

# Learning to program with F#

Jon Spurring & Torben Mogensen

Department of Computer Science,  
University of Copenhagen

July 19, 2017

# Contents

<b>1</b>	<b>Preface</b>	<b>5</b>
<b>2</b>	<b>Introduction</b>	<b>6</b>
2.1	How to learn to program . . . . .	6
2.2	How to solve problems . . . . .	7
2.3	Approaches to programming . . . . .	7
2.4	Why use F# . . . . .	8
2.5	How to read this book . . . . .	9
<b>I</b>	<b>F# basics</b>	<b>10</b>
<b>3</b>	<b>Executing F# code</b>	<b>11</b>
3.1	Source code . . . . .	11
3.2	Executing programs . . . . .	11
<b>4</b>	<b>Quick-start guide</b>	<b>14</b>
<b>5</b>	<b>Using F# as a calculator</b>	<b>19</b>
5.1	Literals and basic types . . . . .	19
5.2	Operators on basic types . . . . .	24
5.3	Boolean arithmetic . . . . .	26
5.4	Integer arithmetic . . . . .	27
5.5	Floating point arithmetic . . . . .	29
5.6	Char and string arithmetic . . . . .	31
5.7	Programming intermezzo . . . . .	32

<b>6</b>	<b>Constants, functions, and variables</b>	<b>34</b>
6.1	Values . . . . .	37
6.2	Non-recursive functions . . . . .	42
6.3	User-defined operators . . . . .	46
6.4	The Printf function . . . . .	48
6.5	Variables . . . . .	51
<b>7</b>	<b>In-code documentation</b>	<b>57</b>
<b>8</b>	<b>Controlling program flow</b>	<b>62</b>
8.1	For and while loops . . . . .	62
8.2	Conditional expressions . . . . .	66
8.3	Recursive functions . . . . .	68
8.4	Programming intermezzo . . . . .	71
<b>9</b>	<b>Ordered series of data</b>	<b>75</b>
9.1	Tuples . . . . .	76
9.2	Lists . . . . .	79
9.3	Arrays . . . . .	84
<b>10</b>	<b>Exceptions</b>	<b>89</b>
<b>11</b>	<b>Input and Output</b>	<b>97</b>
11.1	Interacting with the console . . . . .	98
11.2	Storing and retrieving data from a file . . . . .	99
11.3	Working with files and directories. . . . .	104
11.4	Reading from the internet . . . . .	104
11.5	Programming intermezzo . . . . .	105
<b>II</b>	<b>Imperative programming</b>	<b>108</b>
<b>12</b>	<b>Graphical User Interfaces</b>	<b>110</b>
12.1	Drawing primitives in Windows . . . . .	110

12.2	Programming intermezzo . . . . .	123
12.3	Events, Controls, and Panels . . . . .	125
<b>13</b>	<b>Imperative programming</b>	<b>150</b>
13.1	Introduction . . . . .	150
13.2	Generating random texts . . . . .	151
13.2.1	0'th order statistics . . . . .	151
13.2.2	1'th order statistics . . . . .	151
<b>III</b>	<b>Declarative programming</b>	<b>152</b>
<b>14</b>	<b>Sequences and computation expressions</b>	<b>153</b>
14.1	Sequences . . . . .	153
<b>15</b>	<b>Patterns</b>	<b>159</b>
15.1	Pattern matching . . . . .	159
<b>16</b>	<b>Types and measures</b>	<b>162</b>
16.1	Unit of Measure . . . . .	162
<b>17</b>	<b>Functional programming</b>	<b>166</b>
<b>IV</b>	<b>Structured programming</b>	<b>169</b>
<b>18</b>	<b>Modules and Namespaces</b>	<b>170</b>
<b>19</b>	<b>Object-oriented programming</b>	<b>176</b>
19.1	Object-oriented Analysis . . . . .	176
<b>V</b>	<b>Appendix</b>	<b>173</b>
<b>A</b>	<b>Number systems on the computer</b>	<b>174</b>
A.1	Binary numbers . . . . .	176
A.2	IEEE 754 floating point standard . . . . .	176

