# 11 | Collections of data

F# is tuned to work with collections of data, and there are several built-in types of collections with various properties making them useful for different tasks. Examples include strings, lists, arrays, and sequences. Strings were discussed in Chapter 5 and will be revisited here in more details. Sequences will not be discussed. and we will concentrate on lists and one- and two-dimensional arrays.

## 11.1 Strings

Strings have been discussed in Chapter 5 the content of which will be briefly revisited here followed by a description of some of the many supporting built-in functions in F# on strings.

· System.string

· verbatim string

A string is a sequence of characters. Each character is represented using UTF-16, see Appendix C for further details on the unicode standard. The type string is an alias for System.string. String literals are delimited by quotation marks "" and inside the delimiters, character escape sequences are allowed (see Table 5.2), which are replaced by the corresponding character code. Examples are "This is a string", "\tTabulated string", "A \"quoted\" string", and "". Strings may span several lines, and new lines inside strings are part of the string unless the line is ended with a backslash. Strings may be verbatim by preceding the string with "@", in which case escape sequences are not replaced, but a double quotation marks is an escape sequence which is replaced by a single, e.g., @"This is a string", @"\tNon-tabulated string", @"A ""quoted" string", and @"". Alternatively, a verbatim string may be delimited by tripple quotes, e.g., """This is a string""", """\tNon-tabulated string"", """A "quoted" string"", and """""". Strings may be indexed using the .[] notation, as demonstrated in Listing 5.27]

## 11.1.1 String properties

Strings have a few properties, which are values attached to each string and access using the "." notation. The only to be mentioned here is:

Length: Returns the length of the string. Compare with String.length method.

```
Listing 11.1: Length

| 'abcd'.Length;;
| val it : int = 4
```

<sup>&</sup>lt;sup>1</sup>Jon: Should we discuss sequences?

## 11.1.2 String module

In the String module the following functions are available.

String.collect: (char -> string) -> string -> string. Creates a new string whose characters are the results of applying a specified function to each of the characters of the input string and concatenating the resulting strings.

```
Listing 11.2: String.collect

1 > String.collect (fun c -> (string c) + ", ") "abc";;
2 val it : string = "a, b, c, "
```

String.concat: string -> seq<string> -> string. Returns a new string made by concatenating the given strings with a separator. Here seq<string> is a sequence but can also be a list or an array.

```
Listing 11.3: String.concat

1 > String.concat ", " ["abc"; "def"; "ghi"];;
2 val it : string = "abc, def, ghi"
```

String.exists: (char -> bool) -> string -> bool. Tests if any character of the string satisfies the given predicate.

```
Listing 11.4: String.exists

1 > String.exists (fun c -> c = 'd') "abc";;
2 val it : bool = false
```

String.forall: (char -> bool) -> string -> bool. Tests if all characters in the string satisfy the given predicate.

```
Listing 11.5: String.forall

1 > String.forall (fun c -> c < 'd') "abc";;
2 val it : bool = true
```

String.init: int -> (int -> string) -> string. Creates a new string whose characters are the results of applying a specified function to each index and concatenating the resulting strings.

```
Listing 11.6: String.init

1 > String.init 5 (fun i -> (string i) + ", ");;
2 val it : string = "0, 1, 2, 3, 4, "
```

String.iter: (char -> unit) -> string -> unit. Applies a specified function to each character in the string.

```
Listing 11.7: String.iter

1 > String.iter (fun c -> printfn "%c" c) "abc";;
2 a
3 b
4 c
5 val it : unit = ()
```

String.iteri: (int -> char -> unit) -> string -> unit. Applies a specified function to the index of each character in the string and the character itself.

```
Listing 11.8: String.iteri

> String.iteri (fun i c -> printfn "%d: %c" i c) "abc";;

0: a

1: b

2: c

val it : unit = ()
```

String.length: string -> int. Returns the length of the string.

```
Listing 11.9: String.length

String.length "abcd";;

val it : int = 4
```

String.map: (char -> char) -> string -> string. Creates a new string whose characters are the results of applying a specified function to each of the characters of the input string.

```
Listing 11.10: String.map

1 > let dc = int 'A' - int 'a'
2 - String.map (fun c -> c + char dc) "abcd";;
3 val dc : int = -32
4 val it : string = "ABCD"
```

String.mapi: (int -> char -> char) -> string -> string. Creates a new string whose characters are the results of applying a specified function to each character and index of the input string.

```
Listing 11.11: String.mapi

1 > String.mapi (fun i c -> char (int c + i)) "aaaa";;
2 val it : string = "abcd"
```

String.replicate: int -> string -> string. Returns a string by concatenating a specified number of instances of a string.

```
Listing 11.12: String.replicate

> String.replicate 4 "abc, ";;

val it : string = "abc, abc, abc, "
```

## 11.2 Lists

Lists are unions of immutable values of the same type and have a more flexible structure than tuples. · list
Lists can be expressed as a sequence expression, · sequence expression

```
Listing 11.13 Lists with a sequence expression.

[[<expr>{; <expr>}]]
```

Examples are [1; 2; 3; 4; 5], which represents a list of integers, ["This"; "is"; "a"; "list"], which represents a list of strings, [(fun x  $\rightarrow$  x); (fun x  $\rightarrow$  x\*x)], which represents a list of anonymous functions, and [], which is an empty list. Lists may also be given as ranges,

```
Listing 11.14 Lists with a range expressions.

1 [<expr> ... <expr> [... <expr>]]
```

where <expr> in range expressions must be of integers, floats, or characters. Examples are [1 .. 5], range expressions [-3.0 .. 2.0], and ['a' .. 'z']. Range expressions may include a step size, thus, [1 .. 2 .. 10] evaluates to [1; 3; 5; 7; 9].

