Learning to program with F#

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1 | Preface

This book has been written as an introduction to programming for novice programmers. It is used on the first programming course at the University of Copenhagen's bachelor in computer science program. It has been typeset in LATEX, and all programs have been developed and tested in Mono version 5.2.0.

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2 | Introduction

Programming is a creative process in which exciting problems may be solved and new tools and applications may be created. With programming skills, you can create high-level applications to run on a mobile device that interacts with other users, databases, and artificial intelligences; you may create programs that run on super computers for simulating weather systems on alien planets or social phenomena in the internet economy; and you may create programs that run on small custom-made hardware for controlling your home appliances.

2.1 Learning how to solve problems by programming

In order to learn how to program, there are a couple of steps that are useful to follow:

- 1. Choose a programming language: A programming language such as F# is a vocabulary and a set of gramatical rules for instructing a computer to perform a certain task. It is possible to program without a concrete language, but your ideas and thoughts must be expressed in some fairly rigorous way. Actually, theoretical computer science typically does not rely on computers nor programming languages, but uses mathematics to prove properties of algorithms. However, most computer scientists program, and with a real language, you have the added benefit of checking your algorithm, and hence your thoughts, rigorously on a real computer. This book teaches a subset of F#. The purpose is not to be a reference guide to this language, but to use it as a vessel to teach you, the reader, how to convert your ideas into programs.
- 2. Learn the language: A computer language is a structure for thought, and it influences which thoughts you choose to implement as a program, and how you choose to do it. Any conversion requires you to acquire a sufficient level of fluency, for you to be able to make programs. You do not need to be a master in F# nor to know every corner of the language, and you will expand your knowledge as you expose yourself to solving problems in the language, but you must invest an initial amount of time and energy in order to learn the basics of the language. This book aims at getting you started quickly, which is why we intentionally teach just a small subset of F#. On the net and through other works, you will be able to learn much more.
- 3. Practice: If you want to be a good programmer, then there is only one way: practice, practice, practice! It has been estimated that to master anything, then you have to have spent at least 10000 hours of practice, so get started logging hours! It of course matters, what you practice. This book teaches 3 different programming themes. The point is that programming is thinking, and the scaffold that you use, shapes your thoughts. It is therefore important to recognise this scaffold, and to have the ability to choose that which suits your ideas and your goals best. And the best way to expand your abilities is to sharpen your present abilities, push yourself into new territory, and trying something new. Do not be afraid to make errors or be frustrated at first. These are the experiences that make you grow.

4. Solve real problems: I have found that using my programming skills in real situations with customers demanding solutions, that work for them, has allowed me to put into perspective the programming tools and techniques that I use. Often customers want solutions that work, are secure, cheap, and delivered fast, which has pulled me as a programmer in the direction of "if it works, then sell it". On the other hand, in the longer perspective customers also want bug fixes, upgrades, and new features, which require carefully designed code, well written test-suites, and good documentation. And as always, the right solution is somewhere in between. Regardless, real problems create real programmers.

2.2 How to solve problems

Programming is the act of solving a problem by writing a program to be executed on a computer. A general method for solving problems was given by George Pólya [9] and adapted to programming is:

- **Understand the problem:** To solve any problem it is crucial that the problem formulation is understood: What is to be solved? Do you understand everything in the description of the problem? Is all information for finding the solution available or is something missing?
- **Design a plan:** Good designs mean that programs are faster to program, easier to find errors in and update in the future. So, before you start typing a program consider things like: What are the requirements and constraints for the program? Which components should the program have? How are these components supposed to work together? Designing often involves drawing a diagram of the program, and writing program sketches on paper.
- Implement the plan: Implementation is the act of transforming a program design into code. A crucial part of any implementation is choosing which programming language to use. Also, the solution to many problems will have a number of implementations which vary in how much code they require, to which degree they rely on external libraries, which programming style they are best suited for, what machine resources they require, and what their running times are. With a good design, the coding is usually easy, since the design will have uncovered the major issues and found solutions for these, but sometimes implementation reveals new problems, which requires rethinking the design. Most implementations also include writing documentation of the code.
- Reflect on the result: A crucial part in any programming task is ensuring that the program solves the problem sufficiently. E.g., what are the program's errors, is the documentation of the code sufficient and relevant for its intended use? Is the code easily maintainable and extendable by other programmers? Are there any general lessons to be learned from or general code developed by the programming experience, which may be used for future programming sessions?

Programming is a very complicated process, and Pólya's list is a useful guide, but not a fail-safe approach. Always approach problem solving with an open mind.

2.3 Approaches to programming

This book focuses on 3 fundamentally different approaches to programming:

Imperative programming, emphasises how a program shall accomplish a solution and less on what the solution is. A cooking recipe is an example of the spirit of imperative programming, where the recipe emphasises what should be done in each step rather than describing the result. E.g., for making bread, you first mix yeast and water, then add flour, etc. In imperative programming

· imperative programming

 \cdot statement

 \cdot state

what should be done are called *statements* and they influence the computer's *states*, like adding flour changes the state of our dough. Almost all computer hardware is designed to execute low-level programs written in imperative style. Imperative programming builds on the Turing machine [10]. The first major language was FORTRAN [6] which emphasized an imperative style of programming.

- **Declarative programming,** which emphasises what a program shall accomplish but not how. We will consider Functional programming as an example of declarative programming. A functional programming language evaluates functions and avoids state changes. The program consists of expressions instead of statements. As an example the function $f(x) = x^2$ takes a number x and evaluates the expression x^2 , and returns the result. Functional programming has its roots in lambda calculus [1], and the first language emphasizing functional programming was Lisp [7].
- Structured programming, which emphasises organisation of code in units with well-defined interfaces and isolation of internal states and code from other parts of the program. We will focus on Object-oriented programming as the example of structured programming. Object-oriented programming is a type of programming, where the states and programs are structured into objects. A typical object-oriented design takes a problem formulation and identifies key nouns as potential objects and verbs as potential actions to be taken on objects. The first object-oriented programming language was Simula 67 developed by Dahl and Nygaard at the Norwegian Computing Center in Oslo [2].
- **Event-driven programming,** is often used when dynamically interacting with the real world. E.g., when programming graphical user interfaces, programs will often need to react to a user clicking on the mouse or when text arrives from a web-server to be displayed on the screen. Event-driven programs are often programmed using *call-back functions*, which are small programs that are ready to run, when events occur.

Most programs do not follow a single programming paradigm as, e.g., one of the above, but are a mix. Nevertheless, this book will treat each paradigm separately to emphasize their advantages and disadvantages.

2.4 Why use F#

This book uses F# also known as Fsharp, which is a functional first programming language that also supports imperative and object-oriented programming. It was originally developed for Microsoft's .Net platform, but is available as open source for many operating systems through Mono. As an introduction to programming, F# is a young programming language still under development, with syntax that at times is a bit complex, but it offers a number of advantages:

- Interactive and compile mode: F# has an interactive and a compile mode of operation: In interactive mode you can write code that is executed immediately in a manner similarly to working with a calculator, while in compile mode, you combine many lines of code possibly in many files into a single application, which is easier to distribute to non F# experts and is faster to execute.
- **Indentation for scope:** F# uses indentation to indicate scope: Some lines of code belong together, e.g., should be executed in a certain order and may share data, and indentation helps in specifying this relationship.
- **Strongly typed:** F# is strongly typed, reducing the number of runtime errors. That is, F# is picky, and will not allow the programmer to mix up types such as numbers and text. This is a great advantage for large programs.
- **Multi-platform:** F# is available on Linux, Mac OS X, Android, iOS, Windows, GPUs, and browsers via the Mono platform.

- · declarative programming
- · functional programming
- \cdot function
- \cdot expression
- $\begin{array}{c} \cdot \, \text{structured} \\ \text{programming} \end{array}$
- \cdot Object-oriented programming
- \cdot object
- \cdot event-driven programming
- \cdot call-back functions

Free to use and open source: F# is supported by the Fsharp foundation (http://fsharp.org) and sponsored by Microsoft.

Assemblies: F# is designed to be able to easily communicate with other .Net and Mono programs through the language-independent, platform-independent bytecode called Common Intermediate Language (CIL) organised as assemblies. Thus, if you find that certain parts of a program are easy to express in F# and others in C++, then you will be able to combine these parts later into a single program.

Modern computing: F# supports all aspects of modern computing including Graphical User Interfaces, Web programming, Information rich programming, Parallel algorithms, . . .

Integrated development environments (IDE): F# is supported by major IDEs such as Visual Studio (https://www.visualstudio.com) and Xamarin Studio (https://www.xamarin.com).

2.5 How to read this book

Learning to program requires mastering a programming language, however most programming languages contains details that are rarely used or used in contexts far from a specific programming topic. Hence, this book only includes a subset of F#, but focuses on language structures necessary to understand 4 common programming paradigms: Imperative programming mainly covered in Chapters 6 to 11, functional programming mainly covered in Chapters 13 to 16, object oriented programming in Chapters 20 and 22, and event driven programming in Chapter 23. A number of general topics are given in the appendix for reference. The disadvantage of this approach is that no single part contains a reference guide to F#, and F# topics are revisited and expanded across the book. For further reading please consult http://fsharp.org.

$3 \mid \text{ Executing F} \# \text{ code}$

3.1 Source code

F# is a functional first programming language, meaning that it has strong support for functional programming, but F# also supports imperative and object-oriented programming. It also has strong support for parallel programming and information rich programs. It was originally developed for Microsoft's .Net platform, but is available as open source for many operating systems through Mono. In this text, we consider F# 4.1 and its Mono implementation, which is different from .Net mainly in terms of the number of libraries accessible. The complete language specification is described in http://fsharp.org/specs/language-spec/.

F# has 2 modes of execution, *interactive* and *compiled*. Interactive mode is well suited for small experiments or back-of-an-envelope calculations, but not for programming in general. Both modes can be accessed via the *console*, see Appendix A for more information on the console. The interactive system is started by calling fsharpi at the command prompt in the console, while compilation is performed with fsharpc, and execution of the compiled code is performed using the mono command.

· interactive mode

 \cdot compile mode

 $\cdot \ console$

F# programs comes in many forms, which are identified by suffixes. The *source code* is an F# program written in human readable form using an editor. F# recognises the following types of source code files:

 \cdot source code

.fs An implementation file, e.g., myModule.fs

· implementation file

.fsi A signature file, e.g., myModule.fsi

· signature file

.fsx A script file, e.g., gettingStartedStump.fsx

 \cdot script file

.fsscript Same as .fsx, e.g., gettingStartedStump.fsscript

Compiled code is source code translated into a machine readable language, which can be executed by a machine. Compiled F# code is either:

.dll A library file, e.g., myModule.dll

· library file

.exe A stand-alone executable file, e.g., gettingStartedStump.exe

 \cdot executable file

The implementation, signature, and script files are all typically compiled to produce an executable file, in which case they are called scripts, but can also be entered into the interactive system, in which case these are called script-fragments. The implementation and signature files are special kinds of script files used for building libraries. Libraries in F# are called modules, and they are collections of smaller programs used by other programs, which will be discussed in detail in Chapter 9.

 \cdot scripts

 $\cdot \, script\text{-}fragment$

3.2 Executing programs

Programs may either be executed by the interpreter or by compiling and executing the compiled code. In Mono the interpreter is called fsharpi and can be used in two ways: interactively, where a user enters one or more script-fragments separated by the ";;" characters, or to execute a script file treated as a single script-fragment. ¹

To illustrate the difference between interactive and compile mode, consider the program in Listing 3.1.

```
Listing 3.1 gettingStartedStump.fsx:
A simple demonstration script.

1 let a = 3.0
2 do printfn "%g" a
```

The code declares a value a to be the decimal value 3.0 and finally prints it to the console. The do printfn is a statement for displaying the content of a value to the screen, and "%g" is a special notation to control how the value is printed. In this case, it is printed as a decimal number. This and more will be discussed at length in the following chapters. For now we will concentrate on how to interact with the F# interpreter and compiler.

An interactive session is obtained by starting the console, typing the fsharpi command, typing the lines of the program, and ending the script-fragment with ";;". The dialogue in Listing 3.2 demonstrates the workflow. What the user types has been highlighted by a box,

We see that after typing fsharpi, then the program starts by stating details about itself followed by > indicating that it is ready to receive commands. The user then types let a = 3.0 and presses enter, to which the interpreter responds with -. This indicates that the line has been received, that the script-fragment is not yet completed, and that it is ready to receive more input. When the user types do printfn "%g" a;; followed by enter, then by ";;" the interpreter knows that the script-fragment is completed, it interprets the script-fragment, responds with 3 and extra type information about the entered code, and with > to indicate, that it is ready for more script-fragments. The interpreter is

 $^{^1\}mathrm{Jon}$: Too early to introduce lexeme: "F# uses many characters which at times are given special meanings, e.g., the characters ";;" is compound character denoting end of a script-fragment. Such possibly compound characters are called lexemes."

stopped, when the user types #quit;;. It is also possible to stop the interpreter by typing ctrl-d.

Instead of running fsharpi interactively, we can write the script-fragment from Listing 3.1 into a file, here called gettingStartedStump.fsx. This file can be interpreted directly by fsharpi as shown in Listing 3.3.

```
Listing 3.3: Using the interpreter to execute a script.

1  $ (fsharpi gettingStartedStump.fsx)
2  3
```

Notice that in the file, ";;" is optional. We see that the interpreter executes the code and prints the result on screen without the extra type information.

Finally, the file containing Listing 3.1 may be compiled into an executable file with the program fsharpc, and run using the program mono from the console. This is demonstrated in Listing 3.4.

```
Listing 3.4: Compiling and executing a script.

$\fsharpc \text{gettingStartedStump.fsx}$
F# Compiler for F# 4.1 (Open Source Edition)
Freely distributed under the Apache 2.0 Open Source License
$\text{mono gettingStartedStump.exe}$
$3
```

The compiler takes gettingStartedStump.fsx and produces gettingStarted.exe, which can be run using mono.

Both the interpreter and the compiler translates the source code into a format, which can be executed by the computer. While the compiler performs this translation once and stores the result in the executable file, the interpreter translates the code every time the code is executed. Thus, to run the program again with the interpreter, it must be retranslated as "\$fsharpi gettingStartedStump.fsx". In contrast, compiled code does not need to be recompiled to be run again, only re-executed using "\$ mono gettingStartedStump.exe". On a MacBook Pro, with a 2.9 Ghz Intel Core i5, the time the various stages take for this script are:

Command	Time
fsharpi gettingStartedStump.fsx	1.88s
fsharpc gettingStartedStump.fsx	1.90s
mono gettingStartedStump.exe	0.05s

I.e., executing the script with fsharpi is slightly faster than by first compiling it with fsharpc and then executing the result with mono, 1.88s < 0.05s + 1.90s, if the script were to be executed only once, but every future execution of the script using the compiled version requires only the use of mono, which is much faster than fsharpi, $1.88s \gg 0.05s$.

The interactive session results in extra output on the *type inference* performed, which is very useful for *debugging* and development of code-fragments, but both executing programs with the interpreted directly from a file and compiling and executing the program is much preferred for programming complete programs, since the starting state is well defined, and since this better supports *unit-testing*, which is a method for debugging programs. Thus, **prefer compiling over interpretation.**

- · type inference
- \cdot debugging
- \cdot unit-testing Advice

4 | Quick-start guide

Programming is the art of solving problems by writing a program to be executed by a computer. For example, to solve the following problem,

Problem 4.1 What is the sum of 357 and 864?

we have written the program in F# shown in Listing 4.1.

```
Listing 4.1 quickStartSum.fsx:
A script to add 2 numbers and print the result to the console.

1 let a = 357
2 let b = 864
3 let c = a + b
4 do printfn "%A" c

1 $ fsharpc --nologo quickStartSum.fsx && mono quickStartSum.exe
2 1221
```

In box the above, we see our program was saved as a script in a file called quickStartSum.fsx, and in the console we executed the program by typing the command fsharpc --nologo quickStartSum.fsx && mono quickStartSum.exe. The result is then printed in the console to be 1221. Here, as in the rest of this book, we have used the optional flag --nologo, which informs fsharpc not to print information about its version etc., thus making the output shorter. The && notation tells the console to first run the command on the left, and if that did not report any errors, then run that on the right. This could as well have been performed as two separate commands to the console, and throughout this book, we will use the above shorthand, when convenient.

To solve the problem, we made program consisting of several lines, where each line was a expressions. The first expression let a = 357 in line 1 used the let keyword to bind the value 357 to the name a. This is called a let-binding, and a let-binding makes the name synonymous with the value. Another point to be noted is that F# identifies 357 as an integer number, which is F#'s preferred number type, since computations on integers are very efficient, and since integers are very easy to communicate to other programs. In line 2 we bound the value 864 to the name b, and to the name c, we bound the result of evaluating the sum a + b in line 3. Line 4 is a do-binding, as noted by the keyword do. Dobindings are also sometimes called statements, and the do keyword is optional in F#. Here the value of c was printed to the console followed by a newline (LF possibly preceded by CR, see Appendix C.1) with the printfn function. A function in F# is an entity that takes zero or more arguments and returns a value. The function printfn is very special, since it can take any number of arguments. It need not return any value, but F# insists that every function must return a value, wherefore printfn

 \cdot expression

16+

 \cdot keyword

· binding

· let-binding

· integer number

· do-binding

· do

 \cdot statements

· printfn

 \cdot function

returns a special type of value called unit and written as "()". The do tells F# to ignore this value. · unit Here printfn has been used with 2 arguments: "%A" and c. Notice that in contrast to many other languages, F# does not use parentheses to frame the list of arguments, nor does it use commas to separate them. In general, the printfn function always has 1 or more arguments, and the first is a format string. A string is a sequence of characters starting and ending with double quotation marks. E.g., let s = "this is a string of characters" binds the string "this is..." to the name s. For the printfn function, the format string may be any string, but if it contains format character sequences, such as %A, then the values following the format string are substituted. The format string must match the value type, that is, here c is of type integer, whereas the format string %A matches many types.

Types are a central concept in F#. In the script 4.1 we bound values of integer type to names. There are several different integer types in F#, here we used the one called int. The values were not declared to have these types, instead the types were inferred by F#. Typing these bindings line by line in an

· format string

 \cdot string

· type

· type declaration

 \cdot type inference

```
Listing 4.2: Inferred types are given as part of the response from the interpreter.
```

interactive session, then we see the inferred types as shown in Listing 4.2.

```
> let a = 357;;
val a : int = 357
> let b = 864;;
val b : int = 864
 let c = a + b;;
val c : int = 1221
> do printfn "%A" c;;
1221
val it : unit = ()
```

The interactive session displays the type using the val keyword followed by the name used in the valbinding, its type, and its value. Since the value is also responded, then the last printfn statement is superfluous. However, it is ill advised to design programs to be run in an interactive session, since the scripts needs to be manually copied every time it is to be run, and since the starting state may be unclear. Notice that printfn is automatically bound to the name it of it type unit and value "()". F# insists on binding all statements to values, and in lack of an explicit \cdot () name, then it will use it. Rumor has it that it is an abbreviation for "irrelevant".

Were we to solve a slightly different problem,

```
Problem 4.2
```

What is the sum of 357.6 and 863.4?

where the only difference is that the numbers now use a decimal point. These are called floating point · decimal point numbers, and the internal representation is quite difference to integer numbers used previously, and the algorithms used to perform arithmetic are also quite different from integers. Now the program would look like Listing 4.3.

- · floating point numbers

Listing 4.3 quickStartSumFloat.fsx: Floating point types and arithmetic. let a = 357.6 let b = 863.4 let c = a + b do printfn "%A" c fsharpc --nologo quickStartSumFloat.fsx && mono quickStartSumFloat.exe 1 221.0

On the surface, this could appear as an almost negligible change, but the set of integers and the set of real numbers (floats) require quite different representations, in order to be effective on a computer, and as a consequence, the implementation of their operations such as addition are very different. Thus, although the response is an integer, it has type float, which is indicated by 1221.0, and which is not the same as 1221. F# is very picky about types, and generally does not allow types to be mixed, as demonstrated in the interactive session in Listing 4.4.

we see that binding a name to a number without a decimal point is inferred to be integer, while when binding to a number with a decimal point, then the type is inferred to be a float, and when trying to add values of integer and floating point, we get an error. The error message contains much information. First it states that the error is in stdin(4,13), which means that the error was found on standard-input at line 4 and column 13. Since the program was executed using fsharpi quickStartSumFloat.fsx, then here standard input means the file quickStartSumFloat.fsx shown in Listing 4.3. The corresponding line and column is also shown in Listing 4.4. After the file, line, and column number, F# informs us of the error number, and a description of the error. Error numbers are an underdeveloped feature in Mono, and should be ignored. However, the verbal description often contains useful information for debugging. In the example we are informed that there is a type mismatch in the expression, i.e., since a is an integer, then F# had expected b to be one too. Debugging is the process of solving errors in programs, and here we can solve the error by either making a into a float or b into an int. The right solution depends on the application.

 \cdot error message

· debugging

F# is a functional first programming language, and one implication of this is that names have a *lexical scope*. A scope are the lines in a program, where a binding is valid, and lexical scope means that to find the value of a name F# looks for the value in the above lines. Further, at the outer most level, rebinding is not allowed. If attempted, then F# will return an error as shown in Listing 4.5.

lexical scope

Listing 4.5 quickStartRebindError.fsx: A name cannot be rebound. let a = 357let a = 864\$ fsharpc --nologo -a quickStartRebindError.fsx quickStartRebindError.fsx(2,5): error FS0037: Duplicate definition of value 'a'

However, if the same is performed in an interactive session, then rebinding does not cause an error as shown in Listing 4.6.

```
Listing 4.6: Names may be reused when separated by the lexeme ";;".
> let a = 357;;
val a : int = 357
> let a = 864;;
val a : int = 864
```

The difference is that the ";;" lexeme is used to specifies the end of a script-fragment. A lexeme is a :;; letter or a word, which the F# considers as an atomic unit. Script-fragments may be defined both in scripts and in interactive mode, and rebinding is not allowed at the outermost level in script-fragments. · script-fragment Even with the ";;" lexeme, rebinding is not allowed in compile-mode. In general, avoid rebinding Advice of names.

In F#, functions are also values, and we may define a function sum as part of the solution to the above • function program as shown in Listing 4.7.

```
Listing 4.7 quickStartSumFct.fsx:
A script to add 2 numbers using a user defined function.
let sum x y = x + y
let c = sum 357 864
do printfn "%A" c
$ fsharpc --nologo quickStartSumFct.fsx && mono quickStartSumFct.exe
```

Functions are useful to encapsulate code, such that we can focus on the transformation of data by a encapsulate function while ignore the details on how this is done. Functions are also useful for code reuse, i.e., instead of repeating a piece of code in several places, such code can be encapsulated in a function and replaced with function calls. This makes debugging and maintenance considerably simpler. Entering the function into an interactive session will illustrate the inferred type, the function sum has: val sum: x:int -> y:int -> int. The "->" is the mapping operator in the sense that functions are mappings between sets. The type of the function sum, should be read as val sum: x:int -> (y:int -> int), that is, sum takes an integer and returns a function, which takes an integer and returns an integer. This is an example of a higher-order function.

Type inference in F# may cause problems, since the type of a function is inferred in the context, in which it is defined. E.g., in an interactive session, defining the sum in one scope on a single line will default the types to integers, F#'s favorite type. Thus, if the next script-fragment uses the function with floats, then we will get an error message as shown in Listing 4.8.

```
Listing 4.8: Types are inferred in blocks, and F\# tends to prefer integers.
val sum : x:int -> y:int -> int
> let c = sum 357.6 863.4;;
  let c = sum 357.6 863.4;;
stdin(3,13): error FS0001: This expression was expected to have type
but here has type
     'float'
```

A remedy is to define the function in the same script-fragment as it is used such as shown in Listing 4.9.

```
Listing 4.9: Type inference is per script-fragment.
> let sum x y = x + y
- let c = sum 357.6 863.4;;
val sum : x:float -> y:float -> float
val c : float = 1221.0
```

Alternatively, the types may be explicitly stated as shown in Listing 4.10.

```
Listing 4.10: Function argument and return types may be stated explicitly.
> let sum (x : float) (y : float) : float = x + y;;
val sum : x:float -> y:float -> float
> let c = sum 357.6 863.4;;
val c : float = 1221.0
```

The function sum has two arguments and a return type, and in Listing 4.10 we have specified all three. This is done using the ":" lexeme, and to resolve confusion, we must use parentheses around the arguments such as (y: float), otherwise F# would not be able to understand, whether the type annotation was for the argument or the return value. Often it is sufficient to specify some of the types, since type inference will enforce the remaining types. E.g., in this example, the "+" operator is defined for identical types, so specifying the return value of sum to be a float, implies that the result of the "+" operator is a float, and therefore its arguments must be floats, and finally then the arguments for sum must be floats. However, in this book we advocate the following advice: specify types unless Advice explicitly working with generic functions.

In this chapter, we have scratched the surface of learning how to program by concentrating on a number of key programming concepts and how they are expressed in the F# language. In the following chapters, we will expand the description of F# with features used in all programming approaches.

5 | Using F# as a calculator

In this chapter, we will exclusively use the interactive mode to illustrate basic types and operations in F#.

5.1 Literals and basic types

All programs rely on processing of data, and an essential property of data is its type. A literal is a fixed \cdot type value like the number 3, and if we type the number 3 in an interactive session at the input prompt, \cdot literal then F# responds as shown in Listing 5.1.

```
Listing 5.1: Typing the number 3.

1 > 3;;
2 val it : int = 3
```

What this means is that F# has inferred the type to be int and bound it to the identifier it. For more on binding and identifiers see Chapter 6. Types matter, since the operations that can be performed on integers are quite different from those that can be performed on, e.g., strings. E.g., the number 3 has many different representations as shown in Listing 5.2.

Each literal represents the number 3, but their types are different, and hence they are quite different values. The types int for integer numbers, float for floating point numbers, bool for Boolean values, char for characters, and string for strings of characters are the most common types of literals. A table of all $basic\ types$ predefined in F# is given in Table 5.1. Besides these built-in types, F# is designed such that it is easy to define new types.

·float
·bool
·char
·string

· basic types

Metatype	Type name	Description	
Boolean	bool	Boolean values true or false	
Integer	<u>int</u>	Integer values from -2,147,483,648 to 2,147,483,647	
	byte	Integer values from 0 to 255	
	sbyte	Integer values from -128 to 127	
	int8	Synonymous with sbyte	
	uint8	Synonymous with byte	
	int16	Integer values from -32768 to 32767	
	uint16	Integer values from 0 to 65535	
	int32	Synonymous with int	
	uint32	Integer values from 0 to 4,294,967,295	
	int64	Integer values from -9,223,372,036,854,775,808 to	
		9,223,372,036,854,775,807	
	uint64	Integer values from 0 to 18,446,744,073,709,551,615	
		64-bit IEEE 754 floating point value from $-\infty$ to ∞	
	double	Synonymous with float	
	single	A 32-bit floating point type	
	float32	Synonymous with single	
	decimal	A floating point data type that has at least 28 significant digits	
Character char Unicode character		Unicode character	
	string	Unicode sequence of characters	
None	unit	The value ()	
Object	obj	An object	
Exception	<u>exn</u>	An exception	

Table 5.1: List of some of the basic types. The most commonly used types are underlined. For at description of integer see Appendix B.1, for floating point numbers see Appendix B.2, for ASCII and Unicode characters see Appendix C, for objects see Chapter 20, and for exceptions see Chapter 18.

Humans like to use the decimal number system for representing numbers. Decimal numbers are base 10, which means that a value is represented as two sequences of decimal digits separated by a decimal point, where each digit d has a position and a value $d \in \{0,1,2,\ldots,9\}$. The part before the decimal point is called the whole part and the part after is called the fractional part of the number. The whole part with neither a decimal point nor a fractional part is called an integer. As an example 35.7 is a decimal number, whose value is $3 \cdot 10^1 + 5 \cdot 10^0 + 7 \cdot 10^{-1}$, and 128 is an integer, whose value is $1 \cdot 10^2 + 2 \cdot 10^1 + 8 \cdot 10^0$. In F# a decimal number is called a floating point number. Floating point numbers may alternatively be given using scientific notation, such as 3.5e-4 and 4e2, where the e-notation is translated to a value as $3.5e-4 = 3.5 \cdot 10^{-4} = 0.00035$, and $4e2 = 4 \cdot 10^2 = 400$.

The basic unit of information in almost all computers is the binary digit or *bit* for short. Internally, programs and data is all represented as bits, hence F# has a strong support for binary numbers. A binary number consists of a sequence of binary digits separated by a decimal point, where each digit can have values $b \in \{0,1\}$, and the base is 2. E.g., the binary number $101.01_2 = 1 \cdot 2^2 + 0 \cdot 2^1 + 1 \cdot 2^0 + 0 \cdot 2^{-1} + 1 \cdot 2^{-2} = 5.25$. Subscripts are often used to indicate the base of a number, e.g., 101.01_2 and 101.01_{10} are different numbers. Since base 10 is so common, the subscript for base 10 numbers is often omitted.

Binary numbers are closely related to octal and hexadecimal numbers, where octals uses 8 as basis, and where each octal digit can be represented by exactly 3 bits, while hexadecimal numbers uses 16 as basis, and where each hexadecimal digit can be written in binary using exactly 4 bits. The hexadecimal digits uses 0–9 to represent the values 0–9 and a–f in lower or alternatively upper case to represent the values 10-15. Thus, Octals and hexadecimals conveniently serve as shorthand for the much longer binary representation. As examples, the octal number 37_8 is $3 \cdot 8^1 + 7 \cdot 8^0 = 31$, and the hexadecimal number f_{31_6} is $15 \cdot 16^1 + 3 \cdot 16^0 = 243$.

- · decimal number
- \cdot base
- · decimal point
- · digit
- · whole part
- · fractional part
- $\cdot \, \text{integer}$
- · floating point number
- \cdot scientific notation
- · bit
- · binary number

 $\cdot \ octal \ number$

· hexadecimal number

Character	Escape sequence	Description
BS	\b	Backspace
LF	\n	Line feed
CR	\r	Carriage return
HT	\t	Horizontal tabulation
\	\\	Backslash
"	\"	Quotation mark
,	\ '	Apostrophe
BEL	\a	Bell
FF	\f	Form feed
VT	\v	Vertical tabulation
	\uXXXX, \UXXXXXXXX, \DDD	Unicode character

Table 5.2: Escape characters. For the unicode characters 'X' are hexadecimal digits, while for tricode characters 'D' is a decimal character.

To denote integers on bases different than 10, F# uses the prefix '0b' for binary, '0o' for octal, and '0x' for hexadecimal numbers. For example, the value 367_{10} may be written as an integer 367, as a binary number 0b101101111, as a octal number 0o557, and as a hexadecimal number 0x16f. The character sequences 0b12 and ff are not numbers.

A character is a Unicode code point, and character literals are enclosed in single quotation marks. Appendix C.3 contains more details on code points. The character type in F# is denoted char. Examples of characters are 'a', 'D', '3'. However '23' and 'abc' are not characters. Some characters do not have a visual representation such as the tabulation character. These can still be represented as a character using escape sequences. A character escape sequence starts with "\" followed by either a letter for simple escapes such as \t for tabulation and \n for newline. Escape sequences can also be a numerical representation of a code point, and three versions exist: The trigraph \DDD, where D is a decimal digit, is used to specify the first 256 code points, the hexadecimal escape codes \uXXXX, where X is a hexadecimal digit, is used to specify the first 65536 code points, and \uXXXXXXXX is used to specify any of the approximately $4.3 \cdot 10^9$ possible code points. All escape sequences are shown in Table 5.2. Examples of char representations of the letter 'a' are: 'a', '\097', '\u00061', '\u000000061'.

A string is a sequence of characters enclosed in double quotation marks. Examples are "a", "this · string is a string", and "-&#\@". Note that the string "a" and the character 'a' are not the same. Some strings are so common that they are given special names: One or more spaces, " " is called whitespace, · whitespace and both "\n" and "\r\n" are called newline. The escape-character "\" may be used to break a line · newline in two. This and other examples are shown in Listing 5.3.

 \cdot character

· Unicode

· code point

·char

 \cdot escape sequences

Type	syntax	Examples	Value
int, int32	<int hex="" or=""></int>	3, 0x3	3
	<int hex="" or="">l</int>	31, 0x31	
uint32	<int hex="" or="">u</int>	3u	3
	<int hex="" or="">ul</int>	3ul	
byte, uint8	<int hex="" or="">uy</int>	97uy	97
	' <char>'B</char>	'a'B	
byte[]	" <string>"B</string>	"a\n"B	[97uy; 10uy]
	@" <string>"B</string>	@"a\n"B	[97uy; 92uy; 110uy]
sbyte, int8	<int hex="" or="">y</int>	Зу	3
int16	<int hex="" or="">s</int>	3s	3
uint16	<int hex="" or="">us</int>	3us	3
int64	<int hex="" or="">L</int>	3L	3
uint64	<int hex="" or="">UL</int>	3UL	3
	<int hex="" or="">uL</int>	3uL	
float, double	<float></float>	3.0	3.0
	<hex>LF</hex>	0x013fLF	9.387247271e-323
single, float32	<float>F</float>	3.0F	3.0
	<float>f</float>	3.0f	3.0
	<hex>lf</hex>	0x013flf	4.4701421e-43f
decimal	<float int="" or="">M</float>	3.0M,3M	3.0
	<float int="" or="">m</float>	3.0m,3m	
string	" <string>"</string>	"a \"quote\".\n"	a "quote". <newline></newline>
	@" <string>"</string>	@"a ""quote"".\n"	a "quote". \n .
	"" <string>""</string>	"""a "quote".\n"""	a "quote".\n

Table 5.3: List of literal type. Syntax notation is used such that, e.g., <> means that the programmer replaces the brackets and content with a value on appropriate form. The [||] notation means that the value is an array, see Section 11.3 for details.

Note that the response from fsharpi is shown in double quotation marks, but this is not part of the string.

F# supports literal types, where the type of a literal is indicated as a prefix og suffix as shown in the · literal type Table 5.3. The table uses a simple syntax notation such that <integer or hexadecimal>UL means that the user supplies an integer or a hexadecimal number followed by the characters 'UL'.

The literal type is closely connected to how the values are represented internally. E.g., a value of type int32 use 32 bits and can be both positive and negative, while a uint32 value also use 32 bits, but is unsigned. A byte is an 8-bit number, and sbyte is a signed 8-bit number. Values of type float uses 64 bits, while float32 only uses 32 bits. The number of bits used to represent numbers directly relates to the range and precession these types can represent. This is summarized in Table 5.1 and discussed in more detail in Appendix B. String literals may be verbatim by the @-notation or triple · verbatim double quotation marks, meaning that the escape sequences are not converted to their code point. The two types of string verbatim treat quotation marks differently as illustrated in the table. Further examples are shown in Listing 5.4.

```
Listing 5.4: Named and implied literals.
> 3;;
val it : int = 3
> 4u;;
val it : uint32 = 4u
> 5.6;;
val it : float = 5.6
> 7.9f;;
val it : float32 = 7.9000001f
> 'A';;
val it : char = 'A'
> 'B'B;;
val it : byte = 66uy
> "ABC";;
val it : string = "ABC"
> @"abc\nde";;
val it : string = "abc\nde"
```

Many basic types are compatible, and the type of a literal may be changed by typecasting. An example • typecasting of casting to a float is shown in Listing 5.5.

```
Listing 5.5: Casting an integer to a floating point number.
> float 3;;
 val it : float = 3.0
```

which is a float, since when float is given an argument, then it acts as a function rather than a type, and for the integer 3 it returns the floating point number 3.0. For more on functions see Chapter 6. Boolean values are often treated as the integer values 0 and 1, but no short-hand function names exists for their conversions. Instead use functions from the System. Convert family of functions, as demonstrated in Listing 5.6.

Here System. Convert. To Boolean is the identifier of a function To Boolean, which is a member of the \cdot member class Convert that is included in the namespace System. Namespaces, classes, and members will be \cdot class discussed in Chapter 9.

Typecasting is often a destructive operation, e.g., typecasting a float to int removes the fractional part without rounding as shown in Listing 5.7.

```
Listing 5.7: Fractional part is removed by downcasting.

1 > int 357.6;;
2 val it : int = 357
```

Here we typecasted to a lesser type, in the sense that the set of integers is a subset of floating point numbers, and this is called *downcasting*. The opposite is called *upcasting* and is often non-destructive, as Listing 5.5 showed, where an integer was casted to a float while retaining its value. As a side note, *rounding* a number y.x, where y is the *whole part* and x is the *fractional part*, is the operation of mapping numbers in the interval $y.x \in [y.0, y.5)$ to y and $y.x \in [y.5, y+1)$ to y+1. This can be performed by downcasting as shown in Listing 5.8.

```
\cdot \ down casting
```

·upcasting

· rounding

· whole part

· fractional part

```
Listing 5.8: Fractional part is removed by downcasting.

1 > int (357.6 + 0.5);;
2 val it : int = 358
```

As the example shows, for floating points whose fractional part is equal to or larger than y.5 adding 0.5 will make them above (y+1).0, and downcasting will thus downcase to (y+1).0. Conversely fractional pars below will downcast to y.0. Thus, rounding is achieved by downcasting.

5.2 Operators on basic types

Listing 5.8 is an example of an arithmetic expression using an binary operator written using infix notation, since the operator appears in between the operands. The "+" operator is binary, since it takes two arguments, and since it is written between its arguments, then it uses infix notation. Expressions is the basic building block of all F# programs and this section will discuss operator expressions on basic types.

- \cdot expression
- · binary operator
- \cdot infix notation
- \cdot operands

The syntax of basic binary operators is shown in the following:

```
Listing 5.9 Syntax for a binary expression.
<expr><op><expr>
```

Here <expr> is any expression supplied by the programmer, and <op> is a binary, infix operator. F# supports a range of arithmetic binary infix operators on its built-in types such as addition, subtraction, multiplication, division, and exponentiation using the "+", "-", "*", "/", "**" lexemes. Not all operators are defined for all types, e.g., addition is defined for integer and float types as well as for characters and strings, but multiplication is only defined for integer and floating-point types. A complete list of built-in operators on basic types is shown in Table E.1 and E.2 and a range of mathematical functions shown in Table E.3. An example is 3+4. Note that expressions can themselves be arguments to expressions, and thus, 4+5+6 is also a legal statement. This is called recursion, which means that a rule or a function is used by the rule or function itself in its definition. See Chapter 13 for more on recursive functions.

 \cdot recursion

Unary operators takes only one argument and have the syntax:

```
Listing 5.10 A unary expressions.
<op><expr>
```

An example of a unary operator is -3, where - here is used to negate a positive integer. Since the operator appears before the operand it is a prefix operator.

· prefix operator

The concept of precedence is an important concept in arithmetic expressions. If parentheses are omitted in Listing 5.8, then F# will interpret the expression as (int 357.6) + 0.5, which is erroneous, since addition of an integer with a float is undefined. This is an example of precedence, i.e., function evaluation takes precedence over addition meaning that it is performed before addition. Consider the arithmetic expression,

· precedence

```
Listing 5.11: A simple arithmetic expression.
> 3 + 4 * 5;;
val it : int = 23
```

Here, the addition and multiplication functions are shown in infix notation with the operator lexemes · operator "+" and "*". To arrive at the resulting value 23, F# has to decide in which order to perform the calculation. There are 2 possible orders, 3 + (4 * 5) or (3 + 4) * 5, which gives different results. For integer arithmetic, the correct order is of course to multiply before addition, and we say that multiplication takes precedence over addition. Every atomic operation that F# can perform is ordered in terms of its precedence, and for some common built-in operators shown in Table 5.4, the precedence is shown by the order they are given in the table.

· precedence

Associativity implies the order in which calculations are performed for operators of same precedence. For some operators and type combinations association matters little, e.g., multiplication associates to the left and exponentiation associates to the right, as demonstrated in Listing 5.12.

¹Jon: minor comment on indexing and slice-ranges.

Operator	Associativity	Description
+ <expr>, -<expr>,</expr></expr>	Left	Unary identity, negation, and bitwise negation operator
~~~ <expr></expr>		
f <expr></expr>	Left	Function application
<expr> ** <expr></expr></expr>	Right	Exponent
<pre><expr> * <expr>,</expr></expr></pre>	Left	Multiplication, division and remainder
<expr> / <expr>,</expr></expr>		
<expr> % <expr></expr></expr>		
<expr> + <expr>,</expr></expr>	Left	Addition and subtraction binary operators
<expr> - <expr></expr></expr>		
<expr> ^^^ <expr></expr></expr>	Right	bitwise exclusive or
<expr> &lt; <expr>,</expr></expr>	Left	Comparison operators, bitwise shift, and bitwise 'and'
<expr> &lt;= <expr>,</expr></expr>		and 'or'.
<expr> &gt; <expr>,</expr></expr>		
<expr> &gt;= <expr>,</expr></expr>		
<pre><expr> = <expr>,</expr></expr></pre>		
<expr> &lt;&gt; <expr>,</expr></expr>		
<expr> &lt;&lt;&lt; <expr>&gt;,</expr></expr>		
<expr> &gt;&gt;&gt; <expr>,</expr></expr>		
<expr> &amp;&amp;&amp; <expr>,</expr></expr>		
<pre><expr>     <expr> ,</expr></expr></pre>		
<expr> &amp;&amp; <expr></expr></expr>	Left	Boolean and
<expr>    <expr></expr></expr>	Left	Boolean or

Table 5.4: Some common operators, their precedence, and their associativity. Rows are ordered from highest to lowest precedences, such that <*expr*> * <*expr*> has higher precedence than <*expr*> + <*expr*>. Operators in the same row has same precedence. Full table is given in Table E.5.

the expression for 3.0 * 4.0 * 5.0 associates to the left, and thus is interpreted as (3.0 * 4.0) * 5.0, but gives the same results as 3.0 * (4.0 * 5.0), since association does not matter for multiplication of numbers. However, the expression for 4.0 ** 3.0 ** 2.0 associates to the right, and thus is interpreted as 4.0 ** (3.0 ** 2.0), which is quite different from (4.0 ** 3.0) ** 2.0. Whenever in Advice doubt of association or any other basic semantic rules, it is a good idea to use parentheses as here. It is also a good idea to test your understanding of the syntax and semantic

 $\cdot$  and

 $\cdot$  not

· truth table

a	b	a && b	a    b	not a
false	false	false	false	true
false	true	false	true	true
true	false	false	true	false
true	true	true	true	false

Table 5.5: Truth table for boolean 'and', 'or', and 'not' operators. Value 0 is false and 1 is true.

rules by making a simple script.

#### 5.3 Boolean arithmetic

Boolean arithmetic is the basis of almost all computers and particularly important for controlling program flow, which will be discussed in Chapter 8. Boolean values are one of 2 possible values, true or false, which is also sometimes written as 1 and 0. Basic operations on Boolean values are 'and', 'or', and 'not', which in F# are written respectively as the binary operators &&, ||, and the function not. Since the domain of Boolean values is so small, all possible combination of input on these values can be written on tabular form, known as a truth table, and the truth tables for the basic Boolean operators and functions are shown in Table 5.5. A good mnemonic for remembering the result of the 'and' and 'or' operators is to use 1 for true, 0 for false, multiplication for the Boolean 'and' operator, and addition for Boolean 'or' operator, e.g., true and false in this mnemonic translates to  $1 \cdot 0 = 0$ , and the results translates back to the Boolean value false. In F# the truth table for the basic Boolean operators can be produced by a program as shown in Listing 5.13.

```
Listing 5.13: Boolean operators and truth tables.
> printfn "a b a*b a+b not a"
  printfn "%A %A %A %A %A"
    false false (false && false) (false || false) (not false)
  printfn "%A %A %A %A %A"
    false true (false && true) (false || true) (not false)
  printfn "%A %A %A %A %A"
    true false (true && false) (true || false) (not true)
  printfn "%A %A %A %A %A"
    true true (true && true) (true || true) (not true);;
    a*b a+b not a
false false false true
false true false true true
true false false true false
true true true false
val it : unit = ()
```

Here, we used the printfn function, to present the results of many expressions on something that resembles a tabular form. The spacing produced using the printfn function is not elegant, and in Section 6.5 we will discuss better options for producing more beautiful output. Notice that the arguments for printfn was given on the next line with indentation. The indentation is an important part of telling F# which part of what you write belongs together. This is an example of the so-called lightweight syntax. Generally, F# ignores newlines and whitespaces except when using the lightweight syntax, and the examples of the difference between regular and lightweight syntax is discussed in Chapter 6.

#### 5.4 Integer arithmetic

The set of integers is infinitely large, but since all computers have limited resources, it is not possible to represent it in its entirety. The various integer types listed in Table 5.1 are finite subsets reduced by limiting their ranges. An in-depth description of integer implementation can be found in Appendix B. The type int is the most common type.

Table E.1, E.2, and E.3 give examples operators and functions pre-defined for integer types. Notice that fewer functions are available for integers than for floating point numbers. For most addition, subtraction, multiplication, and negation, the result is straight forward. However, performing arithmetic operations on integers requires extra care, since the result may cause *overflow* and *underflow*. E.g., the range of the integer type sbyte is [-128...127], which causes problems in the example in Listing 5.14.

· overflow · underflow

Here 100 + 30 = 130, which is larger than the biggest sbyte, and the result is an overflow. Similarly, we get an underflow, when the arithmetic result falls below the smallest value storable in an sbyte as demonstrated in Listing 5.15.

```
Listing 5.15: Subtracting integers may cause underflow.

1 > -100y - 30y;;
2 val it : sbyte = 126y
```

I.e., we were expecting a negative number, but got a positive number instead.

The overflow error in Listing 5.14 can be understood in terms of the binary representation of integers: In binary,  $130 = 10000010_2$ , and this binary pattern is interpreted differently as byte and sbyte, see Listing 5.16.