<b>B</b>	<b>Commonly used character sets</b>	<b>177</b>
B.1	ASCII . . . . .	177
B.2	ISO/IEC 8859 . . . . .	178
B.3	Unicode . . . . .	178
<b>3</b>	<b>Common Language Infrastructure</b>	<b>182</b>
<b>C</b>	<b>A brief introduction to Extended Backus-Naur Form</b>	<b>182</b>
<b>D</b>	<b>F<sub>b</sub></b>	<b>186</b>
<b>E</b>	<b>Language Details</b>	<b>191</b>
E.1	Arithmetic operators on basic types . . . . .	191
E.2	Basic arithmetic functions . . . . .	194
E.3	Precedence and associativity . . . . .	195
E.4	Lightweight Syntax . . . . .	197
<b>F</b>	<b>The Some Basic Libraries</b>	<b>198</b>
F.1	System.String . . . . .	199
F.2	List, arrays, and sequences . . . . .	199
F.3	WinForms Details . . . . .	203
F.4	Mutable Collections . . . . .	203
F.4.1	Mutable lists . . . . .	203
F.4.2	Stacks . . . . .	203
F.4.3	Queues . . . . .	203
F.4.4	Sets and dictionaries . . . . .	203
<b>7</b>	<b>To Dos</b>	<b>204</b>
	<b>Bibliography</b>	<b>205</b>
	<b>Index</b>	<b>206</b>

## Chapter 3

# Executing F# code

### 3.1 Source code

F# is a functional first programming language, meaning that it has strong support for functional programming, but F# also supports imperative and object oriented programming. It also has strong support for parallel programming and information rich programs. It was originally developed for Microsoft's .Net platform, but is available as open source for many operating systems through Mono. In this text we consider F# 4.0 and its Mono implementation, which is different from .Net mainly in terms of the number of libraries accessible. The complete language specification is described in <http://fsharp.org/specs/language-spec/4.0/FSharpSpec-4.0-latest.pdf>.

F# has 2 modes of execution, *interactive* and *compiled*. Interactive mode is well suited for small experiments or back-of-an-envelope calculations, but not for programming in general. In Mono, the interactive system is started by calling `fsharpi` from the *console*, while compilation is performed with `fsharpc` and execution of the compiled code is performed using the `mono` command. The various forms of fsharp programs are identified by suffixes:

`.fs` An *implementation file*, e.g., `myModule.fs`

`.fsi` A *signature file*, e.g., `myModule.fsi`

`.fsx` A *script file*, e.g., `gettingStartedStump.fsx`

`.fsscript` Same as `.fsx`, e.g., `gettingStartedStump.fsscript`

`.exe` An *executable file*, e.g., `gettingStartedStump.exe`

· interactive  
· compiled  
· console

· implementation  
file  
· signature file  
· script file

· executable file

The implementation, signature, and script files are all typically compiled to produce an executable file, but syntactically correct code can also be entered into the interactive system, in which case these are called *script-fragments*. The implementation and signature files are special kinds of script files used for building *modules*. Modules are collections of smaller programs used by other programs, which will be discussed in detail in Part IV.

· script-fragments  
· modules

### 3.2 Executing programs

Programs may either be executed by the interpreter or by compiling and executing the compiled code.

In Mono the interpreter is called `fsharpi` and can be used in 2 ways: interactively, where a user enters 1 or more script-fragments separated by the “`;;`” lexeme, or to execute a script file treated as a single script-fragment. To illustrate the difference, consider the following program, which declares a value `a` to be the decimal value 3.0 and finally print it to the console:

**Listing 3.1** `gettingStartedStump.fsx`:  
A simple demonstration script.

```
1 let a = 3.0
2 printfn "%g" a
```

An interactive session is obtained by starting the console, typing the `fsharpi` command, typing the lines of the program, and ending the script-fragment with the “`;;`” lexeme. The following dialogue demonstrates the workflow, where what the user types has been highlighted by a box:

**Listing 3.2:** : An interactive session.

```
1 $ fsharpi
2
3 F# Interactive for F# 4.0 (Open Source Edition)
4 Freely distributed under the Apache 2.0 Open Source License
5
6 For help type #help;;
7
8 > let a = 3.0
9 - printfn "%g" a;;
10 3
11
12 val a : float = 3.0
13 val it : unit = ()
14
15 > #quit;;
```

The interpreter is stopped by pressing `ctrl-d` or typing “`#quit;;`”. Conversely, executing the file with the interpreter as follows,

**Listing 3.3:** : Using the interpreter to execute a script.

```
1 $ fsharpi gettingStartedStump.fsx
2 3
```

Finally, compiling and executing the code is performed as,

**Listing 3.4:** : Compiling and executing a script.

```
1 $ fsharpc gettingStartedStump.fsx
2 F# Compiler for F# 4.0 (Open Source Edition)
3 Freely distributed under the Apache 2.0 Open Source License
4 $ mono gettingStartedStump.exe
5 3
```