A list type is identified with the *list* keyword, such that a list of integers has the type int list. ·list Like strings, lists may be indexed using the ".[]" notation, the lengths of lists is retrieved using the ·.[] · Length property, and we may test whether a list is empty using the *isEmpty* property. These features · Length are demonstrated in Listing [11.15]

```
Listing 11.15 listIndexing.fsx:
Lists are indexed as strings and has a Length property.

let printList (lst : int list) : unit =
for i = 0 to lst.Length - 1 do
printf "%A " lst.[i]
printfn ""

let lst = [3; 4; 5]
printfn "lst = %A, lst.[i] = %A" lst lst.[i]
printfn "lst.Length = %A, lst.isEmpty = %A" lst.Length lst.IsEmpty
printList lst

$ fsharpc --nologo listIndexing.fsx && mono listIndexing.exe
lst = [3; 4; 5], lst.[i] = 4
lst.Length = 3, lst.isEmpty = false
3 4 5
```

F# implements lists as linked lists, see Figure 11.1 which is why indexing element i has computational complexity  $\mathcal{O}(i)$ , since the list has to be traversed from the beginning until element i is located. Thus, indexing lists is slow and should be avoided.

Advice

 $\cdot$  for

·in

Notice especially that lists are zero-indexed, and thus, the last element in a list lst is lst.Length -1. This is a very common source of error! Therefore, indexing in lists using *for*-loops is supported using a special notation with the *in* keyword,



Figure 11.1: A list is a linked list: Here is illustrated the linked list of ["This"; "is"; "a"; "list"].

```
Listing 11.16 For-in loop with in expression.

1 for <ident> in list> do <bodyExpr> [done]
```

In for-in loops, the loop runs through each element of the st>, and assigns it to the identifier <ident>. This is demonstrated in Listing [11.17].

```
Listing 11.17 listFor.fsx:

The loops are preferred over to.

1 let printList (lst : int list) : unit =
2 for elm in lst do
3 printf "%A " elm
4 printfn ""

5 printList [3; 4; 5]

1 $ fsharpc --nologo listFor.fsx && mono listFor.exe
2 3 4 5
```

Using for-in-expressions remove the risk of off-by-one indexing errors, and thus, for-in is to be Advice preferred over for-to.

Lists support slicing identically to strings as demonstrated in Listing 11.18.

```
Listing 11.18 listSlicing.fsx:
Examples of list slicing. Compare with Listing 5.27.
let lst = ['a' .. 'g']
printfn "%A" lst.[0]
printfn "%A" lst.[3]
printfn "%A" lst.[3..]
printfn "%A" lst.[..3]
printfn "%A" lst.[1..3]
printfn "%A" lst.[*]
$ fsharpc --nologo listSlicing.fsx && mono listSlicing.exe
'a'
'd'
['d'; 'e'; 'f'; 'g']
['a'; 'b'; 'c'; 'd']
['b'; 'c'; 'd']
 ['a'; 'b'; 'c'; 'd'; 'e'; 'f'; 'g']
```

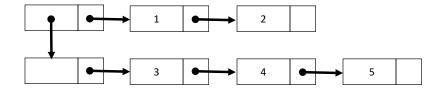


Figure 11.2: A list is a ragged linked list: Here is illustrated the linked list of [[1;2];[3;4;5]].

Lists may be concatenated using either the " $\mathcal{O}$ " concatenation operator or the "::" cons operators.  $\cdot$  C

The differences is that " $\mathcal{O}$ " concatenates two lists of identical types, while "::" concatenates an element and a list of identical types. This is demonstrated in Listing 11.19.

List concatenation :::

· list concatenation

```
Listing 11.19 listCon.fsx:

Examples of list concatenation.

1 printfn "[1] @ [2; 3] = %A" ([1] @ [2; 3])
2 printfn "[1; 2] @ [3; 4] = %A" ([1; 2] @ [3; 4])
3 printfn "1 :: [2; 3] = %A" (1 :: [2; 3])

1 $ fsharpc --nologo listCon.fsx && mono listCon.exe
2 [1] @ [2; 3] = [1; 2; 3]
3 [1; 2] @ [3; 4] = [1; 2; 3; 4]
4 1 :: [2; 3] = [1; 2; 3]
```

Since lists are represented as linked lists, then the cons operator is very efficient and has computational complexity  $\mathcal{O}(1)$ , while concatenation has computational complexity  $\mathcal{O}(n)$ , where n is the length of the first list.

