 wildcardPattern.fsx:

Constant patterns match to constants.

let whatEver (x : int) : string =
match x with
    _ -> "If you say so"

printfn "%s" (whatEver 42)

string for the string in the string
```

the function always returns the same sentence. This is rarely a useful structure on its own, since this could be replaced by a value binding or by a function ignoring its input. However, wildcard patterns are extremely useful, since they act as the final else in if-expressions.

11.2 Constant and Literal Patterns

A *constant pattern* matches any input pattern with constants, see e.g., Listing 11.11. In this example, the input pattern is queried for a match with 0, 1, or the wildcard

```
Listing 11.11 constPattern.fsx:

Constant patterns match to constants.

type Medal = Gold | Silver | Bronze
let intToMedal (x : int) : Medal =

match x with

0 -> Gold
| 1 -> Silver
| -> Bronze

printfn "%A" (intToMedal 0)

$ fsharpc --nologo constPattern.fsx && mono constPattern.exe
Gold
```

pattern. Any simple literal type constants may be used in the constant pattern, such as 8, 23y, 1010u, 1.2, "hello world", 'c', and false. Here we also use the wildcard pattern. Note that matching is performed in a lazy manner and stops at the first matching case from the top. Thus, although the wildcard pattern matches everything, its case expression is only executed if none of the previous patterns match the input.

Constants can also be pre-bound by the [<Literal>] attribute for value-bindings. This is demonstrated in Listing 11.12. The attribute is used to identify the value-

```
Listing 11.12 literalPattern.fsx:
A variant of constant patterns is literal patterns.

[<Literal>]
let TheAnswer = 42
let whatIsTheQuestion (x : int) : string =
match x with
TheAnswer -> "We will need to build a bigger machine..."
| _ -> "Don't know that either"

printfn "%A" (whatIsTheQuestion 42)

string =
match x with
with
the Answer -> "We will need to build a bigger machine..."

printfn "%A" (whatIsTheQuestion 42)
```

binding TheAnswer to be used, as if it were a simple literal type. Literal patterns must be either uppercase or module prefixed identifiers.

11.3 Variable Patterns

A *variable pattern* is a single lower-case letter identifier. Variable pattern identifiers are assigned the value and type of the input pattern. Combinations of constant and variable patterns are also allowed in conjunction with with records and arrays. This is demonstrated in Listing 11.13. In this example, the value identifier n has the

```
Listing 11.13 variablePattern.fsx:

Variable patterns are useful for, e.g., extracting and naming fields

| let (name, age) = ("Jon", 50)
| let getAgeString (age : int) : string =
| match age with
| 0 -> "a newborn"
| 1 -> "1 year old"
| n -> (string n) + " years old"
| printfn "%s is %s" name (getAgeString age)

| $ fsharpc --nologo variablePattern.fsx && mono variablePattern.exe
| Jon is 50 years old|
```

function of a named wildcard pattern. Hence, the case could as well have been | _ -> (string age) + "years old", since age is already defined in this scope. However, variable patterns syntactically act as an argument to an anonymous function and thus act to isolate the dependencies. They are also very useful together with guards, see Section 11.4.

11.4 Guards

A *guard* is a pattern used together with match-expressions including the when-keyword, as shown in Listing 11.5. Here guards are used to iteratively carve out subset of integers to assign different strings to each set. The guard expression in <pat> when <guardExpr> -> <caseExpr> is any expression evaluating to a Boolean, and the case expression is only executed for the matching case.

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Listing 11.14 guardPattern.fsx: Guard expressions can be used with other patterns to restrict matches. let getAgeString (age : int) : string = match age with n when n < 1 -> "infant" | n when n < 13 -> "child" | n when n < 20 -> "teen" | _ -> "adult" printfn "A person aged %d is a/an %s" 50 (getAgeString 50) string for the st

11.5 List Patterns

Lists have a concatenation pattern associated with them. The "::" cons-operator is used to to match the head and the rest of a list, and "[]" is used to match an empty list, which is also sometimes called the nil-case. This is very useful when recursively processing lists, as shown in Listing 11.15 In the example, the function sumList

```
Listing 11.15 listPattern.fsx:

Recursively parsing a list with list patterns.

1 let rec sumList (lst : int list) : int =
2 match lst with
3 n :: rest -> n + (sumList rest)
4 | [] -> 0

5 let rec sumThree (lst : int list) : int =
7 match lst with
8 [a; b; c] -> a + b + c
9 | _ -> sumList lst

10 let aList = [1; 2; 3]
11 printfn "The sum of %A is %d, %d" aList (sumList aList)
12 (sumThree aList)

1 $ fsharpc --nologo listPattern.fsx && mono listPattern.exe
2 The sum of [1; 2; 3] is 6, 6
```

uses the cons operator to match the head of the list with n and the tail with rest. The pattern n :: tail also matches 3 :: [], and in that case tail would be assigned the value []. When 1st is empty, then it matches with "[]". List patterns can also be matched explicitly named elements, as demonstrated in the sumThree function. The elements to be matched can be any mix of constants and variables.

It is also possible to match on a series of cons-operators. For example elm0 :: elm1 :: rest would match a list with at least two elements, where the first will be bound to elm1, the second to elm2, and the remainder to rest.

11.6 Array, Record, and Discriminated Union Patterns

Array, record, and discriminated union patterns are direct extensions on constant, variable, and wildcard patterns. Listing 11.16 gives examples of array patterns. In

the function arrayToString, the first case matches arrays of 3 elements where the first is the integer 1, the second case matches arrays of 3 elements where the second is a 1 and names the first x, and the final case matches all arrays and works as a default match case. As demonstrated, the cases are treated from first to last, and only the expression of the first case that matches is executed.

For record patterns, we use the field names to specify matching criteria. This is demonstrated in Listing 11.17. Here, the record type Address is created, and in the function getZip, a variable pattern z is created for naming zip values, and the remaining fields are ignored. Since the fields are named, the pattern match need not mention the ignored fields, and the example match is equivalent to $\{zip = z\} \rightarrow z$. The curly brackets are required for record patterns.

Discriminated union patterns are similar. For discriminated unions with arguments, the arguments can be matched as constants, variables, or wildcards. A demonstration is given in Listing 11.18. In the project-function, three-dimensional vectors are

Listing 11.17 recordPattern.fsx: Variable patterns for records to match on field values. type Address = {street : string; zip : int; country : string} type Address = {street : string; zip : int; country : string} type Address = { street : "Universitetsparken 1"; zip = 2100; country = "Denmark"} tet getZip (adr : Address) : int = match adr with {street = _; zip = z; country = _} -> z printfn "The zip-code is: %d" (getZip contact) string for the string for

Listing 11.18 unionPattern.fsx: Matching on discriminated union types. type vector = Vec2D of float * float | Vec3D of float * float let project (vec : vector) : vector = match vec with Vec3D (a, b, _) -> Vec2D (a, b) | v -> v let v = Vec3D (1.0, -1.2, 0.9) printfn "%A -> %A" v (project v) f sharpc --nologo unionPattern.fsx && mono unionPattern.exe Vec3D (1.0, -1.2, 0.9) -> Vec2D (1.0, -1.2)

projected to two dimensions by removing the third element. Two-dimensional vectors are unchanged. The example uses the wildcard pattern to emphasize that the third element of three-dimensional vectors is ignored. Named arguments can also be matched, in which case ";" is used instead of "," to delimit the fields in the match.

11.7 Disjunctive and Conjunctive Patterns

Patterns may be combined using the "|" and "&" lexemes. These patterns are called disjunctive and conjunctive patterns, respectively, and work similarly to their logical operator counter parts, "||" and "&&".

Disjunctive patterns require at least one pattern to match, as illustrated in Listing 11.19. Here one or more cases must match for the final case expression, and

```
Listing 11.19 disjunctivePattern.fsx:

Patterns can be combined logically as 'or' syntax structures.

1 let vowel (c : char) : bool =
2 match c with
3 'a' | 'e' | 'i' | 'o' | 'u' | 'y' -> true
4 | _ -> false

5 String.iter (fun c -> printf "%A " (vowel c)) "abcdefg"

1 $ fsharpc --nologo disjunctivePattern.fsx && mono disjunctivePattern.exe
2 true false false false true false false
```

thus, any vowel results in the value **true**. Everything else is matched with the wildcard pattern.

For *conjunctive patterns*, all patterns must match, which is illustrated in Listing 11.20. In this case, we separately check the elements of a pair for the constant value 1 and

```
Listing 11.20 conjunctivePattern.fsx:

Patterns can be combined logically as 'and' syntax structures.

let is11 (v : int * int) : bool =
match v with
(1,_) & (_,1) -> true
| _ -> false

printfn "%A" (List.map is11 [(0,0); (0,1); (1,0); (1,1)])

$\frac{1}{2}$ fsharpc --nologo conjunctivePattern.fsx && mono conjunctivePattern.exe
[false; false; false; true]
```

return true only when both elements are 1. In many cases, conjunctive patters can be replaced by more elegant matches, e.g., using tuples, and in the above example a single case (1,1) -> true would have been simpler. Nevertheless, conjunctive patterns are used together with active patterns, to be discussed below.

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11.8 Active Patterns

The concept of patterns is extendable to functions. Such functions are called *active patterns*, and active patterns come in two flavors: regular and option types. The active pattern cases are constructed as function bindings, but using a special notation. They all take the pattern input as last argument, and may take further preceding arguments. The syntax for active patterns is one of,

```
Listing 11.21: Syntax for binding active patterns to expressions.

| let (|<caseName>|[_| ]) [ <arg> [<arg> ... ]] <inputArgument> = <expr>
| let (|<caseName>|<caseName>|...|<caseName>|) <inputArgumet> = <expr>
```

When using the (|<caseName>|_|]) variants, then the active pattern function must return an option type. (|<caseName>|<caseName>|...|<caseName>|) is the multi-case variant and must return a Fsharp.Core.Choice type. All other variants can return any type. There are no restrictions on arguments <arg>, and <inputArgumetn> is the input pattern to be matched. Notice in particular that the multi-case variant only takes one argument and cannot be combined with the option-type syntax. Below we will demonstrate by example how the various patterns are used.

The single case, (|<caseName>|]), matches all and is useful for extracting information from complex types, as demonstrated in Listing 11.22. Here we define a record to represent two-dimensional vectors and two different single case active patterns. Note that in the binding of the active pattern functions in line 2 and 3, the argument is the input expression match <inputExpr> with ..., see Listing 11.5. However, the argument for the cases in line 6 and 9 are names bound to the output of the active pattern function.

Both Cartesian and Polar match a vector record, but they dismantle the contents differently. For an alternative solution using Class types, see Section 23.1.

More complicated behavior is obtainable by supplying additional arguments to the single case. This is demonstrated in Listing 11.23. Here we supply an offset, which should be subtracted prior to calculating lengths and angles. Notice in line 8 that the argument is given prior to the result binding.

Active pattern functions return option types are called *partial pattern functions*. The option type allows for specifying mismatches, as illustrated in Listing 11.24. In the example, we use the (|<caseName>|_|]) variant to indicate that the active pattern returns an option type. Nevertheless, the result binding res in line 6 uses the underlying value of Some. And in contrast to the two previous examples of single case

Listing 11.22 activePattern.fsx: Single case active pattern for deconstructing complex types. type vec = {x : float; y : float} let (|Cartesian|) (v : vec) = (v.x, v.y) let (|Polar|) (v : vec) = (sqrt(v.x*v.x + v.y * v.y), atan2 v.y v.x) let printCartesian (p : vec) : unit = match p with Cartesian (x, y) -> printfn "%A:\n Cartesian (%A, %A)" let printPolar (p : vec) : unit = match p with Polar (a, d) -> printfn "%A:\n Polar (%A, %A)" p a d let $v = \{x = 2.0; y = 3.0\}$ printCartesian v printPolar v \$ fsharpc --nologo activePattern.fsx && mono activePattern.exe $\{ x = 2.0 \}$ y = 3.0 }: Cartesian (2.0, 3.0) $\{ x = 2.0 \}$ y = 3.0 }: Polar (3.605551275, 0.9827937232)

patterns, the value None results in a mismatch. Thus in this case, if the denominator is 0.0, then Div res does not match but the wildcard pattern does.

Multicase active patterns work similarly to discriminated unions without arguments. An example is given in Listing 11.25. In this example, we define three cases in line 1. The result of the active pattern function must be one of these cases. For the match-expression, the match is based on the output of the active pattern function, hence in line 8, the case expression is executed when the result of applying the active pattern function to the input expression i is Gold. In this case, a solution based on discriminated unions would probably be clearer.

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Listing 11.23 activeArgumentsPattern.fsx: All but the multi-case active pattern may take additional arguments. type vec = {x : float; y : float} let (|Polar|) (o : vec) (v : vec) = let x = v.x - o.xlet y = v.y - o.y(sqrt(x*x + y * y), atan2 y x)let printPolar (o : vec) (p : vec) : unit = match p with Polar o (a, d) -> printfn "%A:\n Cartesian (%A, %A)" p let $v = \{x = 2.0; y = 3.0\}$ let offset = $\{x = 1.0; y = 1.0\}$ printPolar offset v \$ fsharpc --nologo activeArgumentsPattern.fsx && mono activeArgumentsPattern.exe $\{ x = 2.0 \}$ y = 3.0 }: Cartesian (2.236067977, 1.107148718)

Listing 11.25 activeMultiCasePattern.fsx:

Multi-case active patterns have a syntactical structure similar to discriminated unions.

```
let (|Gold|Silver|Bronze|) inp =
  if inp = 0 then Gold
  elif inp = 1 then Silver
  else Bronze
let intToMedal (i : int) =
    match i with
      Gold -> printfn "%d: It's gold!" i
      | Silver -> printfn "%d: It's silver." i
      | Bronze -> printfn "%d: It's no more than bronze." i
List.iter intToMedal [0..3]
$ fsharpc --nologo activeMultiCasePattern.fsx && mono
  activeMultiCasePattern.exe
0: It's gold!
1: It's silver.
2: It's no more than bronze.
3: It's no more than bronze.
```

11.9 Static and Dynamic Type Pattern

Input patterns can also be matched on type. For *static type matching*, the matching is performed at compile time and indicated using the ":" lexeme followed by the type name to be matched. Static type matching is further used as input to the type inference performed at compile time to infer non-specified types, as illustrated in Listing 11.26. Here the head of the list n in the list pattern is explicitly matched as

an integer, and the type inference system thus concludes that 1st must be a list of integers.

In contrast to static type matching, *dynamic type matching* is performed at runtimes and indicated using the ":?" lexeme followed by a type name. Dynamic type patterns allow for matching generic values at runtime. This is an advanced topic, which is included here for completeness. An example is given in Listing 11.27. In F#, all types

are also objects whose type is denoted obj. Thus, the example uses the generic type when defining the argument to isString, and then dynamic type pattern matching for further processing. See Chapter 23 for more on objects. Dynamic type patterns are often used for analyzing exceptions, which is discussed in Section 13.1. While

★ dynamic type patterns are useful, they imply runtime checking, and it is almost always better to prefer compile time over runtime type checking.

11.10 Key concepts and terms in this chapter

Summary text about the key concepts from this chapter

• . . .

Chapter 12

Programming with Types

F# is a strongly typed language, meaning that types are known or inferred at compile time. In the previous chapters, we have used *primitive types* such as float and bool, function types, and compound types implicitly defined by tuples. These types are used for simple programming tasks, and everything that can be programmed can be accomplished using these types. However, larger programs are often easier to read and write when using more complicated type structures. In this chapter, we will discuss type abbreviations, enumerated types, discriminated unions, records, and structs. Class types are discussed in depth in Chapter 23.

12.1 Type Abbreviations

F# allows for renaming of types, which is called *type abbreviation* or *type aliasing*. The syntax is:

```
Listing 12.1: Syntax for type abbreviation.

type <ident> = <aType>
```

where the identifier is a new name, and the type-name is an existing type or a compound of existing types. Listing 12.2 shows examples of the defintion of several type abbreviations. Here we define the abbreviations size, position, person, and intToFloat, and later make bindings enforcing the usage of these abbreviations.

Type abbreviations are used as short abbreviations of longer types, and they add semantic content to the program text, thus making programs shorter and easier to read. Type abbreviations allow the programmer to focus on the intended structure at a higher level by, e.g., programming in terms of a type position rather than float

Listing 12.2 typeAbbreviation.fsx: Defining four type abbreviations, three of which are compound types. 1 type size = int 2 type position = float * float 3 type person = string * int 4 type intToFloat = int -> float 5 6 let sz : size = 3 7 let pos : position = (2.5, -3.2) 8 let pers : person = ("Jon", 50) 9 let conv : intToFloat = fun a -> float a 10 printfn "%A, %A, %A, %A" sz pos pers (conv 2) 1 \$ fsharpc --nologo typeAbbreviation.fsx && mono typeAbbreviation.exe 2 3, (2.5, -3.2), ("Jon", 50), 2.0

* float. Thus, they often result in programs with fewer errors. Type abbreviations also make maintenance easier. For instance, if we at a later stage decide that positions can only have integer values, then we only need to change the definition of the type abbreviation, not every place a value of type position is used.

12.2 Enumerations

Enumerations or *enums* for short are types with named values. Names in enums are assigned to a subset of integer or char values. Their syntax is as follows:

An example of using enumerations is given in Listing 12.4. In this example, we define an enumerated type for medals, which allows us to work with the names rather than the values. Since the values most often are arbitrary, we can program using semantically meaningful names instead. Being able to refer to an underlying integer type allows us to interface with other – typically low-level – programs that require integers, and to perform arithmetic. E.g., for the medal example, we can typecast the enumerated types to integers and calculate an average medal harvest.

Listing 12.4 enum.fsx: An enum type acts as a typed alias to a set of integers or chars. 1 type medal = 2 Gold = 0 3 | Silver = 1 4 | Bronze = 2 5 let aMedal = medal.Gold 7 printfn "%A has value %d" aMedal (int aMedal) 1 \$ fsharpc --nologo enum.fsx && mono enum.exe 2 Gold has value 0

12.3 Discriminated Unions

A discriminated union is a union of a set of named cases. These cases can further be of specified types. The syntax for defining a discriminated union is as follows:

Discriminated unions are reference types, i.e., their content is stored on *The Heap*, see Section 20.2 for a discussion on reference types. Since they are immutable, there is no risk of side-effects. As reference types, they only pass a reference when used as arguments to and returned from a function. This is in contrast to value types, which transport a complete copy of the data structure. Discriminated unions are thus effective for large data structures. Discriminated unions can also be represented as structures using the [<Struct>] attribute, in which case they are value types. See Section 12.5 for a discussion on structs.

An example just using the named cases but no further specification of types is given in Listing 12.6. Here, we define a discriminated union as three named cases signifying three different types of medals. Comparing with the enumerated type in Listing 12.4, we see that the only difference is that the cases of the discriminated unions have no value. A commonly used discriminated union is the *option type*, see Section 13.2 for more detail.

Discriminated unions may also be used to store data. Where the names in enumerated types are aliases of single values, the names used in discriminated unions can hold

Listing 12.6 discriminated Unions.fsx: A discriminated union of medals. Compare with Listing 12.4. type medal = Gold Silver Fronze let aMedal = medal.Gold printfn "%A" aMedal fsharpc --nologo discriminatedUnions.fsx && mono discriminatedUnions.exe Gold

any value specified at the time of creation. An example is given in Listing 12.7. In this case, we define a discriminated union of two and three-dimensional vectors.

Values of these types are created using their names followed by a tuple of their arguments. The names are also called field names. The field names may be used when creating discrimated union values, as shown in Line 6. When used, then the arguments may be given in arbitrary order, nevertheless, values for all fields must be given.

Discriminated unions can be defined recursively. This feature is demonstrated in Listing 12.8. In this example we define a tree as depicted in Figure 12.1.

Pattern matching must be used in order to define functions on values of a discriminated union. E.g., in Listing 12.9 we define a function that traverses a tree and prints the content of the nodes.

Discriminated unions are very powerful and can often be used instead of class hierarchies. Class hierarchies are discussed in Section 24.1.

137 12.4 *Records*

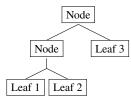


Fig. 12.1 The tree with 3 leaves.

```
Listing 12.9 discriminatedUnionPatternMatching.fsx:

A discriminated union modelling binary trees.

1 type Tree = Leaf of int | Node of Tree * Tree
2 let rec traverse (t : Tree) : string =
3 match t with
4 Leaf(v) -> string v
6 | Node(left, right) -> (traverse left) + ", " +
6 (traverse right)

6 let tree = Node (Node (Leaf 1, Leaf 2), Leaf 3)
8 printfn "%A: %s" tree (traverse tree)

1 $ fsharpc --nologo discriminatedUnionPatternMatching.fsx &&
6 mono discriminatedUnionPatternMatching.exe
2 Node (Node (Leaf 1, Leaf 2), Leaf 3): 1, 2, 3
```

12.4 Records

A record is a compound of named values, and a record type is defined as follows:

```
Listing 12.10: Syntax for defining record types.

[ <attributes> ]
type <ident> = {
        [ mutable ] <label1> : <type1>
        [ mutable ] <label2> : <type2>
        ...
}
```

Records are collections of named variables and values of possibly different types. They are reference types, and thus their content is stored on *The Heap*, see Section 20.2 for a discussion on reference types. Records can also be *struct records* using the [<Struct>] attribute, in which case they are value types. See Section 12.5 for a discussion on structs. An example of using records is given in Listing 12.11. The values of individual members of a record are obtained using the "." notation This

```
Listing 12.11 records.fsx:

A record is defined for holding information about a person.

type person = {
    name : string
    age : int
    height : float
}

let author = {name = "Jon"; age = 50; height = 1.75}

printfn "%A\nname = %s" author author.name

fsharpc --nologo records.fsx && mono records.exe

name = "Jon"

age = 50
    height = 1.75 }

name = Jon
```

example illustrates a how record type is used to store varied data about a person.

If two record types are defined with the same label set, then the latter dominates the former. This is demonstrated in Listing 12.12. In the example, two identical record types are defined, and we use the built-in GetType() method to inspect the type of bindings. We see that lecturer is of RecordsDominance+teacher type, since teacher dominates the identical person type definition. However, we may enforce the person type by either specifying it for the name, as in let author: person = ..., or by fully or partially specifying it in the record expression following the "=" sign. In both cases, they are of RecordsDominance+person type. The built-in GetType() method is inherited from the base class for all types, see Chapter 23 for a discussion on classes and inheritance.

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Listing 12.12 recordsDominance.fsx:

Redefined types dominate old record types, but earlier definitions are still accessible using explicit or implicit specification for bindings.

```
type person = { name : string; age : int; height : float }
type teacher = { name : string; age : int; height : float }
let lecturer = {name = "Jon"; age = 50; height = 1.75}
printfn "%A : %A" lecturer (lecturer.GetType())
let author : person = {name = "Jon"; age = 50; height = 1.75}
printfn "%A : %A" author (author.GetType())
let father = {person.name = "Jon"; age = 50; height = 1.75}
printfn "%A : %A" author (author.GetType())
$ fsharpc --nologo recordsDominance.fsx && mono
   recordsDominance.exe
{ name = "Jon"
  age = 50
  height = 1.75 } : RecordsDominance+teacher
{ name = "Jon"
  age = 50
  height = 1.75 } : RecordsDominance+person
{ name = "Jon"
  age = 50
  height = 1.75 } : RecordsDominance+person
```

Note that when creating a record you must supply a value to all fields, and you cannot refer to other fields of the same record, i.e., {name = "Jon"; age = height * 3; height = 1.75} is illegal.

Since records are per default reference types, binding creates aliases, not copies. This matters for mutable members, in which case when copying, we must explicitly create a new record with the old data. Copying can be done either by using referencing to the individual members of the source or using the short-hand with notation. This is demonstrated in Listing 12.13. Here, age is defined as a mutable value and can be changed using the usual "<-" assignment operator. The example demonstrates two different ways to create records. Note that when the mutable value author age is changed in line 10, then authorAlias also changes, since it is an alias of author, but neither authorCopy nor authorCopyAlt changes, since they are copies. As illustrated, copying using with allows for easy copying and partial updates of another record value.

Listing 12.13 recordCopy.fsx:

Bindings are references. To copy and not make an alias, explicit copying must be performed.

```
type person = {
 name : string;
 mutable age : int;
let author = {name = "Jon"; age = 50}
let authorAlias = author
let authorCopy = {name = author.name; age = author.age}
let authorCopyAlt = {author with name = "Noj"}
author.age <- 51</pre>
printfn "author : %A" author
printfn "authorAlias : %A" authorAlias
printfn "authorCopy : %A" authorCopy
printfn "authorCopyAlt : %A" authorCopyAlt
$ fsharpc --nologo recordCopy.fsx && mono recordCopy.exe
author : { name = "Jon"
 age = 51 }
authorAlias : { name = "Jon"
 age = 51 }
authorCopy : { name = "Jon"
 age = 50 }
authorCopyAlt : { name = "Noj"
  age = 50 }
```

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12.5 Structures

Structures, or structs for short, have much in common with records. They specify a compound type with named fields, but they are value types, and they allow for some customization of what is to happen when a value of its type is created. Since they are value types, they are best used for small amounts of data. The syntax for defining struct types are:

The syntax makes use of the *val* and *new* keywords. Like let, the keyword *val* binds a name to a value, but unlike let, the value is always the type's default value. The *new* keyword denotes the function used to fill values into the fields at time of creation. This function is called the *constructor*. No let or do-bindings are allowed in structure definitions. Fields are accessed using the "." notation. An example is given in Listing 12.15.

```
Listing 12.15 struct.fsx:

Defining a struct type and creating a value of it.

[ <Struct > ]

type position =

val x : float

val y : float

new (a : float, b : float) = {x = a; y = b}

let p = position (3.0, 4.2)

printfn "%A: x = %A, y = %A" p p.x p.y

fsharpc --nologo struct.fsx && mono struct.exe

Struct+position: x = 3.0, y = 4.2
```

Structs are small versions of classes and allows, e.g., for overloading of the new constructor and for overriding of the inherited *ToString()* function. This is demonstrated in Listing 12.16. We defer further discussion of these concepts to Chapter 23.

Listing 12.16 structOverloadNOverride.fsx: Overloading the constructor and overriding the default ToString() function. [<Struct>] type position = val x : float val y : float new (a : float, b : float) = $\{x = a; y = b\}$ new (a : int, b : int) = {x = float a; y = float b} override this.ToString() = "(" + (string this.x) + ", " + (string this.y) + ")" let pFloat = position (3.0, 4.2) let pInt = position (3, 4) printfn "%A and %A" pFloat pInt \$ fsharpc --nologo structOverloadNOverride.fsx && mono structOverloadNOverride.exe (3, 4.2) and (3, 4)

The use of structs are generally discouraged, and instead, it is recommended to use enums, records, and discriminated unions, possibly with the [<Struct>] attribute for the last two in order to make them value types.

12.6 Variable Types

An advanced topic in F# is *variable types*. There are three different versions of variable types in F#: *runtime resolved*, which have the syntax '<ident>, *anonymous*, which are written as "_", and *statically resolved*, which have the syntax ^<ident>. Variable types are particularly useful for functions that work for many types. An example of a generic function and its use is given in Listing 12.17. In this example, the

```
Listing 12.17 variable Type.fsx:
A function apply with runtime resolved types.

1 let apply (f : 'a -> 'a -> 'a) (x : 'a) (y : 'a) : 'a = f x y
2 let intPlus (x : int) (y : int) : int = x + y
3 let floatPlus (x : float) (y : float) : float = x + y
4 printfn "%A %A" (apply intPlus 1 2) (apply floatPlus 1.0 2.0)

1 $ fsharpc --nologo variable Type.fsx && mono variable Type.exe
2 3 3.0
```

function apply has runtime resolved variable type, and it accepts three parameters: f, x, and y. The function will work as long as the parameters for f is a function of two parameters of identical type, and f and f are values of the same type. Thus, in the printfn statement we are able to use apply for both an integer and a float variant.

The example in Listing 12.17 illustrates a very complicated way to add two numbers. The "+" operator works for both types out of the box, so why not something simpler like relying on the F# type inference system by not explicitly specifying types, as attempted in Listing 12.18? Unfortunately, the example fails to compile, since

```
Listing 12.18 variableTypeError.fsx:
Even though the "+" operator is defined for both integers and floats, the type
inference is static and infers plus: int -> int.
let plus x y = x + y
 printfn "%A %A" (plus 1 2) (plus 1.0 2.0)
$ fsharpc --nologo variableTypeError.fsx && mono
    variableTypeError.exe
 variableTypeError.fsx(3,34): error FS0001: This expression
    was expected to have type
     'int'
but here has type
     'float'
 variableTypeError.fsx(3,38): error FS0001: This expression
    was expected to have type
     'int'
but here has type
     'float'
```

the type inference is performed at compile time, and by plus 1 2, it is inferred that plus: int -> int. Hence, calling plus 1.0 2.0 is a type error. Function bindings allow for the use of the *inline* keyword, and adding this successfully reuses the definition of plus for both types, as shown in Listing 12.19. In the example, adding the *inline* does two things: Firstly, it copies the code to be performed to each place the function is used, and secondly, it forces statically resolved variable type checking independently in each place. The type annotations inferred as a result of the *inline*-keyword may be written explicitly, as shown in Listing 12.20. The example in Listing 12.20 demonstrates the statically resolved variable type syntax, ^<ident>, as well as the use of *type constraints*, using the keyword *when*. Type constraints have a rich syntax, but will not be discussed further in this book. In the example, the type constraint when ^a: (static member (+): ^a * ^a -> ^a) is given using the object-oriented properties of the type variable ^a, meaning that the only acceptable type values are those which have a member function (+)

Listing 12.19 variableTypeInline.fsx:

The keyword forces static and independent inference each place the function is used. Compare to the error case in Listing 12.18.

```
1 let inline plus x y = x + y
2
3 printfn "%A %A" (plus 1 2) (plus 1.0 2.0)
1 $ fsharpc --nologo variableTypeInline.fsx && mono variableTypeInline.exe
2 3 3.0
```

Listing 12.20 compiletimeVariableType.fsx:

Explicitly spelling out of the statically resolved type variables from Listing 12.18.

```
1 let inline plus (x : ^a) (y : ^a) : ^a when ^a : (static
    member ( + ) : ^a * ^a -> ^a) = x + y
2
3 printfn "%A %A" (plus 1 2) (plus 1.0 2.0)

1 $ fsharpc --nologo compiletimeVariableType.fsx && mono
    compiletimeVariableType.exe
2 3 3.0
```

taking a tuple and giving a value all of identical type, and where the type can be inferred at compile time. See Chapter 23 for details on member functions.

The inline construction is useful when generating generic functions and still profiting from static type checking. However, explicit copying of functions is often something better left to the compiler to optimize over. An alternative seems to be using runtime resolved variable types with the '<ident> syntax. Unfortunately, this is not possible in case of most operators, since they have been defined in the FSharp.Core namespace to be statically resolved variable types. E.g., the "+" operator has type (+) : ^T1 -> ^T2 -> ^T3 (requires ^T1 with static member (+) and ^T2 with static member (+)).

Chapter 13

Handling Errors and Exceptions

13.1 Exceptions

Exceptions are runtime errors, such as division by zero. E.g., attempting integer division by zero halts execution and a long somewhat cryptic error message is written to screen, as illustrated in Listing 13.1. The error message contains much information.

The first part, System.DivideByZeroException: Attempted to divide by zero is the error-name with a brief ellaboration. Then follows a list libraries that were involved when the error occurred, and finally F# states that it Stopped due to error. System.DivideByZeroException is a built-in exception type, and the built-in integer division operator chooses to raise the exception when the undefined division by zero is attempted. Many times such errors can be avoided by clever program design. However, this is not always possible or desirable, which is why F# implements exception handling for graceful control.

Exceptions are a basic-type called *exn*, and F# has a number of built-in ones, a few of which are listed in Table 13.1.

| Attribute | Description | |
|--------------------------|---|--|
| ArgumentException | Arguments provided are invalid. | |
| DivideByZeroException | Division by zero. | |
| NotFiniteNumberException | floating point value is plus or minus infinity, or Not-a-Number | |
| | (NaN). | |
| OverflowException | Arithmetic or casting caused an overflow. | |
| IndexOutOfRangeException | Attempting to access an element of an array using an index which | |
| | is less than zero or equal or greater than the length of the array. | |

Table 13.1 Some built-in exceptions. The prefix System. has been omitted for brevity.

Exceptions are handled by the try-keyword expressions. We say that an expression may *raise* or *cast* an exception and that the try-expression may *catch* and *handle* the exception by another expression.

Exceptions like in Listing 13.1 may be handled by try—with expressions, as demonstrated in Listing 13.2. In the example, when the division operator raises the

```
Listing 13.2 exceptionDivByZero.fsx:

A division by zero is caught and a default value is returned.

1 let div enum denom =
2 try
3 enum / denom
4 with
5 | :? System.DivideByZeroException -> System.Int32.MaxValue
6 printfn "3 / 1 = %d" (div 3 1)
8 printfn "3 / 0 = %d" (div 3 0)

1 $ fsharpc --nologo exceptionDivByZero.fsx && mono exceptionDivByZero.exe
2 3 / 1 = 3
3 3 / 0 = 2147483647
```

System.DivideByZeroException exception, then try—with catches it and returns the value System.Int32.MaxValue. Division by zero is still an undefined operation, but with the exception system, the program is able to receive a message about this undefined situation and choose an appropriate action.

The try expressions comes in two flavors: try-with and try-finally expressions.

The try-with expression has the following syntax,

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where <testExpr> is an expression which might raise an exception, <path> is a pattern, and <exprHndln> is the corresponding exception handler. The value of the try-expression is either the value of <testExpr>, if it does not raise an exception, or the value of the exception handler <exprHndln> of the first matching pattern <path>. The above is using lightweight syntax. Regular syntax omits newlines.

In Listing 13.2 dynamic type matching is used (see Section 11.9) using the ":?" lexeme, i.e., the pattern matches exception with type System.DivideByZeroException at runtime. The exception value may contain furter information and can be accessed if named using the as-keyword, as demonstrated in Listing 13.4. Here the exception

```
Listing 13.4 exceptionDivByZeroNamed.fsx:
Exception value is bound to a name. Compare to Listing 13.2.
let div enum denom =
   try
     enum / denom
   with
     | :? System.DivideByZeroException as ex ->
       printfn "Error: %s" ex.Message
       System.Int32.MaxValue
printfn "3 / 1 = %d" (div 3 1)
printfn "3 / 0 = %d" (div 3 0)
$ fsharpc --nologo exceptionDivByZeroNamed.fsx && mono
    exceptionDivByZeroNamed.exe
3 / 1 = 3
Error: Attempted to divide by zero.
3 / 0 = 2147483647
```

value is bound to the name ex.

All exceptions may be caught as the dynamic type System.Exception, and F# implements a short-hand for catching an exception and binding its value to a name as demonstrated in Listing 13.5 Finally, the short-hand may be guarded with a when—guard, as demonstrated in Listing 13.6. The first pattern only matches the System.Exception exception when enum is 0, in which case the exception handler returns 0.

Listing 13.5 exceptionDivByZeroShortHand.fsx:

An exception of type System. Exception is bound to a name. Compare to Listing 13.4.

```
let div enum denom =
try
enum / denom
with
| ex -> printfn "Error: %s" ex.Message;
System.Int32.MaxValue

printfn "3 / 1 = %d" (div 3 1)
printfn "3 / 0 = %d" (div 3 0)

$\frac{1}{2}$ fsharpc --nologo exceptionDivByZeroShortHand.fsx && mono exceptionDivByZeroShortHand.exe
3 / 1 = 3
Error: Attempted to divide by zero.
3 / 0 = 2147483647
```

Listing 13.6 exceptionDivByZeroGuard.fsx:

An exception of type System. Exception is bound to a name and guarded. Compare to Listing 13.5.

```
let div enum denom =
try
enum / denom
with
| ex when enum = 0 -> 0
| ex -> System.Int32.MaxValue

printfn "3 / 1 = %d" (div 3 1)
printfn "3 / 0 = %d" (div 3 0)
printfn "0 / 0 = %d" (div 0 0)

f $fsharpc --nologo exceptionDivByZeroGuard.fsx && mono
exceptionDivByZeroGuard.exe
3 / 1 = 3
3 / 0 = 2147483647
4 0 / 0 = 0
```

Thus, if you don't care about the type of exception, then you need only use the short-hand pattern matching and name binding demonstrated in Listing 13.5 and Listing 13.6, but if you would like to distinguish between types of exceptions, then you must use explicit type matching and possibly value binding demonstrated in Listing 13.2 and Listing 13.4

The *try-finally* expression has the following syntax,

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```
Listing 13.7: Syntax for the try-finally exception handling.

try

try

testExpr>
finally

cleanupExpr>
```

The try-finally expression evaluates the <cleanupExpr> expression following evaluation of the <testExpr>, regardless of whether an exception is raised or not, as illustrated in Listing 13.8. Here, the finally branch is evaluated following the

```
Listing 13.8 exceptionDivByZeroFinally.fsx:
           branch is executed regardless of an exception.
let div enum denom =
  printf "Doing division:"
    printf " %d %d." enum denom
     enum / denom
  finally
    printfn " Division finished."
printfn "3 / 1 = %d" (try div 3 1 with ex -> 0)
printfn "3 / 0 = %d" (try div 3 0 with ex -> 0)
$ fsharpc --nologo exceptionDivByZeroFinally.fsx && mono
    exceptionDivByZeroFinally.exe
Doing division: 3 1. Division finished.
3 / 1 = 3
Doing division: 3 0. Division finished.
3 / 0 = 0
```

evaluation of the test expression regardless of whether the test expression raises an exception or not. However, if an exception is raised in a try-finally expression and there is no outer try-with expression, then execution stops without having evaluated the finally branch.

Exceptions can be raised using the raise-function,

```
Listing 13.9: Syntax for the raise function that raises exceptions.

| raise (<expr>)
```

An example of raising the System.ArgumentException is shown in Listing 13.10 In this example, division by zero is never attempted and instead an exception is raised which must be handled by the caller. Note that the type of div is int -> int -> int because denom is compared with an integer in the conditional statement. This contradicts the typical requirements for if statements, where every branch has to return the same type. However, any code that explicitly raise exceptions are ignored, and the type is inferred by the remaining branches.

Programs may define new exceptions using the syntax,

```
Listing 13.11: Syntax for defining new exceptions.

exception <ident> of <typeId> {* <typeId>}
```

An example of defining a new exception and raising it is given in Listing 13.12. Here

an exception called DontLikeFive is defined, and it is raised in the function picky. The example demonstrates that catching the exception as a System. Exception as in Listing 13.5, the Message property includes information about the exception

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name but not its argument. To retrieve the argument "5 sucks", we must match the exception with the correct exception name, as demonstrated in Listing 13.13.

```
Listing 13.13 exceptionDefinitionNCatch.fsx:
Catching a user-defined exception.
exception DontLikeFive of string
let picky a =
  if a = 5 then
    raise (DontLikeFive "5 sucks")
  else
try
  printfn "picky %A = %A" 3 (picky 3)
  printfn "picky %A = %A" 5 (picky 5)
  | DontLikeFive msg -> printfn "Exception caught with
   message: %s" msg
$ fsharpc --nologo exceptionDefinitionNCatch.fsx && mono
    exceptionDefinitionNCatch.exe
picky 3 = 3
Exception caught with message: 5 sucks
```

F# includes the <code>failwith</code> function to simplify the most common use of exceptions. It is defined as <code>failwith</code>: <code>string</code> -> <code>exn</code> and takes a string and raises the builtin <code>System.Exception</code> exception. An example of its use is shown in Listing 13.14. To catch the <code>failwith</code> exception, there are several choices. The exception casts a

```
Listing 13.14 exceptionFailwith.fsx:

An exception raised by failwith.

if true then failwith "hej"

$\fsharpc --nologo exceptionFailwith.fsx && mono exceptionFailwith.exe

Unhandled Exception:
$\fsystem.Exception: hej
at
    <StartupCode\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\frac{\f
```

System. Exception exception, which may be caught using the :? pattern, as shown

in Listing 13.15. However, this gives annoying warnings, since F# internally is built

```
Listing 13.15 exceptionSystemException.fsx:

Catching a failwith exception using type matching pattern.

let _ = 
try 
failwith "Arrrrg"
with 
:? System.Exception -> printfn "So failed"

sharpc --nologo exceptionSystemException.fsx && mono exceptionSystemException.exe

exceptionSystemException.fsx(5,5): warning FS0067: This type test or downcast will always hold

exceptionSystemException.fsx(5,5): warning FS0067: This type test or downcast will always hold

so failed
```

such that all exception match the type of System. Exception. Instead, it is better to either match using the wildcard pattern as in Listing 13.16, or use the built-in

```
Listing 13.16 exceptionMatchWildcard.fsx:

Catching a failwith exception using the wildcard pattern.

let _ = 
try
failwith "Arrrrg"
with
_ --> printfn "So failed"

standard fsx:

fsharpc --nologo exceptionMatchWildcard.fsx && mono exceptionMatchWildcard.exe
So failed
```

Failure pattern as in Listing 13.17. Notice how only the Failure pattern allows for the parsing of the message given to failwith as an argument.

Invalid arguments are such a common reason for failures, that a built-in function for handling them has been supplied in F#. The <code>invalidArg</code> takes 2 strings and raises the built-in <code>ArgumentException</code>, as shown in Listing 13.18. The <code>invalidArg</code> function raises an <code>System.ArgumentException</code>, as shown in Listing 13.19.