Both the interpreter and the compiler translates the source code into a format, which can be executed by the computer. While the compiler performs this translation once and stores the result in the executable file, the interpreter translates the code every time the code is executed. Thus, to run the program again with the interpreter, then it must be retranslated as "`fsharpi gettingStartedStump.fsx`". In contrast, compiled code does not need to be recompiled to be run again, only re-executed using "`mono gettingStartedStump.exe`". On a Macbook Pro, with a 2.9 Ghz Intel Core i5, the time the various stages takes for this script are:

Command	Time
<code>fsharpi gettingStartedStump.fsx</code>	1.88s
<code>fsharpc gettingStartedStump.fsx</code>	1.90s
<code>mono gettingStartedStump.exe</code>	0.05s

I.e., executing the script with `fsharpi` is slightly faster than by first compiling it with `fsharpc` and then executing the result with `mono`,  $1.88s < 0.05s + 1.90s$ , if the script were to be executed only once, but every future execution of the script using the compiled version requires only the use of `mono`, which is much faster than `fsharpi`,  $1.88s \gg 0.05s$ .

The interactive session results in extra output on the *type inference* performed, which is very useful for *debugging* and development of code-fragments, but both executing programs with the interpreted directly from a file and compiling and executing the program is much preferred for programming complete programs, since the starting state is well defined, and since this better supports *unit-testing*, which is a method for debugging programs.

- type inference
- debugging
- unit-testing



## Part IV

# Structured programming

## Chapter 18

# Modules and Namespaces

In this chapter we will focus on a number of ways to make it available as a *library* function in F#, and by library we mean a collection of types, values and functions that an application program can use. A library does not perform calculations on its own.

F# includes several programming structures to organize code in libraries: Modules, namespaces and classes. In this chapter, we will describe modules and namespaces. Classes will be described in detail in Chapter 19.

Consider the following problem:

### Problem 18.1:

Design a library of utility functions that may be reused in several programs. The library should as minimum include the function:

```
type floatFunction = float -> float -> float
let apply (f : floatFunction) (x : float) (y : float) : float = f x y
```

The function `apply` here serves as a dummy.

An F# *module*, not to be confused with a Common Language Infrastructure module see Chapter 3, is a programming structure used to organise type declarations, values, functions etc.

Every implementation and script file in F# implicitly defines a module, and the module name is given by the filename. Thus, creating a script file `Meta.fsx` with the following content:

### Listing 18.1 Meta.fsx:

A script file defining the `apply` function.

```
1 type floatFunction = float -> float -> float
2 let apply (f : floatFunction) (x : float) (y : float) : float = f x y
```

we've implicitly defined a module of name `Meta`. Another script file may now use this function, and it is access using the “.” notation, i.e., `Meta.apply` will refer to this function in other programs. A use could be:

**Listing 18.2 MetaUse.fsx:  
Defining a script calling the module.**

```
1 let add : Meta.floatFunction = fun x y -> x + y
2 let result = Meta.apply add 3.0 4.0
3 printfn "3.0 + 4.0 = %A" result
```

In the above, we have explicitly used the module's type definition for illustration purposes. A shorter and possibly simpler program would have been to define `add` as `let add x y = x + y`, since F#'s typesystem will deduce the its implied type. However, **explicit definitions of types is recommended for readability**. Hence, an alternative to the above's use of lambda functions is, `let add (x: float) (y: float) : float = x + y`. To compile the module and the application program, we write:

Advice

**Listing 18.3: : File order matters, when compiling several files.**

```
1 $ fsharpc Meta.fsx MetaUse.fsx
2 F# Compiler for F# 4.1
3 Freely distributed under the Apache 2.0 Open Source License
4 $ mono MetaUse.exe
5 3.0 + 4.0 = 7.0
```

Notice, since the F# compiler reads through the files once, the order of the filenames in the compile command is very important. Hence, the script containing the module and function definitions must be to the left of the script containing their use. Notice also that if not otherwise specified, then the F# compiler produces an `.exe` file derived from the last filename in the list of filenames.

We may also explicitly define the module name using the “`module`” as illustrated here:

**Listing 18.4 MetaExplicitModuleDefinition.fsx:  
Defining a module containing a meta function.**

```
1 module Meta
2 type floatFunction = float -> float -> float
3 let apply (f : floatFunction) (x : float) (y : float) : float = f x y
```

Since created a new file, where the module `Meta` is explicitly defined, we can use the same application program.