It is possible to make multidimensional lists as lists of lists as shown in Listing 11.20.

```
Listing 11.20 listMultidimensional.fsx:

A ragged multidimensional list, built as lists of lists, and its indexing.

1 let a = [[1;2];[3;4;5]]
2 let row = a.Item 0 in printfn "%A" row
3 let elm = row.Item 1 in printfn "%A" elm
4 let elm = (a.Item 0).Item 1 in printfn "%A" elm

1 $ fsharpc --nologo listMultidimensional.fsx
2 $ mono listMultidimensional.exe
3 [1; 2]
4 2
5 2
```

The example shows a ragged multidimensional list since each row has a different number of elements. · ragged This is also illustrated in Figure 11.2. multidimensional list since each row has a different number of elements. · ragged multidimensional list since each row has a different number of elements.

ragged multidimensional list

The indexing of a particular element is slow due to the linked list implementation of lists, which is

<sup>&</sup>lt;sup>2</sup>Jon: why does the at-symbol not appear in the index?

why arrays are often preferred for two- and higher-dimensional data structures, see Section 11.3.

## 11.2.1 List properties

Lists support a number of properties, i.e., values that are attached to each list and access using the "." notation, some of which are:

Head: Returns the first element of a list.

```
Listing 11.21: Head

1 > [1; 2; 3]. Head;;
2 val it : int = 1
```

IsEmpty: Returns true if the list is empty.

```
Listing 11.22: Head

1 > [1; 2; 3].IsEmpty;;
2 val it : bool = false
```

Length: Returns the number of elements in the list.

```
Listing 11.23: Length

1 > [1; 2; 3].Length;;
2 val it : int = 3
```

Tail: Returns the list except its first element.

```
Listing 11.24: Tail

1 > [1; 2; 3]. Tail;;
2 val it : int list = [2; 3]
```

## 11.2.2 List module

The built-in List module contains a wealth of functions for lists, some of which are briefly summarized below:

List.collect: ('T -> 'U list) -> 'T list -> 'U list. Apply the supplied function to each element in a list and return a concatenated list of the results.

```
Listing 11.25: List.collect

1 > List.collect (fun elm -> [elm; elm; elm]) [1; 2; 3];;
2 val it : int list = [1; 1; 1; 2; 2; 2; 3; 3; 3]
```

List.contains: 'T -> 'T list -> bool. Returns true or false depending on whether an element is contained in the list.

```
Listing 11.26: List.contains

1 > List.contains 3 [1; 2; 3];;
2 val it : bool = true
```

List.empty: 'T list. An empty list of inferred type.

```
Listing 11.27: List.empty

1 > let a : int list = List.empty;;
2 val a : int list = []
```

List.exists: ('T -> bool) -> 'T list -> bool. Returns true or false depending on whether any element is true for a given function.

```
Listing 11.28: List.exists

1 > let odd x = (x % 2 = 1) in List.exists odd [0 .. 2 .. 4];;
2 val it : bool = false
```

List.filter: ('T -> bool) -> 'T list -> 'T list. Returns a new list, of all the elements of the original list for which the supplied function evaluates to true.

```
Listing 11.29: List.filter

1  > let odd x = (x % 2 = 1) in List.filter odd [0 .. 9];;
2  val it : int list = [1; 3; 5; 7; 9]
```

List.find: ('T -> bool) -> 'T list -> 'T. Return the first element for which the given function is true.

```
Listing 11.30: List.find

1 > let odd x = (x % 2 = 1) in List.find odd [0 .. 9];;
2 val it : int = 1
```

List.findIndex: ('T -> bool) -> 'T list -> int. Return the index of the first element for which the given function is true.

List.fold: ('State -> 'T -> 'State) -> 'State -> 'T list -> 'State. Update an accumulator iteratively by applying the supplied function to each element in a list, e.g. for a list consisting of  $x_0, x_1, x_2, \ldots, x_n$ , a supplied function f, and an initial value for the accumulator s, calculate  $f(\ldots f(f(s, x_0), x_1), x_2), \ldots, x_n)$ .

```
Listing 11.32: List.fold

1 > let addSquares acc elm = acc + elm*elm
2 - List.fold addSquares 0 [0 .. 9];;
3 val addSquares : acc:int -> elm:int -> int
4 val it : int = 285
```

List.foldBack: ('T -> 'State -> 'State) -> 'T list -> 'State -> 'State. Update an accumulator iteratively by applying function to each element in a list, e.g. for a list consisting of  $x_0, x_1, x_2, \ldots, x_n$ , a supplied function f, and an initial value for the accumulator s, calculate  $f(x_0, f(x_1, f(x_2, \ldots, f(x_n, s))))$ .

```
Listing 11.33: List.foldBack

1 > let addSquares elm acc = acc + elm*elm
2 - List.foldBack addSquares [0 .. 9] 0;;
3 val addSquares : elm:int -> acc:int -> int
4 val it : int = 285
```

List.forall: ('T -> bool) -> 'T list -> bool. Apply a function to all element and logically and the result.

List.head: 'T list -> int. The first element in the list. Exception if empty.

```
Listing 11.35: List.head

1 > let a = [1; -2; 0] in List.head a;;
2 val it : int = 1
```

List.isEmpty: 'T list -> int. Compare with the empty list

List.item: 'T list -> int. Retrieve an element of a list by its index.

```
Listing 11.37: List.item

1 > let a = [1; -3; 0] in List.item 1 a;;
2 val it : int = -3
```

List.iter: ('T -> unit) -> 'T list -> unit. Apply a procedure to every element in the list.