The **try** construction is typically used to gracefully handle exceptions, but there are times where you may want to pass on the bucket, so to speak, and re-raise the exception. This can be done with the *reraise*, as shown in Listing 13.20. The

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Listing 13.17 exceptionFailure.fsx: Catching a failwith exception using the Failure pattern. let _ = try failwith "Arrrrg" with Failure msg -> printfn "The castle of %A" msg fsharpc --nologo exceptionFailure.fsx && mono exceptionFailure.exe The castle of "Arrrrg"

reraise function is only allowed to be the final call in the expression of a with rule.

Listing 13.19 exceptionInvalidArgNCatch.fsx: Catching the exception raised by invalidArg. let _ = try invalidArg "a" "is too much 'a'" with :? System.ArgumentException -> printfn "Argument is no good!"

\$ fsharpc --nologo exceptionInvalidArgNCatch.fsx && mono exceptionInvalidArgNCatch.exe 2 Argument is no good!

Listing 13.20 exceptionReraise.fsx: Reraising an exception.

```
let _ =
  try
    failwith "Arrrrg"
  with
    Failure msg ->
     printfn "The castle of %A" msg
      reraise()
$ fsharpc --nologo exceptionReraise.fsx && mono
   exceptionReraise.exe
The castle of "Arrrrg"
Unhandled Exception:
System.Exception: Arrrrg
  at
   <StartupCode$exceptionReraise>.$ExceptionReraise$fsx.main@
   () [0x00041] in <62028a640317d799a7450383648a0262>:0
[ERROR] FATAL UNHANDLED EXCEPTION: System.Exception: Arrrrg
   <StartupCode$exceptionReraise>.$ExceptionReraise$fsx.main@
   () [0x00041] in <62028a640317d799a7450383648a0262>:0
```

13.2 Option Types

At exceptions, it is not always obvious what should be returned. E.g., in the Listing 13.2, the exception is handled gracefully, but the return value is somewhat arbitrarily chosen to be the largest possible integer. Instead, we may use the *option type*. The option type is a wrapper that can be put around any type, and which extends the type with the special value *None*. All other values are preceded by the *Some* identifier. An example of rewriting Listing 13.2 to correctly represent the non-computable value is shown in Listing 13.21. The value of an option type

can be extracted and tested for by its member functions, *IsNone*, *IsSome*, and *Value*, as illustrated in Listing 13.22. The Value member is not defined for None,

```
Listing 13.22 option.fsx:
Simple operations on option types.

1 let a = Some 3;
2 let b = None;
3 printfn "%A %A" a b
4 printfn "%A %b %b" a.Value b.IsSome b.IsNone

1 $ fsharpc --nologo option.fsx && mono option.exe
2 Some 3 None
3 false true
```

thus it is adviced to prefer explicit pattern matching for extracting values from an option type. An example is: let get (opt : 'a option) (def : 'a) = match opt with Some $x \rightarrow x \mid _ \rightarrow$ def. Note also that printf prints the value None as <null>. This author hopes that future versions of the option type will have better visual representations of the None value.

Functions on option types are defined using the *option*-keyword. E.g., to define a function with explicit type annotation that always returns None, write let f (x: 'a option) = None.

F# includes an extensive Option module. It defines, among many other functions, Option.bind which implements let bind f opt = match opt with None -> None | Some x -> f x. The function Option.bind is demonstrated in Listing 13.23. The Option.bind is a useful tool for cascading functions that evaluates

```
Listing 13.23: Using Option.bind to perform calculations on option types.

| > Option.bind (fun x -> Some (2*x)) (Some 3);;
| val it : int option = Some 6
```

to option types.

13.3 Programming Intermezzo: Sequential Division of Floats

The following problem illustrates cascading error handling:

```
Problem 13.1 iven a list of floats such as [1.0; 2.0; 3.0], calculate the sequential division 1.0/2.0/3.0.
```

A sequential division is safe if the list does not contain zero values. However, if any element in the list is zero, then error handling must be performed. An example using failwith is given in Listing 13.24. In this example, a recursive function is defined which updates an accumulator element, initially set to the neutral value 1.0. Division by zero results in a failwith exception, wherefore we must wrap its use in a try—with expression.

Instead of using exceptions, we may use Option.bind. In order to use Option.bind for a sequence of non-option floats, we will define a division operator that reverses the order of operands. This is shown in Listing 13.25. Here the function divideBy takes two non-option arguments and returns an option type. Thus, Option.bind (divideBy 2.0) (Some 1.0) is equal to Some 0.5, since divideBy 2.0 is a function that divides any float argument by 2.0. Iterating Option.bind (divideBy 3.0) (Some 0.5), we calculate Some 0.16666666667 or Some (1.0/6.0), as expected. In Listing 13.25, this is written as a single letbinding using piping. Since Option.bind correctly handles the distinction between Some and None values, such piping sequences correctly handle possible errors, as shown in Listing 13.25.

Listing 13.24 seqDiv.fsx: Sequentially dividing a list of numbers. 1 let rec seqDiv acc lst = 2 match lst with 3 | [] -> acc 4 | elm::rest when elm <> 0.0 -> seqDiv (acc/elm) rest 5 | _ -> failwith "Division by zero" 6 7 try 8 printfn "%A" (seqDiv 1.0 [1.0; 2.0; 3.0]) 9 printfn "%A" (seqDiv 1.0 [1.0; 0.0; 3.0]) 10 with 11 Failure msg -> printfn "%s" msg 1 \$ fsharpc --nologo seqDiv.fsx && mono seqDiv.exe 2 0.1666666667 3 Division by zero

Listing 13.25 seqDivOption.fsx: Sequentially dividing a sequence of numbers using Option.bind. Compare with Listing 13.24. let divideBy denom enum = if denom = 0.0 then None else Some (enum/denom) let success = Some 1.0 |> Option.bind (divideBy 2.0) |> Option.bind (divideBy 3.0) printfn "%A" success let fail = Some 1.0 |> Option.bind (divideBy 0.0) |> Option.bind (divideBy 3.0) printfn "%A; isNone: %b" fail fail.IsNone \$ fsharpc --nologo seqDivOption.fsx && mono seqDivOption.exe Some 0.166666667 None; isNone: true

The sequential application can be extended to lists, using List.foldBack, as demonstrated in Listing 13.26. Since List.foldBack processes the list from the right, the list of integers has been reversed. Notice how divideByOption is the function spelled out in each piping step of Listing 13.25.

Listing 13.26 seqDivOptionAdv.fsx: Sequentially dividing a list of numbers, using Option.bind and List.foldBack. Compare with Listing 13.25. let divideBy denom enum = if denom = 0.0 then None else Some (enum/denom) let divideByOption x acc = Option.bind (divideBy x) acc let success = List.foldBack divideByOption [3.0; 2.0; 1.0] (Some 1.0) printfn "%A" success let fail = List.foldBack divideByOption [3.0; 0.0; 1.0] (Some printfn "%A; isNone: %A" fail fail.IsNone \$ fsharpc --nologo seqDivOptionAdv.fsx && mono seqDivOptionAdv.exe Some 0.166666667 None; isNone: true

Exceptions and option type are systems to communicate errors up through a hierarchy of function calls. While exceptions favor imperative style programming, option types belong to functional style programming. Exceptions allow for a detailed report of the type of error to the caller, whereas option types only allow for flagging that an error has occurred.

Chapter 14

Working With Files

An important part of programming is handling data. A typical source of data is hard-coded bindings and expressions from libraries or the program itself, and the result is often shown on a screen as text output on the console. This is a good starting point when learning to program, and one which we have relied heavily upon in this book until now. However, many programs require more: We often need to ask a user to input data via, e.g., typing text on a keyboard, clicking with a mouse, or striking a pose in front of a camera. We also often need to load and save data to files, retrieve and deposit information from the internet, and visualize data graphically, as sounds, or by controlling electrical appliances. Graphical user interfaces will be discussed in Chapter 15, and here we will concentrate on working with the console, files, and the general concept of streams.

File and stream input and output are supported via built-in namespaces and classes. For example, the printf family of functions discussed in ?? is defined in the Printf module of the Fsharp.Core namespace, and it is used to put characters on the stdout stream, i.e., to print on the screen. Likewise, ReadLine discussed in ?? is defined in the System.Console class, and it fetches characters from the stdin stream, that is, reads the characters the user types on the keyboard until newline is pressed.

A *file* on a computer is a resource used to store data in and retrieve data from. Files are often associated with a physical device, such as a hard disk, but can also be a virtual representation in memory. Files are durable, such that other programs can access them independently, given certain rules for access. A file has a name, a size, and a type, where the type is related to the basic unit of storage such as characters, bytes, and words, (char, byte, and int32). Often data requires a conversion between the internal format to and from the format stored in the file. E.g., floating point numbers are sometimes converted to a UTF8 string using fprintf in order to store them in a file in a human-readable form, and interpreted from UTF8 when retrieving them at a later point from the file. Files have a low-level structure, which varies from device

to device, and the low-level details are less relevant for the use of the file and most often hidden for the user. Basic operations on files are *creation*, *opening*, *reading* from, writing to, closing, and deleting.

A *stream* is similar to files in that they are used to store data in and retrieve data from, but streams only allow for handling of data one element at a time, like the readout of a thermometer: we can make temperature readings as often as we like, making notes and thus saving a history of temperatures, but we cannot access the future. Hence, streams are in principle without an end, and thus have infinite size, and data from streams are programmed locally by considering the present and previous elements. In contrast, files are finite in size and allow for global operations on all the file's data. Files may be considered a stream, but the opposite is not true.

14.1 Command Line Arguments

Compiled programs may be started from the console with one or more arguments. E.g., if we have made a program called prog, then arguments may be passed as mono prog arg1 arg2 To read the arguments in the program, we must define a function with the *EntryPoint* attribute, and this function must be of type string array -> int.

<funcIdent> is the function's name, <arg> is the name of an array of strings, and <bodyExpr> is the function body. Return value 0 implies a successful execution of the program, while a non-zero value means failure. The entry point function can only be in the rightmost file in the list of files given to fsharpc. An example is given in Listing 14.2. An example execution with arguments is shown in Listing 14.3.

```
Listing 14.2 commandLineArgs.fsx:
Interacting with a user with ReadLine and WriteLine.

[<EntryPoint>]
let main args =
printfn "Arguments passed to function: %A" args
// Signals that program terminated successfully
```

In Bash, the return value is called the *exit status* and can be tested using Bash's if statements, as demonstrated in Listing 14.4. Also in Bash, the exit status of the last

Listing 14.3: An example dialogue of running Listing 14.2. 1 \$ fsharpc --nologo commandLineArgs.fsx 2 \$ mono commandLineArgs.exe Hello World 3 Arguments passed to function : [|"Hello"; "World"|] Listing 14.4: Testing return values in Bash when running Listing 14.2.

```
Listing 14.4: Testing return values in Bash when running Listing 14.2.

1  $ fsharpc --nologo commandLineArgs.fsx
2  $ if mono commandLineArgs.exe Hello World; then echo
    "success"; else echo "failure"; fi
3  Arguments passed to function : [|"Hello"; "World"|]
4  success
```

executed program can be accessed using the \$? built-in environment variable. In Windows, this same variable is called %errorlevel%.

14.2 Interacting With the Console

From a programming perspective, the console is a stream: A program may send new data to the console, but cannot return to previously sent data and make changes. Likewise, the program may retrieve input from the user, but cannot go back and ask the user to have input something else, nor can we peek into the future and retrieve what the user will input in the future. The console uses three built-in streams in System.Console, listed in Table 14.1. On the console, the standard output

| Stream | Description | |
|--------|--|--|
| stdout | Standard output stream used to display regular output. It typically streams data to the | |
| | console. | |
| stderr | Standard error stream used to display warnings and errors, typically streams to the same | |
| | place as stdout. | |
| stdin | Standard input stream used to read input, typically from the keyboard input. | |

Table 14.1 Three built-in streams in System.Console.

and error streams are displayed as text, and it is typically not possible to see a distinction between them. However, command-line interpreters such as Bash can, and it is possible from the command-line to filter output from programs according to these streams. However, a further discussion on this is outside the scope of this text. In System. Console there are many functions supporting interaction with the console, and the most important ones are shown in Table 14.2. Note that you must supply the empty argument "()" to the Read functions in order to run most of the functions instead of referring to them as values. A demonstration of the use of Write, WriteLine, and ReadLine is given in Listing 14.5. The functions Write and WriteLine act as printfn without a formatting string. These functions have

| Function | Description |
|--|--|
| Write: string -> unit | Write to the console. E.g., |
| | System.Console.Write "Hello world". |
| | Similar to printf. |
| WriteLine: string -> unit | As Write, but followed by a newline |
| | character, e.g., WriteLine "Hello world". |
| | Similar to printfn. |
| Read: unit -> int | Wait until the next key is pressed, and read its |
| | value. The key pressed is echoed to the |
| | screen. |
| ReadKey: bool -> System.ConsoleKeyInfo | As Read, but returns more information about |
| | the key pressed. When given the value true |
| | as argument, then the key pressed is not |
| | echoed to the screen. E.g., ReadKey true. |
| ReadLine unit -> string | Read the next sequence of characters until |
| | newline from the keyboard, e.g., |
| | ReadLine (). |

Table 14.2 Some functions for interacting with the user through the console in the System.Console class. Prefix "System.Console." is omitted for brevity.

```
Listing 14.5 userDialogue.fsx:
Interacting with a user with ReadLine and WriteLine. The user typed "3.5" and "7.4".

System.Console.WriteLine "To perform the multiplication of a and b"

System.Console.Write "Enter a: "
let a = float (System.Console.ReadLine ())

System.Console.Write "Enter b: "
let b = float (System.Console.ReadLine ())

System.Console.WriteLine ("a * b = " + string (a * b))

**System.Console.WriteLine ("a * b = " + string (a * b))

**System.Console.WriteLine ("a * b = " + string (a * b))

**System.Console.WriteLine ("a * b = " + string (a * b))
```

many overloaded definitions, the description of which is outside the scope of this book. For writing to the console, printf is to be preferred.

Often ReadKey is preferred over Read, since the former returns a value of type System.ConsoleKeyInfo which is a structure with three properties:

Key: A System.ConsoleKey enumeration of the key pressed. E.g., the character 'a' is ConsoleKey.A.

KeyChar: A unicode representation of the key.

Modifiers: A System.ConsoleModifiers enumeration of modifier keys shift, crtl, and alt.

An example of a dialogue is shown in Listing 14.6.

```
Listing 14.6 readKey.fsx:
Reading keys and modifiers. The user pressed 'a', 'shift-a', and 'crtl-a', and
the program was terminated by pressing 'crtl-c'. The 'alt-a' combination
does not work on MacOS.
open System
printfn "Start typing"
 while true do
  let key = Console.ReadKey true
  let shift =
    if key.Modifiers = ConsoleModifiers.Shift then "SHIFT+"
    else "'
   let alt =
    if key.Modifiers = ConsoleModifiers.Alt then "ALT+" else
   let ctrl =
     if key.Modifiers = ConsoleModifiers.Control then "CTRL+"
    else ""
   printfn "You pressed: %s%s%s%s" shift alt ctrl
    (key.Key.ToString ())
$ fsharpc --nologo readKey.fsx && mono readKey.exe
Start typing
You pressed: A
You pressed: SHIFT+A
 You pressed: CTRL+A
```

14.3 Storing and Retrieving Data From a File

A file stored on the filesystem has a name, and it must be opened before it can be accessed and closed when finished. Opening files informs the operating system that your program is now going to use the file. While a file is open, the operating system will protect it depending on how the file is opened. E.g., if you are going to write to the file, then this typically implies that no one else may write to the file at the same time, since simultaneous writing to a file may leave the resulting file in an uncertain state. Sometimes the operating system will realize that a file that was opened by a program is no longer being used, e.g., since the program is no longer running, but it is good practice always to release reserved files, e.g., by closing them as

soon as possible, such that other programs may have access to it. On the other hand, it is typically safe for several programs to read the same file at the same time, but it is still important to close files after their use, such that the operating system can effectively manage the computer's resources. Reserved files are just one of the possible obstacles that you may meet when attempting to open a file. Other points of failure may be that the file does not exist, your program may not have sufficient rights for accessing it, or the device where the file is stored may have unreliable access.

* Thus, never assume that accessing files always works, but program defensively, e.g., by checking the return status of the file accessing functions and by try constructions.

Data in files may have been stored in various ways, e.g., it may contain UTF8 encoded characters or sequences of floating point numbers stored as raw bits in chunks of 64 bits, or it may be a sequence of bytes that are later going to be interpreted as an image in jpeg or tiff format. To aid in retrieving the data, F# has a family of open functions, all residing in the System.IO.File class. These are described in Table 14.3.

| System.IO.File | Description |
|--|--|
| Open: | Request the opening of a file on path for reading |
| (path : string) * (mode : FileMod | and writing with access mode FileMode, see |
| -> FileStream | Table 14.4. Other programs are not allowed to |
| | access the file before this program closes it. |
| OpenRead: (path : string) | Request the opening of a file on path for reading. |
| -> FileStream | Other programs may read the file regardless of this |
| | opening. |
| OpenText: (path : string) | Request the opening of an existing UTF8 file on |
| -> StreamReader | path for reading. Other programs may read the file |
| | regardless of this opening. |
| OpenWrite: (path : string) | Request the opening of a file on path for writing |
| -> FileStream | with FileMode.OpenOrCreate. Other programs |
| | may not access the file before this program closes it. |
| Create: (path : string) | Request the creation of a file on path for reading |
| -> FileStream | and writing, overwriting any existing file. Other |
| | programs may not access the file before this program |
| | closes it. |
| <pre>CreateText: (path : string)</pre> | Request the creation of an UTF8 file on path for |
| -> StreamWriter | reading and writing, overwriting any existing file. |
| | Other programs may not access the file before this |
| | program closes it. |

Table 14.3 The family of System.IO.File.Open functions. See Table 14.4 for a description of FileMode, Tables 14.5 and 14.6 for a description of FileStream, Table 14.7 for a description of StreamReader, and Table 14.8 for a description of StreamWriter.

For the general Open function, you must also specify how the file is to be opened. This is done with a special set of values described in Table 14.4. An example of how a file is opened and later closed is shown in Listing 14.7. Notice how the example uses a defensive programming style, where the try-expression is used to return the

| FileMode | Description |
|--------------|---|
| Append | Open a file and seek to its end, if it exists, or create a new file. Can |
| | only be used together with FileAccess.Write. May throw IOException and |
| | NotSupportedException exceptions. |
| Create | Create a new file. If a file with the given filename exists, then that file is deleted. |
| | May throw the UnauthorizedAccessException exception. |
| CreateNew | Create a new file, but throw the IOException exception if the file already exists. |
| 0pen | Open an existing file. System.IO.FileNotFoundException exception is |
| | thrown if the file does not exist. |
| OpenOrCreate | Open a file, if it exists, or create a new file. |
| Truncate | Open an existing file and truncate its length to zero. Cannot be used together with |
| | FileAccess.Read. |

Table 14.4 File mode values for the System. IO. Open function.

optional datatype, and further processing is made dependent on the success of the opening operation.

In F#, the distinction between files and streams is not very clear. F# offers built-in support for accessing files as bytes through the System.IO.FileStream class, and for characters in a particular encoding through the System.IO.TextReader and System.IO.TextWriter.

A successfully opened System.IO.FileStream file by, e.g., System.IO.File.OpenRead from Table 14.3, will result in an FileStream object. From this object we can extract information about the file, such as the permitted operations and more listed in Table 14.5. This information is important in order to restrict the operation that we will perform on the file. Some typical operations are listed in and 14.6. E.g., we may Seek a particular position in the file, but only within the range of legal postions from 0 until the length of the file. Most operating systems do not necessarily write information to files immediately after one of the Write functions, but will often for

| Property | Description | |
|----------|---|--|
| CanRead | Gets a value indicating whether the current stream supports reading. (Overrides | |
| | Stream.CanRead.) | |
| CanSeek | Gets a value indicating whether the current stream supports seeking. (Overrides | |
| | Stream.CanSeek.) | |
| CanWrite | Gets a value indicating whether the current stream supports writing. (Overrides | |
| | Stream.CanWrite.) | |
| Length | Gets the length of a stream in bytes. (Overrides Stream.Length.) | |
| Name | Gets the name of the FileStream that was passed to the constructor. | |
| Position | Gets or sets the current position of this stream. (Overrides Stream.Position.) | |

Table 14.5 Some properties of the System.IO.FileStream class.

| Method | Description |
|--------------------------|---|
| Close () | Closes the stream. |
| Flush () | Causes any buffered data to be written to the file. |
| Read byte[] * int * int | Reads a block of bytes from the stream and writes the data in a |
| | given buffer. |
| ReadByte () | Read a byte from the file and advances the read position to the |
| | next byte. |
| Seek int * SeekOrigin | Sets the current position of this stream to the given value. |
| Write byte[] * int * int | Writes a block of bytes to the file stream. |
| WriteByte byte | Writes a byte to the current position in the file stream. |

Table 14.6 Some methods of the System.IO.FileStream class.

optimization purposes collect information in a buffer that is to be written to a device in batches. However, sometimes is is useful to be able to force the operating system to empty its buffer to the device. This is called *flushing* and can be forced using the Flush function.

```
Listing 14.8 readFile.fsx:
An example of opening a text file and using the StreamReader properties
and methods.
let printFile (reader : System.IO.StreamReader) =
   while not(reader.EndOfStream) do
    let line = reader.ReadLine ()
     printfn "%s" line
let filename = "readFile.fsx"
let reader = System.IO.File.OpenText filename
printFile reader
$ fsharpc --nologo readFile.fsx && mono readFile.exe
let printFile (reader : System.IO.StreamReader) =
   while not(reader.EndOfStream) do
     let line = reader.ReadLine ()
     printfn "%s" line
let filename = "readFile.fsx"
let reader = System.IO.File.OpenText filename
printFile reader
```

Text is typically streamed through the StreamReader and StreamWriter. These may be considered higher-order stream processing, since they include an added interpretation of the bits to strings. A StreamReader has methods similar to a FileStream object and a few new properties and methods, such as the EndOfStream property and ReadToEnd method, see Table 14.7. Likewise, a StreamWriter has

| Property/Method | Description |
|-------------------------|--|
| EndOfStream | Check whether the stream is at its end. |
| Close () | Closes the stream. |
| Flush () | Causes any buffered data to be written to the file. |
| Peek () | Reads the next character, but does not advance the position. |
| Read () | Reads the next character. |
| Read char[] * int * int | Reads a block of bytes from the stream and writes the data in a |
| | given buffer. |
| ReadLine () | Reads the next line of characters until a newline. Newline is dis- |
| | carded. |
| ReadToEnd () | Reads the remaining characters until end-of-file. |

Table 14.7 Some methods of the System.IO.StreamReader class.

an added method for automatically flushing after every writing operation. A simple

| Property/Method | Description |
|------------------|--|
| AutoFlush : bool | Gets or sets the auto-flush. If set, then every call to Write will flush the |
| | stream. |
| Close () | Closes the stream. |
| Flush () | Causes any buffered data to be written to the file. |
| Write 'a | Writes a basic type to the file. |
| WriteLine string | As Write, but followed by newline. |

Table 14.8 Some methods of the System. IO. StreamWriter class.

example of opening a text-file and processing it is given in Listing 14.8. Here the program reads the source code of itself, and prints it to the console.

14.4 Working With Files and Directories.

F# has support for managing files, summarized in the System.IO.File class and summarized in Table 14.9.

| Function | Description |
|------------------------------------|--|
| Copy (src : string, dest : string) | Copy a file from src to dest, possibly overwriting |
| | any existing file. |
| Delete string | Delete a file |
| Exists string | Checks whether the file exists |
| Move (from : string, to : string) | Move a file from src to to, possibly overwriting |
| | any existing file. |

Table 14.9 Some methods of the System. IO. File class.

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In the System.IO.Directory class there are a number of other frequently used functions, summarized in Table 14.10.

| Function | Description |
|---|---------------------------------------|
| CreateDirectory string | Create the directory and all implied |
| | sub-directories. |
| Delete string | Delete a directory. |
| Exists string | Check whether the directory exists. |
| GetCurrentDirectory () | Get working directory of the pro- |
| | gram. |
| GetDirectories (path : string) | Get directories in path. |
| GetFiles (path : string) | Get files in path. |
| Move (from : string, to : string) | Move a directory and its content from |
| | src to to. |
| <pre>SetCurrentDirectory : (path : string) -> unit</pre> | Set the current working directory of |
| | the program to path. |

Table 14.10 Some methods of the System.IO.Directory class.

In the System. IO. Path class there are a number of other frequently used functions summarized in Table 14.11.

| Function | Description |
|--|--|
| Combine string * string | Combine two paths into a new path. |
| GetDirectoryName (path: string) | Extract the directory name from path. |
| GetExtension (path: string) | Extract the extension from path. |
| GetFileName (path: string) | Extract the name and extension from |
| | path. |
| <pre>GetFileNameWithoutExtension (path : string)</pre> | Extract the name without the extension |
| | from path. |
| GetFullPath (path : string) | Extract the absolute path from path. |
| GetTempFileName () | Create a uniquely named and empty file |
| | on disk and return its full path. |

Table 14.11 Some methods of the System. IO. Path class.

14.5 Programming intermezzo: Name of Existing File Dialogue

A typical problem when working with files is

Problem 14.1

sk the user for the name of an existing file.

Such dialogues often require the program to aid the user, e.g., by telling the user which files are available, and by checking that the filename entered is an existing file.

We will limit our request to the present directory and use System.Console.ReadLine to get input from the user. Our strategy will be twofold. Firstly we will query the filesystem for the existing files using System.IO.Directory.GetFiles, and print these to the screen. Secondly, we will use System.IO.File.Exists to ensure that a file exists with the entered filename. We use the Exists function rather than examining the array obtained with GetFiles, since files may have been added or removed, since the GetFiles was called. A solution is shown in Listing 14.9. Note that it is programmed using a while-loop and with a flag fileExists used to exit the loop. The solution has a caveat: What should be done if the user decides not to enter a filename at all. Including a 'cancel'-option is a good style for any user interface, and should be offered when possible. In a text-based dialogue, this would require us to use an input, which cannot be a filename, to ensure that all possible filenames and 'cancel'-option is available to the user. This problem has not been addressed in the code.

Listing 14.9 filenamedialogue.fsx: Ask the user to input a name of an existing file. 1 let getAFileName () = 2 let mutable filename = "" 3 let mutable fileExists = false 4 while not(fileExists) do 5 System.Console.Write("Enter Filename: ") 6 filename <- System.Console.ReadLine() 7 fileExists <- System.IO.File.Exists filename 8 filename 9 let listOfFiles = System.IO.Directory.GetFiles "." 10 printfn "Directory contains: %A" listOfFiles 11 let filename = getAFileName () 12 printfn "You typed: %s" filename

14.6 Reading From the Internet

The internet is a global collection of computers that are connected in a network using the internet protocol suite TCP/IP. The internet is commonly used for transport of data such as emails and for offering services such as web pages on the World Wide Web. Web resources are identified by a *Uniform Resource Locator (URL)*, popularly known as a web page, and an URL contains information about where and how data from the web page is to be obtained. E.g.,

```
https://en.wikipedia.org/wiki/F_Sharp_(programming_language)
```

contains 3 pieces of information: The host uses the https protocol, en.wikipedia.org is its name, and wiki/F_Sharp_(programming_language) is the filename.

F#'s System namespace contains functions for accessing web pages as stream, as illustrated in Listing 14.10. To connect to a URL as a stream, we first need first format the URL string as a *Uniform Resource Identifiers* (*URI*), which is a generalization of the URL concept, using the System.Uri function. Then we must initialize the request by the System.Net.WebRequest function, and the response from the host is obtained by the GetResponse method. Finally, we can access the response as a stream by the GetResponseStream method. In the end, we convert the stream to a StreamReader, such that we can use the methods from Table 14.7 to access the web page.

Listing 14.10 webRequest.fsx: Downloading a web page and printing the first few characters. /// Set up a url as a stream let url2Stream url = let uri = System.Uri url let request = System.Net.WebRequest.Create uri let response = request.GetResponse () response.GetResponseStream () /// Read all contents of a web page as a string let readUrl url = let stream = url2Stream url let reader = new System.IO.StreamReader(stream) reader.ReadToEnd () let url = "http://fsharp.org" let a = 40let html = readUrl url printfn "Downloaded %A. First %d characters are: %A" url a html.[0..a] \$ fsharpc --nologo webRequest.fsx && mono webRequest.exe Downloaded "http://fsharp.org". First 40 characters are: "<!DOCTYPE html> <html lang="en"> <head>"

14.7 Resource Management

Streams and files are examples of computer resources that may be shared by several applications. Most operating systems allow for several applications to be running in parallel, and to avoid unnecessarily blocking and hogging of resources, all responsible applications must release resources as soon as they are done using them. F# has language constructions for automatic releasing of resources: the use binding and the using function. These automatically dispose of resources when the resource's name binding falls out of scope. Technically, this is done by calling the <code>Dispose</code> method on objects that implement the <code>System.IDisposable</code> interface. See Section 24.4 for more on interfaces.

The *use* keyword is similar to let:

```
Listing 14.11: Use binding expression.

| use <valueIdent> = <bodyExpr> [in <expr>]
```

A use binding provides a binding between the <bodyExpr> expression to the name <valueIdent> in the following expression(s), and in contrast to let, it also adds a call to Dispose() on <valueIdent> if it implements System.IDisposable. See for example Listing 14.12. Here, file is an System.IDisposable object,

Listing 14.12 useBinding.fsx: Using instead of releases disposable resources at end of scope. open System.IO let writeToFile (filename : string) (str : string) : unit = use file = File.CreateText filename file.Write str // file.Dispose() is implicitly called here, // implying that the file is closed. writeToFile "use.txt" "Using 'use' closes the file, when out of scope."

and file.Dispose() is called automatically before writeToFile returns. This implies that the file is closed. Had we used let instead, then the file would first be closed when the program terminates.

The higher-order function *using* takes a disposable object and a function, executes the function on the disposable objects, and then calls Dispose() on the disposable object. This is illustrated in Listing 14.13 The main difference between use and

Listing 14.13 using.fsx: The using function executes a function on an object and releases its disposable resources. Compare with Listing 14.12. open System.IO let writeToFile (str : string) (file : StreamWriter) : unit = file.Write str using (File.CreateText "use.txt") (writeToFile "Disposed after call.") // Dispose() is implicitly called on the anonymous file handle, implying // that the file is automatically closed.

using is that resources allocated using use are disposed at the end of its scope, while using disposes the resources after the execution of the function in its argument. In spite of the added control of using, we prefer use over using due to its simpler structure.

Chapter 15

Graphical User Interfaces

A graphical user interface (GUI) uses graphical elements such as windows, icons, and sound to communicate with the user, and a typical way to activate these elements is through a pointing device such as the mouse or by touch. Some of these elements may themselves be textual, and thus most operating systems offer access to a command-line interface (CLI) in a window alongside other interface types.

An example of a graphical user interface is a web-browser, shown in Figure 15.1. The program presents information to the user in terms of text and images, has active

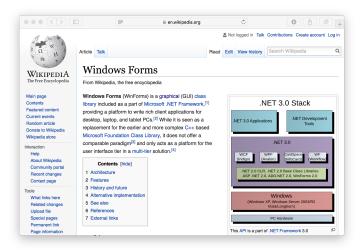


Fig. 15.1 A web-browser is a graphical user interface for accessing a web-server and interacting with its services. Here the browser is showing the page https://en.wikipedia.org/wiki/Windows_Forms at time of writing.

areas that may be activated by clicking, allows the user to go other web-pages by typing a URL or following hyperlinks, and can generate new pages through search queries.

F# includes a number of implementations of graphical user interfaces, and at time of writing, both *GTK*+ and *WinForms 2.0* are supported on both the Microsoft .Net and the Mono platform. WinForms can be used without extra libraries during compilation, and therefore will be the subject of the following chapter.

WinForms is a set of libraries that simplifies many common tasks for applications, and in this chapter, we will focus on the graphical user interface part of WinForms. A *form* is a visual interface used to communicate information with the user, typically a window. Communication is done through *controls*, which are elements that display information or accept input. Examples of controls are a box with text, a button, and a menu. When the user gives input to a control element, this generates an *event* which you can write code to react to. WinForms is designed for *event-driven programming*, meaning that at runtime, most time is spent on waiting for the user to give input. See Chapter 16 for more on event-driven programming.

Designing easy-to-use graphical user interfaces is a challenging task. This chapter will focus on examples of basic graphical elements and how to program these in WinForms.

15.1 Opening a Window

The namespaces *System.Windows.Forms* and *System.Drawing* are central for programming graphical user interfaces with WinForms. System.Windows.Forms includes code for generating forms, controls, and handling events. System.Drawing is used for low-level drawing, and it gives access to the *Windows Graphics Device Interface* (*GDI*+), which allows you to create and manipulate graphics objects targeting several platforms, such as screens and paper. All controls in System.Windows.Forms in Mono are drawn using System.Drawing.

To display a graphical user interface on the screen, the first thing to do is open a window, which acts as a reserved screen-space for our output. In WinForms, windows are called forms. Code for opening a window is shown in Listing 15.1, and the result is shown in Figure 15.2. Note that the present version of WinForms on MacOs only works with the 32-bit implementation of mono, mono32, as demonstrated in the example. The new System.Windows.Forms.Form () creates an object (See Chapter 23), but does not display the window on the screen. We use the optional new keyword, since the form is an IDisposable object and may be implicitly disposed of. I.e., it is recommended to instantiate IDisposable objects using new to contrast them with other object types. Executing System.Windows.Forms.Application.Run is applied to the object, then the control is handed over to the WinForms' event-loop, which continues until the window is closed by, e.g., pressing the icon designated by the operating system. On

Listing 15.1 winforms/openWindow.fsx: Create the window and turn over control to the operating system. See Figure 15.2. // Create a window let win = new System.Windows.Forms.Form () // Start the event-loop. System.Windows.Forms.Application.Run win system.Windows.Forms.Application.Run win



Fig. 15.2 A window opened by Listing 15.1.

the Mac OSX, that is the red button in the top left corner of the window frame, and on Window it is the cross on the top right corner of the window frame.

The window form has a long list of methods and properties. E.g., the background color may be set by BackColor, the title of the window may be set by Text, and you may get and set the size of the window with Size. This is demonstrated in Listing 15.2. These properties are *accessors*, implying that they act as mutable



Fig. 15.3 A window with user-specified size and background color, see Listing 15.2.

Listing 15.2 winforms/windowProperty.fsx: Create the window and change its properties. See Figure 15.3 1 // Prepare window form 2 let win = new System.Windows.Forms.Form () 3 4 // Set some properties 5 win.BackColor <- System.Drawing.Color.White 6 win.Size <- System.Drawing.Size (600, 200) 7 win.Text <- sprintf "Color '%A' and Size '%A'" win.BackColor win.Size 8 9 // Start the event-loop. 10 System.Windows.Forms.Application.Run win

variables.

15.2 Drawing Geometric Primitives

The *System.Drawing.Color* is a structure for specifying colors as 4 channels: alpha, red, green, and blue. Some methods and properties for the Color structure is shown in Table 15.1. Each channel is an 8-bit unsigned integer. The alpha channel specifies the transparency of a color, where values 0–255 denote the range of fully transparent to fully opaque, and the remaining channels denote the amount of red, green, and blue, where 0 is none and 255 is full intensity. As a shorthand, colors are often referred to as a single 32-bit unsigned integer, whose bits are organized in groups of 8 bits as 0xAARRGGBB, where AA is the alpha channel's values 0x00–0xFF etc. Any color may be created using the FromArgb method, e.g., an opaque red is given by System.Drawing.Color.FromArgb (255, 255, 0, 0). There are also many build-in colors, e.g., the same red color is also a known color and may be obtained as System.Drawing.Color.Red. For a given color, the 4 alpha, red, green, and blue channels' values may be obtained as the A, R, G, and B members, see Listing 15.3

The namespace System.Drawing contains many useful functions and values. Listing 15.2 used System.Drawing.Size to specify a size by a pair of integers. Other important values and functions are Point, which specifies a coordinate as a pair of points; Pen, which specifies how to draw lines and curves; Font, which specifies the font of a string; SolidBrush and TextureBrush, used for filling geometric primitives, and Bitmap, which is a type of Image. These are summarized in Table 15.2.

The *System.Drawing.Graphics* is a class for drawing geometric primitives to a display device, and some of its methods are summarized in Table 15.3.

| Method/Property | Description | |
|--|--|--|
| Properties of an existing color structure | | |
| A : byte | The value of the alpha channel. | |
| R : byte | The value of the red channel. | |
| G : byte | The value of the green channel. | |
| B : byte | The value of the blue channel. | |
| ToArgb : unit -> int | The 32-bit integer value of the color. | |
| Static properties returning a color structure by its name | | |
| Black : Color | The ARGB value 0xFF000000. | |
| Blue : Color | The ARGB value 0xFF0000FF. | |
| Brown : Color | The ARGB value 0xFFA52A2A. | |
| Gray : Color | The ARGB value 0xFF808080. | |
| Green : Color | The ARGB value 0xFF00FF00. | |
| Orange : Color | The ARGB value 0xFFFFA500. | |
| Purple : Color | The ARGB value 0xFF800080. | |
| Red : Color | The ARGB value 0xFFFF0000. | |
| White : Color | The ARGB value 0xFFFFFFF. | |
| Yellow : Color | The ARGB value 0xFFFFFF00. | |
| Static methods for converting between color structures and integers representations. | | |
| FromArgb : | Create a color structure from red, green, | |
| r:int * g:int * b:int -> Color | and blue values. | |
| FromArgb : | Create a color structure from alpha, red, | |
| a:int * r:int * g:int * b:int -> Color | green, and blue values. | |
| <pre>FromArgb : argb:int -> Color</pre> | Create a color structure from a single in- | |
| | teger. | |

 $\textbf{Table 15.1} \ \ \textbf{Some methods and properties of the System.Drawing.Color structure}.$

| Constructor | Description |
|------------------------|--|
| Bitmap(int, int) | Create a new empty Image of specified size. |
| Bitmap(Stream) | Create a Image from a System. IO. Stream or |
| Bitmap(string) | from a file specified by a filename. |
| Font(string, single) | Create a new font from the font's name and em- |
| | size. |
| Pen(Brush) | Create a pen to paint either with a brush or solid |
| Pen(Brush), single) | color and possibly with specified width. |
| Pen(Color) | |
| Pen(Color, single) | |
| Point(int, int) | Create an ordered pair of integers or singles |
| Point(Size) | specifying x- and y-coordinates in the plane. |
| PointF(single, single) | |
| Size(int, int) | Create an ordered pair of integers or singles |
| Size(Point) | specifying height and width in the plane. |
| SizeF(single, single) | |
| SizeF(PointF) | |
| SolidBrush(Color) | Create a Brush as a solid color or from an image |
| TextureBrush(Image) | to fill the interior of geometric shapes. |

 Table 15.2 Basic geometrical structures in WinForms. Brush and Image are abstract classes.

```
Listing 15.3 drawingColors.fsx:
Defining colors and accessing their values.
// open namespace for brevity
open System.Drawing
// Define a color from ARGB
let c = Color.FromArgb (0xFF, 0x7F, 0xFF, 0xD4) //Aquamarine
printfn "The color %A is (%x, %x, %x, %x)" c c.A c.R c.G c.B
// Define a list of named colors
let colors =
   [Color.Red; Color.Green; Color.Blue;
   Color.Black; Color.Gray; Color.White]
for col in colors do
  printfn "The color %A is (%x, %x, %x, %x)" col col.A col.R
    col.G col.B
$ fsharpc --nologo drawingColors.fsx && mono drawingColors.exe
The color Color [A=255, R=127, G=255, B=212] is (ff, 7f, ff,
The color Color [Red] is (ff, ff, 0, 0)
The color Color [Green] is (ff, 0, 80, 0)
The color Color [Blue] is (ff, 0, 0, ff)
The color Color [Black] is (ff, 0, 0, 0)
The color Color [Gray] is (ff, 80, 80, 80)
The color Color [White] is (ff, ff, ff, ff)
```

| Constructor | Description |
|---|---|
| DrawImage : Image * (Point []) -> unit | Draw an image at a specific point and size. |
| <pre>DrawImage : Image * (PointF []) -> unit</pre> | |
| DrawImage : Image * Point -> unit | Draw an image at a specific point. |
| DrawImage : Image * PointF -> unit | |
| DrawLines : Pen * (Point []) -> unit | Draw a series of lines between the <i>n</i> 'th and |
| DrawLines : Pen * (PointF []) -> unit | n+1'th points. |
| DrawString : | Draw a string at the specified point. |
| string * Font * Brush * PointF -> uni | |

Table 15.3 Basic geometrical structures in WinForms.

The location and shape of geometrical primitives are specified in a coordinate system, and WinForms operates with 2 coordinate systems: *screen coordinates* and *client coordinates*. Both coordinate systems have their origin in the top-left corner, with the first coordinate, x, increasing to the right, and the second, y, increasing down, as illustrated in Figure 15.4. The Screen coordinate system has its origin in the top-left corner of the screen, while the client coordinate system has its origin in the top-left corner of the drawable area of a form or a control, i.e., for a window, this will be the area without the window borders, scroll, and title bars. A control is a graphical object, such as a clickable button, will be discussed later. Conversion between client and screen coordinates is done with System.Drawing.PointToClient and System.Drawing.PointToClient and System.Drawing.PointToClient.