```
Listing 5.16: The left most bit is interpreted differently for signed and unsigned integers, which gives rise to potential overflow errors.
```

```
1  > 0b10000010uy;;
2  val it : byte = 130uy
3
4  > 0b10000010y;;
5  val it : sbyte = -126y
```

That is, for signed bytes, the left-most bit is used to represent the sign, and since the addition of  $100 = 01100100_2$  and  $30 = 00011110_b$  is  $130 = 10000010_2$  causes the left-most bit to be used, then this is wrongly interpreted as a negative number, when stored in an sbyte. Similar arguments can be

made explaining underflows.

The division and remainder operators, which discards the fractional part after division, and the re- integer division mainder operator calculates the remainder after integer division, as demonstrated in Listing 5.17. • remainder

```
Listing 5.17: Integer division and remainder operators.

1 > 7 / 3;;
2 val it : int = 2
3
4 > 7 % 3;;
5 val it : int = 1
```

Together integer division and remainder is a lossless representation of the original number, see Listing 5.18.

And we see that integer division of 7 by 3 followed by multiplication by 3 is less that 7, and the difference is 7 % 3.

Notice that neither overflow nor underflow error gave rise to an error message, which is why such bugs are difficult to find. Dividing any non-zero number with 0 is infinite, which is also outside the domain of any of the integer types, but in this case, F# casts an *exception* as shown in Listing 5.19.

 $\cdot$  exception

The output looks daunting at first sight, but the first and last line of the error message are the most important parts, which tells us what exception was cast and why the program stopped. The middle are technical details concerning which part of the program caused this, and can be ignored for the time being. Exceptions are a type of *runtime error*, and are treated in Chapter 18

 $\cdot$  runtime error

Integer exponentiation is not defined as an operator, but this is available the built-in function pown.

a	b	a ~~~ b	
false	false	false	
false	true	true	
true	false	true	
true	true	false	

Table 5.6: Boolean exclusive or truth table.

This function is demonstrated in Listing 5.20.

```
Listing 5.20: Integer exponent function.

1 > pown 2 5;;
2 val it : int = 32
```

which is equal to  $2^5$ .

For binary arithmetic on integers, the following operators are available: <leftExpr> <<< <ri>which shifts the bit pattern of <leftExpr> <rightExpr> positions to the left while inserting 0's to right; <leftExpr> >>> <rightExpr>, which shifts the bit pattern of <leftExpr> <rightExpr> positions to the right while inserting 0's to left; <expr> &&& <expr>, bitwise 'and', returns the result of taking the Boolean 'and' operator position-wise; <expr> ||| <expr>, bitwise 'or', as 'and' but using the Boolean 'or' operator; and <expr> ~~~ <expr>, bitwise xor, which is returns the result of the Boolean 'xor' operator defined by the truth table in Table 5.6.

 $\cdot xor$ 

· exclusive or

## 5.5 Floating point arithmetic

Like integers, the set of reals is also infinitely large, hence, floating point types are finite subsets reduced by sampling the space of reals. An in-depth description of floating point implementations can be found in Appendix B. The type float is the most common type.

Table E.1, E.2, and E.3 give examples operators and functions pre-defined for floating point types. Note that the remainder operator for floats calculates the remainder after division and discarding the fractional part, see Listing 5.21.

```
Listing 5.21: Floating point division and remainder operators.

1 > 7.0 / 2.5;;
2 val it : float = 2.8

3 4 > 7.0 % 2.5;;
5 val it : float = 2.0
```

The remainder for floating point numbers can be fractional, but division, discarding fractional part, and remainder is still a lossless representation of the original number as demonstrated in Listing 5.22.

#### Listing 5.22: Floating point division, truncation, and remainder is a lossless representation of a number.

```
> float (int (7.0 / 2.5));;
val it : float = 2.0
 (float (int (7.0 / 2.5))) * 2.5;;
val it : float = 5.0
> (float (int (7.0 / 2.5))) * 2.5 + 7.0 % 2.5;;
val it : float = 7.0
```

Arithmetic using float will not cause over- and underflow problems, since the IEEE 754 standard includes the special numbers  $\pm \infty$  and NaN. As shown in Listing 5.23, no exception is thrown.

#### Listing 5.23: Floating point numbers include infinity and Not-a-Number.

```
> 1.0/0.0;;
val it : float = infinity
> 0.0/0.0;;
val it : float = nan
```

However, the float type has limited precision, since there is only a finite number of numbers that can be stored in a float. E.g., addition and subtraction can give surprising results as demonstrated in Listing 5.24.

```
Listing 5.24: Floating point arithmetic has finite precision.
> 357.8 + 0.1 - 357.9;;
val it : float = 5.684341886e-14
```

That is, addition and subtraction associates to the left, hence the expression is interpreted as (357.8 + 0.1) - 357.9, and we see that we do not get the expected 0. The reason is that the calculation is done stepwise, and in the process, the numbers are represented using the imprecise floating point standard. Thus, 357.8 + 0.1 is represented as number close to but not identical to what 357.9 is represented as, and thus, when subtracting these two representations, we get a very small number but not 0. Such errors tend to accumulate and comparing the result of expressions of floating point values should therefore be treated with care. Thus, equivalence of two floating point expressions should only be considered up to sufficient precision, e.g., comparing 357.8 + 0.1 and 357.9 up to 1e-10 precision should be tested as, abs ((357.8 + 0.1) - 357.9) < 1e-10.

#### 5.6 Char and string arithmetic

Addition is the only operator defined for characters. Nevertheless, character arithmetic is often done by casting to integer. A typical example is conversion of case, e.g., to convert the lowercase character 'z' to uppercase, we use the ASCIIbetical order and add the difference between any Basic Latin Block · ASCIIbetical order letters in upper- and lowercase as integers and cast back to char, see Listing 5.25.

· . []

#### Listing 5.25: Converting case by casting and integer arithmetic.

```
| > char (int 'z' - int 'a' + int 'A');;
| val it : char = 'Z'
```

I.e., the code point difference between upper and lower case for any alphabetical character 'a' to 'z' is constant, hence we can change case by adding or subtracting the difference between any corresponding character. Unfortunately, this does not generalize to characters from other languages.

A large collection of operators and functions exist for string. The simplest is concatenation using the "+" operator as demonstrated in Listing 5.26.

```
Listing 5.26: Example of string concatenation.

1 > "hello" + " " + "world";;
2 val it : string = "hello world"
```

Characters and strings cannot be concatenated, which is why the above example used the string of a space " " instead of the space character ' '. The characters of a string may be indexed as using the . [] notation. This is demonstrated in Listing 5.27.

Notice that the first character has index 0, and to get the last character in a string, we use the string's length property. This is done as shown in Listing 5.28.

```
Listing 5.28: String length attribute and string indexing.

1 > "abcdefg".Length;;
2 val it : int = 7

3 
4 > "abcdefg".[7-1];;
5 val it : char = 'g'
```

Since index counting starts at 0, and the string length is 7, then the index of the last character is 6. The is a long list of built-in functions in System.String for working with strings, some of which will be discussed in Section 11.1.

The dot notation is an example of Structured programming, where technically speaking, the string "abcdefg" is an immutable object of class string, [] is an object method, and Length is a property. For more on object, classes, and methods see Chapter 20.

 $\begin{array}{c} \cdot \ dot \ notation \\ \cdot \ object \\ \cdot \ class \end{array}$ 

· method

Strings are compared letter by letter. For two strings to be equal, they must have the same length and all the letters must be identical. E.g., "abs" = "absalon" is false, while "abs" = "abs" is true. The "<>" operator is the boolean negation of the "=" operator, e.g., "abs" <> "absalon" is true, while "abs" <> "abs" is false. For the "<", "<=", ">", and ">=" operators, the strings are ordered alphabetically, such that "abs" < "absalon" && "absalon" < "milk" is true, that is, the "<" operator on two strings is true, if the left operand should come before the right, when sorting alphabetically. The algorithm for deciding the boolean value of leftOp < rightOp is as follows: we start by examining the first character, and if leftOp.[0] and rightOp.[0] are different, then the leftOp < rightOp is equal to leftOp.[0] < rightOp.[0]. E.g., "milk" < "abs" is the same as 'm' < 'a', which is false, since the letter 'm' does not come before the letter 'a' in the alphabet, or more precisely, the codepoint of 'm' is not less than the codepoint of 'a'. If leftOp.[0] and rightOp.[0] are equal, then we move onto the next letter and repeat the investigation, e.g., "abe" < "abs" is true, since "ab" = "ab" is true and 'e' < 's' is true. If we reach the end of either of the two strings, then the short is smaller than the larger, e.g., "abs" < "absalon" is true, while "abs" < "abs" is false. The "<="", ">", ">", ", ", ">", ", and ">=" operators are defined similarly.

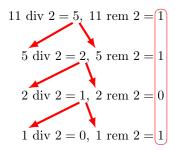
# 5.7 Programming intermezzo: Hand conversion between decimal and binary numbers

Conversion of integers between decimal and binary form is a key concept in order to understand some of the basic properties of calculations on the computer. From binary to decimal is straight forward using the power-of-two algorithm, i.e., given a sequence of n+1 bits that represent an integer  $b_n b_{n-1} \dots b_0$ , where  $b_n$  and  $b_0$  are the most and least significant bits, then the decimal value is calculated as,

$$v = \sum_{i=0}^{n} b_i 2^i \tag{5.1}$$

For example,  $10011_2 = 1 + 2 + 16 = 19$ . From decimal to binary is a little more complex, but a simple divide-by-two algorithm exists. The key to understanding the divide-by-two algorithm is to realize that when you divide a number by two, then that is equivalent to shifting its binary representation 1 to the right. E.g.,  $10 = 1010_2$  and  $10/2 = 5 = 101_2$ . Odd numbers have  $b_0 = 1$ , e.g.,  $11_{10} = 1011_2$  and  $11_{10}/2 = 5.5 = 101.1_2$ . Hence, if we divide any number by two and get a non-integer number, then its least significant bit was 1. Another way to express this is that the least significant bit is the remainder after integer division by two. Sequential application of this idea leads directly to the divide-by-two algorithm. E.g., if we were to convert the number  $11_{10}$  on decimal form to binary form we would

perform the following steps:



Here we used div and rem to signify the integer division and remainder operators. The algorithm stops, when the result of integer division is zero. Reading off the remainder from below and up we find the sequence  $1011_2$ , which is the binary form of the decimal number  $11_{10}$ . Using interactive mode, we can calculate the same as shown in Listing 5.29.

Thus, but reading the second integer-response from printfn from below and up, we again obtain the binary form of  $11_{10}$  to be  $1011_2$ . For integers with a fractional part, the divide-by-two may be used on the whole part, while multiply may be used in a similar manner on the fractional part.

# 6 | Values and functions

In the previous chapter, we saw how to use F# as a calculator working with literals, operators and built-in functions. To save time and make programs easier to read and debug, it is useful to bind expressions to identifiers either as new constants, functions, or operators. As an example, consider the problem,

# Problem 6.1

For given set constants a, b, and c, solve for x in

$$ax^2 + bx + c = 0 (6.1)$$

To solve for x we use the quadratic formula from elementary algebra,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a},\tag{6.2}$$

which gives the general solution for any values of the coefficients. Here, we will assume a positive discriminant,  $b^2 - 4ac > 0$ . In order to write a program, where the code may be reused later, we define a function discriminant: float -> float -> float, that is, a function that takes 3 arguments, a, b, and c, and calculates the discriminant. Details on function definition is given in Section 6.2. Likewise, we will define functions positiveSolution: float -> float -> float -> float and negativeSolution: float -> float -> float -> float, that also takes the polynomial's coefficients as arguments and calculates the solution corresponding to choosing the postive and negative sign for  $\pm$  in the equation. Our solution thus looks like Listing 6.1.

# Listing 6.1 identifiersExample.fsx: Finding roots for quadratic equations using function name binding. let discriminant a b c = b ** 2.0 - 4.0 * a * c let positiveSolution a b c = (-b + sqrt (discriminant a b c)) / (2.0 * a)let negativeSolution a b c = (-b - sqrt (discriminant a b c)) / (2.0 * a)let a = 1.0let b = 0.0c = -1.0let d = discriminant a b c let xp = positiveSolution a b c let xn = negativeSolution a b c do printfn "0 = %A * x ** 2.0 + %A * x + %A" a b c do printfn " has discriminant %A and solutions %A and %A" d xn xp \$ fsharpc --nologo identifiersExample.fsx && mono identifiersExample.exe 0 = 1.0 * x ** 2.0 + 0.0 * x + -1.0has discriminant 4.0 and solutions -1.0 and 1.0

Here, we have further defined names of values a, b, and c used as input to our functions, and the results of function application is bound to the names d, xn, and xp. The names of functions and values given here are examples of identifiers, and with these, we may reuse the quadratic formulas and calculated values later, while avoiding possible typing mistakes and reducing amount of code, which needs to be debugged.

The use of identifiers is central in programming. For F# not to be confused by built-in functionality, identifiers must follow a specific set of rules:

Identifier

 $\cdot$  identifier

- Identifiers are used as names for values, functions, types etc.
- They must start with a letter or underscore ', but can be followed by zero or more of letters, digits, and a range of special characters except SP, LF, and CR (space, line feed, and carriage return). Letters are most unicode codepoints that produces regular letters, see Appendix C.3 for more on codepoints.
- They can also be a sequence of identifiers separated by a period.
- They cannot be keywords, see Table 6.1.

Examples of identifiers are: a, the Character 9, Next_Word, _tok, and f.sharp.rocks. Since programmers often work in multilingual environment dominated by the English language Restrict identifiers Advice to use letters from the english alphabet, numbers, period, and ' '. However, the number of possible identifiers is enormous: the full definition referes to the Unicode general categories described in Appendix C.3, and there are currently 19.345 possible Unicode code points in the letter category and 2.245 possible Unicode code points in the special character category.

Identifiers may be used to carry information about their intended content and use, and careful selection of identifiers can aid programmers communicate thoughts about the code. Thus, identifiers are often a word or several concatenated words from the human language. For example in the function definition let discriminant a b c = b ** 2.0 - 4.0 * a * c, the function identifier has been chosen to be discriminant. F# places no special significance to the word 'discriminant', and the program would work exactly the same, had the function been called let f a b c = b ** 2.0 - 4.0 * a * c. However, to programmers the word 'discriminant' informs us of the intended role of the function, and

Type	Keyword
Regular	abstract, and, as, assert, base, begin, class, default, delegate, do,
	done, downcast, downto, elif, else, end, exception, extern, false,
	finally, for, fun, function, global, if, in, inherit, inline, interface,
	internal, lazy, let, match, member, module, mutable, namespace, new,
	null, of, open, or, override, private, public, rec, return, sig, static,
	struct, then, to, true, try, type, upcast, use, val, void, when, while,
	with, and yield.
Reserved	atomic, break, checked, component, const, constraint, constructor,
	continue, eager, fixed, fori, functor, include, measure, method, mixin,
	object, parallel, params, process, protected, pure, recursive, sealed,
	tailcall, trait, virtual, and volatile.
Symbolic	let!, use!, do!, yield!, return!,  , ->, <-, ., :, (, ), [, ], [<, >], [ ,  ], {,
	}, ', #, :?>, :?, :>,, ::, :=, ;;, ;, =, _, ??, (*), <@, @>, <@@, and @@>.
Reserved symbolic	~ and `

Table 6.1: Table of (possibly future) keywords and symbolic keywords in F#.

thus is much preferred. This is a general principle, identifier names should be chosen to reflect their semantic value. The arguments a, b, and c are short, but adheres to a textbook tradition of elementary algebra. Again, we might as well have used, let discriminant c a b = a ** 2.0 - 4.0 * c * b, which is semantically identical to the original expression, but due to tradition, this would confuse most readers of the code. Thus, identifier names should be chosen consistently with readers tradition. Finally, identifiers are often concatenations of words, as positiveSolution in Listing 6.1. Concatenations can be difficult to read. Without the capitalised second word, we would have had positive solution. This is readable at most times, but takes longer time for humans to parse in general. Typical solutions are to use a separator such as positive_solution, lower camel case also known as mixed case as in the example positiveSolution, and upper camel case also known as pascal case as PositiveSolution. In this book we use lower camel case except where F# requires a capital first letter. Again, the choice does not influence what a program does, only how readable it is to a fellow programmer. The important part is that identifier names consisting of concatenated words are often preferred over few character names, and concatenation should be emphasized, e.g., by camel casing. The length of identifier names is a balancing act, since when working with large programs, very long identifier names can be tiresome to write, and a common practice is that the length of identifier names is proportional to the complexity of the program. I.e., complex programs use long names, simple use short. What is complex and what is simple is naturally in the eye of the beholder, but when we program, remember that a future reader of the program most likely has not had time to work the problem as long as the programmer, thus choose identifier names as if you were to explain the meaning of a program to a knowledgable outsider.

Another key concept in F# is expressions. An expression can be a mathematical expression, such as 3*5, a function application, such as f3, and many other things. Central in this chapter is the binding of values and functions to identifiers, which is done with the keyword let, e.g., let a = 1.0.

Expressions are the main workhorse of F# and have an enormous variety in how they may be written, we will in this book gradually work through some of the more important facets.

# Expressions

- An Expression is a computation such as 3 * 5.
- They can be value bindings between identifiers and expressions that evaluate to a value or a function, see Sections 6.1 and 6.2.
- They can be do bindings that produce side-effects and whose result is ignored, see Section 6.2
- They can be assignments to variables, see Section 6.1.

Advice

- $\cdot$  lower camel case
- $\cdot$  mixed case
- $\cdot$  upper camel case
- · pascal case Advice

Advice

 $\cdot$  expression

- They can be a sequence of expressions separated with ";" lexeme.
- They can be annotated with a type using the ":" lexeme.

Before we begin a deeper discussion on bindings, note that F# has adheres to two different syntaxes: regular and lightweight. In the regular syntax, newlines and whitespaces are generally ignored, while in lightweight syntax, certain keywords and lexemes may be replaced by specific use of newlines and whitespaces. Lightweight syntax is the most common, but the syntaxes may be mixed, and we will highlight the options, when relevant.

· lightweight syntax

## 6.1Value bindings

Binding identifiers to literals or expressions that are evaluated to be values, is called *value-binding*, · value-binding and examples are let a = 3.0 and let b = cos 0.9. Value bindings have the following syntax,

```
Listing 6.2 Value binding expression.
let <valueIdent> = <bodyExpr> [in <expr>]
```

The let keyword binds a value-identifier <valueIdent> with an expression <bodyExpr> that evaluates · let to a value. If the *in* keyword is used, then the value-identifier becomes synonymous with the evaluated value in <expr> only. The square bracket notation [] means that the enclosed is optional. Here the meaning is that for lightweight syntax, the in keyword is replaced with a newline, and the binding is valid in the following lines at the level of scope of the value-binding or deeper lexically.

· lexically

The value identifier annotated with a type using the ":" lexeme followed by the name of a type, e.g., int. The "_" lexeme may be used as a value-identifier. This lexeme is called the wildcard pattern, and for value-bindings it means that the <bodyExpr> is evaluated, but the result is discarded. See · wildcard Chapter 15 for more details on patterns.

For example, letting the identifier p be bound to the value 2.0 and using it in an expression is done as shown in Listing 6.3.

```
Listing 6.3 letValue.fsx:
The identifier p is used in the expression following the
                                                        keyword.
let p = 2.0 in do printfn "%A" (3.0 ** p)
$ fsharpc --nologo letValue.fsx && mono letValue.exe
 9.0
```

F# will ignore most newlines between lexemes, i.e., the above is equivalent to writing as shown in Listing 6.4.

# Listing 6.4 letValueLF.fsx: Newlines after make the program easier to read. 1 let p = 2.0 in 2 do printfn "%A" (3.0 ** p) 1 \$ fsharpc --nologo letValueLF.fsx && mono letValueLF.exe 2 9.0

F# also allows for an alternative notation called *lightweight syntax*, where e.g., the **in** keyword is · lightweight syntax replaced with a newline, and the expression starts on the next line at the same column as **let** starts in, i.e., the above is equivalent to Listing 6.5.

```
Listing 6.5 letValueLightWeight.fsx:
Lightweight syntax does not require the keyword, but expression must be aligned with the keyword.

1 let p = 2.0
2 do printfn "%A" (3.0 ** p)

1 $ fsharpc --nologo letValueLightWeight.fsx
2 $ mono letValueLightWeight.exe
3 9.0
```

The same expression in interactive mode will also respond the inferred types as, e.g., shown in Listing 6.6.

```
Listing 6.6: Interactive mode also responds inferred types.

1 > let p = 2.0
2 - do printfn "%A" (3.0 ** p);;
3 9.0
4 val p : float = 2.0
5 val it : unit = ()
```

By the val keyword in the line val p: float = 2.0 we see that p is inferred to be of type float and bound to the value 2.0. The inference is based on the type of the right-hand-side, which is of type float. Identifiers may be defined to have a type using the ":" lexeme, but the types on the left-hand-side and right-hand-side of the "=" lexeme must be identical. I.e., mixing types gives an error as shown in Listing 6.7.

# Listing 6.7 letValueTypeError.fsx: Binding error due to type mismatch. let p: float = 3 do printfn "%A" (3.0 ** p) fsharpc --nologo letValueTypeError.fsx && mono letValueTypeError.exe letValueTypeError.fsx(1,17): error FS0001: This expression was expected to have type 'float' but here has type 'int'

Here, the left-hand-side is defined to be an identifier of type float, while the right-hand-side is a literal of type integer.

An expression can be a sequence of expressions separated by the lexeme ";", see Listing 6.8.

```
Listing 6.8 letValueSequence.fsx:
A value-binding for a sequence of expressions.

1 let p = 2.0 in do printfn "%A" p; do printfn "%A" (3.0 ** p)

1 $ fsharpc --nologo letValueSequence.fsx && mono letValueSequence.exe
2 2.0
3 9.0
```

The lightweight syntax automatically inserts the ";" lexeme at newlines, hence using the lightweight syntax the above is the same as shown in Listing 6.9.

```
Listing 6.9 let ValueSequenceLight Weight.fsx:
A value-binding for a sequence using lightweight syntax.

1 let p = 2.0
2 do printfn "%A" p
3 do printfn "%A" (3.0 ** p)

1 $ fsharpc --nologo letValueSequenceLightWeight.fsx
2 $ mono letValueSequenceLightWeight.exe
3 2.0
4 9.0
```

A key concept of programming is scope. In F#, the scope of a value-binding is lexically meaning that  $\cdot$  scope when F# determines the value bound to a name, it looks left and upward in the program text for the let statement defining it, see, e.g., Listing 6.10.

# Listing 6.10 letValueScopeLower.fsx: Redefining identifiers is allowed in lower scopes. 1 let p = 3 in let p = 4 in do printfn " %A" p; 1 \$ fsharpc --nologo letValueScopeLower.fsx && mono letValueScopeLower.exe 2 4

F# also has to option of using dynamic scope, where the value of a binding is defined by when it is used, and this will be discussed in Section 6.7.

Scopes are given levels, and scopes may be nested, where the nested scope has a level one lower than its parent.¹ F# distinguishes between the top and lower levels, and at the top level in the lightweight syntax, redefining values is not allowed, as shown in Listing 6.11.

# Listing 6.11 letValueScopeLowerError.fsx: Redefining identifiers is not allowed in lightweight syntax at top level. 1 let p = 3 2 let p = 4 3 do printfn "%A" p; 1 \$ fsharpc --nologo -a letValueScopeLowerError.fsx 2 letValueScopeLowerError.fsx(2,5): error FS0037: Duplicate definition of value 'p'

But using parentheses, we create a block, i.e., a  $nested\ scope$ , and then redefining is allowed, as  $\cdot$  block demonstrated in Listing 6.12.  $\cdot$  nested scope

```
Listing 6.12 letValueScopeBlockAlternative3.fsx:

A block may be created using parentheses.

(
let p = 3
let p = 4
do printfn "%A" p
)

fsharpc --nologo letValueScopeBlockAlternative3.fsx
mono letValueScopeBlockAlternative3.exe
4
```

In both cases we used indentation, which is good practice, but not required here. Bindings inside are not available outside the nested scope as shown in Listing 6.13.

¹Jon: Drawings would be good to describe scope

# Listing 6.13 letValueScopeNestedScope.fsx: Bindings inside a scope are not available outside. let p = 3 ( let q = 4 do printfn "%A" q ) do printfn "%A %A" p q fsharpc --nologo -a letValueScopeNestedScope.fsx letValueScopeNestedScope.fsx(6,22): error FS0039: The value or constructor 'q' is not defined. Maybe you want one of the following: p

Nesting is a natural part of structuring code, e.g., through function definitions to be discussed in Section 6.2 and flow control structures to be discussed in Chapter 8. Blocking code by nesting is a key concept for making robust code that is easy to use by others without the user necessarily needing to know the details of the inner workings of a block of code.

Defining blocks is useful for controlling the extend of a lexical scope of bindings. For example, adding a second printfn statement as in Listing 6.14. will print the value 4 last bound to the identifier p, since F# interprets the above as let p=3 in let p=4 in (printfn "%A" p; printfn "%A" p).

```
Listing 6.14 letValueScopeBlockProblem.fsx:
Overshadowing hides the first binding.

1 let p = 3 in let p = 4 in do printfn "%A" p; do printfn "%A" p

1 $ fsharpc --nologo letValueScopeBlockProblem.fsx
2 $ mono letValueScopeBlockProblem.exe
3 4
4 4
```

Had we intended to print the two different values of p, the we should have create a block as in Listing 6.15.

```
Listing 6.15 letValueScopeBlock.fsx:
Blocks allow for the return to the previous scope.

1 let p = 3 in (let p = 4 in do printfn "%A" p); do printfn "%A" p;

1 $ fsharpc --nologo letValueScopeBlock.fsx && mono letValueScopeBlock.exe
2 4
3 3
```

Here, the lexical scope of let p = 4 in ... is for the nested scope, which ends at ")", returning to the lexical scope of let p = 3 in ....

# 6.2 Function bindings

A function is a mapping between an input and output domain. A key advantage of using functions, when programming, is that they encapsulate code into smaller units, that are easier to debug and may be reused. F# is a functional first programming language, and offers a number of alternative methods for specifying parameters, which will be discussed in this section. Binding identifiers to functions follows a syntax similar to value-binding,

```
Listing 6.16 Function binding expression

1 let <funcIdent> <arg> {<arg>} | () = <bodyExpr> [in <expr>]
```

Here  $\leq$  funcIdent> is an identifier and is the name of the function,  $\leq$  is zero or more identifiers, that bind to the value used when calling the function, and which is to be used in the body of the function, the expression  $\leq$  bodyExpr>. The | notation denotes a choice, i.e., either that on the left-hand-side or that of the right-hand-side. Thus let f x = x * x and let f () = 3 are valid function bindings, but let f = 3 would be a value binding not a function binding. The arguments and the function may be annotated with a type, in which case for arguments we write

```
Listing 6.17 Function binding expression

let <funcIdent> (<arg> : <type>) {(<arg> : <type>)} : <type> | () : <type>
= <bodyExpr> [in <expr>]
```

where <type> is a name of an existing type. The argument types are given In parantheses, and the return type is given last.

Functions are a key concept in F# and in this chapter, we will discuss the very basics. Recursive functions will be discussed in Chapter 8, and higher order functions in Chapter 16.

An example of defining a function and using in interactive mode is shown in Listing 6.18.

```
Listing 6.18: An example of a binding of an identifier and a function.

| Solid Structure | Solid Stru
```

and we see that the function is interpreted to have the type val sum: x:float -> y:float -> float. The "->" lexeme means a mapping between sets, in this case floats. The function is also a higher order function, to be discussed in detail below, and here it suffices to think of sum as a function that takes 2 floats as argument and returns a float.

Not all types need to be declared, just sufficient for F# to be able to infer the types for the full statement. In the example, one specification is sufficient, and we could just have specified the type of the result as in Listing 6.19.

```
Listing 6.19 letFunctionAlterantive.fsx:
All types need most often not be specified.
let sum x y : float = x + y
```

Or even just one of the arguments as in Listing 6.20.

```
Listing 6.20 letFunctionAlterantive2.fsx:
Just one type is often enough for F# to infer the rest.
let sum (x : float) y = x + y
```

In both cases, since the + operator is only defined for operands of the same type, then when the type · operator of either the result, any or both operands are declared, then the type of the remaining follows directly. As for values, lightweight syntax automatically inserts the keyword in and the lexeme ";" as shown in Listing 6.21.

```
Listing 6.21 letFunctionLightWeight.fsx:
Lightweight syntax for function definitions.
let sum x y : float = x + y
let c = sum 357.6 863.4
do printfn "%A" c
$ fsharpc --nologo letFunctionLightWeight.fsx
$ mono letFunctionLightWeight.exe
1221.0
```

Arguments need not always be inferred to types, but may be of generic type, which F# prefers, when type safety is ensured as shown in Listing 6.22.

· type safety

```
Listing 6.22: Type safety implies that a function will work for any type, and hence
it is generic.
```

```
> let second x y = y
- let a = second 3 5
- do printfn "%A" a
- let b = second "horse" 5.0
 do printfn "%A" b;;
5
5.0
val second : x:'a \rightarrow y:'b \rightarrow 'b
val a : int = 5
val b : float = 5.0
val it : unit = ()
```

Here, the function second does not use the first argument x, which therefore can be of any type, and which F# therefore calls 'a, and the type of the second element, y, can also be of any type and not necessarily the same as x, so it is called 'b. Finally the result is the same type as y, whatever it is. This is an example of a *generic function*, since it will work on any type.

· generic function

A function may contain a sequence of expressions, but must return a value. E.g., the quadratic formula may be written as shown in Listing 6.23.

# Listing 6.23 identifiersExampleAdvance.fsx: A function may contain sequences of expressions. let solution a b c sgn = let discriminant a b c = b ** 2.0 - 2.0 * a * c let d = discriminant a b c (-b + sgn * sqrt d) / (2.0 * a)let a = 1.0let b = 0.0let c = -1.0let xp = solution a b c +1.0let xn = solution a b c -1.0do printfn "0 = %A * x ** 2.0 + %A * x + %A" a b c do printfn " has solutions %A and %A" xn xp \$ fsharpc --nologo identifiersExampleAdvance.fsx \$ mono identifiersExampleAdvance.exe 0 = 1.0 * x ** 2.0 + 0.0 * x + -1.0has solutions -0.7071067812 and 0.7071067812

Here, we used the lightweight syntax, where the "=" identifies the start of a nested scope, and F# identifies the scope by indentation. The amount of space used for indentation is does not matter, but all lines following the first must use the same. The scope ends before the first line with the previous indentation or none. Notice how the last expression is not bound to an identifier, but is the result of the function, i.e., in contrast to many other languages, F# does not have an explicit keyword for returning values, but requires a final expression, which will be returned to the caller of the function. Note also that since the function discriminant is defined in the nested scope of solution, then discriminant cannot be called outside solution, since the scope ends before let a = 1.0.

Lexical scope and function definitions can be a cause of confusion as the following example in List-  $\cdot$  lexical scope ing 6.24 shows.²

```
Listing 6.24 lexicalScopeNFunction.fsx:
Lexical scope means that f(z) = 3x and not 4x at the time of calling.

1 let testScope x =
2 let a = 3.0
3 let f z = a * z
4 let a = 4.0
5 f x
6 do printfn "%A" (testScope 2.0)

1 $ fsharpc --nologo lexicalScopeNFunction.fsx
2 $ mono lexicalScopeNFunction.exe
3 6.0
```

²Jon: Add a drawing or possibly a spell-out of lexical scope here.

Here, the value-binding for a is redefined, after it has been used to define a helper function f. So which value of a is used, when we later apply f to an argument? To resolve the confusion, remember that value-binding is lexically defined, i.e., the binding let f z = a * z uses the value of a, it has by the ordering of the lines in the script, not dynamically by when f was called. Hence, think of lexical Advice scope as substitution of an identifier with its value or function immediately at the place of definition. I.e., since a and 3.0 are synonymous in the first lines of the program, then the function f is really defined as, let f z = 3.0 * z.

· ->

Functions do not need a name, but may be declared as an anonymous function using the fun keyword and the "->" lexeme, as shown in Listing 6.25.

· anonymous function · fun

```
Listing 6.25 functionDeclarationAnonymous.fsx:
Anonymous functions are functions as values.
let first = fun x y -> x
do printfn "%d" (first 5 3)
$ fsharpc --nologo functionDeclarationAnonymous.fsx
$ mono functionDeclarationAnonymous.exe
```

Here, a name is bound to an anonymous function, which returns the first of two arguments. The difference to let first x y = x is that anonymous functions may be treated as values, meaning that they may be used as arguments to other functions, and new values may be reassigned to their identifiers, when mutable, as will be discussed in Section 6.7. A common use of anonymous functions is as as arguments to other functions, as demonstrated in Listing 6.26.

```
Listing 6.26 functionDeclarationAnonymousAdvanced.fsx:
Anonymous functions are often used as arguments for other functions.
let apply f x y = f x y
let mul = fun a b \rightarrow a * b
do printfn "%d" (apply mul 3 6)
$ fsharpc --nologo functionDeclarationAnonymousAdvanced.fsx
$ mono functionDeclarationAnonymousAdvanced.exe
```

Note that here apply is given 3 arguments, the function mul and 2 integers. It is not given the result of mul 3 6, since that would not match the definition of apply. Anonymous functions and functions Advice as arguments are powerfull concepts, but tend to make programs harder to read, and their use should be limited.

The result of one function is often used as an argument of another. This is function composition, and an example is shown in Listing 6.27.

# Listing 6.27 functionComposition.fsx: Composing functions using intermediate bindings. let f x = x + 1 let g x = x * x let a = f 2 let b = g a let c = g (f 2) do printfn "a = %A, b = %A, c = %A" a b c f sharpc --nologo functionComposition.fsx mono functionComposition.exe a = 3, b = 9, c = 9

In the example we combine two functions f and g by storing the result of f 2 in a and using that as argument of g. This is the same as g (f 2), and in the later case, the compile creates a temporary value for f 2. Such compositions are so common in F# that a special operator has been invented called the *piping* operators, ">/" and "</". They are used as demonstrated in Listing 6.28.

```
Listing 6.28 functionPiping.fsx:
Composing functions by piping.

let f x = x + 1
let g x = x * x

let a = g (f 2)
let b = 2 |> f |> g
let c = g <| (f <| 2)
do printfn "a = %A, b = %A, c = %A" a b c

fsharpc --nologo functionPiping.fsx && mono functionPiping.exe
a = 9, b = 9, c = 9
```

The example shows regular composition and left-to-right and right-to-left piping. The word piping is a picture of data flowing through pipes, where functions are places, where the pipes have been assembled and the data changes. The three expressions in Listing 6.28 performes the same calculation. The left-to-right piping in line 5 corresponds to the left-to-right reading direction of many human languages, i.e., the value 2 is used as argument to f, and the result is used as argument to g. However, this is opposite arithmetic composition in line 4. Right-to-left piping has the order of arithmetic composition. Unfortunately, since f evaluates the expression from the left, without the parenthesis in line f, f and f in the f evaluates argument not a function. F# can also define composite on a function level, further discussion on this is deferred to Chapter 16. The piping operator comes in four variants: "|>|", "|", "||", and "|0". The allow for piping between pairs and triples to functions of 2 and 3 arguments, see Listing 6.29 for an example.

· piping

 $\cdot$  lstinline|>

. <|

# Listing 6.29 functionTuplePiping.fsx: Tuples can be piped to functions of more than one argument. let f x = printfn "%A" x let g x y = printfn "%A %A" x y let h x y z = printfn "%A %A %A" x y z 1 |> f (1, 2) | | > g $(1, 2, 3) \mid \mid \mid > h$ \$ fsharpc --nologo functionTuplePiping.fsx \$ mono functionTuplePiping.exe 1 1 2 1 2 3

The example demonstrates left-to-right piping, right-to-left works analogously.³

A procedure is a generalisation of the concept of functions, and in contrast to functions procedure · procedure need not return values. This is demonstrated in Listing 6.30.

```
Listing 6.30 procedure.fsx:
A procedure is a function that has no return value, and in F\# returns "()".
let printIt a = printfn "This is '%A'" a
do printIt 3
do printIt 3.0
$ fsharpc --nologo procedure.fsx && mono procedure.exe
This is '3'
This is '3.0'
```

In F# this is automatically given the unit type as return value. Procedural thinking is useful for encapsulation of scripts, but is prone to side-effects and should be minimized by being replaced by functional thinking. More on side-effects in Section 6.7. Procedural thinking is useful for encapsulation, but is prone to side-effects and should be minimized by being replaced by functional thinking.

·encapsulation  $\cdot$  side-effects Advice

In F# functions (and procedures) are first-class citizens, which means that functions are values: They may be passed as arguments, returned from a function, and bound to a name. For first-class citizens, the name it is bound to does not carry significance to the language, as, e.g., illustrated with the use of anonymous functions. Technically, a function is stored as a closures. A closure is a description of  $\cdot$  closures the function, its arguments, its expression, and the environment, at the time it was created, i.e., the tripple: (args, exp, env). Consider the listing in Listing 6.31.

· first-class citizens

³Jon: Tuples have not yet been introduced!

# Listing 6.31 functionFirstClass.fsx: The function timesTwo has a non-trivial closure. 1 let mul x y = x * y 2 let factor = 2.0 3 let applyFactor fct x = 4 let a = fct factor x 5 string a 6 do printfn "%g" (mul 5.0 3.0) 8 do printfn "%s" (applyFactor mul 3.0) 1 \$ fsharpc --nologo functionFirstClass.fsx && mono functionFirstClass.exe 2 15 3 6

It defines two functions mul and applyFactor, where the later is a higher order function taking another function as argument and uses part of the environment to produce its result. The two closures are,

$$mul: (args, exp, env) = ((x, y), (x * y), ())$$

$$(6.3)$$

$$\texttt{applyFactor}: (args, exp, env) = \left((\texttt{x}, \texttt{fct}), \left( \begin{matrix} \texttt{let a} \\ \texttt{string a} \end{matrix} \right. = \begin{matrix} \texttt{fct factor x} \\ \texttt{y} \end{matrix} \right), \left( \texttt{factor} \rightarrow 2.0 \right) \right) \tag{6.4}$$

The function mul does not use its environment, and everything needed to evaluate its expression are values for its arguments. The function applyFactor also takes two arguments, a function and a value. It uses factor from the environment, thus this is stored in its closure. When mul is given as an argument in Listing 6.31 line 8, then it is its closure, which is given to applyFactor, and the closure contains everything that applyFactor requires to use mul. Likewise, if applyFactor is given as argument to yet another function, then its closure includes the relevant part of its environment at time of definition, i.e., factor, such that when applyFactor is applied to two arguments, then its closure contains everything needed to evaluate its expression.

# 6.3 Operators

Operators are functions, and in F#, the infix multiplication operator + is equivalent to the function (+), e.g.,

```
Listing 6.32 addOperatorNFunction.fsx:

Operators have function equivalents.

let a = 3.0
let b = 4.0
let c = a + b
let d = (+) a b
do printfn "%A plus %A is %A and %A" a b c d

fsharpc --nologo addOperatorNFunction.fsx
mono addOperatorNFunction.exe
let c = a + b
sharpc --nologo addOperatorNFunction.fsx
let c = a + b
let d = (+) a b
```

All operators have this option, and you may redefine them and define your own operators, but in F#

names of user-defined operators are limited.

operator

· operator

- A unary operator name can be: "+", "-", "+.", "-.", "%", "&", "&", "~~", "~~", "~~", "~~", ..., unary operator apostropheOp. Here apostropheOp is an operator name starting with "!" followed by one or more of either "!", "%", "&", "*", "+", "-", ".", "/", "<", "=", ">", "@", "~", "|", "~", but apostropheOp cannot be "!=".
- An binary operator name can be: "+", "-", "+.", "-.", "%", "&", "&", ":=", "::", "\$", "?", dotOp. Here dotOp is an operator name starting with "." followed by "+", "-", "+.", "-.", "%", "&", "&", "&", "+", "|", "<", ">", "=", "|", "&", "-", "*", "/", "%", "!=". Only "?" and "?<-" may start with "?".

· binary operator

The precedence rules and associativity of user-defined operators follows the rules for which they share prefixes with built-in rules, see Table E.5. E.g., .*, +++, and <+ are valid operator names for infix operators, they have precedence as ordered, and their associativity are all left. Using ~ as the first character in the definition of an operator makes the operator unary and will not be part of the name. Examples of definitions and use of operators are,

```
Listing 6.33 operator Definitions.fsx:
Operators may be (re)defined by their function equivalent.
let (.*) x y = x * y + 1
 printfn "%A" (3 .* 4)
let (+++) x y = x * y + y
printfn "%A" (3 +++ 4)
let (<+) x y = x < y + 2.0
printfn "%A" (3.0 <+ 4.0)
let (^{-}+.) x = x+1
printfn "%A" (+.1)
$ fsharpc --nologo operatorDefinitions.fsx
$ mono operatorDefinitions.exe
13
16
true
2
```

Operators beginning with * must use a space in its definition, ( * in order for it not to be confused with the beginning of a comment (*, see Chapter 7 for more on comments in code.

Beware, redefining existing operators lexically redefines all future uses of the operators for all types, hence it is not a good idea to redefine operators, but better to define new. In Chapter 20 Advice we will discuss how to define type specific operators including prefix operators.

# 6.4 Do bindings

Aside from let bindings, that binds names with values or functions, sometimes we just need to execute code. This is called a do binding or alternatively a statement. The syntax is as follows.

- ·do
- $\cdot$  do binding
- $\cdot \, statement$

```
Listing 6.34 Syntax for do bindings.

[do ] <expr>
```

The expression <expr> must return unit. The keyword do is optional in most cases, but using it emphasises that the expression is not a function that returns a useful value. Procedures are examples of such expressions and a very useful family of procedures are the printf family described below. In the remainder of this book, we will refrain from using the do keyword.

# 6.5 The Printf function

A common way to output information to the console is to use one of the family of *printf* commands. · printf These functions are special, since they take a variable number of arguments, and the number is decided by the first - the format string,

```
Listing 6.35 printf statement.

printf <format-string> {<ident>}
```

where a formatString is a string (simple or verbatim) with placeholders. The function printf prints formatString to the console, where all placeholder has been replaced by the value of the corresponding argument formatted as specified, e.g., in printfn "1 2 %d" 3 the formatString is "1 2 %d", and the placeholder is %d, and the printf replaced the placeholder with the value of the corresponding argument, and the result is printed to the console, in this case 1 2 3. There are specifiers for all the basic types and more as elaborated in Table 6.2. The placeholder can be given a specified with, either by setting a specific integer, or using the * character, indicating that the with is given as an argument prior to the replacement value. E.g., the placeholder string %8s will print a right-aligned string that is eight characters wide padded with spaces, if needed. For floating point numbers, %8f will print a number that is exactly seven digits and a decimal making eight characters in total. Zeros are added after the decimal as needed. Alternatively, we may specify the number of decimals, such that \%8.1f will print a floating point number, aligned to the right with one digit after the decimal padded with spaces where needed. Default is for the value to be right justified in the field, but left justification can be specified by the - character. For number types, you can specify their format by: "0" for padding the number with zeros to the left, when right justifying the number; "+" to explicitly show a plus sign for positive numbers; SP to enforce a space, where there otherwise would be a plus sign for positive numbers. Examples of some of these combinations are shown in Listing 6.36.

Specifier	Type	Description
%b	bool	Replaces with boolean value
%s	string	
%с	char	
%d, %i	basic integer	
%u	basic unsigned integers	
%x	basic integer	formatted as unsigned hexadecimal
		with lower case letters
%X	basic integer	formatted as unsigned hexadecimal
		with upper case letters
%0	basic integer	formatted as unsigned octal integer
%f, %F,	basic floats	formatted on decimal form
%e, %E,	basic floats	formatted on scientific form. Lower
		case uses "e" while upper case uses
		"E" in the formatting.
%g, %G,	basic floats	formatted on the shortest of the cor-
		responding decimal or scientific form.
%M	decimal	
%0	Objects ToString method	
%A	any built-in types	Formatted as a literal type
%a	Printf.TextWriterFormat ->'a -> ()	
%t	(Printf.TextWriterFormat -> ()	

Table 6.2: Printf placeholder string

```
Listing 6.36 printfExample.fsx:
Examples of printf and some of its formatting options.
let pi = 3.1415192
let hello = "hello"
printf "An integer: %d\n" (int pi)
printf "A float %f on decimal form and on %e scientific form\n" pi pi
printf "A char '%c' and a string \"%s\"\n" hello.[0] hello
printf "Float using width 8 and 1 number after the decimal:\n"
printf " \"%8.1f\" \"%8.1f\"\n" pi -pi
printf " \"%08.1f\" \"%08.1f\"\n" pi -pi
printf " \"% 8.1f\" \"% 8.1f\"\n" pi -pi
printf " \"%-8.1f\" \"%-8.1f\"\n" pi -pi
printf " \"%+8.1f\" \"%+8.1f\"\n" pi -pi
printf " \"%8s\"\n\"%-8s\"\n" "hello" "hello"
$ fsharpc --nologo printfExample.fsx && mono printfExample.exe
An integer: 3
A float 3.141519 on decimal form and on 3.141519e+000 scientific form
A char 'h' and a string "hello"
Float using width 8 and 1 number after the decimal:
  " 3.1" " -3.1"
  "000003.1" "-00003.1"
       3.1" " -3.1"
        " "-3.1 "
       +3.1" " -3.1"
    hello"
"hello "
```

Function	Example	Description
printf	printf "%d apples" 3	Prints to the console, i.e., stdout
printfn		as printf and adds a newline.
fprintf	fprintf stream "%d apples" 3	Prints to a stream, e.g., stderr and stdout,
		which would be the same as printf and
		eprintf.
fprintfn		as fprintf but with added newline.
eprintf	eprintf "%d apples" 3	Print to stderr
eprintfn		as eprintf but with added newline.
sprintf	printf "%d apples" 3	Return printed string
failwithf	failwithf "%d failed apples" 3	prints to a string and used for raising an ex-
		ception.

Table 6.3: The family of printf functions.

Not all combinations of flags and identifier types are supported, e.g., strings cannot have number of integers after the decimal specified. The placeholder types "%A", "%a", and "%t" are special for F#, examples of their use are shown in Listing 6.37.