List.Length: 'T list -> int. The number of elements in a list

```
Listing 11.39: List.Length

1 > List.length [1; 2; 3];;
2 val it : int = 3
```

List.map: ('T -> 'U) -> 'T list -> 'U list. Return a list, where the supplied function has been applied to every element.

```
Listing 11.40: List.map

1 > let square x = x*x in List.map square [0 .. 9];;
2 val it : int list = [0; 1; 4; 9; 16; 25; 36; 49; 64; 81]
```

List.ofArray: 'T list -> int. Return a list whose elements are the same as the supplied array.

```
Listing 11.41: List.ofArray

1 > List.ofArray [|1; 2; 3|];;
2 val it : int list = [1; 2; 3]
```

List.rev: 'T list -> 'T list. Return a list whose elements have been reversed.

```
Listing 11.42: List.rev

1 > List.rev [1; 2; 3];;
2 val it : int list = [3; 2; 1]
```

List.sort: 'T list -> 'T list. Return a list whos elements have been sorted.

```
Listing 11.43: List.sort

1 > List.sort [3; 1; 2];;
2 val it : int list = [1; 2; 3]
```

List.tail: 'T list -> 'T list. The list except its first element. Exception if empty.

List.toArray: 'T list -> 'T []. Return an array whos elements are the same as the supplied list.

```
Listing 11.45: List.toArray

1 > List.toArray [1; 2; 3];;
2 val it : int [] = [|1; 2; 3|]
```

List.unzip: ('T1 \* 'T2) list -> 'T1 list \* 'T2 list. Return a pair of lists, whos elements are take from pairs of a list.

List.zip: 'T1 list -> 'T2 list -> ('T1 \* 'T2) list. Return a list of pairs, whos elements are take iteratively from two lists.

```
Listing 11.47: List.zip

1 > List.zip [1; 2; 3] ['a'; 'b'; 'c'];;
2 val it : (int * char) list = [(1, 'a'); (2, 'b'); (3, 'c')]
```

## 11.3 Arrays

One dimensional arrays or just arrays for short are mutable lists of the same type and follow a similar syntax as lists. Arrays can be stated as sequence expressions, sequence expressions

```
Listing 11.48 Arrays with a sequence expression.

[|[<expr>{; <expr>}]|]
```

and examples are [|1; 2; 3; 4; 5|], which is an array of integers, [|"This"; "is"; "an"; "array"|], which is an array of strings, [|(fun  $x \rightarrow x$ ); (fun  $x \rightarrow x*x$ )|], which is an array of anonymous functions, and [||], which is an empty array. Arrays may also be given as ranges,

```
Listing 11.49 Arrays with a range expressions.

[|<expr> ... <expr> [... <expr>]|]
```

but arrays of range expressions must be of <expr> integers, floats, or characters. Examples are ·range expressions [|1 .. 5|], [|-3.0 .. 2.0|], and [|'a' .. 'z'|]. Range expressions may include a step size, thus, [|1 .. 2 .. 10|] evaluates to [|1; 3; 5; 7; 9|].

The array type is defined using the array keyword or alternatively the "[]" lexeme. Like strings and lists, arrays may be indexed using the ".[]" notation. Arrays cannot be resized, but are mutable as ..[] shown in Listing [11.50].

```
Listing 11.50 arrayReassign.fsx:
    Arrays are mutable in spite the missing mutable keyword.

1 let square (a : int array) =
    for i = 0 to a.Length - 1 do
    a.[i] <- a.[i] * a.[i]

4 let A = [| 1; 2; 3; 4; 5 |]
    printfn "%A" A

square A
    printfn "%A" A

1 $ fsharpc --nologo arrayReassign.fsx && mono arrayReassign.exe
    [|1; 2; 3; 4; 5|]
    [|1; 4; 9; 16; 25|]
```

Notice that in spite the missing mutable keyword, the function square still had the side-effect of squaring all entries in A. F# implements arrays as chunks of memory and indexes arrays via address arithmetic. I.e., element i in an array, whose first element is in memory address  $\alpha$  and whose elements fill  $\beta$  addresses each is found at address  $\alpha + i\beta$  Hence, indexing has computational complexity of  $\mathcal{O}(1)$ , but appending and prepending values to arrays and array concatenation requires copying the new and existing values to a fresh area in memory and thus has computational complexity  $\mathcal{O}(n)$ , where n is the total number of elements. Thus, indexing arrays is fast, but cons and concatenation Advice is slow and should be avoided.

Arrays support *slicing*, that is, indexing an array with a range results in a copy of the array with  $\cdot$  slicing values corresponding to the range. This is demonstrated in Listing 11.51

<sup>&</sup>lt;sup>3</sup>Jon: Add a figure illustrating address indexing.