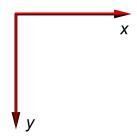


Fig. 15.4 Coordinate systems in Winforms have the y axis pointing down.

Displaying graphics in WinForms is performed as the reaction to an event. E.g., windows are created by the program, moved, minimized, occluded by other windows, resized, etc., by the user or the program, and each action may require that the content of the window is refreshed. Thus, we must create a function that WinForms can call any time. This is known as a *call-back function*, and it is added to an existing form using the form's *Paint.Add* method. Due to the event-driven nature of WinForms, functions for drawing graphics primitives are only available when responding to an event, e.g., *System.Drawing.Graphics.DrawLines* draws a line in a window, and *it is only possible to call this function as part of an event handling*.

As an example, consider the problem of drawing a triangle in a window. For this we need to make a function that can draw a triangle not once, but at any amount of times as deemed necessary by the operating system. An example of such a program is shown in Listing 15.4. A walk-through of the code is as follows: First, we open the

```
Listing 15.4 winforms/triangle.fsx:
Adding line graphics to a window. See Figure 15.5
// Open often used libraries, beware of namespace polution!
open System.Windows.Forms
open System.Drawing
// Prepare window form
let win = new Form ()
win.Size <- Size (320, 170)
// Set paint call-back function
let paint (e : PaintEventArgs) : unit =
  let pen = new Pen (Color.Black)
  let points =
     [|Point (0,0); Point (10,170); Point (320,20); Point
  e.Graphics.DrawLines (pen, points)
win.Paint.Add paint
// Start the event-loop.
Application.Run win
```

two libraries that we will use heavily. This will save us some typing, but also pollute

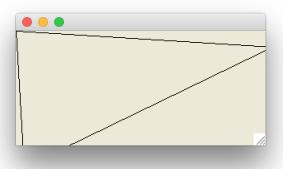


Fig. 15.5 Drawing a triangle using Listing 15.4.

our namespace. E.g., now Point and Color are existing types, and we cannot define our own identifiers with these names. Then we create the form with size 320×170 , we add a paint call-back function, and we start the event-loop. The event-loop will call the paint function, whenever the system determines that the window's content needs to be refreshed. This function is to be called as a response to a paint event and takes a System.Windows.Forms.PaintEventArgs object, which includes the System.Drawing.Graphics object. The function paint chooses a pen and a set of points and draws a set of lines connecting the points.

The code in Listing 15.4 is not optimal. Despite the fact that the triangle spans the rectangle (0,0) to (320,170) and the window's size is set to (320,170), our window is too small and the triangle is clipped at the window border. The error is that we set the window's Size property, which determines the size of the window including top bar and borders. Alternatively, we may set the ClientSize, which determines the size of the drawable area, and this is demonstrated in Listing 15.5 and Figure 15.6.

★ Thus, prefer the ClientSize over the Size property for internal consistency.

Considering the program in Listing 15.4, we may identify a part that concerns the specification of the triangle, or more generally the graphical model, and some which concern system specific details. For future maintenance, it is often a good idea to

separate the model from how it is viewed on a specific system. E.g., it may be that at some point you decide that you would rather use a different library than WinForms. In this case, the general graphical model will be the same, but the specific details on initialization and event handling will be different. We think of the model and the viewing part of the code as top and bottom layers, respectively, and these are often connected with a connection layer. This *Model-View paradigm* is shown in Figure 15.7. While it is not easy to completely separate the general from the specific, it is often a good idea to strive for some degree of separation.

Listing 15.5 winforms/triangleClientSize.fsx: Adding line graphics to a window. See Figure 15.6. // Open often used libraries, beware of namespace polution! open System.Windows.Forms open System.Drawing // Prepare window form let win = new Form () win.ClientSize <- Size (320, 170)</pre> // Set paint call-back function let paint (e : PaintEventArgs) : unit = let pen = new Pen (Color.Black) let points = [|Point (0,0); Point (10,170); Point (320,20); Point e.Graphics.DrawLines (pen, points) win.Paint.Add paint // Start the event-loop. Application.Run win

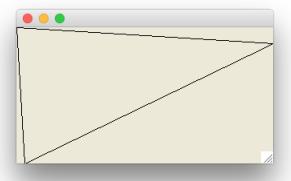


Fig. 15.6 Setting the ClientSize property gives a predictable drawing area, see Listing 15.5 for code.

In Listing 15.6, the program has been redesigned to follow the Model-View paradigm, where view contains most of the WinForms-specific code, and model contains most of the geometry, which could be reused with other graphical user interfaces. The model still uses the geometric primitives from WinForms for brevity, since a general implementation of geometric primitives avoiding WinForms would have a very similar interface. This program is longer, but there is a much better separation of what is to be displayed (model) from how it is to be done (view).

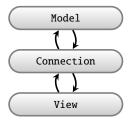


Fig. 15.7 Separating model from view gives flexibility later.

```
Listing 15.6 winforms/triangleOrganized.fsx:
Improved organization of code for drawing a triangle. See Figure 15.8.
// Open often used libraries, beware of namespace polution!
open System.Windows.Forms
open System.Drawing
/////// WinForm specifics /////////
/// Setup a window form and return function which can
   activate it
let view (sz : Size) (pen : Pen) (pts : Point []) : (unit ->
   unit) =
  let win = new System.Windows.Forms.Form ()
  win.ClientSize <- sz
  win.Paint.Add (fun e -> e.Graphics.DrawLines (pen, pts))
  fun () -> Application.Run win // function as return value
/////// Model /////////
// A black triangle, using winform primitives for brevity
let model () : Size * Pen * (Point []) =
  let size = Size (320, 170)
  let pen = new Pen (Color.FromArgb (0, 0, 0))
  let lines =
     [|Point (0,0); Point (10,170); Point (320,20); Point
    (0,0)
  (size, pen, lines)
//////// Connection //////////
// Tie view and model together and enter main event loop
let (size, pen, lines) = model ()
let run = view size pen lines
```

To further our development of a general program for displaying graphics, consider the case where we are to draw another two triangles, that are a translation and rotations of the original, and where we would like to specify the color of each triangle individually. A simple extension of model in Listing 15.6 for generating many shapes of different colors is model: unit -> Size * ((Point []) * Pen) list, i.e., semantically augment each point array with a pen and return a list of such pairs. For this example, we also program translation and rotation transformations. See Listing 15.7 for the result. We update view accordingly to iterate through this

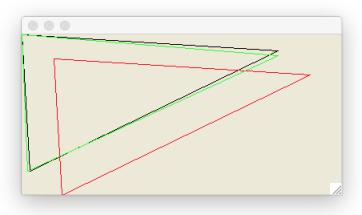


Fig. 15.8 Better organization of the code for drawing a triangle, see Listing 15.6.

list as shown in Listing 15.8. Since we are using WinForms primitives in the model, the connection layer is trivial, as shown in Listing 15.9.

Listing 15.7 winforms/transformWindows.fsx: Model of a triangle and simple transformations of it. See also Listing 15.8 and 15.9.

```
//////// Model /////////
// A black triangle, using WinForm primitives for brevity
let model () : Size * ((Pen * (Point [])) list) =
  /// Translate a primitive
  let translate (d : Point) (arr : Point []) : Point [] =
    let add (d : Point) (p : Point) : Point =
      Point (d.X + p.X, d.Y + p.Y)
    Array.map (add d) arr
  /// Rotate a primitive
  let rotate (theta : float) (arr : Point []) : Point [] =
    let toInt = int << round</pre>
    let rot (t : float) (p : Point) : Point =
      let (x, y) = (float p.X, float p.Y)
      let (a, b) = (x * cos t - y * sin t, x * sin t + y *
   cos t)
      Point (toInt a, toInt b)
    Array.map (rot theta) arr
  let size = Size (400, 200)
  let lines =
    [|Point (0,0); Point (10,170); Point (320,20); Point
   (0,0)
  let black = new Pen (Color.FromArgb (0, 0, 0))
  let red = new Pen (Color.FromArgb (255, 0, 0))
  let green = new Pen (Color.FromArgb (0, 255, 0))
  let shapes =
    [(black, lines);
     (red, translate (Point (40, 30)) lines);
     (green, rotate (1.0 *System.Math.PI / 180.0) lines)]
  (size, shapes)
```

Listing 15.8 winforms/transformWindows.fsx:

A view for lists of pairs of pen and point arrays. See also Listing 15.7 and 15.9.

Listing 15.9 winforms/transformWindows.fsx:

Model of a triangle and simple transformations of it. See also Listing 15.7 and 15.8.

```
and 15.0.

45 //////// Connection ////////

46 // Tie view and model together and enter main event loop

1et (size, shapes) = model ()

1et run = view size shapes

run ()
```

15.3 Programming Intermezzo: Hilbert Curve

A curve in 2 dimensions has a length but no width, and we can only visualize it by giving it a width. Thus, it came as a surprise to many when Giuseppe Peano in 1890 demonstrated that there exist curves which fill every point in a square. The method he used to achieve this was recursion:

Problem 15.1

onsider a curve consisting of piecewise straight lines all with the same length but with varying angles 0° , 90° , 180° , or 270° w.r.t. the horizontal axis. To draw this curve, we need 3 basic operations: Move forward (F), turn right (R), and turn left (L). The turning is w.r.t. the present direction. A Hilbert Curve is a space-filling curve which can be expressed recursively as:

$$A \to LBFRAFARFBL,$$
 (15.1)

$$B \to RAFLBFBLFAR$$
, (15.2)

starting with A. For practical illustrations, we typically only draw space-filling curves to a specified depth of recursion, which is called the order of the curve. To keep track of the level of recursion, we introduce an index as:

$$A_{n+1} \rightarrow LB_nFRA_nFA_nRFB_nL,$$

 $B_{n+1} \rightarrow RA_nFLB_nFB_nLFA_nR,$

for n > 0 and $A_0 \to \emptyset$ and $B_0 \to \emptyset$. Thus, the first-order curve is

$$A_1 \rightarrow LB_0FRA_0FA_0RFB_0L \rightarrow LFRFRFL$$

and the second order curve is

$$A_2 \rightarrow LB_1FRA_1FA_1RFB_1L$$

 $\rightarrow LRFLFRFRLFRFRLFRFRFLFLFRFRFLFRFLFLFRL.$

Since $LR = RL = \emptyset$ the above simplifies to

$$A_2 \rightarrow FLFLFRFFRFRFRFLFLF$$

Make a program that given an order produces an image of the Hilbert curve.

Our strategy to solve this problem will be first to define the curves in terms of movement commands LRFL... For this, we will define a discriminated union type Command = F | L | R. The movement commands can then be defined as a Command list type. The list for a specific order is a simple set of recursive functions in F# which we will call A and B.

To produce a graphical drawing of a command list, we must transform it into coordinates, and during the conversion, we need to keep track of both the present position and the present heading, since not all commands draw. This is a concept similar to Turtle Graphics, which is often associated with the Logo programming language from the 1960's. In Turtle graphics, we command a little robot - a turtle - which moves in 2 dimensions and can turn on the spot or move forward, and its track is the line being drawn. Thus we introduce a type Turtle = {x : float; y : float; d : float} record. Conversion of command lists to turtle lists is a fold programming structure, where the command list is read from left-to-right, building up an accumulator by adding each new element. For efficiency, we choose to prepend the new element to the accumulator. This we have implemented as the addRev function. Once the full list of turtles has been produced, then it is reversed.

Finally, the turtle list is converted to WinForms Point array, and a window of appropriate size is chosen. The resulting model part is shown in Listing 15.10. The view and connection parts are identical to Listing 15.8 and 15.9, and Figure 15.9 shows the result of using the program to draw Hilbert curves of orders 1, 2, 3, and 5

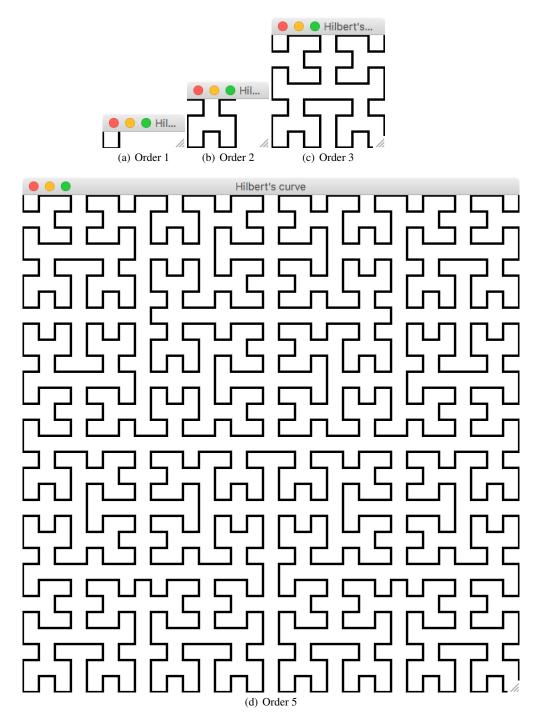


Fig. 15.9 Hilbert curves of orders 1, 2, 3, and 5 by code in Listing 15.10.

Listing 15.10 winforms/hilbert.fsx:

Using simple turtle graphics to produce a list of points on a polygon. The code continues in Listing 15.11. The view and connection parts are identical to Listing 15.8 and 15.9.

```
\ensuremath{//} Turtle commands, type definitions must be in outermost
   scope
type Command = F | L | R
type Turtle = {x : float; y : float; d : float}
// A black Hilbert curve using WinForm primitives for brevity
let model () : Size * ((Pen * (Point [])) list) =
  /// Hilbert recursion production rules
  let rec A n : Command list =
    if n > 0 then
      [L]@B (n-1)@[F; R]@A (n-1)@[F]@A (n-1)@[R; F]@B
   (n-1)@[L]
    else
      []
  and B n : Command list =
    if n > 0 then
      [R]@A (n-1)@[F; L]@B (n-1)@[F]@B (n-1)@[L; F]@A
   (n-1)@[R]
    else
      []
  /// Convert a command to turtle record and prepend to list
  let addRev (lst : Turtle list) (cmd : Command) (len :
   float) : Turtle list =
    let toInt = int << round</pre>
    match 1st with
      | t::rest ->
        match cmd with
          | L -> \{t \text{ with } d = t.d + 3.141592/2.0\}::rest // left
          | R -> \{t \text{ with } d = t.d - 3.141592/2.0\}::rest //
   right
          \mid F -> {t with x = t.x + len * cos t.d; // forward
                          y = t.y + len * sin t.d}::lst
      | _ -> failwith "Turtle list must be non-empty."
  let maxPoint (p1 : Point) (p2 : Point) : Point =
    Point (max p1.X p2.X, max p1.Y p2.Y)
```

Listing 15.11 winforms/hilbert.fsx: Continued from Listing 15.10.

```
// Calculate commands for a specific order
let curve = A 5
// Convert commands to point array
let initTrtl = \{x = 0.0; y = 0.0; d = 0.0\}
let len = 20.0
let line =
 List.fold (fun acc elm -> addRev acc elm len) [initTrtl]
 curve // Convert command list to reverse turtle list
 |> List.rev // Reverse list
 |> List.map (fun t -> Point (int (round t.x), int (round
 t.y))) // Convert turtle list to point list
 |> List.toArray // Convert point list to point array
let black = new Pen (Color.FromArgb (0, 0, 0))
// Set size to as large as shape
let minVal = System.Int32.MinValue
let maxPoint = Array.fold maxPoint (Point (minVal, minVal))
let size = Size (maxPoint.X + 1, maxPoint.Y + 1)
(size, [(black, line)]) // return shapes as singleton list
```

15.4 Handling Events

In the previous section, we have looked at how to draw graphics using the Paint method of an existing form object. Forms have many other event handlers that we may use to interact with the user. Listing 15.12 demonstrates event handlers for moving and resizing a window, for clicking in a window, and for typing on the keyboard. Listing 15.12 shows the output from an interaction with the program which is the

```
Listing 15.12 winforms/windowEvents.fsx:
Catching window, mouse, and keyboard events.
open System.Windows.Forms
open System.Drawing
open System
let win = new Form () // create a form
// Window event
let windowMove (e : EventArgs) =
  printfn "Move: %A" win.Location
win.Move.Add windowMove
let windowResize (e : EventArgs) =
  printfn "Resize: %A" win.DisplayRectangle
win.Resize.Add windowResize
// Mouse event
let mutable record = false; // records when button down
let mouseMove (e : MouseEventArgs) =
  if record then printfn "MouseMove: %A" e.Location
win.MouseMove.Add mouseMove
let mouseDown (e : MouseEventArgs) =
  printfn "MouseDown: %A" e.Location; (record <- true)</pre>
win.MouseDown.Add mouseDown
let mouseUp (e : MouseEventArgs) =
  printfn "MouseUp: %A" e.Location; (record <- false)</pre>
win.MouseUp.Add mouseUp
let mouseClick (e : MouseEventArgs) =
  printfn "MouseClick: %A" e.Location
win.MouseClick.Add mouseClick
// Keyboard event
win.KeyPreview <- true
let keyPress (e : KeyPressEventArgs) =
  printfn "KeyPress: %A" (e.KeyChar.ToString ())
win.KeyPress.Add keyPress
Application.Run win // Start the event-loop.
```

Listing 15.13: Output from an interaction with the program in Listing 15.12. Move: $\{X=22, Y=22\}$ Move: $\{X=22, Y=22\}$ Move: $\{X=50, Y=71\}$ Resize: {X=0, Y=0, Width=307, Height=290} MouseDown: $\{X=144, Y=118\}$ MouseClick: {X=144,Y=118} MouseUp: {X=144,Y=118} MouseDown: $\{X=144, Y=118\}$ MouseUp: $\{X=144, Y=118\}$ MouseDown: $\{X=96, Y=66\}$ MouseMove: $\{X=96, Y=67\}$ MouseMove: {X=97,Y=69} MouseMove: {X=99,Y=71} MouseMove: $\{X=103, Y=74\}$ MouseMove: {X=107,Y=77} MouseMove: $\{X=109, Y=79\}$ MouseMove: {X=112,Y=81} $\texttt{MouseMove: } \{\texttt{X=}114\,,\texttt{Y=}82\}$ MouseMove: {X=116,Y=84} MouseMove: $\{X=117, Y=85\}$ MouseMove: {X=118,Y=85} MouseClick: {X=118,Y=85} MouseUp: {X=118,Y=85} KeyPress: "a" KeyPress: "b" KeyPress: "c"

result of the following actions: moving the window, resizing the window, clicking the left mouse key, pressing and holding the down the left mouse key while moving the mouse, releasing the left mouse key, and typing "abc". As demonstrated, some actions, like moving the mouse, result in a lot of events, and some, like the initial window moves results, are surprising. Thus, event-driven programming should take care to interpret the events robustly and carefully.

Common for all event-handlers is that they listen for an event, and when the event occurs, the functions that have been added using the Add method are called. This is also known as sending a message. Thus, a single event can give rise to calling zero or more functions.

Graphical user interfaces and other systems often need to perform actions that depend on specific lengths of time or a certain point in time. To measure length of time F# has the <code>System.Windows.Forms.Timer</code> class, which technically is an optimized of <code>System.Timers.Timer</code> for graphical user interfaces. The Timer class can be used to create an event after a specified duration of time. F# also has the <code>System.DateTime</code> class to specify points in time. An often used property is <code>System.DateTime.Now</code>, which returns a <code>DateTime</code> object for the date and time when the property is accessed. The use of these two classes is demonstrated in Listing <code>15.14</code> and Figure <code>15.10</code>. In the code, a label has been created to show the present date and time. The label is a

Listing 15.14 winforms/clock.fsx: Using System.Windows.Forms.Timer and System.DateTime.Now to update the display of the present date and time. See Figure 15.10 for the result. open System.Windows.Forms open System.Drawing open System let win = new Form () // make a window form win.ClientSize <- Size (200, 50) // make a label to show time let label = new Label() win.Controls.Add label label.Width <- 200 label.Text <- string System.DateTime.Now // get present time and date // make a timer and link to label

timer.Interval <- 1000 // create an event every 1000

timer.Enabled <- true // activate the timer
timer.Tick.Add (fun e -> label.Text <- string</pre>

Application.Run win // start event-loop

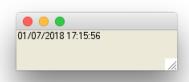


Fig. 15.10 See Listing 15.14.

let timer = new Timer()

System.DateTime.Now)

millisecond

type of control, and it is displayed using the default font which is rather small. How to change this and other details on controls will be discussed in the next section.

In the example, the label is redrawn everytime the text is changed, such that the current value is correctly displayed on the screen. Sometimes it is necessary to force a control to redraw which can be done with the Refresh() method. Since a Form is also a type of control, it is common to trigger a redraw event for the top form, which in Listing 15.14 would be win.Refresh(). Thus, Refresh() and a Timer object can be used to produce animations.

15.5 Labels, Buttons, and Pop-up Windows

In WinForms, buttons, menus and other interactive elements are called *Controls*. A form is a type of control, and thus, programming controls are very similar to programming windows. Listing 15.15 shows a small program that displays a label and a button in a window, and when the button is pressed, then the label is updated. As the list-

```
Listing 15.15 winforms/buttonControl.fsx:
Create the button and an event, see also Figure 15.11.
open System.Windows.Forms
open System.Drawing
open System
let win = new Form () // make a window form
win.ClientSize <- Size (140, 120)
// Create a label
let label = new Label()
win.Controls.Add label
label.Location <- new Point (20, 20)
label.Width <- 120
let mutable clicked = 0
let setLabel clicked =
  label.Text <- sprintf "Clicked %d times" clicked
setLabel clicked
// Create a button
let button = new Button ()
win.Controls.Add button
button.Size <- new Size (100, 40)
button.Location <- new Point (20, 60)
button.Text <- "Click me"</pre>
button.Click.Add (fun e -> clicked <- clicked + 1; setLabel
    clicked)
Application.Run win // Start the event-loop.
```

ing demonstrates, the button is created using the *System.Windows.Forms.Button* constructor, and it is added to the window's form's control list. The Location property controls its position w.r.t. the enclosing form. Other accessors are Width, Text, and Size.

System.Windows.Forms includes a long list of controls, some of which are summarized in Table 15.4. Examples are given in controls, shown in Listing 15.16 and Figure 15.12.

Some controls open separate windows for more involved dialogue with the user. Some examples are MessageBox, OpenFileDialog, and SaveFileDialog.



Fig. 15.11 After pressing the button 3 times. See Listing 15.15.

| Method/Property | Description |
|-----------------|--|
| Button | A clickable button. |
| CheckBox | A clickable check box. |
| DateTimePicker | A box showing a date with a drop-down menu for choosing another. |
| Label | A displayable text. |
| ProgressBar | A box showing a progress bar. |
| RadioButton | A single clickable radio button. Can be paired with other radio buttons. |
| TextBox | A text area, which can accept input from the user. |

Table 15.4 Some types of System.Windows.Forms.Control.

System.Windows.Forms.MessageBox is used to have a simple but restrictive dialogue with the user, which is demonstrated in Listing 15.17 and Figure 15.13. As an alternative to the YesNo response button, the message box also offers AbortRetryIgnore, OK, OKCancel, RetryCancel, and YesNoCancel. Note that all other windows of the process are blocked until the user closes the dialogue window.

With System.Windows.Forms.OpenFileDialog, you can ask the user to select an existing filename, as demonstrated in Listing 15.18 and Figure 15.14. Similarly to OpenFileDialog, System.Windows.Forms.SaveFileDialog asks for a file name, but if an existing file is selected, then the user will be asked to confirm the choice.

Listing 15.16 winforms/controls.fsx:

```
Examples of control elements added to a window form, see also Figure 15.12.
open System.Windows.Forms
open System.Drawing
let win = new Form () // Create a window
win.ClientSize <- Size (300, 300)
let button = new Button () // Make a button
win.Controls.Add button
button.Location <- new Point (20, 20)
button.Text <- "Click me"</pre>
let lbl = new Label () // Add a label
win.Controls.Add lbl
lbl.Location <- new Point (20, 60)</pre>
lbl.Text <- "A text label"</pre>
let chkbox = new CheckBox () // Add a check box
win.Controls.Add chkbox
chkbox.Location <- new Point (20, 100)
let pick = new DateTimePicker () // Add a date and time picker
win.Controls.Add pick
pick.Location <- new Point (20, 140)
let prgrss = new ProgressBar () // Show a progress bar
win.Controls.Add prgrss
prgrss.Location <- new Point (20, 180)
prgrss.Minimum <- 0</pre>
prgrss.Maximum <- 9
prgrss.Value <- 3
let rdbttn = new RadioButton () // Add a radio button
win.Controls.Add rdbttn
rdbttn.Location <- new Point (20, 220)
let txtbox = new TextBox () // Add a text input field
win.Controls.Add txtbox
txtbox.Location <- new Point (20, 260)
txtbox.Text <- "Type something"</pre>
Application.Run win // Show everything and start event-loop
```

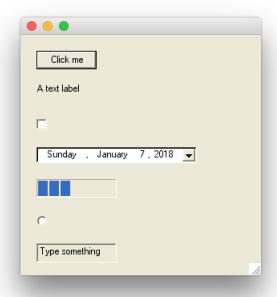


Fig. 15.12 Examples of control elements. See Listing 15.16.



Fig. 15.13 After pressing the "Click-me" button. See Listing 15.17.

Listing 15.17 winforms/messageBox.fsx: Create the MessageBox, see also Figure 15.13. open System.Windows.Forms open System.Drawing open System let win = new Form () win.ClientSize <- Size (140, 80) let button = new Button () win.Controls.Add button button.Size <- new Size (100, 40) button.Location <- new Point (20, 20)</pre> button.Text <- "Click me"</pre> // Open a message box when button clicked let buttonClicked (e : EventArgs) = let question = "Is this statement false?" let caption = "Window caption" let boxType = MessageBoxButtons.YesNo let response = MessageBox.Show (question, caption, boxType) printfn "The user pressed %A" response button.Click.Add buttonClicked Application.Run win

Create the OpenFileDialog, see also Figure 15.14. open System.Windows.Forms open System.Drawing open System let win = new Form () win.ClientSize <- Size (140, 80) let button = new Button () win.Controls.Add button button.Size <- new Size (100, 40) button.Location <- new Point (20, 20) button.Text <- "Click me"</pre> // Open a message box when button clicked let buttonClicked (e : EventArgs) = let opendlg = new OpenFileDialog() let okOrCancel = opendlg.ShowDialog() printfn "The user pressed %A and selected %A" okOrCancel

Listing 15.18 winforms/openFileDialog.fsx:

opendlg.FileName

Application.Run win

button.Click.Add buttonClicked

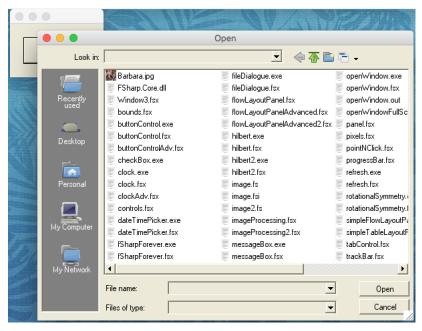


Fig. 15.14 Ask the user for a filename to read from. See Listing 15.18.

15.6 Organizing Controls

It is often useful to organize the controls in groups, and such groups are called *Panels* in WinForms. An example of creating a System.Windows.Forms.Panel that includes a System.Windows.Forms.TextBox and System.Windows.Forms.Label for getting user input is shown in Listing 15.19 and Figure 15.15. The label and

```
Listing 15.19 winforms/panel.fsx:
Create a panel, label, and text input controls.
open System.Drawing
open System.Windows.Forms
let win = new Form () // Create a window form
win.ClientSize <- new Size (200, 100)
// Customize the Panel control
let panel = new Panel ()
panel.ClientSize <- new Size (160, 60)
panel.Location <- new Point (20,20)
panel.BorderStyle <- BorderStyle.Fixed3D</pre>
win.Controls.Add panel // Add panel to window
// Customize the Label and TextBox controls
let label = new Label ()
label.ClientSize <- new Size (120, 20)
label.Location <- new Point (15,5)
label.Text <- "Input"</pre>
panel.Controls.Add label // add label to panel
let textBox = new TextBox ()
textBox.ClientSize <- new Size (120, 20)
textBox.Location <- new Point (20,25)
textBox.Text <- "Initial text"</pre>
panel.Controls.Add textBox // add textbox to panel
Application.Run win // Start the event-loop
```

textbox are children of the panel, and the main advantage of using panels is that the coordinates of the children are relative to the top left corner of the panel. I.e., moving the panel will move the label and the textbox at the same time.

A very flexible panel is the *System.Windows.Forms.FlowLayoutPanel*, which arranges its objects according to the space available. This is useful for graphical user interfaces targeting varying device sizes, such as a computer monitor and a tablet, and it also allows the program to gracefully adapt when the user changes window size. A demonstration of System.Windows.Forms.FlowLayoutPanel together with System.Windows.Forms.CheckBox and System.Windows.Forms.RadioButton is given in Listing 15.20–15.21 and in Figure 15.16. The program illustrates how the button elements flow under four possible flow directions with System.Windows.FlowDirection,

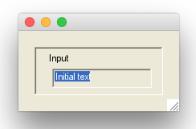


Fig. 15.15 A panel including a label and a text input field, see Listing 15.19.

and how System.Windows.WrapContents influences what happens to content that flows outside the panel's region. A walkthrough of the program is as follows. The

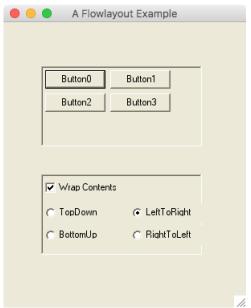


Fig. 15.16 Demonstration of the FlowLayoutPanel panel, CheckBox, and RadioButton controls, see Listing 15.20–15.21.

goal is to make 2 areas, one giving the user control over display parameters, and another displaying the result of the user's choices. These are FlowLayoutPanel and Panel. In the FloatLayoutPanel there are four Buttons to be displayed in a region that is not tall enough for the buttons to be shown in vertical sequence and not wide enough to be shown in horizontal sequence. Thus the FlowDirection rules come into play, i.e., the buttons are added in sequence as they are named, and the default FlowDirection.LeftToRight arranges the buttonLst.[0] in the top

Listing 15.20 winforms/flowLayoutPanel.fsx: Create a FlowLayoutPanel with checkbox and radio buttons. open System.Windows.Forms open System.Drawing let flowLayoutPanel = new FlowLayoutPanel () let buttonLst = [(new Button (), "Button0"); (new Button (), "Button1"); (new Button (), "Button2"); (new Button (), "Button3")] let panel = new Panel () let wrapContentsCheckBox = new CheckBox () let initiallyWrapped = true let radioButtonLst = [(new RadioButton (), (3, 34), "TopDown", FlowDirection.TopDown); (new RadioButton (), (3, 62), "BottomUp", FlowDirection.BottomUp); (new RadioButton (), (111, 34), "LeftToRight", FlowDirection.LeftToRight); (new RadioButton (), (111, 62), "RightToLeft", FlowDirection.RightToLeft)] // customize buttons for (btn, txt) in buttonLst do btn.Text <- txt // customize wrapContentsCheckBox wrapContentsCheckBox.Location <- new Point (3, 3)</pre>

wrapContentsCheckBox.Text <- "Wrap Contents"
wrapContentsCheckBox.Checked <- initiallyWrapped
wrapContentsCheckBox.CheckedChanged.Add (fun _ ->

for (btn, loc, txt, dir) in radioButtonLst do
 btn.Location <- new Point (fst loc, snd loc)</pre>

flowLayoutPanel.FlowDirection <- dir)</pre>

flowLayoutPanel.WrapContents <wrapContentsCheckBox.Checked)</pre>

btn.CheckedChanged.Add (fun _ ->

// customize radio buttons

btn.Text <- txt

left corner, and buttonLst.[1] to its right. Other flow directions do it differently, and the reader is encouraged to experiment with the program.

btn.Checked <- flowLayoutPanel.FlowDirection = dir</pre>

The program in Listing 15.21 has not completely separated the semantic blocks of the interface and relies on explicit setting of coordinates of controls. This can be avoided by using nested panels. E.g., in Listing 15.22–15.23, the program has been rewritten as a nested set of FloatLayoutPanel in three groups: The button panel,

Listing 15.21 winforms/flowLayoutPanel.fsx: Create a FlowLayoutPanel with checkbox and radio buttons. Continued from Listing 15.20.

```
// customize flowLayoutPanel
for (btn, txt) in buttonLst do
  flowLayoutPanel.Controls.Add btn
flowLayoutPanel.Location <- new Point (47, 55)</pre>
flowLayoutPanel.BorderStyle <- BorderStyle.Fixed3D</pre>
flowLayoutPanel.WrapContents <- initiallyWrapped</pre>
// customize panel
panel.Controls.Add (wrapContentsCheckBox)
for (btn, loc, txt, dir) in radioButtonLst do
  panel.Controls.Add (btn)
panel.Location <- new Point (47, 190)
panel.BorderStyle <- BorderStyle.Fixed3D</pre>
// Create a window, add controls, and start event-loop
let win = new Form ()
win.ClientSize <- new Size (302, 356)</pre>
win.Controls.Add flowLayoutPanel
win.Controls.Add panel
win.Text <- "A Flowlayout Example"</pre>
Application.Run win
```

the checkbox, and the radio button panel. Adding a Resize event handler for the window to resize the outermost panel according to the outer window allows for the three groups to change position relative to each other. This results in three different views, all shown in Figure 15.17.

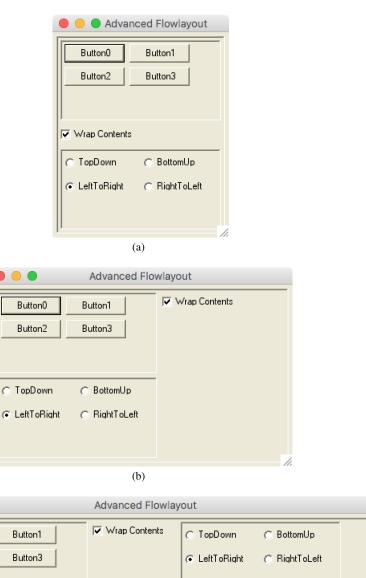


Fig. 15.17 Nested FlowLayoutPanel, see Listing 15.22–15.23, allows for dynamic arrangement of content. Content flows when the window is resized.

Listing 15.22 winforms/flowLayoutPanelAdvanced.fsx: Create nested FlowLayoutPanel.

```
open System.Windows.Forms
open System.Drawing
open System
let win = new Form ()
let mainPanel = new FlowLayoutPanel ()
let mainPanelBorder = 5
let flowLayoutPanel = new FlowLayoutPanel ()
let buttonLst =
  [(new Button (), "Button0");
   (new Button (), "Button1");
(new Button (), "Button2");
(new Button (), "Button3")]
let wrapContentsCheckBox = new CheckBox ()
let panel = new FlowLayoutPanel ()
let initiallyWrapped = true
let radioButtonLst =
  [(new RadioButton (), "TopDown", FlowDirection.TopDown);
   (new RadioButton (), "BottomUp", FlowDirection.BottomUp);
(new RadioButton (), "LeftToRight",
   FlowDirection.LeftToRight);
   (new RadioButton (), "RightToLeft",
   FlowDirection.RightToLeft)]
// customize buttons
for (btn, txt) in buttonLst do
  btn.Text <- txt</pre>
// customize radio buttons
for (btn, txt, dir) in radioButtonLst do
  btn.Text <- txt
  btn.Checked <- flowLayoutPanel.FlowDirection = dir</pre>
  btn.CheckedChanged.Add (fun _ ->
   flowLayoutPanel.FlowDirection <- dir)</pre>
// customize flowLayoutPanel
for (btn, txt) in buttonLst do
  flowLayoutPanel.Controls.Add btn
flowLayoutPanel.BorderStyle <- BorderStyle.Fixed3D</pre>
flowLayoutPanel.WrapContents <- initiallyWrapped</pre>
// customize wrapContentsCheckBox
wrapContentsCheckBox.Text <- "Wrap Contents"</pre>
wrapContentsCheckBox.Checked <- initiallyWrapped</pre>
wrapContentsCheckBox.CheckedChanged.Add (fun _ ->
   flowLayoutPanel.WrapContents <-</pre>
   wrapContentsCheckBox.Checked)
```

Listing 15.23 winforms/flowLayoutPanelAdvanced.fsx: Create nested FlowLayoutPanel. Continued from Listing 15.22.

```
// customize panel
// changing border style changes ClientSize
panel.BorderStyle <- BorderStyle.Fixed3D</pre>
let width = panel.ClientSize.Width / 2 - panel.Margin.Left -
   panel.Margin.Right
for (btn, txt, dir) in radioButtonLst do
  btn.Width <- width
  panel.Controls.Add (btn)
mainPanel.Location <- new Point (mainPanelBorder,</pre>
   mainPanelBorder)
mainPanel.BorderStyle <- BorderStyle.Fixed3D</pre>
mainPanel.Controls.Add flowLayoutPanel
{\tt mainPanel.Controls.Add\ wrapContentsCheckBox}
mainPanel.Controls.Add panel
// customize window, add controls, and start event-loop
win.ClientSize <- new Size (220, 256)</pre>
let windowResize _ =
  let size = win.DisplayRectangle.Size
  mainPanel.Size <- new Size (size.Width - 2 *
   mainPanelBorder, size.Height - 2 * mainPanelBorder)
windowResize ()
win.Resize.Add windowResize
win.Controls.Add mainPanel
win.Text <- "Advanced Flowlayout"</pre>
Application.Run win
```

Chapter 16

The Event-driven Programming Paradigm

In event-driven programming, the flow of the program is determined by events, such as the user moving the mouse, an alarm going off, a message arriving from another program, or an exception being thrown, and is very common for programs with extensive interaction with a user, such as a graphical user interface. The events are monitored by listeners, and the programmer can set handlers which are call-back functions to be executed when an event occurs. In event-driven programs, there is almost always a main loop to which the program relinquishes control to when all handlers have been set up. Event-driven programs can be difficult to test, since they often rely on difficult-to-automate mechanisms for triggering events, e.g., testing a graphical user interface often requires users to point-and-click, which is very slow compared to automatic unit testing.

Chapter 17

Assemblies

. . .

However, it is ill-advised to design programs to be run in an interactive session, \star since the scripts need to be manually copied every time it is to be run, and since the starting state may be unclear.

Both the interpreter and the compiler translates the source code into a format which can be executed by the computer. While the compiler performs this translation once and stores the result in the executable file, the interpreter translates the code every time the code is executed. Thus, to run the program again with the interpreter, it must be retranslated as "\$fsharpi gettingStartedStump.fsx". In contrast, compiled code does not need to be recompiled to be run again, only re-executed using "\$ mono gettingStartedStump.exe". On a MacBook Pro, with a 2.9 GHz Intel Core i5, the time the various stages take for this script are:

| Command | Time |
|--|-------|
| fsharpi gettingStartedStump.fsx | 1.88s |
| <pre>fsharpc gettingStartedStump.fsx</pre> | |
| mono gettingStartedStump.exe | 0.05s |

I.e., executing the script with fsharpi is slightly faster than by first compiling it with fsharpc and then executing the result with mono (1.88s < 0.05s + 1.90s), if the script were to be executed only once, but every future execution of the script using the compiled version requires only the use of mono, which is much faster than fsharpi $(1.88s \gg 0.05s)$.

Finally, the file containing gettingStartedStump.tex may be compiled into an executable file with the program fsharpc, and run using the program mono from the console. This is demonstrated in Listing 17.1.

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```
Listing 17.1: Compiling and executing a script.

1  $ (fsharpc gettingStartedStump.fsx)
2  F# Compiler for F# 4.1 (Open Source Edition)
3  Freely distributed under the Apache 2.0 Open Source License
4  $ (mono gettingStartedStump.exe)
5  3
```

The compiler reads gettingStartedStump.fsx and makes gettingStartedStump.exe, which can be run using mono.

Executing programs with the interpreted directly from a file and compiling and executing the program is much preferred for programming complete programs, since the starting state is well defined, and since this better supports *unit testing*, which is

★ a method for debugging programs. Thus, **prefer compiling over interpretation.**

Chapter 18

Organising Code in Libraries and Application Programs

In this chapter, we will focus on a number of ways to make the code available as *library* functions in F#. A library is a collection of types, values, and functions that an application program can use. A library does not perform calculations on its own.

F# includes several programming structures to organize code in libraries: Modules, namespaces, and classes. In this chapter, we will describe modules and namespaces. Classes will be described in detail in Chapter 23.

18.1 Modules

An F# *module*, not to be confused with a Common Language Infrastructure module (see Appendix D), is a programming structure used to organize type declarations, values, functions, etc.

Every implementation and script file in F# implicitly defines a module, and the module name is given by the filename. Consider the script file Meta.fsx shown in Listing 18.1. Here, we have implicitly defined a module with the name Meta. Another

```
Listing 18.1 Meta.fsx:
A script file defining the apply function.

1 type floatFunction = float -> float -> float
2 let apply (f : floatFunction) (x : float) (y : float) : float
= f x y
```

script file may now use this function, which is accessed using the "." notation, i.e., Meta.apply will refer to this function in other programs. An application program could be as the one shown in Listing 18.3. In the example above, we have explicitly

```
Listing 18.2 MetaApp.fsx:

Defining a script calling the module.