```
Listing 6.37 printfExampleAdvance.fsx:

Custom format functions may be used to specialise output.

1 let noArgument writer = printf "I will not print anything"
2 let customFormatter writer arg = printf "Custom formatter got: \"%A\""
4 arg
3 printf "Print examples: %A, %A, %A\n" 3.0m 3uy "a string"
4 printf "Print function with no arguments: %t\n" noArgument
5 printf "Print function with 1 argument: %a\n" customFormatter 3.0

1 $ fsharpc --nologo printfExampleAdvance.fsx
2 $ mono printfExampleAdvance.exe

Print examples: 3.0M, 3uy, "a string"
4 Print function with no arguments: I will not print anything
5 Print function with 1 argument: Custom formatter got: "3.0"
```

The %A is special in that all built-in types including tuples, lists, and arrays to be discussed in Chapter 11 can be printed using this formatting string, but notice that the formatting performed includes the named literal string. The two formatting strings %t and %a are options for user-customizing the formatting, and will not be discussed further.

Beware, formatString is not a string but a Printf.TextWriterFormat, so to predefine a formatString as, e.g., let str = "hello %s" in printf str "world" will be a type error.

The family of printf is shown in Table 6.3. The function fprintf prints to a stream, e.g., stderr and stdout, of type System.IO.TextWriter. Streams will be discussed in further detail in Chapter 19. The function failwithf is used with exceptions, see Chapter 18 for more details. The function has a number of possible return value types, and for testing the *ignore* function ignores it all, e.g., ·ignore ignore (failwithf "%d failed apples" 3)

# 6.6 Reading from the console

The printf and printfn functions allow us to write text on the screen, i.e., stdout. A program often needs to ask a user to input data, e.g., by typing text on a keyboard. Text typed on the keyboard is accessible through the stdin stream, and F# provides several library functions for capturing text typed on the keyboard. In the following, we will briefly discuss the System.Console.ReadLine function. For more details and other methods of input see Chapters 19 and 23.

The function System.Console.ReadLine takes a unit value as argument and returns the string the user typed. The program will not advance until the user presses newline. An example of a program that multiplies two floating point numbers supplied by a user is given in Listing 6.38,

```
Listing 6.38 userDialoguePrintf.fsx:
Interacting with a user with ReadLine.

1 printfn "To perform the multiplication of a and b"
2 printf "Enter a: "
3 let a = float (System.Console.ReadLine ())
4 printf "Enter b: "
5 let b = float (System.Console.ReadLine ())
6 printfn "a * b = %A" (a * b)
```

and an example dialogue is shown in Listing 6.39.

```
Listing 6.39: An example dialogue of running Listing 6.38. What the user typed has been framed in red boxes.

$ fsharpc --nologo userDialoguePrintf.fsx && mono userDialoguePrintf.exe
To perform the multiplication of a and b
Enter a: 3.5
Enter b: 7.4
a * b = 25.9
```

Note that the string is immediately casted to floats, such that we can multiply the input using the float multiplication operator. This also implies, that if the user inputs anything but floating point value, then mono will halt with an error message.

# 6.7 Variables

The mutable in let bindings means that the identifier may be rebound to a new value using the "<-" ·mutable lexeme with the following syntax, 4

```
Listing 6.40 Syntax for defining variables and their initial value.

1 let mutable <ident> = <expr> [in <expr>]
```

and values are changed using the assignment operator,

⁴Jon: Discussion on heap and stack should be added here.

# Listing 6.41 Value reassignment for mutable variables. | (ident) <- (ident)

Mutable data is synonymous with the term variable. A variable is an area in the computers working  $\cdot$  mutable data memory associated with an identifier and a type, and this area may be read from and written to during  $\cdot$  variable program execution, see Listing 6.42 for an example.

```
Listing 6.42 mutableAssignReassingShort.fsx:

A variable is defined and later reassigned a new value.

let mutable x = 5
printfn "%d" x
x <- -3
printfn "%d" x

$ fsharpc --nologo mutableAssignReassingShort.fsx
$ mono mutableAssignReassingShort.exe
5
-3
```

Here, an area in memory was denoted x, initially assigned the integer value 5, hence the type was inferred to be int. Later, this value of x was replaced with another integer using the "<-" lexeme. The "<-" lexeme is used to distinguish the assignment from the comparison operator, i.e., if we by mistake had written as shown in Listing 6.43, then we instead would have obtained the default assignment of the result of the comparison of the content of a with the integer 3, which is false.

```
Listing 6.43: It is a common error to mistake "=" and "<-" lexemes for mutable variables.

> let mutable a = 0
- a = 3;;
val mutable a : int = 0
val it : bool = false
```

However, it is important to note, that when the variable is initially defined, then the "=" operator must be used, while later reassignments must use the "<-" expression.

Assignment type mismatches will result in an error as demonstrated in Listing 6.44.

was expected to have type

\$ mono mutableAssignReassingTypeError.exe

'int'
but here has type
'float'

or directory.

# Listing 6.44 mutableAssignReassingTypeError.fsx: Assignment type mismatching causes a compile time error. let mutable x = 5 printfn "%d" x x <- -3.0 printfn "%d" x \$ fsharpc --nologo mutableAssignReassingTypeError.fsx

mutableAssignReassingTypeError.fsx(3,6): error FS0001: This expression

I.e., once the type of an identifier has been declared or inferred, then it cannot be changed.

A typical variable is a counter of type integer, and a typical use of counters is to increment them, see Listing 6.45 for an example.

Cannot open assembly 'mutableAssignReassingTypeError.exe': No such file

```
Listing 6.45 mutableAssignIncrement.fsx:

Variable increment is a common use of variables.

1 let mutable x = 5 // Declare a variable x and assign the value 5 to it printfn "%d" x

3 x <- x + 1 // Assign a new value -3 to x
4 printfn "%d" x

1 $ fsharpc --nologo mutableAssignIncrement.fsx
2 $ mono mutableAssignIncrement.exe
5 5
4 6
```

Using variables in expressions as opposed to the left-hand-side of an assignment operation, reads the value of the variable. Thus, when using a variable as the return value of a function, then the value is copied from the local scope of the function to the scope from which it is called. This is demonstrated in Listing 6.46.

```
Listing 6.46: Returning a mutable variable returns its value.

1 > let g () =
2 - let mutable y = 0
3 - y
4 - printfn "%d" (g ());;
5 0
6 val g : unit -> int
7 val it : unit = ()
```

In the example, we see that the type is a value, and not mutable.

Variables implement dynamic scope, e.g., in comparison with the lexical scope, where the value of an identifier depends on *where* it is defined, dynamic scope depends on, *when* it is used. E.g., the script in Listing 6.24 defines a function using lexical scope and returns the number 6.0, however, if a is made mutable, then the behavior is different as shown in Listing 6.47.

```
Listing 6.47 dynamicScopeNFunction.fsx:

Mutual variables implement dynamics scope rules. Compare with Listing 6.24.

1 let testScope x =
2 let mutable a = 3.0
3 let f z = a * z
4 a <- 4.0
5 f x
6 printfn "%A" (testScope 2.0)

1 $ fsharpc --nologo dynamicScopeNFunction.fsx
2 $ mono dynamicScopeNFunction.exe
3 8.0
```

Here, the respons is 8.0, since the value of a changed befor the function f was called.

# 6.8 Reference cells

F# has a variation of mutable variables called *reference cells*. Reference cells have built-in function · reference cells *ref* and operators "!" and ":=", where ref creates a reference variable, and the "!" and the ":=" · ref operators reads and writes its value. An example of using reference cells is given in Listing 6.48. · :=

```
Listing 6.48 refCell.fsx:
Reference cells are variants of mutable variables.

1 let x = ref 0
2 printfn "%d" !x
3 x := !x + 1
4 printfn "%d" !x

1 $ fsharpc --nologo refCell.fsx && mono refCell.exe
2 0
3 1
```

Reference cells are different from mutable variables, since their content is allocated on *The Heap*. The Heap is a global data storage that is not destroyed, when a function returns, which is in contrast to the *call stack* also known as *The Stack*. The Stack maintains all the local data for a specific instance of a function call, see Section 13.2 for more detail on the call stack. As a consequence, when a reference cell is returned from a function, then it is the reference to the location on The Heap, which is returned as a value. Since this points outside the local data area of the function, then this location is still valid after the function returns, and the variable stored there is accessible to the caller. This is illustrated in Figure 6.1

The Heap

call stack

· The Stack

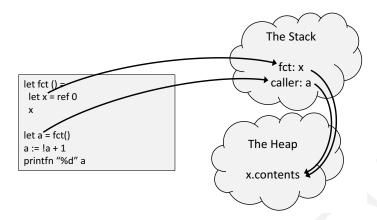


Figure 6.1: A reference cell is a pointer to The Heap and the content is not destroyed when its reference falls out of scope.

Reference cells may cause *side-effects*, where variable changes are performed across independent scopes. · side-effects Some side-effects are useful, e.g., the printf family changes the content of the screen, and the screen is outside the scope of the caller. Another example of a useful side-effect is a counter shown in Listing 6.49.

```
Listing 6.49 refEncapsulation.fsx:
An increment function with a local state using a reference cell.
let incr =
  let counter = ref 0
   fun () ->
     counter := !counter + 1
     !counter
printfn "%d" (incr ())
printfn "%d" (incr ())
printfn "%d" (incr ())
$ fsharpc --nologo refEncapsulation.fsx && mono refEncapsulation.exe
1
2
3
```

Here incr is an anonymous function with an internal state counter. At first glance, it may be surprising, that incr () does not return the value 1 at every call. The reason is that the value of the incr is the closure of the anonymous function fun () -> counter := ..., which is

```
\mathtt{incr}: (\mathtt{args}, \mathtt{exp}, \mathtt{env}) = \big((), \big( \begin{smallmatrix} \mathtt{counter} \\ ! \mathtt{counter} \end{smallmatrix} := \begin{smallmatrix} ! \mathtt{counter} \\ + \end{smallmatrix} 1 \big), \big( \mathtt{counter} \to \mathtt{ref} \end{smallmatrix} 0 \big) \big).
                                                                                                                                                                                                                                                                                                                  (6.5)
```

Thus, counter is only initiated once at the initial binding, while every call of incr () updates its value on The Heap. Such a programming structure is called encapsulation, since the counter state has been encapsulated in the anonymous function, and the only way to access it is by calling the same anonymous function. Encapsulation is good programming practice, but side-effects should Advice be avoided wherever possible.

· encapsulation

The incr example in Listing 6.49 is an example of a useful side-effect. An example to be avoided is shown in Listing 6.50.

# Listing 6.50 refSideEffect.fsx: Intertwining independent scopes is typically a bad idea. let updateFactor factor = factor := 2 let multiplyWithFactor x = let a = ref 1 updateFactor a !a * x printfn "%d" (multiplyWithFactor 3) fsharpc --nologo refSideEffect.fsx && mono refSideEffect.exe fsharpc --nologo refSideEffect.fsx && mono refSideEffect.exe

In the example, the function updateFactor changes a variable in the scope of multiplyWithFactor, which is prone to errors, since the computations are not local at the place of writing, i.e., in multiplyWithFactor, and if updateFactor were defined in a library, then the source code may not be available. Better style of programming is shown in Listing 6.51.

```
Listing 6.51 refWithoutSideEffect.fsx:
A solution of Listing 6.50 avoiding side-effects.

1 let updateFactor () =
2 2
3 let multiplyWithFactor x =
1 let a = ref 1
2 a := updateFactor ()
2 !a * x
4 printfn "%d" (multiplyWithFactor 3)

1 $ fsharpc --nologo refWithoutSideEffect.fsx
2 $ mono refWithoutSideEffect.exe
3 6
```

Here, there can be no doubt in multiplyWithFactor that the value of a is changing. Side-effects do have their use, but should in general be avoided at almost all costs, and in general it is advised to minimize the use of side effects.

Advice

Reference cells gives rise to an effect called *aliasing*, where two or more identifiers refer to the same  $\cdot$  aliasing data as illustrated in Listing 6.52.

# Listing 6.52 refCellAliasing.fsx: Aliasing can cause surprising results and should be avoided. 1 let a = ref 1 2 let b = a 3 printfn "%d, %d" !a !b 4 b := 2 5 printfn "%d, %d" !a !b 1 \$ fsharpc --nologo refCellAliasing.fsx && mono refCellAliasing.exe 2 1, 1 3 2, 2

Here, a is defined as a reference cell, and by defining b to be equal to a, we have created an alias. This can be very confusing, since as the example shows, changing the value of b causes a to change as well. Aliasing is a variant of side-effects, and aliasing should be avoided at all costs.

Advice

Since F# version 4.0, the compiler has automatically converted mutable variables to reference cells, when needed. E.g., Listing 6.49 can be rewritten using a mutable variable as shown in Listing 6.53.

```
Listing 6.53 mutableEncapsulation.fsx:
Local mutable content can be indirectly accessed outside its scope.

let incr =
let mutable counter = 0
fun () ->
counter <- counter + 1
counter
printfn "%d" (incr ())
printfn "%d" (incr ())
printfn "%d" (incr ())
fsharpc --nologo mutableEncapsulation.fsx
mono mutableEncapsulation.exe

fsharpc --nologo mutableEncapsulation.exe

none mutableEncapsulation.exe
```

Reference cells is preferred over mutable variables for encapsulation to avoid confusion.

# 6.9 Tuples

Tuples are a direct extension of constants. They are immutable and do not have concatenations nor  $\cdot$  tuple indexing operations. Tuples are unions of immutable types and have the following syntax,

```
Listing 6.54

1 <expr>{, <expr>}
```

Tuples are identified by the "," lexeme and often enclosed in parentheses, but that is not required. An example is the tripel, also known as a 3-tuple, (2,true, "hello"). In interactive mode, the type of tuples are shown as demonstrated in Listing 6.55.

```
Listing 6.55: Tuple types are products of sets.
> let tp = (2, true, "hello")
- printfn "%A" tp;;
(2, true, "hello")
val tp : int * bool * string = (2, true, "hello")
val it : unit = ()
```

The values 2, true, and "hello" are members, and the number of elements of a tuple is its length. . member From the response of F#, we see that the tuple is inferred to have the type int * bool * string. The "*" denotes the cartesian product between sets. Tuples can be products of any types and have lexical scope like value and function bindings. Notice also that a tuple may be printed as a single entity by the %A placeholder. In the example, we bound tp to the tuple, the opposite is also possible, where an identifier is bound to a tuple as shown in Listing 6.56.

```
Listing 6.56: Definition of a tuple.
> let deconstructNPrint tp =
    let (a, b, c) = tp
    printfn "tp = (%A, %A, %A)" a b c
- deconstructNPrint (2, true, "hello")
- deconstructNPrint (3.14, "Pi", 'p');;
tp = (2, true, "hello")
tp = (3.14, "Pi", 'p')
val deconstructNPrint : 'a * 'b * 'c -> unit
val it : unit = ()
```

In this a function is defined that takes 1 argument, a 3-tuple. If we wanted a function of 3 arguments, then the function binding should have been let deconstructNPrint a b c = .... The value binding let (a, b, c) = tp, binds a tuple with 3 named members to a value, thus deconstructing it in terms of its members. This is called pattern matching and will be discussed in further details in Chapter 15. Since we used the \%A placeholder in the printfn function, then the function can be called with 3tuples of different types. F# informs us that the tuple type is variable by writing 'a * 'b * 'c. The "" notation means that the type can be decided at run-time, see Section 14.6 for more on variable types.

Pairs or 2-tuples are so common that F# includes two built-in functions fst and snd, to extract the .fst first and second element of a pair. This is demonstrated in Listing 6.57.  $\cdot$  snd

```
Listing 6.57 pair.fsx:
Deconstruction of pairs with the built-in functions fst and snd.
let pair = ("first", "second")
printfn "fst(pair) = %s, snd(pair) = %s" (fst pair) (snd pair)
$ fsharpc --nologo pair.fsx && mono pair.exe
fst(pair) = first, snd(pair) = second
```

Tuples comparison are defined similarly as strings. Tuples of different lengths are different. For tuples of equal length, then they are compared element by element. E.g., (1,2) = (1,3) is false, while (1,2) = (1,2) is true. The "<>" operator is the boolean negation of the "=" operator. For the "<", "<=", ">", and ">=" operators, the strings are ordered lexicographically, such that ('a', 'b', 'c') < ('a', 'b', 's') && ('a', 'b', 's') < ('c', 'o', 's') is true, that is, the "<" operator on two tuples is true, if the left operand should come before the right, when sorting alphabetically, see Listing 6.58 for an example.

```
Listing 6.58 tupleCompare.fsx:
Tuples are compared as strings are compared alphabetically.
let lessThan (a, b, c) (d, e, f) =
  if a <> d then a < d
  elif b \iff e then b \leqslant d
  elif c <> f then c < f
  else false
let printTest x y =
  printfn "%A < %A is %b" x y (lessThan x y)</pre>
let a = ('a', 'b', 'c');
let b = ('d', 'e', 'f');
let c = ('a', 'b', 'b');
let d = ('a', 'b', 'd');
printTest a b
printTest a c
printTest a d
$ fsharpc --nologo tupleCompare.fsx && mono tupleCompare.exe
('a', 'b', 'c') < ('d', 'e', 'f') is true
('a', 'b', 'c') < ('a', 'b', 'b') is false
('a', 'b', 'c') < ('a', 'b', 'd') is true
```

The algorithm for deciding the boolean value of (a1, a2) < (b1, b2) is as follows: we start by examining the first elements, and if a1 and b1 are different, in which case the result of (a1, a2) < (b1, b2) is equal to the result of a1 < b1. If la1 and b1 are equal, then we move onto the next letter and repeat the investigation. The "<=", ">", and ">=" operators are defined similarly.

Binding tuples to mutables does not make the tuple mutable. This is demonstrated in Listing 6.59.

```
Listing 6.59 tupleOfMutables.fsx:

A mutable change value, but the tuple defined by it does not refer to the new value.

let mutable a = 1
let mutable b = 2
let c = (a, b)
printfn "%A, %A, %A" a b c
a <- 3
printfn "%A, %A, %A" a b c

$ fsharpc --nologo tupleOfMutables.fsx && mono tupleOfMutables.exe
1, 2, (1, 2)
3, 2, (1, 2)
```

However, it is possible to define a mutable variable of type tuple such that new tuple values can be assigned to it as shown in Listing 6.60.

```
Listing 6.60 mutable Tuple.fsx:

A mutable tuple can be assigned a new value.

1 let mutable pair = 1,2
2 printfn "%A" pair
3 pair <- (3,4)
4 printfn "%A" pair

1 $ fsharpc --nologo mutable Tuple.fsx && mono mutable Tuple.exe
2 (1, 2)
3 (3, 4)
```

Mutable tuples are value types meaning that binding to new names are copies not aliases as demonstrated in Listing 6.61.

```
Listing 6.61 mutable TupleValue.fsx:

A mutable tuple is a value type.

let mutable pair = 1,2
let mutable aCopy = pair
pair <- (3,4)
printfn "%A %A" pair aCopy

fsharpc --nologo mutableTupleValue.fsx && mono mutableTupleValue.exe
(3, 4) (1, 2)
```

The use of tuples shortens code and highlights semantic content at a higher level, e.g., instead of focusing on the elements, tuples focus on their union. While this may look elegant and short there is the risk of *obfuscation*, i.e., writing compact code that is difficult to read, where an unprepared reader of the code may not easily understand the computation nor appreciate its elegance without an accompanying explanation. Hence, always keep an eye out for compact and concise ways to write code, but never at the expense of readability.

· obfuscation

Advice

# 7 In-code documentation

Documentation is a very important part of writing programs, since it is most unlikely, that you will be writing really obvious code. Moreover, what seems obvious at the point of writing may be mystifying months later to the author and to others. Documentation serves several purposes:

- 1. Communicate what the code should be doing
- 2. Highlight big insights essential for the code
- 3. Highlight possible conflicts and/or areas, where the code could be changed later

The essential point is that coding is a journey in problem solving, and proper documentation is an aid in understanding the solution and the journey that lead to it. Documentation is most often a mixture between in-code documentation and accompanying documents. Here, we will focus on in-code documentation, which arguably causes problems in multi-language environments and run the risk of bloating code.

F# has two different syntaxes for comments. Comments are either block comments,

```
Listing 7.1 Block comments.

(*<any text>*)
```

The comment text (*<any text>*) can be any text and it is stilled parsed by F# as keywords and basic types implying that (* a comment (* in a comment *) *) and (* "*)" *) are valid comments, while (* " *) is invalid.

Alternatively, comments may be given as line comments,

```
Listing 7.2 Line comments.

1 //<any text>newline
```

where the comment text ends after the first newline.

The F# compiler has an option for generating  $Extensible\ Markup\ Language\ (XML)$  files from scripts using the C# documentation comments tags¹. The XML documentation starts with a triple-slash ///, i.e., a lineComment and a slash, which serves as comments for the code construct, that follows immediately after. XML consists of tags which always appears in pairs, e.g., the tag "tag" would look

[·] Extensible Markup Language

 $[\]cdot XML$ 

¹For specification of C# documentations comments see ECMA-334 3rd Edition, Annex E, Section 2: http://www.ecma-international.org/publications/files/ECMA-ST/Ecma-334.pdf

Tag	Description
<c></c>	Set text in a code-font.
<code></code>	Set one or more lines in code-font.
<example></example>	Set as an example.
<exception></exception>	Describe the exceptions a function can throw.
<li>t&gt;</li>	Create a list or table.
<para></para>	Set text as a paragraph.
<pre><param/></pre>	Describe a parameter for a function or constructor.
<pre><paramref></paramref></pre>	Identify that a word is a parameter name.
<pre><permission></permission></pre>	Document the accessibility of a member.
<remarks></remarks>	Further describe a function.
<returns></returns>	Describe the return value of a function.
<see></see>	Set as link to other functions.
<seealso></seealso>	Generate a See Also entry.
<summary></summary>	Main description of a function or value.
<typeparam></typeparam>	Describe a type parameter for a generic type or method.
<typeparamref></typeparamref>	Identify that a word is a type parameter name.
<value></value>	Describe a value.

Table 7.1: Recommended XML tags for documentation comments, from ECMA-334 3rd Edition, Annex E, Section 2.

like <tag> . . . </tag>. The F# accept any tags, but recommends those listed in Table 7.1. If no tags are used, then it is automatically assumed to be a <summary>. An example of a documented script is,

# Listing 7.3 commentExample.fsx: Code with XML comments. /// The discriminant of a quadratic equation with parameters a, b, and c let discriminant a b c = b ** 2.0 - 4.0 * a * c /// <summary>Find x when 0 = ax^2+bx+c.</summary> /// <remarks > Negative discriminant are not checked. </remarks > /// <example> The following code: /// /// <code> 111 let a = 1.0/// let b = 0.0/// let c = -1.0let xp = (solution a b c +1.0)/// printfn "0 = %.1fx^2 + %.1fx + %.1f => x_+ = %.1f" a b c xp 111 111 </code> /// prints $< c > 0 = 1.0x^2 + 0.0x + -1.0 => x_+ = 0.7 </ c > to the console.$ /// </example> /// <param name="a">Quadratic coefficient.</param> /// <param name="b">Linear coefficient.</param> /// <param name="c">Constant coefficient.</param> /// <param name="sgn">+1 or -1 determines the solution.</param> /// <returns>The solution to x.</returns> let solution a b c sgn = let d = discriminant a b c (-b + sgn * sqrt d) / (2.0 * a)let a = 1.0let b = 0.0let c = -1.0let xp = (solution a b c +1.0)printfn "0 = %.1fx^2 + %.1fx + %.1f => x_+ = %.1f" a b c xp \$ fsharpc --nologo commentExample.fsx && mono commentExample.exe $0 = 1.0x^2 + 0.0x + -1.0 \Rightarrow x_+ = 1.0$

Mono's fsharpc command may be used to extract the comments into an XML file as demonstrated in Listing 7.4.

```
Listing 7.4, Converting in-code comments to XML.

1  $ fsharpc --doc:commentExample.xml commentExample.fsx
2  F# Compiler for F# 4.0 (Open Source Edition)
3  Freely distributed under the Apache 2.0 Open Source License
```

This results in an XML file with the following content as shown in Listing 7.5.

Listing 7.5, An XML file generated by fsharpc. <?xml version="1.0" encoding="utf-8"?> <assembly><name>commentExample</name></assembly> <members> <member name="M:CommentExample.solution(System.Double,System.Double,</pre> System.Double,System.Double)"> <summary>Find x when 0 = ax^2+bx+c.</summary> <remarks>Negative discriminant are not checked.</remarks> <example> The following code: <code> let a = 1.0let b = 0.0let c = -1.0let xp = (solution a b c +1.0)printfn "0 =  $%.1fx^2 + %.1fx + %.1f => x_+ = %.1f$ " a b c xp </code> prints <c>0 = 1.0x^2 + 0.0x + -1.0 => x_+ = 0.7</c> to the console. </example> <param name="a">Quadratic coefficient.</param> <param name="b">Linear coefficient.</param> <param name="c">Constant coefficient.</param> <param name="sgn">+1 or -1 determines the solution.</param> <returns>The solution to x.</returns> </member> <member name="M:CommentExample.discriminant(System.Double,System.Double,</pre> System.Double)"> <summary> The discriminant of a quadratic equation with parameters a, b, and c </summary> </member> </members> </doc>

The extracted XML is written in C# type by convention, since F# is part of the Mono and .Net framework that may be used by any of the languages using Assemblies. Besides the XML inserted in the script, the XML has added <?xml ...> header, <doc>, <assembly>, <members>, and <member> tags. The header and the <doc> tag are standards for XML. The extracted XML is geared towards documenting big libraries of codes and thus highlights the structured programming organisation, see Chapters 9 and 20, and <assembly>, <members>, and <member> are indications for where the functions belong in the hierarchy. As an example, the prefix M:CommentExample. means that it is a method in the namespace commentExample, which in this case is the name of the file. Further, the function type val solution: a:float -> b:float -> c:float -> sgn:float -> float is in the XML documentation M:CommentExample.solution(System.Double,System.Double,System.Double,System.Double), which is the C# equivalent.

An accompanying program in the Mono suite is mdoc, whose primary use is to perform a syntax analysis of an assembly and generate a scaffold XML structure for an accompanying document. With the -i flag, it is further possible to include the in-code comments as initial descriptions in the XML. The XML may be updated gracefully by mdoc as the code develops, without destroying manually entered documentation in the accompanying documentation. Finally, the XML may be exported to HTML.

The primary use of the mdoc command is to analyse compiled code and generate an empty XML structure with placeholders to describe functions, values, and variables. This structure can then be updated and edited as the program develops. The edited XML files can then be exported to *Hyper* 

Text Markup Language (HTML) files, which can be viewed in any browser. Using the console, all of · Hyper Text Markup this is accomplished by the procedure shown in Listing 7.6, and the result is shown in Figure 7.1.

Language  $\cdot$  HTML

```
Listing 7.6, Converting an XML file to HTML.
$ mdoc update -o commentExample -i commentExample.xml commentExample.exe
New Type: CommentExample
Member Added: public static double determinant (double a, double b,
   double c);
Member Added: public static double solution (double a, double b, double
   c, double sgn);
Member Added: public static double a { get; }
Member Added: public static double b { get; }
Member Added: public static double c { get; }
Member Added: public static double xp { get; }
Namespace Directory Created:
New Namespace File:
Members Added: 6, Members Deleted: 0
$ mdoc export-html -out commentExampleHTML commentExample
 .CommentExample
```

A full description of how to use mdoc is found here².

 $^{^2}$ http://www.mono-project.com/docs/tools+libraries/tools/monodoc/generating-documentation/

# solution Method

Find x when  $0 = ax^2+bx+c$ .

# **Syntax**

```
[Microsoft.FSharp.Core.CompilationArgumentCounts(Mono.Cecil.CustomAttributeArgument[])] public static double solution (double a, double b, double c, double sgn)
```

# **Parameters**

```
a Quadratic coefficient.
b Linear coefficient.
c Constant coefficient.
sgn +1 or -1 determines the solution.
```

# Returns

The solution to x.

# Remarks

Negative discriminant are not checked.

# **Example**

```
The following code:
```

```
Example

let a = 1.0
let b = 0.0
let c = -1.0
let xp = (solution a b c +1.0)
printfn "0 = %.1fx^2 + %.1fx + %.1f => x_+ = %.1f" a b c xp

prints 0 = 1.0x^2 + 0.0x + -1.0 => x_+ = 0.7 to the console.
```

# Requirements

```
Namespace:
Assembly: commentExample (in commentExample.dll)
Assembly Versions: 0.0.0.0
```

Figure 7.1: Part of the HTML documentation as produce by mdoc and viewed in a browser.

# 8 | Controlling program flow

Non-recursive functions encapsulate code and allow for control of execution flow. That is, if a piece of code needs to be executed many times, then we can encapsulate it in the body of a function, and call the function several times. In this chapter, we will look at more general control of flow via loops and conditional execution. Recursion is another mechanism for controlling flow, but this is deferred to Chapter 13.

# 8.1 While and for loops

Many programming constructs need to be repeated, and F# contains many structures for repetition. A while-loop has the syntax,

·while

```
Listing 8.1 While loop.

while <condition> do <expr> [done]
```

The condition <condition> is an expression that evaluates to true or false. A while-loop repeats the <expr> expression as long as the condition is true. Using lightweight syntax the block following the do keyword up to and including the done keyword may be replaced by a newline and indentation. As an example, the program in Listing 8.5 counts from 1 to 10.

· condition

· do · done

```
Listing 8.2 countWhile.fsx:
Count to 10 with a counter variable.

let mutable i = 1 in while i <= 10 do printf "%d " i; i <- i + 1 done;
printf "\n"

fsharpc --nologo countWhile.fsx && mono countWhile.exe
1 2 3 4 5 6 7 8 9 10
```

We will call i for the counter variable. The counting is done by performing the following computation: In line 1, the counter variable is first given an initial value 1. Then execution enters the while-loop and examines the condition. Since  $1 \le 10$  then the condition is true, and execution enters the body of the loop. The body prints the value of the counter to screen and increases counter by 1. Then execution returns to the top of the while-loop. Now the condition is  $2 \le 10$  which is also true, and so execution enters the body and so on until the counter has reach value 11, in which case the condition  $11 \le 10$  is false, and execution continues in line 2.

In lightweight syntax this would be as shown in Listing 8.3.

```
Listing 8.3 countWhileLightweight.fsx:
Count to 10 with a counter variable using lightweight syntax, see Listing 8.2.

1 let mutable i = 1
2 while i <= 10 do
3 printf "%d " i
4 i <- i + 1
5 printf "\n"

1 $ fsharpc --nologo countWhileLightweight.fsx
2 $ mono countWhileLightweight.exe
3 1 2 3 4 5 6 7 8 9 10
```

Notice that although the expression following the condition is preceded with a do keyword, and do <expr> is a do binding, the keyword do is mandatory.

Counters are so common that a special syntax has been reserved for loops using counters. These are called *for*-loops. For-loops comes in several variants, and here we will focus on the one using an ·for explicit counter. Its syntax is,

```
Listing 8.4 For loop.

1 for <ident> = <firstExpr> to <lastExpr> do <bodyExpr> [done]
```

A for-loop initially binds the counter identifier <ident> to be the value <firstExpr>. Then execution enters the body and <bodyExpr> is evaluated. Once done, then the counter is increased and execution evaluates once again <bodyExpr>. This is repeated until and including the counter has the value <lastExpr>. As for while-loops, using lightweight syntax the block following the do keyword up to do and including the done keyword may be replaced by a newline and indentation.

The counting example from Listing 8.2 using a for-loop is shown in Listing 8.5

```
Listing 8.5 count.fsx:
Counting from 1 to 10 using a -loop.

1 for i = 1 to 10 do printf "%d " i done
2 printfn ""

1 $ fsharpc --nologo count.fsx && mono count.exe
2 1 2 3 4 5 6 7 8 9 10
```

As this interactive script demonstrates, the identifier i takes all the values between 1 and 10, but in spite of its changing state, it is not mutable. Note also that the return value of the for expression is "()" like the printf functions. The lightweight equivalent is shown in Listing 8.6.

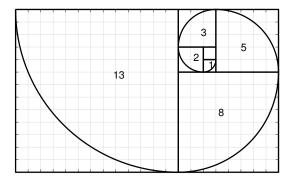


Figure 8.1: The Fibonacci spiral is an approximation of the golden spiral. Each square has side lengths of successive Fibonacci numbers, and the curve in each square is the circular arc with radius of the square it is drawn in.

```
Listing 8.6 countLightweight.fsx:

Counting from 1 to 10 using a -loop, see Listing 8.5.

for i = 1 to 10 do
   printf "%d " i
   printfn ""

$ fsharpc --nologo countLightweight.fsx && mono countLightweight.exe
2 1 2 3 4 5 6 7 8 9 10
```

To further compare for- and while-loops, consider the following problem.

## Problem 8.1

Write a program that calculates the n'th Fibonacci number.

The Fibonacci's numbers is a sequence of numbers starting with 1, 1, and where the next number is calculated as the sum of the previous two. Hence the first ten numbers are: 1, 1, 2, 3, 5, 8, 13, 21, 34, 55. Fibonacci's numbers are related to Golden spirals shown in Figure 8.1. Often the sequence is extended with a preceding number 0, to be  $0, 1, 1, 2, 3, \ldots$ , which we will do here as well.

We could solve this problem with a for-loop as follows,

## Listing 8.7 fibFor.fsx: The *n*'th Fibonacci number is the sum of the previous 2. let fib n = let mutable pair = (0, 1) for i = 2 to n do pair <- (snd pair, (fst pair) + (snd pair))</pre> snd pair printfn "fib(1) = %d" (fib 1) printfn "fib(2) = %d" (fib 2) printfn "fib(3) = %d" (fib 3) printfn "fib(10) = %d" (fib 10) \$ fsharpc --nologo fibFor.fsx && mono fibFor.exe fib(1) = 1fib(2) = 1fib(3) = 2fib(10) = 55

The basic idea of the solution is that if we are given the (n-1)'th and (n-2)'th numbers, then the n'th number is trivial to compute. And assume that fib(1) and fib(2) are given, then it is trivial to calculate the fib(3). For the fib(4) we only need fib(3) and fib(2), hence we may disregard fib(1). Thus, we realize that we can cyclicly update the previous, current, and next values by shifting values until we have reached the desired fib(n). This is implement in Listing 8.7 as function fib, which takes an integer n as argument and returns the n'th Fibonacci number. The function does this iteratively using a for-loop, where i is the counter value, pair is the pair of the i-1'th and i'th Fibonacci numbers. In the body of the loop, the i'th and i+1'th numbers are assigned to pair. The for-loop automatically updates i for next iteration. When n < 2 then the body of the for-loop is not evaluated, and 1 is returned. This is of course wrong for n < 1, but we will ignore this for now.

The same program but using a while-loop is shown in Listing 8.8.

## Listing 8.8 fibWhile.fsx: Search for the largest Fibonacci number less than a specified number. let fib (n : int) : int = let mutable pair = (0, 1) let mutable i = 1while i < n do pair <- (snd pair, fst pair + snd pair) i <- i + 1 snd pair printfn "fib(1) = %d" (fib 1) printfn "fib(2) = %d" (fib 2) printfn "fib(3) = %d" (fib 3) printfn "fib(10) = %d" (fib 10) \$ fsharpc --nologo fibWhile.fsx && mono fibWhile.exe fib(1) = 1fib(2) = 1fib(3) = 2fib(10) = 55

As can be seen, the program is almost identical. In this case, the for-loop is to be preferred, since more lines of code typically means more chances of making a mistake. However, while-loops are still simpler and possibly easier to argue correctness about. To understand what is being calculated in code such as the while-loop in Listing 8.8, we can describe the loop in terms of its loop invariant. An invariant is a statement that is always true at a particular point in a program, and a loop invariant is a statement which is true at the beginning and end of a loop. In line 4 in Listing 8.8, we may state the invariant: The variable pair is the pair of the i-1'th and i'th Fibonacci numbers. This is provable by induction:

· loop invariant · invariant

Base case: Before entering the while loop, i is 1, pair is (0, 1). Thus, the invariant is true.

**Induction step:** Assuming that pair is the i-1'th and i'th Fibonacci numbers, then the body first assigns a new value to pair as the i'th and i+1'th Fibonacci numbers, then increases i with one such that at the end of the loop the pair again contains the the i-1'th and i'th Fibonacci numbers. Thus, the invariant is true.

Thus when know that the second value in pair holds the value of the i'th Fibonacci number, and since we further may prove that when line 7 is only reached, then i = n, and thus that fib returns the n'th Fibonacci number.

While-loops also allows for other logical structures than for-loops, such as the case when the number of iteration cannot easily be decided, when entering the loop. As an example, consider slight variation of the above problem, where we wish to find the largest Fibonacci number less than some number. An solution to this problem is shown in Listing 8.9.

## Listing 8.9 fibWhileLargest.fsx: Search for the largest Fibonacci number less than a specified number. let largestFibLeq n = let mutable pair = (0, 1) while snd pair <= n do pair <- (snd pair, fst pair + snd pair) snd pair for i = 1 to 10 do printfn "largestFibLeq(%d) = %d" i (largestFibLeq i) \$ fsharpc --nologo fibWhileLargest.fsx && mono fibWhileLargest.exe largestFibLeq(1) = 2largestFibLeq(2) = 3largestFibLeq(3) = 5largestFibLeq(4) = 5largestFibLeq(5) = 8largestFibLeq(6) = 8largestFibLeq(7) = 8largestFibLeq(8) = 13largestFibLeq(9) = 13largestFibLeq(10) = 13

The strategy here is to iteratively calculate numbers in Fibonacci's sequence until we've found one larger than the argument n, and then return the previous. This could not be calculated with a forloop.

## 8.2 Conditional expressions

Programs often contains code, which only should be executed under certain conditions. This can be expressed as **if**-expressions, whos syntax is as follows.

```
Listing 8.10 Conditional expressions.

if <cond> then <expr> {elif <cond> then <expr>} [else <expr>]
```

The condition <con> is an expression resulting in a Boolean value, and there can be zero or more elif conditions as indicated by {}. Each expression <expr> is called a branch, and all branches must have identical type, such that regardless which branch is chosen, then the type of the result of the conditional expression is the same. The result of the conditional expression is the first branch, for which its condition was true and if all conditions are false then the else-branch is evaluated. If no else expression is present, then "()" will be returned. See Listing 8.11 for a simple example.

 $\cdot$  branch

·if

# Listing 8.11 condition.fsx: Conditions evaluates their branches depending on the value of the condition. if true then printfn "hi" else printfn "bye" if false then printfn "hi" else printfn "bye" fsharpc --nologo condition.fsx && mono condition.exe hi bye

Lightweight syntax allows for newlines entered everywhere, but indentation must be used to express scope.

To demonstrate conditional expressions, let us write a program, which writes the sentence, "I have n apple(s)", where the plural 's' is added appropriately for various ns. This is done in Listing 8.12 using the lightweight syntax.

```
Listing 8.12 conditionalLightweight.fsx:
Using conditional expression to generate different strings.
let applesIHave n =
  if n < -1 then
     "I owe " + (string -n) + " apples"
  elif n < 0 then
     "I owe " + (string -n) + " apple"
   elif n < 1 then
     "I have no apples"
   elif n < 2 then
     "I have 1 apple"
     "I have " + (string n) + " apples"
printfn "%A" (applesIHave -3)
printfn "%A" (applesIHave -1)
printfn "%A" (applesIHave 0)
printfn "%A" (applesIHave 1)
printfn "%A" (applesIHave 2)
printfn "%A" (applesIHave 10)
$ fsharpc --nologo conditionalLightWeight.fsx
$ mono conditionalLightWeight.exe
"I owe 3 apples"
"I owe 1 apple"
"I have no apples"
"I have 1 apple"
"I have 2 apples"
"I have 10 apples"
```

The sentence structure and its variants gives rise to a more compact solution, since the language to be returned to the user is a variant of "I have/or no/number apple(s)", i.e., under certain conditions should the sentence use "have" and "owe" etc. So, we could instead make decisions on each of these sentence parts, and then built the final sentence from its parts. This is accomplished in the following example:

## Listing 8.13 conditionalLightweightAlt.fsx: Using sentence parts to construct the final sentence. let applesIHave n = let haveOrOwe = if n < 0 then "owe" else "have"</pre> let pluralS = if $(n = 0) \mid \mid (abs n) > 1$ then "s" else "" let number = if n = 0 then "no" else (string (abs n)) "I " + haveOrOwe + " " + number + " apple" + pluralS printfn "%A" (applesIHave -3) printfn "%A" (applesIHave -1) printfn "%A" (applesIHave 0) printfn "%A" (applesIHave 1) printfn "%A" (applesIHave 2) printfn "%A" (applesIHave 10) \$ fsharpc --nologo conditionalLightWeightAlt.fsx \$ mono conditionalLightWeightAlt.exe "I owe 3 apples" "I owe 1 apple" "I have no apples" "I have 1 apple" "I have 2 apples" "I have 10 apples"

While arguably shorter, this solution is also denser, and for a small problem like this, it is most likely more difficult to debug and maintain.

Note that both elif and else branches are optional, which may cause problems. For example, both let a = if true then 3 and let a = if true then 3 elif false then 4 will be invalid, since F# is not smart enough to realize that the type of the expression is uniquely determined. Instead F# looks for the else to ensure all cases have been covered, and that a always will be given a unique value of the same type regardless of the branch taken in the conditional statement, hence, let a = if true then 3 else 4 is the only valid expression of the 3. In practice, F# assumes that the omitted branch returns "()", and thus it is fine to say let a = if true then () and if true then printfn "hej". Nevertheless, it is good practice in F# always to include an else branch.

## 8.3 Programming intermezzo: Automatic conversion of decimal to binary numbers

Using loops and conditional expressions, we are now able to solve the following problem:

## Problem 8.2

Given an integer on decimal form, write its equivalent value on binary form.

To solve this problem, consider odd numbers: They all have the property, that the least significant bit is 1, e.g.,  $1_2 = 1,101_2 = 5$  in contrast to even numbers such as  $110_2 = 6$ . Division by 2 is equal to right-shifting by 1, e.g.,  $1_2/2 = 0.1_2 = 0.5,101_2/2 = 10.1_2 = 2.5,110_2/2 = 11_2 = 3$ . Thus, by integer division by 2 and checking the remainder, we may sequentially read off the least significant bit. This

leads to the algorithm shown in Listing 8.14.

Listing 8.14 dec2bin.fsx: Using integer division and remainder to write any positive integer on binary form. let dec2bin n = if n < 0 then "Illegal value" elif n = 0 then"0ъ0" else let mutable v = nlet mutable str = "" while v > 0 do str <- (string (v % 2)) + str v <- v / 2 "0b" + str printfn " 4 d ->  8 s" -1 (dec2bin -1) printfn " 4d  ->  8s " 0 (dec2bin 0) for i = 0 to 3 do printfn "%4d -> %s" (pown 10 i) (dec2bin (pown 10 i)) \$ fsharpc --nologo dec2bin.fsx && mono dec2bin.exe -1 -> Illegal value 0 -> 0b0 1 -> 0b1 10 -> 0b1010 100 -> 0b1100100 1000 -> 0b1111101000

In the code, the states v and str are iteratively updated until str finally contains the desired solution.

To prove that Listing 8.14 calculates the correct sequence we use induction. First we realize, that for v < 1 then the while loop is skipped, and the result is trivially true. We will concentrate on line 9 in Listing 8.14, and we will prove the following loop invariant: The string str contains all the bits of n to the right of the bit pattern remaining in variable v.

Base case n = 000...000x: If n only uses the lowest bit then n = 0 or n = 1. If n = 0 then it is trivially correct. Considering the case n = 1: Before entering into the loop, v is 1, str is the empty string, so the invariant is true. The condition of the while-loop is 1 > 0 so execution enters the loop. Since integer division of 1 by 2 gives 0 with remainder 1, then str is set to "1" and v to 0. Now we reexamine the while-loop's condition, 0 > 0, which is false, so we exit the loop. At this point, v is 0 and str is "1", so all bits have been shifted from v to str and none are left in v. Thus the invariant is true. Finally, the program returns "0b1".

Induction step: Consider the case of n > 1, and assume that the invariant is true when entering the loop, i.e., that m bits already have been shifted to  $\mathtt{str}$  and that  $n > 2^m$ . In this case  $\mathtt{v}$  contains the remaining bits of  $\mathtt{n}$ , which is the integer division  $\mathtt{v} = \mathtt{n} / 2 **\mathtt{m}$ . Since  $n > 2^m$  then  $\mathtt{v}$  is non-zero and the loop conditions is true, so we enter the loop body. In the loop body we concatenate the rightmost bit of  $\mathtt{v}$  to the left of  $\mathtt{str}$  using  $\mathtt{v}$  % 2, and right-shift  $\mathtt{v}$  one bit to the right with  $\mathtt{v} <- \mathtt{v} / 2$ . Thus, when returning to the condition, the invariant is true, since the right-most bit in  $\mathtt{v}$  has been shifted to  $\mathtt{str}$ . This continues until all bits have been shifted to  $\mathtt{str}$  and  $\mathtt{v} = \mathtt{0}$ , in which case the loop terminates, and "0b"+str is returned.

Thus we have proven, that  $\mathtt{dec2bin}$  correctly converts integers to strings representing binary numbers.

## 9 Organising code in libraries and application programs

In this chapter, we will focus on a number of ways to make code available as *library* functions in F#. · library By library we mean a collection of types, values and functions that an application program can use. A library does not perform calculations on its own.

F# includes several programming structures to organize code in libraries: Modules, namespaces and classes. In this chapter, we will describe modules and namespaces. Classes will be described in detail in Chapter 20.

## 9.1 Modules

An F# module, not to be confused with a Common Language Infrastructure module (see Appendix D), · module is a programming structure used to organise type declarations, values, functions, etc.

Every implementation and script file in F# implicitly defines a module, and the module name is given by the filename. Thus, creating a script file Meta.fsx as shown in Listing 9.1.¹

```
Listing 9.1 Meta.fsx:
A script file defining the apply function.

type floatFunction = float -> float -> float
let apply (f : floatFunction) (x : float) (y : float) : float = f x y
```

we've implicitly defined a module of name Meta. Another script file may now use this function, which is accessed using the "." notation, i.e., Meta.apply will refer to this function in other programs. An application program could be as shown in Listing 9.3.