## Listing 11.51 arraySlicing.fsx: Examples of array slicing. Compare with Listing 11.18 and Listing 5.27. let arr = [|'a' .. 'g'|] printfn "%A" arr.[0] printfn "%A" arr.[3] printfn "%A" arr.[3..] printfn "%A" arr.[..3] printfn "%A" arr.[1..3] printfn "%A" arr.[\*] \$ fsharpc --nologo arraySlicing.fsx && mono arraySlicing.exe 'a' 'd' [|'d'; 'e'; 'f'; 'g'|] [|'a'; 'b'; 'c'; 'd'|] [|'b'; 'c'; 'd'|] [|'a'; 'b'; 'c'; 'd'; 'e'; 'f'; 'g'|]

As illustrated, the missing start or end index implies from the first or to the last element.

Arrays have explicit operator support for appending and concatenation, instead the Array namespace includes an Array.append function, as shown in Listing 11.52.

Arrays are reference types, meaning that identifiers are references and thus suffers from aliasing, as reference types illustrated in Listing 11.53.

```
Listing 11.53 arrayAliasing.fsx:
Arrays are reference types and suffer from aliasing.

let a = [|1; 2; 3|];
let b = a
a.[0] <- 0
printfn "a = %A, b = %A" a b;;

fsharpc --nologo arrayAliasing.fsx && mono arrayAliasing.exe
a = [|0; 2; 3|], b = [|0; 2; 3|]
```

## 11.3.1 Array properties and methods

Arrays support a number of properties and methods, i.e., values and functions that are attached to each array and access using the "." notation, some of which are:

Clone(): Returns a copy of the array.

Length: Returns the number of elements in the array.

## 11.3.2 Array module

There are quite a number of built-in procedures for arrays in the Array module, some of which are summarized below 4

Array.append: 'T [] -> 'T []. Creates an array that contains the elements of one array followed by the elements of another array.

```
Listing 11.56: Array.append

1 > Array.append [|1; 2;|] [|3; 4; 5|];;
2 val it : int [] = [|1; 2; 3; 4; 5|]
```

Array.compareWith: ('T -> 'T -> int) -> 'T [] -> int. Compares two arrays using the given comparison function, element by element.

```
Listing 11.57: Array.compareWith

| Solid compart | clm2 | clm2 | clm2 | clm2 | clm2 | clm4 | clm5 | clm5 | clm6 |
```

<sup>&</sup>lt;sup>4</sup>Jon: rewrite description

Array.concat: seq<'T []> -> 'T []. Creates an array that contains the elements of each of the supplied sequence of arrays.

```
Listing 11.58: Array.concat

| > Array.concat [[|1; 2; 3|]; [|4; 5|]; [|6; 7; 8|]];;
| val it : int [] = [|1; 2; 3; 4; 5; 6; 7; 8|]
```

Array.contains: • Evaluates to true if the given element is in the input array.

```
Listing 11.59: Array.contains

1 > Array.contains 3 [|1; 2; 3|];;
2 val it : bool = true
```

Array.copy: 'T [] -> 'T []. Creates an array that contains the elements of the supplied array.

```
Listing 11.60: Array.copy

1 > let a = [|1; 2; 3|]
2 - let b = Array.copy a;;
3 val a : int [] = [|1; 2; 3|]
4 val b : int [] = [|1; 2; 3|]
```

Array.create: int -> 'T -> 'T []. Creates an array whose elements are initiallized the supplied value.

```
Listing 11.61: Array.create

1 > Array.create 4 3.14;;
2 val it : float [] = [|3.14; 3.14; 3.14; 3.14|]
```

Array.empty: 'T []. Returns an empty array of the given type.

```
Listing 11.62: Array.empty

1 > let a : int [] = Array.empty;;
2 val a : int [] = [||]
```

Array.exists: ('T  $\rightarrow$  bool)  $\rightarrow$  'T []  $\rightarrow$  bool. Tests whether any element of an array satisfies the supplied predicate.

```
Listing 11.63: Array.exists

1 > let odd x = (x % 2 = 1) in Array.exists odd [|0 .. 2 .. 4|];;
2 val it : bool = false
```

Array.fill: 'T [] -> int -> int -> 'T -> unit. Fills a range of elements of an array with the supplied value.

```
Listing 11.64: Array.fill

1 > let arr = Array.zeroCreate 10;
2 - Array.fill arr 2 5 2;;
3 val arr : int [] = [|0; 0; 2; 2; 2; 2; 0; 0; 0|]
4 val it : unit = ()
```

Array.filter: ('T -> bool) -> 'T [] -> 'T []. Returns a collection that contains only the elements of the supplied array for which the supplied condition returns true.

```
Listing 11.65: Array.filter

1 > let odd x = (x % 2 = 1) in Array.filter odd [|0 .. 9|];;
2 val it : int [] = [|1; 3; 5; 7; 9|]
```

Array.find: ('T -> bool) -> 'T [] -> 'T. Returns the first element for which the supplied function returns true. Raises System.Collections.Generic.KeyNotFoundException

```
Listing 11.66: Array.find

1 > let odd x = (x % 2 = 1) in Array.find odd [|0 .. 9|];;
2 val it : int = 1
```

Array.findIndex: ('T -> bool) -> 'T [] -> int. Returns the index of the first element in an array that satisfies the supplied condition. Raises System.Collections.Generic.KeyNotFoundException if none of the elements satisfy the condition.