1 let add: Meta.floatFunction = fun x y -> x + y
2 let result = Meta.apply add 3.0 4.0
3 printfn "3.0 + 4.0 = %A" result
```

used the module's type definition for illustration purposes. A shorter and possibly simpler program would have been to define add as let add x y = x + y, since F#'s type system will infer the implied type. However, explicit definitions of types is recommended for readability. Hence, an alternative to the above example's use of anonymous functions is: let add (x: float) (y: float) : float = x + y. To compile the module and the application program, we write as demonstrated in Listing 18.3. Since the F# compiler reads through the files once, the order of the

```
Listing 18.3: Compiling both the module and the application code. Note that file order matters when compiling several files.

$\f$ fsharpc \text{--nologo Meta.fsx MetaApp.fsx && mono MetaApp.exe} \]

$\f$ 3.0 + 4.0 = 7.0
```

filenames in the compile command is very important. Hence, the script containing the module and function definitions must be to the left of the script containing their use. Notice also that if not otherwise specified, the F# compiler produces an .exe file derived from the last filename in the list of filenames.

We may also explicitly define the module name using the *module* with the following syntax,

```
Listing 18.4: Outer module.

| module <ident>
| <script>
```

Here, the identifier <ident> is a name not necessarily related to the filename, and the script <script> is an expression. An example is given in Listing 18.20. Since

```
Listing 18.5 MetaExplicit.fsx:
Explicit definition of the outermost module.

1 module Meta
2 type floatFunction = float -> float -> float
3 let apply (f : floatFunction) (x : float) (y : float) : float
= f x y
```

we have created a new file, where the module Meta is explicitly defined, we can use the same application program. This is demonstrated in Listing 18.6. Since MetaExplicit.fsx explicitly defines the module name, apply is not available to an application program as MetaExplicit.apply. It is recommended that mod-

* an application program as MetaExplicit.apply. It is recommended that module names are defined explicitly, since filenames may change due to external 213 18.1 *Modules*

Listing 18.6: Changing the module definition to explicit naming has no effect on the application nor the compile command.

```
1 $ fsharpc --nologo MetaExplicit.fsx MetaApp.fsx && mono
    MetaApp.exe
2 3.0 + 4.0 = 7.0
```

conditions. In other words, filenames are typically set from the perspective of the filesystem. The user may choose to change names to suit a filesystem structure, or different platforms may impose different file naming conventions. Thus, direct linking of filenames with the internal workings of a program is a needless complication of structure.

The definitions inside a module may be accessed directly from an application program, omitting the "."-notation, by use of the *open* keyword,

```
Listing 18.7: Open module.

open <ident>
```

We can modify MetaApp.fsx, as shown in Listing 18.9. In this case, the namespace

```
Listing 18.8 MetaAppWOpen.fsx:

Avoiding the "."-notation by the keyword.

1 open Meta
2 let add: floatFunction = fun x y -> x + y
3 let result = apply add 3.0 4.0
4 printfn "3.0 + 4.0 = %A" result
```

of our previously defined module is included into the scope of the application functions, and its types, values, functions, etc. can be used directly, as shown in Listing 18.9. The open-keyword should be used sparingly, since including a library's

```
Listing 18.9: How the application program opens the module has no effect on the module code nor compile command.
```

definitions into the application scope can cause surprising naming conflicts, because the user of a library typically has no knowledge of the inner workings of the library. E.g., the user may accidentally use code defined in the library, but with different type and functionality than intended, which the type system will use to deduce types in the application program, and therefore will either give syntax or runtime errors that are difficult to understand. This problem is known as *namespace pollution*, and for clarity, **it is recommended to use the open-keyword sparingly**. Note that for historical reasons, the phrase 'namespace pollution' is used to cover pollution both due to modules and namespaces.

Modules may also be nested, in which case the nested definitions must use the "="-sign and must be appropriately indented.

```
Listing 18.10: Nested modules.

| module <ident> = <script>
```

In lightweight syntax, a newline may be entered before the script <script>, and the script must be indented. An example is shown in Listing 18.11. In this case, Meta and

```
Listing 18.11 nestedModules.fsx:

Modules may be nested.

1 module Utilities
2 let PI = 3.1415
3 module Meta =
4 type floatFunction = float -> float -> float
5 let apply (f : floatFunction) (x : float) (y : float) :
6 float = f x y
7 module MathFcts =
7 let add : Meta.floatFunction = fun x y -> x + y
```

MathFcts are defined at the same level and said to be siblings, while Utilities is defined at a higher level. In this relation, the former two are said to be the children of the latter. Note that the nesting respects the lexical scope rules, such that the constant PI is directly accessible in both modules Meta and MathFcts, as is the module Meta in MathFcts, but not MathFcts in Meta. The "."-notation is reused to index deeper into the module hierarchy, as the example in Listing 18.12 shows. Modules can be

```
Listing 18.12 nestedModulesApp.fsx:
Applications using nested modules require additional usage of the "." notation to navigate the nesting tree.

let add: Utilities.Meta.floatFunction = fun x y -> x + y
let result = Utilities.Meta.apply Utilities.MathFcts.add 3.0
Utilities.PI
printfn "3.0 + 4.0 = %A" result
```

recursive using the **rec**-keyword, meaning that in our example we can make the outer module recursive, as demonstrated in Listing 18.13. The consequence is that the modules Meta and MathFcts are accessible in both modules, but compilation will now give a warning since soundness of the code will first be checked at runtime. In

★ general, it is advised to **avoid programming constructions whose validity cannot be checked at compile-time.**

Listing 18.13 nestedRecModules.fsx:

Mutual dependence on nested modules requires the keyword in the module definition.

```
module rec Utilities
module Meta =

type floatFunction = float -> float -> float

let apply (f : floatFunction) (x : float) (y : float) :
 float = f x y

module MathFcts =

let add : Meta.floatFunction = fun x y -> x + y
```

18.2 Namespaces

An alternative way to structure code in modules is to use a *namespace*, which can only hold modules and type declarations and only works in compiled mode. Namespaces are defined as explicitly defined outer modules, using the *namespace* keyword in accordance with the following syntax.

```
Listing 18.14: Namespace.

namespace <ident>
<cri>cscript>
```

An example is given in Listing 18.15. Notice that when organizing code in a

```
Listing 18.15 namespace.fsx:

Defining a namespace is similar to explicitly named modules.

1 namespace Utilities
2 type floatFunction = float -> float -> float
3 module Meta =
4 let apply (f : floatFunction) (x : float) (y : float) :
float = f x y
```

namespace, the first line of the file, other than comments and compiler directives, must be the one starting with namespace.

As for modules, the content of a namespace is accessed using the "." notation, as demonstrated in Listing 18.16. Likewise, the compilation is performed in the same

```
Listing 18.16 namespaceApp.fsx:
The "."-notation lets the application program access functions and types in a namespace.

1 let add: Utilities.floatFunction = fun x y -> x + y
2 let result = Utilities.Meta.apply add 3.0 4.0
3 printfn "3.0 + 4.0 = %A" result
```

way as for modules, see Listing 18.17. Hence, from an application point of view, it is

Listing 18.17: Compilation of files including namespace definitions uses the same procedure as modules.

not immediately possible to see that Utilities is defined as a namespace and not a module. However, in contrast to modules, namespaces may span several files. E.g., we may add a third file extending the Utilities namespace with the MathFcts module, as demonstrated in Listing 18.18. To compile, we now need to include all three files

Listing 18.18 namespaceExtension.fsx:

Namespaces may span several files. Here is shown an extra file which extends the Utilities namespace.

```
namespace Utilities
module MathFcts =
let add : floatFunction = fun x y -> x + y
```

in the right order, see Listing 18.19. The order matters:namespaceExtension.fsx

Listing 18.19: Compilation of namespaces defined in several files requires careful consideration of order, since the compiler reads once and only once through the files in the order they are given.

```
$ fsharpc --nologo namespace.fsx namespaceExtension.fsx
    namespaceApp.fsx && mono namespaceApp.exe
2 3.0 + 4.0 = 7.0
```

uses the definition of floatFunction in the file namespace.fsx. You can use extensions to extend existing namespaces included with the F# compiler.

Namespaces may also be nested. In contrast to modules, nesting is defined using the "." notation. That is, to create a child namespace more of Utilities, we must use initially write namespace Utilities.more. Indentation is ignored in the namespace line, thus left-most indentation is almost always used. Namespaces follow lexical scope rules, and identically to modules, namespaces containing mutually dependent children can be declared using the rec keyword, e.g., namespace rec Utilities.

18.3 Compiled Libraries

Libraries may be distributed in compiled form as .dl1 files. This saves the user from having to recompile a possibly large library every time library functions needs to be compiled with an application program. In order to produce a library file

from MetaExplicit.fsx and then compile an application program, we first use the compiler's -a option to produce the .dll. A demonstration is given in Listing 18.20. This produces the file MetaExplicit.dll, which may be linked to an application

Listing 18.20: A stand-alone .dll file is created and used with special compile commands.

```
1 $ fsharpc --nologo -a MetaExplicit.fsx
```

by using the -r option during compilation, see Listing 18.21. A library can be

Listing 18.21: The library is linked to an application during compilation to produce runnable code.

```
$ fsharpc --nologo -r MetaExplicit.dll MetaApp.fsx && mono
    MetaApp.exe
2 3.0 + 4.0 = 7.0
```

the result of compiling a number of files into a single .dll file. .dll-files may be loaded dynamically in script files (.fsx-files) by using the #r directive, as illustrated in Listing 18.22. We may now omit the explicit mentioning of the library when

Listing 18.22 MetaHashApp.fsx:

The .dll file may be loaded dynamically in .fsx script files and in interactive mode. Nevertheless, this usage is not recommended.

```
#r "MetaExplicit.dll"
let add : Meta.floatFunction = fun x y -> x + y
let result = Meta.apply add 3.0 4.0
printfn "3.0 + 4.0 = %A" result
```

compiling, as shown in Listing 18.23. The #r directive is also used to include a

Listing 18.23: When using the #r directive, then the .dll file need not be explicitly included in the list of files to be compiled.

```
$\frac{1}{2}$ fsharpc --nologo MetaHashApp.fsx && mono MetaHashApp.exe 3.0 + 4.0 = 7.0
```

library in interactive mode. However, for the code to be compiled, the use of the #r directive requires that the filesystem path to the library is coded inside the script. As for module names, direct linking of filenames with the internal workings of a program is a needless complication of structure, and it is recommended not to rely on the use of the #r directive.

In the above listings we have compiled *script files* into libraries. However, F# has reserved the .fs filename suffix for library files, and such files are called *implementation files*. In contrast to script files, implementation files do not support the #r directive. When compiling a list of implementation and script files, all but the last file must explicitly define a module or a namespace.

Both script and implementation files may be augmented with *signature files*. A signature file contains no implementation, only type definitions. Signature files offer three distinct features:

- 1. Signature files can be used as part of the documentation of code, since type information is of paramount importance for an application programmer to use a library.
- Signature files may be written before the implementation file. This allows for a higher-level programming design that focuses on *which* functions should be included and *how* they can be composed.
- 3. Signature files allow for access control. Most importantly, if a type definition is not available in the signature file, then it is not available to the application program. Such definitions are private and can only be used internally in the library code. More fine-grained control related to classes is available and will be discussed in Chapter 23.

Signature files can be generated automatically using the --sig:<filename> compiler directive. To demonstrate this feature, we will first move the definition of add to the implementation file, see Listing 18.28. A signature file may be automatically

Listing 18.24 MetaWAdd.fs: An implementation file including the add function. 1 module Meta 2 type floatFunction = float -> float -> float 3 let apply (f : floatFunction) (x : float) (y : float) : float = f x y 4 let add (x : float) (y : float) : float = x + y

generated, as shown in Listing 18.25. The warning can safely be ignored, since at this

```
Listing 18.25: Automatic generation of a signature file at compile time.

1 $ fsharpc --nologo --sig:MetaWAdd.fsi -a MetaWAdd.fs
```

point it is not our intention to produce runnable code. The above listing has generated the signature file in Listing 18.26. We can generate a library using the automatically

```
Listing 18.26 MetaWAdd.fsi:

An automatically generated signature file from MetaWAdd.fs.

1 module Meta
2 type floatFunction = float -> float -> float
3 val apply : f:floatFunction -> x:float -> y:float -> float
4 val add : x:float -> y:float -> float
```

generated signature file by writing fsharpc -a MetaWAdd.fsi MetaWAdd.fs, which is identical to compiling the .dll file without the signature file. However, if

we remove, e.g., the type definition for add in the signature file, then this function becomes private to the module and cannot be accessed outside. Hence, using the signature file in Listing 18.27, and recompiling the .dll with Listing 18.24 does not generates errors. However, when using the newly created MetaWAdd.dll with

Listing 18.27 MetaWAddRemoved.fsi: Removing the type defintion for add from MetaWAdd.fsi. 1 module Meta 2 type floatFunction = float -> float -> float 3 val apply : f:floatFunction -> x:float -> y:float -> float

Listing 18.28: Automatic generation of a signature file at compile time.

```
n application that does not itself supply a definition of add, we get a syntax
```

\$ fsharpc --nologo -a MetaWAdd.fsi MetaWAdd.fs

an application that does not itself supply a definition of add, we get a syntax error, since add now is inaccessible to the application program. This is demonstrated in Listing 18.29 and 18.30.

```
Listing 18.29 MetaWOAddApp.fsx:
A version of Listing 18.3 without a definition of add.

let result = Meta.apply add 3.0 4.0
printfn "3.0 + 4.0 = %A" result
```

```
Listing 18.30: Automatic generation of a signature file at compile time.
```

```
1  $ fsharpc --nologo -r MetaWAdd.dll MetaWAddRemoved.fsi
    MetaWOAddApp.fsx
2
2  MetaWOAddApp.fsx(1,25): error FS0039: The value or
    constructor 'add' is not defined.
4  MetaWAddRemoved.fsi(1,1): error FS0240: The signature file
    'Meta' does not have a corresponding implementation file.
    If an implementation file exists then check the 'module'
    and 'namespace' declarations in the signature and
    implementation files match.
```

18.4 Debugging modules

Chapter 19

Testing Programs

A software bug is an error in a computer program that causes it to produce an incorrect result or behave in an unintended manner. The term 'bug' was used by Thomas Edison in 1878¹², but made popular in computer science by Grace Hopper, who found a moth interfering with the electronic circuits of the Harward Mark II electromechanical computer and coined the term *bug* for errors in computer programs. The original bug is shown in Figure 19.1. Software is everywhere, and



Fig. 19.1 The first computer bug, caught by Grace Hopper, U.S. Naval Historical Center Online Library Photograph NH 96566-KN.

errors therein have a huge economic impact on our society and can threaten lives3.

The ISO/IEC organizations have developed standards for software testing⁴. To illustrate basic concepts of software quality, consider a hypothetical route planning system. Essential factors of its quality are:

https://en.wikipedia.org/wiki/Software_bug

² http://edison.rutgers.edu/NamesSearch/DocImage.php3?DocId=LB003487

³ https://en.wikipedia.org/wiki/List_of_software_bugs

 $^{^4}$ ISO/IEC 9126, International standard for the evaluation of software quality, December 19, 1991, later replaced by ISO/IEC 25010:2011

Functionality: Does the software compile and run without internal errors. Does it solve the problem it was intended to solve? E.g., does the route planning software find a suitable route from point a to b?

Reliability: Does the software work reliably over time? E.g., does the route planning software work when there are internet dropouts?

Usability: Is the software easy and intuitive to use by humans? E.g., is it easy to enter addresses and alternative routes in the software's interface?

Efficiency: How many computer and human resources does the software require? E.g., does it take milliseconds or hours to find a requested route? Can the software run on a mobile platform with limited computer speed and memory?

Maintainability: In case of the discovery of new bugs, is it easy to test and correct the software? Is it easy to extend the software with new functionality? E.g., is it easy to update the map with updated roadmaps and new information? Can the system be improved to work both for car drivers and bicyclists?

Portability: Is it easy to port the software to new systems such as new server architecture and screen sizes? E.g., if the routing software originally was written for IOS devices, will it be easy to port to Android systems?

The above-mentioned concepts are ordered based on the requirements of the system. Functionality and reliability are perhaps the most important concepts, since if the software does not solve the specified problem, then the software design process has failed. However, many times the problem definition will evolve along with the software development process. But as a bare minimum, the software should run without internal errors and not crash under a well-defined set of circumstances. Furthermore, it is often the case that software designed for the general public requires a lot of attention to the usability of the software, since in many cases non-experts are expected to be able to use the software with little or no prior training. On the other hand, software used internally in companies will be used by a small number of people who become experts in using the software, and it is often less important that the software is easy to understand by non-experts. An example is text processing software like Microsoft Word versus Gnu Emacs and LaTeX. Word is designed to be used by non-experts for small documents such as letters and notes and relies heavily on interfacing with the system using click-interaction. On the other hand, Emacs and LaTeX are for experts for longer and professionally typeset documents and relies heavily on keyboard shortcuts and text-codes for typesetting document entities.

The purpose of *software testing* is to find bugs. When errors are found, then we engage in *debugging*, which is the process of diagnosing and correcting bugs. Once we have a failed software test, i.e., one that does not find any bugs, then we have strengthened our belief in the software, but it is important to note that software testing and debugging rarely removes all bugs, and with each correction or change

of software there is a fair risk new bugs being introduced. It is not exceptional that the testing-software is as large as the software being tested.

In this chapter, we will focus on two approaches to software testing which emphasize functionality: white-box and black-box testing. An important concept in this context is unit testing, where the program is considered in smaller pieces, called units, and for which accompanying programs for testing can be made which test these units automatically. Black-box testing considers the problem formulation and the program interface, and can typically be written early in the software design phase. In contrast, white-box testing considers the program text, and thus requires the program to be available. Thus, there is a tendency for black-box test programs to be more stable, while white-box testing typically is developed incrementally alongside the software development.

To illustrate software testing, we'll start with a problem:

Problem 19.1

iven any date in the Gregorian calendar, calculate the day of the week.

Facts about dates in the Gregorian calendar are:

- Combinations of dates and weekdays repeat themselves every 400 years.
- The typical length of the months January, February, . . . follow the knuckle rule, i.e., January belongs to the index knuckle, February to the space between the index and the middle finger, and August restarts or starts on the other hand. All knuckle months have 31 days, all spacing months have 30 days except February, which has 29 days on leap years and 28 days all other years.
- A leap year is a multiple of 4, except if it is also a multiple of 100 but not of 400.

Many solutions to the problem have been discovered, and here we will base our program on Gauss' method, which is based on integer division and calculates the weekday of the 1st of January of a given year. For any other date, we will count our way through the weeks from the previous 1st of January. The algorithm relies on an enumeration of weekdays starting with Sunday = 0, Monday = 1, ..., and Saturday = 0. Our proposed solution is shown in Listing 19.1.

19.1 White-box Testing

White-box testing considers the text of a program. The degree to which the text of the program is covered in the test is called the *coverage*. Since our program is small,

Listing 19.1 date2Day.fsx:

A function that can calculate day-of-week from any date in the Gregorian calendar.

```
let januaryFirstDay (y : int) =
  let a = (y - 1) \% 4
  let b = (y - 1) \% 100
let c = (y - 1) \% 400
  (1 + 5 * a + 4 * b + 6 * c) % 7
let rec sum (lst : int list) j =
  if 0 <= j && j < lst.Length then</pre>
    lst.[0] + sum lst.[1..] (j - 1)
  else
let date2Day d m y =
  let dayPrefix =
    ["Sun"; "Mon"; "Tues"; "Wednes"; "Thurs"; "Fri"; "Satur"]
  let feb = if (y % 4 = 0) && ((y % 100 <> 0) || (y % 400 =
   0)) then 29 else 28
  let daysInMonth = [31; feb; 31; 30; 31; 30; 31; 30; 31;
   30; 31]
  let dayOne = januaryFirstDay y
  let daysSince = (sum daysInMonth (m - 2)) + d - 1
  let weekday = (dayOne + daysSince) % 7;
  dayPrefix.[weekday] + "day"
```

we have the opportunity to ensure that all functions are called at least once, which is called *function coverage*, and we will also be able to test every branching in the program, which is called *branching coverage*. If both are fulfilled, we say that we have *statement coverage*. The procedure is as follows:

- 1. Decide which units to test: The program shown in Listing 19.1 has 3 functions, and we will consider these each as a unit, but we might as well just have chosen date2Day as a single unit. The important part is that the union of units must cover the whole program text, and since date2Day calls both januaryFirstDay and sum, designing test cases for the latter two is superfluous. However, we may have to do this anyway when debugging, and we may choose at a later point to use these functions separately, and in both cases, we will be able to reuse the testing of the smaller units.
- 2. Identify branching points: The function januaryFirstDay has no branching function, sum has one, and depending on the input values, two paths through the code may be used, and date2Day has one where the number of days in February is decided. Note that in order to test this, our test-date must be March 1 or later. In this example, there are only examples of if-branch points, but they may as well be loops and pattern matching expressions. In the Listing 19.2 it is shown that the branch points have been given a comment and a number.

Listing 19.2 date2DayAnnotated.fsx: In white-box testing, the branch points are identified. // Unit: januaryFirstDay let januaryFirstDay (y : int) = let a = (y - 1) % 4(1 + 5 * a + 4 * b + 6 * c) % 7 // Unit: sum let rec sum (lst : int list) j = (* WB: 1 *) if 0 <= j && j < lst.Length then</pre> lst.[0] + sum lst.[1..] (j - 1)else 0 // Unit: date2Day let date2Day d m y = let dayPrefix = ["Sun"; "Mon"; "Tues"; "Wednes"; "Thurs"; "Fri"; "Satur"] (* WB: 1 *) let feb = if (y % 4 = 0) && ((y % 100 <> 0) || (y % 400 = 0)) then 29 else 28 let daysInMonth = [31; feb; 31; 30; 31; 30; 31; 31; 30; 31; 30; 31] let dayOne = januaryFirstDay y let daysSince = (sum daysInMonth (m - 2)) + d - 1 let weekday = (dayOne + daysSince) % 7; dayPrefix.[weekday] + "day"

- 3. For each unit, produce an input set that tests each branch: In our example, the branch points depend on a Boolean expression, and for good measure, we are going to test each term that can lead to branching. Using 't' and 'f' for true and false, we thus write as shown in Table 19.1. The impossible cases have been intentionally blank, e.g., it is not possible for j < 0 and j > n for some positive value n.
- 4. Write a program that tests all these cases and checks the output, see Listing 19.3.

Notice that the output of the tests is organized such that they are enumerated per unit, hence we can rearrange as we like and still uniquely refer to a unit's test. Also, the output of the test program produces a list of tests that should return true or success or a similar positively loaded word, but without further or only little detail, such that we at a glance can identify any test that produced unexpected results.

| Unit | Branch | Condition | Input | Expected output |
|-----------------|--------|-----------------|--------------|-----------------|
| januaryFirstDay | 0 | - | 2016 | 5 |
| sum | 1 | 0 <= j && | | |
| | | j < lst.Length | | |
| | 1a | t && t | [1; 2; 3] 1 | 3 |
| | 1b | f && t | [1; 2; 3] -1 | 0 |
| | 1c | t && f | [1; 2; 3] 10 | 0 |
| | 1d | f && f | - | - |
| date2Day | 1 | (y % 4 = 0) && | | |
| | | ((y % 100 <> 0) | | |
| | | 11 | | |
| | | (y % 400 = 0)) | | |
| | - | t && (t t) | - | - |
| | 1a | t && (t f) | 8 9 2016 | Thursday |
| | 1b | t && (f t) | 8 9 2000 | Friday |
| | 1c | t && (f f) | 8 9 2100 | Wednesday |
| | - | f && (t t) | - | - |
| | 1d | f && (t f) | 8 9 2015 | Tuesday |
| | - | f && (f t) | - | - |
| | - | f && (f f) | - | - |

Table 19.1 Unit test

Listing 19.3 date2DayWhiteTest.fsx:

The tests identified by white-box analysis. The program from Listing 19.2 has been omitted for brevity.

```
printfn "White-box testing of date2Day.fsx"
printfn " Unit: januaryFirstDay"
printfn "
           Branch: 0 - %b" (januaryFirstDay 2016 = 5)
printfn " Unit: sum"
printfn "
           Branch: 1a - %b" (sum [1; 2; 3] 1 = 3)
printfn "
             Branch: 1b - \%b'' (sum [1; 2; 3] -1 = 0)
printfn "
           Branch: 1c - \%b'' (sum [1; 2; 3] 10 = 0)
printfn " Unit: date2Day"
printfn " Branch: 1a - %b" (date2Day 8 9 2016 =
   "Thursday")
printfn " Branch: 1b - %b" (date2Day 8 9 2000 =
   "Friday")
printfn "
            Branch: 1c - %b" (date2Day 8 9 2100 =
   "Wednesday")
printfn " Branch: 1d - %b" (date2Day 8 9 2015 =
   "Tuesday")
$ fsharpc --nologo date2DayWhiteTest.fsx && mono
   date2DayWhiteTest.exe
White-box testing of date2Day.fsx
  Unit: januaryFirstDay
   Branch: 0 - true
  Unit: sum
    Branch: 1a - true
    Branch: 1b - true
    Branch: 1c - true
  Unit: date2Day
    Branch: 1a - true
    Branch: 1b - true
    Branch: 1c - true
    Branch: 1d - true
```

After the white-box testing has failed to find errors in the program, we have some confidence in the program, since we have run every line at least once. It is, however, in no way a guarantee that the program is error free, which is why white-box testing is often accompanied with black-box testing to be described next.

19.2 Black-box Testing

In black-box testing, the program is considered a black box, and no knowledge is required about how a particular problem is solved. In fact, it is often useful not to have that knowledge at all. It is rarely possible to test all input to a program, so in black-box testing, the solution is tested for typical and extreme cases based on knowledge of the problem. The procedure is as follows:

- 1. Decide on the interface to use: It is useful to have an agreement with the software developers about what interface is to be used, e.g., in our case, the software developer has made a function date2Day d m y where d, m, and y are integers specifying the day, month, and year.
- 2. Make an overall description of the tests to be performed and their purpose:
 - 1 a consecutive week, to ensure that all weekdays are properly returned
 - 2 two set of consecutive days across boundaries that may cause problems: across a new year, and across a regular month boundary.
 - 3 a set of consecutive days across February-March boundaries for a leap and non-leap year
 - 4 four dates after February in a non-leap year, a non-multiple-of-100 leap year, a multiple-of-100-but-not-of-400 non-leap year, and a multiple-of-400 leap year.

Given no information about the program's text, there are other dates that one could consider as likely candidates for errors, but the above is judged to be a fair coverage.

- 3. Choose a specific set of input and expected output relations on the tabular form as shown in Table 19.2.
- 4. Write a program executing the tests, as shown in Listing 19.4 and 19.5. Notice

| Test number | Input | Expected output |
|-------------|------------|-----------------|
| 1a | 1 1 2016 | Friday |
| 1b | 2 1 2016 | Saturday |
| 1c | 3 1 2016 | Sunday |
| 1d | 4 1 2016 | Monday |
| 1e | 5 1 2016 | Tuesday |
| 1f | 6 1 2016 | Wednesday |
| 1g | 7 1 2016 | Thursday |
| 2a | 31 12 2014 | Wednesday |
| 2b | 1 1 2015 | Thursday |
| 2c | 30 9 2017 | Saturday |
| 2d | 1 10 2017 | Sunday |
| 3a | 28 2 2016 | Sunday |
| 3b | 29 2 2016 | Monday |
| 3c | 1 3 2016 | Tuesday |
| 3d | 28 2 2017 | Tuesday |
| 3e | 1 3 2017 | Wednesday |
| 4a | 1 3 2015 | Sunday |
| 4b | 1 3 2012 | Thursday |
| 4c | 1 3 2000 | Wednesday |
| 4d | 1 3 2100 | Monday |

Table 19.2 Black-box testing

how the program has been made such that it is almost a direct copy of the table produced in the previous step.

A black-box test is a statement of what a solution should fulfill for a given problem. Hence, it is a good idea to make a black-box test early in the software design phase, in order to clarify the requirements for the code to be developed and take an outside view of the code prior to developing it.

After the black-box testing has failed to find errors in the program, we have some confidence in the program, since, from a user's perspective, the program produces sensible output in many cases. It is, however, in no way a guarantee that the program is error free.

19.3 Debugging by Tracing

Once an error has been found by testing, the *debugging* phase starts. The cause of a bug can either be that the chosen algorithm is the wrong one for the job, or the implementation of it has an error. In the debugging process, we have to keep an open mind and not rely on assumptions. A frequent source of errors is that the state of a program is different than expected, e.g., because the calculation performed is different than intended, or that the return of a library function is different than

Listing 19.4 date2DayBlackTest.fsx:

The tests identified by black-box analysis. The program from Listing 19.2 has been omitted for brevity.

```
let testCases = [
   ("A complete week",
    [(1, 1, 2016, "Friday");
(2, 1, 2016, "Saturday");
(3, 1, 2016, "Sunday");
(4, 1, 2016, "Monday");
(5, 1, 2016, "Tuesday");
      (6, 1, 2016, "Wednesday");
(7, 1, 2016, "Thursday");]);
   ("Across boundaries",
     [(31, 12, 2014, "Wednesday");
      (1, 1, 2015, "Thursday");
(30, 9, 2017, "Saturday");
(1, 10, 2017, "Sunday")]);
   ("Across Feburary boundary",
     [(28, 2, 2016, "Sunday");
(29, 2, 2016, "Monday");
(1, 3, 2016, "Tuesday");
      (28, 2, 2017, "Tuesday");
(1, 3, 2017, "Wednesday")]);
   ("Leap years",
    [(1, 3, 2015, "Sunday");
(1, 3, 2012, "Thursday");
(1, 3, 2000, "Wednesday");
(1, 3, 2100, "Monday")]);
printfn "Black-box testing of date2Day.fsx"
for i = 0 to testCases.Length - 1 do
   let (setName, testSet) = testCases.[i]
   printfn " %d. %s" (i+1) setName
   for j = 0 to testSet.Length - 1 do
      let (d, m, y, expected) = testSet.[j]
      let day = date2Day d m y
      printfn "
                          test %d - %b'' (j+1) (day = expected)
```

```
Listing 19.5: Output from Listing 19.4.
$ fsharpc --nologo date2DayBlackTest.fsx && mono
    date2DayBlackTest.exe
Black-box testing of date2Day.fsx
  1. A complete week
    test 1 - true
    test 2 - true
    test 3 - true
    test 4 - true
    test 5 - true
    test 6 - true
    test 7 - true
  2. Across boundaries
    test 1 - true
    test 2 - true
   test 3 - true
    test 4 - true
  3. Across Feburary boundary
    test 1 - true
test 2 - true
    test 3 - true
    test 4 - true
    test 5 - true
  4. Leap years
    test 1 - true
    test 2 - true
    test 3 - true
    test 4 - true
```

introduce *Trace by hand* as a technique to simulate the execution of a program by hand. In the following section, tracing will refer to the Trace by hand method.

To understand the method of Tracing by hand, we will consider 3 imperative programs of gradually increasing complexity: a program using function call, a program including a for-loop, and a program with dynamic scope. In Section 7.4 we give a fourth example using recursion, a concept to be introduced in Chapter 7.

Tracing may seem tedious in the beginning, but in conjunction with strategically placed debugging printfn statements, it is a very valuable tool for debugging.

19.3.1 Tracing Function Calls

Consider the program in Listing 19.6. The program calls testScope 2.0, and by

```
Listing 19.6 lexicalScopeTracing.fsx:

Example of lexical scope and closure environment.

1 let testScope x =
2 let a = 3.0
3 let f z = a * z
4 let a = 4.0
5 f x
6 printfn "%A" (testScope 2.0)

1 $ fsharpc --nologo lexicalScopeTracing.fsx && mono lexicalScopeTracing.exe
2 6.0
```

running the program, we see that the return-value is 6.0 and not 8.0, as we had expected. Hence, we will use tracing to understand the result.

Tracing a program by hand means that we simulate its execution and, as part of that, keep track of the bindings, assignments closures, scopes, and input and output of the program. To do this, we need to consider the concept of *environments*.

Environments describe bindings available to the program at the present scope and at a particular time and place in the code. There is always an outer environment, called E_0 , and each time we call a function or create a scope, we create a new environment. Only one environment can be active at a time, and it is updated as we simulate the execution of code with new bindings and temporary evaluations of expressions. Once a scope is closed, then its environment is deleted and a return-value is transported to its enclosing environment. In tracing, we note return-values explicitly. Likewise, output from, e.g., printfn is reported with a special notation.

To trace code, we make a table with 4 columns: Step, Line, Environment, and Bindings and evaluations. The Step column enumerates the steps performed. The Line column contains the program-line treated in a step *where* the present environment is updated. The Environment contains the name of the present environment, and Bindings . . . shows *what* in the environment is updated.

The code in Listing 19.6 contains a function definition and a call, hence, the first lines of our table looks like,

```
Step Line Env. Bindings and evaluations

\begin{array}{c|cccc}
\hline
0 & - & E_0 & () \\
1 & 1 & E_0 & testScope = ((x), testScope-body, ()) \\
2 & 6 & E_0 & testScope = 2.0 = ?
\end{array}
```

The elements of the table is to be understood as follows. Step 0 initializes the outer environment. In order for us to remember that the environment is empty, we write the unit value "()". Reading the code from top to bottom, the first nonempty and noncomment line we meet is line 1, hence, in Step 1, we update the environment with the binding of a function to the name testScope. Since functions are values in F#, we note their bindings by their closures: a tuple of argument names, the function-body, and the values lexically available at the place of binding. See Section 4.2 for more information on closures. Following the function-binding, the printfn statement is called in line 6 to print the result testScope 2.0. However, before we can produce any output, we must first evaluate testScope 2.0. Since we do not yet know what this function evaluates to, in Step 2 we simply write the call with a question mark. The call causes the creation of a new environment, and we continue our table as follows.

Step Line Env. Bindings and evaluations

3 1
$$E_1$$
 (($x = 2.0$), testScope-body, ())

This means that we are going to execute the code in testScope-body. The function was called with 2.0 as argument, causing x = 2.0. Hence, the only binding available at the start of this environment is to the name x. In the testScope-body, we make 3 further bindings and a function call. First to a, then to f, then to another a, which will overshadow the previous binding, and finally we call f. Thus, our table is updated as follows.

Note that by lexical scope, the closure of f includes everything above its binding in E_1 , and therefore we add a = 3.0 and x = 2.0 to the environment element in its

closure. This has consequences for the following call to f in line 5, which creates a new environment based on f's closure and the value of its arguments. The value of f in Step 7 is found by looking in the previous steps for the last binding to the name f in f in Step 3. Note that the binding to a name f in Step 5 is an internal binding in the closure of f and is irrelevant here. Hence, we continue the table as,

Step Line Env. Bindings and evaluations

8 3
$$E_2$$
 $((z = 2.0), a * z, (a = 3.0, x = 2.0))$

Executing the body of f, we initially have 3 bindings available: z = 2.0, a = 3.0, and x = 2.0. Thus, to evaluate the expression a * z, we use these bindings and write,

| Step | Line | Env. | Bindings and evaluations |
|------|------|-------|--------------------------|
| 9 | 3 | E_2 | a*z=6.0 |
| 10 | 3 | E_2 | return = 6.0 |

The 'return'-word is used to remind us that this is the value to replace the question mark with in Step 7. Here we will make a mental note and not physically replace the question mark with the calculated value. If you are ever in doubt which call is connected with which return value, seek upwards in the table from the return statement for the first question mark. Now we delete E_2 and return to the enclosing environment, E_1 . Here the function call was the last expression, hence the return-value from testScope will be equal to the return-value from f, and we write,

Step Line Env. Bindings and evaluations

11 3
$$E_1$$
 return = 6.0

Similarly, we delete E_1 and return to the question mark in Step 2, which is replaced by the value 6.0. We can now finish the printfn statement and produce the output,

Step Line Env. Bindings and evaluations

12 | 6 |
$$E_0$$
 output = "6.0\n"

The return-value of a printfn statement is (), and since this line is the last of our program, we return () and end the program:

Step Line Env. Bindings and evaluations
$$\begin{array}{c|cccc}
13 & 6 & E_0 & \text{return} = ()
\end{array}$$

The full table is shown for completeness in Table 19.3. Hence, we conclude that the program outputs the value 6.0, since the function f uses the first binding of

```
Step | Line Env. Bindings and evaluations
           E_0 ()
           E_0 testScope = ((x), \text{testScope-body}, ())
2
     6
          E_0 testScope 2.0 = ?
3
          E_1 ((x = 2.0), testScope-body, ())
     1
4
           E_1
     2
              a = 3.0
5
           E_1 f = ((z), a * z, (a = 3.0, x = 2.0))
6
     4
           E_1
               a = 4.0
     5
           E_1 f x = ?
7
8
     3
          E_2 ((z = 2.0), a * z, (a = 3.0, x = 2.0))
     3
           E_2 \quad a * z = 6.0
10
     3
           E_2 return = 6.0
11
     3
           E_1
               return = 6.0
12.
     6
          E_0 output = "6.0\n"
13
    6
          E_0 return = ()
```

Table 19.3 The complete table produced while tracing the program in Listing 19.6 by hand.

a = 3.0, and this is because the binding of f to the expression a * z creates a closure with a lexical scope. Thus, in spite that there is an overshadowing value of a, when f is called, this binding is ignored in the body of f. To correct this, we update the code as shown in Listing 19.7.