**Listing 18.5: : File order matters, when compiling several files.**

```
1 $ fsharpc MetaExplicitModuleDefinition.fsx MetaUse.fsx
2 F# Compiler for F# 4.1
3 Freely distributed under the Apache 2.0 Open Source License
4 $ mono MetaUse.exe
5 3.0 + 4.0 = 7.0
```

Note that, since `MetaExplicitModuleDefinition.fsx` explicitly defines the module name, `apply` is not available to an application program as `MetaExplicitModuleDefinition.apply`. **It is recommended that module names are defined explicitly, since filenames may change due to**

Advice

**external conditions.** I.e., filenames are typically set from the perspective of the filesystem. The user may choose to change names to suit a filesystem structure, or different platforms may impose different filename convention. Thus, direct linking of filenames with the internal workings of a program is a needless complication of structure.

The definitions inside a module may be access directly from an application program omitting the “.”-notation by use of the “**open**” keyword. I.e., we can modify `MetaUse.fsx` to

**Listing 18.6 MetaUseWOpen.fsx:**  
Defining a script calling the module.

```
1 open Meta
2 let add : floatFunction = fun x y -> x + y
3 let result = apply add 3.0 4.0
4 printfn "3.0 + 4.0 = %A" result
```

In this case, the namespace of our previously define module is included into the scope of the application functions, and its types, values, functions etc. can be used directly. Thus

**Listing 18.7: : File order matters, when compiling several files.**

```
1 $ fsharpc MetaExplicitModuleDefinition.fsx MetaUseWOpen.fsx
2 F# Compiler for F# 4.1
3 Freely distributed under the Apache 2.0 Open Source License
4 $ mono MetaUseWOpen.exe
5 3.0 + 4.0 = 7.0
```

The “**open**”-keyword should used sparingly, since including a library’s definitions into the application scope can cause surprising naming conflicts, since the user of a library typically has no knowledge of the inner workings of the library. E.g., the user may accidentally use code defined in the library, but with different type and functionality than intended, which the typesystem will use to deduce types in the application program, and therefore will either give syntax or run-time errors that are difficult to understand. This is known as *namespace polution*, and for clarity **it is recommended to use the “open”-keyword sparingly**. Note that for historical reasons, the work namespace polution is used to cover both polution due to modules and namespaces.

· namespace  
polution  
Advice

Modules may also be nested, in which case the nested definitions must use the “=”-sign and must be appropriately indendet.

**Listing 18.8 nestedModules.fsx:**  
A script file defining the apply function.

```
1 module Utilities
2   let PI = 3.1415
3   module Meta =
4     type floatFunction = float -> float -> float
5     let apply (f : floatFunction) (x : float) (y : float) : float = f x y
6   module MathFcts =
7     let add : Meta.floatFunction = fun x y -> x + y
```

In this case, `Meta` and `MathFcts` are defined on the same level and said to be siblings, while `Utilities`

is defined on a higher level. In this relation the former two are said to be the children of the latter. Note that the nesting respects the lexical scope rules, such that the constant `PI` is directly accessible in both modules `Meta` and `MathFcts`, as is the module `Meta` in `MathFcts` but not `MathFcts` in `Meta`. The “.”-notation is reused to index deeper into the module hierarchy as the following example shows.

**Listing 18.9 nestedModulesUse.fsx:**  
Defining a script calling the module.

```
1
2 let add : Utilities.Meta.floatFunction = fun x y -> x + y
3 let result = Utilities.Meta.apply Utilities.MathFcts.add 3.0 4.0
4 printfn "3.0 + 4.0 = %A" result
```

Modules can be recursive using the “`rec`”-keyword, meaning that in our example we can make the outer module recursive as follows.<sup>1</sup>

**Listing 18.10 nestedRecModules.fsx:**  
A script file defining the apply function.

```
1 module rec Utilities
2   module Meta =
3     type floatFunction = float -> float -> float
4     let apply (f : floatFunction) (x : float) (y : float) : float = f x y
5   module MathFcts =
6     let add : Meta.floatFunction = fun x y -> x + y
```

The consequence is that the modules `Meta` and `MathFcts` are accessible in both modules, but compilation will now give a warning, since soundness of the code will first be checked at run-time. In general it is advised to **avoid programming constructions, whose validity cannot be checked at compile-time.**

Advice

An alternative structure to modules is a *namespace*, which only can hold modules and type declarations and only works in compiled mode. Namespaces are defined as explicitly defined outer modules, e.g.,

· namespace

**Listing 18.11 namespace.fsx:**  
Defining a namespace containing a meta function.

```
1 namespace Utilities
2 type floatFunction = float -> float -> float
3 module Meta =
4   let apply (f : floatFunction) (x : float) (y : float) : float = f x y
```

Note that when putting code in a namespace, then the first line of the file other than comments and compiler directives must be the one starting with `namespace`.