Array.fold: ('State -> 'T -> 'State) -> 'State -> 'T [] -> 'State. Applies a function to each element of an array, threading an accumulator argument through the computation. If the input function is f and the array elements are i0...iN, this function computes f (...(f s i0)...) iN.

```
Listing 11.68: Array.fold

1 > let addSquares acc elm = acc + elm*elm
2 - Array.fold addSquares 0 [|0 .. 9|];;
3 val addSquares : acc:int -> elm:int -> int
4 val it : int = 285
```

Array.foldBack: ('T -> 'State -> 'State) -> 'T [] -> 'State -> 'State. Applies a function to each element of an array, threading an accumulator argument through the computation. If the input function is f and the array elements are i0...iN, this function computes f i0 (...(f iN s)).

```
Listing 11.69: Array.foldBack

1 > let addSquares elm acc = acc + elm*elm
2 - Array.foldBack addSquares [|0 .. 9|] 0;;
3 val addSquares : elm:int -> acc:int -> int
4 val it : int = 285
```

Array.forall: ('T -> bool) -> 'T [] -> bool. Tests whether all elements of an array satisfy the supplied condition.

```
Listing 11.70: Array.forall

1 > let odd x = (x % 2 = 1) in Array.forall odd [|0 .. 9|];;

2 val it : bool = false
```

Array.get: 'T [] -> int -> 'T. Gets an element from an array.

```
Listing 11.71: Array.get

1 > Array.get [|1; 2; 3|] 2;;
2 val it : int = 3
```

Array.init: int -> (int -> 'T) -> 'T []. Uses a supplied function to create an array of the supplied dimension.

Array.isEmpty: 'T [] -> bool. Tests whether an array has any elements.

```
Listing 11.73: Array.isEmpty

Array.isEmpty [||];;

val it : bool = true
```

Array.iter: ('T -> unit) -> 'T [] -> unit. Applies the supplied function to each element of an array.

```
Listing 11.74: Array.iter

1 > let prt x = printfn "%A " x in Array.iter prt [|0; 1; 2|];;
2 0
3 1
4 2
5 val it : unit = ()
```

Array.length: 'T [] -> int. Returns the length of an array. The System.Array.Length property does the same thing.

```
Listing 11.75: Array.length

1 > let a = [|1; 2; 3|] in a.Length;;
2 val it : int = 3
```

Array.map: ('T -> 'U) -> 'T [] -> 'U []. Creates an array whose elements are the results of applying the supplied function to each of the elements of a supplied array.

```
Listing 11.76: Array.map

1 > let square x = x*x in Array.map square [|0 .. 9|];;

2 val it : int [] = [|0; 1; 4; 9; 16; 25; 36; 49; 64; 81|]
```

Array.ofList: 'T list -> 'T []. Creates an array from the supplied list.

```
Listing 11.77: Array.ofList

1 > Array.ofList [1; 2; 3];;
2 val it : int [] = [|1; 2; 3|]
```

Array.rev: 'T [] -> 'T []. Reverses the order of the elements in a supplied array.

```
Listing 11.78: Array.rev

1 > Array.rev [|1; 2; 3|];;
2 val it : int [] = [|3; 2; 1|]
```

Array.set: 'T [] -> int -> 'T -> unit. Sets an element of an array.

```
Listing 11.79: Array.set

1 > let arr = [|1; 2; 3|]
2 - Array.set arr 2 10
3 - printfn "%A" arr;;
4 [|1; 2; 10|]
5 val arr : int [] = [|1; 2; 10|]
6 val it : unit = ()
```

Array.sort: 'T[] -> 'T []. Sorts the elements of an array and returns a new array. Operators.compare is used to compare the elements.

```
Listing 11.80: Array.sort

1 > Array.sort [|3; 1; 2|];;
2 val it : int [] = [|1; 2; 3|]
```

Array.sub: 'T [] -> int -> int -> 'T []. Creates an array that contains the supplied subrange, which is specified by starting index and length.

```
Listing 11.81: Array.sub

| Array.sub [|0..9|] 2 5;;
| val it : int [] = [|2; 3; 4; 5; 6|]
```

Array.toList: 'T [] -> 'T list. Converts the supplied array to a list.

```
Listing 11.82: Array.toList

| > Array.toList [|1; 2; 3|];;
| val it : int list = [1; 2; 3]
```

Array.unzip: ('T1 \* 'T2) [] -> 'T1 [] \* 'T2 []. Splits an array of tuple pairs into a tuple of two arrays.

```
Listing 11.83: Array.unzip

1 > Array.unzip [|(1, 'a'); (2, 'b'); (3, 'c')|];;
2 val it : int [] * char [] = ([|1; 2; 3|], [|'a'; 'b'; 'c'|])
```

Array.zip: 'T1 [] -> 'T2 [] -> ('T1 \* 'T2) []. Combines three arrays into an array of tuples that have three elements. The three arrays must have equal lengths; otherwise, System.ArgumentException is raised.

```
Listing 11.84: Array.zip

1 > Array.zip [|1; 2; 3|] [|'a'; 'b'; 'c'|];;
2 val it : (int * char) [] = [|(1, 'a'); (2, 'b'); (3, 'c')|]
```

## 11.4 Multidimensional arrays

Multidimensional arrays can be created as arrays of arrays (of arrays ...). These are known as jagged · multidimensional arrays since there is no inherent guarantee that all sub-arrays are of the same size. E.g., the example in Listing 11.85 is a jagged array of increasing width.