```
Listing 9.2 MetaApp.fsx:
Defining a script calling the module.

1 let add: Meta.floatFunction = fun x y -> x + y
2 let result = Meta.apply add 3.0 4.0
3 printfn "3.0 + 4.0 = %A" result
```

In the above, we have explicitly used the module's type definition for illustration purposes. A shorter

¹Jon: Type definitions have not been introduced at this point!

and possibly simpler program would have been to define add as let add x y = x + y, since F#'s typesystem will infer the implied type. However, explicit definitions of types is recommended for Advice readability. Hence, an alternative to the above's use of lambda functions is, let add (x: float) (y: float): float = x + y. To compile the module and the application program, we write as demonstrated in Listing 9.3.

```
Listing 9.3: Compiling both the module and the application code. Note that fileorder
matters, when compiling several files.
```

```
$ fsharpc --nologo Meta.fsx MetaApp.fsx && mono MetaApp.exe
3.0 + 4.0 = 7.0
```

Notice, since the F# compiler reads through the files once, the order of the filenames in the compile command is very important. Hence, the script containing the module and function definitions must be to the left of the script containing their use. Notice also that if not otherwise specified, then the F# compiler produces an .exe file derived from the last filename in the list of filenames.

We may also explicitly define the module name using the module using the syntax,

·module

```
Listing 9.4 Outer module.
module <ident>
<script>
```

Here, the identifier <ident> is a name not necessarily related to the filename, and the script <script> is expression. An example is given in Listing 9.20.

```
Listing 9.5 MetaExplicit.fsx:
Explicit definition of the outermost module.
module Meta
type floatFunction = float -> float -> float
let apply (f : floatFunction) (x : float) (y : float) : float = f x y
```

Since we have created a new file, where the module Meta is explicitly defined, we can use the same application program. This is demonstrated in Listing 9.6.

```
Listing 9.6: Changing the module definition to explicit naming has no effect on the
application nor the compile command.
```

```
$ fsharpc --nologo MetaExplicit.fsx MetaApp.fsx && mono MetaApp.exe
3.0 + 4.0 = 7.0
```

Notice that, since MetaExplicit.fsx explicitly defines the module name, apply is not available to an application program as MetaExplicit.apply. It is recommended that module names are Advice defined explicitly, since filenames may change due to external conditions. I.e., filenames are typically set from the perspective of the filesystem. The user may choose to change names to suit a filesystem structure, or different platforms may impose different file naming convention. Thus, direct linking of filenames with the internal workings of a program is a needless complication of structure.

The definitions inside a module may be accessed directly from an application program, omitting the

"."-notation, by use of the open keyword,

```
·open
```

```
Listing 9.7 Open module.

open <ident>
```

I.e., we can modify MetaApp.fsx as shown in Listing 9.9.

```
Listing 9.8 MetaAppWOpen.fsx:
Avoiding the "."-notation by the keyword.

1 open Meta
2 let add: floatFunction = fun x y -> x + y
3 let result = apply add 3.0 4.0
4 printfn "3.0 + 4.0 = %A" result
```

In this case, the namespace of our previously defined module is included into the scope of the application functions, and its types, values, functions, etc. can be used directly, as shown in Listing 9.9.

```
Listing 9.9: How the application program opens the module has no effect on the module code nor compile command.

1  $ fsharpc --nologo MetaExplicit.fsx MetaAppWOpen.fsx && mono MetaAppWOpen.exe
2  3.0 + 4.0 = 7.0
```

The open-keyword should be used sparingly, since including a library's definitions into the application scope can cause surprising naming conflicts, since the user of a library typically has no knowledge of the inner workings of the library. E.g., the user may accidentally use code defined in the library, but with different type and functionality than intended, which the type system will use to deduce types in the application program, and therefore will either give syntax or runtime errors that are difficult to understand. This problem is known as namespace pollution, and for clarity it is recommended to use the open-keyword sparingly. Notice that for historical reasons, the work namespace pollution is used to cover both pollution due to modules and namespaces.

· namespace pollution Advice

Modules may also be nested, in which case the nested definitions must use the "="-sign and must be appropriately indented.

```
Listing 9.10 Nested modules.

1 module <ident> = <script>
```

In lightweight syntax, a newline may be entered before the script <script>, and the script must be indented. An example is shown in Listing 9.11.

## Listing 9.11 nestedModules.fsx: Modules may be nested. module Utilities let PI = 3.1415module Meta = type floatFunction = float -> float -> float let apply (f : floatFunction) (x : float) (y : float) : float = f x y module MathFcts = let add : Meta.floatFunction = fun x y -> x + y

In this case, Meta and MathFcts are defined at the same level and said to be siblings, while Utilities is defined at a higher level. In this relation, the former two are said to be the children of the latter. Note that the nesting respects the lexical scope rules, such that the constant PI is directly accessible in both modules Meta and MathFcts, as is the module Meta in MathFcts but not MathFcts in Meta. The "."-notation is reused to index deeper into the module hierarchy as the example in Listing 9.12 shows.

```
Listing 9.12 nestedModulesApp.fsx:
Applications using nested modules require additional usage of the "." notation to
navigate the nesting tree.
let add : Utilities.Meta.floatFunction = fun x y -> x + y
let result = Utilities.Meta.apply Utilities.MathFcts.add 3.0 Utilities.PI
printfn "3.0 + 4.0 = %A" result
```

Modules can be recursive using the rec-keyword, meaning that in our example we can make the outer rec module recursive as demonstrated in Listing 9.13.²

```
Listing 9.13 nestedRecModules.fsx:
Mutual dependence on nested modules requires the keyword in the module def-
inition.
module rec Utilities
  module Meta =
    type floatFunction = float -> float -> float
    let apply (f : floatFunction) (x : float) (y : float) : float = f x y
  module MathFcts =
    let add : Meta.floatFunction = fun x y -> x + y
```

The consequence is that the modules Meta and MathFcts are accessible in both modules, but compilation will now give a warning, since soundness of the code will first be checked at runtime. In general it is advised to avoid programming constructions, whose validity cannot be checked Advice at compile-time.

### 9.2 Namespaces

An alternative to structure code in modules is use a namespace, which only can hold modules and type · namespace

²Jon: Dependence on version 4.1 and higher.

declarations and only works in compiled mode. Namespaces are defined as explicitly defined outer modules using the namespace keyword,

·namespace

```
Listing 9.14 Namespace.

namespace <ident>

cscript>
```

An example is given in Listing 9.15.

```
Listing 9.15 namespace.fsx:
Defining a namespace is similar to explicitly named modules.

1 namespace Utilities
2 type floatFunction = float -> float -> float
3 module Meta =
4 let apply (f : floatFunction) (x : float) (y : float) : float = f x y
```

Notice that when organising code in a namespace, the first line of the file, other than comments and compiler directives, must be the one starting with namespace.

As for modules, the content of a namespace is accessed using the "." notation, as demonstrated in Listing 9.17.

```
Listing 9.16 namespaceApp.fsx:

The "."-notation lets the application program accessing functions and types in a namespace.

1 let add: Utilities.floatFunction = fun x y -> x + y
2 let result = Utilities.Meta.apply add 3.0 4.0
3 printfn "3.0 + 4.0 = %A" result
```

Likewise, compilation is performed identically, see Listing 9.17.

```
Listing 9.17: Compilation of files including namespace definitions uses the same procedure as modules.

1  $ fsharpc --nologo namespace.fsx namespaceApp.fsx && mono namespaceApp.exe
2  3.0 + 4.0 = 7.0
```

Hence, from an application point of view, it is not immediately possible to see, that Utilities is defined as a namespace and not a module. However, in contrast to modules, namespaces may span several files. E.g., we may add a third file extending the Utilities namespace with the MathFcts module as demonstrated in Listing 9.18.

## Listing 9.18 namespaceExtension.fsx:

Namespaces may span several files. Here is shown an extra file, which extends the Utilities namespace.

```
namespace Utilities
module MathFcts =
let add : floatFunction = fun x y -> x + y
```

To compile we now need to include all three files in the right order. Likewise, compilation is performed identically, see Listing 9.19.

Listing 9.19: Compilation of namespaces defined in several files requires careful consideration of order, since the compiler reads once and only once through the files in the order they are given.

```
$ fsharpc --nologo namespace.fsx namespaceExtension.fsx namespaceApp.fsx
&& mono namespaceApp.exe
2 3.0 + 4.0 = 7.0
```

The order matters since namespaceExtension.fsx relies on the definition of floatFunction in the file namespace.fsx. You can use extensions to extend existing namespaces included with the F# compiler.³⁴

Namespaces may also be nested. In contrast to modules, nesting is defined using the "." notation. That is, to create a child namespace more of Utilities we must use initially write namespace Utilities.more. Indentation is ignored in the namespace line, thus left-most indentation is almost always used. Namespaces follow lexical scope rules, and identically to modules, namespaces containing mutually dependent children can be declared using the rec keyword, e.g., namespace rec Utilities.

## 9.3 Compiled libraries

Libraries may be distributed in compiled form as .dll files. This saves the user for having to recompile a possibly large library every time library functions needs to be compiled with an application program. In order to produce a library file from MetaExplicitModuleDefinition.fsx and then compile an application program, we first use the compiler's -a option to produce the .dll. A demonstration is given in Listing 9.20.

```
Listing 9.20: A stand-alone .dll file is created and used with special compile commands.

1  $ fsharpc --nologo -a MetaExplicit.fsx
```

This produces the file MetaExplicit.dll, which may be linked to an application using the -r option during compilation, see Listing 9.21.⁵

 $^{^3\}mathrm{Jon}$ : Something about intrinsic and optional extension <code>https://docs.microsoft.com/en-us/dotnet/fsharp/language-reference/type-extensions.</code>

⁴Jon: Perhaps something about the global namespace global.

⁵Jon: This is the MacOS option standard, Windows is slightly different.

Listing 9.21: The library is linked to an application during compilation to produce runnable code.

```
$ fsharpc --nologo -r MetaExplicit.dll MetaApp.fsx && mono MetaApp.exe
3.0 + 4.0 = 7.0
```

A library can be the result of compiling a number of files into a single .dll file. .dll-files may be loaded dynamically in script files (.fsx-files) using the #r directive as illustrated in Listing 9.23.

 $\cdot$  #r directive

## Listing 9.22 MetaHashApp.fsx:

The .dll file may be loaded dynamically in .fsx script files and in interactive mode. Nevertheless, this usage is not recommended.

```
#r "MetaExplicit.dll"
let add : Meta.floatFunction = fun x y -> x + y
let result = Meta.apply add 3.0 4.0
printfn "3.0 + 4.0 = %A" result
```

We may now omit the explicit mentioning of the library when compiling as shown in Listing 9.23.

Listing 9.23: When using the #r directive, then the .dll file need not be explicitly included in the list of files to be compiled.

```
$ fsharpc --nologo MetaHashApp.fsx && mono MetaHashApp.exe
3.0 + 4.0 = 7.0
```

The #r directive is also used to include a library in interactive mode. However, for code to be compiled, the use of the #r directive requires that the filesystem path to the library is coded inside the script. As for module names, direct linking of filenames with the internal workings of a program is a needless complication of structure, and it is recommended not to rely on the use of the #r directive.

Advice

In the above, we have compiled script files into libraries. However, F# has reserved the .fs filename suffix for library files, and such files are called *implementation files*. In contrast to script files, implementation files do not support the #r directive. When compiling a list of implementation and script files, all but the last file must explicitly define a module or a namespace.

· script files · implementation files

Both script and implementation files may be augmented with signature files. A signature file contains · signature files no implementation but only type definitions. Signature files offers three distinct features:

- 1. Signature files can be used as part of the documentation of code, since type information is of paramount importance for an application programmer to use a library.
- 2. Signature files may be written before the implementation file. This allows for a higher-level programming design that focuses on which functions should be included and how they can be composed.
- 3. Signature files allow for access control. Most importantly, if a type definition is not available in the signature file, then it is not available to the application program. Such definitions are private and can only be used internally in the library code. More fine grained control is available relating to classes, and will be discussed in Chapter 20.

Signature files can be generated automatically using the --sig:<filename> compiler directive. To

demonstrate this feature, we will first move the definition of add to the implementation file, see Listing 9.28.

## Listing 9.24 MetaWAdd.fs: An implementation file including the add function. 1 module Meta 2 type floatFunction = float -> float -> float 3 let apply (f : floatFunction) (x : float) (y : float) : float = f x y 4 let add (x : float) (y : float) : float = x + y

A signature file may be automatically generated as shown in Listing 9.25.

```
Listing 9.25: Automatic generation of a signature file at compile time.

1  $ fsharpc --nologo --sig:MetaWAdd.fsi MetaWAdd.fs

2  MetaWAdd.fs(4,48): warning FS0988: Main module of program is empty:
    nothing will happen when it is run
```

The warning can safely be ignored, since it is at this point not our intention to produce runnable code. The above has generated the signature file in Listing 9.28.

```
Listing 9.26 MetaWAdd.fsi:
An automatically generated signature file from MetaWAdd.fs.

1 module Meta
2 type floatFunction = float -> float -> float
3 val apply : f:floatFunction -> x:float -> y:float -> float
4 val add : x:float -> y:float -> float
```

We can generate a library using the automatically generated signature file using fsharpc -a MetaWAdd.fsi MetaWAdd.fs, which is identical to compiling the .dll file without the signature file. However, if we remove, e.g., the type definition for add in the signature file, then this function becomes private to the module, and cannot be accessed outside. Hence, using the signature file in Listing 9.30 and recompiling the .dll as Listing 9.28 generates no error.

```
Listing 9.27 MetaWAddRemoved.fsi:
Removing the type defintion for add from MetaWAdd.fsi.

1 module Meta
2 type floatFunction = float -> float -> float
3 val apply : f:floatFunction -> x:float -> y:float -> float
```

```
Listing 9.28: Automatic generation of a signature file at compile time.

1 $ fsharpc --nologo -a MetaWAddRemoved.fsi MetaWAdd.fs
```

But, when using the newly created MetaWAdd.dll with a modified version of Listing 9.3, which does

not itself supply a definition of add as shown in Listing 9.29, we get a syntax error, since add now is inaccessible to the application program. This is demonstrated in Listing 9.30.

## Listing 9.29 MetaWOAddApp.fsx:

A version of Listing 9.3 without a definition of add.

```
let result = Meta.apply add 3.0 4.0
printfn "3.0 + 4.0 = %A" result
```

## Listing 9.30: Automatic generation of a signature file at compile time.

```
$ fsharpc --nologo -r MetaWAdd.dll MetaWOAddApp.fsx

MetaWOAddApp.fsx(1,25): error FS0039: The value or constructor 'add' is not defined.
```

## 10 Testing programs

A software bug is an error in a computer program that causes it to produce an incorrect result or behave in an unintended manner. The term bug was used by Thomas Edison in 1878¹, but made popular in computer science by Grace Hopper, who found a moth interfering with the electronic circuits of the Harward Mark II electromechanical computer and coined the term *bug* for errors in computer programs. The original bug is shown in Figure 10.1. Software is everywhere, and errors therein have huge economic impact on our society and can threaten lives².

hug

The ISO/IEC organizations have developed standards for software testing³. To illustrate basic concepts of software quality, consider a hypothetical route planning system. Essential factors of its quality are,

· functionality

**Functionality:** Does the software compile and run without internal errors. Does it solve the problem, it was intended to solve? E.g., does the route planning software finde a suitable route from point a to b?

· reliability

**Reliability:** Does the software work reliably over time? E.g., does the route planning software work in case of internet dropouts?

· usability

**Usability:** Is the software easy and intuitive to use by humans? E.g., is it easy to enter adresses and alternative routes in the software's interface?

· efficiency

 $^{^3}$ ISO/IEC 9126, International standard for the evaluation of software quality, December 19, 1991, later replaced by ISO/IEC 25010:2011

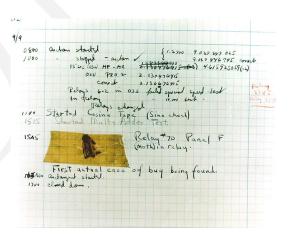


Figure 10.1: The first computer bug caught by Grace Hopper, U.S. Naval Historical Center Online Library Photograph NH 96566-KN.

 $^{^{1}} https://en.wikipedia.org/wiki/Software_bug, possibly http://edison.rutgers.edu/NamesSearch/DocImage.php3?DocId=LB003487$ 

²https://en.wikipedia.org/wiki/List_of_software_bugs

**Efficiency:** How many computer and human resources does the software require? E.g., does it take milliseconds or hours to find a requested route? Can the software run on a mobile platform with limited computer speed and memory?

· maintainability

Maintainability: In case of the discovery of new bugs, is it easy to test and correct the software? Is it easy to extend the software with new functionality? E.g., is it easy to update the map with updated roadmaps and new information? Can the system be improved to work both for car drivers and bicyclists?

· portability

**Portability:** Is it easy to port the software to new systems such as new server architecture and screen sizes? E.g., if the routing software originally was written for IOS devices, will it be easy to port to Android systems?

The above-mentioned concepts are ordered based on the requirements of the system. Functionality and reliability ares perhaps the most important concepts, since if the software does not solve the specified problem, then the software design process has failed. However, many times the problem definition will evolve along with the software development process. But as a bare minimum, the software should run without internal errors and not crash under a well-defined set of circumstances. Furthermore, it is often the case that software designed for the general public requires a lot of attention to the usability of the software, since in many cases non-experts are expected to be able to use the software with little or no prior training. On the other hand, software used internally in companies will be used by a small number of people, who become experts in using the software, and it is often less important that the software is easy to understand by non-experts. An example is text processing software Microsoft Word versus Gnu Emacs and LaTeX. Word is designed to be used by non-experts for small documents such as letters and notes, and relies heavily on interfacing with the system using click-interaction. On the other hand, Emacs and LaTeX are for experts for longer and professionally typeset documents, and relies heavily on keyboard shortcuts and text-codes for typesetting document entities.

The purpose of software testing is to find bugs. When errors are found, then we engage in debugging, which is the process of diagnosing and correcting bugs. Once we have a failed software test, i.e., one that does not find any bugs, then we have strengthened our belief in the software, but it is important to note that software testing and debugging rarely removes all bugs, and with each correction or change of software, there is a fair chance of introducing new bugs. It is not exceptional that the software testing the software is as large as the software itself.

· software testing · debugging

In this chapter, we will focus on two approaches to software testing, which emphasizes functionality: white-box and black-box testing. An important concept in this context is unit testing, where the program is considered in smaller pieces, called units, and for which accompanying programs for testing can be made, which tests these units automatically. Black-box testing considers the problem formulation and the program interface, and can typically be written early in the software design phase. In contrast, white-box testing considers the program text, and thus requires the program to be available. Thus, there is a tendency for black-box test programs to be more stable, while white-box testing typically is developed incrementally along side the software development.

 $\cdot$  white-box testing  $\cdot$  black-box testing

· unit testing

To illustrate software testing we'll start with a problem:

## Problem 10.1

Given any date in the Gregorian calendar, calculate the day of week.

Facts about dates in the Gregorian calendar are:

- combinations of dates and weekdays repeat themselves every 400 years;
- the typical length of the months January, February, ...follow the knucle rule, i.e., January belongs to the index knuckle, February to the space between the index and the middle finger,

and August restarts or starts on the other hand. All knuckle months have 31 days, all spacing months have 30 days except February, which has 29 days on leap years and 28 days all other vears.

• A leap year is a multiplum of 4, except if it is also a multiplum of 100 but not of 400.

Many solutions to the problem have been discovered, and here we will base our program on Gauss' method, which is based on integer division and calculates the weekday of the 1st of January of a given year. For any other date, we will count our way through the weeks from the previous 1st of January. The algorithm relies on an enumeration of weekdays starting with Sunday = 0, Monday  $= 1, \ldots$ , and Saturday = 6. Our proposed solution is shown in Listing  $10.1.^4$ 

Listing 10.1 date2Day.fsx: A function that can calculate day-of-week from any date in the Gregorian calendar. let januaryFirstDay (y : int) = let a = (y - 1) % 4let b = (y - 1) % 100let c = (y - 1) % 400(1 + 5 * a + 4 * b + 6 * c) % 7let rec sum (lst : int list) j = if 0 <= j && j < lst.Length then</pre> lst.[0] + sum lst.[1..] (j - 1)else let date2Day d m y = let dayPrefix = ["Sun"; "Mon"; "Tues"; "Wednes"; "Thurs"; "Fri"; "Satur"] let feb = if (y % 4 = 0) && ((y % 100 <> 0) || (y % 400 = 0)) then 29 let daysInMonth = [31; feb; 31; 30; 31; 30; 31; 30; 31; 30; 31] let dayOne = januaryFirstDay y let daysSince = (sum daysInMonth (m - 2)) + d - 1 let weekday = (dayOne + daysSince) % 7; dayPrefix.[weekday] + "day"

## 10.1White-box testing

White-box testing considers the text of a program. The degree to which the text of the program is · white-box testing covered in the test is called *coverage*. Since our program is small, we do have the opportunity to ensure that all functions are called at least once, which is called function coverage, we will also be able to test every branching in the program, which is called branching coverage, an in this case that implies statement coverage. The procedure is as follows:

- $\cdot$  coverage
- · function coverage
- · branching coverage
- · statement coverage
- 1. Decide which are the units to test: The program shown in Listing 10.1 has 3 functions, and we will consider these each as a unit, but we might as well just have chosen date2Day as a single unit. The important part is that the union of units must cover the whole program text, and since date2Day calls both januaryFirstDay and sum, designing test cases for the two later is superfluous. However, we may have to do this anyway, when debugging, and we may choose at

⁴Jon: This example relies on lists, which has not been introduced yet.

- a later point to use these functions separately, and in both cases, we will be able to reuse the testing of the smaller units.
- 2. Identify branching points: The function <code>januaryFirstDay</code> has no branching function, <code>sum</code> has one, and depending on the input values two paths through the code may be used, and <code>date2Day</code> has one, where the number of days in February is decided. Note that in order to test this, our test-date must be March 1 or later. In this example, there are only examples of <code>if-branch</code> points, but they may as well be loops and pattern matching expressions. In the following code, the branch points have been given a comment and a number, as shown in Listing 10.2.

```
Listing 10.2 date2DayAnnotated.fsx:
In white-box testing, the branch points are identified.
// Unit: januaryFirstDay
let januaryFirstDay (y : int) =
   let a = (y - 1) \% 4
  let b = (y - 1) \% 100
  let c = (y - 1) \% 400
   (1 + 5 * a + 4 * b + 6 * c) \% 7
// Unit: sum
let rec sum (lst : int list) j =
   (* WB: 1 *)
   if 0 <= j && j < lst.Length then</pre>
    lst.[0] + sum lst.[1..] (j - 1)
   else
     0
// Unit: date2Day
let date2Day d m y =
  let dayPrefix =
     ["Sun"; "Mon"; "Tues"; "Wednes"; "Thurs"; "Fri"; "Satur"]
   (* WB: 1 *)
   let feb = if (y % 4 = 0) && ((y % 100 <> 0) || (y % 400 = 0)) then
   29 else 28
   let daysInMonth = [31; feb; 31; 30; 31; 30; 31; 30; 31; 30; 31]
  let dayOne = januaryFirstDay y
   let daysSince = (sum daysInMonth (m - 2)) + d - 1
   let weekday = (dayOne + daysSince) % 7;
   dayPrefix.[weekday] + "day"
```

3. For each unit, produce an input set that tests each branches: In our example the branch points depends on a Boolean expression, and for good measure, we are going to test each term that can lead to branching. Thus,

Unit	Branch	Condition	Input	Expected output
				1
januaryFirstDay	0	-	2016	5
sum	1	0 <= j && j < lst.Length		
	1a	true && true	[1; 2; 3] 1	3
	1b	false && true	[1; 2; 3] -1	0
	1c	true && false	[1; 2; 3] 10	0
	1d	false && false	-	-
date2Day	1	(y % 4 = 0)		
		&& ((y % 100 <> 0)		
		(y % 400 = 0))		
	-	true && (true    true)	-	-
	1a	true && (true    false)	8 9 2016	Thursday
	1b	true && (false    true)	8 9 2000	Friday
	1c	true && (false    false)	8 9 2100	Wednesday
	-	false && (true    true)	-	-
	1d	false && (true    false)	8 9 2015	Tuesday
	-	false && (false    true)	-	-
	-	false && (false    false)	-	-

The impossible cases have been intentionally blank, e.g., it is not possible for j < 0 and j > n for some positive value n.

4. Write a program that test all these cases and checks the output, e.g.,

## Listing 10.3 date2DayWhiteTest.fsx: The tests identified by white-box analysis. The program from Listing 10.2 has been omitted for brevity. printfn "White-box testing of date2Day.fsx" printfn " Unit: januaryFirstDay" printfn " Branch: 0 - %b" (januaryFirstDay 2016 = 5) printfn " Unit: sum" printfn " Branch: 1a - %b'' (sum [1; 2; 3] 1 = 3) printfn " Branch: 1b - %b'' (sum [1; 2; 3] -1 = 0) printfn " Branch: 1c - %b'' (sum [1; 2; 3] 10 = 0) printfn " Unit: date2Day" printfn " Branch: 1a - %b" (date2Day 8 9 2016 = "Thursday") printfn " Branch: 1b - %b" (date2Day 8 9 2000 = "Friday") printfn " Branch: 1c - %b" (date2Day 8 9 2100 = "Wednesday") printfn " Branch: 1d - %b" (date2Day 8 9 2015 = "Tuesday") \$ fsharpc --nologo date2DayWhiteTest.fsx && mono date2DayWhiteTest.exe White-box testing of date2Day.fsx Unit: januaryFirstDay Branch: 0 - true Unit: sum Branch: 1a - true Branch: 1b - true Branch: 1c - true Unit: date2Day Branch: 1a - true Branch: 1b - true Branch: 1c - true Branch: 1d - true

Notice that the output of the tests is organized such that they are enumerated per unit, hence we can rearrange as we like and still uniquely refer to a unit's test. Also, the output of the test program produces a list of tests that should return true or success or a similar positively loaded word, but without further or only little detail, such that we at a glance can identify any test that produced unexpected results.

After the white-box testing has failed to find errors in the program, we have some confidence in the program, since we have run every line at least once. It is, however, in no way a guarantee that the program is error free, which is why white-box testing is often accompanied with black-box testing to be described next.

## 10.2 Black-box testing

In black-box testing the program is considered a black box, and no knowledge is required about how a particular problem is solved, in fact, it is often useful not to have that knowledge at all. It is rarely possible to test all input to a program, so in black-box testing, the solution is tested for typical and extreme cases based on knowledge of the problem. The procedure is as follows:

Decide on the interface to use: It is useful to have an agreement with the software developers about what interface is to be used, e.g., in our case, the software developer has made a function date2Day d m y, where d, m, and y are integers specifying the day, month, and year.

Make an overall description of the tests to be performed and their purpose:

- 1 a consecutive week, to ensure that all weekdays are properly returned
- 2 two set of consecutive days across boundaries that may cause problems: across a new year, across a regular month boundary.
- 3 a set of consecutive days across February-March boundaries for a leap and non-leap year
- 4 four dates after February in a non-multiplum-of-100 leap year and in a non-leap year, a multiplum-of-100-but-not-of-400 non-leap year, and a multiplum-of-400 leap year.

Given no information about the program's text, there are other dates that one could consider as likely candidates of errors, but the above is judged to be a fair coverage.

Choose a specific set of input and expected output relations on tabular form:

Test number	Input	Expected output
1a	1 1 2016	Friday
1b	2 1 2016	Saturday
1c	3 1 2016	Sunday
1d	4 1 2016	Monday
1e	5 1 2016	Tuesday
1f	6 1 2016	Wednesday
1g	7 1 2016	Thursday
2a	31 12 2014	Wednesday
2b	1 1 2015	Thursday
2c	30 9 2017	Saturday
2d	1 10 2017	Sunday
3a	28 2 2016	Sunday
3b	29 2 2016	Monday
3c	1 3 2016	Tuesday
3d	28 2 2017	Tuesday
3e	1 3 2017	Wednesday
4a	1 3 2015	Sunday
4b	1 3 2012	Thursday
4c	1 3 2000	Wednesday
4d	1 3 2100	Monday

Write a program executing the tests as shown in Listing 10.4 and 10.5.

been omitted for brevity.

Listing 10.4 date2DayBlackTest.fsx:

The tests identified by black-box analysis. The program from Listing 10.2 has

```
let testCases = [
  ("A complete week",
   [(1, 1, 2016, "Friday");
    (2, 1, 2016, "Saturday");
    (3, 1, 2016, "Sunday");
    (4, 1, 2016, "Monday");
    (5, 1, 2016, "Tuesday");
    (6, 1, 2016, "Wednesday");
    (7, 1, 2016, "Thursday");]);
  ("Across boundaries",
   [(31, 12, 2014, "Wednesday");
    (1, 1, 2015, "Thursday");
    (30, 9, 2017, "Saturday");
    (1, 10, 2017, "Sunday")]);
  ("Across feburary boundary",
   [(28, 2, 2016, "Sunday");
    (29, 2, 2016, "Monday");
    (1, 3, 2016, "Tuesday");
    (28, 2, 2017, "Tuesday");
    (1, 3, 2017, "Wednesday")]);
 ("Leap years",

[(1, 3, 2015, "Sunday");

(1, 3, 2012, "Thursday");
    (1, 3, 2000, "Wednesday");
    (1, 3, 2100, "Monday")]);
 ]
printfn "Black-box testing of date2Day.fsx"
for i = 0 to testCases.Length - 1 do
 let (setName, testSet) = testCases.[i]
 printfn " %d. %s" (i+1) setName
  for j = 0 to testSet.Length - 1 do
    let (d, m, y, expected) = testSet.[j]
    let day = date2Day d m y
               test %d - %b" (j+1) (day = expected)
```

```
Listing 10.5: Output from Listing 10.4.
$ fsharpc --nologo date2DayBlackTest.fsx && mono
   date2DayBlackTest.exe
Black-box testing of date2Day.fsx
  1. A complete week
    test 1 - true
     test 2 - true
     test 3 - true
     test 4 - true
     test 5 - true
     test 6 - true
     test 7 - true
  2. Across boundaries
     test 1 - true
     test 2 - true
     test 3 - true
     test 4 - true
  3. Across feburary boundary
     test 1 - true
     test 2 - true
     test 3 - true
     test 4 - true
     test 5 - true
  4. Leap years
     test 1 - true
     test 2 - true
     test 3 - true
     test 4 - true
```

Notice how the program has been made such that it is almost a direct copy of the table, produced in the previous step.

A black-box test is a statement of what a solution should fulfill for a given problem. Hence, it is a Advice good idea to make a black-box test early in the software design phase, in order to clarify the requirements for the code to be developed, and take an outside view of the code prior to developing it.

After the black-box testing has failed to find errors in the program, we have some confidence in the program, since from a user's perspective, the program produces sensible output in many cases. It is, however, in no way a guarantee that the program is error free.

## 10.3Debugging by tracing

Once an error has been found by testing, then the debugging phase starts. The cause of a bug can either be that the algorithm chosen is the wrong one for the job, or the implementation of it has an error. In the debugging process, we have to keep an open mind, and not rely on assumptions, since assumptions tend to blind the reader of a text. A frequent source of errors is that the state of a program is different, than expected, e.g., because the calculation performed is different than intended, or that the return of a library function is different than expected. The most important tool for debugging is simplification. This is similar to white-box testing, but where the units tested are very small. E.g., the suspected piece of code could be broken down into smaller functions or code snippets, which is given well-defined input, and, e.g., use printfn statements to obtain the output of the code snippet. Another related technique is to use mockup code, which replaces parts of the code with code that produces safe and · mockup code

relevant results. If the bug is not obvious then more rigorous techniques must be used such as *tracing*. · tracing Some development interfaces has built-in tracing system, e.g., <code>fsharpi</code> will print inferred types and some binding values. However, often a source of a bug is due to a misunderstanding of the flow of data through a program execution, and we will in the following introduce *hand tracing* a technique to · hand tracing simulate the execution of a program by hand.

Consider the program in Listing 10.6. ⁵

```
Listing 10.6 gcd.fsx:
gcd

let rec gcd a b =
    if a < b then
        gcd b a
    elif b > 0 then
        gcd b (a % b)
    else
    a

let a = 10
let b = 15
printfn "gcd %d %d = %d" a b (gcd a b)

fsharpc --nologo gcd.fsx && mono gcd.exe
gcd 10 15 = 5
```

The greatest common divisor of 2 integers. which includes a function for calculating the greatest common divisor of 2 integers, and calls this function with the numbers 10 and 15. Hand tracing this program means that we simulate its execution and as part of that keep track of the bindings, assignments and input and output of the program. To do this, we need to consider code snippet's environment. E.g., to hand trace the above program, we start by noting the outer environment, called  $\cdot$  environment  $E_0$  for short. In line 1, then the gcd identifier is bound to a function, hence we write:

$$E_0$$
: gcd  $\rightarrow$   $\big((a,b), \text{gcd-body}, \varnothing\big)$ 

Function bindings like this one is noted as a closure, which is the triplet (arguments, expression, environment). The closure is everything needed for the expression to be calculated. Here we wrote gcd-body to denote everything after the equal sign in the function binding. Next, F# executes line 9 and 10, and we update our environment to reflect the bindings as,

```
E_0:

\gcd \to ((a, b), \gcd\text{-body}, \varnothing)

a \to 10

b \to 15
```

⁵Jon: This program uses recursion, which has not been introduced yet.

In line 11 the function is evaluated. This initiates a new environment  $E_1$ , and we update our trace as,

$$E_0$$
:  
 $\gcd \to ((a, b), \gcd\text{-body}, \varnothing)$   
 $a \to 10$   
 $b \to 15$   
line 11:  $\gcd a b \to ?$   
 $E_1:((a \to 10, b \to 15), \gcd\text{-body}, \varnothing)$ 

where the new environment is noted to have gotten its argument names a and b bound to the values 10 and 15 respectively, and where the return of the function to environment  $E_0$  is yet unknown, so it is noted as a question mark. In line 2 the comparison a < b is checked, and since we are in environment  $E_1$  then this is the same as checking 10 < 15, which is true so the program executes line 3. Hence, we initiate a new environment  $E_2$  and update our trace as,

$$E_0: \\ \gcd \to \big((a,b), \gcd\text{-body}, \varnothing\big) \\ a \to 10 \\ b \to 15 \\ \text{line 11: gcd a b} \to ? \\ E_1: \big((a \to 10, b \to 15), \gcd\text{-body}, \varnothing\big) \\ \text{line 3: gcd b a} \to ? \\ E_2: \big((a \to 15, b \to 10), \gcd\text{-body}, \varnothing\big)$$

where in the new environment a and b bound to the values 15 and 10 respectively. In  $E_2$ , 10 < 15 is false, so the program evaluates b > 0, which is true, hence line 5 is executed. This calls gcd once again, but with new arguments, and a % b is parenthesized, then it is evaluated before gcd is called.

Hence, we update our trace as,

$$E_0: \\ \gcd \to \big((a,b), \gcd\text{-body}, \varnothing\big) \\ a \to 10 \\ b \to 15 \\ \text{line 11: gcd a b} \to ? \\ E_1: \big((a \to 10, b \to 15), \gcd\text{-body}, \varnothing\big) \\ \text{line 3: gcd b a} \to ? \\ E_2: \big((a \to 15, b \to 10), \gcd\text{-body}, \varnothing\big) \\ \text{line 5: a \% b} \to 5 \\ \text{line 5: gcd b (a \% b)} \to ? \\ E_3: \big((a \to 10, b \to 5), \gcd\text{-body}, \varnothing\big) \\ \end{aligned}$$

Again we fall through to line 5, evaluate the remainder operator and initiates a new environment,

$$E_0: \gcd \to \big((a,b), \gcd\text{-body}, \varnothing\big)$$

$$a \to 10$$

$$b \to 15$$

$$\text{line 11: } \gcd \text{ a b} \to ?$$

$$E_1: \big((a \to 10, b \to 15), \gcd\text{-body}, \varnothing\big)$$

$$\text{line 3: } \gcd \text{ b a} \to ?$$

$$E_2: \big((a \to 15, b \to 10), \gcd\text{-body}, \varnothing\big)$$

$$\text{line 5: } \text{ a \% b} \to 5$$

$$\text{line 5: } \gcd \text{ b (a \% b)} \to ?$$

$$E_3: \big((a \to 10, b \to 5), \gcd\text{-body}, \varnothing\big)$$

$$\text{line 5: } \text{ a \% b} \to 0$$

$$\text{line 5: } \gcd \text{ b (a \% b)} \to ?$$

$$E_4: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big)$$

This time both a < b and b > 0 are false, so we fall through to line 7, and gcd from  $E_4$  returns its value of a, which is 5, so we scratch  $E_4$  and change the question mark in  $E_3$  to 5:

$$E_0: \\ \gcd \to \big((a,b), \gcd\text{-body}, \varnothing\big) \\ a \to 10 \\ b \to 15 \\ \text{line 11: } \gcd \text{ a b} \to ? \\ E_1: \big((a \to 10, b \to 15), \gcd\text{-body}, \varnothing\big) \\ \text{line 3: } \gcd \text{ b a} \to ? \\ E_2: \big((a \to 15, b \to 10), \gcd\text{-body}, \varnothing\big) \\ \text{line 5: } a \% \text{ b} \to 5 \\ \text{line 5: } \gcd \text{ b (a \% b)} \to ? \\ E_3: \big((a \to 10, b \to 5), \gcd\text{-body}, \varnothing\big) \\ \text{line 5: } a \% \text{ b} \to 0 \\ \text{line 5: } \gcd \text{ b (a \% b)} \to ? \\ S_4: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_5: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_6: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_7: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ S_8: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big)$$

Now line 5 in  $E_3$  is also a return point of gcd, hence we scratch  $E_3$  and change the question mark in

 $E_2$  to 5,

$$E_0: \\ \gcd \to \big((a,b), \gcd\text{-body}, \varnothing\big) \\ a \to 10 \\ b \to 15 \\ \text{line 11: } \gcd \text{ a b} \to ? \\ E_1: \big((a \to 10, b \to 15), \gcd\text{-body}, \varnothing\big) \\ \text{line 3: } \gcd \text{ b a} \to ? \\ E_2: \big((a \to 15, b \to 10), \gcd\text{-body}, \varnothing\big) \\ \text{line 5: } \text{ a \% b} \to 5 \\ \text{line 5: } \gcd \text{ b (a \% b)} \to \lozenge 5 \\ \text{line 5: } \gcd \text{ b (a \% b)} \to \lozenge 5 \\ \text{line 5: } \text{ a \% b} \to 0 \\ \text{line 5: } \text{ gcd b (a \% b)} \to \lozenge 5 \\ \text{Se}_{\&}: \big((a \to 10, b \to 5), \gcd\text{-body}, \varnothing\big) \\ \text{line 5: } \text{ gcd b (a \% b)} \to \lozenge 5 \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big) \\ \text{Se}_{\&}: \big((a \to 5, b \to 0), \deg\text{-$$

and likewise, for  $E_2$  and  $E_1$ :

$$E_0: \gcd \to \big((a,b), \gcd\text{-body}, \varnothing\big)$$

$$a \to 10$$

$$b \to 15$$

$$\lim 11: \gcd a b \to 3$$

$$\mathcal{E}_{\mathbf{k}}: \big((a \to 10, b \to 15), \gcd\text{-body}, \varnothing\big)$$

$$\lim 3: \gcd b a \to 3$$

$$\mathcal{E}_{\mathbf{k}}: \big((a \to 15, b \to 10), \gcd\text{-body}, \varnothing\big)$$

$$\lim 5: a \% b \to 5$$

$$\lim 5: \gcd b (a \% b) \to 3$$

$$\mathcal{E}_{\mathbf{k}}: \big((a \to 10, b \to 5), \gcd\text{-body}, \varnothing\big)$$

$$\lim 5: a \% b \to 0$$

$$\lim 5: \gcd b (a \% b) \to 3$$

$$\mathcal{E}_{\mathbf{k}}: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big)$$

Now we are able to continue the program in environment  $E_0$  with the printfn statement, and we

write:

```
E_0: \gcd \to \big((a,b), \gcd\text{-body}, \varnothing\big)
a \to 10
b \to 15
\text{line 11: } \gcd \text{ a } b \to \cong 5
\text{line 11: }  \operatorname{stdout} \to \cong 2d 10 15 = 5
E_k: \big((a \to 10, b \to 15), \gcd\text{-body}, \varnothing\big)
\text{line 3: }  \gcd \text{ b } a \to \cong 5
E_2: \big((a \to 15, b \to 10), \gcd\text{-body}, \varnothing\big)
\text{line 5: }  a \% \text{ b} \to 5
\text{line 5: }  \gcd \text{ b } (a \% \text{ b}) \to \cong 5
E_3: \big((a \to 10, b \to 5), \gcd\text{-body}, \varnothing\big)
\text{line 5: }  a \% \text{ b} \to 0
\text{line 5: }  \gcd \text{ b } (a \% \text{ b}) \to \cong 5
E_4: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big)
```

which completes the hand tracing of gcd.fsx.

F# uses lexical scope, which implies that besides function arguments, we also at times need to consider the environment at place of writing. Consider the program in Listing 10.7.