```
Listing 19.7 lexicalScopeTracingCorrected.fsx:

Tracing the code in Listing 19.6 by hand produced the table in Table 19.3, and to get the desired output, we correct the code as shown here.

let testScope x =
let a = 4.0
let f z = a * z
f x
printfn "%A" (testScope 2.0)

$\frac{1}{2}$ fsharpc --nologo lexicalScopeTracingCorrected.fsx && mono lexicalScopeTracingCorrected.exe

2 8.0
```

19.3.2 Tracing Loops

Consider the program in Listing 19.8. The program includes a function for printing the sequence of the first *N* squares of integers. It uses a **for**-loop with a counting value. F# creates a new environment each time the loop body is executed. Thus, to trace this program, we mentally *unfold* the loop as shown in Listing 19.9. The unfolding contains 3 new scopes lines 3–7, lines 8–12, and lines 13–17 corresponding

Listing 19.8 printSquares.fsx: Print the squares of a sequence of positive integers. 1 let N = 3 2 let printSquares n = 3 for i = 1 to n do 4 let p = i * i 5 printfn "%d: %d" i p 6 printSquares N 1 \$ fsharpc --nologo printSquares.fsx && mono printSquares.exe 2 1: 1 3 2: 4 4 3: 9

```
Listing 19.9 printSquaresUnfold.fsx:
An unfolded version of Listing 19.8.
let N = 3
let printSquaresUnfold n =
     let i = 1
    let p = i * i
     printfn "%d: %d" i p
     let i = 2
     let p = i * i
     printfn "%d: %d" i p
     let i = 3
     let p = i * i
     printfn "%d: %d" i p
{\tt printSquaresUnfold} \ {\tt N}
$ fsharpc --nologo printSquaresUnfold.fsx && mono
    printSquaresUnfold.exe
1: 1
2: 4
3: 9
```

to the 3 times, the loop is repeated, and each scope starts by binding the counting value to the name i.

In the rest of this section, we will refer to the code in Listing 19.8. The first rows in our tracing-table looks as follows:

Step Line Env. Bindings and evaluations $\begin{array}{c|cccc}
\hline
0 & - & E_0 & () \\
1 & 1 & E_0 & N = 3 \\
2 & 2 & E_0 & printSquares = ((n), printSquares-body, (N = 3)) \\
3 & 7 & E_0 & printSquares N = ?
\end{array}$

Note that due to the lexical scope rule, the closure of printSquares includes N in its environment element. Calling printSquares N causes the creation of a new environment,

Step Line Env. Bindings and evaluations
4 2
$$E_1$$
 ($(n = 3)$, printSquares-body, $(N = 3)$)

The first statement of printSquares-body is the for-loop. As our unfolding in Listing 19.9 demonstrated, each time the loop-body is executed, a new scope is created with a new binding to i. Reusing the notation from closures, we write

Step Line Env. Bindings and evaluations
$$5 \quad 3 \quad E_1 \quad \text{for} \dots = ?$$

and create a new environment as if it had been a function,

Step Line Env. Bindings and evaluations

$$E_2 = E_2 = E_3$$
 $E_3 = E_4 = E_3$
 $E_4 = E_4$
 $E_5 = E_6$
 $E_6 = E_7$
 $E_7 = E_8$

As for functions, this denotes the bindings available at beginning of the execution of the **for**-body. The first line in the **for**-body is the binding of the value of an expression to p. The expression is i*i, and to calculate its value, we look in the **for**-loop's pseudo-closure where we find the i = 1 binding. Hence,

Step Line Env. Bindings and evaluations7
$$4$$
 E_2 $i * i = 1$ 8 4 E_2 $p = 1$

The final step in the for-body is the printfn-statement. Its arguments we get from the updated, active environment E_2 and write,

At this point, the **for**-loop has reached its last line, E_2 is deleted, we create a new environment with the counter variable increased by 1, and repeat. Hence,

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```
Step Line Env. Bindings and evaluations

10 3 E_3 ((i = 2), for-body, (n = 3, N = 3))

11 4 E_3 i * i = 4
```

11 | 4 |
$$E_3$$
 | $t * t = 4$
12 | 4 | E_3 | $p = 4$
13 | 5 | E_3 | output = "2 : 4\n"

Again, we delete E_3 , create E_4 where i is incremented, and repeat,

Step Line Env. Bindings and evaluations

14 3 E_4 ((i = 3), for-body, (n = 3, N = 3))

15 4 E_4 i * i = 916 4 E_4 p = 917 5 E_4 output = "3:9\n"

Finally, incrementing i would mean that i > n, hence the **for**-loop ends and as all statements returns ()

Step Line Env. Bindings and evaluations
$$\begin{array}{c|cccc}
18 & 3 & E_4 & \text{return} = ()
\end{array}$$

At this point, the environment E_4 is deleted, and we return to the enclosing environment E_1 and the statement or expression following Step 5. Since the for-loop is the last expression in the printSquares function, its return value is that of the for-loop,

Step Line Env. Bindings and evaluations
$$\begin{array}{c|cccc}
19 & 3 & E_1 & \text{return} = ()
\end{array}$$

Returning to Step 3 and environment E_0 , we have now calculated the return-value of printSquares N to be (), and since this line is the last of our program, we return () and end the program:

Step Line Env. Bindings and evaluations
$$20 \quad 3 \quad E_0 \quad \text{return} = ()$$

19.3.3 Tracing Mutable Values

For mutable bindings, the scope is dynamic. For this, we need the concept of storage. Consider the program in Listing 19.10. To trace the dynamic behavior of this program, we add a second table to our hand tracing, which is initially empty and has the columns Step and Value to hold the Step number when the value was updated and the value stored. For Listing 19.10, the firsts 4 steps thus look like,

Listing 19.10 dynamicScopeTracing.fsx: Example of lexical scope and closure environment. 1 let testScope x = 2 let mutable a = 3.0 3 let f z = a * z 4 a <- 4.0 5 f x 6 printfn "%A" (testScope 2.0) 1 \$ fsharpc --nologo dynamicScopeTracing.fsx && mono dynamicScopeTracing.exe 2 8.0

| Step | Line | Env. | Bindings and evaluations | Step | Value |
|------|------|-------|-----------------------------|------|-------|
| 0 | - | E_0 | | 0 | - |
| 1 | 1 | E_0 | testScope = ((x), body, ()) | | |
| 2 | 6 | E_0 | testScope $2.0 = ?$ | | |
| 3 | 1 | E_1 | ((x = 2.0), body, ()) | | |

The mutable binding in line 2 creates an internal name and a dynamic storage location. The name a will be bound to a reference value, which we call α_1 , and which is a unique name shared between the two tables:

Step | Line Env. Bindings and evaluationsStep | Value4 | 2 |
$$E_1$$
 | $a = \alpha_1$ 4 | $\alpha_1 = 3.0$

The following closure of f uses the reference-name instead of its value,

Step Line Env. Bindings and evaluations
$$5 \mid 3 \mid E_1 \mid f = ((z), a * z, (x = 2.0, a = \alpha_1))$$
 Step Value $4 \mid \alpha_1 = 3.0$

In line 4, the value in the storage is updated by the assignment operator, which we denote as,

Step Line Env. Bindings and evaluationsStep Value64
$$E_1$$
 $a < -4.0$

Hence, when we evaluate the function f, its closure looks up the value of a by following the reference and finding the new value:

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```
Step | Line Env. Bindings and evaluations
                                                               \alpha_1 = 4.0
           E_1 f x = ?
8
           E_2 ((z = 2.0), a * z, (x = 2.0, a = \alpha_1))
9
     5
           E_2 \quad a*z = 8.0
10
           \overline{E_2} return = 8.0
10
           E_1 return = 8.0
11
     6
           E_0 output = "8.0\n"
12
    6
           E_0 return = ()
```

For reference, the complete pair of tables is shown in Table 19.4. By comparing this

| Step | Line | Env | . Bindings and evaluations | Step | Value |
|------|--|-------|---|------|------------------|
| 0 | - | E_0 | () | 0 | - |
| 1 | 1 | E_0 | testScope = ((x), body, ()) | 4 | $\alpha_1 = 3.0$ |
| 2 | | | testScope $2.0 = ?$ | 6 | $\alpha_1 = 4.0$ |
| 3 | 1 | E_1 | ((x = 2.0), body, ()) | | , |
| 4 | 2 | E_1 | $a = \alpha_1$ | | |
| 5 | $\begin{vmatrix} 2 \\ 3 \end{vmatrix}$ | E_1 | $f = ((z), a * z, (x = 2.0, a = \alpha_1))$ | | |
| 6 | 4 | E_1 | a < -4.0 | | |
| 7 | 5 | E_1 | f x = ? | | |
| 8 | 5 | E_2 | $((z = 2.0), a * z, (x = 2.0, a = \alpha_1))$ | | |
| 9 | 5 | E_2 | a * z = 8.0 | | |
| 10 | 5 | E_2 | return = 8.0 | | |
| 10 | 5 | E_1 | return = 8.0 | | |
| 11 | 6 | E_0 | $output = "8.0 \n"$ | | |
| 12 | 6 | E_0 | return = () | | |

Table 19.4 The complete table produced while tracing the program in Listing 19.10 by hand.

to the value-bindings in Listing 19.6, we see that the mutable values give rise to a different result due to the difference between lexical and dynamic scope.

Chapter 20

Mutable values

20.1 Variables

Identifiers may be mutable, which means that the it may be rebound to a new value. Mutable identifiers are specified using the *mutable* keyword with the following syntax:

```
Listing 20.1: Syntax for defining mutable values with an initial value.

let mutable <ident> = <expr> [in <expr>]
```

Changing the value of an identifier is called *assignment* and is done using the "<-" lexeme. Assignments have the following syntax:

```
Listing 20.2: Value reassignment for mutable variables.
```

Mutable values is synonymous with the term variable. A variable is an area in the computer's working memory associated with an identifier and a type, and this area may be read from and written to during program execution, see Listing 20.3 for an example. Here, an area in memory was denoted x, initially assigned the integer value 5, hence the type was inferred to be int. Later, this value of x was replaced with another integer using the "<-" lexeme. The "<-" lexeme is used to distinguish the assignment from the comparison operator. For example, the statement a = 3 in Listing 20.4 is not an assignment but a comparison which is evaluated to be false. However, it is important to note that when the variable is initially defined, then the "'=" operator must be used, while later reassignments must use the "<-" expression.

Assignment type mismatches will result in an error, as demonstrated in Listing 20.5. I.e., once the type of an identifier has been declared or inferred, it cannot be changed.

Listing 20.3 mutableAssignReassingShort.fsx:

A variable is defined and later reassigned a new value.

```
let mutable x = 5
printfn "%d" x
x <- -3
printfn "%d" x

1 $ fsharpc --nologo mutableAssignReassingShort.fsx && mono mutableAssignReassingShort.exe
5 -3</pre>
```

Listing 20.4: It is a common error to mistake "=" and "<-" lexemes for mutable variables.

```
1 > let mutable a = 0
2 - a = 3;;
3 val mutable a : int = 0
4 val it : bool = false
```

Listing 20.5 mutableAssignReassingTypeError.fsx: Assignment type mismatching causes a compile-time error.

```
let mutable x = 5
printfn "%d" x
x <- -3.0
printfn "%d" x

$ fsharpc --nologo mutableAssignReassingTypeError.fsx && mono mutableAssignReassingTypeError.exe

mutableAssignReassingTypeError.fsx(3,6): error FS0001: This expression was expected to have type
    'int'
but here has type
    'float'</pre>
```

A typical variable is a counter of type integer, and a typical use of counters is to increment them, see Listing 20.6 for an example. Using variables in expressions, as opposed to the left-hand-side of an assignment operation, reads the value of the variable. Thus, when using a variable as the return value of a function, then the value is copied from the local scope of the function to the scope from which it is called. This is demonstrated in Listing 20.7. In the example we see that the type is a value, and not mutable.

Variables implement dynamic scope, that is, the value of an identifier depends on *when* it is used. This is in contrast to lexical scope, where the value of an identifier

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Listing 20.6 mutableAssignIncrement.fsx: Variable increment is a common use of variables. 1 let mutable x = 5 // Declare a variable x and assign the value 5 to it 2 printfn "%d" x 3 x <- x + 1 // Increment the value of x 4 printfn "%d" x 1 \$ fsharpc --nologo mutableAssignIncrement.fsx && mono mutableAssignIncrement.exe 2 5 3 6

depends on *where* it is defined. As an example, consider the script in Listing 4.24 which defines a function using lexical scope and returns the number 6.0, however, if a is made mutable, then the behavior is different, as shown in Listing 20.8. Here,

```
Listing 20.8 dynamicScopeNFunction.fsx:

Mutual variables implement dynamic scope rules. Compare with Listing 4.24.

1 let testScope x =
2 let mutable a = 3.0
3 let f z = a * z
4 a <- 4.0
5 f x
6 printfn "%A" (testScope 2.0)

1 $ fsharpc --nologo dynamicScopeNFunction.fsx && mono dynamicScopeNFunction.exe
2 8.0
```

the response is 8.0, since the value of a changed before the function f was called.

20.2 Reference Cells

F# has a variation of mutable variables called *reference cells*. Reference cells have the built-in function *ref* and the operators "!" and ":=", where ref creates a reference variable, and the "!" and the ":=" operators respectively reads and writes its value. An example of using reference cells is given in Listing 20.9. Reference cells

```
Listing 20.9 refCell.fsx:

Reference cells are variants of mutable variables.

1 let x = ref 0
2 printfn "%d" !x
3 x := !x + 1
4 printfn "%d" !x

1 $ fsharpc --nologo refCell.fsx && mono refCell.exe
2 0
3 1
```

are different from mutable variables, since their content is allocated on *The Heap*. The Heap is a global data storage that is not destroyed when a function returns, which is in contrast to the *call stack*, also known as *The Stack*. The Stack maintains all the local data for a specific instance of a function call, see Section 7.2 for more details. As a consequence, when a reference cell is returned from a function, then it is the reference to the location on The Heap, which is returned as a value. Since this points outside the local data area of the function, this location is still valid after the function returns, and the variable stored there is accessible to the caller. This is illustrated in Figure 20.1

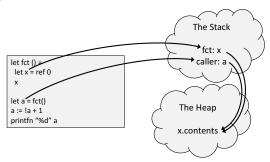


Fig. 20.1 A reference cell is a pointer to The Heap, and the content is not destroyed when its reference falls out of scope.

Reference cells may cause *side-effects*, where variable changes are performed across independent scopes. Some side-effects are useful, e.g., the printf family changes the content of the screen, and the screen is outside the scope of the caller. Another example of a useful side-effect is a counter shown in Listing 20.10. Here incr is

Listing 20.10 refEncapsulation.fsx: An increment function with a local state using a reference cell. 1 let incr = 2 let counter = ref 0 3 fun () -> 4 counter := !counter + 1 5 !counter 6 printfn "%d" (incr ()) 7 printfn "%d" (incr ()) 8 printfn "%d" (incr ()) 1 \$ fsharpc --nologo refEncapsulation.fsx && mono refEncapsulation.exe 2 1 3 2 4 3

an anonymous function with an internal state counter. At first glance, it may be surprising that incr () does not return the value 1 at every call. The reason is that the value of the incr is the closure of the anonymous function fun () -> counter := ..., which is

```
incr: (args, exp, env) = ((), (counter := !counter + 1), (counter \rightarrow ref 0)).
```

Thus, counter is only initiated once at the initial binding, while every call of incr () updates its value on The Heap. Such a programming structure is called *encapsulation*, since the counter state has been encapsulated in the anonymous function, and the only way to access it is by calling the same anonymous function. In general, it is advisable to **use encapsulation to hide implementation details irrelevant to the user of the code.**

The incr example in Listing 20.10 is an example of a useful side-effect. An example to be avoided is shown in Listing 20.11. In the example, the function updateFactor changes a variable in the scope of the function multiplyWithFactor. The code style is prone to errors, since the computations are not local at the place of writing, i.e., in multiplyWithFactor, and if updateFactor were defined in a library, then the source code may not be available. Better style of programming is shown in Listing 20.12. Here, there can be no doubt in multiplyWithFactor that the value of a is changing. Side-effects do have their use, but should, in general, be avoided at almost all costs, and it is advised to minimize the use of side effects.

Reference cells give rise to an effect called *aliasing*, where two or more identifiers refer to the same data, as illustrated in Listing 20.13. Here, a is defined as a reference cell, and by defining b to be equal to a, we have created an alias. This can be very confusing since as the example shows, changing the value of b causes a to change

Listing 20.11 refSideEffect.fsx: Intertwining independent scopes is typically a bad idea. 1 let updateFactor factor = 2 factor := 2 3 let multiplyWithFactor x = 1 let a = ref 1 2 updateFactor a 3 !a * x 9 printfn "%d" (multiplyWithFactor 3) 1 \$ fsharpc --nologo refSideEffect.fsx && mono refSideEffect.exe 2 6

```
Listing 20.12 refWithoutSideEffect.fsx:
A solution similar to Listing 20.11 without side-effects.

let updateFactor () =
2
let multiplyWithFactor x =
let a = ref 1
a := updateFactor ()
!a * x

printfn "%d" (multiplyWithFactor 3)

$ fsharpc --nologo refWithoutSideEffect.fsx && mono refWithoutSideEffect.exe
6
```

★ as well. Aliasing is a variant of side-effects, and aliasing should be avoided at all costs

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Since F# version 4.0, the compiler has automatically converted mutable variables to reference cells, where needed. E.g., Listing 20.10 can be rewritten using a mutable variable, as shown in Listing 20.14. Reference cells are preferred over mutable

Listing 20.14 mutableEncapsulation.fsx: Local mutable content can be indirectly accessed outside its scope. let incr = let mutable counter = 0 fun () -> counter <- counter + 1 counter printfn "%d" (incr ()) printfn "%d" (incr ()) printfn "%d" (incr ()) f fsharpc --nologo mutableEncapsulation.fsx && mono mutableEncapsulation.exe 1 2 4 3

variables for encapsulation, in order to avoid confusion.

20.3 Arrays

One dimensional *arrays*, or just arrays for short, are mutable lists of the same type and follow a similar syntax as lists. Arrays can be stated as a *sequence expression*,

```
Listing 20.15: The syntax for an array using the sequence expression.

[[[<expr>{; <expr>}]]]
```

E.g., [|1; 2; 3|] is an array of integers, [|"This"; "is"; "an"; "array"|] is an array of strings, [|(fun $x \rightarrow x$); (fun $x \rightarrow x*x$)|] is an array of functions, [||] is the empty array. Arrays may also be given as ranges,

```
Listing 20.16: The syntax for an array using the range expression.

| [|<expr> ... <expr> [... <expr>]|]
```

but arrays of *range expressions* must be of <expr> integers, floats, or characters. Examples are [|1 .. 5|], [|-3.0 .. 2.0|], and [|'a' .. 'z'|]. Range expressions may include a step size, thus, [|1 .. 2 .. 10|] evaluates to [|1; 3; 5; 7; 9|].

The array type is defined using the array keyword or alternatively the "[]" lexeme. Like strings and lists, arrays may be indexed using the ".[]" notation. Arrays cannot be resized, but are mutable, as shown in Listing 20.17. Notice that in spite

```
Listing 20.17 arrayReassign.fsx:

Arrays are mutable in spite of the missing keyword.

| let square (a : int array) = for i = 0 to a.Length - 1 do a.[i] <- a.[i] * a.[i] |
| let A = [| 1; 2; 3; 4; 5 |] printfn "%A" A square A printfn "%A" A
| square A printfn "%A" A |
| fsharpc --nologo arrayReassign.fsx && mono arrayReassign.exe [|1; 2; 3; 4; 5|] |
| [|1; 4; 9; 16; 25|]
```

of the missing mutable keyword, the function square still has the *side-effect* of squaring all entries in A. F# implements arrays as chunks of memory and indexes arrays via address arithmetic. I.e., element i in an array, whose first element is in memory address α and whose elements fill β addresses each, is found at address $\alpha + i\beta$. Hence, indexing has computational complexity of O(1), but appending and prepending values to arrays and array concatenation requires copying the new and existing values to a fresh area in memory and thus has computational complexity $O(\alpha)$ where α is the total number of elements. Thus, indexing arrays is feet, but

 \star O(n), where n is the total number of elements. Thus, **indexing arrays is fast, but** cons and concatenation is slow and should be avoided.

Arrays support *slicing*, that is, indexing an array with a range result in a copy of the array with values corresponding to the range. This is demonstrated in Listing 20.18. As illustrated, the missing start or end index imply from the first or to the last element, respectively.

Arrays do not have explicit operator support for appending and concatenation, instead the Array namespace includes an Array. append function, as shown in Listing 20.19.

Arrays are *reference types*, meaning that identifiers are references and thus suffer from aliasing, as illustrated in Listing 20.20.

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Listing 20.18: Examples of array slicing. Compare with Listing 6.6 and Listing 3.27.

```
1 > let arr = [|'a' ... 'g'|];;
2 val arr : char [] = [|'a'; 'b'; 'c'; 'd'; 'e'; 'f'; 'g'|]
3
4 > arr.[0];;
5 val it : char = 'a'
6
7 > arr.[3];;
8 val it : char = 'd'
9
10 > arr.[3..];;
11 val it : char [] = [|'d'; 'e'; 'f'; 'g'|]
12
13 > arr.[..3];;
14 val it : char [] = [|'a'; 'b'; 'c'; 'd'|]
15
16 > arr.[1..3];;
17 val it : char [] = [|'b'; 'c'; 'd'|]
18
19 > arr.[*];;
20 val it : char [] = [|'a'; 'b'; 'c'; 'd'; 'e'; 'f'; 'g'|]
```

Listing 20.19 arrayAppend.fsx:

Two arrays are appended with Array.append.

```
let a = [|1; 2;|]
let b = [|3; 4; 5|]
let c = Array.append a b
printfn "%A, %A, %A" a b c

statement of the statement of
```

Listing 20.20 arrayAliasing.fsx:

Arrays are reference types and suffer from aliasing.

```
let a = [|1; 2; 3|];
let b = a
a.[0] <- 0
printfn "a = %A, b = %A" a b;;

standard from the stand
```

20.3.1 Array Properties and Methods

Some important properties and methods for arrays are:

Clone(): 'T [].

Returns a copy of the array.

```
Listing 20.21: Clone

1 > let a = [|1; 2; 3|];
2 - let b = a.Clone()
3 - a.[0] <- 0
4 - printfn "a = %A, b = %A" a b;;
5 a = [|0; 2; 3|], b = [|1; 2; 3|]
6 val a : int [] = [|0; 2; 3|]
7 val b : obj = [|1; 2; 3|]
8 val it : unit = ()
```

Length: int.

Returns the number of elements in the array.

```
Listing 20.22: Length

| > [|1; 2; 3|].Length;;
| val it : int = 3
```

20.3.2 The Array Module

There are quite a number of built-in procedures for arrays in the Array module, some of which are summarized below.

```
Array.append: arr1:'T [] -> arr2:'T [] -> 'T [].
```

Creates an new array whose elements are a concatenated copy of arr1 and arr2.

```
Listing 20.23: Array.append

1 > Array.append [|1; 2;|] [|3; 4; 5|];;
2 val it : int [] = [|1; 2; 3; 4; 5|]
```

Array.contains: elm:'T -> arr:'T [] -> bool.

Returns true if arr contains elm.

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```
Listing 20.24: Array.contains

| > Array.contains 3 [|1; 2; 3|];;
| val it : bool = true
```

Array.exists: $f:('T \rightarrow bool) \rightarrow arr:'T [] \rightarrow bool.$

Returns true if any application of f evaluates to true when applied to the elements of arr.

```
Listing 20.25: Array.exists

1 > Array.exists (fun x -> x % 2 = 1) [|0 ... 2 ... 4|];;
2 val it : bool = false
```

Array.filter: f:('T -> bool) -> arr:'T [] -> 'T [].

Returns an array of elements from arr who evaluate to true when f is applied to them.

```
Listing 20.26: Array.filter

| > Array.filter (fun x -> x % 2 = 1) [|0 .. 9|];;
| val it : int [] = [|1; 3; 5; 7; 9|]
```

Array.find: $f:('T \rightarrow bool) \rightarrow arr:'T [] \rightarrow 'T$.

Returns the first element in arr for which f evaluates to true. The KeyNotFoundException exception is raised if no element is found. See Section 13.1 for more on exceptions.

```
Listing 20.27: Array.find

| > Array.find (fun x -> x % 2 = 1) [|0 .. 9|];;
| val it : int = 1
```

Array.findIndex: f:('T -> bool) -> arr:'T [] -> int.

Returns the index of the first element in in arr for which f evaluates to true. If none are found, then the System.Collections.Generic.KeyNotFoundException exception is raised. See Section 13.1 for more on exceptions.

```
Listing 20.28: Array.findIndex

| > Array.findIndex (fun x -> x = 'k') [|'a' .. 'z'|];;
| val it : int = 10
```

Array.fold: $f:('S \rightarrow 'T \rightarrow 'S) \rightarrow elm:'S \rightarrow arr:'T [] \rightarrow 'S$.

Updates an accumulator iteratively by applying f to each element in arr. The initial value of the accumulator is elm. For example, when arr consists of n+1 elements Array. fold calculates:

```
f (... (f (f elm arr.[0]) arr.[1]) ...) arr.[n].
```

```
Listing 20.29: Array.fold

1 > let addSquares acc elm = acc + elm*elm
2 - Array.fold addSquares 0 [|0 .. 9|];;
3 val addSquares : acc:int -> elm:int -> int
4 val it : int = 285
```

Array.foldBack: f:('T -> 'S -> 'S) -> arr:'T [] -> elm:'S -> 'S.

Updates an accumulator iteratively backwards by applying f to each element in arr. The initial value of the accumulator is elm. For exampel, when arr consists of n+1 elements Array.foldBack calculates:

f arr.[0] (f arr.[1](...(f arr.[n] elm)...)).

```
Listing 20.30: Array.foldBack

1 > let addSquares elm acc = acc + elm*elm
2 - Array.foldBack addSquares [|0 .. 9|] 0;;
3 val addSquares : elm:int -> acc:int -> int
4 val it : int = 285
```

Array.forall: f:('T -> bool) -> arr:'T [] -> bool.

Returns true if f evaluates to true for every element in arr.

```
Listing 20.31: Array.forall

1 > Array.forall (fun x -> (x % 2 = 1)) [|0 .. 9|];;
2 val it : bool = false
```

Array.init: $m:int \rightarrow f:(int \rightarrow T) \rightarrow T$

Create an array with m elements and whose value is the result of applying f to the index of the element.

```
Listing 20.32: Array.init

1 > Array.init 10 (fun i -> i * i);;
2 val it : int [] = [|0; 1; 4; 9; 16; 25; 36; 49; 64; 81|]
```

Array.isEmpty: arr:'T [] -> bool.
Returns true if arr is empty.

```
Listing 20.33: Array.isEmpty

1 > Array.isEmpty [||];;
2 val it : bool = true
```

Array.iter: f:('T -> unit) -> arr:'T [] -> unit.
Applies f to each element of arr.

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```
Listing 20.34: Array.iter

| > Array.iter (fun x -> printfn "%A " x) [|0; 1; 2|];;
| 0
```

Array.map: f:('T -> 'U) -> arr:'T [] -> 'U [].

Creates an new array whose elements are the results of applying f to each of the elements of arr.

```
Listing 20.35: Array.map
```

Array.ofList: lst:'T list -> 'T [].

Creates an array whose elements are copied from 1st.

```
Listing 20.36: Array.ofList

1 > Array.ofList [1; 2; 3];;
2 val it : int [] = [|1; 2; 3|]
```

Array.rev: arr:'T [] -> 'T [].

Creates a new array whose elements are identical to arr but in reverse order.

```
Listing 20.37: Array.rev

| > Array.rev [|1; 2; 3|];;
| val it : int [] = [|3; 2; 1|]
```

Array.sort: arr:'T[] -> 'T [].

Creates a new array with the same elements as in arr but in sorted order

```
Listing 20.38: Array.sort

1 > Array.sort [|3; 1; 2|];;
2 val it : int [] = [|1; 2; 3|]
```

Array.toList: arr:'T [] -> 'T list.

Creates a new list whose elements are copied from arr.

```
Listing 20.39: Array.toList

1 > Array.toList [|1; 2; 3|];;
2 val it : int list = [1; 2; 3]
```

Array.unzip: arr:('T1 * 'T2) [] -> 'T1 [] * 'T2 [].

Returns a pair of arrays of all the first elements and all the second elements of arr, respectively.

```
Listing 20.40: Array.unzip

| > Array.unzip [|(1, 'a'); (2, 'b'); (3, 'c')|];;
| val it : int [] * char [] = ([|1; 2; 3|], [|'a'; 'b';
| 'c'|])
```

Array.zip: arr1:'T1 [] -> arr2:'T2 [] -> ('T1 * 'T2) [].

Returns a list of pairs, where elements in arr1 and arr2 are iteratively paired.

```
Listing 20.41: Array.zip

1 > Array.zip [|1; 2; 3|] [|'a'; 'b'; 'c'|];;
2 val it : (int * char) [] = [|(1, 'a'); (2, 'b'); (3, 'c')|]
```

20.4 Multidimensional Arrays

Multidimensional arrays can be created as arrays of arrays (of arrays...). These are known as *jagged arrays*, since there is no inherent guarantee that all sub-arrays are of the same size. The example in Listing 20.42 is a jagged array of increasing width. Indexing arrays of arrays is done sequentially, in the sense that in the above example,

```
Listing 20.42 arrayJagged.fsx:

An array of arrays. When row lengths are of non-equal elements, then it is a jagged array.

let arr = [|[|1|]; [|1; 2|]; [|1; 2; 3|]|]

for row in arr do
for elm in row do
printf "%A" elm
printf "\n"

1 $ fsharpc --nologo arrayJagged.fsx && mono arrayJagged.exe

1 1 2 1 2 3
```

the number of outer arrays is a .Length, a.[i] is the i'th array, the length of the i'th array is a .[i].Length, and the j'th element of the i'th array is thus a .[i].[j]. Often 2-dimensional rectangular arrays are used, which can be implemented as a jagged array, as shown in Listing 20.43. Note that the for-in cannot be used in pownArray, e.g.,

```
for row in arr do for elm in row do elm <- pown elm p done done,
```

Listing 20.43 arrayJaggedSquare.fsx: A rectangular array. let pownArray (arr : int array array) p = for i = 1 to arr.Length - 1 do for j = 1 to arr.[i].Length - 1 do arr.[i].[j] <- pown arr.[i].[j] p</pre> let printArrayOfArrays (arr : int array array) = for row in arr do for elm in row do printf "%3d " elm printf "\n" let A = [|[|1 ... 4|]; [|1 ... 2 ... 7|]; [|1 ... 3 ... 10|]|]pownArray A 2 printArrayOfArrays A \$ fsharpc --nologo arrayJaggedSquare.fsx && mono arrayJaggedSquare.exe 2 3 9 25 49 1 16 49 100

since the iterator value elm is not mutable, even though arr is an array.

Square arrays of dimensions 2 to 4 are so common that F# has built-in modules for their support. Here, we will describe <code>Array2D</code>. The workings of <code>Array3D</code> and <code>Array4D</code> are very similar. A generic <code>Array2D</code> has type 'T [,], and it is indexed also using the [,] notation. The <code>Array2D.length1</code> and <code>Array2D.length2</code> functions are supplied by the <code>Array2D</code> module for obtaining the size of an array along the first and second dimension. Rewriting the with jagged array example in Listing 20.43 to use <code>Array2D</code> gives a slightly simpler program, which is shown in Listing 20.44. Note that the <code>printf</code> supports direct printing of the 2-dimensional array. <code>Array2D</code>

```
Listing 20.44 array2D.fsx:

Creating a 3 by 4 rectangular array of integers.

1 let arr = Array2D.create 3 4 0
2 for i = 0 to (Array2D.length1 arr) - 1 do
3 for j = 0 to (Array2D.length2 arr) - 1 do
4 arr.[i,j] <- j * Array2D.length1 arr + i
5 printfn "%A" arr

1 $ fsharpc --nologo array2D.fsx && mono array2D.exe
2 [[0; 3; 6; 9]
3 [1; 4; 7; 10]
4 [2; 5; 8; 11]]
```

arrays support slicing. The "*" lexeme is particularly useful to obtain all values along a dimension. This is demonstrated in Listing 20.45. Note that in almost all

```
Listing 20.45: Examples of Array2D slicing. Compare with Listing 20.44.
> let arr = Array2D.init 3 4 (fun i j -> i + 10 * j);;
val arr : int [,] = [[0; 10; 20; 30]
                      [1; 11; 21; 31]
                      [2; 12; 22; 32]]
> arr.[2,3];;
val it : int = 32
> arr.[1..,3..];;
val it : int [,] = [[31]]
> arr.[..1,*];;
val it : int [,] = [[0; 10; 20; 30]
                     [1; 11; 21; 31]]
> arr.[1,*];;
val it : int [] = [|1; 11; 21; 31|]
> arr.[1..1,*];;
val it : int [,] = [[1; 11; 21; 31]]
```

cases, slicing produces a sub-rectangular 2 dimensional array, except for arr.[1,*], which is an array, as can be seen by the single "[". In contrast, A.[1..1,*] is an Array2D. Note also that printfn typesets 2 dimensional arrays as [[...]] and not [[[... |]]], which can cause confusion with lists of lists.

Multidimensional arrays have the same properties and methods as arrays, see Section 20.3.1.

20.4.1 The Array2D Module

There are quite a number of built-in procedures for arrays in the Array2D namespace, some of which are summarized below.

copy: arr:'T [,] -> 'T [,].

Creates a new array whose elements are copied from arr.

create: $m:int \rightarrow n:int \rightarrow v:'T \rightarrow 'T$ [,].

Creates an m by n array whose elements are set to v.

```
Listing 20.47: Array2D.create

1 > Array2D.create 2 3 3.14;;
2 val it : float [,] = [[3.14; 3.14; 3.14]
3 [3.14; 3.14; 3.14]]
```

init: m:int \rightarrow n:int \rightarrow f:(int \rightarrow int \rightarrow 'T) \rightarrow 'T [,].

Creates an m by n array whose elements are the result of applying f to the index of an element.

iter: f:('T -> unit) -> arr:'T [,] -> unit.

Applies f to each element of arr.

length1: arr:'T [,] -> int.

Returns the length the first dimension of arr.

```
Listing 20.50: Array2D.length1

1 > let arr = Array2D.create 2 3 0.0 in Array2D.length1
arr;;
2 val it : int = 2
```

length2: arr:'T [,] -> int.

Returns the length of the second dimension of arr.

```
Listing 20.51: Array2D.forall length2

1 > let arr = Array2D.create 2 3 0.0 in Array2D.length2
arr;;
2 val it : int = 3
```

```
map: f:('T -> 'U) -> arr:'T [,] -> 'U [,].
```

Creates a new array whose elements are the results of applying f to each of the elements of arr.

Chapter 21

While and For Loops

Non-recursive functions encapsulate code and allow for control of execution flow. That is, if a piece of code needs to be executed many times, then we can encapsulate it in the body of a function and call this function several times. In this chapter, we will look at more general control of flow via loops and conditional execution. Recursion is another mechanism for controlling flow, but this is deferred to Chapter 7.

Many programming constructs need to be repeated, and F# contains many structures for repetition. A *while*-loop has the following syntax:

```
Listing 21.1: While loop.

while <condition> do <expr> [done]
```

The *condition* < condition> is an expression that evaluates to true or false. A while-loop repeats the <expr> expression as long as the condition is true. Using lightweight syntax, the block following the *do* keyword up to and including the *done* keyword may be replaced by a newline and indentation.

The program in Listing 21.5 is an example of a while-loop which counts from 1 to 10. The variable i is customarily called the counter variable. The counting is

```
Listing 21.2 countWhile.fsx:

Count to 10 with a counter variable.

1 let mutable i = 1 in while i <= 10 do printf "%d " i; i <- i + 1 done;
2 printf "\n"

1 $ fsharpc --nologo countWhile.fsx && mono countWhile.exe
2 1 2 3 4 5 6 7 8 9 10
```

done by performing the following computation: In line 1, the counter variable is first

given an initial value of 1. Then execution enters the while-loop and examines the condition. Since $1 \le 10$, the condition is true, and execution enters the body of the loop. The body prints the value of the counter to the screen and increases the counter by 1. Then execution returns to the top of the while-loop. Now the condition is $2 \le 10$, which is also true, and so execution enters the body and so on until the counter has reached the value 11, in which case the condition $11 \le 10$ is false, and execution continues in line 2.

In lightweight syntax, this would be as shown in Listing 21.3. Notice that although the

```
Listing 21.3 countWhileLightweight.fsx:

Count to 10 with a counter variable using lightweight syntax.

1 let mutable i = 1
2 while i <= 10 do
3 printf "%d " i
4 i <- i + 1
5 printf "\n"

1 $ fsharpc --nologo countWhileLightweight.fsx && mono countWhileLightweight.exe
2 1 2 3 4 5 6 7 8 9 10
```

expression following the condition is preceded with a do keyword, and do <expr> is a do-binding, the keyword do is mandatory.

Counters are so common that a special syntax has been reserved for loops using counters. These are called *for-to*-loops. For-loops come in several variants, and here we will focus on the one using an explicit counter. Its syntax is:

```
Listing 21.4: For loop.

| for <ident> = <firstExpr> to <lastExpr> do <bodyExpr> [done]
```

A for-loop initially binds the counter identifier <ident> to be the value <firstExpr>. Then execution enters the body, and <bodyExpr> is evaluated. Once done, the counter is increased, and execution evaluates <bodyExpr> once again. This is repeated as long as the counter is not greater than <lastExpr>. As for while-loops, when using lightweight syntax the block following the *do* keyword up to and including the *done* keyword may be replaced by a newline and indentation.

The counting example from Listing 21.2 using a **for**-loop is shown in Listing 21.5 As this interactive script demonstrates, the identifier i takes all the values between 1 and 10, but in spite of its changing state, it is not mutable. Note also that the return value of the **for** expression is "()", like the printf functions. The lightweight equivalent is shown in Listing 21.6.

Listing 21.5 count.fsx: Counting from 1 to 10 using a -loop. 1 for i = 1 to 10 do printf "%d " i done 2 printfn "" 1 \$ fsharpc --nologo count.fsx && mono count.exe 2 1 2 3 4 5 6 7 8 9 10

```
Listing 21.6 countLightweight.fsx:

Counting from 1 to 10 using a -loop using the lightweight syntax.

for i = 1 to 10 do
   printf "%d " i
   printfn ""

$ fsharpc --nologo countLightweight.fsx && mono countLightweight.exe
2 1 2 3 4 5 6 7 8 9 10
```

Counting backwards is sufficiently common that F# has a *for-downto* structure, which works exactly like a *for-to-*loop except that the counter is decreased by 1 in each iteration. An example of this is shown in Listing 21.7.

```
Listing 21.7 countLightweightBackwards.fsx:

Counting from 10 to 1 using a - -loop using the lightweight syntax.

for i = 10 downto 1 do
   printf "%d " i
   printfn ""

1 $ fsharpc --nologo countLightweightBackwards.fsx && mono countLightweightBackwards.exe
2 10 9 8 7 6 5 4 3 2 1
```

To further compare for- and while-loops, consider the following problem.

```
Problem 21.1
rite a program that calculates the n'th Fibonacci number.
```

Fibonacci numbers is a sequence of numbers starting with 1, 1, and where the next number is calculated as the sum of the previous two. Hence the first ten numbers are: 1, 1, 2, 3, 5, 8, 13, 21, 34, 55. Fibonacci numbers are related to Golden spirals shown in Figure 21.1. Often the sequence is extended with a preceding number 0, to be $0, 1, 1, 2, 3, \ldots$, which we will do here as well.

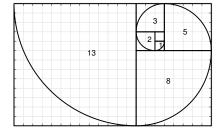


Fig. 21.1 The Fibonacci spiral is an approximation of the golden spiral. Each square has side lengths of successive Fibonacci numbers, and the curve in each square is the circular arc with a radius of the square it is drawn in.

We could solve this problem with a for-loop, as shown in Listing 21.8. The basic

```
Listing 21.8 fibFor.fsx:
The n'th Fibonacci number calculated using a for-loop.
let fib n =
   let mutable pair = (0, 1)
   for i = 2 to n do
     pair <- (snd pair, (fst pair) + (snd pair))</pre>
   snd pair
printfn "fib(1) = %d" (fib 1)
printfn "fib(2) = %d" (fib 2)
printfn "fib(3) = %d" (fib 3)
printfn "fib(10) = %d" (fib 10)
$ fsharpc --nologo fibFor.fsx && mono fibFor.exe
fib(1) = 1
fib(2) = 1
fib(3) = 2
fib(10) = 55
```

idea of the solution is that if we are given the (n-1)'th and (n-2)'th numbers, the n'th number is trivial to compute. And assuming that fib(1) and fib(2) are given, then it is trivial to calculate fib(3). For fib(4), we only need fib(3) and fib(2), hence we may disregard fib(1). Thus, we realize that we can cyclicly update the previous, current, and next values by shifting values until we have reached the desired fib(n). This is implement in Listing 21.8 as the function fib, which takes an integer n as argument and returns the n'th Fibonacci number. The function does this iteratively using a for-loop, where i is the counter value, and pair is the pair of the i-1'th and i'th Fibonacci numbers. In the body of the loop, the i'th and i+1'th numbers are assigned to pair. The for-loop automatically updates i for next iteration. When n < 2 the body of the for-loop is not evaluated, and 1 is returned. This is of course wrong for n < 1, but we will ignore this for now.

Listing 21.9 shows a program similar to Listing 21.8 using a while-loop instead of for-loop. The programs are almost identical. In this case, the for-loop is to

Listing 21.9 fibWhile.fsx: The *n*'th Fibonacci number calculated using a while-loop. let fib (n : int) : int = let mutable pair = (0, 1) let mutable i = 1while i < n do pair <- (snd pair, fst pair + snd pair)</pre> i < -i + 1snd pair printfn "fib(1) = %d" (fib 1) printfn "fib(2) = %d" (fib 2) printfn "fib(3) = %d" (fib 3) printfn "fib(10) = %d" (fib 10) \$ fsharpc --nologo fibWhile.fsx && mono fibWhile.exe fib(1) = 1fib(2) = 1fib(3) = 2fib(10) = 55

be preferred, since more lines of code typically mean more chances of making a mistake. However, while-loops are somewhat easier to argue correctness about.

The correctness of fib in Listing 21.9 can be proven using a *loop invariant*. An *invariant* is a statement that is always true at a particular point in a program, and a loop invariant is a statement which is true at the beginning and end of a loop. In line 4 in Listing 21.9, we may state the invariant: The variable pair is the pair of the i-1'th and i'th Fibonacci numbers. This is provable by induction:

Base case: Before entering the while loop, i is 1, pair is (0, 1). Thus, the invariant is true.

Induction step: Assuming that pair is the i-1'th and i'th Fibonacci numbers, the body first assigns a new value to pair as the i'th and i+1'th Fibonacci numbers, then increases i by one such that at the end of the loop the pair again contains the the i-1'th and i'th Fibonacci numbers.

Thus, since our invariant is true for the first case, and any iteration following an iteration where the invariant is true, is also true, then it is true for all iterations.

Thus we know that the second value in pair holds the value of the i'th Fibonacci number, and since we further may prove that i = n when line 7 is reached, then it is proven that fib returns the n'th Fibonacci number.

While-loops also allow for logical structures other than for-loops, such as the case when the number of iteration cannot easily be decided when entering the loop. As

an example, consider a slight variation of the above problem, where we wish to find the largest Fibonacci number less or equal some number. A solution to this problem is shown in Listing 21.10. The strategy here is to iteratively calculate Fibonacci