# Listing 11.85 arrayJagged.fsx: An array of arrays. When row lengths are of non-equal elements, then it is a Jagged array. let arr = [|[|1|]; [|1; 2|]; [|1; 2; 3|]|] for row in arr do for elm in row do printf "%A " elm printf "\n" \$ fsharpc --nologo arrayJagged.fsx && mono arrayJagged.exe 1 1 2 1 2 1 2 3

Indexing arrays of arrays is done sequentially, in the sense that in the above example, the number of outer arrays is a.Length, a.[i] is the i'th array, the length of the i'th array is a.[i].Length, and the j'th element of the i'th array is thus a.[i].[j]. Often 2-dimensional rectangular arrays are used, which can be implemented as a jagged array as shown in Listing 11.86.

```
Listing 11.86 arrayJaggedSquare.fsx:
A rectangular array.
let pownArray (arr : int array array) p =
  for i = 1 to arr.Length - 1 do
    for j = 1 to arr.[i].Length - 1 do
      arr.[i].[j] <- pown arr.[i].[j] p
let printArrayOfArrays (arr : int array array) =
  for row in arr do
    for elm in row do
      printf "%3d " elm
    printf "\n"
let A = [|[|1 ... 4|]; [|1 ... 2 ... 7|]; [|1 ... 3 ... 10|]|]
pownArray A 2
printArrayOfArrays A
$ fsharpc --nologo arrayJaggedSquare.fsx && mono arrayJaggedSquare.exe
      2 3 4
  1
         25 49
      9
  1
     16 49 100
```

Notice, the for-in cannot be used in pownArray, e.g.,

```
for row in arr do for elm in row do elm <- pown elm p done done,
```

since the iterator value elm is not mutable even though arr is an array. In fact, square arrays of dimensions 2 to 4 are so common that F# has built-in modules for their support. In the following, we describe Array2D. The workings of Array3D and Array4D are very similar. An example of creating Array3D the same 2-dimensional array as above but as an Array2D is shown in Listing 11.87.

Array4D

# Listing 11.87 array2D.fsx: Creating a 3 by 4 rectangular arrays of intigers. 1 let arr = Array2D.create 3 4 0 2 for i = 0 to (Array2D.length1 arr) - 1 do 3 for j = 0 to (Array2D.length2 arr) - 1 do 4 arr.[i,j] <- j \* Array2D.length1 arr + i 5 printfn "%A" arr 1 \$ fsharpc --nologo array2D.fsx && mono array2D.exe 2 [[0; 3; 6; 9] 3 [1; 4; 7; 10] 4 [2; 5; 8; 11]]

Notice that the indexing uses a slightly different notation [,] and the length functions are also slightly different. The statement A.Length would return the total number of elements in the array, in this case, 12. As can be seen, the printf supports direct printing of the 2-dimensional array. Higher dimensional arrays support slicing as shown in Listing 11.88.

```
Listing 11.88 array2DSlicing.fsx:
Examples of Array2D slicing. Compare with Listing 11.87.
let arr = Array2D.create 3 4 0
for i = 0 to (Array2D.length1 arr) - 1 do
  for j = 0 to (Array2D.length2 arr) - 1 do
     arr.[i,j] <- j * Array2D.length1 arr + i</pre>
printfn "%A" arr.[2,3]
printfn "%A" arr.[1..,3..]
printfn "%A" arr.[..1,*]
printfn "%A" arr.[1,*]
printfn "%A" arr.[1..1,*]
$ fsharpc --nologo array2DSlicing.fsx && mono array2DSlicing.exe
[[10]
 [11]]
[[0; 3; 6; 9]
 [1; 4; 7; 10]]
 [|1; 4; 7; 10|]
 [[1; 4; 7; 10]]
```

Note that in almost all cases, slicing produces a **sub** rectangular 2 dimensional **array** except for arr.[1,\*], which is an array, as can be seen by the single "[". In contrast, A.[1..1,\*] is an Array2D. Note also, that printfn typesets 2 dimensional arrays as [[ ... ]] and not [|[| ... |]|], which can cause confusion with lists of lists. [5]

Multidimensional arrays have the same properties and methods as arrays, see Section [11.3.1]

 $<sup>^5</sup>$ Jon: Array2D.ToString produces [[ ... ]] and not [|[| ... |]|], which can cause confusion.