```
Listing 10.7 lexicalScopeTracing.fsx:
lexicalScopeTracing

let testScope x =
let a = 3.0
let f z = a * z
let a = 4.0
f x
printfn "%A" (testScope 2.0)

fsharpc --nologo lexicalScopeTracing.fsx
mono lexicalScopeTracing.exe
6.0
```

Example of lexical scope and closure environment. To hand trace this, we start by creating the outer environment, define the closure for testScope, and reach line 6,

```
E_0:

testScope \rightarrow (x, \text{testScope-body}, \varnothing)

line 6: testScope 2.0 \rightarrow ?
```

We create new environment for testScope and note the bindings,

$$E_0$$
:  
testScope  $\rightarrow$   $(x, \text{testScope-body}, \varnothing)$   
line 6: testScope  $2.0 \rightarrow ?$   
 $E_1: (x \rightarrow 2.0, \text{testScope-body}, \varnothing)$   
 $a \rightarrow 3.0$   
 $f \rightarrow (z, a * z, (a \rightarrow 3.0, x \rightarrow 2.0))$   
 $a \rightarrow 4.0$ 

Since we are working with lexical scope, then a is noted twice, and its interpretation is by lexical order. Hence, the environment for the closure of f is everything above in  $E_1$ , so we add  $a \to 3.0$  and  $x \to 2.0$ . In line 5 f is called, so we create an environment based on its closure,

$$E_0: \\ \text{testScope} \to \big(x, \text{testScope-body}, \varnothing\big) \\ \text{line 6: testScope } 2.0 \to ? \\ E_1: \big(x \to 2.0, \text{testScope-body}, \varnothing\big) \\ a \to 3.0 \\ \text{f} \to \big(z, \text{a * z}, (a \to 3.0, x \to 2.0)\big) \\ a \to 4.0 \\ \text{line 5: f x } \to ? \\ E_2: \big(z \to 2.0, \text{a * z}, (a \to 3.0, x \to 2.0\big) \\ \end{cases}$$

The expression in the environment  $E_2$  evaluates to 6.0, and unravelling the scopes we get,

$$E_0: \\ \text{testScope} \to \left(x, \text{testScope-body}, \varnothing\right) \\ \text{line 6: testScope } 2.0 \to \% 6.0 \\ \text{line 6: stdout} \to "6.0" \\ \mathcal{E}_{\mathbb{Q}}: \left(x \to 2.0, \text{testScope-body}, \varnothing\right) \\ a \to 3.0 \\ \text{f} \to \left(z, \text{a * z}, \left(a \to 3.0, x \to 2.0\right)\right) \\ a \to 4.0 \\ \text{line 5: f x} \to \% 6.0 \\ \mathcal{E}_{\mathbb{Q}}: \left(z \to 2.0, \text{a * z}, \left(a \to 3.0, x \to 2.0\right)\right) \\ \end{aligned}$$

For mutable bindings, i.e., variables, the scope is dynamic. For this we need the concept of storage. Consider the program in Listing 10.8.

printfn "%A" (testScope 2.0)

## Listing 10.8 dynamicScopeTracing.fsx: dynamicScopeTracing let testScope x = let mutable a = 3.0 let f z = a * z a <- 4.0 f x

```
s fsharpc --nologo dynamicScopeTracing.fsx mono dynamicScopeTracing.exe 8.0
```

Example of lexical scope and closure environment. We add a storage area to our hand tracing, e.g., line 6,

```
Store : E_0: \operatorname{testScope} \to \left(x,\operatorname{testScope-body},\varnothing\right) line 6: \operatorname{testScope} 2.0 \to ?
```

So when we generate environment  $E_1$ , the mutable binding is to a storage location,

```
Store: \alpha_1 \to 3.0
E_0:
\operatorname{testScope} \to (x, \operatorname{testScope-body}, \varnothing)
\operatorname{line} 6: \operatorname{testScope} 2.0 \to ?
E_1: (x \to 2.0, \operatorname{testScope-body}, \varnothing)
a \to \alpha_1
```

which is assigned the value 3.0 at the definition of a. Now the definition of f is uses the storage location

```
Store: \alpha_1 \to 3.0
E_0:
\operatorname{testScope} \to \left(x, \operatorname{testScope-body}, \varnothing\right)
\operatorname{line} 6: \operatorname{testScope} 2.0 \to ?
E_1: \left(x \to 2.0, \operatorname{testScope-body}, \varnothing\right)
a \to \alpha_1
f \to \left(z, \mathbf{a} * \mathbf{z}, (a \to \alpha_1, x \to 2.0)\right)
```

and in line 4 it is the value in the storage, which is updated,

```
Store: \alpha_1 \to 3.04.0
E_0:
\operatorname{testScope} \to (x,\operatorname{testScope-body},\varnothing)
\operatorname{line} 6: \operatorname{testScope} 2.0 \to ?
E_1: (x \to 2.0,\operatorname{testScope-body},\varnothing)
a \to \alpha_1
f \to (z, a * z, (a \to \alpha_1, x \to 2.0))
```

Hence,

Store: 
$$\alpha_1 \to 3.0 \ 4.0$$

$$E_0:$$

$$\operatorname{testScope} \to (x, \operatorname{testScope-body}, \varnothing)$$

$$\operatorname{line} 6: \ \operatorname{testScope} \ 2.0 \to ?$$

$$E_1: (x \to 2.0, \operatorname{testScope-body}, \varnothing)$$

$$a \to \alpha_1$$

$$f \to (z, a * z, (a \to \alpha_1, x \to 2.0))$$

$$\operatorname{line} 5: \ f \ x \to ?$$

$$E_2: (z \to 2.0, a * z, (a \to \alpha_1, x \to 2.0))$$

and the return value from f evaluated in environment  $E_2$  now reads the value 4.0 for a and returns 8.0. Hence,

Store: 
$$\alpha_1 \to 3.0 \ 4.0$$

$$E_0:$$

$$\operatorname{testScope} \to (x, \operatorname{testScope-body}, \varnothing)$$

$$\operatorname{line} 6: \ \operatorname{testScope} \ 2.0 \to \S \ 8.0$$

$$\operatorname{line} 6: \ \operatorname{stdout} \to "8.0"$$

$$E_1: (x \to 2.0, \operatorname{testScope-body}, \varnothing)$$

$$a \to \alpha_1$$

$$f \to (z, a * z, (a \to \alpha_1, x \to 2.0))$$

$$\operatorname{line} 5: \ f \ x \to \S \ 8.0$$

$$E_2: (z \to 2.0, a * z, (a \to \alpha_1, x \to 2.0))$$

As can be seen by the above examples, hand tracing can be used to in detail study the flow of data through a program. It may seem tedious in the beginning, but the care illustrated above is useful at start to ensure rigor in the analysis. Most will find that once accustomed to the method, the analysis can be performed rigorously but with less paperwork, and in conjunction with strategically placed debugging printfn statements, it is a very valuable tool for debugging.

## 11 | Collections of data

F# is tuned to work with collections of data, and there are several built-in types of collections with various properties making them useful for different tasks. Examples include: strings, lists, arrays, and sequences. Strings were discussed in Chapter 5 and will be revisited here in more details. Sequences will not be discussed, 1 and we will concentrate on lists and one- and two-dimensional arrays.

## 11.1 Strings

Strings have been discussed in Chapter 5, the content of which will be briefly revisited here followed by a description of some of the many supporting built-in functions in F# on strings.

A string is a sequence of characters. Each character is represented using UTF-16, see Appendix C for further details on the unicode standard. The type string is an alias for <code>System.string</code>. String literals are delimited by quotation marks "" and inside the delimiters, character escape sequences are allowed (see Table 5.2), which are replaced by the corresponding character code. Examples are "This is a string", "\tTabulated string", "A \"quoted\" string", and "". Strings may span several lines, and new lines inside strings are part of the string unless the line is ended with a backslash. Strings may be <code>verbatim</code> by preceding the string with "@", in which case escape sequences are not replaced, but a double quotation marks is an escape sequence which is replaced by a single, e.g., Q"This is a string", Q"\tNon-tabulated string", Q"A ""quoted" string", and Q"". Alternatively, a verbatim string may be delimited by tripple quotes, e.g., """This is a string"", """\tNon-tabulated string"", """A "quoted" string"", and """"". Strings may be indexed using the .[] notation, as demonstrated in Listing 5.27.

## · string · System.string

· verbatim string

## 11.1.1 String properties

Strings have a few properties, which are values attached to each string and access using the " ." notation. The only to be mentioned here is:

Length: Returns the length of the string. Compare with String.length method.

```
Listing 11.1: Length

| 'abcd'.Length;;
| val it : int = 4
```

¹Jon: Should we discuss sequences?

#### 11.1.2 String module

In the String module the following functions are available.

String.collect: (char -> string) -> string -> string. Creates a new string whose characters are the results of applying a specified function to each of the characters of the input string and concatenating the resulting strings.

```
Listing 11.2: String.collect

> String.collect (fun c -> (string c) + ", ") "abc";;

val it : string = "a, b, c, "
```

String.concat: string -> seq<string> -> string. Returns a new string made by concatenating the given strings with a separator. Here seq<string> is a sequence but can also be a list or an array.

```
Listing 11.3: String.concat

String.concat ", " ["abc"; "def"; "ghi"];;

val it : string = "abc, def, ghi"
```

String.exists: (char -> bool) -> string -> bool. Tests if any character of the string satisfies the given predicate.

```
Listing 11.4: String.exists

1 > String.exists (fun c -> c = 'd') "abc";;
2 val it : bool = false
```

String.forall: (char -> bool) -> string -> bool. Tests if all characters in the string satisfy the given predicate.

```
Listing 11.5: String.forall

1 > String.forall (fun c -> c < 'd') "abc";;
2 val it : bool = true
```

String.init: int -> (int -> string) -> string. Creates a new string whose characters are the results of applying a specified function to each index and concatenating the resulting strings.

```
Listing 11.6: String.init

1 > String.init 5 (fun i -> (string i) + ", ");;
2 val it : string = "0, 1, 2, 3, 4, "
```

String.iter: (char -> unit) -> string -> unit. Applies a specified function to each character in the string.

```
Listing 11.7: String.iter

1 > String.iter (fun c -> printfn "%c" c) "abc";;
2 a
3 b
4 c
5 val it : unit = ()
```

String.iteri: (int -> char -> unit) -> string -> unit. Applies a specified function to the index of each character in the string and the character itself.

```
Listing 11.8: String.iteri

> String.iteri (fun i c -> printfn "%d: %c" i c) "abc";;

0: a

1: b

2: c

val it : unit = ()
```

String.length: string -> int. Returns the length of the string.

```
Listing 11.9: String.length

> String.length "abcd";;

val it : int = 4
```

String.map: (char -> char) -> string -> string. Creates a new string whose characters are the results of applying a specified function to each of the characters of the input string.

```
Listing 11.10: String.map

1 > let dc = int 'A' - int 'a'
2 - String.map (fun c -> c + char dc) "abcd";;
3 val dc : int = -32
4 val it : string = "ABCD"
```

String.mapi: (int -> char -> char) -> string -> string. Creates a new string whose characters are the results of applying a specified function to each character and index of the input string.

```
Listing 11.11: String.mapi

> String.mapi (fun i c -> char (int c + i)) "aaaa";;

val it : string = "abcd"
```

String.replicate: int -> string -> string. Returns a string by concatenating a specified number of instances of a string.

```
Listing 11.12: String.replicate

> String.replicate 4 "abc, ";;

val it : string = "abc, abc, abc, "
```

#### 11.2 Lists

Lists are unions of immutable values of the same type and have a more flexible structure than tuples.  $\cdot$  list Lists can be expressed as a sequence expression,  $\cdot$  sequence expression

```
Listing 11.13 Lists with a sequence expression.

[[<expr>{; <expr>}]]
```

Examples are [1; 2; 3; 4; 5], which represents a list of integers, ["This"; "is"; "a"; "list"], which represents a list of strings, [(fun x  $\rightarrow$  x); (fun x  $\rightarrow$  x*x)], which represents a list of anonymous functions, and [], which is an empty list. Lists may also be given as ranges,

```
Listing 11.14 Lists with a range expressions.

[<expr> .. <expr> [.. <expr>]
```

where <expr> in range expressions must be of integers, floats, or characters. Examples are [1 .. 5], range expressions [-3.0 .. 2.0], and ['a' .. 'z']. Range expressions may include a step size, thus, [1 .. 2 .. 10] evaluates to [1; 3; 5; 7; 9].

A list type is identified with the *list* keyword, such that a list of integers has the type int list. ·list Like strings, lists may be indexed using the ". []" notation, the lengths of lists is retrieved using the ·. [] · Length property, and we may test whether a list is empty using the *isEmpty* property. These features · Length are demonstrated in Listing 11.15. · isEmpty

```
Listing 11.15 listIndexing.fsx:
Lists are indexed as strings and has a Length property.

let printList (lst : int list) : unit =
for i = 0 to lst.Length - 1 do
printf "%A " lst.[i]
printfn ""

let lst = [3; 4; 5]
printfn "lst = %A, lst.[1] = %A" lst lst.[1]
printfn "lst.Length = %A, lst.isEmpty = %A" lst.Length lst.IsEmpty
printList lst

$ fsharpc --nologo listIndexing.fsx && mono listIndexing.exe
lst = [3; 4; 5], lst.[1] = 4
lst.Length = 3, lst.isEmpty = false
3 4 5
```

F# implements lists as linked lists, see Figure 11.1, which is why indexing element i has computational complexity  $\mathcal{O}(i)$ , since the list has to be traversed from the beginning until element i is located. Thus, indexing lists is slow and should be avoided.

Advice

 $\cdot$  for

·in

Notice especially that lists are zero-indexed, and thus, the last element in a list lst is lst.Length -1. This is a very common source of error! Therefore, indexing in lists using *for*-loops is supported using a special notation with the *in* keyword,



Figure 11.1: A list is a linked list: Here is illustrated the linked list of ["This"; "is"; "a"; "list"].

```
Listing 11.16 For-in loop with in expression.

1 for <ident> in list> do <bodyExpr> [done]
```

In for-in loops, the loop runs through each element of the st>, and assigns it to the identifier <ident>. This is demonstrated in Listing 11.17.

```
Listing 11.17 listFor.fsx:

The - loops are preferred over - .

1 let printList (lst : int list) : unit =
2 for elm in lst do
3 printf "%A " elm
4 printfn ""

5 printList [3; 4; 5]

1 $ fsharpc --nologo listFor.fsx && mono listFor.exe
2 3 4 5
```

Using for-in-expressions remove the risk of off-by-one indexing errors, and thus, for-in is to be Advice preferred over for-to.

Lists support slicing identically to strings as demonstrated in Listing 11.18.

```
Listing 11.18 listSlicing.fsx:
Examples of list slicing. Compare with Listing 5.27.
let lst = ['a' .. 'g']
printfn "%A" lst.[0]
printfn "%A" lst.[3]
printfn "%A" lst.[3..]
printfn "%A" lst.[..3]
printfn "%A" lst.[1..3]
printfn "%A" lst.[*]
$ fsharpc --nologo listSlicing.fsx && mono listSlicing.exe
'a'
'd'
['d'; 'e'; 'f'; 'g']
['a'; 'b'; 'c'; 'd']
['b'; 'c'; 'd']
 ['a'; 'b'; 'c'; 'd'; 'e'; 'f'; 'g']
```

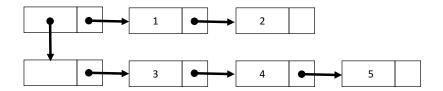


Figure 11.2: A list is a ragged linked list: Here is illustrated the linked list of [[1;2];[3;4;5]].

Lists may be concatenated using either the " $\mathcal{O}$ " concatenation operator or the "::" cons operators. • © The differences is that " $\mathcal{O}$ " concatenates two lists of identical types, while "::" concatenates an element • list of identical types. This is demonstrated in Listing 11.19.

· list concatenation

·::

 $\cdot$  list cons

```
Listing 11.19 listCon.fsx:

Examples of list concatenation.

printfn "[1] @ [2; 3] = %A" ([1] @ [2; 3])
printfn "[1; 2] @ [3; 4] = %A" ([1; 2] @ [3; 4])
printfn "1 :: [2; 3] = %A" (1 :: [2; 3])

fsharpc --nologo listCon.fsx && mono listCon.exe
[1] @ [2; 3] = [1; 2; 3]
[1; 2] @ [3; 4] = [1; 2; 3; 4]
1 :: [2; 3] = [1; 2; 3]
```

Since lists are represented as linked lists, then the cons operator is very efficient and has computational complexity  $\mathcal{O}(1)$ , while concatenation has computational complexity  $\mathcal{O}(n)$ , where n is the length of the first list.

It is possible to make multidimensional lists as lists of lists as shown in Listing 11.20.

```
Listing 11.20 listMultidimensional.fsx:

A ragged multidimensional list, built as lists of lists, and its indexing.

1 let a = [[1;2];[3;4;5]]
2 let row = a.Item 0 in printfn "%A" row
3 let elm = row.Item 1 in printfn "%A" elm
4 let elm = (a.Item 0).Item 1 in printfn "%A" elm

1 $ fsharpc --nologo listMultidimensional.fsx
2 $ mono listMultidimensional.exe
3 [1; 2]
4 2
5 2
```

The example shows a ragged multidimensional list, since each row has a different number of elements. · ragged This is also illustrated in Figure 11.2. · multidimensional list, since each row has a different number of elements.

ragged multidimensional list

The indexing of a particular element is slow due to the linked list implementation of lists, which is

²Jon: why does the at-symbol not appear in the index?

why arrays are often preferred for two- and higher-dimensional data structures, see Section 11.3.

#### 11.2.1 List properties

Lists supports a number of properties, i.e., values that are attached to each list and access using the "." notation, some of which are:

Head: Returns the first element of a list.

```
Listing 11.21: Head

1 > [1; 2; 3]. Head;;
2 val it : int = 1
```

IsEmpty: Returns true if the list is empty.

```
Listing 11.22: Head

1 > [1; 2; 3].IsEmpty;;
2 val it : bool = false
```

Length: Returns the number of elements in the list.

Tail: Returns the list except its first element.

```
Listing 11.24: Tail

1 > [1; 2; 3].Tail;;
2 val it : int list = [2; 3]
```

#### 11.2.2 List module

The built-in List module contains a wealth of functions for lists, some of which are briefly summarized below:

List.collect: ('T -> 'U list) -> 'T list -> 'U list. Apply the supplied function to each element in a list and return a concatenated list of the results.

```
Listing 11.25: List.collect

1 > List.collect (fun elm -> [elm; elm; elm]) [1; 2; 3];;
2 val it : int list = [1; 1; 1; 2; 2; 2; 3; 3; 3]
```

List.contains: 'T -> 'T list -> bool. Returns true or false depending on whether an element is contained in the list.

```
Listing 11.26: List.contains

1 > List.contains 3 [1; 2; 3];;
2 val it : bool = true
```

List.empty: 'T list. An empty list of inferred type.

```
Listing 11.27: List.empty

> let a : int list = List.empty;;

val a : int list = []
```

List.exists: ('T -> bool) -> 'T list -> bool. Returns true or false depending on whether any element is true for a given function.

```
Listing 11.28: List.exists

1 > let odd x = (x % 2 = 1) in List.exists odd [0 .. 2 .. 4];;
2 val it : bool = false
```

List.filter: ('T -> bool) -> 'T list -> 'T list. Returns a new list, of all the elements of the original list for which the supplied function evaluates to true.

```
Listing 11.29: List.filter

1 > let odd x = (x % 2 = 1) in List.filter odd [0 .. 9];;
2 val it : int list = [1; 3; 5; 7; 9]
```

List.find: ('T -> bool) -> 'T list -> 'T. Return the first element for which the given function is true.

```
Listing 11.30: List.find

1 > let odd x = (x % 2 = 1) in List.find odd [0 .. 9];;
2 val it : int = 1
```

List.findIndex: ('T -> bool) -> 'T list -> int. Return the index of the first element for which the given function is true.

```
Listing 11.31: List.findIndex

| | > let isK x = (x = 'k') in List.findIndex isK ['a' .. 'z'];;
| val it : int = 10
```

List.fold: ('State -> 'T -> 'State) -> 'State -> 'T list -> 'State. Update an accumulator iteratively by applying the supplied function to each element in a list, e.g. for a list consisting of  $x_0, x_1, x_2, \ldots, x_n$ , a supplied function f, and an initial value for the accumulator s, calculate  $f(\ldots f(f(s, x_0), x_1), x_2), \ldots, x_n)$ .

```
Listing 11.32: List.fold

1 > let addSquares acc elm = acc + elm*elm
2 - List.fold addSquares 0 [0 .. 9];;
3 val addSquares : acc:int -> elm:int -> int
4 val it : int = 285
```

List.foldBack: ('T -> 'State -> 'State) -> 'T list -> 'State -> 'State. Update an accumulator iteratively by applying function to each element in a list, e.g. for a list consisting of  $x_0, x_1, x_2, \ldots, x_n$ , a supplied function f, and an initial value for the accumulator s, calculate  $f(x_0, f(x_1, f(x_2, \ldots, f(x_n, s))))$ .

```
Listing 11.33: List.foldBack

1 > let addSquares elm acc = acc + elm*elm
2 - List.foldBack addSquares [0 .. 9] 0;;
3 val addSquares : elm:int -> acc:int -> int
4 val it : int = 285
```

List.forall: ('T -> bool) -> 'T list -> bool. Apply a function to all element and logically and the result.

List.head: 'T list -> int. The first element in the list. Exception if empty.

```
Listing 11.35: List.head

1 > let a = [1; -2; 0] in List.head a;;
2 val it : int = 1
```

List.isEmpty: 'T list -> int. Compare with the empty list

List.item: 'T list -> int. Retrieve an element of a list by its index.

```
Listing 11.37: List.item

1 > let a = [1; -3; 0] in List.item 1 a;;
2 val it : int = -3
```

List.iter: ('T -> unit) -> 'T list -> unit. Apply a procedure to every element in the list.

```
Listing 11.38: List.iter

1  > let prt x = printfn "%A " x in List.iter prt [0; 1; 2];;
2  0
3  1
4  2
5  val it : unit = ()
```

List.Length: 'T list -> int. The number of elements in a list

```
Listing 11.39: List.Length

1 > List.length [1; 2; 3];;
2 val it : int = 3
```

List.map: ('T -> 'U) -> 'T list -> 'U list. Return a list, where the supplied function has been applied to every element.

```
Listing 11.40: List.map

1 > let square x = x*x in List.map square [0 .. 9];;
2 val it : int list = [0; 1; 4; 9; 16; 25; 36; 49; 64; 81]
```

List.ofArray: 'T list -> int. Return a list whose elements are the same as the supplied array.

```
Listing 11.41: List.ofArray

1 > List.ofArray [|1; 2; 3|];;
2 val it : int list = [1; 2; 3]
```

List.rev: 'T list -> 'T list. Return a list whose elements have been reversed.

```
Listing 11.42: List.rev

1 > List.rev [1; 2; 3];;
2 val it : int list = [3; 2; 1]
```

List.sort: 'T list -> 'T list. Return a list whos elements have been sorted.

```
Listing 11.43: List.sort

1 > List.sort [3; 1; 2];;
2 val it : int list = [1; 2; 3]
```

List.tail: 'T list -> 'T list. The list except its first element. Exception if empty.

List.toArray: 'T list -> 'T []. Return an array whos elements are the same as the supplied list.

```
Listing 11.45: List.toArray

1 > List.toArray [1; 2; 3];;
2 val it : int [] = [|1; 2; 3|]
```

List.unzip: ('T1 * 'T2) list -> 'T1 list * 'T2 list. Return a pair of lists, whos elements are take from pairs of a list.

List.zip: 'T1 list -> 'T2 list -> ('T1 * 'T2) list. Return a list of pairs, whos elements are take iteratively from two lists.

```
Listing 11.47: List.zip

1 > List.zip [1; 2; 3] ['a'; 'b'; 'c'];;
2 val it : (int * char) list = [(1, 'a'); (2, 'b'); (3, 'c')]
```

# 11.3 Arrays

One dimensional arrays or just arrays for short are mutable lists of the same type and follow a similar  $\cdot$  arrays syntax as lists. Arrays can be stated as  $sequence\ expressions$ ,  $\cdot$  sequence\ expressions

```
Listing 11.48 Arrays with a sequence expression.

[|[<expr>{; <expr>}]|]
```

and examples are [|1; 2; 3; 4; 5|], which is an array of integers, [|"This"; "is"; "an"; "array"|], which is an array of strings, [|(fun  $x \rightarrow x$ ); (fun  $x \rightarrow x*x$ )|], which is an array of anonymous functions, and [||], which is an empty array. Arrays may also be given as ranges,

```
Listing 11.49 Arrays with a range expressions.
 [|<expr> .. <expr> [.. <expr>]|]
```

but arrays of range expressions must be of <expr> integers, floats, or characters. Examples are ·range expressions [|1 .. 5|], [|-3.0 .. 2.0|], and [|'a' .. 'z'|]. Range expressions may include a step size, thus, [|1 .. 2 .. 10|] evaluates to [|1; 3; 5; 7; 9|].

The array type is defined using the array keyword or alternatively the "[]" lexeme. Like strings and lists, arrays may be indexed using the ".[]" notation. Arrays cannot be resized, but are mutable as ..[] shown in Listing 11.50.

```
Listing 11.50 arrayReassign.fsx:
Arrays are mutable in spite the missing
                                            keyword.
let square (a : int array) =
  for i = 0 to a.Length - 1 do
    a.[i] <- a.[i] * a.[i]
let A = [| 1; 2; 3; 4; 5 |]
printfn "%A" A
square A
printfn "%A" A
$ fsharpc --nologo arrayReassign.fsx && mono arrayReassign.exe
[|1; 2; 3; 4; 5|]
 [|1; 4; 9; 16; 25|]
```

Notice that in spite the missing mutable keyword, the function square still had the side-effect of · side-effect squaring alle entries in A. F# implements arrays as chunks of memory and indexes arrays via adresse arithmetic. I.e., element i in an array, whose first element is in memory addresse  $\alpha$  and whose elements fill  $\beta$  addresses each is found at addresse  $\alpha + i\beta$ . Hence, indexing has computational complexity of  $\mathcal{O}(1)$ , but appending and prepending values to arrays and array concatenation requires copying the new and existing values to a fresh area in memory and thus has computational complexity  $\mathcal{O}(n)$ , where n is the total number of elements. Thus, indexing arrays is fast, but cons and concatenation is slow Advice and should be avoided.

Arrays support *slicing*, that is, indexing an array with a range results in a copy of array with values · slicing corresponding to the range. This is demonstrated in Listing 11.51.

³Jon: Add a figure illustrating adress indexing.

# Listing 11.51 arraySlicing.fsx: Examples of array slicing. Compare with Listing 11.18 and Listing 5.27. let arr = [|'a' .. 'g'|] printfn "%A" arr.[0] printfn "%A" arr.[3] printfn "%A" arr.[3..] printfn "%A" arr.[..3] printfn "%A" arr.[1..3] printfn "%A" arr.[*] \$ fsharpc --nologo arraySlicing.fsx && mono arraySlicing.exe 'a' 'd' [|'d'; 'e'; 'f'; 'g'|] [|'a'; 'b'; 'c'; 'd'|] [|'b'; 'c'; 'd'|] [|'a'; 'b'; 'c'; 'd'; 'e'; 'f'; 'g'|]

As illustrated, the missing start or end index implies from the first or to the last element.

Arrays have explicit operator support for appending and concatenation, instead the Array namespace includes an Array.append function, as shown in Listing 11.52.

```
Listing 11.52 arrayAppend.fsx:
Two arrays are appended with Array.append.

1 let a = [|1; 2;|]
2 let b = [|3; 4; 5|]
3 let c = Array.append a b
4 printfn "%A, %A, %A" a b c

1 $ fsharpc --nologo arrayAppend.fsx && mono arrayAppend.exe
2 [|1; 2|], [|3; 4; 5|], [|1; 2; 3; 4; 5|]
```

Arrays are reference types, meaning that identifiers are references and thus suffers from aliasing, as  $\cdot$  reference types illustrated in Listing 11.53.

```
Listing 11.53 arrayAliasing.fsx:
Arrays are reference types and suffers from aliasing.

let a = [|1; 2; 3|];
let b = a
a.[0] <- 0
printfn "a = %A, b = %A" a b;;

fsharpc --nologo arrayAliasing.fsx && mono arrayAliasing.exe
a = [|0; 2; 3|], b = [|0; 2; 3|]
```

#### 11.3.1 Array properties and methods

Arrays supports a number of properties and methods, i.e., values and functions that are attached to each array and access using the "." notation, some of which are:

Clone(): Returns a copy of the array.

```
Listing 11.54: Clone

| Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone | Clone
```

Length: Returns the number of elements in the array.

#### 11.3.2 Array module

There are quite a number of built-in procedures for arrays in the  $\mathtt{Array}$  module, some of which are summarized below.

Array.append: 'T [] -> 'T []. Creates an array that contains the elements of one array followed by the elements of another array.

```
Listing 11.56: Array.append

1 > Array.append [|1; 2;|] [|3; 4; 5|];;
2 val it : int [] = [|1; 2; 3; 4; 5|]
```

Array.compareWith: ('T -> 'T -> int) -> 'T [] -> int. Compares two arrays using the given comparison function, element by element.

⁴Jon: rewrite description

Array.concat: seq<'T []> -> 'T []. Creates an array that contains the elements of each of the supplied sequence of arrays.

```
Listing 11.58: Array.concat

| > Array.concat [[|1; 2; 3|]; [|4; 5|]; [|6; 7; 8|]];;
| val it : int [] = [|1; 2; 3; 4; 5; 6; 7; 8|]
```

Array.contains: . Evaluates to true if the given element is in the input array.

```
Listing 11.59: Array.contains

1 > Array.contains 3 [|1; 2; 3|];;
2 val it : bool = true
```

Array.copy: 'T [] -> 'T []. Creates an array that contains the elements of the supplied array.

```
Listing 11.60: Array.copy

1 > let a = [|1; 2; 3|]
2 - let b = Array.copy a;;
3 val a : int [] = [|1; 2; 3|]
4 val b : int [] = [|1; 2; 3|]
```

Array.create: int -> 'T -> 'T []. Creates an array whose elements are initiallized the supplied value.

```
Listing 11.61: Array.create

1 > Array.create 4 3.14;;
2 val it : float [] = [|3.14; 3.14; 3.14; 3.14|]
```

Array.empty: 'T []. Returns an empty array of the given type.

```
Listing 11.62: Array.empty

1 > let a : int [] = Array.empty;;
2 val a : int [] = [||]
```

Array.exists: ('T  $\rightarrow$  bool)  $\rightarrow$  'T []  $\rightarrow$  bool. Tests whether any element of an array satisfies the supplied predicate.

```
Listing 11.63: Array.exists

1 > let odd x = (x % 2 = 1) in Array.exists odd [|0 .. 2 .. 4|];;
2 val it : bool = false
```

Array.fill: 'T [] -> int -> int -> 'T -> unit. Fills a range of elements of an array with the supplied value.

# Listing 11.64: Array.fill 1 > let arr = Array.zeroCreate 10; 2 - Array.fill arr 2 5 2;; 3 val arr : int [] = [|0; 0; 2; 2; 2; 2; 0; 0; 0|] 4 val it : unit = ()

Array.filter: ('T -> bool) -> 'T [] -> 'T []. Returns a collection that contains only the elements of the supplied array for which the supplied condition returns true.

```
Listing 11.65: Array.filter

1 > let odd x = (x % 2 = 1) in Array.filter odd [|0 .. 9|];;
2 val it : int [] = [|1; 3; 5; 7; 9|]
```

Array.find: ('T -> bool) -> 'T [] -> 'T. Returns the first element for which the supplied function returns true. Raises System.Collections.Generic.KeyNotFoundException

```
Listing 11.66: Array.find

1 > let odd x = (x % 2 = 1) in Array.find odd [|0 .. 9|];;
2 val it : int = 1
```

Array.findIndex: ('T -> bool) -> 'T [] -> int. Returns the index of the first element in an array that satisfies the supplied condition. Raises System.Collections.Generic.KeyNotFoundException if none of the elements satisfy the condition.

```
Listing 11.67: Array.findIndex

1 > let isK x = (x = 'k') in Array.findIndex isK [|'a' .. 'z'|];;
2 val it : int = 10
```

Array.fold: ('State -> 'T -> 'State) -> 'State -> 'T [] -> 'State. Applies a function to each element of an array, threading an accumulator argument through the computation. If the input function is f and the array elements are i0...iN, this function computes f (...(f s i0)...) iN.

```
Listing 11.68: Array.fold

| > let addSquares acc elm = acc + elm*elm
| - Array.fold addSquares 0 [|0 .. 9|];;
| val addSquares : acc:int -> elm:int -> int
| val it : int = 285
```

Array.foldBack: ('T -> 'State -> 'State) -> 'T [] -> 'State -> 'State. Applies a function to each element of an array, threading an accumulator argument through the computation. If the input function is f and the array elements are i0...iN, this function computes f i0 (...(f iN s)).

```
Listing 11.69: Array.foldBack

1 > let addSquares elm acc = acc + elm*elm
2 - Array.foldBack addSquares [|0 .. 9|] 0;;
3 val addSquares : elm:int -> acc:int -> int
4 val it : int = 285
```

Array.forall: ('T -> bool) -> 'T [] -> bool. Tests whether all elements of an array satisfy the supplied condition.

```
Listing 11.70: Array.forall

1 > let odd x = (x % 2 = 1) in Array.forall odd [|0 .. 9|];;

2 val it : bool = false
```

Array.get: 'T [] -> int -> 'T. Gets an element from an array.

```
Listing 11.71: Array.get

1 > Array.get [|1; 2; 3|] 2;;
2 val it : int = 3
```

Array.init: int -> (int -> 'T) -> 'T []. Uses a supplied function to create an array of the supplied dimension.

Array.isEmpty: 'T [] -> bool. Tests whether an array has any elements.

```
Listing 11.73: Array.isEmpty

Array.isEmpty [||];;

val it : bool = true
```

Array.iter: ('T -> unit) -> 'T [] -> unit. Applies the supplied function to each element of an array.

```
Listing 11.74: Array.iter

1 > let prt x = printfn "%A " x in Array.iter prt [|0; 1; 2|];;
2 0
3 1
4 2
5 val it : unit = ()
```

Array.length: 'T [] -> int. Returns the length of an array. The System.Array.Length property does the same thing.

```
Listing 11.75: Array.length

1 > let a = [|1; 2; 3|] in a.Length;;
2 val it : int = 3
```

Array.map: ('T -> 'U) -> 'T [] -> 'U []. Creates an array whose elements are the results of applying the supplied function to each of the elements of a supplied array.

```
Listing 11.76: Array.map

| > let square x = x*x in Array.map square [|0 .. 9|];;
| val it : int [] = [|0; 1; 4; 9; 16; 25; 36; 49; 64; 81|]
```

Array.ofList: 'T list -> 'T []. Creates an array from the supplied list.

```
Listing 11.77: Array.ofList

1 > Array.ofList [1; 2; 3];;
2 val it : int [] = [|1; 2; 3|]
```

Array.rev: 'T [] -> 'T []. Reverses the order of the elements in a supplied array.

```
Listing 11.78: Array.rev

1 > Array.rev [|1; 2; 3|];;
2 val it : int [] = [|3; 2; 1|]
```

Array.set: 'T [] -> int -> 'T -> unit. Sets an element of an array.

```
Listing 11.79: Array.set

1 > let arr = [|1; 2; 3|]
2 - Array.set arr 2 10
3 - printfn "%A" arr;;
4 [|1; 2; 10|]
5 val arr : int [] = [|1; 2; 10|]
6 val it : unit = ()
```

Array.sort: 'T[] -> 'T []. Sorts the elements of an array and returns a new array. Operators.compare is used to compare the elements.

```
Listing 11.80: Array.sort

1 > Array.sort [|3; 1; 2|];;
2 val it : int [] = [|1; 2; 3|]
```

Array.sub: 'T [] -> int -> int -> 'T []. Creates an array that contains the supplied subrange, which is specified by starting index and length.

```
Listing 11.81: Array.sub

| Array.sub [|0..9|] 2 5;;
| val it : int [] = [|2; 3; 4; 5; 6|]
```

Array.toList: 'T [] -> 'T list. Converts the supplied array to a list.

```
Listing 11.82: Array.toList

| > Array.toList [|1; 2; 3|];;
| val it : int list = [1; 2; 3]
```

Array.unzip: ('T1 * 'T2) [] -> 'T1 [] * 'T2 []. Splits an array of tuple pairs into a tuple of two arrays.

```
Listing 11.83: Array.unzip

| Array.unzip [|(1, 'a'); (2, 'b'); (3, 'c')|];;
| val it : int [] * char [] = ([|1; 2; 3|], [|'a'; 'b'; 'c'|])
```

Array.zip: 'T1 [] -> 'T2 [] -> ('T1 * 'T2) []. Combines three arrays into an array of tuples that have three elements. The three arrays must have equal lengths; otherwise, System.ArgumentException is raised.

```
Listing 11.84: Array.zip

1 > Array.zip [|1; 2; 3|] [|'a'; 'b'; 'c'|];;
2 val it : (int * char) [] = [|(1, 'a'); (2, 'b'); (3, 'c')|]
```

# 11.4 Multidimensional arrays

Multidimensional arrays can be created as arrays of arrays (of arrays . . . ). These are known as jagged · multidimensional arrays, since there is no inherent guarantee that all sub-arrays are of the same size. E.g., the example in Listing 11.85 is a jagged array of increasing width.

# Listing 11.85 arrayJagged.fsx: An array of arrays. When row lengths are of non-equal elements, then it is a Jagged array. let arr = [|[|1|]; [|1; 2|]; [|1; 2; 3|]|] for row in arr do for elm in row do printf "%A " elm printf "\n" \$ fsharpc --nologo arrayJagged.fsx && mono arrayJagged.exe 1 1 2 1 2 3

Indexing arrays of arrays is done sequentially, in the sense that in the above example, the number of outer arrays is a. Length, a. [i] is the i'th array, the length of the i'th array is a. [i]. Length, and the j'th element of the i'th array is thus a. [i]. [j]. Often 2 dimensional rectangular arrays are used, which can be implemented as a jagged array as shown in Listing 11.86.

```
Listing 11.86 arrayJaggedSquare.fsx:
A rectangular array.
let pownArray (arr : int array array) p =
  for i = 1 to arr.Length - 1 do
    for j = 1 to arr.[i].Length - 1 do
      arr.[i].[j] <- pown arr.[i].[j] p
let printArrayOfArrays (arr : int array array) =
  for row in arr do
    for elm in row do
      printf "%3d " elm
    printf "\n"
let A = [|[|1 ... 4|]; [|1 ... 2 ... 7|]; [|1 ... 3 ... 10|]|]
pownArray A 2
printArrayOfArrays A
$ fsharpc --nologo arrayJaggedSquare.fsx && mono arrayJaggedSquare.exe
      2 3 4
  1
          25 49
      9
  1
     16 49 100
```

Notice, the for-in cannot be used in pownArray, e.g.,

```
for row in arr do for elm in row do elm <- pown elm p done done,
```

since the iterator value elm is not mutable even though arr is an array. In fact, square arrays of dimensions 2 to 4 are so common that F# has built-in modules for their support. In the following, we describe Array2D. The workings of Array3D and Array4D are very similar. An example of creating · Array3D the same 2-dimensional array as above but as an Array2D is shown in Listing 11.87.

· Array2D · Array4D

# Listing 11.87 array2D.fsx: Creating a 3 by 4 rectangular arrays of intigers. 1 let arr = Array2D.create 3 4 0 2 for i = 0 to (Array2D.length1 arr) - 1 do 3 for j = 0 to (Array2D.length2 arr) - 1 do 4 arr.[i,j] <- j * Array2D.length1 arr + i 5 printfn "%A" arr 1 \$ fsharpc --nologo array2D.fsx && mono array2D.exe 2 [[0; 3; 6; 9] 3 [1; 4; 7; 10] 4 [2; 5; 8; 11]]

Notice that the indexing uses a slightly different notation [,] and the length functions are also slightly different. The statement A.Length would return the total number of elements in the array, in this case 12. As can be seen, the printf supports direct printing of the 2 dimensional array. Higher dimensional arrays support slicing as shown in Listing 11.88.

```
Listing 11.88 array2DSlicing.fsx:
Examples of Array2D slicing. Compare with Listing 11.87.
let arr = Array2D.create 3 4 0
for i = 0 to (Array2D.length1 arr) - 1 do
  for j = 0 to (Array2D.length2 arr) - 1 do
     arr.[i,j] \leftarrow j * Array2D.length1 arr + i
printfn "%A" arr.[2,3]
printfn "%A" arr.[1..,3..]
printfn "%A" arr.[..1,*]
printfn "%A" arr.[1,*]
printfn "%A" arr.[1..1,*]
$ fsharpc --nologo array2DSlicing.fsx && mono array2DSlicing.exe
[[10]
 [11]]
[[0; 3; 6; 9]
 [1; 4; 7; 10]]
 [|1; 4; 7; 10|]
 [[1; 4; 7; 10]]
```

Note that in almost all cases, slicing produces a sub rectangular 2 dimensional array except for arr. [1,*], which is an array, as can be seen by the single "[". In contrast, A. [1..1,*] is an Array2D. Note also, that printfn typesets 2 dimensional arrays as [[ ... ]] and not [|[| ... |]|], which can cause confusion with lists of lists. ⁵

Multidimensional arrays have the same properties and methods as arrays, see Section 11.3.1.

 $^{^5}$ Jon: Array2D.ToString produces [[ ... ]] and not [|[| ... |]|], which can cause confusion.

#### 11.4.1 Array2D module

There are quite a number of built-in procedures for arrays in the  $\tt Array2D$  namespace, some of which are summarized below.

copy: 'T [,] -> 'T [,]. Creates a new array whose elements are the same as the input array.

create: int -> int -> 'T -> 'T [,]. Creates an array whose elements are all initially the given
value.

```
Listing 11.90: Array2D.create

1 > Array2D.create 2 3 3.14;;
2 val it : float [,] = [[3.14; 3.14; 3.14]]
3 [3.14; 3.14; 3.14]]
```

get: 'T [,] -> int -> int -> 'T. Fetches an element from a 2D array. You can also use the syntax
array.[index1,index2].

```
Listing 11.91: Array2D.get

| > let arr = Array2D.init 3 4 (fun i j -> i + 10 * j) |
|- Array2D.get arr 1 2;
| val arr : int [,] = [[0; 10; 20; 30] |
| [1; 11; 21; 31] |
| [2; 12; 22; 32]]
| val it : int = 21
```

init: int -> int -> (int -> int -> 'T) -> 'T [,]. Creates an array given the dimensions and a generator function to compute the elements.

iter: ('T -> unit) -> 'T [,] -> unit. Applies the given function to each element of the array.

⁶Jon: rewrite description

# 

length1: 'T [,] -> int. Returns the length of an array in the first dimension.

```
Listing 11.94: Array2D.length1

1 > let arr = Array2D.create 2 3 0.0 in Array2D.length1 arr;;
2 val it : int = 2
```

length2: 'T [,] -> int. Returns the length of an array in the second dimension.

```
Listing 11.95: Array2D.forall length2

1 > let arr = Array2D.create 2 3 0.0 in Array2D.length2 arr;;
2 val it : int = 3
```

map: ('T -> 'U) -> 'T [,] -> 'U [,]. Creates a new array whose elements are the results of applying the given function to each of the elements of the array.

set: 'T [,] -> int -> int -> 'T -> unit. Sets the value of an element in an array. You can also
use the syntax array.[index1,index2] <- value.</pre>

# 12 The imperative programming paradigm

Imperative programming is a paradigm for programming states. In imperative programming, the focus is on how a problem is to be solved as a list of statements that affects states. In F# states are mutable and immutable values, and they are affected by functions and procedures. An imperative program is typically identified as using

· Imperative programming

 $\cdot$  statements

 $\cdot$  states

#### mutable values

Mutable values are holders of state, they may change over time, and thus have a dynamic scope.

· mutable values

#### Procedures

Procedures are functions that returns "()", instead of functions that transform data. They are the embodiment of side-effects.

 $\cdot$  procedures

#### Side-effects

Side-effects are changes of state that are not reflected in the arguments and return values of a function. The printf is an example of a procedure that uses side-effects to communicate with the terminal.

 $\cdot$  side-effects

· for

·while

#### Loops

The for- and while-loops typically uses an iteration value to update some state, e.g., for-loops are often used to iterate through a list and summarize its content.

In contrast, mono state or stateless programs as functional programming can be seen as a subset of imperative programming and is discussed in Chapter 17. Object oriented programming is an extension of imperative programming, where statements and states are grouped into classes. For a discussion on object oriented programming, see Chapter 22.

· functional programming

· Object oriented programming

Imperative programs are like Turing machines, a theoretical machine introduced by Alan Turing in 1936 [10]. Almost all computer hardware is designed for *machine code*, which is a common term used for many low-level computer programming language, and almost all machine languages follow the imperative programming paradigm.

 $\cdot$  machine code

A prototypical example is a baking recipe, e.g., to make a loaf of bread do the following:

- 1. Mix yeast with water
- 2. Stir in salt, oil, and flour
- 3. Knead until the dough has a smooth surface
- 4. Let the dough rise until it has double size
- 5. Shape dough into a loaf
- 6. Let the loaf rise until double size

7. Bake in oven until the bread is golden brown

Each line in this example consists of one or more statements that are to be executed, and while executing them states such as size of the dough, color of the bread changes. Some execution will halt execution until certain conditions of these states are fulfilled, e.g., the bread will not be put into the oven for baking before it has risen sufficiently.

# 12.1 Imperative design

Programming is the act of solving a problem by writing a program to be executed on a computer. And imperative programming focusses on states. To solve a problem, you could work through the following list of actions

- 1. Understand the problem. As Pólya described it, see Chapter 2, the first step in any solution is to understand the problem. A good trick to check, whether you understand the problem is to briefly describe it in your own words.
- 2. Identify the main values, variables, functions, and procedures needed. If the list of procedures is large, then you most likely should organize them in modules. It is also useful to start in a coarse to fine manner.
- 3. For each function and procedure, write a precise description of what it should do. This can conveniently be performed as an in-code comment for the procedure using the F# XML documentation standard.
- 4. Make mockup functions and procedures using the intended types, but don't necessarily compute anything sensible. Run through examples in your mind, using this mockup program to identify any obvious oversights.
- 5. Write a suite of unit-tests that tests the basic requirements for your code. The unit tests should be runnable with your mockup code. Writing unit-tests will also allow you to evaluate the usefulness of the code pieces as seen from and application point of view.
- 6. Replace the mockup functions in a prioritized order, i.e., write the must-have code before you write the nice-to-have code, while regularly running your unit-tests to keep track on your progress.
- 7. Evaluate the code in relation to the desired goal, and reiterate earlier actions as needed until the task has been sufficiently completed.
- 8. Complete your documentation both in-code and outside to ensure that the intended user has sufficient knowledge to effectively use your program, and to ensure that you or a fellow programmer will be able to maintain and extend the program in the future.

# 13 | Recursion

Recursion is a central concept in F# and used to control flow in loops without the for and while constructions. Figure 13.1 illustrates the concept of an infinite loop with recursion.

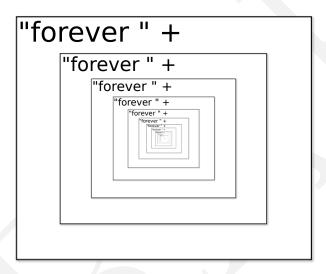


Figure 13.1: An infinitely long string of "forever forever forever...", conceptually calculated by let rec forever () = "fsharp " + (forever ()).

## 13.1 Recursive functions

A recursive function is a function, which calls itself, and the syntax for defining recursive functions is  $\cdot$  recursive function an extension of that for regular functions:

```
Listing 13.1 Syntax for defining one or more mutually dependent recursive functions.

1 let rec <ident> = <expr> {and <ident> = <expr>} [in] <expr>
```

From a compiler point of view, the *rec* is necessary, since the function is used before the compiler has completed its analysis. If two functions are mutually recursive, then they must be defined jointly using the *and* keyword.

• and

An example of a recursive function that counts from 1 to 10 similarly to Listing 8.5 is given in Listing 13.2.

```
Listing 13.2 countRecursive.fsx:

Counting to 10 using recursion.

let rec prt a b =
    if a > b then
        printf "\n"
    else
        printf "%d " a
        prt (a + 1) b

prt 1 10

standard for the first process of the first process
```

Here the prt function calls itself repeatedly, such that the first call is prt 1 10, which calls prt 2 10, and so on until the last call prt 11 10. Each time prt is called, new bindings named a and b are made to new values. This is illustrated in Figure 13.2. The old values are no longer accessible as indicated by subscript in the figure. E.g., in prt₃ the scope has access to a₃ but not a₂ and a₁. Thus, in this program, process is similar to a for loop, where the counter is a and in each loop its value is reduced.

The structure of the function is typical for recursive functions. They very often following pattern.