```
Listing 21.10 fibWhileLargest.fsx:
Search for the largest Fibonacci number less than a specified number.
let largestFibLeq n =
   let mutable pair = (0, 1)
   while snd pair <= n do</pre>
    pair <- (snd pair, fst pair + snd pair)</pre>
   fst pair
for i = 1 to 10 do
   printfn "largestFibLeq(%d) = %d" i (largestFibLeq i)
$ fsharpc --nologo fibWhileLargest.fsx && mono
    fibWhileLargest.exe
largestFibLeq(1) = 1
largestFibLeq(2) = 2
largestFibLeq(3) = 3
largestFibLeq(4) = 3
largestFibLeq(5) = 5
largestFibLeq(6) = 5
largestFibLeq(7) = 5
largestFibLeq(8) = 8
largestFibLeq(9) = 8
largestFibLeq(10) = 8
```

numbers until we've found one larger than the argument n, and then return the previous. This could not be calculated with a for-loop.

21.1 Programming Intermezzo: Automatic Conversion of Decimal to Binary Numbers

Using loops and conditional expressions, we are now able to solve the following problem:

Problem 21.2

iven an integer on decimal form, write its equivalent value on the binary form.

To solve this problem, consider odd numbers: They all have the property that the least significant bit is 1, e.g., $1_2 = 1,101_2 = 5$, in contrast to even numbers such as $110_2 = 6$. Division by 2 is equal to right-shifting by 1, e.g., $1_2/2 = 0.1_2 = 0.5, 101_2/2 = 10.1_2 = 2.5, 110_2/2 = 11_2 = 3$. Thus, through dividing by 2 and checking the remainder, we may sequentially read off the least significant bit. This leads to the algorithm shown in Listing 21.11. In the code, the states v and str are

Listing 21.11 dec2bin.fsx: Using integer division and remainder to write any positive integer in binary form. let dec2bin n = if n < 0 then "Illegal value" elif n = 0 then"0b0" else let mutable v = nlet mutable str = "" while v > 0 do $str \leftarrow (string (v \% 2)) + str$ v < -v / 2"0b" + strprintfn "%4d -> %s" -1 (dec2bin -1) printfn "%4d -> %s" 0 (dec2bin 0) for i = 0 to 3 do printfn "%4d -> %s" (pown 10 i) (dec2bin (pown 10 i)) \$ fsharpc --nologo dec2bin.fsx && mono dec2bin.exe -1 -> Illegal value $0 \rightarrow 0b0$ 1 -> 0b110 -> 0b1010 100 -> 0b1100100 1000 -> 0b1111101000

iteratively updated until str finally contains the desired solution.

To prove that Listing 21.11 calculates the correct sequence, we use induction. First we realize that for v < 1, the while-loop is skipped, and the result is trivially true. We will concentrate on line 9 in Listing 21.11 and will prove the following loop invariant: The string str contains all the bits of n to the right of the bit pattern remaining in variable v.

Base case n = 000...000x: If n only uses the lowest bit, then n = 0 or n = 1. If n = 0, then it is trivially correct. Considering the case n = 1: Before entering into the loop, v is 1, and v is the empty string, so the invariant is true. The condition of the while-loop is v 0, so execution enters the loop. Since integer division of 1 by 2 gives 0 with remainder 1, v is set to "1" and v to 0. Now we reexamine the while-loop's condition, v 0, which is false, so we exit the loop. At this point, v is 0 and v is "1", so all bits have been shifted from v to v 1, and none are left in v 1. Thus the invariant is true. Finally, the program returns "0b1".

Induction step: Consider the case of n > 1, and assume that the invariant is true when entering the loop, i.e., that m bits already have been shifted to str and that $n > 2^m$. In this case, v contains the remaining bits of n, which is the integer division $v = n / 2^*m$. Since $n > 2^m$, v is non-zero, and the loop conditions is true, so we enter the loop body. In the loop body we concatenate the rightmost bit of v to the left of str using v % 2, and right-shift v one bit to the right with v < -v / 2. Thus, when returning to the condition the invariant is true, since the right-most bit in v has been shifted to str. This continues until all bits have been shifted to str and v = 0, in which case the loop terminates, and "0b"+str is returned.

Thus we have proven that dec2bin correctly converts integers to strings representing binary numbers.

Chapter 22

The Imperative Programming paradigm

Imperative programming is a paradigm for programming states. In imperative programming, the focus is on how a problem is to be solved, as a list of *statements* that affects *states*. In F#, states are mutable and immutable values, and they are affected by functions and procedures. An imperative program is typically identified as using:

Mutable values

Mutable values are holders of states, they may change over time, and thus have a dynamic scope.

Procedures

Procedures are functions that returns "()", as opposed to functions that transform data. They are the embodiment of side-effects.

Side-effects

Side-effects are changes of state that are not reflected in the arguments and return values of a function. The printf is an example of a procedure that uses side-effects to communicate with the terminal.

Loops

The for- and while-loops typically use an iteration value to update some state, e.g., for-loops are often used to iterate through a list and summarize its contents.

Mono state or stateless programs, as *functional programming*, can be seen as a subset of imperative programming and is discussed in Chapter 10. *Object-oriented programming* is an extension of imperative programming, where statements and states are grouped into classes. For a discussion on object-oriented programming, see Chapter 25.

An imperative program is like a Turing machine, a theoretical machine introduced by Alan Turing in 1936 [10]. Almost all computer hardware is designed for *machine*

code, which is a common term used for many low-level computer programming languages, and almost all machine languages follow the imperative programming paradigm.

A prototypical example is a baking recipe, e.g., to make a loaf of bread, do the following:

- 1. Mix yeast with water.
- 2. Stir in salt, oil, and flour.
- 3. Knead until the dough has a smooth surface.
- 4. Let the dough rise until it has doubled its size.
- 5. Shape dough into a loaf.
- 6. Let the loaf rise until double size.
- 7. Bake in the oven until the bread is golden brown.

Each line in this example consists of one or more statements that are to be executed, and while executing them, states such as the size of the dough and the color of the bread changes. Some execution will halt execution until certain conditions of these states are fulfilled, e.g., the bread will not be put into the oven for baking before it has risen sufficiently.

22.1 Imperative Design

Programming is the act of solving a problem by writing a program to be executed on a computer. The imperative programming paradigm focuses on states. To solve a problem, you could work through the following list of actions:

- 1. Understand the problem. As Pólya described it, see Chapter 1, the first step in any solution is to understand the problem. A good trick to check whether you understand the problem, is to briefly describe it in your own words.
- 2. Identify the main values, variables, functions, and procedures needed. If the list of procedures is large, then you most likely should organize them in modules.

- 3. For each function and procedure, write a precise description of what it should do. This can conveniently be performed as an in-code comment for the procedure, using the F# XML documentation standard.
- 4. Make mockup functions and procedures using the intended types, but do not necessarily compute anything sensible. Run through examples in your mind, using this mockup program to identify any obvious oversights.
- 5. Write a suite of unit tests that tests the basic requirements for your code. The unit tests should be runnable with your mockup code. Writing unit tests will also allow you to evaluate the usefulness of the code pieces as seen from an application point of view.
- Replace the mockup functions in a prioritized order, i.e., write the must-have code before you write the nice-to-have code, while regularly running your unit tests to keep track of your progress.
- 7. Evaluate the code in relation to the desired goal, and reiterate earlier actions as needed until the task has been sufficiently completed.
- 8. Complete your documentation both in-code and outside to ensure that the intended user has sufficient knowledge to effectively use your program and to ensure that you or a fellow programmer will be able to maintain and extend the program in the future.

Chapter 23

Classes and Objects

Object-oriented programming is a programming paradigm that focuses on objects such as a persons, places, things, events, and concepts relevant for the problem.

Object-oriented programming has a rich language for describing objects and their relations, which can seem overwhelming at first, and they will be explained in detail in this and following chapters. Here is a brief overview: The main programming structures are called a *classes* and *objects*. It is useful to think of classes as user defined types and objects as values of such types. However, there is more to classes and objects than types and values. Objects may contain both data and code, and it is sometimes useful to draw the corresponding class definition as shown in Figure 23.1. In this illustration, objects of type aClass will each contain an int and a pair of a

```
aClass

// The object's values (properties)
aValue : int
anotherValue : float*bool

// The object's functions (methods)
aMethod: () -> int
anotherMethod: float -> float
```

Fig. 23.1 A class is sometimes drawn as a figure.

float and a boolean, and each object has two functions associated with them. The values stored in each object may differ, but the types are fixed by the class definition. It is common to call an object's values *properties* and an object's functions *methods*. In short, properties and methods are collectively called *members*. When an object is created, memory is set aside on *The Heap* to each object's property. Creating an object is commonly called *instantiation*. The members serve as the interface to each object, and each instantiated object will have the same type of members as all objects of that class, but their content may differ.

Object-oriented programming is an extension of data types, in the sense that objects contain both data and functions in a similar manner as a module, but object-oriented

programming emphasizes the semantic unity of the data and functions. Thus, objects are often *models* of real-world entities, and object-oriented programming leads to a particular style of programming analysis and design called *object-oriented analysis* and design to be discussed in Chapter 25.

23.1 Constructors and Members

A class is defined using the type keyword. Note that there are *always* parentheses after the class name to distinguish it from a regular type definition. The basic syntax for a class definition is as follows:

```
Listing 23.1: Syntax for simple class definitions.

type <classIdent> ({<arg>}) [as <selfIdent>]
{let <binding> | do <statement>}
{member <memberDef>}
```

The first line is the header of the class, where the <classIdent> is the name of the class, <arg> are its optional arguments, and <selfIdent> is an optional self identifier. The body of a class consists of the constructor and the member section. The header and the constructor section is often collectively called the *constructor*, and the body of the constructor consist of optional let-bindings and do-statements. Note that the do-statements in a class definition *must* use the do-keyword. The member section consisting of all the optional member definitions, where each definition use the member-keyword.

The header and constructor section is commonly called the *constructor*, and the constructor is executed at instantiation. In contrast to many other languages, the constructor is always stated as the initial code of a class definition. The values and variables in the constructor are called *fields*, while functions are just called *functions*.

Members are declared using the *member*-keyword, which defines values and functions that are accessible from outside the class using the "."-notation. In this manner, the members define the *interface* between the internal bindings in the constructor and an application program. Member values are called *properties*, and member functions are called *methods*. Note that members are immutable. The body of a member has access to the arguments, the constructor's bindings, and to all class members, regardless of the member's lexicographical order. In contrast, members are not available in the constructor unless the self identifier has been declared in the header using the keyword *as*, e.g., type classMutable(name: string) as this =

Consider the example in Figure 23.2. Here we have defined a class car, instantiated three objects, and bound them to the names sportsCar, stationWagon, and

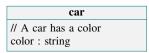




Fig. 23.2 A class car is instantiated trice and bound to the names sportsCar, stationWagon, and miniBus, and each object's properties are set to different values.

miniBus. Each object has been given different values for the color property. In F# this could look like the code in Listing 23.2. In the example, the class car is

```
Listing 23.2 car.fsx:

Defining a class car, and making three instances of it. See also Figure 23.2.

type car (aColor: string) =
// Member section
member this.color = aColor

let sportsCar = car ("red")
let stationWagon = car ("green")
let miniBus = car ("blue")
printfn "%s %s %s" sportsCar.color stationWagon.color
miniBus.color

f sharpc --nologo car.fsx && mono car.exe
red green blue
```

defined in lines 1–3. Its header includes one string argument, aColor. The body of the constructor is empty, and the member section consists of lines 2-3. The class defines one property color: string. Note that when referring to a member inside an object, then we must use a self identifier. Here we use this as the self identifier, and as the example shows, we need not declare it in the class' header. A self identifier refers to the memory set aside to the particular instance of an object. It is common among other programming languages to use this as self identifier. F# is very flexible regarding what name can be used for the self-identifier, and the member section could as well have been self.value, __.value, or anything else, and it need not be the same in every member definition. Nevertheless, **consistency** in the name used as self-identifier is strongly encouraged, preferably using a name that reflects the nature of the reference, such as this or me. The objects are instantiated in lines 5–7, and the value of their properties are accessed in line 8. In many languages, objects are instantiated using the *new* keyword, but in F# this is optional. I.e., let sportsCar = car ("red") is identical to let sportsCar = new car ("red"). Note that both the self identifier and member access uses the "." notation.

A more advanced implementation of a car class might include notions of a fuel gauge, fuel economy, and the ability to update the fuel gauge as the car is driven. An example of an implementation of this is given In Listing 23.3. Here in line 1,

```
Listing 23.3 class.fsx:
Extending Listing 23.2 with fields and methods.
 type car (econ : float, fuel : float) =
   // Constructor body section
   let mutable fuelLeft = fuel // liters in the tank
   do printfn "Created a car (%.1f, %.1f)" econ fuel
   // Member section
  member this.fuel = fuelLeft
  member this.drive distance =
     fuelLeft <- fuelLeft - econ * distance / 100.0</pre>
let sport = car (8.0, 60.0)
 let economy = car (5.0, 45.0)
sport.drive 100.0
economy.drive 100.0
printfn "Fuel left after 100km driving:"
printfn " sport: %.1f" sport.fuel
printfn " economy: %.1f" economy.fuel
$ fsharpc --nologo class.fsx && mono class.exe
Created a car (8.0, 60.0)
Created a car (5.0, 45.0)
Fuel left after 100km driving:
  sport: 52.0
  economy: 40.0
```

the constructor has 2 arguments: the fuel economy parameter and the initial amount of fuel in the tank. Thus, we are able to create 2 different cars with different fuel economy, as shown in lines 10–11. The amount of fuel left en each car object is stored in the mutable field fuelLeft. This is an example of a state of an object: It can be accessed outside the object by the fuel property, and it can be updated by the drive method.

Field names and functions defined in the constructor do not use the self identifier and cannot be accessed outside and object using the "." notation. However, they are available in both the constructor and the member section following the regular scope rules. Fields are a common way to hide implementation details, and they are *private* to the object or class in contrast to members that are *public*.

275 23.2 *Accessors*

23.2 Accessors

Methods are most often used as an interface between the fields of an object and the application program. Consider the example in Listing 23.4. In the example, the

```
Listing 23.4 classAccessor.fsx:
Accessor methods interface with internal bindings.

1 type aClass () =
2   let mutable v = 1
3   member this.setValue (newValue : int) : unit =
4   v <- newValue
5   member this.getValue () : int = v

6   let a = aClass ()
8   printfn "%d" (a.getValue ())
9   a.setValue (2)
10   printfn "%d" (a.getValue ())

1 $ fsharpc --nologo classAccessor.fsx && mono classAccessor.exe
2   1
3   2
```

data contained in objects of type aClass is stored in the mutable field v. Since only members can be accessed from an application, it is not possible to retrieve or change the data of these object of class aClass directly. We could have programmed v as a member instead, i.e., member this.v = 1, however, often we are in a situation, where there is a range of possible choices of data representation, details of which we do wish to share with an application program. E.g., implementation details of arrays are not important for our ability to use them in applications. What matters is that the members that work on the array elements are well defined and efficient. Thus, the example demonstrates how we can build two simple methods setValue and getValue to set and get the data stored v. By making a distinction between the internal representation and how members give access to the data, we retain the possibility to change the internal representation without having to reprogram all the application programs. Analogously, we can change the engine in a car from one type to another without having to change the car's interaction with the driver and the road: steering wheel, pedals, wheels etc.

Such functions are called *accessors*. Internal states with setters and getters are a typical construction, since they allow for complicated computations when states are read to and written from, and gives the designer of the class the freedom to change the internal representation while keeping the interface the same. Accessors are so common that F# includes a special syntax for them: Classes can be made to act like variables using member...with...and keywords and the special function bindings get() and set(), as demonstrated in Listing 23.5. The expression defining

Listing 23.5 classGetSet.fsx: Members can act as variables with the built-in get and set functions. 1 type aClass () = 2 let mutable v = 0 3 member this.value 4 with get () = v 5 and set (a) = v <- a 6 7 let a = aClass () 8 printfn "%d" a.value 9 a.value<-2 10 printfn "%d" a.value 1 \$ fsharpc --nologo classGetSet.fsx && mono classGetSet.exe 2 0 3 2

get: () -> 'a and set: 'a -> (), where 'a is any type, can be any usual expression. The application calls the get and set as if the property were a mutable value. If set is omitted, then the property acts as a value rather than a variable, and values cannot be assigned to it in the application program.

Setters and getters are so common that F# has a short-hand for this using member val value = 0 with get, set, which creates the internal mutable value value, but this is discouraged in this text.

Defining an *Item* property with extended get and set makes objects act as indexed variables, as demonstrated in Listing 23.6. Higher dimensional indexed properties are defined by adding more indexing arguments to the definition of get and set, such as demonstrated in Listing 23.7.

277 23.2 *Accessors*

Listing 23.6 classGetSetIndexed.fsx: Properties can act as indexed variables with the built-in get and set functions. type aClass (size : int) = let arr = Array.create<int> size 0 member this.Item with get (ind : int) = arr.[ind] and set (ind : int) (p : int) = arr.[ind] <- p</pre> let a = aClass (3)printfn "%A" a printfn "%d %d %d" a.[0] a.[1] a.[2] a.[1] < -3printfn "%d %d %d" a.[0] a.[1] a.[2] \$ fsharpc --nologo classGetSetIndexed.fsx && mono classGetSetIndexed.exe ClassGetSetIndexed+aClass 0 0 0 0 3 0

```
Listing 23.7 classGetSetHigherIndexed.fsx:
Getters and setters for higher dimensional index variables.
type aClass (rows : int, cols : int) =
  let arr = Array2D.create<int> rows cols 0
  member this.Item
    with get (i : int, j : int) = arr.[i,j]
     and set (i : int, j : int) (p : int) = arr.[i,j] <- p
let a = aClass(3, 3)
printfn "%A" a
printfn "%d %d %d" a.[0,0] a.[0,1] a.[2,1]
a.[0,1] < -3
printfn "%d %d %d" a.[0,0] a.[0,1] a.[2,1]
$ fsharpc --nologo classGetSetHigherIndexed.fsx && mono
    classGetSetHigherIndexed.exe
{\tt ClassGetSetHigherIndexed+aClass}
0 0 0
0 3 0
```

23.3 Objects are Reference Types

Objects are reference type values, implying that copying objects copies their references, not their values, and their content is stored on *The Heap*, see Section 20.2. Consider the example in Listing 23.8. Thus, the binding to b in line 6 is an alias to a, not a copy, and changing object a also changes b! This is a common cause of error, and you should **think of objects as arrays.** For this reason, it is often seen that classes implement a copy function returning a new object with copied values, as shown in Listing 23.9. In the example, we see that since b now is a copy, we do not change it by changing a. This is called a *copy constructor*.

```
Listing 23.8 classReference.fsx:

Objects assignment can cause aliasing.

type aClass () =
let mutable v = 0
member this.value with get () = v and set (a) = v <- a

let a = aClass ()
let b = a
a.value <- 2
printfn "%d %d" a.value b.value

fightharpc --nologo classReference.fsx && mono classReference.exe
2 2 2
```

```
Listing 23.9 classCopy.fsx:
A copy method is often needed. Compare with Listing 23.8.

type aClass () =
let mutable v = 0
member this.value with get () = v and set (a) = v <- a
member this.copy () =
let o = aClass ()
o.value <- v
o
let a = aClass ()
let b = a.copy ()
a.value <-2
printfn "%d %d" a.value b.value

f sharpc --nologo classCopy.fsx && mono classCopy.exe
2 2 0
```

279 23.4 Static Classes

23.4 Static Classes

Classes can act as modules and hold data which is identical for all objects of its type. These are defined using the *static*-keyword. And since they do not belong to a single object, but are shared between all objects, they are defined without the self-identifier and accessed using the class name, and they cannot refer to the arguments of the constructor. For example, consider a class whose objects each hold a unique identification number (id): When an object is instantiated, the object must be given the next available identification number. The next available id could be given as an argument to the constructor, however, this delegates the task of maintaining the uniqueness of ids to the application program. It is better to use a static field and delegate the administration of ids completely to the constructors, as demonstrated in Listing 23.10. Notice in line 2 that a static field nextAvailableID is created for the

```
Listing 23.10 classStatic.fsx:
Static fields and members are identical to all objects of the type.
type student (name : string) =
   static let mutable nextAvailableID = 0 // A global id for
    all objects
   let studentID = nextAvailableID // A per object id
   do nextAvailableID <- nextAvailableID + 1</pre>
   member this.id with get () = studentID
   member this.name = name
   static member nextID = nextAvailableID // A global member
let a = student ("Jon") // Students will get unique ids, when
    instantiated
let b = student ("Hans")
printfn "%s: %d, %s: %d" a.name a.id b.name b.id
 printfn "Next id: %d" student.nextID // Accessing the class's
    member
$ fsharpc --nologo classStatic.fsx && mono classStatic.exe
Jon: 0, Hans: 1
 Next id: 2
```

value to be shared by all objects. The initialization of its value is only performed once, at the beginning of program execution. However, every time an object is instantiated, the value of nextAvailableID is copied to the object's field studentID in line 3, and nextAvailableID is updated. The static field can be accessed with a static accessor, as demonstrated in line 7. Notice how this definition does not include a self-identifier, and that the member is accessible from the application in line 11 using the class' name, in both cases since it is not a member of any particular object.

23.5 Recursive Members and Classes

The members of a class are inherently recursive: static and non-static methods may recurse using the self identifier and other members regardless of their lexicographical scope. This is demonstrated in Listing 23.11. For mutually recursive classes, the

```
Listing 23.11 classRecursion.fsx:

Members can recurse without the keyword and refer to other members regardless of their lexicographical scope.

1 type twice (v : int) =
2 static member fac n = if n > 1 then n * (twice.fac (n-1)) else 1 // No rec
3 member this.copy = this.twice // No lexicographical scope member this.twice = 2*v

5 let a = twice (2)
7 let b = twice.fac 3
8 printfn "%A %A %A" a.copy a.twice b

1 $ fsharpc --nologo classRecursion.fsx && mono classRecursion.exe
2 4 4 6
```

keyword and must be used, as shown in Listing 23.12. Here anInt and aFloat

```
Listing 23.12 classAssymetry.fsx:
Mutually recursive classes are defined using the
                                             keyword.
 type anInt (v : int) =
  member this.value = v
   member this.add (w : aFloat) : aFloat = aFloat ((float
    this.value) + w.value)
and aFloat (w : float) =
  member this.value = w
  member this.add (v : anInt) : aFloat = aFloat ((float
    v.value) + this.value)
let a = anInt (2)
let b = aFloat (3.2)
let c = a.add b
let d = b.add a
printfn "%A %A %A %A" a.value b.value c.value d.value
$ fsharpc --nologo classAssymetry.fsx && mono
    classAssymetry.exe
2 3.2 5.2 5.2
```

hold an integer and a floating point value respectively, and they both implement

an addition of anInt an aFloat that returns and aFloat. Thus, they are mutually dependent and must be defined in the same type definition using and.

23.6 Function and Operator Overloading

It is often convenient to define different methods that have the same name, but with functionalities that depend on the number and type of arguments given. This is called *overloading*, and F# supports method overloading. An example is shown in Listing 23.13. In the example we define an object which can produce greetings

```
Listing 23.13 classOverload.fsx:
Overloading methods set: int -> () and set: int * int -> () is
permitted, since they differ in argument number or type.
type Greetings () =
  let mutable greetings = "Hi"
  let mutable name = "Programmer"
  member this.str = greetings + " " + name
  member this.setName (newName : string) : unit =
    name <- newName
  member this.setName (newName : string, newGreetings :
   string) : unit =
    greetings <- newGreetings
    name <- newName
let a = Greetings ()
printfn "%s" a.str
a.setName ("F# programmer")
printfn "%s" a.str
a.setName ("Expert", "Hello")
printfn "%s" a.str
$ fsharpc --nologo classOverload.fsx && mono classOverload.exe
Hi Programmer
Hi F# programmer
Hello Expert
```

strings of the form <greeting> <name>, using the str member. It has a default greeting "Hi" and name "Programmer", but the name can be changed by calling the setName accessor with one argument, and both greeting and name can be changed by calling the overloaded setName with two arguments. Overloading in class definition is allowed as long as the arguments differ in number or type.

In Listing 23.12, the notation for addition is less than elegant. For such situations, F# supports *operator overloading*. All usual operators may be overloaded (see Section 4.3), and in contrast to regular operator overloading, the compiler uses type

inference to decide which function is to be called. All operators have a functional equivalence, and to overload the binary "+" and unary "-" operators, we overload their functional equivalence (+) and (\sim -) as static members. This is demonstrated in Listing 23.14. Thus, writing v + w is equivalent to writing anInt.(+) (v, w).

Listing 23.14 classOverloadOperator.fsx: Operators can be overloaded using their functional equivalents. type anInt (v : int) = member this.value = v static member (+) (v : anInt, w : anInt) = anInt (v.value + w.value) static member (~-) (v : anInt) = anInt (-v.value) and aFloat (w : float) = member this.value = w static member (+) (v : aFloat, w : aFloat) = aFloat (v.value + w.value) static member (+) (v : anInt, w : aFloat) = aFloat ((float v.value) + w.value) static member (+) (w : aFloat, v : anInt) = v + w // reuse def. above static member (~-) (v : aFloat) = aFloat (-v.value) let a = anInt (2)let b = anInt (3)let c = aFloat (3.2)let d = a + b // anInt + anIntlet e = c + a // aFloat + anIntlet f = a + c // anInt + aFloatlet g = -a // unitary minus anInt let h = a + -b // anInt + unitary minus anIntprintf "a=%A, b=%A, c=%A, d=%A" a.value b.value c.value d.value printf ", e=%A, f=%A, g=%A, h=%A" e.value f.value g.value h.value \$ fsharpc --nologo classOverloadOperator.fsx && mono classOverloadOperator.exe a=2, b=3, c=3.2, d=5, e=5.2, f=5.2, g=-2, h=-1

Presently, the former is to be preferred, but at times, e.g., when using functions as arguments, it is useful to be able to refer to an operator by its function-equivalent. Note that the functional equivalence of the multiplication operator (*) shares a prefix with the begin block comment lexeme "(*", which is why the multiplication function is written as (*). Note also that unitary operators have a special notation using the "~"-lexeme, as illustrated in the above example for unitary minus. With the unitary minus, we are able to subtract objects of anInt by first negating the right-hand operand and then adding the result to the left-hand operand. In contrast, the binary minus would have been defined as static member (-) (v : anInt, w : aFloat) = anInt ((float v.value) - w.value).

In Listing 23.14, notice how the second (+) operator overloads the first by calling the first with the proper order of arguments. This is a general principle: **avoid duplication of code, reuse of existing code is almost always preferred.** Here it is to be preferred for two reasons. Firstly, if we discover a mistake in the multiplication code, then we need only correct it once, which implies that both multiplication methods are corrected once and reduces the chance of introducing new mistakes by attempting to correct old ones. Secondly, if we later decide to change the internal representation, then we only need to update one version of the multiplication function, hence we reduce programming time and risk of errors as well.

Beware that operator overloading outside class definitions overwrites *all* definitions of the operator. E.g., overloading (+) (v, w) outside a class will influence integer, real, string, etc. Thus, **operator overloading should only be done inside class** \star **definitions.**

23.7 Additional Constructors

Like methods, constructors can also be overloaded by using the *new* keyword. E.g., the example in Listing 23.13 may be modified, such that the name and possibly greeting is set at object instantiation rather than by using the accessor. This is illustrated in Listing 23.15. The top constructor that does not use the *new*-keyword is called the *pri*-

```
Listing 23.15 classExtraConstructor.fsx:
Extra constructors can be added, using
type classExtraConstructor (name : string, greetings :
   string) =
  static let defaultGreetings = "Hello"
 // Additional constructors are defined by new ()
  new (name : string) =
    classExtraConstructor (name, defaultGreetings)
  member this.name = name
  member this.str = greetings + " " + name
let s = classExtraConstructor ("F#") // Calling additional
   constructor
let t = classExtraConstructor ("F#", "Hi") // Calling primary
   constructor
printfn "%A, %A" s.str t.str
$ fsharpc --nologo classExtraConstructor.fsx && mono
    classExtraConstructor.exe
"Hello F#", "Hi F#"
```

mary constructor. The body of the additional constructor must call the primary constructor, and the body cannot extend the primary constructor's fields and functions. It is useful to think of the primary constructor as a superset of arguments and the additional ones as subsets or specializations. As regular scope rules dictate, the additional constructor has access to the primary constructor's bindings. However, in order to access the object's members, the self identifier has to be explicitly declared, using the as-keyword in the header. E.g., writing new(x : float, y : float) as alsoThis = However beware. Even though the body of the additional constructor now may access the property alsoThis.x, this value has first been created once the primary constructor has been called. E.g., calling the primary constructor in the additional constructor as new(x : float, y : float) as alsoThis = classExtraConstructor(fst alsoThis.x, y, defaultSeparator) will result in an exception at runtime. Code may be executed in additional constructors: Before the call to the primary constructor, let and do statements are allowed. If code is to be executed after the primary constructor has been called, then it must be preceded by the then keyword, as shown in Listing 23.16. The do-keyword is often understood to be implied by F#, e.g., in front of all printf-statements, but in the above examples they are required where used. This may change in future releases of F#. F# allows for many additional constructors, but they must be distinguishable by type.

Listing 23.16 classDoThen.fsx:

The optional —- and ——-keywords allow for computations before and after the primary constructor is called.

```
type classDoThen (aValue : float) =
 // "do" is mandatory to execute code in the primary
   constructor
  do printfn " Primary constructor called"
  // Some calculations
  do printfn " Primary done" (* *)
  new() =
    // "do" is optional in additional constructors \,
    printfn " Additional constructor called"
    classDoThen (0.0)
    // Use "then" to execute code after construction
    then
      printfn " Additional done"
  member this.value = aValue
printfn "Calling additional constructor"
let v = classDoThen ()
printfn "Calling primary constructor"
let w = classDoThen (1.0)
$ fsharpc --nologo classDoThen.fsx && mono classDoThen.exe
Calling additional constructor
  Additional constructor called
  Primary constructor called
  Primary done
  Additional done
Calling primary constructor
  Primary constructor called
  Primary done
```

23.8 Programming Intermezzo: Two Dimensional Vectors

Consider the following problem.

Problem 23.1

Euclidean vector is a geometric object that has a direction, a length, and two operations: vector addition and scalar multiplication, see Figure 23.3. Define a class for a vector in two dimensions.

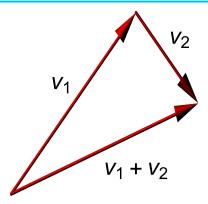


Fig. 23.3 Illustration of vector addition in two dimensions.

An essential part in designing a solution for the above problem is to decide which representation to use internally for vectors. The Cartesian representation of a vector is as a tuple of real values (x, y), where x and y are real values, and where we can imagine that the tail of the vector is in the origin, and its tip is at the coordinate (x, y). For vectors on Cartesian form,

$$\mathbf{v} = (x, y),\tag{23.1}$$

the basic operations are defined as

$$\mathbf{v}_1 + \mathbf{v}_2 = (x_1 + x_2, y_1 + y_2), \tag{23.2}$$

$$a\mathbf{v} = (ax, ax),\tag{23.3}$$

$$\operatorname{dir}(\mathbf{v}) = \tan \frac{y}{x}, \ x \neq 0, \tag{23.4}$$

$$len(\mathbf{v}) = \sqrt{x^2 + y^2},\tag{23.5}$$

where x_i and y_i are the elements of vector \mathbf{v}_i , a is a scalar, and dir and len are the direction and length functions, respectively. The polar representation of vectors is also a tuple of real values (θ, l) , where θ is the vector's angle from the x-axis and l is the vector's length. This representation is closely tied to the definition of a vector, and has the constraint that $0 \le \theta < 2\pi$ and $0 \le l$. This representation reminds us

that vectors do not have a position. For vectors on polar form,

$$\mathbf{v} = (\theta, l),\tag{23.6}$$

their basic operations are defined as

$$x(\theta, l) = l\cos(\theta),\tag{23.7}$$

$$y(\theta, l) = l\sin(\theta),\tag{23.8}$$

$$\mathbf{v}_1 + \mathbf{v}_2 = (x(\theta_1, l_1) + x(\theta_2, l_2), y(\theta_1, l_1) + y(\theta_2, l_2))$$
(23.9)

$$a\mathbf{v} = (\theta, al),\tag{23.10}$$

where θ_i and l_i are the elements of vector \mathbf{v}_i , a is a scalar, and x and y are the Cartesian coordinate functions.

So far in our analysis, we have realized that:

- both the Cartesian and polar representations use a pair of reals to represent the vector.
- both require functions to calculate the elements of the other representation,
- the polar representation is invalid for negative lengths, and
- the addition operator under the polar representation is also more complicated and essentially requires access to the Cartesian representation.

The first step in shaping our solution is to decide on file structure: For conceptual separation, we choose to use a library and an application file. F# wants files to define namespaces or modules, so we choose the library to be a Geometry module, which implements the vector class to be called vector. Furthermore, when creating vector objects we would like to give the application program the ability to choose either Cartesian or polar form. This is can be done using discriminated unions. Discriminated unions allow us to tag values of possibly identical form, but they also lead to longer programs. Thus, we will also provide an additional constructor on implicit Cartesian form, since this is the most common representation of vectors.

A key point when defining libraries is to consider their interface with the application program. Hence, our second step is to write an application using the yet to be written library in order to get a feel for how such an interface could be. This is demonstrated in the application program Listing 23.17. The application of the vector class seems natural, makes use of the optional discriminated unions, uses the infix operators "+" and "*" in a manner close to standard arithmetic, and interacts smoothly with the printf family. Thus, we have further sketched requirements to the library with the emphasis on application.

Listing 23.17 vectorApp.fsx: An application using the library in Listing 23.18. open Geometry let v = vector(Cartesian (1.0,2.0)) let w = vector(Polar (3.2,1.8)) let p = vector() let q = vector(1.2, -0.9) let a = 1.5 printfn "%A * %A = %A" a v (a * v) printfn "%A + %A = %A" v w (v + w) printfn "vector() = %A" p printfn "vector(1.2, -0.9) = %A" q printfn "v.dir = %A" v.dir printfn "v.len = %A" v.len

After a couple of trials, our library implementation has ended up as shown in Listing 23.18. Realizations achieved during writing this code are: Firstly, in order to implement a vector class using discriminated unions, we had to introduce a constructor with helper variables _x, _y, etc. The consequence is that the Cartesian and polar representation is evaluated once and only once every time an object is created. Unfortunately, discriminated unions do not implement guards on subsets, so we still have to cast an exception when the application attempts to create an object with a negative length. Secondly, for the ToString override we have implemented static members for typesetting vectors, since it seems more appropriate that all vectors should be typeset identically. Changing typesetting thus respects dynamic scope.

The output of our combined library and application is shown in Listing 23.19. The output is as expected, and for the vector class, our solution seems to be a good compromise between versatility and syntactical bloating.

Listing 23.18 vector.fs: A library serving the application in Listing 23.19. module Geometry type Coordinate = Cartesian of float * float // (x, y) | Polar of float * float // (dir, len) type vector(c : Coordinate) = let (_x, _y, _dir, _len) = match c with Cartesian (x, y) -> (x, y, atan2 y x, sqrt (x * x + y * y))| Polar (dir, len) when len >= 0.0 ->(len * cos dir, len * sin dir, dir, len) | Polar (dir, _) -> failwith "Negative length in polar representation." new(x : float, y : float) = vector(Cartesian (x, y)) new() =vector(Cartesian (0.0, 0.0)) $member this.x = _x$ $member this.y = _y$ member this.len = _len member this.dir = _dir static member val left = "(" with get, set static member val right = ")" with get, set static member val sep = ", " with get, set static member (*) (a : float, v : vector) : vector = vector(Polar (v.dir, a * v.len)) static member (*) (v : vector, a : float) : vector = a * v static member (+) (v : vector, w : vector) : vector = vector(Cartesian (v.x + w.x, v.y + w.y)) override this.ToString() = ${\tt sprintf~"\%s\%A\%s\%A\%s"~vector.left~this.x~vector.sep~this.y}$ vector.right

Listing 23.19: Compiling and running the code from Listing 23.18 and 23.17.

Chapter 24

Derived Classes

24.1 Inheritance

Sometimes it is useful to derive new classes from old ones in order to reuse code or to emphasize a program structure. For example, consider the concepts of a *car* and *bicycle*. They are both *vehicles* that can move forward and turn, but a car can move in reverse, has 4 wheels, and uses gasoline or electricity, while a bicycle has 2 wheels and needs to be pedaled. Structurally, we can say that "a car is a vehicle" and "a bicycle is a vehicle". Such a relation is sometimes drawn as a tree as shown in Figure 24.1 and is called an *is-a relation*. Is-a relations can be implemented using

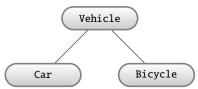


Fig. 24.1 Both a car and a bicycle is a (type of) vehicle.

class *inheritance*, where vehicle is called the *base class*, and car and bicycle are each a *derived class*. The advantage is that a derived class can inherent the members of the base class, *override*, and possibly add new members. Another advantage is that objects from derived classes can be made to look like as if they were objects of the base class while still containing all their data. Such mascarading is useful when, for example, listing cars and bicycles in the same list.

In F#, inheritance is indicated using the inherit keyword in the class definition. An extensions of the syntax in Listing 24.1 is:

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```
Listing 24.1: A class definition with inheritance.

type <classIdent> ({<arg>}) [as <selfIdent>]
[inherit <baseClassIdent>({<arg>})]
{[let <binding>] | [do <statement>]}
{(member | abstract member | default | override)
<memberDef>}
```

New syntactical elements are: the inherit keyword, which indicates that this is a derived class and where <baseClassIdent> is the name of the base class. Further, members may be regular members using the member keyword as discussed in the previous chapter, and members can also be other types, as indicated by the keywords: abstract member, default, and override.

An example of defining base and derived classes for vehicles is shown In Listing 24.2. In the example, a simple base class vehicle is defined to include wheels as its

```
Listing 24.2 vehicle.fsx:
New classes can be derived from old ones.
/// All vehicles have wheels
type vehicle (nWheels : int ) =
  member this.wheels = nWheels
/// A car is a vehicle with 4 wheels
type car (nPassengers : int) =
  inherit vehicle (4)
  member this.maxPassengers = nPassengers
/// A bicycle is a vehicle with 2 wheels
type bicycle () =
  inherit vehicle (2)
  member this.mustUseHelmet = true
let aVehicle = vehicle (1)
let aCar = car (4)
let aBike = bicycle ()
printfn "aVehicle has %d wheel(s)" aVehicle.wheels
printfn "aCar has %d wheel(s) with room for %d passenger(s)"
   aCar.wheels aCar.maxPassengers
printfn "aBike has %d wheel(s). Is helmet required? %b"
   aBike.wheels aBike.mustUseHelmet
$ fsharpc --nologo vehicle.fsx && mono vehicle.exe
aVehicle has 1 wheel(s)
aCar has 4 wheel(s) with room for 4 passenger(s)
aBike has 2 wheel(s). Is helmet required? true
```

single member. The derived classes inherit all the members of the base class, but do not have access to any non-members of the base constructor. I.e., car and bicycle

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automatically have the wheels property. Both derived classes additional members maxPassengers and mustUseHelmet, respectively.

Derived classes can replace base class members by defining new members *over-shadow* the base members. The base members are still available through the *base-*keyword. Consider the example in the Listing 24.3. In this case, we have defined three

Listing 24.3 memberOvershadowingVar.fsx: Inherited members can be overshadowed, but we can still access the base member. Compare with Listing 24.7. /// hi is a greeting type greeting () = member this.str = "hi" /// hello is a greeting type hello () = inherit greeting () member this.str = "hello" /// howdy is a greeting type howdy () = inherit greeting () member this.str = "howdy" let a = greeting () let b = hello () let c = howdy ()printfn "%s, %s, %s" a.str b.str c.str \$ fsharpc --nologo memberOvershadowingVar.fsx && mono memberOvershadowingVar.exe hi, hello, howdy

greetings: greeting, hello, and howdy. The two later inherit member this.str = "hi" from greeting, but since they both also define a member property str, these overshadow the one from greeting. In hello and howdy the base value of str is available as base.str.

Even though derived classes are different from their base, the derived class includes the base class, which can be recalled using *upcasting* by the upcast operator ":>". At compile-time, this operator removes the additions and overshadowing of the derived class, as illustrated in Listing 24.4. Here howdy is derived from hello, overshadows str, and adds property altStr. By upcasting object b, we create object c as a copy of b with all its fields, functions, and members, as if it had been of type hello. I.e., c contains the base class version of str and does not have property altStr. Objects a and c are now of same type and can be put into, e.g., an array as let arr = [|a, c|]. Previously upcasted objects can also be downcasted again using the *downcast* operator :?>, but the validity of the operation is checked at runtime. Thus, avoid downcasting when possible.

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Listing 24.4 upCasting.fsx:

Objects can be upcasted resulting in an object to appear to be of the base type. Implementations from the derived class are ignored.

```
/// hello holds property str
type hello () =
member this.str = "hello"
/// howdy is a hello class and has property altStr
type howdy () =
inherit hello ()
member this.str = "howdy"
member this.altStr = "hi"

let a = hello ()
let b = howdy ()
let c = b :> hello // a howdy object as if it were a hello object
printfn "%s %s %s %s" a.str b.str b.altStr c.str

$ fsharpc --nologo upCasting.fsx && mono upCasting.exe
hello howdy hi hello
```

24.2 Interfacing with the printf Family

In previous examples, we accessed the property in order to print the contents of objects. Luckily, a more elegant solution is available. Objects can be printed directly, but the result is most often not very useful, as can be seen in Listing 24.5. All classes

```
Listing 24.5 classPrintf.fsx:
Printing classes yields low-level information about the class.

1 type vectorDefaultToString (x : float, y : float) =
2 member this.x = (x,y)

3 let v = vectorDefaultToString (1.0, 2.0)
5 printfn "%A" v // Printing objects gives low-level
information

1 $ fsharpc --nologo classPrintf.fsx && mono classPrintf.exe
2 ClassPrintf+vectorDefaultToString
```

implicitely inherit from a class with the peculiar name, <code>System.Object</code>, and as a consequence, all classes have a number of already defined members. One example is the <code>ToString()</code>: () -> string function, which is useful in conjunction with, e.g., <code>printf</code>. When an object is given as argument to a <code>printf</code> function with the %A or %O placeholders in the formatting string, <code>printf</code> calls the object's <code>ToString()</code> function. The default implementation returns low-level information about the object, as can be seen above, but we may <code>override</code> this member using the <code>override</code>-keyword, as demonstrated in Listing 24.6. Note, despite that <code>ToString()</code> returns a string, the %s placerholder only accepts values of the basic <code>string</code> type. We see

```
Listing 24.6 classToString.fsx:

Overriding ToString() function for better interaction with members of the printf family of procedures. Compare with Listing 24.5.

type vectorWToString (x : float, y : float) = member this.x = (x,y)

// Custom printing of objects by overriding this.ToString() override this.ToString() = sprintf "(%A, %A)" (fst this.x) (snd this.x)

let v = vectorWToString(1.0, 2.0)

printfn "%A" v // No change in application but result is better

$ fsharpc --nologo classToString.fsx && mono classToString.exe (1.0, 2.0)
```

that as a consequence, the printf statement is much simpler. However beware, an

application program may require other formatting choices than selected at the time of designing the class, e.g., in our example, the application program may prefer square brackets as delimiters for vector tuples. So in general when designing an override to ToString(), choose simple, generic formatting for the widest possible use.