As for modules, the content of a namespace is accessed using the “.” notation.

<sup>1</sup>Todo: **Dependence on version 4.1 and higher.**

**Listing 18.12 namespaceUse.fsx:**  
Defining a script calling the namespace.

```
1 let add : Utilities.floatFunction = fun x y -> x + y
2 let result = Utilities.Meta.apply add 3.0 4.0
3 printfn "3.0 + 4.0 = %A" result
```

Likewise, compilation is performed identically.

**Listing 18.13: : File order matters, when compiling several files.**

```
1 $ fsharp namespace.fsx namespaceUse.fsx
2 F# Compiler for F# 4.1
3 Freely distributed under the Apache 2.0 Open Source License
4 $ mono namespaceUse.exe
5 3.0 + 4.0 = 7.0
```

Hence, from an application point of view, it is not immediately possible to see, that `Utilities` is defined as a namespace and not a module. However, in contrast to modules, namespaces may span several files. E.g., we may add a third file containing extending the `Utilities` namespace with the `MathFcts` module as demonstrated below.

**Listing 18.14 namespaceExtension.fsx:**  
Defining a namespace containing a meta function.

```
1 namespace Utilities
2 module MathFcts =
3     let add : floatFunction = fun x y -> x + y
```

To compile we now need to include all three files in the right order. Likewise, compilation is performed identically.

**Listing 18.15: : File order matters, when compiling several files.**

```
1 $ fsharp namespace.fsx namespaceExtension.fsx namespaceUse.fsx
2 F# Compiler for F# 4.1
3 Freely distributed under the Apache 2.0 Open Source License
4 $ mono namespaceUse.exe
5 3.0 + 4.0 = 7.0
```

The order matters since `namespaceExtension.fsx` relies on the definition of `floatFunction` in `namespace.fsx`. You can use extensions to extend existing namespaces included with the F# compiler.<sup>2</sup>

Namespaces may also be nested. In contrast to modules, nesting defined using the “.” notation, i.e., to create a child namespace `more` of `Utilities` we must use initially write `namespace Utilities` `more`. Indentation is ignored in the `namespace` line, thus left-most indentation is almost always used. Namespaces observed lexical scope, and identically to modules, namespaces containing mutually dependent children can be declared using the “`rec`” keyword, e.g., `namespace rec Utilities`.

<sup>2</sup>Todo: Perhaps something about the global namespace `global`.

Libraries may be distributed in compile form as `.dll` files. This saves the use for having recompile a possibly large library everytime an application program needs it. In order to produce a library file from `MetaExplicitModuleDefinition.fsx` and then compile an application program, we first use the compiler's `-a` option to produce the `.dll`, and the `-r` option to compile the application program with the newly created library.<sup>3</sup>

**Listing 18.16: : File order matters, when compiling several files.**

```
1 $ fsharp -a MetaExplicitModuleDefinition.fsx
2 F# Compiler for F# 4.1
3 Freely distributed under the Apache 2.0 Open Source License
4 $ fsharp -r MetaExplicitModuleDefinition.dll MetaUse.fsx
5 F# Compiler for F# 4.1
6 Freely distributed under the Apache 2.0 Open Source License
7 $ mono MetaUse.exe
8 3.0 + 4.0 = 7.0
```

Libraries can of course be a compilation of any number of files into a single `.dll` file. `.dll`-files may be loaded dynamically in script files (`.fsx`-files) using the `#r` directive as illustrated below.

· `#r` directive

**Listing 18.17 MetaUseHash.fsx:  
Defining a namespace containing a meta function.**

```
1 #r "MetaExplicitModuleDefinition.dll"
2 let add : Meta.floatFunction = fun x y -> x + y
3 let result = Meta.apply add 3.0 4.0
4 printfn "3.0 + 4.0 = %A" result
```

We may now omit the explicit mentioning of the library when compiling.