```
Listing 13.3 Recursive functions consists of a stopping criterium, a stopping expression, and a recursive step.

let rec f a =
if <stopping condition>
then <stopping step>
else <recursion step>
```

The match - with are also very common conditional structures. In Listing 13.2 a > b is the stopping · match condition, printfn "\n" is stopping step, and printfn "\%d " a; prt (a + 1) b is the recursion · with step.

stopping step.

matchwithstopping condition

· stopping step · recursion step

#### 13.2 The call stack and tail recursion

Fibonacci's sequence of numbers is a recursive sequence of numbers with relations to the Golden ratio and structures in biology. Fibonacci's sequence is the sequence of numbers  $1, 1, 2, 3, 5, 8, 13, \ldots$  The sequence starts with 1, 1 and the next number is recursively given as the sum of the two previous. A direct implementation of this is given in Listing 8.7.

```
$ fsharpc countRecursive.fsx && mono countRecursive.exe
prt 1 10
   prt_1: a_1= 1, b_1= 10
   1 > 10: 🗡
      printf "1 "
     prt 2 10
         prt_2: a_2 = 2, b_2 = 10
         2 > 10: 🗡
           printf "2 "
           prt 3 10
               prt_3: a_3= 3, b_3= 10
               3 > 10: X
                 printf "3 "
                 prt 4 10
                     prt 11 10
                         prt_{11}: a_{11}= 1, b_{11}= 10
                         11 > 10 <
                            printf "\\n"
                         ()
               ()
         ()
   ()
()
```

Figure 13.2: Illustration of the recursion used to write the sequence "1 2 3 ... 10" in line 8 in Listing 13.2. Each frame corresponds to a call to prt, where new values overshadow old. All return unit.

Listing 13.4 fibRecursive.fsx: The n'th Fibonacci number using recursive. let rec fib n = if n < 1 then 0 elif n = 1 then1 else fib (n - 1) + fib (n - 2)for i = 0 to 10 do printfn "fib(%d) = %d" i (fib i) \$ fsharpc --nologo fibRecursive.fsx && mono fibRecursive.exe fib(0) = 0fib(1) = 1fib(2) = 1fib(3) = 2fib(4) = 3fib(5) = 5fib(6) = 8fib(7) = 13fib(8) = 21fib(9) = 34fib(10) = 55

Here we extended the sequence to  $0, 1, 1, 2, 3, 5, \ldots$  and starting sequence 0, 1 allowing us to define all fib(n) = 0, n < 1. Thus, our function is defined for all integers, and the irrelevant negative arguments fails gracefully by returning 0. This is a general advice: **make functions that fails gracefully.** 

Advice

A visualization of the calls and the scopes created by fibRecursive is shown in Figure 13.3. The figure illustrates that each recursive step results in two calls to the function, thus creating two new scopes. And it gets worse. Figure 13.4 illustrates the tree of calls for fib 5. Thus a call to the function fib generates a tree of calls that is five levels deep and has fib(5) number of nodes. In general for the program in Listing 13.4, a call to fib(n) produces a tree with fib(n)  $\leq c\alpha^n$  calls to the function for some positive constant c and  $\alpha \geq \frac{1+\sqrt{5}}{2} \sim 1.6^1$ . Each call takes time and requires memory, and we have thus created a slow and somewhat memory intensive function. This is a hugely ineffective implementation of calculating entries into Fibonacci's sequence, since many of the calls are identical. E.g., in Figure 13.4 fib 1 is called five times. Before we examine a faster algorithm, we first need to discuss how F# executes function calls.

When a function is called, then memory is dynamically allocated internally for the function on what is known as the *call stack*. Stacks are used for many things in programming, but typically the call stack is considered special, since it is almost always implicitly part of any program execution. Hence, it is often just referred to as *The Stack*. When a function is called, a new *stack frame* is stacked (pushed) on the call stack including its arguments, local storage such as mutable values, and where execution should return to, when the function is finished. When the function finishes, the stack frame is unstacked (popped) and in its stead the return value of the function is stacked. This return value is then unstacked and used by the caller. After unstacking the return value, the call stack is identical to its state prior to the call. Figure 13.5 shows snapshots of the call stack, when calling fib 5 in Listing 13.4. The call first stacks a frame onto the call stack with everything needed to execute the function body plus a reference to where the return to, when the execution is finished. Then the body

· call stack

 $\cdot$  The Stack  $\cdot$  stack frame

 $^{^1\}mathrm{Jon}$ : https://math.stackexchange.com/questions/674533/prove-upper-bound-big-o-for-fibonaccis-sequence

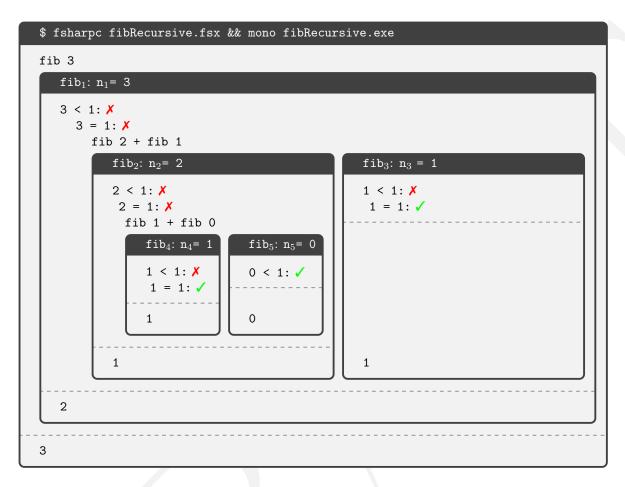


Figure 13.3: Illustration of the recursion used to write the sequence "1 2 3 ... 10" in line 8 in Listing 13.2. Each frame corresponds to a call to fib, where new values overshadow old.

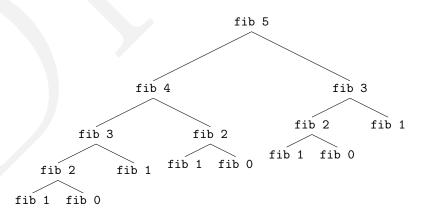


Figure 13.4: The function calls involved in calling fib 5.



Figure 13.5: A call to fib 5 in Listing 13.4 starts a sequence of function calls and stack frames on the call stack.

of fib is executed, which includes calling fib 4 and fib 3 in turn. The call to fib 4 stacks a frame onto the call stack, and its body is executed. Once execution is returned from the call to fib 4, the result of the function is on top of the stack. It is unstacked, saved and the call to fib 3 is treated equally. When the end of fib 5 is reached, its frame is unstacked, and its result is stacked. In this way, the call stack is returned to its original state except for the result of the function, and execution is returned to the point right after the original call to fib 5. Thus, for Listing 13.4  $\mathcal{O}(\alpha^n)$ ,  $\alpha = \frac{1+\sqrt{5}}{2}$  stacking operations are performed for a call to fib n. The  $\mathcal{O}(f(n))$  is the Landau symbol used to denote the order of a function, such that if  $g(n) = \mathcal{O}(f(n))$  then there exists two real numbers M > 0 and a  $n_0$  such that for all  $n \geq n_0$ ,  $|g(n)| \leq M|f(n)|$ . As indicated by the tree in Figure 13.4, the call tree is maximally n high, which corresponds to a maximum of n additional stack frames as compared to the starting point.

· Landau symbol

The implementation of Fibonacci's sequence in Listing 13.4 can be improved to run faster and use less memory. One such algorithm is given in Listing 13.5

```
Listing 13.5 fibRecursiveAlt.fsx:
A fast, recursive implementation of Fibonacci's numbers. Compare with Listing 13.4.

let fib n =
let rec fibPair n pair =
if n < 2 then pair
else fibPair (n - 1) (snd pair, fst pair + snd pair)
if n < 1 then 0
elif n = 1 then 1
else fibPair n (0, 1) |> snd

printfn "fib(10) = %d" (fib 10)

f fsharpc --nologo fibRecursiveAlt.fsx && mono fibRecursiveAlt.exe
fib(10) = 55
```

Calculating the 45th Fibonacci number a Macbook Pro, with a 2.9 Ghz Intel Core i5 using Listing 13.4 takes about 11.2s, while using Listing 13.5 is about 224 times faster and only takes 0.050s. The reason is that fib in Listing 13.5 calculates every number in the sequence once and only once by processing the list recursively, while maintaining the previous two values needed to calculate the next in the sequence. I.e., the function helper transforms the pair (a,b) to (b,a+b) such that, e.g., the 4th and 5th pair (3,5) is transformed into the 5th and the 6th pair (5,8) in the sequence. What complicates the algorithm is that besides the transformation, we must keep track of when to stop, which here is done using a counter variable, that is recursively reduced by 1 until our stopping criterium.

Listing 13.5 also uses much less memory than Listing 13.4, since its recursive call is the last expression

²Jon: Introduction of Landau notation needs to be moved earlier, since it used in Collections chapter.

in the function, and since the return value of two recursive calls to helper is the same as the return value of the last. In fact, the return value of any number of recursive calls to helper is the return value of the last. This structure is called tail-recursion. Compilers can easily optimize the call stack usage for tail recursion, since when in this example helper calls itself, then its frame is no longer needed, and may be replaced by the new helper with the slight modification, that the return point should be to fib and not the end of the previous helper. Once the recursion reaches the stopping criteria, then instead of popping a long list of calls of helper frames, then there is only one, and the return value is equal to the return value of the last call and the return point is to fib. Thus, many stack frames in tail recursion is replaced by one. Hence, prefer tail-recursion whenever possible.

· tail-recursion

Advice

#### Mutual recursive functions 13.3

Listing 13.6 mutually Recursive.fsx:

let rec even x = if x = 0 then true

Functions that recursively call each other are called mutually recursive functions. F# offers the · mutually recursive let - rec - and notation for co-defining mutually recursive functions. As an example, consider the function even: int -> bool, which returns true if its argument is even and false otherwise, and the opposite function odd: int -> bool. A mutually recursive implementation of these functions can be developed from the following relations: even 0 = true, odd 0 = false, and for n > 0, even n = odd (n-1), which implies that for n > 0, odd n = even (n-1):

```
Using mutual recursion to implement even and odd functions.
```

```
else odd (x - 1)
and odd x =
  if x = 0 then false
  else even (x - 1);;
let w = 5;
printfn "%*s %*s %*s" w "i" w "even" w "odd"
for i = 1 to w do
  printfn "%*d %*b %*b" w i w (even i) w (odd i)
$ fsharpc --nologo mutuallyRecursive.fsx && mono mutuallyRecursive.exe
      even
              odd
    1 false
             true
       true false
    3 false
             true
       true false
```

Notice that in the lightweight notation the and must be on the same indentation level as the original let.

Without the and keyword, F# will issue a compile error at the definition of even. However, it is possible to implement mutual recursion by using functions as an argument, e.g.,

Listing 13.7 mutuallyRecursiveAlt.fsx: Mutual recursion without the keyword needs a helper function. let rec evenHelper (notEven: int -> bool) x = if x = 0 then true else notEven (x - 1) let rec odd x = if x = 0 then false else evenHelper odd (x - 1);; let even x = evenHelper odd x let w = 5; printfn "%*s %*s %*s" w "i" w "Even" w "Odd" for i = 1 to w do printfn "%*d %*b %*b" w i w (even i) w (odd i) \$ fsharpc --nologo mutuallyRecursiveAlt.fsx \$ mono mutuallyRecursiveAlt.exe i Even Odd 1 false true true false 3 false true true false 5 false true

But, Listing 13.6 is clearly to be preferred over Listing 13.7.

In the above we used the even and odd function problems to demonstrate mutual recursion. There is, of course, a much simpler solution, which does not use recursion at all:

```
Listing 13.8 parity.fsx:
A better way to test for parity without recursion.

1 let even x = (x % 2 = 0)
2 let odd x = not (even x)
```

which is to be preferred anytime as the solution to the problem. ³

³Jon: Here it would be nice to have an intermezzo, giving examples of how to write a recursive program by thinking the problem has been solved.

# 14 | Programming with types

F# is a strongly typed language, meaning that types are known or inferred at compile time. In the previous chapters, we have used *primitive types* such as float and bool, function types, and compound types implicitly defined by tuples. These types are useful for simple programming tasks, and everything that can be programmed can be accomplished using these types. However, larger programs are often easier to read and write when using more complicated type structures. In this chapter, we will discuss type abbreviations, enumerated types, discriminated unions, records and structs. Class types are discussed in depth in Chapter 20.

· primitive types

### 14.1 Type abbreviations

F# allows for renaming of types, which is called type abbreviation or type aliasing. The syntax is

type abbreviationtype aliasing

```
Listing 14.1 Syntax for type abbreviation.

type <ident> = <aType>
```

where the identifier is a new name, and the type-name is an existing or a compound of existing types. E.g., in Listing 14.2 several type abbreviations are defined.

```
Listing 14.2 typeAbbreviation.fsx:
Defining 3 type abbreviations, two of which are compound types.

1 type size = int
2 type position = float * float
3 type person = string * int
4 type intToFloat = int -> float

5 let sz : size = 3
7 let pos : position = (2.5, -3.2)
8 let pers : person = ("Jon", 50)
9 let conv : intToFloat = fun a -> float a
10 printfn "%A, %A, %A, %A" sz pos pers (conv 2)

1 $ fsharpc --nologo typeAbbreviation.fsx && mono typeAbbreviation.exe
2 3, (2.5, -3.2), ("Jon", 50), 2.0
```

Here we define the abbreviations size, position, person, and intToFloat, and later make bindings

enforcing the usage of these abbreviations.

Type abbreviations are useful as short abbreviations of longer types, and they add semantic content to the program text, thus making programs shorter and easier to read. Type abbreviations allow the programmer to focus on the intended structure at a higher level by, e.g., programming in terms of a type position rather than float * float. Thus, they often result in programs with fewer errors. Type abbreviations also make maintenance easier. For instance, if we at a later stage decide that positions only can have integer values, then we only need to change the definition of the type abbreviation, not every place, a value of type position is used.

#### 14.2 Enumerations

Enumerations or enums for short are types with named values. Names in enums are assigned to a  $\cdot$  enumerations subset of integer or char values. Their syntax is as follows:

```
Listing 14.3 Syntax for enumerations.

type <ident> =
    [ | ] <ident> = <integerOrChar>
    | <ident> = <integerOrChar>
    | <ident> = <integerOrChar>
    | <ident> = <integerOrChar>
    | ...
```

An example of using enumerations is given in Listing 14.4.

```
Listing 14.4 enum.fsx:
An enum type acts as a typed alias to a set of integers or chars.

type medal =
Gold = 0
| Silver = 1
| Bronze = 2

let aMedal = medal.Gold
printfn "%A has value %d" aMedal (int aMedal)

fsharpc --nologo enum.fsx && mono enum.exe
Gold has value 0
```

In the example, we define an enumerated type for medals, which allows us to work with the names rather than the values. Since the values most often are arbitrary, we can program using semantically meaningful names instead. Being able to refer to an underlying integer type allows us to interface with other – typically low-level – programs that requires integers, and to perform arithmetic. E.g., for the medal example, we can typecast the enumerated types to integers and calculate an average medal harvest.

#### Discriminated Unions 14.3

A discriminated union is a union of a set of named cases. These cases can further be of specified types. The syntax for defining a discriminated union is as follows:

```
Listing 14.5 Syntax for type abbreviation.
 [<attributes>]
type <ident> =
   [| ] < ident > [of [ < ident > :] < a Type > [* [ < ident > :] < a Type > ...]]
   | <ident> [of [<ident> :] <aType> [* [<ident> :] <aType> ...]]
```

Discriminated unions are reference types, i.e., their content is stored on The Heap, see Section 6.8 for • The Heap a discussion on reference types. Since they are immutable, there is no risk of side-effects. As reference types, when used as arguments to and returned from a function, then only a reference is passed. This is in contrast to value types, which transport a complete copy of the data structure. Discriminated unions are thus effective for large data structures. However, there is a slight overhead, since working with the content of reference types is indirect through their reference. Discriminated unions can also be represented as structures using the [<Struct>] attribute, in which case they are value types. See Section 14.5 for a discussion on structs.

An example just using the named cases but no further specification of types is given in Listing 14.6.

```
Listing 14.6 discriminated Unions.fsx:
A discriminated union of medals. Compare with Listing 14.4.
 type medal =
   Gold
   | Silver
   | Bronze
let aMedal = medal.Gold
printfn "%A" aMedal
$ fsharpc --nologo discriminatedUnions.fsx
$ mono discriminatedUnions.exe
 Gold
```

Here we define a discriminated union as three named cases signifying three different types of medals. Comparing with the enumerated type in Listing 14.4, we see that the only difference is that the cases of the discriminated unions have no value. A commonly used discriminated union is the option type, · option type see Section 18.2 for more detail.

Discriminated unions may also be used to store data. Where the names in enumerated types are aliases of single values, the names in discriminated unions can hold any value specified at the time of creation. An example is given in Listing 14.7.

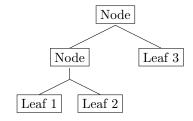


Figure 14.1: The tree with 3 leaves.

```
Listing 14.7 discriminatedUnionsOf.fsx:
A discriminated union using explicit subtypes.

1 type vector =
2    Vec2D of float * float
3    | Vec3D of x : float * y : float * z : float
4    let v2 = Vec2D (1.0, -1.2)
6    let v3 = Vec3D (x = 1.0, z = -1.2, y = 0.9)
7    printfn "%A and %A" v2 v3

1 $ fsharpc --nologo discriminatedUnionsOf.fsx
$ mono discriminatedUnionsOf.exe
Vec2D (1.0,-1.2) and Vec3D (1.0,0.9,-1.2)
```

In this case, we define a discriminated union of two and three-dimensional vectors. Values of these types are created using their names followed by a tuple of their arguments. As can be seen, the arguments may be given field names, and if they are, then the names may be used when creating values of this type. As also demonstrated, the field names can be used to specify the field values in arbitrary order. However, values for all fields must be given.

Discriminated unions can be defined recursively. This feature is demonstrated in Listing 14.8.

In this example we define a tree as depicted in Figure 14.1.

Pattern matching must be used in order to define functions on values of discriminated union. E.g., in

Listing 14.9 we define a function that traverses a tree and prints the content of the nodes.¹

```
Listing 14.9 discriminatedUnionPatternMatching.fsx:
A discriminated union modelling binary trees.

1 type Tree = Leaf of int | Node of Tree * Tree
2 let rec traverse (t : Tree) : string =
3 match t with
4 Leaf(v) -> string v
5 | Node(left, right) -> (traverse left) + ", " + (traverse right)

6 let tree = Node (Node (Leaf 1, Leaf 2), Leaf 3)
8 printfn "%A: %s" tree (traverse tree)

1 $ fsharpc --nologo discriminatedUnionPatternMatching.fsx
2 $ mono discriminatedUnionPatternMatching.exe
Node (Node (Leaf 1, Leaf 2), Leaf 3): 1, 2, 3
```

Discriminated unions are very powerful and can often be used instead of class hierarchies. Class hierarchies are discussed in Section 21.1.

# 14.4 Records

A record is a compound of named values, and a record type is defined as follows:

```
Listing 14.10 Syntax for defining record types.

[ <attributes> ]
type <ident> = {
        [ mutable ] <label1> : <type1>
        [ mutable ] <label2> : <type2>
        ...
}
```

Records are collections of named variables and values of varied type. They are reference types, and thus their content is stored on *The Heap*, see Section 6.8 for a discussion on reference types. Records can also be *struct records* using the [<Struct>] attribute, in which case they are value types. See Section 14.5 for a discussion on structs. An example of using records is given in Listing 14.11. The values of individual members of a record is obtained using the "." notation

· The Heap · struct records

٠.

¹Jon: Example uses pattern matching, which has yet to be introduced.

# Listing 14.11 records.fsx: A record is defined for holding information about a person. type person = { name : string age : int height : float } let author = {name = "Jon"; age = 50; height = 1.75} printfn "%A\nname = %s" author author.name fsharpc --nologo records.fsx && mono records.exe {name = "Jon"; age = 50; height = 1.75;} name = Jon

The examples illustrates a how record type is defined to store varied data about a person, and how a value is created by a record expression defining its field values.

If two record types are defined with the same label set, then the later dominates the former, and the compiler will at a binding infer that later. This is demonstrated in Listing 14.12.

```
Listing 14.12 recordsDominance.fsx:
Redefined types dominates old record types, but earlier definitions are still accessible
using explicit or implicit specification for bindings.
type person = { name : string; age : int; height : float }
type teacher = { name : string; age : int; height : float }
let lecturer = {name = "Jon"; age = 50; height = 1.75}
printfn "%A : %A" lecturer (lecturer.GetType())
let author : person = {name = "Jon"; age = 50; height = 1.75}
printfn "%A : %A" author (author.GetType())
let father = {person.name = "Jon"; age = 50; height = 1.75}
printfn "%A : %A" author (author.GetType())
$ fsharpc --nologo recordsDominance.fsx && mono recordsDominance.exe
{name = "Jon";}
 age = 50;
 height = 1.75;} : RecordsDominance+teacher
{name = "Jon";}
 age = 50;
 height = 1.75;} : RecordsDominance+person
{name = "Jon";
 age = 50;
 height = 1.75;} : RecordsDominance+person
```

In the example, two identical record types are defined, and we use the built-in GetType() method to inspect the type of bindings. We see that lecturer is of RecordsDominance+teacher type, since teacher dominates the identical author type definition. However, we may enforce the person type by either specifying it for the name as in let author: person = ... or by fully or partially

specifying it in the record expression following the "=" sign. In both cases, they are therefore of RecordsDominance+author type. The built-in GetType() method is inherited from the base class for all types, see Chapter 20 for a discussion on classes and inheritance.

Note that when creating a record, you must supply a value to all fields, and you cannot refer to other fields of the same record, e.g., {name = "Jon"; age = height * 3; height = 1.75} is illegal.

Since records are per default reference types, binding creates aliases not copies. This matters for mutable members, in which case when copying, we must explicitly create a new record with the old data. Copying can be done either by using referencing to the individual members of the source or using the short-hand with notation. This is demonstrated in Listing 14.13.

·with

```
Listing 14.13 recordCopy.fsx:
Bindings are references. To copy and not make an alias, explicit copying must be
performed.
type person = {
  name : string;
  mutable age : int;
}
let author = {name = "Jon"; age = 50}
let authorAlias = author
let authorCopy = {name = author.name; age = author.age}
let authorCopyAlt = {author with name = "Noj"}
author.age <- 51
printfn "author : %A" author
printfn "authorAlias : %A" authorAlias
printfn "authorCopy : %A" authorCopy
printfn "authorCopyAlt : %A" authorCopyAlt
$ fsharpc --nologo recordCopy.fsx && mono recordCopy.exe
author : {name = "Jon";
 age = 51;}
authorAlias : {name = "Jon";
 age = 51;}
authorCopy : {name = "Jon";
 age = 50;
authorCopyAlt : {name = "Noj";
  age = 50;
```

Here age is defined as a mutable value, and can be changed using the usual "<-" assignment operator. The example demonstrates two different ways to create records. Note that when the mutable value author.age is changed in line 10, then authorAlias also changes, since it is an alias of author, but neither authorCopy nor authorCopyAlt changes, since they are copies. As illustrated, copying using with allows for easy copying and partial updates of another record value.

### 14.5Structures

Structures or structs for short have much in common with records. They specify a compound type · structures with named fields, but they are value types, and they allow for some customization of what is to happen when a value of its type is created. Since they are value types, then they are best used for small amount of data. The syntax for defining struct types are:

# Listing 14.14 Syntax for type abbreviation. [ <attributes> ] [ <Struct>] type <ident> = ual [ mutable ] <label1> : <type1> ual [ mutable ] <label2> : <type2> ... [new (<arg1>, <arg2>, ...) = {<label1> = <arg1>; <label1> = <arg2>; ...} new (<arg1>, <arg2>, ...) = {<label1> = <arg1>; <label1> = <arg2>; ...} ...

The syntax makes use of the *val* and *new* keywords. Keyword *val* like *let* binds a name to a value, but unlike *let* the value is always the type's default value. The *new* keyword denotes the function used to fill values into the fields at time of creation. This function is called the *constructor*. No *let* nor do bindings are allowed in structure definitions. Fields are accessed using the "." notation. An example is given in Listing 14.15.

```
Listing 14.15 struct.fsx:

Defining a struct type and creating a value of it.

[<Struct>]

type position =

val x : float

val y : float

new (a : float, b : float) = {x = a; y = b}

let p = position (3.0, 4.2)

printfn "%A: x = %A, y = %A" p p.x p.y

fsharpc --nologo struct.fsx && mono struct.exe

Struct+position: x = 3.0, y = 4.2
```

Structs are small versions of classes and allows, e.g., for overloading of the **new** constructor and for · overload overriding of the inherited *ToString()* function. This is demonstrated in Listing 14.16. · override · ToString()

# Listing 14.16 structOverloadNOverride.fsx: Overloading the constructor and overriding the default ToString() function. [<Struct>] type position = val x : float val y : float new (a : float, b : float) = $\{x = a; y = b\}$ new (a : int, b : int) = {x = float a; y = float b} override this.ToString() = "(" + (string this.x) + ", " + (string this.y) + ")" let pFloat = position (3.0, 4.2) let pInt = position (3, 4) printfn "%A and %A" pFloat pInt \$ fsharpc --nologo structOverloadNOverride.fsx \$ mono structOverloadNOverride.exe (3, 4.2) and (3, 4)

We defer further discussion of these concepts to Chapter 20.

The use of structs are generally discouraged, and instead it is recommended to use enums, records, and discriminated unions possibly with the [<Struct>] attribute for the last two in order to make them value types.

# 14.6 Variable types

An advanced topic in F# is variable types. There are three different versions of variable types in F#: runtime resolved, which has the syntax '<ident>, anonymous, which are written as "_", and statically resolved, which have the syntax ^<ident>. Variable types are particularly useful for functions that work for many types. An example of a generic function and its use is given in Listing 14.17.

```
Listing 14.17 variableType.fsx:
A function apply with runtime resolved types.

let apply (f : 'a -> 'a -> 'a) (x : 'a) (y : 'a) : 'a = f x y
let intPlus (x : int) (y : int) : int = x + y
let floatPlus (x : float) (y : float) : float = x + y

printfn "%A %A" (apply intPlus 1 2) (apply floatPlus 1.0 2.0)

$ fsharpc --nologo variableType.fsx && mono variableType.exe
3 3.0
```

In this example, the function apply has runtime resolved variable type, and it accepts three parameters f, x, and y. The function will work as long as the parameters for f is a function of two parameters of identical type, and x and y are values of the same type. Thus, in the printfn statement, we are able to use apply for both an integer and a float variant.

· runtime resolved variable type

· variable types

- $\cdot$ anonymous variable type
- ٠. –
- · statically resolved variable type

The example in Listing 14.17 illustrates a very complicated way to add two numbers. And the "+" operator works for both types out of the box, so why not something simpler like relying on the F# type inference system by not explicitly specifying types as attempted in Listing 14.18.

# Listing 14.18 variableTypeError.fsx: Even though the "+" operator is defined for both integers and floats, the type inference is static and infers plus: int -> int. let plus x y = x + yprintfn "%A %A" (plus 1 2) (plus 1.0 2.0) \$ fsharpc --nologo variableTypeError.fsx && mono variableTypeError.exe variableTypeError.fsx(3,34): error FS0001: This expression was expected to have type 'int' but here has type 'float' variableTypeError.fsx(3,38): error FS0001: This expression was expected to have type 'int' but here has type 'float'

Unfortunately, the example fails to compile, since the type inference is performed at compile time, and by plus 1 2, it is inferred that plus: int -> int. Hence, calling plus 1.0 2.0 is a type error. Function bindings allow for the use of the *inline* keyword, and adding this successfully reuses the ·inline definition of plus for both types as shown in Listing 14.19.

```
Listing 14.19 variableTypeInline.fsx:
                   forces static and independent inference each place the function
The keyword
is used. Compare to the error case in Listing 14.18.
let inline plus x y = x + y
printfn "%A %A" (plus 1 2) (plus 1.0 2.0)
$ fsharpc --nologo variableTypeInline.fsx && mono variableTypeInline.exe
```

In the example, adding the inline does two things: Firstly, it copies the code to be performed to each place, the function is used, and secondly, it forces statically resolved variable type checking independently in each place. The type annotations inferred as a result of the inline-keyword may be written explicitly as shown in Listing 14.20.

# Listing 14.20 compiletimeVariableType.fsx: Explicitely spelling out of the statically resolved type variables from Listing 14.18. 1 let inline plus (x : ^a) (y : ^a) : ^a when ^a : (static member ( + ) : ^a * ^a -> ^a) = x + y 2 printfn "%A %A" (plus 1 2) (plus 1.0 2.0) 1 \$ fsharpc --nologo compiletimeVariableType.fsx 2 \$ mono compiletimeVariableType.exe 3 3 3.0

The example in Listing 14.20 demonstrates the statically resolved variable type syntax, ^<ident>, as well as the use of type constraints using the keyword when. Type constraints have a rich syntax, but will not be discussed further in this book.² In the example, the type constraint when ^a : (static member ( + ) : ^a * ^a -> ^a) is given using the object oriented properties of the type variable ^a, meaning that the only acceptable type values are those, which have a member function (+) taking a tuple and giving a value all of identical type, and which where the type can be inferred at compile time. See Chapter 20 for details on member functions.

· type constraints
· when

The use of inline is useful, when generating generic functions and still profiting from static type checking. However, explicit copying of functions is often something better left to the compiler to optimize over. An alternative seems to be using runtime resolved variable types with the '<ident> syntax. Unfortunately, this is not possible in case of most operators, since they have been defined in the FSharp.Core namespace to be statically resolved variable type. E.g., the "+" operator has type ( + ): ^T1 -> ^T2 -> ^T3 (requires ^T1 with static member (+) and ^T2 with static member (+)).

 $^{^2\}mathrm{Jon}$ : Should I extend on type constraints? Perhaps it is better left for a specialize chapter on generic functions.

# 15 | Pattern matching

Pattern matching is used to transform values and variables into a syntactical structure. The simplest example is value-bindings. The *let*-keyword was introduced in Section 6.1, its extension with pattern ·let matching is given as,

```
Listing 15.1 Syntax for let-expressions with pattern matching.

[[<Literal>]]

let [mutable] <pat> [: <returnType>] = <bodyExpr> [in <expr>]
```

A typical use of this is to extract elements of tuples as demonstrated in Listing 15.2.

```
Listing 15.2 letPattern.fsx:

Patterns in expressions may be used to extract elements of tuples.

let a = (3,4)
let (x,y) = a
let (alsoX,_) = a
printfn "%A: %d %d %d" a x y alsoX

fsharpc --nologo letPattern.fsx && mono letPattern.exe
(3, 4): 3 4 3
```

Here we extract the elements of a pair twice. First by binding to x and y, and second by binding to alsoX while using the wildcard pattern to ignore the second element. Thus, again the wildcard pattern in value-bindings is used to underline a disregarded value.

Another common use of patterns is as alternative to if - then - else expressions particularly when parsing input for a function. Consider the example in Listing 15.3.

```
Listing 15.3 switch.fsx:
                    to print discriminated unions.
Using – –
type Medal = Gold | Silver | Bronze
let statement (m : Medal) : string =
  if m = Gold then "You won"
  elif m = Silver then "You almost won"
  else "Maybe you can win next time"
let m = Silver
printfn "%A : %s" m (statement m)
$ fsharpc --nologo switch.fsx && mono switch.exe
Silver : You almost won
```

In the example, is a discriminated union and a function defined. The function converts each case to a supporting statement using an if-expression. The same can be done with the match - with expression . match and patterns as is demonstrated in Listing 15.4.

·with

```
Listing 15.4 switchPattern.fsx:
                 to print discriminated unions.
Using
type Medal = Gold | Silver | Bronze
let statement (m : Medal) : string =
  match m with
    Gold -> "You won"
     | Silver -> "You almost won"
     | _ -> "Maybe you can win next time"
let m = Silver
printfn "%A : %s" m (statement m)
$ fsharpc --nologo switchPattern.fsx && mono switchPattern.exe
Silver : You almost won
```

Here we used a pattern for the discriminated union cases and a wildcard pattern as default. The lightweight syntax for match-expressions is,

```
Listing 15.5 Syntax for match-expressions.
match <inputExpr> with
 [| ]<pat> [when <guardExpr>] -> <caseExpr>
 | <pat> [when <guardExpr>] -> <caseExpr>
 | <pat> [when <guardExpr>] -> <caseExpr>
```

where <inputExpr> is the input pattern to find matches of, <pat> is a pattern to match with, ·input pattern <guardExpr> is an optional guard expression, and <caseExpr> is the resulting expression. Each set starting with <pat> is called a case. In lightweight syntax, the indentation must be equal to or higher than the indentation of match. All cases must return a value of the same type, and F# report an error, when not the complete domain of the input pattern is covered by cases in match-expressions.

·for

Patterns are also used in a version of *for*-loop expressions, and its lightweight syntax is given as,

```
Listing 15.6 Syntax for for-expressions with pattern matching.
for <pat> in <sourceExpr> do
  <bodyExpr>
```

Typically, <sourceExpr> is a list or an array. An example is given in Listing 15.7.

```
Listing 15.7 for Pattern.fsx:
Patterns may be used in
                          -loops.
for (_,y) in [(1,3); (2,1)] do
  printfn "%d" y
$ fsharpc --nologo forPattern.fsx && mono forPattern.exe
3
1
```

The wildcard pattern is used to disregard the first element in a pair, while iterating over the complete list. It is good practice to use wildcard patterns to emphasize unused values.

Advice

The final expression involving patterns to be discussed is anonymous functions. Patterns for anonymous functions mous functions has the syntax,

```
Listing 15.8 Syntax for anonymous functions with pattern matching.
fun <pat> [<pat> ...] -> <bodyExpr>
```

This is an extension of the syntax discussed in Section 6.2. A typical use for patterns in *fun*-expressions • fun is shown in Listing 15.9.

```
Listing 15.9 funPattern.fsx:
Patterns may be used in -expressions.
let f = fun _ -> "hello"
printfn "%s" (f 3)
$ fsharpc --nologo funPattern.fsx && mono funPattern.exe
hello
```

Here we use an anonymous function expression and bind it to f. The expression has one argument of any type, which it ignores using the wildcard pattern. Some limitations apply to the patterns allowed in fun-expressions. The wildcard pattern in fun-expressions are often used for mockup functions, where the code requires the said function, but its content has yet to be decided. Thus, mockup functions can be used as loose place-holders, while experimenting with program design.

· mockup functions

Patterns are also used in exceptions to be discussed in Section 18.1, and in conjunction with the

¹Jon: Remove or elaborate.

function-keyword, a keyword we discourage in this book. We will now demonstrate a list of important patterns in F#.

# 15.1 Wildcard pattern

A wildcard pattern is denoted "_" and matches anything, see e.g., Listing 15.10.

· wildcard pattern

```
Listing 15.10 wildcardPattern.fsx:
Constant patterns matches to constants.

1 let whatEver (x : int) : string =
2 match x with
3 - -> "If you say so"
4 printfn "%s" (whatEver 42)

1 $ fsharpc --nologo wildcardPattern.fsx && mono wildcardPattern.exe
2 If you say so
```

In this example, anything matches the wildcard pattern, so all cases are covered and the function always returns the same sentence. This is rarely a useful structure on its own, since this could be replaced by a value binding or by a function ignoring its input. However, wildcard patterns are extremely useful, since they act as the final else in if-expressions.

# 15.2 Constant and literal patterns

A constant pattern matches any input pattern with constants, see e.g., Listing 15.11.

 $\cdot$  constant pattern

```
Listing 15.11 constPattern.fsx:
Constant patterns matches to constants.

type Medal = Gold | Silver | Bronze
let intToMedal (x : int) : Medal =

match x with
0 -> Gold
| 1 -> Silver
| _ -> Bronze

printfn "%A" (intToMedal 0)

fsharpc --nologo constPattern.fsx && mono constPattern.exe
Gold
```

In this example, the input pattern are queried for a match with 0 and 1 or the wildcard pattern. Any simple literal type constants may be used in the constant pattern such as 8, 23y, 1010u, 1.2, "hello world", 'c', and , false. Here we also use the wildcard pattern. Notice, matching is performed in a lazy manner and stops for the first matching case from the top. Thus, although the wildcard pattern

matches everything, its case expression is only executed if none of the previous patterns matches the input.

Constants can also be pre-bound by the [<Literal>] attribute for value-bindings. This is demonstrated in Listing 15.12.

```
Listing 15.12 literalPattern.fsx:
A variant of constant patterns are literal patterns.

[<Literal>]
let TheAnswer = 42
let whatIsTheQuestion (x : int) : string =
match x with
TheAnswer -> "We will need to build a bigger machine..."
| _ -> "Don't know that either"

printfn "%A" (whatIsTheQuestion 42)

$ fsharpc --nologo literalPattern.fsx && mono literalPattern.exe
"We will need to build a bigger machine..."
```

The attributed is used to identify the value-binding **TheAnswer** to be used as if it were a simple literal type. Literal patterns must be either uppercase or module prefixed identifiers.

# 15.3 Variable patterns

A variable pattern is a single lower-case letter identifier. Variable pattern identifiers are assigned the variable pattern value and type of the input pattern. Combinations of constant and variable patters are also allowed together with records and arrays. This is demonstrated in Listing 15.13.

```
Listing 15.13 variablePattern.fsx:

Variable patterns are useful for extracting and naming fields etc.

1 let (name, age) = ("Jon", 50)
2 let getAgeString (age : int) : string =
3 match age with
4 0 -> "newborn"
5 | 1 -> "1 year old"
6 | n -> (string n) + " years old"
7 printfn "%s is %s" name (getAgeString age)

1 $ fsharpc --nologo variablePattern.fsx && mono variablePattern.exe
2 Jon is 50 years old
```

In this example, the use of the value identifier n has the function of a named wildcard pattern. Hence, the case could as well have been | _ -> (string age) + "years old", since age is already defined in this scope. However, variable patterns syntactically act as an argument to an anonymous function, and thus act to isolate the dependencies. They are also very useful together with guards, see Section 15.4.

# 15.4 Guards

A guard is a pattern used together with match-expressions including the when-keyword, as shown in · guard Listing 15.5.

```
Listing 15.14 guardPattern.fsx:

Guard expressions can be used with other patterns to restrict matches.

1 let getAgeString (age : int) : string =
2 match age with
3 n when n < 1 -> "infant"
4 | n when n < 13 -> "child"
5 | n when n < 20 -> "teen"
6 | _ -> "adult"

7 printfn "A person aged %d is a/an %s" 50 (getAgeString 50)

1 $ fsharpc --nologo guardPattern.fsx && mono guardPattern.exe
2 A person aged 50 is a/an adult
```

Here guards are used to iteratively carve out subset of integers to assign different strings to each set. The guard expression in <pat> when <guardExpr> -> <caseExpr> is any expression evaluating to a Boolean, and the case expression is only executed for the matching case.

# 15.5 List patterns

Lists have a concatenation pattern associated with them. The "::" cons-operator is used to to match the head and the rest of a list, and "[]" is used to match an empty list, which is also sometimes called the nil-case. This is very useful, when recursively processing lists as shown in Listing 15.15

• []

```
Listing 15.15 listPattern.fsx:
Recursively parsing a list using list patterns.

let rec sumList (lst : int list) : int =
match lst with
n :: rest -> n + (sumList rest)
| [] -> 0

let rec sumThree (lst : int list) : int =
match lst with
[a; b; c] -> a + b + c
| _ -> sumList lst

let aList = [1; 2; 3]
printfn "The sum of %A is %d, %d" aList (sumList aList) (sumThree aList)

$ fsharpc --nologo listPattern.fsx && mono listPattern.exe
The sum of [1; 2; 3] is 6, 6
```

In the example, the function sumList uses the cons operator to match the head of the list with n and the tail with rest. The pattern n :: tail also matches 3 :: [], and in that case tail would be assigned the value []. When lst is empty, then it matches with "[]". List patterns can also be matched explicitly named elements as demonstrated in the sumThree function. The elements to be matched can be any mix of constants and variables.

# 15.6 Array, record, and discriminated union patterns

Array, record, and discriminated union patterns are direct extensions on constant, variable, and wild-card patterns. Listing 15.16 gives examples of array patterns.

- $\cdot$ array pattern
- · record pattern
- · discriminated union patterns

```
Listing 15.16 arrayPattern.fsx:

Using variable patterns to match on size and content of arrays.

1 let arrayToString (x : int []) : string =

match x with

[|1;_;_|] -> "3 elements, first of is a one"

| [|x;1;_|] -> "3 elements, first is " + (string x) + "Second is one"

| x -> "A general array"

6 printfn "%s" (arrayToString [|1; 1; 1|])

printfn "%s" (arrayToString [|3; 1; 1|])

printfn "%s" (arrayToString [|1|])

1 $ fsharpc --nologo arrayPattern.fsx && mono arrayPattern.exe

3 elements, first of is a one

3 elements, first is 3Second is one

4 A general array
```

In the function arrayToString the first case matches arrays of 3 elements, where the first is the integer 1, the second case matches arrays of 3 elements, where the second is a 1 and names the first x, and the final case matches all arrays and works as a default match case. As demonstrated, the cases are treated from first to last, and only the expression of the first case that matches is executed.

For record pattern, we use the field names to specify matching criteria. This is demonstrated in Listing 15.17.

# Listing 15.17 recordPattern.fsx: Variable patterns for records to match on field values. 1 type Address = {street : string; zip : int; country : string} 2 let contact : Address = { 3 street = "Universitetsparken 1"; 4 zip = 2100; 5 country = "Denmark"} 6 let getZip (adr : Address) : int = 7 match adr with 8 {street = _; zip = z; country = _} -> z 9 printfn "The zip-code is: %d" (getZip contact) 1 \$ fsharpc --nologo recordPattern.fsx && mono recordPattern.exe 2 The zip-code is: 2100

Here, the record type Address is created, and in the function getZip, a variable pattern z is created for naming zip values, and the remaining fields are ignored. Since the fields are named, the pattern match needs not mention the ignored fields, and the example match is equivalent to {zip = z} -> z. The curly brackets are required for record patterns.

Discriminated union patterns are similar. For discriminated unions with arguments, the arguments can be match as constants, variables, or wildcards. A demonstration is given in Listing 15.18.

In the project-function, three dimensional vectors are projected to two dimensions by removing the third element. Two dimensional vectors are unchanged. The example uses the wildcard pattern to emphasize, that the third element of three dimensional vectors is ignored. Named arguments can also be matched, in which case ";" is used to delimit the fields in the match instead of ",".

### 15.7Disjunctive and conjunctive patterns

Patterns may be combined disjunctively using the "/" lexeme and conjunctively using the "8" lexeme. Disjunctive patterns combine as fall-through as illustrated in Listing 15.19.

```
Listing 15.19 disjunctivePattern.fsx:
Patterns can be combined logically as 'or' syntax structures.
let wovel (c : char) : bool =
  match c with
     'a' | 'e' | 'i' | 'o' | 'u' | 'y' -> true
     | _ -> false
String.iter (fun c -> printf "%A " (wovel c)) "abcdefg"
$ fsharpc --nologo disjunctivePattern.fsx && mono disjunctivePattern.exe
true false false false true false false
```

Here one or more cases must match for the final case expression, and thus, any vowel results in the same case expression true. All else is matched with the wildcard pattern.

For conjunctive patterns all patterns must match, which is illustrated in Listing 15.20.

 $\cdot$  conjunctive patterns

· disjunctive pattern

```
Listing 15.20 conjunctivePattern.fsx:
Patterns can be combined logically as 'or' syntax structures.
let is11 (v : int * int) : bool =
  match v with
     (1,_) & (_,1) -> true
     | _ -> false
printfn "%A" (List.map is11 [(0,0); (0,1); (1,0); (1,1)])
$ fsharpc --nologo conjunctivePattern.fsx && mono conjunctivePattern.exe
 [false; false; false; true]
```

In this case, we separately check the elements of a pair for the constant value 1, and return true only when both elements are 1. In many cases, conjunctive patters can be replaced by more elegant matches, e.g., using tuples, and in the above example a single case (1,1) -> true would have been simpler. Nevertheless, conjunctive patterns are useful together with active patterns, to be discussed below.

### Active Pattern 15.8

The concept of patterns is extendable to functions. Such functions are called active patterns, and active patterns patterns comes in two flavors: regular and option types. The active pattern cases are constructed as function bindings, but using a special notation. They all take the pattern input as last argument, and may take further preceding arguments. The syntax for active patterns is one of,

# Listing 15.21 Syntax for binding active patterns to expressions. let (|<caseName>|[_| ]) [ <arg> [<arg> ... ]] <inputArgument> = <expr> let (|<caseName>|<caseName>|...|<caseName>|) <inputArgumetn> = <expr>

When using the (|<caseName>|_|]) variants, then the active pattern function must return an option type. The multi-case variant (|<caseName>|<caseName>|...|<caseName>|) must return a Fsharp.Core.Choice type. All other variants can return any type. There are no restrictions on arguments <arg>, and <inputArgumetn> is the input pattern to be matched. Notice in particular that the multi-case variant only takes one argument and cannot be combined with the option-type syntax. Below we will demonstrate how the various patterns are used by example.

The single case, (|<caseName>|]) matches all, and is useful for extracting information from complex types, as demonstrated in Listing 15.22.