The most generic formatting is not always obvious, and in the vector case some candidates for the formatting string of ToString() are "%A %A", "%A, %A", "(%A, %A)", and "[%A, %A]". Considering each carefully, it seems that arguments can be made against all them. A common choice is to let the formatting be controlled by static members that can be changed by the application program through accessors.

24.3 Abstract Classes

In the previous sections, we have discussed inheritance as a method to modify and extend any class. I.e., the definition of the base classes were independent of the definitions of inherited classes. In that sense, the base classes were oblivious to any future derivation of them. Sometimes it is useful to define base classes which are not independent of derived classes and which impose design constraints of derived classes. Two such dependencies in F# are abstract classes and interfaces.

An abstract class contains members defined using the abstract member and optionally the *default* keywords. An abstract member in the base class is a type definition, and derived classes must provide an implementation using the override keyword. Optionally, the base class may provide a default implementation using the default keyword, in which case overriding is not required in derived classes. Objects of classes containing abstract members without default implementations cannot be instantiated, but derived classes that provide the missing implementations can. Note that abstract classes must be given the [<AbstractClass>] attribute. Note also that in contrast to overshadowing, upcasting keeps the implementations of the derived classes. Examples of this are shown in Listing 24.7. In the example, we define a base class and two derived classes. Note how the abstract member is defined in the base class using the ":"-operator as a type declaration rather than a name binding. Note also that since the base class does not provide a default implementation, the derived classes supply an implementation using the override-keyword. In the example, objects of baseClass cannot be created, since such objects would have no implementation for this.hello. Finally, the two different derived and upcasted objects can be put in the same array, and when calling their implementation of this.hello, we still get the derived implementations, which is in contrast to overshadowing.

Abstract classes may also specify a default implementation, such that derived classes have the option of implementing an overriding member, but are not forced to. In spite

Listing 24.7 abstractClass.fsx:

In contrast to regular objects, upcasted derived objects use the derived implementation of abstract methods. Compare with Listing 24.3.

```
/// An abstract class for general greeting classes with
   property str
[<AbstractClass>]
type greeting () =
  abstract member str : string
/// hello is a greeting
type hello () =
  inherit greeting ()
  override this.str = "hello"
/// howdy is a greeting
type howdy () =
  inherit greeting ()
  override this.str = "howdy"
let a = hello ()
let b = howdy ()
let c = [| a :> greeting; b :> greeting |] // arrays of
   areetinas
Array.iter (fun (elm : greeting) -> printfn "%s" elm.str) c
$ fsharpc --nologo abstractClass.fsx && mono abstractClass.exe
hello
howdy
```

of implementations being available in the abstract class, the abstract class still cannot be used to instantiate objects. The example in Listing 24.8 shows an extension of Listing 24.7 with a default implementation. In the example, the program in Listing 24.7 has been modified such that greeting is given a default implementation for str, in which case hello does not need to supply one. However, in order for howdy to provide a different greeting, it still needs to provide an override member.

Note that even if all abstract members in an abstract class have defaults, objects of its type can still not be created, but must be derived as, e.g., shown with hello above.

As a side note, every class implicitly derives from a base class <code>System.Object</code>, which is an abstract class defining among other members, the <code>ToString</code> method with default implementation.

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Listing 24.8 abstractDefaultClass.fsx: Default implementations in abstract classes make implementations in derived classes optional. Compare with Listing 24.7. /// An abstract class for general greeting classes with property str [<AbstractClass>] type greeting () = abstract member str : string default this.str = "hello" // Provide default implementation /// hello is a greeting type hello () = inherit greeting () /// howdy is a greeting type howdy () = inherit greeting () override this.str = "howdy" let a = hello () let b = howdy ()let c = [| a :> greeting; b :> greeting |] // arrays of greetings Array.iter (fun (elm : greeting) -> printfn "%s" elm.str) c \$ fsharpc --nologo abstractDefaultClass.fsx && mono abstractDefaultClass.exe hello howdy

24.4 Interfaces

Inheritance of an abstract base class allows an application to rely on the definition of the base, regardless of any future derived classes. This gives great flexibility, but at times even less knowledge is needed about objects in order to write useful applications. This is what *interfaces* offer. An interface specifies which members must exist, but nothing more. Interfaces are defined as an abstract class *without arguments* and *only with abstract members*. Classes implementing interfaces must specify implementations for the abstract members using the *interface with* keywords. Objects of classes implementing interfaces can be upcasted as if they had an abstract base class of the interface's name. Consider the example in Listing 24.9. Here, two distinctly different classes are defined: house and person. These are not related by inheritance, since no sensible common structure seems available. However, they share structures in the sense that they both have an integer property and a float -> float method. For each of the derived classes, these members have different meanings. Still, some treatment of these members by an application will only rely on their type and not their meaning. E.g., in Listing 24.9, the printfn

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Listing 24.9 classInterface.fsx:

Interfaces specify which members classes contain, and with upcasting gives more flexibility than abstract classes.

```
/// An interface for classes that have method fct and member
   value
type IValue =
  abstract member fct : float -> float
  abstract member value : int
/// A house implements the IValue interface
type house (floors: int, baseArea: float) =
  interface IValue with
    // calculate total price based on per area average
    member this.fct (pricePerArea : float) =
      pricePerArea * (float floors) * baseArea
    // return number of floors
    member this.value = floors
/// A person implements the IValue interface
type person(name : string, height: float, age : int) =
  interface IValue with
   // calculate body mass index (kg/(m*m)) using hypothetic
   mass
   member this.fct (mass : float) = mass / (height * height)
    // return the length of name
    member this.value = name.Length
  member this.data = (name, height, age)
let a = house(2, 70.0) // a two storage house with 70 m*m
   base area
let b = person("Donald", 1.8, 50) // a 50 year old person 1.8
   m high
let lst = [a :> IValue; b :> IValue]
let printInterfacePart (o : IValue) =
  printfn "value = %d, fct(80.0) = %g" o.value (o.fct 80.0)
List.iter printInterfacePart lst
$ fsharpc --nologo classInterface.fsx && mono
   classInterface.exe
value = 2, fct(80.0) = 11200
value = 6, fct(80.0) = 24.6914
```

function only needs to know the member's type, not its meaning. As a consequence, the application can upcast them both to the implicit abstract base class IValue, put them in an array, and apply a function using the member definition of IValue with the higher-order List.iter function. Another example could be a higher-order function calculating average values: For average values of the number of floors and average value of the length of people's names, the higher-order function would only need to know that both of these classes implement the IValue interfaces in order to calculate the average of list of either objects' types.

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As a final note, inheritance ties classes together in a class hierarchy. Abstract members enforce inheritance and impose constraints on the derived classes. Like abstract classes, interfaces impose constraints on derived classes, but without requiring a hierarchical structure.

24.5 Programming Intermezzo: Chess

To demonstrate the use of hierarchies, consider the following problem.

Problem 24.1

he game of chess is a turn-based game for two which consists of a board of 8×8 squares, and a set of 16 black and 16 white pieces. A piece can be either a king, queen, rook, bishop, knight or pawn, and each piece has a specific movement pattern on the board. Pieces are added to, moved on, and removed from the board during the game, and there can be at most one piece per square. A piece strikes another piece of opposing color by moving to its square and the piece of opposing color is removed from the game. The game starts with the configuration shown in Figure 24.2.

Make a program that allows two humans to play simple chess using only kings and rooks. The king must be able to move to all neighboring squares not occupied by a piece of the same color and cannot move onto a square where it can be struck in the next turn. The rook must be able to move in horizontal and vertical lines until a piece of the same color or up to and including a piece of opposing color.

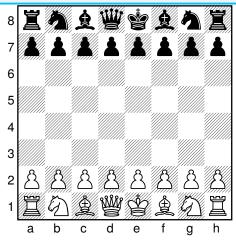


Fig. 24.2 Starting position for the game of chess.

Since we expect that the solution to the above problem is going to be a relatively long program, we have decided to split the code into a library and an application program. Before writing a library, it is often useful to start thinking about how the library should be used. Thus we start by sketching the application program, and in the process consider options for the main methods and properties to be used.

We also foresee future extensions to include more pieces, but also that these pieces will obey the same game mechanics that we design for the present problem. Thus,

we will put the main part of the library in a file defining the module called Chess and the derived pieces in another file defining the module Pieces.

Every game needs a board, and we will define a class Board. A board is like an array, so it seems useful to be able to move pieces by index notation. Thus, the board must have a two-dimensional Item property. We also decide that each position will hold an option type, such that when a square is empty it holds None, and otherwise it holds piece p as Some p. Although chess notation would be neat, for ease of programming we will let index (0,0) correspond to position a1 in chess notation, etc. The most common operation will probably be to move pieces around, so we will give the board a move method. We will most likely also like to print the board with pieces in their right locations. For simplicity, we choose to override the ToString method in Board, and that this method also prints information about each individual piece, such as where it is, where it can move to, and which pieces it can either protect or hit. The pieces that a piece can protect or hit we will call the piece's neighbor pieces.

A piece can be one of several types, so this gives a natural hierarchical structure which is well suited for inheritance. Each piece must be given a color, which may conveniently be given as argument at instantiation. Thus, we have decided to make a base class called chessPiece with argument Color, and derived classes king and rook. The color may conveniently be define as a discriminated union type of either White or Black. Each piece will also override the ToString method for ease of printing. The override will be used in conjunction with the board's override, so it should only give information about the piece's type and color. For compact printing, we will use a single letter for the type of piece, upper case if white, and lower case if black. We expect the pieces also to need to know something about the their relation to board, so we will make a position property which holds the coordinates of the piece, and we will make a availableMoves method that lists the possible moves a piece can make. Thus, we produce the application in Listing 24.10, and an illustration of what the program should do is shown in Figure 24.3. At this point, we are fairly happy with the way the application is written. The double bookkeeping of pieces in an array and on the board seems a bit excessive, but for testing it seems useful to be able to easily access all pieces, both those in play and struck. Although the position property of a chessPiece could be replaced by a function searching for a specific piece on the board, we have a hunch that we will need to retrieve a piece's position often, and that this double bookkeeping will most likely save execution time later.

Continuing our outer to inner approach, as a second step, we consider the specific pieces: They will inherit a base piece and implement the details that are special for that piece. Each piece is signified by its color and its type, and each type has a specific motion pattern. Since we have already decided to use discriminated unions for the color, it seems natural to let the color be part of the constructor of the base class. As in the example application in Listing 24.10, pieces are upcasted to chessPiece, thus, the base class must know how to print the piece type. For this, we will define an

Listing 24.10 chessApp.fsx: A chess application. open Chess open Pieces /// Print various information about a piece let printPiece (board : Board) (p : chessPiece) : unit = printfn "%A: %A %A" p p.position (p.availableMoves board) // Create a game let board = Chess.Board () // Create a board // Pieces are kept in an array for easy testing let pieces = [| king (White) :> chessPiece; rook (White) :> chessPiece; king (Black) :> chessPiece |] // Place pieces on the board board.[0,0] <- Some pieces.[0]</pre> board.[1,1] <- Some pieces.[1]</pre> board.[4,1] <- Some pieces.[2]</pre> printfn "%A" board Array.iter (printPiece board) pieces // Make moves board.move (1,1) (3,1) // Moves a piece from (1,1) to (3,1)printfn "%A" board Array.iter (printPiece board) pieces

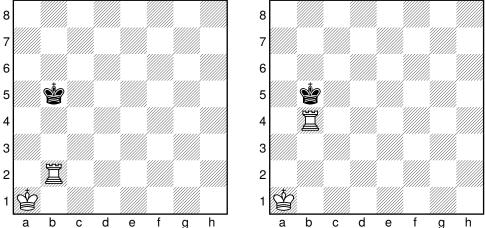


Fig. 24.3 Starting at the left and moving white rook to b4.

abstract property, such that everything needed for overriding ToString is available to the base class, but also such that the name of the type of the piece is set in the derived class.

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For a piece on the board, its available moves depend on its type and the other pieces. The application program will need to make a decision on whether to move the piece depending on which vacant squares it can move to, and its relation to its neighbors, i.e., is the piece protecting one of its own color, or does it have the opportunity to hit an opponent's piece. Thus, given the board with all the pieces, it seems useful that availableMoves returns two lists: a list of vacant squares and a list of neighboring pieces of either color. Each piece has a certain movement pattern which we will specify regardless of the piece' position on the board and relation to other pieces. Thus, this will be an abstract member called candidateRelativeMoves implemented in the derived pieces. These candidate relative moves are then to be sifted for legal moves, and the process will be the same for all pieces. Thus, sifting can be implemented in the base class as the availableMoves.

Many pieces move in runs, e.g., the rook can move horizontally and vertically until there is another piece. Vacant squares behind the blocking piece are unavailable. For a rook, we must analyze four runs: northward, eastward, southward, and westward. For each run, we must consult the board to see how many vacant fields there are in that direction, and which is the piece blocking, if any. Thus, we decide that the board must have a function that can analyze a list of runs, and that the result is concatenated into a single list of vacant squares and a single list of neighboring pieces, if any. This function we call getVacentNNeighbours. And so we arrive at Listing 24.11.

Listing 24.11 pieces.fs:

```
An extension of chess base.
module Pieces
open Chess
/// A king moves 1 square in any direction
type king(col : Color) =
  inherit chessPiece(col)
  // A king has runs of length 1 in 8 directions:
  // (N, NE, E, SE, S, SW, W, NW)
  override this.candidateRelativeMoves =
       [[(-1,0)];[(-1,1)];[(0,1)];[(1,1)];
       [(1,0)];[(1,-1)];[(0,-1)];[(-1,-1)]]
  override this.nameOfType = "king"
/// A rook moves horizontally and vertically
type rook(col : Color) =
  inherit chessPiece(col)
  // A rook can move horizontally and vertically
  // Make a list of relative coordinate lists. We consider the
  \ensuremath{//} current position and try all combinations of relative
  // moves (1,0); (2,0) ... (7,0); (-1,0); (-2,0); ...;
  // Some will be out of board, but will be assumed removed as
  // illegal moves.
  // A list of functions for relative moves
  let indToRel = [
     fun elm -> (elm,0); // South by elm
     fun elm -> (-elm,0); // North by elm
     fun elm -> (0,elm); // West by elm
     fun elm \rightarrow (0,-elm) // East by elm
  // For each function f in indToRel, we calculate
      List.map f [1..7].
```

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The king has the simplest relative movement candidates, being the hypothetical eight neighboring squares. Rooks have a considerably longer list of candidates of relative moves, since it potentially can move to all 7 squares northward, eastward, southward, and westward. This could be hardcoded as 4 potential runs, [[(1,0); (2,0); ... (7,0)]; [(-1,0); (-2,0); ... (0,-7)]]. Each run will be based on the list [1..7], which gives us the idea to use List.map to convert a list of single indices [1..7] into lists of runs as required by candidateRelativeMoves. Each run may be generated from [1..7] as

```
South: List.map (fun elm -> (elm, 0)) [1..7]
North: List.map (fun elm -> (-elm, 0)) [1..7]
West: List.map (fun elm -> (0, elm)) [1..7]
East: List.map (fun elm -> (0, -elm)) [1..7]
```

and which can be combined as a list of 4 lists of runs. Further, since functions are values, we can combine the 4 different anonymous functions into a list of functions and use a for-loop to iterate over the list of functions. This is shown in Listing 24.12. However, this solution is imperative in nature and does not use the elegance of the

```
Listing 24.12 imperativeRuns.fsx:
Calculating the runs of a rook using imperative programming.

30 let mutable listOfRuns : ((int * int) list) list = []

31 for f in indToRel do

32 let run = List.map f [1..7]

33 listOfRuns <- run :: listOfRuns
```

functional programming paradigm. A direct translation into functional programming is given in Listing 24.13. The functional version is slightly longer, but avoids the

```
Listing 24.13 functionalRuns.fsx:

Calculating the runs of a rook using functional programming.

let rec makeRuns lst =
    match lst with
    | [] -> []
    | f :: rest ->
    let run = List.map f [1..7]
    run :: makeRuns rest
    makeRuns indToRel
```

mutable variable.

Generating lists of runs from the two lists [1..7] and indToRel can also be performed with two List.maps, as shown in Listing 24.14.

The anonumous function,

```
fun e -> List.map e [1..7],
```

```
Listing 24.14 ListMapRuns.fsx:
Calculating the runs of a rook using double List.maps.

30 List.map (fun e -> List.map e [1..7]) indToRel
```

is used to wrap the inner List.map functional. An alternative, sometimes seen is to use currying with argument swapping: Consider the function, let altMap lst e = List.map e lst, which reverses the arguments of List.map. With this, the anonymous function can be written as fun e -> altMap [1..7] e or simply replaced by currying as altMap [1..7]. Reversing orders of arguments like this in combination with currying is what the swap function is for,

```
let swap f a b = f b a.
```

With swap we can write let altMap = swap List.map. Thus,

```
swap List.map [1..7]
```

is the same function as $fun e \rightarrow List.map e [1..7]$, and in which case we could rewrite the solution in Listing 24.14 as

```
List.map (swap List.map [1..7]) indToRel
```

if we wanted a very compact, but possible less readable solution.

The final step will be to design the Board and chessPiece classes. The Chess module implements discriminated unions for color and an integer tuple for a position. These are shown in Listing 24.15. The chessPiece will need to know what a board

```
Listing 24.15 chess.fs:
A chess base: Module header and discriminated union types.

1 module Chess
2 type Color = White | Black
3 type Position = int * int
```

is, so we must define it as a mutually recursive class with Board. Furthermore, since all pieces must supply an implementation of availableMoves, we set it to be abstract by the abstract class attribute and with an abstract member. The board will need to be able to ask for a string describing each piece, and to keep the board on the screen we include an abbreviated description of the piece's properties color and piece type. The result is shown in Listing 24.16.

Our Board class is by far the largest and will be discussed in Listing 24.17–24.19. The constructor is shown in Listing 24.17. For memory efficiency, the board has been

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Listing 24.16 chess.fs: A chess base. Abstract type chessPiece. /// An abstract chess piece [<AbstractClass>] type chessPiece(color : Color) = let mutable _position : Position option = None abstract member nameOfType : string // "king", "rook", ... member this.color = color // White, Black member this.position // E.g., (0,0), (3,4), etc. with get() = _position and set(pos) = _position <- pos</pre> override this.ToString () = // E.g. "K" for white king match color with White -> (string this.nameOfType.[0]).ToUpper () | Black -> (string this.nameOfType.[0]).ToLower () /// A list of runs, which is a list of relative movements, /// [[(1,0); (2,0);...]; [(-1,0); (-2,0)]...]. Runs must be /// ordered such that the first in a list is closest to the piece /// at hand. abstract member candidateRelativeMoves : Position list list /// Available moves and neighbours ([(1,0); (2,0);...], [p1; p2]) member this.availableMoves (board : Board) : (Position list * chessPiece list) = board.getVacantNNeighbours this

implemented using a Array2D, since pieces will move around often. For later use, in the members shown in Listing 24.19 we define two functions that convert relative coordinates into absolute coordinates on the board, and remove those that fall outside the board. These are called validPositionWrap and relativeToAbsolute.

For ease of use in an application, Board implements Item, such that the board can be read and written to using array notation. And ToString is overridden, such that an application may print the board anytime using a printf function. This is shown in Listing 24.18. Note that for efficiency, location is also stored in each piece, so set also needs to update the particular piece's position, as done in line 48. Note also that the board is printed with the first coordinate of the board being rows and second columns, and such that element (0,0) is at the bottom right complying with standard chess notation.

Listing 24.17 chess.fs:

A chess base: the constructor

```
/// A board
and Board () =
  let _board = Collections.Array2D.create<chessPiece option>
   8 8 None
  /// Wrap a position as option type
  let validPositionWrap (pos : Position) : Position option =
    let (rank, file) = pos // square coordinate
    if rank < 0 \mid \mid rank > 7 \mid \mid file < 0 \mid \mid file > 7 then
      None
    else
      Some (rank, file)
  /// Convert relative coordinates to absolute and remove
  /// out-of-board coordinates.
  let relativeToAbsolute (pos : Position) (lst : Position
   list) : Position list =
   let addPair (a : int, b : int) (c : int, d : int) :
   Position =
      (a+c,b+d)
    // Add origin and delta positions
    List.map (addPair pos) lst
    // Choose absolute positions that are on the board
    |> List.choose validPositionWrap
```

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Listing 24.18 chess.fs:

A chess base: Board header, constructor, and non-static members.

```
/// Board is indexed using .[,] notation
member this.Item
  with get(a : int, b : int) = _board.[a, b]
  and set(a : int, b : int) (p : chessPiece option) =
    if p.IsSome then p.Value.position <- Some (a,b)</pre>
    _board.[a, b] <- p
/// Produce string of board for, e.g., the printfn function.
override this.ToString() =
  let mutable str = ""
  for i = Array2D.length1 _board - 1 downto 0 do
    str <- str + string i
    for j = 0 to Array2D.length2 _board - 1 do
      let p = _board.[i,j]
      let pieceStr =
          match p with
            None -> " ";
      | Some p -> p.ToString()
str <- str + " " + pieceStr
    str <- str + "\n"
  str + " 0 1 2 3 4 5 6 7"
/// Move piece by specifying source and target coordinates
member this.move (source : Position) (target : Position) :
 unit =
  this.[fst target, snd target] <- this.[fst source, snd
 source]
  this.[fst source, snd source] <- None</pre>
/// Find the tuple of empty squares and first neighbour if
member this.getVacantNOccupied (run : Position list) :
 (Position list * (chessPiece option)) =
    // Find index of first non-vacant square of a run
    let idx = List.findIndex (fun (i, j) ->
 this.[i,j].IsSome) run
```

The main computations are done in the static methods of the board, as shown in Listing 24.19. A chess piece must implement candidateRelativeMoves, and we de-

```
Listing 24.19 chess.fs:
A chess base: Board static members.
       let (i,j) = run.[idx]
       let piece = this.[i, j] // The first non-vacant
   neighbour
       if idx = 0 then
         ([], piece)
       else
         (run.[..(idx-1)], piece)
         -> (run, None) // outside the board
   /// find the list of all empty squares and list of
   neighbours
  member this.getVacantNNeighbours (piece : chessPiece) :
    (Position list * chessPiece list) =
     match piece.position with
       None ->
         ([],[])
       | Some p ->
         let convertNWrap =
           (relativeToAbsolute p) >> this.getVacantNOccupied
         let vacantPieceLists = List.map convertNWrap
   piece.candidateRelativeMoves
         // Extract and merge lists of vacant squares
         let vacant = List.collect fst vacantPieceLists
         // Extract and merge lists of first obstruction pieces
         let neighbours = List.choose snd vacantPieceLists
         (vacant, neighbours)
```

cided in Listing 24.16 that moves should be specified relative to the piece's position. Since the piece does not know which other pieces are on the board, it can only specify all potential positions. For convenience, we will allow pieces to also specify positions outside the board, such that, e.g., the rook can specify the 7 nearest neighboring squares up, down, left, and right, regardless that some may be outside the board. Thus getVacantNNeighbours must first convert the relative positions to absolute and clip any outside the board. This is done by relativeToAbsolute. Then for each run, the first occupied square must be identified. Since availableMoves must return two lists, vacant squares, and immediate neighbors, this structure is imposed on the output of convertNWrap as well. This is computed in getVacantNOccupied by use of the built-in List.findIndex function. This function returns the index of the first element in a list for which the supplied function is true and otherwise throws an exception. Exceptions are always somewhat inelegant, but in this case, it is harmless, since the exception signifies a valid situation where no pieces exist on the run. After having analyzed all runs independently, then all the vacant lists are merged, all the neighboring pieces are merged and both are returned to the caller.

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Compiling the library files with the application and executing gives the result shown in Listing 24.20. We see that the program has correctly determined that initially, the

```
Listing 24.20: Running the program. Compare with Figure 24.3.
$ fsharpc --nologo chess.fs pieces.fs chessApp.fsx && mono
    chessApp.exe
7
6
5
4
3
2
    R
1
0 K
  0 1 2 3 4 5 6 7
K: Some (0, 0) ([(0, 1); (1, 0)], [R])
R: Some (1, 1) ([(2, 1); (3, 1); (0, 1); (1, 2); (1, 3); (1,
    4); (1, 5); (1, 6); (1, 7); (1, 0)],
k: Some (4, 1) ([(3, 1); (3, 2); (4, 2); (5, 2); (5, 1); (5,
    0); (4, 0); (3, 0)], [])
6
5
4
    k
3
    R
2
1
0 K
  0 1 2 3 4 5 6 7
K: Some (0, 0) ([(0, 1); (1, 1); (1, 0)], [])
R: Some (3, 1) ([(2, 1); (1, 1); (0, 1); (3, 2); (3, 3); (3,
    4); (3, 5); (3, 6); (3, 7); (3, 0)],
k: Some (4, 1) ([(3, 2); (4, 2); (5, 2); (5, 1); (5, 0); (4,
    0); (3, 0)], [R])
```

white king has the white rook as its neighbors and due to its location in the corner only has two free positions to move to. The white rook has many and the black king as its neighbor. The black king is free to move to all its eight neighboring fields. After moving the white rook to (3,1) or b4 in regular chess notation, then the white king has no neighbors, and the white rook and the black king are now neighbors with an appropriate restriction on their respective vacant squares. These simple use-tests are in no way a thorough test of the quality of the code, but they give us a good indication that our library offers a tolerable interface for the application, and that at least major parts of the code function as expected. Thus, we conclude this intermezzo.

24.6 Debugging Classes

Chapter 25

The Object-Oriented Programming Paradigm

Object-oriented programming is a paradigm for encapsulating data and methods into cohesive units. Key features of object-oriented programming are:

Encapsulation

Data and methods are collected into a cohesive unit, and an application program need only focus on how to use the object, not on its implementation details.

Inheritance

Objects are organized in a hierarchy of gradually increased specialty. This promotes a design of code that is of general use, and code reuse.

Polymorphism

By overriding methods from a base class, derived classes define new data types while their methods still produce results compatible with the base class definitions.

Object-oriented programming has a well-developed methodology for analysis and design. The analysis serves as input to the design phase, where the analysis reveals *what* a program is supposed to do, and the design *how* it is supposed to be doing it. The analysis should be expressed in general terms irrespective of the technologic constraints, while the design should include technological constraints such as defined by the targeted language and hardware.

The primary steps for *object-oriented analysis and design* are:

- 1. identify objects,
- 2. describe object behavior,
- 3. describe object interactions,

- 4. describe some details of the object's inner workings,
- 5. write a precise description for classes, properties and methods using, e.g., F#'s XML documentation standard,
- 6. write mockup code,
- 7. write unit tests and test the basic framework using the mockup code,
- 8. replace the mockup with real code while testing to keep track of your progress. Extend the unit test as needed,
- 9. evaluate code in relation to the desired goal,
- 10. complete your documentation both in-code and outside.

Steps 1–4 are the analysis phase which gradually stops in step 4, while the design phase gradually starts at step 4 and gradually stops when actual code is written in step 7. Notice that the last steps are identical to imperative programming, Chapter 22. Programming is never a linear experience, and you will often need to go back to previous steps to update or change decisions. You should not refrain from improving your program design and implementation, but you should always be mindful of the goal. Often less than the perfect solution will suffice.

An object-oriented analysis can be a daunting process. A good starting point is a *use case*, *problem statement*, or a *user story*, which in human language describes a number of possibly hypothetical interactions between a user and a system with the purpose of solving some task. Two useful methodologies for performing an object-oriented analysis is the method of nouns-and-verbs and the unified modeling language, described in the following sections.

25.1 Identification of Objects, Behaviors, and Interactions by Nouns-and-Verbs

A key point in object-oriented programming is that objects should to a large extent be independent and reusable. As an example, the type int models the concept of integer numbers. It can hold integer values from -2,147,483,648 to 2,147,483,647, and a number of standard operations and functions are defined for it. We may use integers in many different programs, and it is certain that the original designers did not foresee our use, but strived to make a general type applicable for many uses. Such a design is a useful goal when designing objects, that is, our objects should model the general concepts and be applicable in future uses.

Analyzing a specific use-case, good candidates for objects are persons, places, things, events, concept etc., which are almost always characterized by being *nouns* in the text. Interactions between objects are actions that bind objects together, and actions are often associated with *verbs*. When choosing methods, it is important to maintain an object-centered perspective, i.e., for a general-purpose object, we should limit the need for including information about other objects. E.g., a value of type int need not know anything about the program in which it is being used.

Said briefly, the nouns-and-verbs method is:

Nouns are object candidates, and verbs are candidate methods that describe interactions between objects.

25.2 Class Diagrams in the Unified Modelling Language

Having found an initial list of candidate objects and interactions, it is often useful to make a drawing of these relations with an increased focus on the object's inner workings. A *class diagram* is a schematic drawing of the program, highlighting its object-oriented structure, and we will use the *Unified Modelling Language 2 (UML)* [5] standard. The standard is very broad, and here we will discuss structure diagrams for use in describing objects.

A class is drawn as shown in Figure 25.1. In UML, classes are represented as

```
Value-identifier: type
value-identifier: type = default value

function-identifier (arg: type) (arg: type) ...: type
function-identifier (arg: type) (arg: type) ...: type
```

Fig. 25.1 A UML diagram for a class consists of it's name, zero or more attributes, and zero or more methods.

boxes with their class name. Depending on the desired level of details, zero or more properties and methods are described. These describe the basic interface to the class and objects of its type. Abstract members that require an implementation are shown in cursive. Here we have used F# syntax to conform with this book theme, but typically C# syntax is used. Interfaces are a special type of class that require an implementation. To highlight this, UML uses the notation shown in Figure 25.2.

Relations between classes and objects are indicated by lines and arrows. The most common ones are summarized in Figure 25.3. Their meaning will be described in detail in the following.

Fig. 25.2 An interface is a class that requires an implementation.

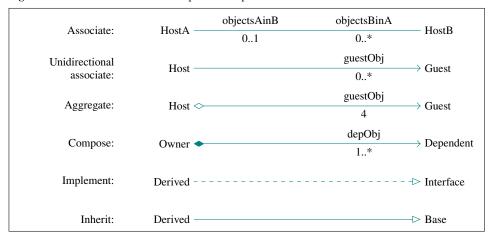


Fig. 25.3 Arrows used in class diagrams to show relations between objects.

25.2.1 Associations

A family of relations is association, aggregation, and composition, and these are distinguished by how they handle the objects they are in relation with. The relation between the three relations is shown in Figure 25.4. Aggregational and compositional

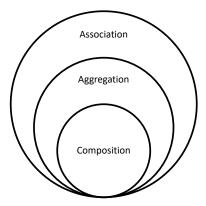


Fig. 25.4 The relation between Association, Aggregation and Composition in UML.

are specialized types of associations that imply ownership and are often called has-a relations. A composition is a collection of parts that makes up a whole. In

object-oriented design, a compositional relation is a strong relation, where a guest object makes little sense without the host, as a room cannot exist without a house. An aggregation is a collection of assorted items, and in object-oriented design, an aggregational relation is a loose relation, like how a battery can meaningfully be separated from a torchlight. Some associations are neither aggregational nor compositional, and commonly just called an association. An association is a group of people or things linked for some common purpose a cooccurrence. In object-oriented design, associations between objects are the loosest possible relations, like how a student may be associated with the local coffee shop. Sometimes associational relations are called a *knows-about*.

Association

The most general type of association, which is just called an association, is the possibility for objects to send messages to each other. This implies that one class knows about the other, e.g., uses it as arguments of a function or similar. A host is associated with a guest if the host has a reference to the guest. Objects are reference types, and therefore, any object which is not created by the host, but where a name is bound to a guest object but not explicitly copied, then this is an association relation.

Bidirectional association means that classes know about each other. The UML notation is shown in Figure 25.5. Association may be annotated by an identifier and



Fig. 25.5 Bidirectional association is shown as a line with optional annotation.

a multiplicity. In the figure, HostA has 0 or more variables of type HostB named objectsBinA, while HostB has 0 or 1 variables of HostA named objectsAinB. The multiplicity notation is very similar to F#'s slicing notation. Typical values are shown in Table 25.1. If the association is unidirectional, then an arrow is added for empha-

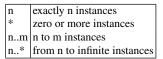


Table 25.1 Notation for association multiplicities is similar to F#'s slicing notation.

sis, as shown in Figure 25.6. In this example, Host knows about Guest and has one



Fig. 25.6 Unidirectional association shows a one-side has-a relation.

instance of it, and Guest is oblivious about Host.

A programming example showing a unidirectional association is given in Listing 25.1. Here, the student is unidirectionally associated with a teacher since the

```
Listing 25.1 umlAssociation.fsx:
The student is associated with a teacher.

1 type teacher () =
2 member this.answer (q : string) = "4"
3 type student (t : teacher) =
4 member this.ask () = t.answer("What is 2+2?")

5 let t = teacher ()
7 let s = student (t)
8 s.ask()
```

student can send and receive messages to and from the teacher. The teacher, on the other hand, does not know anything about the student. In UML this is depicted as shown in Figure 25.7.



Fig. 25.7 The teacher and student objects can access each other's functions, and thus they have an association relation.

Aggregation

Aggregated relationships are a specialization of associations. As an example, an author may have written a book, but once created, the book gets a life independent of the author and may, for example, be given to a reader, and the book continues to exist even when the author dies. That is, In aggregated relations, the host object has a reference to a guest object and may have created the guest, but the guest will be shared with other objects, and when the host is deleted, the guest is not.

Aggregation is illustrated using a diamond tail and an open arrow, as shown in Figure 25.8. Here the Host class has stored aliases to four different Guest objects.



Fig. 25.8 Aggregation relations are a subset of associations where local aliases are stored for later use.

An programming example of an aggregation relation is given in Listing 25.2. In aggregated relations, there is a sense of ownership, and in the example, the author object creates a book object which is published and bought by a reader. Hence the book change ownership during the execution of the program. In UML this is to be depicted as shown in Figure 25.9.

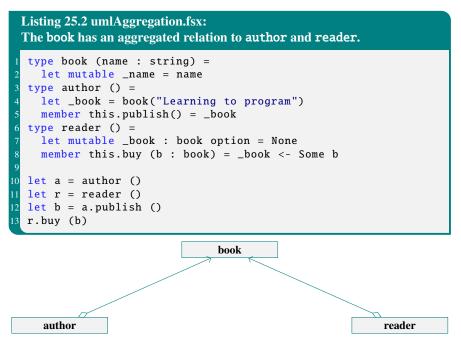


Fig. 25.9 A book is an object that can be owned by both an author and a reader.

Composition

A compositional relationship is a specialization of aggregations. As an example, a dog has legs, and dog legs can not very sensibly be given to other animals. That is, in compositional relations, the host creates the guest, and when the host is deleted, so is the guest. A composition is a stronger relation than aggregation and is illustrated using a filled filled diamond tail, as illustrated in Figure 25.10. In this example,



Fig. 25.10 Composition relations are a subset of aggregation where the host controls the lifetime of the guest objects.

Owner has created 1 or more objects of type Dependent, and when Owner is deleted, so are these objects.

A programming example of a composition relation is given in Listing 25.3. In Listing 25.3, a dog object creates four leg objects, and it makes less sense to be able to turn over the ownership of each leg to other objects. Thus, a dog is a composition of leg objects. Using UML, this should be depicted as shown in Figure 25.11.

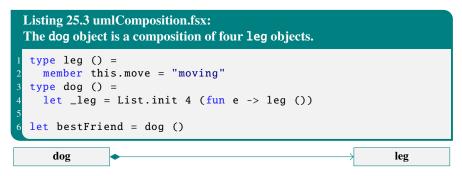


Fig. 25.11 A dog is a composition of legs.

25.2.2 Inheritance-type relations

Classes may inherit other classes where the parent is called the base class and the children its derived classes. Such a relation is often called an *is-a* relation, since the derived class *is a* kind of base class.

Inheritance

Inheritance is a relation between properties of classes. As an example, a student and a teacher is a type of person. All persons have names, while a student also has a reading list, and a teacher also has a set of slides. Thus, both students and teacher may inherit from a person to gain the common property, name. In UML this is illustated with an non-filled, closed arrow as shown in Figure 25.12. Here two

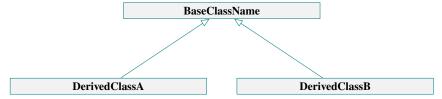


Fig. 25.12 Inheritance is shown by a closed arrowhead pointing to the base.

classes inherit the base class.

A programming example of an inheritance is given in Listing 25.4. In Listing 25.4, the student and the teacher classes are derived from the same person class. Thus, they all three have the name property. Using UML, this should be depicted as shown in Figure 25.13.

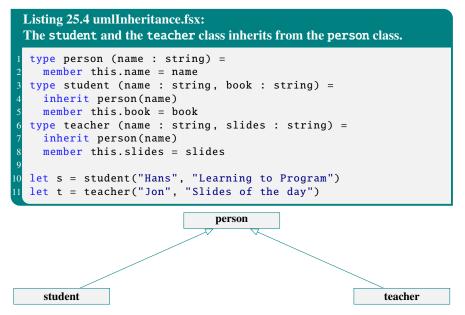


Fig. 25.13 A student and a teacher inherit from a person class.

Interface

An interface is a relation between the properties of an abstract class and a regular class. As an example, a television and a car both have buttons, that you can press, although their effect will be quite different. Thus, a television and a car may both implement the same interface. In UML, interfaces are shown similarly to inheritance, but using a stippled line, as shown in Figure 25.14.

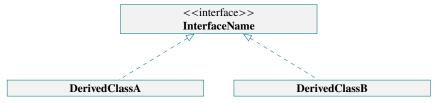


Fig. 25.14 Implementations of interfaces is shown with stippled line and closed arrowhead pointing to the base.

A programming example of an interface is given in Listing 25.5. In Listing 25.5, the television and the car classes implement the button interface. Hence, although they are different classes, they both have the press () method and, e.g., can be given as a function requiring only the existence of the press () method. Using UML, this should be depicted as shown in Figure 25.15.

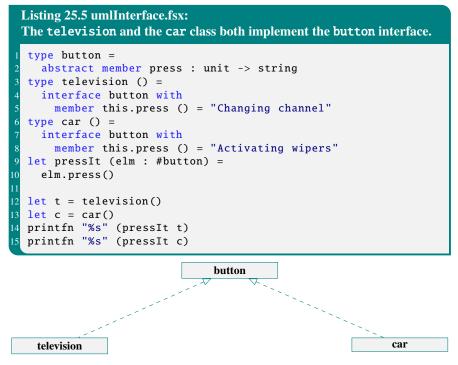


Fig. 25.15 A student and a teacher inherit from a person class.

25.2.3 Packages

Namespace and modules

For visual flair, modules and namespaces are often visualized as *packages*, as shown in Figure 25.16. A package is like a module in F#.

25.3 Programming Intermezzo: Designing a Racing Game

An example is the following *problem statement*:

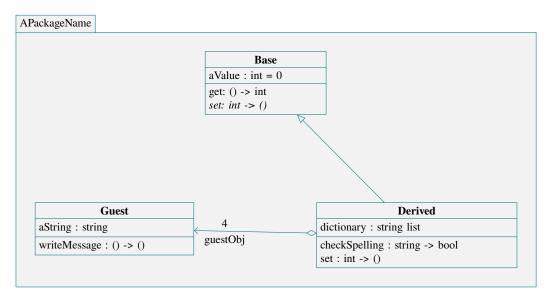


Fig. 25.16 Packages are a visualizations of modules and namespaces.

Problem 25.1

rite a racing game, where each player controls his or her vehicle on a track. Each vehicle must have individual features such as top acceleration, speed, and handling. The player must be able to turn the vehicle left and right, and to accelerate up and down. At the beginning of the game, each vehicle is placed behind the starting line. Once the start signal is given, then the players may start to operate their vehicles. The player who first completes 3 rounds wins.

To seek a solution, we will use the *nouns-and-verbs method*. Below, the problem statement is repeated with nouns and verbs highlighted.

Write a racing game, where each player controls his or her vehicle on a track. Each vehicle must have individual features such as top acceleration, speed, and handling. The player must be able to turn the vehicle left and right, and to accelerate up and down. At the beginning of the game, each vehicle is placed behind the starting line. Once the start signal is given, then the players may start to operate their vehicles. The player who first completes 3 rounds wins.

The above nouns and verbs are candidates for objects, their behaviour, and their interaction. A deeper analysis is:

Identification of objects by nouns (Step 1):

Identified unique nouns are: racing game (game), player, vehicle, track, feature, top acceleration, speed, handling, beginning, starting line, start signal, rounds. From this list we seek cohesive units that are independent and reusable. The nouns

game, player, vehicle, and track

seem to fulfill these requirements, while all the rest seems to be features of the former and thus not independent concepts. E.g., top acceleration is a feature of a vehicle, and starting line is a feature of a track.

Object behavior and interactions by verbs (Steps 2 and 3):

To continue our object-oriented analysis, we will consider the object candidates identified above, and verbalize how they would act as models of general concepts useful in our game.

player The player is associated with the following verbs:

- A player controls/operates a vehicle.
- A player turns and accelerates a vehicle.
- A player completes rounds.
- A player wins.