## 11.4.1 Array2D module

There are quite a number of built-in procedures for arrays in the Array2D namespace, some of which are summarized below.

copy: 'T [,] -> 'T [,]. Creates a new array whose elements are the same as the input array.

create: int -> int -> 'T -> 'T [,]. Creates an array whose elements are all initially the given
value.

```
Listing 11.90: Array2D.create

1 > Array2D.create 2 3 3.14;;
2 val it : float [,] = [[3.14; 3.14; 3.14]
3 [3.14; 3.14; 3.14]]
```

get: 'T [,] -> int -> 'T. Fetches an element from a 2D array. You can also use the syntax array. [index1,index2].

```
Listing 11.91: Array2D.get

| > let arr = Array2D.init 3 4 (fun i j -> i + 10 * j) |
|- Array2D.get arr 1 2;
| val arr : int [,] = [[0; 10; 20; 30] |
| [1; 11; 21; 31] |
| [2; 12; 22; 32]]
| val it : int = 21
```

init: int -> int -> (int -> int -> 'T) -> 'T [,]. Creates an array given the dimensions and a generator function to compute the elements.

iter: ('T -> unit) -> 'T [,] -> unit. Applies the given function to each element of the array.

<sup>&</sup>lt;sup>6</sup>Jon: rewrite description

## 

length1: 'T [,] -> int. Returns the length of an array in the first dimension.

```
Listing 11.94: Array2D.length1

1 > let arr = Array2D.create 2 3 0.0 in Array2D.length1 arr;;
2 val it : int = 2
```

length2: 'T [,] -> int. Returns the length of an array in the second dimension.

```
Listing 11.95: Array2D.forall length2

1 > let arr = Array2D.create 2 3 0.0 in Array2D.length2 arr;;
2 val it : int = 3
```

map: ('T -> 'U) -> 'T [,] -> 'U [,]. Creates a new array whose elements are the results of applying the given function to each of the elements of the array.

set: 'T [,] -> int -> int -> 'T -> unit. Sets the value of an element in an array. You can also
use the syntax array.[index1,index2] <- value.</pre>

## 12 The imperative programming paradigm

Imperative programming is a paradigm for programming states. In imperative programming, the focus is on how a problem is to be solved as a list of *statements* that affects *states*. In  $\mathbb{F}_{+}$  states are mutable and immutable values, and they are affected by functions and procedures. An imperative program is typically identified as using

· Imperative programming

 $\cdot$  statements

 $\cdot$  states

## mutable values

Mutable values are holders of state, they may change over time, and thus have a dynamic scope.

## · mutable values

### Procedures

Procedures are functions that returns "()", instead of functions that transform data. They are the embodiment of side-effects.

· procedures

## Side-effects

Side-effects are changes of state that are not reflected in the arguments and return values of a function. The printf is an example of a procedure that uses side-effects to communicate with the terminal.

 $\cdot \ side-effects$ 

· for

·while

## Loops

The for- and while-loops typically uses an iteration value to update some state, e.g., for-loops are often used to iterate through a list and summarize its content.

In contrast, mono state or stateless programs as functional programming can be seen as a subset of imperative programming and is discussed in Chapter 17. Object oriented programming is an extension of imperative programming, where statements and states are grouped into classes. For a discussion on object-oriented programming, see Chapter 22.

· functional programming

· Object oriented programming

Imperative programs are like Turing machines, a theoretical machine introduced by Alan Turing in 1936  $\boxed{10}$ . Almost all computer hardware is designed for *machine code*, which is a common term used for many low-level computer programming languages, and almost all machine languages follow the imperative programming paradigm.

 $\cdot$  machine code

A prototypical example is a baking recipe, e.g., to make a loaf of bread do the following:

- 1. Mix yeast with water
- 2. Stir in salt, oil, and flour
- 3. Knead until the dough has a smooth surface
- 4. Let the dough rise until it has double size
- 5. Shape dough into a loaf
- 6. Let the loaf rise until double size

7. Bake in the oven until the bread is golden brown

Each line in this example consists of one or more statements that are to be executed, and while executing them, states such as the size of the dough and the color of the bread changes. Some execution will halt execution until certain conditions of these states are fulfilled, e.g., the bread will not be put into the oven for baking before it has risen sufficiently.

## 12.1 Imperative design

Programming is the act of solving a problem by writing a program to be executed on a computer. And imperative programming focusses on states. To solve a problem, you could work through the following list of actions

- 1. Understand the problem. As Pólya described it, see Chapter 2, the first step in any solution is to understand the problem. A good trick to check, whether you understand the problem is to briefly describe it in your own words.
- 2. Identify the main values, variables, functions, and procedures needed. If the list of procedures is large, then you most likely should organize them in modules. It is also useful to start in a coarse to fine manner.
- 3. For each function and procedure, write a precise description of what it should do. This can conveniently be performed as an in-code comment for the procedure using the F# XML documentation standard.
- 4. Make mockup functions and procedures using the intended types, but don't necessarily compute anything sensible. Run through examples in your mind, using this mockup program to identify any obvious oversights.
- 5. Write a suite of unit-tests that tests the basic requirements for your code. The unit tests should be runnable with your mockup code. Writing unit-tests will also allow you to evaluate the usefulness of the code pieces as seen from an application point of view.
- 6. Replace the mockup functions in a prioritized order, i.e., write the must-have code before you write the nice-to-have code, while regularly running your unit-tests to keep track on your progress.
- 7. Evaluate the code in relation to the desired goal and reiterate earlier actions as needed until the task has been sufficiently completed.
- 8. Complete your documentation both in-code and outside to ensure that the intended user has sufficient knowledge to effectively use your program and to ensure that you or a fellow programmer will be able to maintain and extend the program in the future.