```
Listing 15.22 activePattern.fsx:
Single case active pattern for deconstructing complex types.
type vec = {x : float; y : float}
let (|Cartesian|) (v : vec) = (v.x, v.y)
let (|Polar|) (v : vec) = (sqrt(v.x*v.x + v.y * v.y), atan2 v.y v.x)
let printCartesian (p : vec) : unit =
    match p with
       Cartesian (x, y) -> printfn "%A:\n Cartesian (%A, %A)" p x y
let printPolar (p : vec) : unit =
    match p with
       Polar (a, d) -> printfn "%A:\n Cartesian (%A, %A)" p a d
let v = \{x = 2.0; y = 3.0\}
printCartesian v
printPolar v
$ fsharpc --nologo activePattern.fsx && mono activePattern.exe
{x = 2.0;}
 y = 3.0;:
 Cartesian (2.0, 3.0)
{x = 2.0;}
 y = 3.0;:
  Cartesian (3.605551275, 0.9827937232)
```

Here we define a record to represent two-dimensional vectors and two different single case active patterns. Note that in the binding of the active pattern functions in line 2 and 3, the argument is the input expression match <inputExpr> with ..., see Listing 15.5. However, the argument for the cases in line 6 and 9 are names bound to the output of the active pattern function.

Both Cartesian and Polar matches a vector record, but they dismantle the contents differently. For an alternative solution using Class types, see Section 20.1.

More complicated behavior is obtainable by supplying additional arguments to the single case. This is demonstrated in Listing 15.23.

# Listing 15.23 activeArgumentsPattern.fsx: All but the multi-case active pattern may take additional arguments. type vec = {x : float; y : float} let (|Polar|) (o : vec) (v : vec) = let x = v.x - o.xlet y = v.y - o.y(sqrt(x*x + y * y), atan2 y x)let printPolar (o : vec) (p : vec) : unit = match p with Polar o (a, d) -> printfn "%A:\n Cartesian (%A, %A)" p a d let $v = \{x = 2.0; y = 3.0\}$ let offset = $\{x = 1.0; y = 1.0\}$ printPolar offset v \$ fsharpc --nologo activeArgumentsPattern.fsx \$ mono activeArgumentsPattern.exe ${x = 2.0;}$ y = 3.0;: Cartesian (2.236067977, 1.107148718)

Here we supply an offset, which should be subtracted prior to calculating lengths and angles. Notice in line 8, that the argument is given prior to the result binding.

Active pattern functions return option types are called  $partial\ pattern\ functions$ . The option type  $\cdot$  partial pattern allows for specifying mismatches as illustrated in Listing 15.24.

In the example, we use the (|<caseName>|_|]) variant to indicate, that the active pattern returns an option type. Nevertheless, the result binding res in line 6 uses the underlying value of Some. And in contrast to the two previous examples of single case patterns, the value None results in a mismatch. Thus in this case, if the denominator is 0.0, then Div res does not match but the wildcard pattern does.

Multicase active patterns work similarly to discriminated unions without arguments.² An example is · multicase active given in Listing 15.25. patterns

```
Listing 15.25 activeMultiCasePattern.fsx:
Multi-case active patterns have a syntactical structure similar to discriminated
unions.
let (|Gold|Silver|Bronze|) inp =
  if inp = 0 then Gold
   elif inp = 1 then Silver
   else Bronze
let intToMedal (i : int) =
     match i with
       Gold -> printfn "%d: Its gold!" i
       | Silver -> printfn "%d: Its silver." i
       | Bronze -> printfn "%d: Its no more than bronze." i
List.iter intToMedal [0..3]
$ fsharpc --nologo activeMultiCasePattern.fsx
$ mono activeMultiCasePattern.exe
0: Its gold!
   Its silver.
   Its no more than bronze.
3: Its no more than bronze.
```

In this example, we define three cases in line 1. The result of the active pattern function must be one of these cases. For the match-expression, the match is based on the output of the active pattern function, hence in line 8, the case expression is executed, when the result of applying the active pattern function to the input expression i is Gold. In this case, a solution based on discriminated unions would probably be clearer.

### Static and dynamic type pattern 15.9

Input patterns can also be matched on type. For static type matching the matching is performed at . static type pattern compile time, and indicated using the ":" lexeme followed by the type name to be matched. Static type :: matching is further used as input to the type inference performed at compile time to infer non-specified types as illustrated in Listing 15.26.

²Jon: This may be too advanced for this book.

# Listing 15.26 staticTypePattern.fsx: Static matching on type binds the type of other values by type inference. let rec sum lst = match 1st with (n : int) :: rest -> n + (sum rest) | [] -> 0 printfn "The sum is %d" (sum [0..3]) \$ fsharpc --nologo staticTypePattern.fsx && mono staticTypePattern.exe The sum is 6

Here the head of the list n in the list pattern is explicitly matched as an integer, and the type inference system thus concludes that 1st must be a list of integers.

In contrast to static type matching, dynamic type matching is performed at runtime, and indicated · dynamic type pattern using the ":?" lexeme followed by a type name. Dynamic type patterns allow for matching generic ::? values at runtime. This is an advanced topic, which is included here for completeness. An example is given in Listing 15.27.

```
Listing 15.27 dynamicTypePattern.fsx:
Static matching on type binds the type of other values by type inference.
let isString (x : obj) : bool =
     match x with
       :? string -> true
       | _ -> false
let a = "hej"
printfn "Is %A a string? %b" a (isString a)
let b = 3
printfn "Is %A a string? %b" b (isString b)
$ fsharpc --nologo dynamicTypePattern.fsx && mono dynamicTypePattern.exe
Is "hej" a string? true
Is 3 a string? false
```

In F# all types are also objects, whose type is denoted obj. Thus, the example uses the generic type when defining the argument to isString, and then dynamic type pattern matching for further processing. See Chapter 20 for more on objects. Dynamic type patterns are often used for analysing exceptions, which is discussed in Section 18.1. While dynamic type patterns are useful, they imply runtime checking, and it is almost always better to prefer compile time than runtime type Advice checking.

# 16 | Higher order functions

A higher order function is a function that takes a function as an argument and/or returns a function. Higher order functions are also sometimes called functionals or functors. F# is a functions-first programming language with strong support for working with functions as values: Functions evaluate as closures, see Section 6.2, which can be passed to and from functions as any other value. An example of a higher order function is List.map, which takes a function and a list and produces a list, demonstrated in Listing 16.1.

 $\cdot$  higher order function

· closures

```
Listing 16.1 higherOrderMap.fsx:
List.map is a higher order function, since it takes a function as argument.

1 let inc x = x + 1
2 let newList = List.map inc [2; 3; 5]
3 printfn "%A" newList

1 $ fsharpc --nologo higherOrderMap.fsx && mono higherOrderMap.exe
2 [3; 4; 6]
```

Here List.map applies the function inc to every element of the list. Anonymous functions are expressions that results in a function, which need not be named. A typical example is to use anonymous functions as arguments to higher order functions such as List.map shown in Listing 16.2.

· anonymous functions

```
Listing 16.2 higherOrderAnonymous.fsx:
An anonymous function is a higher order function used here as an unnamed argument.
Compare with Listing 16.1.

let newList = List.map (fun x -> x + 1) [2; 3; 5]
printfn "%A" newList

$ fsharpc --nologo higherOrderAnonymous.fsx
$ mono higherOrderAnonymous.exe
[3; 4; 6]
```

A very brief version of Listing 16.2 is shown in Listing 16.3.

# Listing 16.3 higherOrderAnonymousBrief.fsx: A compact version of Listing 16.1. 1 printfn "%A" (List.map (fun x -> x + 1) [2; 3; 5]) 1 \$ fsharpc --nologo higherOrderAnonymousBrief.fsx 2 \$ mono higherOrderAnonymousBrief.exe 3 [3; 4; 6]

What was originally three lines in Listing 16.1 as been reduced to a single line in Listing 16.3. While the result is exactly the same, the later is more difficult to read: First the reader has to understand what the anonymous function does on a single argument, then how this applies to the list through list.Map, and finally what printfn does with the result.

Anonymous functions are also useful as return values of functions as shown in Listing 16.4

```
Listing 16.4 higherOrderReturn.fsx:

The procedure inc returns an increment function. Compare with Listing 16.1.

1 let inc n =
2 fun x -> x + n
3 printfn "%A" (List.map (inc 1) [2; 3; 5])

1 $ fsharpc --nologo higherOrderReturn.fsx && mono higherOrderReturn.exe
2 [3; 4; 6]
```

Here the inc function produces a customized incrementation function as argument to List.map: It adds a prespecified number to an integer argument. Note that the closure of this customized function is only produced once, when the arguments for List.map is prepared, and not every time List.map maps the function to the elements of the list. Compare with Listing 16.1.

Piping is another example of a set of higher order function: (<|), (|>), (<||), (||), ·piping (|||>). E.g., the functional equivalent of the right-to-left piping operator takes a value and a function and applies the function to the value as demonstrated in Listing 16.5.

```
Listing 16.5 higherOrderPiping.fsx:

The functional equivalent of the right-to-left piping operator is a higher order function.

1 let inc x = x + 1
2 let aValue = 2
3 let anotherValue = (|>) aValue inc
4 printfn "%d -> %d" aValue anotherValue

1 $ fsharpc --nologo higherOrderPiping.fsx && mono higherOrderPiping.exe
2 -> 3
```

Here the piping operator is used to apply the inc function to aValue. A more elegant way to write

¹Jon: Make piping operators go into index.

this would be aValue |> inc, or even just inc aValue.

# 16.1 Function composition

Piping is a useful shorthand for composing functions where the focus is on the transformation of arguments and results. Using higher order functions, we can forgo the arguments and compose functions as functions directly. This is done with the ">>" and "<<" operators. An example is given in Listing 16.6.

· function composition

```
. <<
```

```
Listing 16.6 higherOrderComposition.fsx:
Functions defined as composition of other functions.

1 let f x = x + 1
2 let g x = x * x
3 let h = f >> g
4 let k = f << g
5 printfn "%d" (g (f 2))
6 printfn "%d" (h 2)
7 printfn "%d" (f (g 2))
8 printfn "%d" (k 2)

1 $ fsharpc --nologo higherOrderComposition.fsx
2 $ mono higherOrderComposition.exe
3 9
4 9
5 5
6 5
```

In the example we see that (f >> g) x gives the same result as g (f x), while (f << g) x gives the same result as f (g x). A memo technique for remembering the order of the application, when using the function composition operators, is that (f >> g) x is the same as x > f > g, i.e., the result of applying f to x is the argument to g. However, there is a clear distinction between the piping and composition operators. The type of the piping operator is

```
(|>) : ('a, 'a -> 'b) -> 'b
```

i.e., the piping operator takes a value of type 'a and a function of type 'a -> 'b and applies the function to the value and produces the value 'b. In contrast, the composition operator has type

```
(>>) : ('a -> 'b, 'b -> 'c) -> ('a -> 'c)
```

i.e., it takes two functions of type  $'a \rightarrow 'b$  and  $'b \rightarrow 'c$  respectively, and produces a new function of type  $a' \rightarrow 'c$ .

# 16.2 Currying

Consider a function f of two generic arguments. It's type in F# will be f: 'a -> 'b -> 'c, meaning that f takes an argument of type 'a and returns a function of type 'b -> 'c. That is, if just one argument is given, then the result is a function, not a value. This is called *partial specification* or

 $\cdot$  partial specification

currying in tribute of Haskell Curry². An example is given in Listing 16.7.

# Listing 16.7 higherOrderCurrying.fsx: Currying: defining a function as a partial specification of another. 1 let mul x y = x*y 2 let timesTwo = mul 2.0 3 printfn "%g" (mul 5.0 3.0) 4 printfn "%g" (timesTwo 3.0) 1 \$ fsharpc --nologo higherOrderCurrying.fsx 2 \$ mono higherOrderCurrying.exe 3 15 4 6

Here, mul 2.0 is a partial application of the function mul x y, where the first argument is fixed, and hence, timesTwo is a function of 1 argument being the second argument of mul. The same can be achieved using tuple arguments, as shown in Listing 16.8.

```
Listing 16.8 higherOrderTuples.fsx:
Partial specification of functions using tuples is less elegant. Compare with Listing 16.7.

let mul (x, y) = x*y
let timesTwo y = mul (2.0, y)
printfn "%g" (mul (5.0, 3.0))
printfn "%g" (timesTwo 3.0)

$ fsharpc --nologo higherOrderTuples.fsx && mono higherOrderTuples.exe
15
6
```

Conversion between multiple and tuple arguments is easily done with higher order functions as demonstrated in Listing 16.9.

```
Listing 16.9: Two functions to convert between two and 2-tuple arguments.

1 > let curry f x y = f (x,y)
2 - let uncurry f (x,y) = f x y;;
3 val curry : f:('a * 'b -> 'c) -> x:'a -> y:'b -> 'c
4 val uncurry : f:('a -> 'b -> 'c) -> x:'a * y:'b -> 'c
```

Conversion between multiple and tuple arguments are useful, when working with higher order functions such as Lst.map. E.g., if let mul (x, y) = x * y as in Listing 16.8, then curry mul has the type  $x:'a \rightarrow y:'b \rightarrow 'c$  as can be seen in Listing 16.9, and thus, is equal to the anonymous function fun  $x y \rightarrow x * y$ . Hence, curry mul 2.0 is equal to fun  $y \rightarrow 2.0 * y$ , since the precedence of function calls is (curry mul) 2.0.

Currying makes elegant programs and is often used in functional programming. Nevertheless, currying

²Haskell Curry (1900–1982) was an American mathematician and logician, who also has a programming language named after him: Haskell.

may lead to lower readability of code, and in generally **currying should be used with care and** Advice **be well documented for proper readability of code.** 

# 17 The functional programming paradigm

Functional programming is a style of programming which performs computations by evaluating functions. Functional programming avoids mutable values and side-effects. It is declarative in nature, e.g., by the use of value- and function-bindings – let-bindings – and avoids statements – do-bindings. Thus, the result of a function in functional programming depends only on its arguments, and therefore functions have no side-effect and are deterministic, such that repeated call to a function with the same arguments always gives the same result. In functional programming, data and functions are clearly separated, and hence data structures are dum as compared to objects in object oriented programming paradigm, see Chapter 22. Functional programs clearly separate behavior from data and subscribes to the view that it is better to have 100 functions operate on one data structure than 10 functions on 10 data structures. Simplifying the data structure has the advantage that it is much easier to communicate data than functions and procedures between programs and environments. The .Net, mono, and java's virtual machine are all examples of attempt to rectify this, however, the argument still holds.

The functional programming paradigm can trace its roots to lambda calculus introduced by Alonzo Church in 1936 [1]. Church designed lambda calculus to discuss computability. Some of the forces of the functional programming paradigm is that it is often easier to prove correctness of code, and since no states are involved, then functional programs are often also much easier to parallelize than other paradigms.

Functional programming has a number of features:

## Pure functions

Functional programming is performed with pure functions. A pure function always returns the same value, when given the same arguments, and it has no side-effects. A function in F# is an example of a pure function. Pure functions can be replaced by their result without changing the meaning of the program. This is known as referential transparency.

# Higher order functions

Functional programming makes use of higher order functions, where functions may be given as arguments and returned as results of a function application. Higher order functions and first-class citizenship are related concepts, where higher order functions are the mathematical description of functions that operator on functions, while a first-class citizen is the computer science term for functions as values. F# implements higher order functions.

# Recursion

Functional programs use recursion instead of for- and while-loops. Recursion can make programs ineffective, but compilers are often designed to optimize tail-recursion calls. Common recursive programming structures are often available as optimized higher order functions such as iter, map, reduce, fold, and foldback. F# has good support for all of these features.

## Immutable states

Functional programs operate on values not on variables. This implies lexicographical scope in contrast to mutable values, which implies dynamic scope.

 $\cdot$  pure function

- · referential transparency
- $\cdot$  higher order function
- · first-class citizenship
- $\cdot$  recursion
- $\cdot$  iter
- $\cdot$  map
- $\cdot$  reduce
- · fold
- $\cdot$  foldback
- $\cdot$ immutable state
- $\cdot$  immutable state
- $\cdot$  strongly typed

# Strongly typed

Functional programs are often strongly typed, meaning that types are set no later than at compile-time. F# does have the ability to perform runtime type assertion, but for most parts it relies on explicit type annotations and type inference at compile-time. The implication is that type errors are caught at compile time instead of at runtime.

# Lazy evaluation

Due to referential transparency, values can be compute any time up until the point, when needed. Hence, they need not be computed at compilation time, which allows for infinite data structures. F# has support for lazy evaluations using the lazy-keyword, sequences using the seq-type, and computation expressions, all of which are advanced topics and not treated in this book.

· lazy evaluation

 $\cdot$  lazy  $\cdot$  seq

Immutable states imply that data structures in functional programming are different than in imperative programming. E.g., in F# lists are immutable, so if an element of a list is to be changed, a new list must be created copying all old values except that which is to be changed. Such an operation is therefore linear in computational complexity. In contrast, arrays are mutable values, and changing a value is done by reference to the value's position and change the value at that location. This has constant computational complexity. While fast, mutable values give dynamic scope, makes reasoning about the correctness of a program harder, since mutable states do not have referential transparency.

Functional programming may be considered a subset of *imperative programming*, in the sense that functional programming does not include the concept of a state, or one may think of functional programming as only having one unchanging state. Functional programming has also a bigger focus on declaring rules for *what* should be solved, and not explicitly listing statements describing *how* these rules should be combined and executed in order to solve a given problem. Functional programming is often found to be less error-prone at runtime making more stable, safer programs, and less open for, e.g., hacking.

imperative programming

# 17.1 Functional design

A key to all good programming designs is encapsulating code into modules. For functional programs, the essence is to consider data and functions as transformations of data. I.e., the basic pattern is a piping sequence,

$$x \mid > f \mid > g \mid > h$$
,

where x is the input data, and f, g, and h are functions that transform the data. Of course, most long programs include lots of control structure implying that we would need junctions in the pipe system, however, piping is a useful memo technique.

In functional programming there are some pitfalls, that you should avoid:

- Creating large data structures, such as a single record containing all data. Since data is immutable, changing a single field in a monstrous record would mean a lot of copying in many parts of your program. Better is to use a range of data structures that express isolated semantic units of your problem.
- Non-tail recursion. Relying on the built-in functions map, fold, etc., is a good start for efficiency.
- Single character identifiers. Since functional programming tends produce small, well-defined functions, there is a tendency to the usage of single character identifiers, e.g., let f x = .... In the very small, this can be defended, but the names used as identifiers can be used to increase the readability of code to yourself or to others. Typically, identifiers are long and informative in the outer most scope, while decreasing in size as you move in.

- Few comments. Since functional programming is very concise, there is a tendency, that we as programmers forget to add sufficient comments to the code, since at the time of writing, the meaning may be very clear and well thought through, but experience shows that this clarity deteriorates fast with time.
- Identifiers that are meaningless clones of each other. Since identifiers cannot be reused except by overshadowing in deeper scopes, there is often a tendency to have family of identifiers like a, a2, newA etc. Better is to use names, that more clearly states the semantic meaning the values, or, if only used as temporary storage, to discard them completely in lieu of piping and function composition. However, the latter most often requires comments describing the transformation being performed.

Thus, a design pattern for functional programs must focus on,

- What is the input data to be processed
- How is the data to be transformed

For large programs, the design principle is often similar to other programming paradigms, which are often visualized graphically as components that take input, interact, and produces results often together with a user. The effect of functional programming is mostly seen in the small, i.e., where a subtask is to be structure functionally.

# 18 Handling Errors and Exceptions

# 18.1 Exceptions

Exceptions are runtime errors, such as division by zero. E.g., attempting integer division by zero halts execution and a long a somewhat cryptic error message is written to screen as illustrated in Listing 18.1.

The error message starts by System.DivideByZeroException: Attempted to divide by zero, followed by a description of which libraries were involved when the error occurred, and finally fsharp informs us that it Stopped due to error. The type System.DivideByZeroException is a built-in exception type, and the built-in integer division operator chooses to raise the exception, when the undefined division by zero is attempted. Many times such errors can be avoided by clever program design. However, this is not always possible or desirable, which is why F# implements exception handling for graceful control.

Exceptions are a basic-type called exn, and F# has a number of built-in, a few of which are listed in Table 18.1.

Exceptions are handled by the try-keyword expressions. We say that an expression may raise or cast an exception, the try-expression may catch and handle the exception by another expression.

Exceptions like in Listing 18.1 may be handled by try-with expressions as demonstrated in Listing 18.2.

 $\cdot$  raising exception

 $\cdot$  casting exceptions

· catching exception · handling exception

-

Attribute	Description
ArgumentException	Arguments provided are invalid.
DivideByZeroException	Division by zero.
NotFiniteNumberException	floating point value is plus or minus infinity, or Not-a-Number
	(NaN).
OverflowException	Arithmetic or casting caused an overflow.
IndexOutOfRangeException	Attempting to access an element of an array using an index which
	is less than zero or equal or greater than the length of the array.

Table 18.1: Some built-in exceptions. The prefix System. has been omitted for brevity.

```
Listing 18.2 exceptionDivByZero.fsx:
A division by zero is caught and a default value is returned.

let div enum denom =
try
enum / denom
with
| :? System.DivideByZeroException -> System.Int32.MaxValue

printfn "3 / 1 = %d" (div 3 1)
printfn "3 / 0 = %d" (div 3 0)

f sharpc --nologo exceptionDivByZero.fsx && mono exceptionDivByZero.exe
3 / 1 = 3
3 / 0 = 2147483647
```

In the example, when the division operator raises the System.DivideByZeroException exception, then try—with catches it and returns the value System.Int32.MaxValue. Division by zero is still an undefined operation, but with the exception system, the program is able to receive a message about this undefined situation and choose an appropriate action.

The try expressions comes in two flavors: try-with and try-finally expressions.

The *try-with* expression has the following syntax,

·try-with

where <testExpr> is an expression, which might raise an exception, <path> is a pattern, and <exprHndln> is the corresponding exception handler. The value of the try-expression is either the value of <testExpr>, if it does not raise an exception, or the value of the exception handler <exprHndln> of the first matching pattern <path> The above is lightweight syntax. Regular syntax omits newlines.

In Listing 18.2 dynamic type matching is used (see Section 15.9) using the ":?" lexeme, i.e., the ·dynamic type pattern pattern matches exceptions at runtime which has the System.DivideByZeroException type. The

exception value may contain furter information and can be accessed if named using the as-keyword · as as demonstrated in Listing 18.4.

```
Listing 18.4 exceptionDivByZeroNamed.fsx:

Exception value is bound to a name. Compare to Listing 18.2.

let div enum denom =
try
enum / denom
with
| :? System.DivideByZeroException as ex ->
printfn "Error: %s" ex.Message
System.Int32.MaxValue

printfn "3 / 1 = %d" (div 3 1)
printfn "3 / 0 = %d" (div 3 0)

fsharpc --nologo exceptionDivByZeroNamed.fsx
mono exceptionDivByZeroNamed.exe
3 / 1 = 3
Error: Attempted to divide by zero.
5 / 0 = 2147483647
```

Here the exception value is bound to the name ex.

All exceptions may be caught as the dynamic type System.Exception, and F# implements a shorthand for catching exceptions and binding its value to a name as demonstrated in

```
Listing 18.5 exceptionDivByZeroShortHand.fsx:
An exception of type System.Exception is bound to a name. Compare to Listing 18.4.

let div enum denom =
try
enum / denom
with
| ex -> printfn "Error: %s" ex.Message; System.Int32.MaxValue

printfn "3 / 1 = %d" (div 3 1)
printfn "3 / 0 = %d" (div 3 0)

fsharpc --nologo exceptionDivByZeroShortHand.fsx
mono exceptionDivByZeroShortHand.exe
3 / 1 = 3
Error: Attempted to divide by zero.
3 / 0 = 2147483647
```

Finally, the short-hand may be guarded with a when-guard as demonstrated in Listing 18.6.

·when

# Listing 18.6 exceptionDivByZeroGuard.fsx: An exception of type System. Exception is bound to a name and guarded. Compare to Listing 18.5. let div enum denom = try enum / denom with | ex when enum = 0 -> 0 | ex -> System.Int32.MaxValue printfn "3 / 1 = %d" (div 3 1) printfn "3 / 0 = %d" (div 3 0) printfn "0 / 0 = %d" (div 0 0) \$ fsharpc --nologo exceptionDivByZeroGuard.fsx \$ mono exceptionDivByZeroGuard.exe 3 / 1 = 33 / 0 = 21474836470 / 0 = 0

The first pattern only matches the System. Exception exception when enum is 0, in which case the exception handler returns 0.

Thus, if you don't care about the type of exception, then you need only use the short-hand pattern matching and name binding demonstrated in Listing 18.5 and Listing 18.6, but if you would like to distinguish between types of exceptions, then you must use explicit type matching and possibly value binding demonstrated in Listing 18.2 and Listing 18.4

The try-finally expression has the following syntax,

· try-finally

```
Listing 18.7 Syntax for the try—finally exception handling.

1 try
2 <testExpr>
3 finally
4 <cleanupExpr>
```

The try-finally expression evaluates the <cleanupExpr> expression following evaluation of the <testExpr> regardless of whether an exception is raised or not as illustrated in Listing 18.8.

# Listing 18.8 exceptionDivByZeroFinally.fsx: The branch is executed regardless of an exception. let div enum denom = printf "Doing division:" printf " %d %d." enum denom enum / denom finally printfn " Division finished." printfn "3 / 1 = %d" (try div 3 1 with ex -> 0) printfn "3 / 0 = %d" (try div 3 0 with ex -> 0) \$ fsharpc --nologo exceptionDivByZeroFinally.fsx \$ mono exceptionDivByZeroFinally.exe Doing division: 3 1. Division finished. 3 / 1 = 3Doing division: 3 0. Division finished. 3 / 0 = 0

Here, the finally branch is evaluated following the evaluation of the test expression regardless of whether the test expression raises an exception or not. However, if an exception is raised in a try-finally expression and there is no outer try-with expression, then execution stops without having evaluated the finally branch.

Exceptions can be raised using the raise-function

 $\cdot$ raise

```
Listing 18.9 Syntax for the raise function that raises exceptions.

raise (<expr>)
```

An example of raising the System.ArgumentException is shown in Listing 18.10

```
Listing 18.10 raiseArgumentException.fsx:
Raising the division by zero with customized message.

1 let div enum denom =
2    if denom = 0 then
3        raise (System.ArgumentException "Error: \"division by 0\"")
4    else
5        enum / denom

6    printfn "3 / 0 = %s" (try (div 3 0 |> string) with ex -> ex.Message)

1    $ fsharpc --nologo raiseArgumentException.fsx
2    $ mono raiseArgumentException.exe
3    3 / 0 = Error: "division by 0"
```

In this example, division by zero is never attempted, instead an exception is raised, which must be handled by the caller. Note that the type of div is int -> int because denom is compared with

an integer in the conditional statement. This contradicts the typical requirements for **if** statements, where every branch has to return the same type. However, any code that explicitly raises exceptions are ignored, and the type is inferred by the remaining branches.

Programs may define new exceptions using the syntax,

```
Listing 18.11 Syntax for defining new exceptions.

1 exception <ident> of <typeId> {* <typeId>}
```

An example of defining a new exception and raising it is given in Listing 18.12.

Here an exception called <code>DontLikeFive</code> is defined, and it is raised in the function <code>picky</code>. The example demonstrates that catching the exception as a <code>System.Exception</code> as in Listing 18.5 the <code>Message</code> property includes information about the exception name but not its argument. To retrieve the argument "5 <code>sucks</code>", we must match the exception with correct exception name as demonstrated in Listing 18.13.

# Listing 18.13 exceptionDefinitionNCatch.fsx: Catching a user-defined exception. exception DontLikeFive of string let picky a = if a = 5 then raise (DontLikeFive "5 sucks") a try printfn "picky %A = %A" 3 (picky 3) printfn "picky %A = %A" 5 (picky 5) with | DontLikeFive msg -> printfn "Exception caught with message: %s" msg \$ fsharpc --nologo exceptionDefinitionNCatch.fsx \$ mono exceptionDefinitionNCatch.exe picky 3 = 3Exception caught with message: 5 sucks

F# includes the *failwith* function to simplify the most common use of exceptions. It is defined as ·failwith failwith: string -> exn and takes a string and raises the built-in System.Exception exception. An example of its use is shown in Listing 18.14.

```
Listing 18.14 exceptionFailwith.fsx:
An exception raised by failwith.

1 if true then failwith "hej"

1 $ fsharpc --nologo exceptionFailwith.fsx && mono exceptionFailwith.exe

2 Unhandled Exception:
System.Exception: hej
at <StartupCode$exceptionFailwith>.$ExceptionFailwith$fsx.main@()
[0x0000b] in <599574c21515099da7450383c2749559>:0

[ERROR] FATAL UNHANDLED EXCEPTION: System.ExceptionFailwith$fsx.main@()
at <StartupCode$exceptionFailwith>.$ExceptionFailwith$fsx.main@()
[0x0000b] in <599574c21515099da7450383c2749559>:0
```

To catch the failwith exception, there are two choices, either use the :? or the Failure pattern. the :? pattern matches types, and we can match with the type of System.Exception as shown in Listing 18.15.

# 

However, this gives annoying warnings, since F# internally is built such that all exception matches the type of System.Exception. Instead it is better to either match using the wildcard pattern as in Listing 18.16,

```
Listing 18.16 exceptionMatchWildcard.fsx:
Catching a failwith exception using the wildcard pattern.

let _ = 
try 
failwith "Arrrrg"
with 
_ -> printfn "So failed"

fsharpc --nologo exceptionMatchWildcard.fsx
mono exceptionMatchWildcard.exe
So failed
```

or use the built-in Failure pattern as in Listing 18.17.

```
Listing 18.17 exceptionFailure.fsx:

Catching a failwith exception using the Failure pattern.

let _ = 
try 
failwith "Arrrrg"

with 
Failure msg -> 
printfn "The castle of %A" msg

fsharpc --nologo exceptionFailure.fsx && mono exceptionFailure.exe
The castle of "Arrrrg"
```

Notice how only the Failure pattern allows for the parsing of the message given to failwith as argument.

Invalid arguments is such a common reason for failures that a built-in function has been supplied in F#. The *invalidArq* takes 2 strings and raises the built-in ArgumentException

·invalidArg

```
Listing 18.18 exceptionInvalidArg.fsx:
An exception raised by invalidArg. Compare with Listing 18.10.

if true then invalidArg "a" "is too much 'a'"

fsharpc --nologo exceptionInvalidArg.fsx
mono exceptionInvalidArg.exe

Unhandled Exception:
System.ArgumentException: is too much 'a'
Parameter name: a

at <StartupCode$exceptionInvalidArg>.$ExceptionInvalidArg$fsx.main@()
[0x0000b] in <599574c911642f55a7450383c9749559>:0

[ERROR] FATAL UNHANDLED EXCEPTION: System.ArgumentException: is too much
'a'
Parameter name: a

at <StartupCode$exceptionInvalidArg>.$ExceptionInvalidArg$fsx.main@()
[0x0000b] in <599574c911642f55a7450383c9749559>:0
```

The invalidArg function raises an System.ArgumentException as shown in Listing 18.19.

The try construction is typically used to gracefully handle exceptions, but there are times, where you may want to pass on the bucket, so to speak, and re-raise the exception. This can be done with the *reraise* as shown in Listing 18.20.

·reraise

### Listing 18.20 exceptionReraise.fsx: Reraising an exception. let _ = try failwith "Arrrrg" with Failure msg -> printfn "The castle of %A" msg reraise() \$ fsharpc --nologo exceptionReraise.fsx && mono exceptionReraise.exe The castle of "Arrrrg" Unhandled Exception: System. Exception: Arrrrg at <StartupCode\$exceptionReraise>.\$ExceptionReraise\$fsx.main@ () [0x00041] in <599574d491e0c9eea7450383d4749559>:0[ERROR] FATAL UNHANDLED EXCEPTION: System.Exception: Arrrrg at <StartupCode\$exceptionReraise>. \$ExceptionReraise\$fsx.main@ () [0x00041] in <599574d491e0c9eea7450383d4749559>:0

The reraise function is only allowed to be the final call in the expression of a with rule.

### 18.2 Option types

At exceptions, it is not always obvious what should be returned. E.g., in the Listing 18.2, the exception is handled gracefully, but the return value is somewhat arbitrarily chosen to be the largest possible integer, which is still far from infinity, which is the correct result. Instead we could use the *option type*. The option type is a wrapper, that can be put around any type, and which extends the type with the special value <code>None</code>. All other values are preceded by the <code>Some</code> identifier. An example of rewriting Listing 18.2 to correctly represent the non-computable value is shown in Listing 18.21.

· option type

- ·None
- ·Some

·IsNone

 $\cdot$  IsSome

·Value

The value of an option type can be extracted by and tested for by its member function, *IsNone*, *IsSome*, and *Value* as illustrated in Listing 18.22.

# Listing 18.22 option.fsx: Simple operations on option types. 1 let a = Some 3; 2 let b = None; 3 printfn "%A %A" a b 4 printfn "%A %b %b" a.Value b.IsSome b.IsNone 1 \$ fsharpc --nologo option.fsx && mono option.exe 2 Some 3 <null> 3 false true

The Value member is not defined for None, thus explicit pattern matching for extracting values Advice from an option type is preferred, e.g., let get (opt : 'a option) (def : 'a) = match opt with Some  $x \to x \mid _ \to def$ . Note also that printf prints the value None as <null>. This author hopes, that future versions of the option type will have better visual representations of the None value.

Functions of option types are defined using the *option*-keyword. E.g., to define a function with explicit  $\cdot$  option type annotation that always returns None, write let f (x : 'a option) = None.

F# includes an extensive Option module. It defines among many other functions Option.bind · Option.bind which implements let bind f opt = match opt with None -> None | Some x -> f x. The function Option.bind is demonstrated in Listing 18.23.

```
Listing 18.23: Option.bind is useful for cascading calculations on option types.

1 > Option.bind (fun x -> Some (2*x)) (Some 3);;
2 val it : int option = Some 6
```

The Option.bind is a useful tool for cascading functions that evaluates to option types.

### 18.3 Programming intermezzo: Sequential division of floats

The following problem illustrates cascading error handling:

### Problem 18.1

Given a list of floats such as [1.0; 2.0; 3.0], calculate the sequential division 1.0/2.0/3.0.

Sequential division is safe, if the list does not contain zero values. However, if any element in the list is zero, then error handling must be performed. An example using failwith is given in Listing 18.24.

# Listing 18.24 seqDiv.fsx: Sequentially dividing a list of numbers. let rec seqDiv acc lst = match lst with | [] -> acc | elm::rest when elm <> 0.0 -> seqDiv (acc/elm) rest | _ -> failwith "Division by zero" try printfn "%A" (seqDiv 1.0 [1.0; 2.0; 3.0]) printfn "%A" (seqDiv 1.0 [1.0; 0.0; 3.0]) with Failure msg -> printfn "%s" msg \$ fsharpc --nologo seqDiv.fsx && mono seqDiv.exe 0.1666666667 Division by zero

In this example, a recursive function is defined which updates an accumulator element, initially set to the neutral value 1.0. Division by zero results in a failwith exception, wherefore we must wrap its use in a try—with expression.

Instead of using exceptions, we may use Option.bind. In order to use Option.bind for a sequence of non-option floats, we will define a division operator, that reverses the order of operands. This is shown in Listing 18.25.

```
Listing 18.25 seqDivOption.fsx:
Sequentially dividing a sequence of numbers using Option.bind. Compare with List-
ing 18.24.
let divideBy denom enum =
  if denom = 0.0 then
     None
  else
     Some (enum/denom)
let success =
  Some 1.0
  |> Option.bind (divideBy 2.0)
  |> Option.bind (divideBy 3.0)
printfn "%A" success
let fail =
  Some 1.0
   |> Option.bind (divideBy 0.0)
  |> Option.bind (divideBy 3.0)
printfn "%A; isNone: %b" fail fail.IsNone
$ fsharpc --nologo seqDivOption.fsx && mono seqDivOption.exe
Some 0.166666667
<null>; isNone: true
```

Here the function divideBy takes two non-option arguments and returns an option type. Thus, Option.bind (divideBy 2.0) (Some 1.0) is equal to Some 0.5, since divideBy 2.0 is a function that divides any float argument by 2.0. Iterating Option.bind (divideBy 3.0) (Some 0.5) we calculate Some 0.1666666667 or Some (1.0/6.0) as expected. In Listing 18.25 this is written as a single let binding using piping. And since Option.bind correctly handles the distinction between Some and None values, such piping sequences correctly handles possible errors as shown in Listing 18.25.

The sequential application can be extended to lists using List.foldBack as demonstrated in Listing 18.26.

```
Listing 18.26 segDivOptionAdv.fsx:
Sequentially dividing a list of numbers using Option.bind and List.foldBack. Compare
with Listing 18.25.
let divideBy denom enum =
  if denom = 0.0 then
     None
   else
     Some (enum/denom)
let divideByOption x acc =
  Option.bind (divideBy x) acc
let success = List.foldBack divideByOption [3.0; 2.0; 1.0] (Some 1.0)
printfn "%A" success
let fail = List.foldBack divideByOption [3.0; 0.0; 1.0] (Some 1.0)
printfn "%A; isNone: %A" fail fail. IsNone
$ fsharpc --nologo seqDivOptionAdv.fsx && mono seqDivOptionAdv.exe
Some 0.166666667
<null>; isNone: true
```

Since List.foldBack processes the list from the right, the list of integers have been reversed. Notice how divideByOption is the function spelled out in each piping step of Listing 18.25.

Exceptions and option type are systems to communicate errors up through a hierarchy of function calls. While exceptions favor imperativ style programming, option types are functional style programming. Exceptions allows for a detailed report of the type of error to the caller, whereas option types only allows for flagging that an error has occurred.

# 19 Working with files

An important part of programming is handling data. A typical source of data are hard-coded bindings and expressions from libraries or the program itself, and the result is often shown on a screen either as text output on the console. This is a good starting point, when learning to program, and one which we have relied heavily upon in this book until now. However, many programs require more: We often need to ask a user to input data via, e.g., typing text on a keyboard, clicking with a mouse, striking a pose in front of a camera. We also often need to load and save data to files, retrieve and deposit information from the internet, and visualize data as graphically, as sounds, or by controlling electrical appliances. Graphical user interfaces will be discussed in Chapter 23, and here we will concentrate on working with the console, with files, and with the general concept of streams.

File and stream input and output are supported via built-in namespaces and classes. For example, the printf family of functions discussed in Section 6.5 is defined in the Printf module of the Fsharp.Core namespace, and it is used to put characters on the stdout stream, i.e., to print on the screen. Likewise, ReadLine discussed in Section 6.6 is defined in the System.Console class, and it fetches characters from the stdin stream, that is, reads the characters the user types on the keyboard until newline is pressed.

A file on a computer is a resource used to store data in and retrieve data from. Files are often associated with a physical device, such as a harddisk, but can also be a virtual representation in memory. Files are durable, such that other programs can access them independently, given certain rules for access. A file has a name, a size, and a type, where the type is related to the basic unit of storage such as characters, bytes, and words, (char, byte, and int32). Often data requires a conversion between the internal format to and from the format stored in the file. E.g., floating point numbers are sometimes converted to a UTF8 string using fprintf in order to store them to file in a human readable form, and interpreted from UTF8 when retrieving them at a later point from file. Files have a low-level structure and representation, which varies from device to device, and the low-level details are less relevant for the use of the file and most often hidden for the user. Basic operations on files are creation, opening, reading from, writing to, closing, and deleting files.

A stream is similar to files in that they are used to store data in and retrieve data from, but streams only allow for handling of data one element at a time like the readout of a thermometer: we can make temperature readings as often as we like, making notes and thus saving a history of temperatures, but we cannot access the future. Hence, streams are in principle without an end, and thus have infinite size, and data from streams are programmed locally by considering the present and previous elements. In contrast, files are finite in size and allow for global operations on all the file's data. Files may be considered a stream, but the opposite is not true.¹

пlе

 $\cdot$  create file

· open file

 $\cdot$  read file

· write file

 $\cdot$  close file

· delete file

 $\cdot$  stream

¹Jon: Maybe add a figure illustrating the difference between files and streams.

### 19.1 Command line arguments

Compiled programs may be started from the console with one or more arguments. E.g., if we have made a program called prog, then arguments may be passed as mono prog arg1 arg2 .... To read the arguments in the program must define a function with the EntryPoint attribute, and this function · EntryPoint must be of type string array -> int.

```
Listing 19.1 Defining an entry point function with arguments from the console.
 [<EntryPoint>]
let <funcIdent> <arg> =
  <bodyExpr>
```

<funcIdent> is the function's name, <arg> is the name of an array of strings, and <bodyExpr> is the function body. Return value 0 implies a successful execution of the program, while non-zero means failure. The entry point function must be in the last file compiled. An example is given in Listing 19.2.

```
Listing 19.2 commandLineArgs.fsx:
Interacting with a user with ReadLine and WriteLine.
[<EntryPoint>]
let main args =
     printfn "Arguments passed to function : %A" args
     0 // Signals that program terminated successfully
```

An example execution with arguments is shown in Listing 19.3.

```
Listing 19.3: An example dialogue of running Listing 19.2.
$ fsharpc --nologo commandLineArgs.fsx
$ mono commandLineArgs.exe Hello World
Arguments passed to function : [|"Hello"; "World"|]
```

In Bash, the return values is called the exit status and can be tested using Bash's if statements as · exit status demonstrated in Listing 19.4.

```
Listing 19.4: Testing return values in Bash when running Listing 19.2.
$ fsharpc --nologo commandLineArgs.fsx
$ if mono commandLineArgs.exe Hello World; then echo "success"; else
   echo "failure"; fi
Arguments passed to function : [|"Hello"; "World"|]
success
```

Also in Bash, the exit status of the last executed program can be accessed using the \$? built-in environment variable. In Windows this same variable is called %errorlevel%.

Stream	Description
stdout	Standard output stream used by printf and printfn.
stderr	Standard error stream used to display warnings and errors by Mono.
stdin	Standard input stream used to read keyboard input.

Table 19.1: Three built-in streams in System.Console.

Function	Description	
Write: string -> unit	Write to the console. E.g.,	
	System.Console.Write "Hello world". Similar	
	to printf.	
WriteLine: string -> unit	As Write but followed by a newline character,	
	e.g., WriteLine "Hello world". Similar to	
	printfn.	
Read: unit -> int	Read the next key from the keyboard blocking	
	execution as long, e.g., Read (). The key pressed	
	is echoed to the screen.	
ReadKey: bool -> System.ConsoleKeyInfo	As Read but returns more information about the	
	key pressed. When given the value true as	
	argument, then the key pressed is not echoed to	
	the screen. E.g., ReadKey true.	
ReadLine unit -> string	Read the next sequence of characters until	
	newline from the keyboard, e.g., ReadLine ().	

Table 19.2: Some functions for interacting with the user through the console in the System.Console class. Prefix "System.Console." is omitted for brevity.

### 19.2 Interacting with the console

From a programming perspective, the console is a stream: A program may send new data to the console, but cannot return to previously sent data and make changes. Likewise, the program may retrieve input from the user, but cannot go back and ask the user to have inputted something else, nor can we peak into the future and retrieve what the user will input in the future. The console uses three built-in streams in System.Console listed in Table 19.1. On the console, the standard output and error streams are displayed as text, and it is typically not possible to see a distinction between them. However, command-line interpreters such as Bash can, and it is possible from the command-line to filter output from programs according to these streams. However, a further discussion on this is outside the scope of this text. In System.Console there are many functions supporting interaction with the console, and the most important ones are shown in Table 19.2. Note that you must supply the empty argument "()" to the Read functions, in order to run most of the functions instead of referring to them as values. A demonstration of the use of Write, WriteLine, and ReadLine is given in Listing 19.5.

# Listing 19.5 userDialogue.fsx: Interacting with a user with ReadLine and WriteLine. The user typed "3.5" and "7.4". System.Console.WriteLine "To perform the multiplication of a and b" System.Console.Write "Enter a: " let a = float (System.Console.ReadLine ()) System.Console.Write "Enter b: " let b = float (System.Console.ReadLine ()) System.Console.WriteLine ("a * b = " + string (a * b)) f sharpc --nologo userDialogue.fsx && mono userDialogue.exe To perform the multiplication of a and b Enter a: 3.5 Enter b: 7.4 a * b = 25.9

The functions Write and WriteLine acts as printfn but without a formatting string. These functions have many overloaded definitions the description of which is outside the scope of this book. For Advice writing to the console, printf is to be preferred.

Often ReadKey is preferred over Read, since the former returns a value of type System. ConsoleKeyInfo, which is a structure with three properties:

Key A System. Console Key enumeration of the key pressed. E.g., the character 'a' is Console Key. A.

KeyChar A unicode representation of the key.

Modifiers A System. Console Modifiers enumeration of modifier keys shift, crtl, and alt.

An example of a dialogue is shown in Listing 19.6.

### Listing 19.6 readKey.fsx:

Reading keys and modifiers. The user press 'a', 'shift-a', and 'crtl-a', and the program was terminated by pressing 'crtl-c'. The 'alt-a' combination does not work on MacOS.