**Listing 18.18: : File order matters, when compiling several files.**

```
1 $ fsharp MetaUseHash.fsx
2 F# Compiler for F# 4.1
3 Freely distributed under the Apache 2.0 Open Source License
4 $ mono MetaUseHash.exe
5 3.0 + 4.0 = 7.0
```

The `#r` directive is also used to include a library in interactive mode. However, for code to be compiled, the use of the `#r` directive requires that the filesystem path to the library is coded inside the script. As for module names, direct linking of filenames with the internal workings of a program is a needless complication of structure, and **it is recommended not to rely on the use of the `#r` directive.**

Advice

In the above, we have compiled *script files* into libraries. However, F# has reserved the `.fs` filename suffix for library files, and such files are called *implementation files*. In contrast to script files, implementation files do not support the `#r` directive. When compiling a list of implementation and script files all but the last file must explicitly define a module or a namespace.

· script files  
· implementation files

Both script and implementation files may be augmented with *signature files*. A signature file contains no implementation but only type definitions. Signature files can be generated automatically using

· signature files

<sup>3</sup>Todo: This is the MacOS option standard, Windows is slightly different.

the `--sig:<filename>` compiler directive. To demonstrate this, This offers three distinct features. Firstly, signature files can be used as part of the documentation of code, since type information is of paramount importance for an application programmer to use a library. Secondly,

Code to be compile to libraries are

Things to remember:

- difference between .fs and .fsx Spec-4.0 Chapter 12.1 and 12.3
- signature files and their usefulness

4 5

---

<sup>4</sup>Todo: **Difference between namespaces and modules** <https://stackoverflow.com/questions/795172/what-the-difference-between-a-namespace-and-a-module-in-f>

<sup>5</sup>Todo: <https://fsharpforfunandprofit.com/posts/organizing-functions/>, <https://fsharpforfunandprofit.com/posts/recipe-part3/>



# Chapter 7

## To Dos

- Remove EBNF from main body of the text, possibly extend the appendix
- Add appendix on regular expressions
- Add Torben's notes on functional programming
- Rewrite list chapter (add sequences?)
- Add a chapter comparing the 3 paradigms
- Write structured programming part
- Write chapter on pattern matching (if not already in Torben's notes)
- Move modules and namespaces earlier
- Should we add something about assemblies ([https://msdn.microsoft.com/en-us/library/hk5f40ct\(v=vs.90\).aspx](https://msdn.microsoft.com/en-us/library/hk5f40ct(v=vs.90).aspx), <https://msdn.microsoft.com/en-us/library/ms973231.aspx>, <https://stackoverflow.com/questions/2972732/what-are-net-assemblies>)
- Add something on piping (if not already in Torben's notes)
- Add abstraction of computer: places  $\leftrightarrow$  memory/disk. Mutable objects are abstractions of places <https://www.infoq.com/presentations/Value-Values>. Facts does not rime with set and get.
- Hickey: Difference between syntax and semantics. Values or locations, add a good figure. Functional programming: All values are freely shareable.

# Bibliography

- [1] M. Auer, J. Poelz, A. Fuernweger, L. Meyer, and T. Tschurtschenthaler. Umlet, free uml tool for fast uml diagrams. <http://www.umlet.com>, Present version 14.2, version 1.0 was released June 21, 2002.
- [2] Alonzo Church. A set of postulates for the foundation of logic. *Annals of Mathematics*, 33(2):346–366, 1932.
- [3] European Computer Manufacturers Association (ECMA). Standard ecma-335, common language infrastructure (cli). <http://www.ecma-international.org/publications/standards/Ecma-335.htm>.
- [4] International Organization for Standardization. Iso/iec 23271:2012, common language infrastructure (cli). <https://www.iso.org/standard/58046.html>.
- [5] Object Management Group. Uml version 2.0. <http://www.omg.org/spec/UML/2.0/>.
- [6] Programming Research Group. Specifications for the ibm mathematical formula translating system, fortran. Technical report, Applied Science Division, International Business Machines Corporation, 1954.
- [7] John McCarthy. Recursive functions of symbolic expressions and their computation by machine, part i. *Communications of the ACM*, 3(4):184–195, 1960.
- [8] X3: ASA Sectional Committee on Computers and Information Processing. American standard code for information interchange. Technical Report ASA X3.4-1963, American Standards Association (ASA), 1963. <http://worldpowersystems.com/projects/codes/X3.4-1963/>.
- [9] George Pólya. *How to solve it*. Princeton University Press, 1945.