Verbalizing a player, we say that a player in general must be able to control the vehicle. In order to do this, the player must receive information about the track and all vehicles, or at least some information about the nearby vehicles and track. Furthermore, the player must receive information about the state of the game, i.e., when the race starts and stops.

vehicle A vehicle is controlled by a player and further associated with the following verbs:

- A vehicle has features top acceleration, speed, and handling.
- A vehicle is placed on the track.

To further describe a vehicle, we say that a vehicle is a model of a physical object which moves around on the track under the influence of a player. A vehicle must have a number of attributes such as top acceleration, speed, and handling, and must be able to receive information about when to turn and accelerate. A vehicle must be able to determine its location in particular if it is on or off track and, and it must be able to determine if it has crashed into an obstacle such as another vehicle.

track A track is the place where vehicles operate and is further associated with the following verbs:

• A track has a starting line.

• A track has rounds.

Thus, a track is a fixed entity on which the vehicles race. It has a size and a shape, a starting and a finishing line, which may be the same, and vehicles may be placed on the track and can move on and possibly off the track.

game Finally, a game is associated with the following verbs:

- A game has a beginning and a start signal.
- A game can be won.

A game is the total sum of all the players, the vehicles, the tracks, and their interactions. A game controls events, including inviting players to race, sending the start signal, and monitoring when a game is finished and who won.

From the above we see that the object candidates features seems to be a natural part of the description of the vehicle's attributes, and similarly, a starting line may be an intricate part of a track. Also, many of the *verbs* used in the problem statement and in our extended verbalization of the general concepts indicate methods that are used to interact with the object. The object-centered perspective tells us that for a general-purpose vehicle object, we need not include information about the player, analogous to how a value of type int need not know anything about the program, in which it is being used. In contrast, the candidate game is not as easily dismissed and could be used as a class which contains all the above.

With this description, we see that 'start signal' can be included as a natural part of the game object. Being confident in our working hypothesis of the essential objects for the solution, we continue our investigation into further details about the objects and their interactions.

Analysis details (Step 4):

A class diagram of our design for the proposed classes and their relations is shown in Figure 25.17.

In the present description, there will be a single Game object that initializes the other objects, executes a loop updating the clock, queries the players for actions, and informs the vehicles that they should move and under what circumstances. The track has been chosen to be dumb and does not participate much in the action. Player's method getAction will be an input from a user by keyboard, joystick or similar, but the complexity of the code for a computer player will be large, since it needs to take a sensible decision based on the track and the location of the other vehicles. What at present is less clear, is whether it is the responsibility of Game or Vehicle to detect an off track or a crash event. If a vehicle is to do this, then each vehicle must have aggregated association to all other vehicles and obstacles. So, on the one hand, it

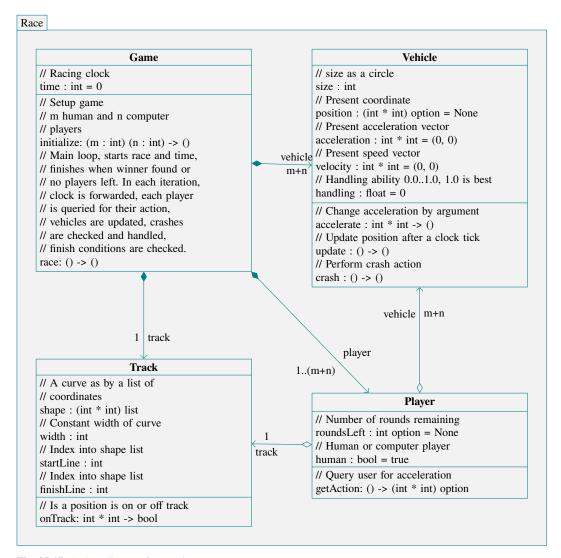


Fig. 25.17 A class diagram for a racing game.

would seem an elegant delegation of responsibilities that a vehicle knows whether it has crashed into an obstacle or not, but on the other hand, it seems wasteful of memory resources to have duplicated references of all obstacles in every vehicle. The final choice is thus one of elegance versus resource management, and in the above, we have favored resource management. Thus, the main loop in Game must check all vehicles for a crash event after the vehicle's positions have been updated, and in case of a crash, informs the relevant vehicles.

Having created a design for a racing game, we are now ready to start coding (Step 6–). It is not uncommon that transforming our design into code will reveal new structures

and problems that possibly require our design to be updated. Nevertheless, a good design phase is almost always a sure course to avoid many problems once coding, since the design phase allows the programmer to think about the problem from a helicopter perspective before tackling details of specific sub-problems.

Chapter 26

Where to Go from Here

You have now learned to program in a number of important paradigms and mastered the basics of F#, so where are good places to go now? I will highlight a number of options:

Program, program, program

You are at this stage no longer a novice programmer, so it is time for you to use your skills and create programs that solve problems. I have always found great inspiration in interacting with other domains and seeking solutions by programming. Experience is a must if you want to become a good programmer, since your newly acquired skills need to settle in your mind, and you need to be exposed to new problems that require you to adapt and develop your skills.

Learn to use an Integrated Development Environment effectively

An Integrated Development Environment (IDE) is a tool that may increase your coding efficiency. IDEs can help you get started in different environments, such as on a laptop or a phone, and it can quickly give you an overview of available options when you are programming. E.g., all IDEs will show you available members for identifiers as you type, reducing time to search members and reducing the risk of spelling errors. Many IDEs will also help you to quickly refactor your code, e.g., by highlighting all occurrences of a name in a scope and letting you change all of them in one action.

In this book, we have emphasized the console. Compiling and running from the console is the basis of which all IDEs build, and many of the problems with using IDEs efficiently are related to understanding how it can best help you compiling and running programs.

Learn other cool features of F#

F# is a large language with many features. Some have been presented in this book, but more advanced topics have been neglected. Examples are:

- regular expressions: Much computations concern processing of text. Regular expressions is a simple but powerful language for searching and replacing in strings. F# has built-in support for regular expressions as System.Text.RegularExpressions.
- sequence seq: All list type data structures in F# are built on sequences.
 Sequences are, however, more than lists and arrays. A key feature is that sequences can effectively contain large or even infinite ordered lists which you do not necessarily need or use, i.e., they are lazy and only compute its elements as needed. Sequences are programmed using computation expressions.
- computation expressions: Sequential expressions is an example of computation expressions, e.g., the sequence of squares i², i = 0..9 can be written as seq {for i in 0 ... 9 -> i * i}
- asynchronous computations async: F# has a native implementation of asynchronous computation, which means that you can very easily set up computations that run independently of others, such that they do not block each other. This is extremely convenient if you, e.g., need to process a list of homepages, where each homepage may be slow to read, such that reading them in sequence will be slow. With asynchronous computations, they can easily be read in parallel with a huge speedup for the total task as a result. Asynchronous workflows rely on computation expressions.

Learn another programming language

F# is just one of a great number of programming languages, and you should not limit yourself. Languages are often designed to be used for particular tasks, and when looking to solve a problem, you would do well in selecting the language that best fits the task. C# is an example from the Mono family which emphasizes object-oriented programming, and many of the built-in libraries in F# are written in C#. C++ and C are ancestors of C# and are very popular since they allow for great control over the computer at the expense of programming convenience. Python is a popular prototyping language which emphasizes interactive programming like fsharpi, and it is seeing a growing usage in web-backends and machine learning. And the list goes on. To get an idea of the wealth of languages, browse http://www.99-bottles-of-beer.net which has examples of solutions to the simple problem: Write a program that types the lyrics of song "99 bottles of beer on the wall" and stop. At the present time, many solutions in more than 1500 different languages have been submitted.

Appendix A

The Console in Windows, MacOS X, and Linux

Almost all popular operating systems are accessed through a user-friendly *graphical user interface* (*GUI*) that is designed to make typical tasks easy to learn to solve. As a computer programmer, you often need to access some of the functionalities of the computer, which, unfortunately, are sometimes complicated by this particular graphical user interface. The *console*, also called the *terminal* and the *Windows command line*, is the right hand of a programmer. The console is a simple program that allows you to complete text commands. Almost all the tasks that can be done with the graphical user interface can be done in the console and vice versa. Using the console, you will benefit from its direct control of the programs we write, and in your education, you will benefit from the fast and raw information you get through the console.

A.1 The Basics

When you open a *directory* or *folder* in your preferred operating system, the directory will have a location in the file system, whether from the console or through the operating system's graphical user interface. The console will almost always be associated with a particular directory or folder in the file system, and it is said that it is the directory that the console is in. The exact structure of file systems varies between Linux, MacOS X, and Windows, but common is that it is a hierarchical structure. This is illustrated in Figure A.1.

There are many predefined console commands, available in the console, and you can also make your own. In the following sections, we will review the most important commands in the three different operating systems. These are summarized in Table A.1.

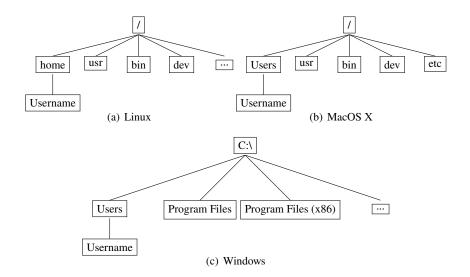


Fig. A.1 The top file hierarchy levels of common operating systems.

| Windows | MacOS X/Linux | Description |
|--------------------------------|------------------------------|--|
| dir | ls | Show content of present directory. |
| cd <d></d> | cd <d></d> | Change present directory to <d>.</d> |
| mkdir <d></d> | mkdir <d></d> | Create directory <d>.</d> |
| rmdir <d></d> | rmdir <d></d> | Delete <d> (Warning: cannot be reverted).</d> |
| move <f> <f d="" =""></f></f> | mv <f> <f d="" =""></f></f> | Move <fil> to <f d="" ="">.</f></fil> |
| copy <f1> <f2></f2></f1> | cp <f1> <f2></f2></f1> | Create a new file called <f2> as a copy of <f1>.</f1></f2> |
| del <f></f> | rm <f></f> | delete <f> (Warning: cannot be reverted).</f> |
| echo <s v="" =""></s> | echo <s v="" =""></s> | Write a string or content of a variable to screen. |

Table A.1 The most important console commands for Windows, MacOS X, and Linux. Here <f*> is shorthand for any filename, <d> for any directory name, <s> for any string, and <v> for any shell-variable.

A.2 Windows

In this section we will discuss the commands summarized in Table A.1. Windows 7 and earlier versions: To open the console, press Start->Run in the lower left corner, and then type cmd in the box. In Windows 8 and 10, you right-click on the windows icon, choose Run or equivalent in your local language, and type cmd. Alternatively, you can type Windows-key + R. Now you should open a console window with a prompt showing something like Listing A.1.

335 A.2 Windows

```
Listing A.1: The Windows console.

| Microsoft Windows [Version 6.1.7601] | Copyright (c) 2009 Microsoft Corporation. All rights reserved.
| C:\Users\sporring>
```

To see which files are in the directory, use *dir*, as shown in Listing A.2.

```
Listing A.2: Directory listing with dir.
C:\Users\sporring>dir
 Volume in drive C has no label.
 Volume Serial Number is 94F0-31BD
 Directory of C:\Users\sporring
30-07-2015 15:23
                      <DIR>
30-07-2015
            15:23
                      <DIR>
                                     . .
 30-07-2015
            14:27
                      <DIR>
                                     Contacts
            14:27
30-07-2015
                      <DIR>
                                     Desktop
30-07-2015 17:40
                      <DIR>
                                     Documents
30-07-2015 15:11
                      <DIR>
                                     Downloads
30-07-2015
           14:28
                      <DIR>
                                     Favorites
30-07-2015 14:27
                      <DIR>
                                     Links
30-07-2015 14:27
                      <DIR>
                                     Music
30-07-2015
            14:27
                      <DIR>
                                     Pictures
                                     Saved Games
30-07-2015
            14:27
                      <DIR>
            17:27
30-07-2015
                      <DIR>
                                     Searches
30-07-2015 14:27
                      <DIR>
                                     Videos
                                       0 bytes
                0 File(s)
               13 Dir(s) 95.004.622.848 bytes free
C:\Users\sporring>
```

We see that there are no files and thirteen directories (DIR). The columns tell from left to right: the date and time of their creation, the file size or if it is a folder, and the name file or directory name. The first two folders "." and ".." are found in each folder and refer to this folder as well as the one above in the hierarchy. In this case, the folder "." is an alias for C:\Users\sporring and ".." for C:\Users.

Use *cd* to change directory, e.g., to Documents, as in Listing A.3.

```
Listing A.3: Change directory with cd.

C:\Users\sporring>cd Documents

C:\Users\sporring\Documents>
```

Note that some systems translate default filenames, so their names may be given different names in different languages in the graphical user interface as compared to the console.

You can use *mkdir* to create a new directory called, e.g., myFolder, as illustrated in Listing A.4.

```
Listing A.4: Creating a directory with mkdir.
C:\Users\sporring\Documents>mkdir myFolder
C:\Users\sporring\Documents>dir
 Volume in drive C has no label.
 Volume Serial Number is 94F0-31BD
 Directory of C:\Users\sporring\Documents
30-07-2015 19:17
                     <DIR>
30-07-2015 19:17
                     <DIR>
                     <DIR>
30-07-2015 19:17
                                  myFolder
               0 File(s)
                                     0 bytes
               3 Dir(s) 94.656.638.976 bytes free
C:\Users\sporring\Documents>
```

By using dir we inspect the result.

Files can be created by, e.g., *echo* and *redirection*, as demonstrated in Listing A.5.

```
Listing A.5: Creating a file with echo and redirection.
C:\Users\sporring\Documents>echo "Hi" > hi.txt
C:\Users\sporring\Documents>dir
 Volume in drive C has no label.
 Volume Serial Number is 94F0-31BD
 Directory of C:\Users\sporring\Documents
30-07-2015 19:18
                    <DIR>
30-07-2015 19:18
                    <DIR>
30-07-2015 19:17
                   <DIR>
                                 myFolder
              8 hi.txt
1 File(s)
30-07-2015 19:18
                                8 bytes
              3 Dir(s) 94.656.634.880 bytes free
C:\Users\sporring\Documents>
```

To move the file hi.txt to the directory myFolder, use move, as shown in Listing A.6.

337 A.2 Windows

Finally, use *del* to delete a file and *rmdir* to delete a directory, as shown in Listing A.7.

```
Listing A.7: Delete files and directories with del and rmdir.
C:\Users\sporring\Documents>cd myFolder
C:\Users\sporring\Documents\myFolder>del hi.txt
C:\Users\sporring\Documents\myFolder>cd ..
C:\Users\sporring\Documents>rmdir myFolder
C:\Users\sporring\Documents>dir
 Volume in drive C has no label.
 Volume Serial Number is 94F0-31BD
 Directory of C:\Users\sporring\Documents
30-07-2015 19:20
                      <DIR>
30-07-2015 19:20
                      <DIR>
                                       0 bytes
                0 File(s)
                2 Dir(s) 94.651.142.144 bytes free
C:\Users\sporring\Documents>
```

The commands available from the console must be in its *search path*. The search path can be seen using echo, as shown in Listing A.8.

The path can be changed using the Control panel in the graphical user interface. In Windows 7, choose the Control panel, choose System and Security \rightarrow System \rightarrow Advanced system settings \rightarrow Environment Variables. In Windows 10, you can find this window by searching for "Environment" in the Control panel. In

the window's System variables box, double-click on Path and add or remove a path from the list. The search path is a list of paths separated by ";". Beware, Windows uses the search path for many different tasks, so remove only paths that you are certain are not used for anything.

A useful feature of the console is that you can use the tab-key to cycle through filenames. E.g., if you write cd followed by a space and tab a couple of times, then the console will suggest to you the available directories.

A.3 MacOS X and Linux

MacOS X (OSX) and Linux are very similar, and both have the option of using bash as console. It is in the standard console on MacOS X and on many Linux distributions. A summary of the most important bash commands is shown in Table A.1. In MacOS X, you find the console by opening Finder and navigating to Applications \rightarrow Utilities -> Terminal. In Linux, the console can be started by typing Ctrl + Alt + T. Some Linux distributions have other key-combinations such as Super + T.

Once opened, the console is shown in a window with content, as shown in Listing A.9.

```
Listing A.9: The MacOS console.

Last login: Thu Jul 30 11:52:07 on ttys000
FN11194:~ sporring$
```

"FN11194" is the name of the computer, the character \sim is used as an alias for the user's home directory, and "sporring" is the username for the user presently logged onto the system. Use 1s to see which files are present, as shown in Listing A.10.

```
Listing A.10: Display a directory content with 1s.

FN11194:~ sporring$ ls
Applications Documents Library Music
Public
Desktop Downloads Movies Pictures
FN11194:~ sporring$
```

More details about the files are available by using flags to 1s as demonstrated in Listing A.11.

Listing A.11: Display extra information about files using flags to 1s. FN11194:~ sporring\$ ls -l drwx----- 6 sporring staff 204 Jul 30 14:07 Applications drwx----+ 32 sporring staff 1088 Jul 30 14:34 Desktop drwx----+ 76 sporring staff 2584 Jul 2 15:53 Documents drwx----+ 4 sporring staff 136 Jul 30 14:35 Downloads drwx-----@ 63 sporring staff 2142 Jul 30 14:07 Library drwx----+ 3 sporring staff drwx----+ 4 sporring staff drwx----+ 3 sporring staff 102 Jun 29 21:48 Movies 136 Jul 4 17:40 Music 102 Jun 29 21:48 Pictures drwxr-xr-x+ 5 sporring staff 170 Jun 29 21:48 Public FN11194:~ sporring\$

The flag -1 means long, and many other flags can be found by querying the built-in manual with man 1s. The output is divided into columns, where the left column shows a number of codes: "d" stands for directory, and the set of three of optional "rwx" denote whether respectively the owner, the associated group of users, and anyone can respectively "r" - read, "w" - write, and "x" - execute the file. In all directories but the Public directory, only the owner can do any of the three. For directories, "x" means permission to enter. The second column can often be ignored, but shows how many links there are to the file or directory. Then follows the username of the owner, which in this case is sporring. The files are also associated with a group of users, and in this case, they all are associated with the group called staff. Then follows the file or directory size, the date of last change, and the file or directory name. There are always two hidden directories: "." and "..", where "." is an alias for the present directory, and ".." for the directory above. Hidden files will be shown with the -a flag.

Use *cd* to change to the directory, for example to Documents as shown in Listing A.12.

```
Listing A.12: Change directory with cd.

FN11194:~ sporring$ cd Documents/
FN11194:Documents sporring$
```

Note that some graphical user interfaces translate standard filenames and directories to the local language, such that navigating using the graphical user interface will reveal other files and directories, which, however, are aliases.

You can create a new directory using mkdir, as demonstrated in Listing A.13.

Listing A.13: Creating a directory using mkdir. FN11194:Documents sporring\$ mkdir myFolder FN11194:Documents sporring\$ ls

myFolder
FN11194:tmp sporring\$

A file can be created using echo and with redirection, as shown in Listing A.14.

Listing A.14: Creating a file with echo and redirection.

```
FN11194:Documents sporring$ echo "hi" > hi.txt
FN11194:Documents sporring$ ls
hi.txt myFolder
```

To move the file hi.txt into myFolder, use mv. This is demonstrated in Listing A.15.

Listing A.15: Moving files with mv.

```
FN11194:Documents sporring$ echo mv hi.txt myFolder/FN11194:Documents sporring$
```

To delete the file and the directory, use *rm* and *rmdir*, as shown in Listing A.16.

Listing A.16: Deleting files and directories.

```
FN11194:Documents sporring$ cd myFolder/
FN11194:myFolder sporring$ rm hi.txt
FN11194:myFolder sporring$ cd ..
FN11194:Documents sporring$ rmdir myFolder/
FN11194:Documents sporring$ ls
FN11194:Documents sporring$
```

Only commands found on the *search path* are available in the console. The content of the search path is seen using the **echo** command, as demonstrated in Listing A.17.

Listing A.17: The content of the search path.

```
FN11194:Documents sporring$ echo $PATH
/Applications/Maple
    17/:/Applications/PackageMaker.app/Contents/MacOS/:
    /Applications/MATLAB_R2014b.app/bin/:/opt/local/bin:
    /opt/local/sbin:/usr/local/bin:/usr/bin:/usr/sbin:
    /sbin:/opt/X11/bin:/Library/TeX/texbin
FN11194:Documents sporring$
```

The search path can be changed by editing the setup file for Bash. On MacOS X it is called \sim /.profile, and on Linux it is either \sim /.bash_profile or \sim /.bashrc.

Here new paths can be added by adding the following line: export PATH="<new path>:<another new path>:\$PATH".

A useful feature of Bash is that the console can help you write commands. E.g., if you write fs followed by pressing the tab-key, and if Mono is in the search path, then Bash will typically respond by completing the line as fsharp, and by further pressing the tab-key some times, Bash will show the list of options, typically fshpari and fsharpc. Also, most commands have an extensive manual which can be accessed using the man command. E.g., the manual for rm is retrieved by man rm.

Appendix B

Number Systems on the Computer

B.1 Binary Numbers

Humans like to use the *decimal number* system for representing numbers. Decimal numbers are *base* 10 meaning that a decimal number consists of a sequence of digits separated by a *decimal point*, where each *digit* can have values $d \in \{0, 1, 2, ..., 9\}$ and the weight of each digit is proportional to its place in the sequence of digits with respect to the decimal point, i.e., the number $357.6 = 3 \cdot 10^2 + 5 \cdot 10^1 + 7 \cdot 10^0 + 6 \cdot 10^{-1}$, or in general, for a number consisting of digits d_i with n + 1 and m digits to the left and right of the decimal point, the value v is calculated as:

$$v = \sum_{i=-m}^{n} d_i 10^i. (B.1)$$

The basic unit of information in almost all computers is the binary digit, or *bit* for short. A *binary number* consists of a sequence of binary digits separated by a decimal point, where each digit can have values $b \in \{0, 1\}$, and the base is 2. The general equation is,

$$v = \sum_{i=-m}^{n} b_i 2^i, \tag{B.2}$$

and examples are $1011.1_2 = 1 \cdot 2^3 + 0 \cdot 2^2 + 1 \cdot 2^1 + 1 \cdot 2^0 + 1 \cdot 2^{-1} = 11.5$. Notice that we use subscript 2 to denote a binary number, while no subscript is used for decimal numbers. The left-most bit is called the *most significant bit*, and the right-most bit is called the *least significant bit*. Due to typical organisation of computer memory, 8 binary digits is called a *byte*, and the term *word* is not universally defined but typically related to the computer architecture, a program is running on, such as 32 or 64 bits.

Other number systems are often used, e.g., octal numbers, which are base 8 numbers and have digits $o \in \{0, 1, ..., 7\}$. Octals are useful short-hand for binary, since 3 binary digits map to the set of octal digits. Likewise, hexadecimal numbers are base 16 with digits $h \in \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, a, b, c, d, e, f\}$, such that $a_{16} = 10$, $b_{16} = 11$ and so on. Hexadecimals are convenient, since 4 binary digits map directly to the set of hexadecimal digits. Thus $367 = 101101111_2 = 557_8 = 16f_{16}$. A list of the integers 0–63 in various bases is given in Table B.1.

| Dec | Bin | Oct | Hex | Dec | Bin | Oct | Hex |
|-----|-------|-----|-----|-----|---------|-----|-----|
| 0 | 0 | 0 | 0 | 32 | 100000 | 40 | 20 |
| 1 | 1 | 1 | 1 | 33 | 100001 | 41 | 21 |
| 2 | 10 | 2 | 2 | 34 | 100010 | 42 | 22 |
| 3 | 11 | 3 | 3 | 35 | 100011 | 43 | 23 |
| 4 | 100 | 4 | 4 | 36 | 100100 | 44 | 24 |
| 5 | 101 | 5 | 5 | 37 | 100101 | 45 | 25 |
| 6 | 110 | 6 | 6 | 38 | 100110 | 46 | 26 |
| 7 | 111 | 7 | 7 | 39 | 100111 | 47 | 27 |
| 8 | 1000 | 10 | 8 | 40 | 101000 | 50 | 28 |
| 9 | 1001 | 11 | 9 | 41 | 101001 | 51 | 29 |
| 10 | 1010 | 12 | a | 42 | 101010 | 52 | 2a |
| 11 | 1011 | 13 | b | 43 | 101011 | 53 | 2b |
| 12 | 1100 | 14 | С | 44 | 101100 | 54 | 2c |
| 13 | 1101 | 15 | d | 45 | 101101 | 55 | 2d |
| 14 | 1110 | 16 | e | 46 | 101110 | 56 | 2e |
| 15 | 1111 | 17 | f | 47 | 101111 | 57 | 2f |
| 16 | 10000 | 20 | 10 | 48 | 110000 | 60 | 30 |
| 17 | 10001 | 21 | 11 | 49 | 110001 | 61 | 31 |
| 18 | 10010 | 22 | 12 | 50 | 110010 | 62 | 32 |
| 19 | 10011 | 23 | 13 | 51 | 110011 | 63 | 33 |
| 20 | 10100 | 24 | 14 | 52 | 110100 | 64 | 34 |
| 21 | 10101 | 25 | 15 | 53 | 110101 | 65 | 35 |
| 22 | 10110 | 26 | 16 | 54 | 110110 | 66 | 36 |
| 23 | 10111 | 27 | 17 | 55 | 110111 | 67 | 37 |
| 24 | 11000 | 30 | 18 | 56 | 111000 | 70 | 38 |
| 25 | 11001 | 31 | 19 | 57 | 111001 | 71 | 39 |
| 26 | 11010 | 32 | 1a | 58 | 111010 | 72 | 3a |
| 27 | 11011 | 33 | 1b | 59 | 111011 | 73 | 3b |
| 28 | 11100 | 34 | 1c | 60 | 111100 | 74 | 3c |
| 29 | 11101 | 35 | 1d | 61 | 111101 | 75 | 3d |
| 30 | 11110 | 36 | 1e | 62 | 111110 | 76 | 3e |
| 31 | 11111 | 37 | 1f | 63 | 1111111 | 77 | 3f |

Table B.1 A list of the integers 0-63 in decimal, binary, octal, and hexadecimal.

B.2 IEEE 754 Floating Point Standard

The set of real numbers, also called *reals*, includes all fractions and irrational numbers. It is infinite in size both in the sense that there is no largest nor smallest number,

and that between any 2 given numbers there are infinitely many numbers. Reals are widely used for calculation, but since any computer only has finite memory, there are infinitely many numbers which cannot be represent on a computer. Hence, any computation performed on a computer with reals must rely on approximations. *IEEE 754 double precision floating-point format (binary64)*, known as a *double*, is a standard for representing an approximation of reals using 64 bits. These bits are divided into 3 parts: sign, exponent and fraction,

$$s e_1 e_2 \dots e_{11} m_1 m_2 \dots m_{52}$$

where s, e_i , and m_j are binary digits. The bits are converted to a number using the equation by first calculating the exponent e and the mantissa m,

$$e = \sum_{i=1}^{11} e_i 2^{11-i}, \tag{B.3}$$

$$m = \sum_{j=1}^{52} m_j 2^{-j}.$$
 (B.4)

I.e., the exponent is an integer, where $0 \le e < 2^{11}$, and the mantissa is a rational, where $0 \le m < 1$. For most combinations of e and m, the real number v is calculated as

$$v = (-1)^{s} (1+m) 2^{e-1023}$$
(B.5)

with the exceptions that

| | *** | $m \neq 0$ |
|------------------|------------------------------|---------------------------------------|
| e = 0 | $v = (-1)^s 0$ (signed zero) | $v = (-1)^s m2^{1-1023}$ (subnormals) |
| $e = 2^{11} - 1$ | $v = (-1)^s \infty$ | $v = (-1)^s$ NaN (not-a-number) |

where $e = 2^{11} - 1 = 111111111111_2 = 2047$. The largest and smallest number that is not infinity is thus

$$e = 2^{11} - 2 = 2046,$$
 (B.6)

$$m = \sum_{j=1}^{52} 2^{-j} = 1 - 2^{-52} \approx 1,$$
 (B.7)

$$v_{\text{max}} = \pm \left(2 - 2^{-52}\right) 2^{1023} \simeq \pm 2^{1024} \simeq \pm 10^{308}.$$
 (B.8)

The density of numbers varies in such a way that when e - 1023 = 52, then

$$v = (-1)^{s} \left(1 + \sum_{j=1}^{52} m_j 2^{-j} \right) 2^{52}$$
 (B.9)

$$= \pm \left(2^{52} + \sum_{j=1}^{52} m_j 2^{-j} 2^{52}\right)$$
 (B.10)

$$= \pm \left(2^{52} + \sum_{j=1}^{52} m_j 2^{52-j}\right)$$
 (B.11)

$$\stackrel{k=52-j}{=} \pm \left(2^{52} + \sum_{k=51}^{0} m_{52-k} 2^k \right), \tag{B.12}$$

which are all integers in the range $2^{52} \le |v| < 2^{53}$. When e - 1023 = 53, then the same calculation gives

$$v \stackrel{k=53-j}{=} \pm \left(2^{53} + \sum_{k=52}^{1} m_{53-k} 2^k\right),$$
 (B.13)

which are every second integer in the range $2^{53} \le |v| < 2^{54}$, and so on for larger values of e. When e - 1023 = 51, the same calculation gives,

$$v \stackrel{k=51-j}{=} \pm \left(2^{51} + \sum_{k=50}^{-1} m_{51-k} 2^k\right),$$
 (B.14)

which is a distance between numbers of 1/2 in the range $2^{51} \le |v| < 2^{52}$, and so on for smaller values of e. Thus we may conclude that the distance between numbers in the interval $2^n \le |v| < 2^{n+1}$ is 2^{n-52} , for $-1022 = 1 - 1023 \le n < 2046 - 1023 = 1023$. For subnormals, the distance between numbers is

$$v = (-1)^s \left(\sum_{j=1}^{52} m_j 2^{-j} \right) 2^{-1022}$$
 (B.15)

$$= \pm \left(\sum_{j=1}^{52} m_j 2^{-j} 2^{-1022}\right) \tag{B.16}$$

$$= \pm \left(\sum_{j=1}^{52} m_j 2^{-j-1022}\right) \tag{B.17}$$

$$\stackrel{k=-j-1022}{=} \pm \left(\sum_{j=-1023}^{-1074} m_{-k-1022} 2^k \right), \tag{B.18}$$

which gives a distance between numbers of $2^{-1074} \simeq 10^{-323}$ in the range $0 < |v| < 2^{-1022} \simeq 10^{-308}$.

Appendix C

Commonly Used Character Sets

Letters, digits, symbols, and space are the core of how we store data, write programs, and communicate with computers and each other. These symbols are in short called characters and represent a mapping between numbers, also known as codes, and a pictorial representation of the character. E.g., the ASCII code for the letter 'A' is 65. These mappings are for short called character sets, and due to differences in natural languages and symbols used across the globe, many different character sets are in use. E.g., the English alphabet contains the letters 'a' to 'z'. These letters are common to many other European languages which in addition use even more symbols and accents. For example, Danish has further the letters 'æ', 'ø', and 'å'. Many non-European languages have completely different symbols, where the Chinese character set is probably the most extreme, and some definitions contain 106,230 different characters, albeit only 2,600 are included in the official Chinese language test at the highest level.

Presently, the most common character set used is Unicode Transformation Format (UTF), whose most popular encoding schemes are 8-bit (UTF-8) and 16-bit (UTF-16). Many other character sets exist, and many of the later build on the American Standard Code for Information Interchange (ASCII). The ISO-8859 codes were an intermediate set of character sets that are still in use, but which is greatly inferior to UTF. Here we will briefly give an overview of ASCII, ISO-8859-1 (Latin1), and UTF.

C.1 ASCII

The American Standard Code for Information Interchange (ASCII) [8], is a 7 bit code tuned for the letters of the English language, numbers, punctuation symbols, control codes and space, see Tables C.1 and C.2. The first 32 codes are reserved for

| x0+0x | 00 | 10 | 20 | 30 | 40 | 50 | 60 | 70 |
|-------|-----|-----|----|----|----|----|----|-----|
| 00 | NUL | DLE | SP | 0 | @ | P | • | р |
| 01 | SOH | DC1 | ! | 1 | A | Q | a | q |
| 02 | STX | DC2 | " | 2 | В | R | b | r |
| 03 | ETX | DC3 | # | 3 | С | S | c | S |
| 04 | EOT | DC4 | \$ | 4 | D | T | d | t |
| 05 | ENQ | NAK | % | 5 | Е | U | e | u |
| 06 | ACK | SYN | & | 6 | F | V | f | v |
| 07 | BEL | ETB | , | 7 | G | W | g | W |
| 08 | BS | CAN | (| 8 | Н | X | h | х |
| 09 | HT | EM |) | 9 | I | Y | i | y |
| 0A | LF | SUB | * | : | J | Z | j | Z |
| 0B | VT | ESC | + | ; | K | [| k | { |
| 0C | FF | FS | , | < | L | \ | 1 | |
| 0D | CR | GS | - | = | M |] | m | } |
| 0E | SO | RS | | > | N | ٨ | n | ~ |
| 0F | SI | US | / | ? | O | _ | 0 | DEL |

Table C.1 ASCII

non-printable control characters to control printers and similar devices or to provide meta-information. The meaning of each control character is not universally agreed upon.

The code order is known as *ASCIIbetical order*, and it is sometimes used to perform arithmetic on codes, e.g., an uppercase letter with code *c* may be converted to lower case by adding 32 to its code. The ASCIIbetical order also has a consequence for sorting, i.e., when sorting characters according to their ASCII code, 'A' comes before 'a', which comes before the symbol '{'.

C.2 ISO/IEC 8859

The ISO/IEC 8859 report http://www.iso.org/iso/catalogue_detail?csnumber= 28245 defines 10 sets of codes specifying up to 191 codes and graphics characters using 8 bits. Set 1, also known as ISO/IEC 8859-1, Latin alphabet No. 1, or *Latin1*, covers many European languages and is designed to be compatible with ASCII, such that code for the printable characters in ASCII is the same in ISO 8859-1. Table C.3 shows the characters above 7e. Codes 00-1f and 7f-9f are undefined in ISO 8859-1.

351 C.3 Unicode

| Code | Description |
|------------|---------------------------|
| NUL | Null |
| SOH | Start of heading |
| STX | Start of text |
| ETX | End of text |
| EOT | End of transmission |
| ENQ | Enquiry |
| ACK | Acknowledge |
| BEL | Bell |
| BS | Backspace |
| HT | Horizontal tabulation |
| LF | Line feed |
| VT | Vertical tabulation |
| FF | Form feed |
| CR | Carriage return |
| SO | Shift out |
| SI | Shift in |
| DLE | Data link escape |
| DC1 | Device control one |
| DC2 | Device control two |
| DC3 | Device control three |
| DC4 | Device control four |
| NAK | Negative acknowledge |
| SYN | Synchronous idle |
| ETB | End of transmission block |
| CAN | Cancel |
| EM | End of medium |
| SUB | Substitute |
| ESC | Escape |
| FS | File separator |
| GS | Group separator |
| RS | Record separator |
| US | Unit separator |
| SP | Space |
| DEL | Delete |

Table C.2 ASCII symbols.

C.3 Unicode

Unicode is a character standard defined by the Unicode Consortium, http://unicode.org, as the *Unicode Standard*. Unicode allows for 1,114,112 different codes. Each code is called a *code point* which represents an abstract character. Code points are divided into 17 planes, each with $2^{16} = 65,536$ code points. Planes are further subdivided into named *blocks*. The first plane is called the *Basic Multilingual plane* and its block of the first 128 code points is called the *Basic Latin block* and is identical to ASCII, see Table C.1, and code points 128-255 are called the *Latin-1 Supplement block*, and are identical to the upper range of ISO 8859-1, see Table C.3. Each code-point has a number of attributes such as the *Unicode general category*. Presently more than 128,000 code points are defined as covering 135 modern and historical writing systems, and obtained

| x0+0x | 80 | 90 | A0 | В0 | C0 | D0 | E0 | F0 |
|-------|----|----|------|--------------------------|----|----|----|----|
| 00 | | | NBSP | 0 | À | Đ | à | ð |
| 01 | | | i | ± | Á | Ñ | á | ñ |
| 02 | | | ¢ | 2 | Â | Ò | â | ò |
| 03 | | | £ | 3 | Ã | Ó | ã | ó |
| 04 | | | ¤ | , | Ä | Ô | ä | ô |
| 05 | | | ¥ | μ | Å | Õ | å | õ |
| 06 | | | - | ¶ | Æ | Ö | æ | ö |
| 07 | | | § | • | Ç | × | ç | ÷ |
| 08 | | | | 3 | È | Ø | è | ø |
| 09 | | | © | 1 | É | Ù | é | ù |
| 0a | | | a | Ω | Ê | Ú | ê | ú |
| 0b | | | « | » | Ë | Û | ë | û |
| 0c | | | Г | $\frac{1}{4}$ | Ì | Ü | ì | ü |
| 0d | | | SHY | $\frac{1}{2}$ | Í | Ý | í | ý |
| 0e | | | ® | $\frac{\overline{3}}{4}$ | Î | Þ | î | þ |
| Of | | | - | i | Ϊ | В | ï | ÿ |

Table C.3 ISO-8859-1 (latin1) non-ASCII part. Note that the codes 7f – 9f are undefined.

| | Description |
|------|---------------------|
| NBSP | Non-breakable space |
| SHY | Soft hypen |

Table C.4 ISO-8859-1 special symbols.

at http://www.unicode.org/Public/UNIDATA/UnicodeData.txt, which includes the code point, name, and general category.

A Unicode code point is an abstraction from the encoding and the graphical representation of a character. A code point is written as "U+" followed by its hexadecimal number, and for the Basic Multilingual plane, 4 digits are used, e.g., the code point with the unique name LATIN CAPITAL LETTER A has the Unicode code point "U+0041", and is in this text visualized as 'A'. More digits are used for code points of the remaining planes.

The general category is used to specify valid characters that do not necessarily have a visual representation but possibly transform text. Some categories and their letters in the first 256 code points are shown in Table C.5.

To store and retrieve code points, they must be encoded and decoded. A common encoding is *UTF-8*, which encodes code points as 1 to 4 bytes, and which is backward-compatible with ASCII and ISO 8859-1. Hence, in all 3 coding systems, the character with code 65 represents the character 'A'. Another popular encoding scheme is *UTF-16*, which encodes characters as 2 or 4 bytes, but which is not backward-compatible with ASCII or ISO 8859-1. UTF-16 is used internally in many compilers, interpreters, and operating systems.

353 C.3 Unicode

| General | Code points | Name |
|----------|-------------------------------|---|
| category | | |
| Lu | U+0041–U+005A, U+00C0–U+00D6, | Upper case letter |
| | U+00D8-U+00DE | |
| Ll | U+0061-U+007A, U+00B5, | Lower case letter |
| | U+00DF-U+00F6, U+00F8-U+00FF | |
| Lt | None | Digraphic letter, with first part uppercase |
| Lm | None | Modifier letter |
| Lo | U+00AA, U+00BA | Gender ordinal indicator |
| Nl | None | Letterlike numeric character |
| Pc | U+005F | Low line |
| Mn | None | Nonspacing combining mark |
| Mc | None | Spacing combining mark |
| Cf | U+00AD | Soft Hyphen |

 Table C.5
 Some general categories for the first 256 code points.

Appendix D

Common Language Infrastructure

The Common Language Infrastructure (CLI), not to be confused with Command Line Interface with the same acronym, is a technical standard developed by Microsoft [4, 3]. The standard specifies a language, its format, and a runtime environment that can execute the code. The main feature is that it provides a common interface between many languages and many platforms, such that programs can collaborate in a language-agnostic manner and can be executed on different platforms without having to be recompiled. Main features of the standard are:

Common Type System (CTS) which defines a common set of types that can be used across different languages as if it were their own.

Metadata which defines a common method for referencing programming structures such as values and functions in a language-independent manner.

Common Intermediate Language (CIL) which is a platform-independent, stack-based, object-oriented assembly language that can be executed by the Virtual Execution System.

Virtual Execution System (VES) which is a platform dependent, virtual machine, which combines the above into code that can be executed at runtime. Microsoft's implementation of VES is called *Common Language Runtime* (*CLR*) and uses *just-in-time* compilation. In this book, we have been using the mono command.

The process of running an F# program is shown in Figure D.1. First the F# code is compiled or interpreted to CIL. This code possibly combined with other CIL code is then converted to a machine-readable code, and the result is then executed on the platform.

CLI defines a *module* as a single file containing executable code by VES. Hence, CLI's notion of a module is somewhat related to F#'s notion of module, but the

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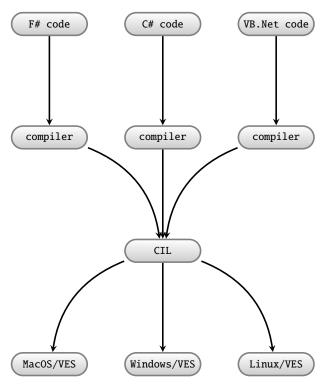


Fig. D.1 The relation between some .NET/Mono languages with the Common intermediate language (CIL), and the Virtual execution systems (VES) on some operating system (mono).

two should not be confused. A collection of modules, a *manifest*, and possibly other resources, which jointly define a complete program is called an *assembly*. The manifest is the description of which files are included in the assembly together with its version, name, security information, and other bookkeeping information.

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