```
open System

printfn "Start typing"
while true do
let key = Console.ReadKey true
let shift =
if key.Modifiers = ConsoleModifiers.Shift then "SHIFT+" else ""
let alt =
if key.Modifiers = ConsoleModifiers.Alt then "ALT+" else ""
let ctrl =
if key.Modifiers = ConsoleModifiers.Control then "CTRL+" else ""
printfn "You pressed: %s%s%s%s" shift alt ctrl (key.Key.ToString ())

$ fsharpc --nologo readKey.fsx && mono readKey.exe
Start typing
You pressed: A
You pressed: SHIFT+A
You pressed: CTRL+A
```

System.IO.File	Description	
Open:	Request the opening of a file on path for reading	
<pre>(path : string) * (mode : FileMode)</pre>	and writing with access mode FileMode, see	
-> FileStream	Table 19.4. Other programs are not allowed to	
	access the file, before this program closes it.	
OpenRead: (path : string)	Request the opening of a file on path for reading.	
-> FileStream	Other programs may read the file regardless of this	
	opening.	
OpenText: (path : string)	Request the opening of an existing UTF8 file on	
-> StreamReader	path for reading. Other programs may read the file	
	regardless of this opening.	
OpenWrite: (path : string)	Request the opening of a file on path for writing	
-> FileStream	with FileMode.OpenOrCreate. Other programs	
	may not access the file, before this program closes it.	
Create: (path : string)	Request the creation of a file on path for reading	
-> FileStream	and writing, overwriting any existing file. Other	
	programs may not access the file, before this	
	program closes it.	
CreateText: (path : string)	Request the creation of an UTF8 file on path for	
-> StreamWriter	reading and writing, overwriting any existing file.	
	Other programs may not access the file, before this	
	program closes it.	

Table 19.3: The family of System.IO.File.Open functions. See Table 19.4 for a description of FileMode, Tables 19.5 and 19.6 for a description of FileStream, Table 19.7 for a description of StreamReader, and Table 19.8 for a description of StreamWriter.

### 19.3 Storing and retrieving data from a file

A file stored on the filesystem has a name, and it must be opened before it can be accessed and closed when finished. Opening files informs the operating system that your program is now going to use the file. While a file is open, the operating system will protect it depending on how the file is opened. E.g., if you are going to write to the file, then this typically implies that no one else may write to the file at the same time, since simultaneous writing to a file may leave the resulting file in an uncertain state. Sometimes the operating system will realize that a file, that was opened by a program, is no longer being used, e.g., since the program is no longer running, but it is good practice always to release reserved files, e.g., by closing them as soon as possible, such that other programs may have access to it. On the other hand, it is typically safe for several programs to read the same file at the same time, but it is still important to close files after their use, such that the operating system can effectively manage the computer's resources. Reserved files are just one of the possible obstacles that you may meet, when attempting to open a file. Other points of failure may be that the file may not exist, your program may not have sufficient rights for accessing it, or the device, where the file is stored, may have unreliable access. Thus, never assume that accessing files always works, but program defensively, e.g., by checking the return status of the file accessing functions and by try constructions.

Advice

Advice

Data in files may have been stored in various ways, e.g., it may contain UTF8 encoded characters or sequences of floating point numbers stored as raw bits in chunks of 64 bits, or it may be a sequence of bytes that are later going to be interpreted as an image in jpeg or tiff format. To aid in retrieving the data, F# has a family of open functions, all residing in the System.IO.File class. These are described in Table 19.3.

For the general Open function, you must also specify how the file is to be opened. This is done with

FileMode	Description		
Append	Open a file and seek to its end, if it exists, or create a new file. Can		
	only be used together with FileAccess.Write. May throw IOException and		
	NotSupportedException exceptions.		
Create	Create a new file, and delete an already existing file. May throw the		
	UnauthorizedAccessException exception.		
CreateNew	Create a new file, but throw the IOException exception, if the file already exists.		
Open	Open an existing file, and System.IO.FileNotFoundException exception is		
	thrown if the file does not exist.		
OpenOrCreate	Open a file, if exists, or create a new file.		
Truncate	Open an existing file and truncate its length to zero. Cannot be used together		
	with FileAccess.Read.		

Table 19.4: File mode values for the System. IO. Open function.

a special set of values described in Table 19.4. An example of how a file is opened and later closed is shown in Listing 19.7.

```
Listing 19.7 openFile.fsx:
Opening and closing a file, in this case the source code of this same file.

let filename = "openFile.fsx"

let reader = 
try
Some (System.IO.File.Open (filename, System.IO.FileMode.Open))
with
- -> None

if reader.IsSome then
printfn "The file %A was successfully opened." filename
reader.Value.Close ()

fsharpc --nologo openFile.fsx && mono openFile.exe
The file "openFile.fsx" was successfully opened.
```

Notice how the example uses the defensive programming style, where the try-expression is used to return the optional datatype, and further processing is made dependent on the success of the opening operation.

In F# the distinction between files and streams are not very clear. F# offers built-in support for accessing files as bytes through the System.IO.FileStream class, and for characters in a particular encoding through the System.IO.TextReader and System.IO.TextWriter.

A successfully opened System.IO.FileStream file, e.g., using System.IO.File.OpenRead from Table 19.3, will result in an FileStream object. From this object we can extract information about the file, such as the permitted operations and more listed in Table 19.5. This information is important in order to restrict the operation that we will perform on the file. Some typical operations are listed in and 19.6. E.g., we may Seek a particular position in the file, but only within the range of legal postions from 0 until the length of the file. Most operating systems do not necessarily write information to files immediately after one of the Write functions, but will often for optimization purposes will often collect information in a buffer that is to be written to a device in batches. However, sometimes is is useful to be able to force the operating system to empty its buffer to the device. This is called *flushing* and can be forced using the Flush function.

flushing

Property	Description	
CanRead	Gets a value indicating whether the current stream supports reading. (Overrides	
	Stream.CanRead.)	
CanSeek	Gets a value indicating whether the current stream supports seeking. (Overrides	
	Stream.CanSeek.)	
CanWrite	Gets a value indicating whether the current stream supports writing. (Overrides	
	Stream.CanWrite.)	
Length	Gets the length in bytes of the stream. (Overrides Stream.Length.)	
Name	Gets the name of the FileStream that was passed to the constructor.	
Position	Gets or sets the current position of this stream. (Overrides Stream.Position.)	

Table 19.5: Some properties of the System.IO.FileStream class.

Method	Description
Close ()	Closes the stream.
Flush ()	Causes any buffered data to be written to the file.
Read byte[] * int * int	Reads a block of bytes from the stream and writes the data in a
	given buffer.
ReadByte ()	Read a byte from the file and advances the read position to the next
	byte.
Seek int * SeekOrigin	Sets the current position of this stream to the given value.
Write byte[] * int * int	Writes a block of bytes to the file stream.
WriteByte byte	Writes a byte to the current position in the file stream.

Table 19.6: Some methods of the System.IO.FileStream class.

Text is typically streamed through the StreamReader and StreamWriter. These may be considered higher order stream processing, since they include an added interpretation of the bits to strings. A StreamReader has methods similar to a FileStream object and a few new properties and methods, such as the EndOfStream property and ReadToEnd method, see Table 19.7. Likewise, a StreamWriter has an added method for automatically flushing following every writing operation. A simple example of opening a text-file and processing it is given in Listing 19.8.

Property/Method	Description	
EndOfStream	Check whether the stream is at its end.	
Close ()	Closes the stream.	
Flush ()	Causes any buffered data to be written to the file.	
Peek ()	Reads the next character, but does not advance the position.	
Read ()	Reads the next character.	
Read char[] * int * int	Reads a block of bytes from the stream and writes the data in a given	
	buffer.	
ReadLine ()	Reads the next line of characters until a newline. Newline is dis-	
	carded.	
ReadToEnd ()	Reads the remaining characters till end-of-file.	

Table 19.7: Some methods of the System. IO. StreamReader class.

Property/Method	Description
AutoFlush : bool	Get or set the auto-flush. If set, then every call to Write will flush the stream.
Close ()	Closes the stream.
Flush ()	Causes any buffered data to be written to the file.
Write 'a	Write a basic type to the file.
WriteLine string	As Write but followed by newline.

Table 19.8: Some methods of the System.IO.StreamWriter class.

Function	Description	
Copy (src : string, dest : string)	Copy a file from src to dest possibly overwriting any	
	existing file.	
Delete string	Delete a file	
Exists string	Check whether the file exists	
Move (from : string, to : string)	Move a file from src to to possibly overwriting any	
	existing file.	

Table 19.9: Some methods of the System.IO.File class.

```
Listing 19.8 readFile.fsx:
An example of opening a text file, and using the StreamReader properties and methods.
let printFile (reader : System.IO.StreamReader) =
  while not(reader.EndOfStream) do
    let line = reader.ReadLine ()
    printfn "%s" line
let filename = "readFile.fsx"
let reader = System.IO.File.OpenText filename
printFile reader
$ fsharpc --nologo readFile.fsx && mono readFile.exe
let printFile (reader : System.IO.StreamReader) =
  while not(reader.EndOfStream) do
    let line = reader.ReadLine ()
    printfn "%s" line
let filename = "readFile.fsx"
let reader = System.IO.File.OpenText filename
printFile reader
```

Here the program reads the source code of itself, and prints it to the console.

### 19.4 Working with files and directories.

F# has support for managing files summarized in the System.IO.File class and summarized in Table 19.9.

In the System.IO.Directory class there are a number of other frequently used functions summarized in Table 19.10.

Function	Description	
CreateDirectory string	Create the directory and all implied sub-	
	directories.	
Delete string	Delete a directory	
Exists string	Check whether the directory exists	
<pre>GetCurrentDirectory ()</pre>	Get working directory of the program	
GetDirectories (path : string)	Get directories in path	
GetFiles (path : string)	Get files in path	
Move (from : string, to : string)	Move a directory and its content from src	
	to to.	
<pre>SetCurrentDirectory : (path : string) -&gt; unit</pre>	Set the current working directory of the	
	program to path.	

Table 19.10: Some methods of the System. IO. Directory class.

Function	Description	
Combine string * string	Combine 2 paths into a new path.	
GetDirectoryName (path: string)	Extract the directory name from path.	
GetExtension (path: string)	Extract the extension from path.	
GetFileName (path: string)	Extract the name and extension from path.	
<pre>GetFileNameWithoutExtension (path : string)</pre>	Extract the name without the extension	
	from path.	
GetFullPath (path : string)	Extract the absolute path from path.	
GetTempFileName ()	Create a uniquely named and empty file on	
	disk and return its full path.	

Table 19.11: Some methods of the System. IO. Path class.

In the System.IO.Path class there are a number of other frequently used functions summarized in Table 19.11.

### 19.5 Reading from the internet

The internet is a global collection of computers that are connected in a network using the internet protocol suite TCP/IP. The internet is commonly used for transport of data such as emails and for offering services such as web pages on the World Wide Web. Web resources are identified by a *Uniform Resource Locator* (*URL*) popularly known as a web page, and an URL contains information about where and how data from the web page is to be obtained. E.g., the URL https://en.wikipedia.org/wiki/F_Sharp_(programming_language), contains 3 pieces of information: https is the protocol to be used to interact with the resource, en.wikipedia.org is the host's name, and wiki/F_Sharp_(programming_language) is the filename.

F#'s System namespace contains functions for accessing web pages as stream as illustrated in Listing 19.9.

- · Uniform Resource Locator
- $\cdot$  URI

### Listing 19.9 webRequest.fsx: Downloading a web page and printing the first few characters. /// Set a url up as a stream let url2Stream url = let uri = System.Uri url let request = System.Net.WebRequest.Create uri let response = request.GetResponse () response.GetResponseStream () /// Read all contents of a web page as a string let readUrl url = let stream = url2Stream url let reader = new System.IO.StreamReader(stream) reader.ReadToEnd () let url = "http://fsharp.org" let a = 40let html = readUrl url printfn "Downloaded %A. First %d characters are: %A" url a html.[0..a] \$ fsharpc --nologo webRequest.fsx && mono webRequest.exe Downloaded "http://fsharp.org". First 40 characters are: "<!DOCTYPE html> <html lang="en"> <head>"

To connect to a URL as a stream, we first need first format the URL string as a Uniform Resource Identifiers (URI), which is a generalization of the URL concept, using the System. Uri function. Then Uniform Resource we must initialize the request by the System.Net.WebRequest function, and the response from the host is obtained by the GetResponse method. Finally, we can access the response as a stream by the · URI GetResponseStream method. In the end, we convert the stream to a StreamReader, such that we can use the methods from Table 19.7 to access the web page. ²

## Identifiers

### 19.6 Programming intermezzo: Ask user for existing file

A typical problem, when working with files, is

### Problem 19.1

Ask the user for the name of an existing file.

Such a dialogue most often requires the program to aid the user, e.g., by telling the user, which files are available, and to check that the filename entered is an existing file. A solution could be,

²Jon: This section could be extended...

### Listing 19.10 filenamedialogue.fsx:

```
let getAFileName () =
let mutable filename = Unchecked.defaultof<string>
let mutable fileExists = false
while not(fileExists) do
System.Console.Write("Enter Filename: ")
filename <- System.Console.ReadLine()
fileExists <- System.IO.File.Exists filename
filename

let listOfFiles = System.IO.Directory.GetFiles "."
printfn "Directory contains: %A" listOfFiles
let filename = getAFileName ()
printfn "You typed: %s" filename
```

# 

Almost all popular operating systems are accessed through a user-friendly graphical user interface (GUI) that is designed to make typical tasks easy to learn to solve. As a computer programmer, you often need to access some of the functionalities of the computer, which, unfortunately, are sometimes complicated by this particular graphical user interface. The console, also called the terminal and the Windows command line, is the right hand of a programmer. The console is a simple program that allows you to complete text commands. Almost all the tasks that can be done with the graphical user interface can be done in the console and vice versa. Using the console, you will benefit from its direct control of the programs we write, and in your education, you will benefit from the fast and raw information you get through the console.

- · graphical user interface
- $\cdot$  GUI
- $\cdot$  console
- $\cdot$  terminal
- · Windows command line

### A.1 The basics

When you open a *directory* or *folder* in your preferred operating system, the directory will have a location in the file system, whether from the console or through the operating system's graphical user interface. The console will almost always be associated with a particular directory or folder in the file system, and it is said that it is the directory that the console is in. The exact structure of file systems varies between Linux, MaxOS X and Windows, but common is that it is a hierarchical structure. This is illustrated in Figure A.1.

· directory

There are many predefined console commands, available in the console, and you can make your own. In the following, we will review the most important commands in the three different operating systems. These are summarized in Table A.1.

### A.2 Windows

In this section we will discuss the commands summarized in Table A.1. Windows 7 and earlier versions: To open the console, press Start->Run in the lower left corner, and then type cmd In the box. In Windows 8 and 10, you right-click on the windows icon, choose Run or equivalent in your local language, and type cmd. Alternatively you can type Windows-key + R. Now you should open a console window with a prompt showing something like Listing A.1.

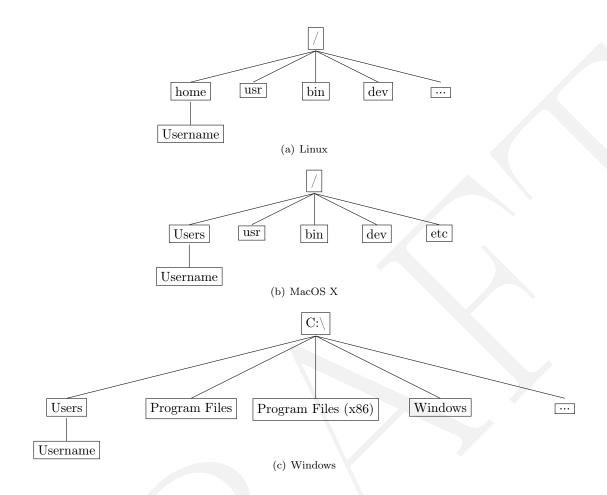


Figure A.1: The top file hierarchy levels of common operating systems.

Windows	MacOS X/Linux	Description
dir	ls	Show content of present direc-
		tory.
cd <dir></dir>	cd <dir></dir>	Change present directory to
		<dir>.</dir>
mkdir <dir></dir>	mkdir <dir></dir>	create directory <dir>.</dir>
rmdir <dir></dir>	rmdir <dir></dir>	delete <dir> (Warning: can-</dir>
		not be reverted).
move <file> <file dir="" or=""></file></file>	mv <file> <file dir="" or=""></file></file>	Move <fil> to <file or<="" td=""></file></fil>
		dir>.
copy <file> <file></file></file>	cp <file> <file></file></file>	Create a new file called <file></file>
		as a copy of <file>.</file>
del <file></file>	rm <file></file>	delete <file> (Warning: can-</file>
		not be reverted).
echo <string or="" variable=""></string>	echo <string or="" variable=""></string>	Write a string or content of a
		variable to screen.

Table A.1: The most important console commands for Windows, MacOS X, and Linux.

· dir

# Listing A.1: The Windows console. 1 Microsoft Windows [Version 6.1.7601] 2 Copyright (c) 2009 Microsoft Corporation. All rights reserved. 3 C:\Users\sporring>

To see which files are in the directory, use dir as shown in Listing A.2.

```
Listing A.2: Directory listing with dir.
C:\Users\sporring>dir
 Volume in drive C has no label.
 Volume Serial Number is 94F0-31BD
 Directory of C:\Users\sporring
30-07-2015 15:23
                      < DTR.>
30-07-2015
            15:23
                      <DIR>
30-07-2015 14:27
                      <DIR>
                                      Contacts
30-07-2015 14:27
                      <DIR>
                                      Desktop
30-07-2015 17:40
                      <DIR>
                                      Documents
30-07-2015 15:11
                      <DIR>
                                      Downloads
30-07-2015 14:28
                      <DIR>
                                      Favorites
30-07-2015 14:27
                      <DIR>
                                      Links
30-07-2015 14:27
                      <DIR>
                                      Music
30-07-2015
            14:27
                      <DIR>
                                      Pictures
30-07-2015
            14:27
                      <DIR>
                                      Saved Games
30-07-2015
            17:27
                      <DIR>
                                      Searches
30-07-2015
            14:27
                      <DIR>
                                      Videos
                                       0 bytes
                0 File(s)
               13 Dir(s) 95.004.622.848 bytes free
C:\Users\sporring>
```

We see that there are no files and thirteen directories (DIR). The columns tell from left to right, the date and time of their creation, the file size or if it is a folder, and the name file or directory name. The first two folders "." and ".." are found in each folder and refers to this folder as well as the one above in the hierarchy. In this case, the folder "." is an alias for C:\Users\tracking and ".." for C:\Users.

Use *cd* to change directory, e.g., to Documents as in Listing A.3.

```
Listing A.3: Change directory with cd.

C:\Users\sporring>cd Documents

C:\Users\sporring\Documents>
```

The directory Documents is that Windows Explorer selects, when you press the Documents short-cut in Explorer. Note that some systems translate default filenames so their names may be given different names in different languages in the graphical user interface as compared to the console.

You can use mkdir to create a new directory called, e.g., myFolder as illustrated in Listing A.4.

 $\cdot$  mkdir

· cd

### Listing A.4: Creating a directory with mkdir. C:\Users\sporring\Documents>mkdir myFolder C:\Users\sporring\Documents>dir Volume in drive C has no label. Volume Serial Number is 94F0-31BD Directory of C:\Users\sporring\Documents 30-07-2015 19:17 <DIR> 30-07-2015 19:17 <DIR> 30-07-2015 19:17 <DIR> myFolder 0 bytes 0 File(s) 3 Dir(s) 94.656.638.976 bytes free C:\Users\sporring\Documents>

By using dir we inspect the result.

Files can be created by, e.g., *echo* and *redirection* as demonstrated in Listing A.5.

· echo · redirection

```
Listing A.5: Creating a file with echo and redirection.
C:\Users\sporring\Documents>echo "Hi" > hi.txt
C:\Users\sporring\Documents>dir
 Volume in drive C has no label.
 Volume Serial Number is 94F0-31BD
 Directory of C:\Users\sporring\Documents
30-07-2015 19:18
                    <DIR>
30-07-2015 19:18
                     <DIR>
30-07-2015 19:17
                     <DIR>
                                  myFolder
30-07-2015 19:18
                                  8 hi.txt
               1 File(s)
                                      8 bytes
               3 Dir(s) 94.656.634.880 bytes free
C:\Users\sporring\Documents>
```

To move the file hi.txt to the directory myFolder use move as shown in Listing A.6.

```
Listing A.6: Move a file with move.

C:\Users\sporring\Documents>move hi.txt myFolder

1 file(s) moved.

C:\Users\sporring\Documents>
```

Finally, use del to delete a file and rmdir to delete a directory as shown in Listing A.7.

·del ·rmdir

 $\cdot$  move

### Listing A.7: Delete files and directories with del and rmdir. C:\Users\sporring\Documents>cd myFolder C:\Users\sporring\Documents\myFolder>del hi.txt C:\Users\sporring\Documents\myFolder>cd .. C:\Users\sporring\Documents>rmdir myFolder C:\Users\sporring\Documents>dir Volume in drive C has no label. Volume Serial Number is 94F0-31BD Directory of C:\Users\sporring\Documents 30-07-2015 19:20 <DIR> 30-07-2015 19:20 <DIR> 0 bytes 0 File(s) 2 Dir(s) 94.651.142.144 bytes free C:\Users\sporring\Documents>

The commands available from the console must be in its search path. The search path can be seen · search path using echo as shown in Listing A.8.

The path can be changed using the Control panel in the graphical user interface. In Windows 7, choose the Control panel, choose System and Security  $\rightarrow$  System  $\rightarrow$  Advanced system settings  $\rightarrow$  Environment Variables. In Windows 10 you can find this window by searching for "Environment" in the Control panel. In the window's System variables box, double-click on Path and add or remove a path from the list. The search path is a list of paths separated by ";". Beware, Windows uses the search path for many different tasks, so remove only paths that you are certain are not used for anything.

A useful feature of the console is that you can use the tab-key to cycle through filenames. E.g., if you write cd followed by a space and tab a couple of times, then the console will suggest you the available directories.

### A.3 MacOS X and Linux

MacOS X (OSX) and Linux are very similar, and both have the option of using bash as console. It ·bash is in the standard console on MacOS X and on many Linux distributions. A summary of the most important bash commands are shown in Table A.1. In MacOS X, you find the console by opening

Finder and navigating to Applications  $\rightarrow$  Utilities -> Terminal. In Linux, the console can be started by typing Ctrl + Alt + T. Some Linux distributions have other key-combinations such as Super + T.

Once opened, the console is shown in a window with content as shown in Listing A.9.

```
Listing A.9: The Windows console.

Last login: Thu Jul 30 11:52:07 on ttys000
FN11194:~ sporring$
```

"FN11194" is the name of the computer, the character  $\sim$  is used as an alias for the user's home directory, and "sporring" is the username for the user presently logged onto the system. Use ls to see  $\cdot ls$  which files are present, as shown in Listing A.10.

```
Listing A.10: Display a directory content with 1s.

1 FN11194:~ sporring$ 1s
2 Applications Documents Library Music Public
3 Desktop Downloads Movies Pictures
4 FN11194:~ sporring$
```

More details about the files are available by using flags to 1s as demonstrated in Listing A.11.

```
Listing A.11: Display extra information about files using flags to 1s.
FN11194:~ sporring$ ls -l
             6 sporring staff
                                 204 Jul 30 14:07 Applications
drwx----+ 32 sporring
                         staff
                                 1088 Jul 30 14:34 Desktop
drwx----+ 76 sporring
                         staff
                                 2584 Jul
                                          2 15:53 Documents
drwx----+ 4 sporring
                         staff
                                 136 Jul 30 14:35 Downloads
drwx----0 63 sporring
                         staff
                                 2142 Jul 30 14:07 Library
drwx----+ 3 sporring
                         staff
                                 102 Jun 29 21:48 Movies
drwx----+ 4 sporring
                         staff
                                 136 Jul
                                          4 17:40 Music
drwx ----+
            3 sporring
                                 102 Jun 29 21:48 Pictures
                         staff
drwxr-xr-x+ 5 sporring
                         staff
                                  170 Jun 29 21:48 Public
FN11194: sporring$
```

The flag -1 means long, and many other flags can be found by querying the built-in manual with man ls. The output is divided into columns, where the left column shows a number of codes: "d" means they are directory followed by three sets of optional "rwx" denoting whether the owner, the associated group of users and anyone can "r" - read, "w" - write, or "x" - execute the files. In this case, only the owner can do any of the three. For directories, "x" means permission to enter. The second column can often be ignored, but shows how many links there are to the file or directory. Then follows the username of the owner, which in this case is sporring. The files are also associated with a group of users, and in this case, they all are associated with the group called staff. Then follows the file or directory size, the date of last change, and the file or directory name. There are always two hidden directories: "." and "..", where "." is an alias for the present directory, and ".." for the directory above. Hidden files will be shown with the -a flag.

Use cd to change to the directory Documents as shown in Listing A.12.

# Listing A.12: Change directory with cd. 1 FN11194:~ sporring\$ cd Documents/ 2 FN11194:Documents sporring\$

Note that some graphical user interfaces translate standard filenames and directories to the local language, such that navigating using the graphical user interface will reveal other files and directories, which, however, are aliases.

You can yourself create a new directory using mkdir as demonstrated in Listing A.13.

·mkdir

```
Listing A.13: Creating a directory using mkdir.

1 FN11194:Documents sporring$ mkdir myFolder
2 FN11194:Documents sporring$ ls
3 myFolder
4 FN11194:tmp sporring$
```

A file can be created using echo and with redirection as shown in Listing A.14.

 $\cdot$  echo  $\cdot$  redirection

• mv

 $\cdot rm$ 

```
Listing A.14: Creating a file with echo and redirection.

1 FN11194:Documents sporring$ echo "hi" > hi.txt
2 FN11194:Documents sporring$ ls
3 hi.txt myFolder
```

To move the file hi.txt into myFolder, use mv. This is demonstrated in Listing A.15.

```
Listing A.15: Moving files with mv.

FN11194:Documents sporring$ echo mv hi.txt myFolder/
FN11194:Documents sporring$
```

To delete the file and the directory, use rm and rmdir as shown in Listing A.16.

```
Listing A.16: The Windows console.

1 FN11194:Documents sporring$ cd myFolder/
2 FN11194:myFolder sporring$ rm hi.txt
3 FN11194:myFolder sporring$ cd ..
4 FN11194:Documents sporring$ rmdir myFolder/
5 FN11194:Documents sporring$ ls
6 FN11194:Documents sporring$
```

Only commands found on the *search-path* are available in the console. The content of the search-path · search-path is seen using the echo command as demonstrated in Listing A.17.

# Listing A.17: The content of the search-path. FN11194:Documents sporring\$ echo \$PATH /Applications/Maple 17/:/Applications/PackageMaker.app/Contents/MacOS/:

/Applications/MATLAB_R2014b.app/bin/:/opt/local/bin:/opt/local/sbin:/usr/local/bin:/usr/bin:/usr/sbin:/opt/X11/bin:/Library/TeX/texbin

FN11194: Documents sporring\$

The search-path can be changed by editing the setup file for Bash. On MacOS X it is called ~/.profile, and on Linux it is either ~/.bash_profile or ~/.bashrc. Here new paths can be added by adding the following line: export PATH="<new path>:<another new path>:\$PATH".

A useful feature of Bash is that the console can help you write commands. E.g., if you write fs followed by pressing the tab-key, and if Mono is in the search-path, then Bash will typically respond by completing the line as fsharp, and by further pressing the tab-key some times, Bash will show the list of options, typically fshpari and fsharpc. Also, most commands have an extensive manual, which can be accessed using the man command. E.g., the manual for rm is retrieved by man rm.

# Number systems on the computer

### B.1 Binary numbers

Humans like to use the *decimal number* system for representing numbers. Decimal numbers are base 10 means that for a number consisting of a sequence of digits separated by a decimal point, where each digit can have values  $d \in \{0, 1, 2, \dots, 9\}$  and the weight of each digit is proportional  $\cdot$  decimal point to its place in the sequence of digits with respect to the decimal point, i.e., the number 357.6 = . digit  $3 \cdot 10^2 + 5 \cdot 10^1 + 7 \cdot 10^0 + 6 \cdot 10^{-1}$  or in general:

· decimal number

$$v = \sum_{i=-m}^{n} d_i 10^i \tag{B.1}$$

The basic unit of information in almost all computers is the binary digit or bit for short. A binary bit number consists of a sequence of binary digits separated by a decimal point, where each digit can have binary number values  $b \in \{0,1\}$ , and the base is 2. The general equation is,

$$v = \sum_{i=-m}^{n} b_i 2^i \tag{B.2}$$

and examples are  $1011.1_2 = 1 \cdot 2^3 + 0 \cdot 2^2 + 1 \cdot 2^1 + 1 \cdot 2^0 + 1 \cdot 2^{-1} = 11.5$ . Notice that we use subscript 2 to denote a binary number, while no subscript is used for decimal numbers. The left-most bit is called the most significant bit, and the right-most bit is called the least significant bit. Due to typical organisation of computer memory, 8 binary digits is called a byte, and 32 digits a word.

· most significant bit

· least significant bit

· byte

 $\cdot$  word

 $\cdot$  octal number

 $\cdot$  hexadecimal number

Other number systems are often used, e.g., octal numbers, which are base 8 numbers, where each digit is  $o \in \{0, 1, \dots, 7\}$ . Octals are useful short-hand for binary, since 3 binary digits maps to the set of octal digits. Likewise, hexadecimal numbers are base 16 with digits  $h \in \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, a, b, c, d, e, f\}$ , such that  $a_{16} = 10$ ,  $b_{16} = 11$  and so on. Hexadecimals are convenient since 4 binary digits map directly to the set of octal digits. Thus  $367 = 101101111_2 = 557_8 = 16f_{16}$ . A list of the integers 0–63 is various bases is given in Table B.1.

### B.2IEEE 754 floating point standard

The set of real numbers also called *reals* includes all fractions and irrational numbers. It is infinite in size both in the sense that there is no largest nor smallest number, and between any 2 given numbers there are infinitely many numbers. Reals are widely used for calculation, but since any computer only has finite memory, it is impossible to represent all possible reals on one. Hence, any computation performed on a computer with reals must rely on approximations. IEEE 754 double precision floatingpoint format (binary64), known as a double, is a standard for representing an approximation of reals

· IEEE 754 double precision floating-point format

· binarv64

 $\cdot$  double

Dec	Bin	Oct	Hex	Dec	Bin	Oct	Hex
0	0	0	0	32	100000	40	20
1	1	1	1	33	100001	41	21
2	10	2	2	34	100010	42	22
3	11	3	3	35	100011	43	23
4	100	4	4	36	100100	44	24
5	101	5	5	37	100101	45	25
6	110	6	6	38	100110	46	26
7	111	7	7	39	100111	47	27
8	1000	10	8	40	101000	50	28
9	1001	11	9	41	101001	51	29
10	1010	12	a	42	101010	52	2a
11	1011	13	b	43	101011	53	2b
12	1100	14	c	44	101100	54	2c
13	1101	15	d	45	101101	55	2d
14	1110	16	e	46	101110	56	2e
15	1111	17	f	47	101111	57	2f
16	10000	20	10	48	110000	60	30
17	10001	21	11	49	110001	61	31
18	10010	22	12	50	110010	62	32
19	10011	23	13	51	110011	63	33
20	10100	24	14	52	110100	64	34
21	10101	25	15	53	110101	65	35
22	10110	26	16	54	110110	66	36
23	10111	27	17	55	110111	67	37
24	11000	30	18	56	111000	70	38
25	11001	31	19	57	111001	71	39
26	11010	32	1a	58	111010	72	3a
27	11011	33	1b	59	111011	73	3b
28	11100	34	1c	60	111100	74	3c
29	11101	35	1d	61	111101	75	3d
30	11110	36	1e	62	111110	76	3e
31	11111	37	1f	63	111111	77	3f

Table B.1: A list of the integers 0–63 in decimal, binary, octal, and hexadecimal.

using 64 bits. These bits are divided into 3 parts: sign, exponent and fraction,

$$s e_1 e_2 \dots e_{11} m_1 m_2 \dots m_{52},$$

where s,  $e_i$ , and  $m_j$  are binary digits. The bits are converted to a number using the equation by first calculating the exponent e and the mantissa m,

$$e = \sum_{i=1}^{11} e_i 2^{11-i}, \tag{B.3}$$

$$m = \sum_{j=1}^{52} m_j 2^{-j}.$$
 (B.4)

I.e., the exponent is an integer, where  $0 \le e < 2^{11}$ , and the mantissa is a rational, where  $0 \le m < 1$ . For most combinations of e and m the real number v is calculated as,

$$v = (-1)^{s} (1+m) 2^{e-1023}$$
(B.5)

with the exception that

	m = 0	$m \neq 0$
e = 0	$v = (-1)^s 0 \text{ (signed zero)}$	$v = (-1)^s m2^{1-1023}$ (subnormals)
$e = 2^{11} - 1$	$v = (-1)^s \infty$	$v = (-1)^s \text{ NaN (not a number)}$

 $\cdot$  subnormals

· NaN

where  $e = 2^{11} - 1 = 111111111111_2 = 2047$ . The largest and smallest number that is not infinity is thus · not a number

$$e = 2^{11} - 2 = 2046 \tag{B.6}$$

$$m = \sum_{j=1}^{52} 2^{-j} = 1 - 2^{-52} \simeq 1.$$
 (B.7)

$$v_{\text{max}} = \pm (2 - 2^{-52}) 2^{1023} \simeq \pm 2^{1024} \simeq \pm 10^{308}$$
 (B.8)

The density of numbers varies in such a way that when e - 1023 = 52, then

$$v = (-1)^{s} \left( 1 + \sum_{j=1}^{52} m_j 2^{-j} \right) 2^{52}$$
 (B.9)

$$= \pm \left(2^{52} + \sum_{j=1}^{52} m_j 2^{-j} 2^{52}\right) \tag{B.10}$$

$$= \pm \left(2^{52} + \sum_{j=1}^{52} m_j 2^{52-j}\right)$$
 (B.11)

$$\stackrel{k=52-j}{=} \pm \left( 2^{52} + \sum_{k=51}^{0} m_{52-k} 2^k \right)$$
 (B.12)

which are all integers in the range  $2^{52} \le |v| < 2^{53}$ . When e - 1023 = 53, then the same calculation gives

$$v \stackrel{k=53-j}{=} \pm \left(2^{53} + \sum_{k=52}^{1} m_{53-k} 2^k\right)$$
 (B.13)

which are every second integer in the range  $2^{53} \le |v| < 2^{54}$ , and so on for larger values of e. When e - 1023 = 51, the same calculation gives,

$$v \stackrel{k=51-j}{=} \pm \left( 2^{51} + \sum_{k=50}^{-1} m_{51-k} 2^k \right)$$
 (B.14)

which is a distance between numbers of 1/2 in the range  $2^{51} \le |v| < 2^{52}$ , and so on for smaller values of e. Thus we may conclude that the distance between numbers in the interval  $2^n \le |v| < 2^{n+1}$  is  $2^{n-52}$ , for  $-1022 = 1 - 1023 \le n < 2046 - 1023 = 1023$ . For subnormals, the distance between numbers are

$$v = (-1)^s \left(\sum_{j=1}^{52} m_j 2^{-j}\right) 2^{-1022}$$
(B.15)

$$= \pm \left(\sum_{j=1}^{52} m_j 2^{-j} 2^{-1022}\right) \tag{B.16}$$

$$= \pm \left(\sum_{j=1}^{52} m_j 2^{-j-1022}\right) \tag{B.17}$$

$$\stackrel{k=-j-1022}{=} \pm \left( \sum_{j=-1023}^{-1074} m_{-k-1022} 2^k \right)$$
 (B.18)

which gives a distance between numbers of  $2^{-1074} \simeq 10^{-323}$  in the range  $0 < |v| < 2^{-1022} \simeq 10^{-308}$ .

# C | Commonly used character sets

Letters, digits, symbols and space are the core of how we store data, write programs, and communicate with computers and each other. These symbols are in short called characters, and represent a mapping between numbers, also known as codes, and a pictorial representation of the character. E.g., the ASCII code for the letter 'A' is 65. These mappings are for short called character sets, and due to differences in natural languages and symbols used across the globe, many different character sets are in use. E.g., the English alphabet contains the letters 'a' to 'z', which is shared by many other European languages, but which have other symbols and accents. For example, Danish has further the letters 'æ', 'ø', and 'å'. Many non-European languages have completely different symbols, where the Chinese character set is probably the most extreme, and some definitions contains 106,230 different characters albeit only 2,600 are included in the official Chinese language test at highest level.

Presently, the most common character set used is Unicode Transformation Format (UTF), whose most popular encoding schemes are 8-bit (UTF-8) and 16-bit (UTF-16). Many other character sets exist, and many of the later build on the American Standard Code for Information Interchange (ASCII). The ISO-8859 codes were an intermediate set of character sets that are still in use, but which is greatly inferior to UTF. Here we will briefly give an overview of ASCII, ISO-8859-1 (Latin1), and UTF.

### C.1 ASCII

The American Standard Code for Information Interchange (ASCII) [8], is a 7 bit code tuned for the letters of the english language, numbers, punctuation symbols, control codes and space, see Tables C.1 and C.2. The first 32 codes are reserved for non-printable control characters to control printers and similar devices or to provide meta-information. The meaning of each control character is not universally agreed upon.

· American Standard Code for Information Interchange

· ASCII

The code order is known as  $ASCIIbetical\ order$ , and it is sometimes used to perform arithmetic on codes, e.g., an upper case letter with code c may be converted to lower case by adding 32 to its code. The ASCIIbetical order also has consequence for sorting, i.e., when sorting characters according to their ASCII code, 'A' comes before 'a', which comes before the symbol ' $\{$ '.

· ASCIIbetical order

### C.2 ISO/IEC 8859

The ISO/IEC 8859 report http://www.iso.org/iso/catalogue_detail?csnumber=28245 defines 10 sets of codes specifying up to 191 codes and graphic characters using 8 bits. Set 1, also known as ISO/IEC 8859-1, Latin alphabet No. 1 or *Latin1*, covers many European languages and is designed to be compatible with ASCII, such that code for the printable characters in ASCII are the same in ISO 8859-1. Table C.3 shows the characters above 7e. Codes 00-1f and 7f-9f are undefined in ISO 8859-1.

Latin1

x0+0x	00	10	20	30	40	50	60	70
00	NUL	DLE	SP	0	0	P		p
01	SOH	DC1	!	1	A	Q	a	q
02	STX	DC2	"	2	В	R	b	r
03	ETX	DC3	#	3	С	S	С	s
04	EOT	DC4	\$	4	D	Т	d	t
05	ENQ	NAK	%	5	Е	U	e	u
06	ACK	SYN	&	6	F	V	f	V
07	$\operatorname{BEL}$	ETB	,	7	G	W	g	W
08	BS	CAN	(	8	Η	X	h	X
09	HT	EM	)	9	I	Y	i	У
0A	$_{ m LF}$	SUB	*	:	J	Z	j	Z
0B	VT	ESC	+	;	K	[	k	{
0C	$\operatorname{FF}$	FS	,	<	L	\	1	
0D	CR	GS	_	=	M	]	m	}
0E	SO	RS	•	>	N	^	n	~
0F	SI	US	/	?	O	_	О	DEL

Table C.1: ASCII

### C.3 Unicode

Unicode is a character standard defined by the Unicode Consortium, http://unicode.org as the Unicode Standard. Unicode allows for 1,114,112 different codes. Each code is called a code point, which represents an abstract character. However, not all abstract characters require a unit of several code points to be specified. Code points are divided into 17 planes each with  $2^{16} = 65,536$  code points. Planes are further subdivided into named blocks. The first plane is called the Basic Multilingual plane and its block of the first 128 code points is called the Basic Latin block and are identical to ASCII, see Table C.1, and code points 128-255 is called the Latin-1 Supplement block, and are identical to the upper range of ISO 8859-1, see Table C.3. Each code-point has a number of attributes such as the Unicode general category. Presently more than 128,000 code points are defined covering 135 modern and historic writing systems, and obtained at http://www.unicode.org/Public/UNIDATA/UnicodeData.txt, which includes the code point, name, and general category.

A Unicode code point is an abstraction from the encoding and the graphical representation of a character. A code point is written as "U+" followed by its hexadecimal number, and for the Basic Multilingual plane 4 digits are used, e.g., the code point with the unique name LATIN CAPITAL LETTER A has the Unicode code point "U+0041", and is in this text it is visualized as 'A'. More digits are used for code points of the remaining planes.

The general category is used to specify valid characters that not necessarily have a visual representation but possibly transforms text. Some categories and their letters in the first 256 code points are shown in Table C.5.

To store and retrieve code points, they must be encoded and decoded. A common encoding is UTF-8, which encodes code points as 1 to 4 bytes, and which is backward-compatible with ASCII and ISO 8859-1. Hence, in all 3 coding systems the character with code 65 represents the character 'A'. Another popular encoding scheme is UTF-16, which encodes characters as 2 or 4 bytes, but which is not backward-compatible with ASCII or ISO 8859-1. UTF-16 is used internally in many compilers, interpreters and operating systems.

- · Unicode Standard
- · code point
- · blocks
- · Basic Multilingual plane
- $\cdot$ Basic Latin block
- · Latin-1 Supplement block
- · Unicode general category

UTF-8

UTF-16

Code	Description
NUL	Null
SOH	Start of heading
STX	Start of text
ETX	End of text
EOT	End of transmission
ENQ	Enquiry
ACK	Acknowledge
$\operatorname{BEL}$	Bell
BS	Backspace
HT	Horizontal tabulation
LF	Line feed
VT	Vertical tabulation
FF	Form feed
CR	Carriage return
SO	Shift out
SI	Shift in
DLE	Data link escape
DC1	Device control one
DC2	Device control two
DC3	Device control three
DC4	Device control four
NAK	Negative acknowledge
SYN	Synchronous idle
ETB	End of transmission block
CAN	Cancel
EM	End of medium
SUB	Substitute
ESC	Escape
FS	File separator
GS	Group separator
RS	Record separator
US	Unit separator
SP	Space
DEL	Delete

Table C.2: ASCII symbols.

x0+0x	80	90	A0	В0	C0	D0	E0	F0
00			NBSP	0	À	Đ	à	ð
01			i	土	Á	Ñ	á	ñ
02			¢	2	Â	Ò	â	ò
03			£	3	Ã	Ó	$ ilde{ ext{a}}$	ó
04			¤	1	Ä	Ô	ä	ô
05			¥	$\mu$	Å	Õ	å	õ
06				$\P$	Æ	Ö	æ	ö
07			§	•	Ç	×	ç	÷
08			••	3	È	Ø	è	Ø
09			©	1	É	Ù	é	ù
0a			<u>a</u>	Ō	Ê	Ú	ê	ú
0b			«	<b>»</b>	Ë	Û	ë	û
0c			Г	$\frac{1}{4}$	Ì	Ü	ì	ü
0d			SHY	$ \begin{array}{r} \frac{1}{4} \\ \frac{1}{2} \\ \frac{3}{4} \end{array} $	Í	Ý	í	ý
0e			R	$\frac{3}{4}$	Î	Þ	î	þ
Of			-	i	Ϊ	ſŝ	ï	þ ÿ

Table C.3: ISO-8859-1 (latin1) non-ASCII part. Note that the codes 7f - 9f are undefined.

Code	Description
NBSP	Non-breakable space
SHY	Soft hypen

Table C.4: ISO-8859-1 special symbols.

General	Code points	Name
category		
Lu	$U+0041-U+005A,\ U+00C0-U+00D6,$	Upper case letters
	U+00D8-U+00DE	
Ll	$U+0061-U+007A,\ U+00B5,$	Lower case letter
	$U+00DF-U+00F6,\ U+00F8-U+00FF$	
$\operatorname{Lt}$	None	Digraphic letter, with first part uppercase
Lm	None	Modifier letter
Lo	$\mathrm{U}{+}00\mathrm{AA},\mathrm{U}{+}00\mathrm{BA}$	Gender ordinal indicator
Nl	None	Letterlike numeric character
Pc	$\mathrm{U}{+}005\mathrm{F}$	Low line
Mn	None	Nonspacing combining mark
Mc	None	Spacing combining mark
Cf	U+00AD	Soft Hyphen

Table C.5: Some general categories for the first 256 code points.

# D | Common Language Infrastructure

The Common Language Infrastructure (CLI), not to be confused with Command Line Interface with the same acronym, is a technical standard developed by Microsoft [4, 3]. The standard specifies a language, its format, and a runtime environment that can execute the code. The main feature is that it provides a common interface between many languages and many platforms, such that programs can collaborate in a language agnostic manner and can be executed on different platforms without having to be recompiled. Main features of the standard are:

- · Common Language Infrastructure
- $\cdot$  CLI
- · Command Line Interface
- Common Type System (CTS) which defines a common set of types that can be used across different languages as if it were their own.
- · Common Type System · CTS
- Metadata which defines a common method for referencing programming structures such as values and functions in a language independent manner.
- · Metadata
- Common Intermediate Language (CIL) which is a platform-independent, stack-based, object-oriented assembly language that can be executed by the Virtual Execution System.
- $\begin{array}{c} \cdot \ \text{Common Intermediate} \\ \ \ \text{Language} \\ \cdot \ \text{CIL} \end{array}$
- Virtual Execution System (VES) which is a platform dependent, virtual machine, which combines the above into code that can be executed at runtime. Microsoft's implementation of VES is called Common Language Runtime (CLR) and uses just-in-time compilation.
- · Virtual Execution
- The process of running an F# program is shown in Figure D.1¹: First the F# code is compiled or interpreted to CIL. This code possibly combined with other CIL code is then converted to a machine-
- · VES · Common Language

interpreted to CIL. This code possibly combined with other CIL code is then converted to a machinereadable code, and the result is then executed on the platform.

CLI defines a *module* as a single file containing executable code by VES. Hence, CLI's notion of module

 $\begin{array}{c} {\rm Runtime} \\ \cdot {\rm CLR} \end{array}$ 

System

- is somewhat related to F#'s notion of module, but the two should not be confused. A collection of modules, a *manifest*, and possibly other resources, which jointly define a complete program is called an *assembly*. The manifest is the description of which files are included in the assembly together with its version, name, security information, and other bookkeeping information.
- · just-in-time
- · module
- · manifest · assembly

¹Jon: update figure

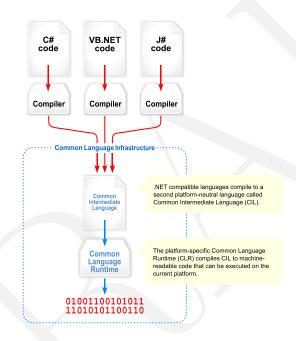


Figure D.1: Visual overview of CLI. Figure by Jarkko Piiroinen - Own work, Public Domain, https://commons.wikimedia.org/w/index.php?curid=3602584.

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