Classes and Objects

Object-oriented programming is a programming paradigm that focuses on objects such as object-oriented a persons, places, things, events, and concepts relevant for the problem.

programming

Object-oriented programming has a rich language for describing objects and their relations, which can seem overwhelming at first, and they will be explained in detail in this and following chapters. Here is a brief overview: The main programming structures are called a classes and objects. It is useful to think of classes as user defined types and objects as values of such types. However, there is more to classes and objects than types and values. Objects may contain both data and code, and it is sometimes useful to draw the corresponding class definition as shown in Figure 1.1. In this illustration, objects of type

· object

```
aClass
// The object's values (properties)
aValue: int
anotherValue: float*bool
// The object's functions (methods)
aMethod: () -> int
anotherMethod: float -> float
```

Figure 1.1: A class is sometimes drawn as a figure.

aClass will each contain an int and a pair of a float and a boolean, and each object has two functions associated with them. The values stored in each object may differ, but the types are fixed by the class definition. It is common to call an object's values properties and an object's functions methods. In short, properties and methods are collectively called members. When an object is created, memory is set aside on The Heap to each object's property. Creating an object is commonly called *instantiation*. The members serve as the interface to each object, and each instantiated object will have the same type of members as all objects of that class, but their content may differ.

· properties

 \cdot method

 \cdot member · The Heap

 \cdot instantiate

Object-oriented programming is an extension of data types, in the sense that objects contain both data and functions in a similar manner as a module, but object-oriented programming emphasizes the semantic unity of the data and functions. Thus, objects are often models of real-world entities, and object-oriented programming leads to a particular style of programming analysis and design called object-oriented analysis and design to be discussed in ??.

- \cdot models
- · object-oriented analysis
- · object-oriented design

1.1 Constructors and Members

A class is defined using the type keyword. Note that there are always parentheses after the class name to distinguish it from a regular type definition. The basic syntax for a class definition is as follows:

```
Listing 1.1: Syntax for simple class definitions.

type <classIdent> ({<arg>}) [as <selfIdent>]

{let <binding> | do <statement>}

{member <memberDef>}
```

The first line is the header of the class, where the <classIdent> is the name of the class, <arg> are its optional arguments, and <selfIdent> is an optional self identifier. The body of a class consists of the constructor and the member section. The header and the constructor section is often collectively called the constructor, and the body of the constructor consist of optional let-bindings and do-statements. Note that the do-statements in a class definition must use the do-keyword. The member section consisting of all the optional member definitions, where each definition use the member-keyword.

· self identifier

 \cdot constructor

The header and constructor section is commonly called the *constructor*, and the constructor is executed at instantiation. In contrast to many other languages, the constructor is always stated as the initial code of a class definition. The values and variables in the constructor are called *fields*, while functions are just called *functions*.

 $\cdot \ constructor$

· field

 \cdot functions

· member@member

 \cdot interface

 \cdot properties

· method

·as

Members are declared using the *member*-keyword, which defines values and functions that are accessible from outside the class using the "."-notation. In this manner, the members define the *interface* between the internal bindings in the constructor and an application program. Member values are called *properties*, and member functions are called *methods*. Note that members are immutable. The body of a member has access to the arguments, the constructor's bindings, and to all class members, regardless of the member's lexicographical order. In contrast, members are not available in the constructor unless the self identifier has been declared in the header using the keyword *as*, e.g., type classMutable(name: string) as this =

Consider the example in Figure 1.2. Here we have defined a class car, instantiated three

```
car
// A car has a color
color : string
```

Figure 1.2: A class car is instantiated trice and bound to the names sportsCar, stationWagon, and miniBus, and each object's properties are set to different values.

objects, and bound them to the names sportsCar, stationWagon, and miniBus. Each object has been given different values for the color property. In F# this could look like the code in Listing 1.2.

Listing 1.2 car.fsx: Defining a class car, and making three instances of it. See also Figure 1.2. type car (aColor: string) = // Member section member this.color = aColor let sportsCar = car ("red") let stationWagon = car ("green") let miniBus = car ("blue") printfn "%s %s %s" sportsCar.color stationWagon.color miniBus.color f sharpc --nologo car.fsx && mono car.exe red green blue

In the example, the class car is defined in lines 1-3. Its header includes one string argument, aColor. The body of the constructor is empty, and the member section consists of lines 2-3. The class defines one property color: string. Note that when referring to a member inside an object, then we must use a self identifier. Here we use this as the self identifier, and as the example shows, we need not declare it in the class' header. A self identifier refers to the memory set aside to the particular instance of an object. It is common among other programming languages to use this as self identifier. F# is very flexible regarding what name can be used for the self-identifier, and the member section could as well have been self.value, __.value, or anything else, and it need not be the same in every member definition. Nevertheless, consistency in the name used as self-identifier is strongly encouraged, preferably using a name that reflects the nature of the reference, such as this or me. The objects are instantiated in lines 5-7, and the value of their properties are accessed in line 8. In many languages, objects are instantiated using the new keyword, but in F# this is optional. I.e., let sportsCar = car ("red") is identical to let sportsCar = new car ("red"). Note that both the self identifier and member access uses the "." notation.

· self identifier

Advice

· new@new

A more advanced implementation of a car class might include notions of a fuel gauge, fuel economy, and the ability to update the fuel gauge as the car is driven. An example of an implementation of this is given In Listing 1.3.

Listing 1.3 class.fsx: Extending Listing 1.2 with fields and methods. type car (econ : float, fuel : float) = // Constructor body section let mutable fuelLeft = fuel // liters in the tank do printfn "Created a car (%.1f, %.1f)" econ fuel // Member section member this.fuel = fuelLeft member this.drive distance = fuelLeft <- fuelLeft - econ * distance / 100.0</pre> let sport = car (8.0, 60.0)let economy = car (5.0, 45.0)sport.drive 100.0 economy.drive 100.0 printfn "Fuel left after 100km driving:" printfn " sport: %.1f" sport.fuel printfn " economy: %.1f" economy.fuel \$ fsharpc --nologo class.fsx && mono class.exe Created a car (8.0, 60.0) Created a car (5.0, 45.0) Fuel left after 100km driving: sport: 52.0 economy: 40.0

Here in line 1, the constructor has 2 arguments: the fuel economy parameter and the initial amount of fuel in the tank. Thus, we are able to create 2 different cars with different fuel economy, as shown in lines 10-11. The amount of fuel left en each car object is stored in the mutable field fuelLeft. This is an example of a state of an object: It can be accessed outside the object by the fuel property, and it can be updated by the drive method.

Field names and functions defined in the constructor do not use the self identifier and cannot be accessed outside and object using the "." notation. However, they are available in both the constructor and the member section following the regular scope rules. Fields are a common way to hide implementation details, and they are private to the object or · private class in contrast to members that are public.

· public

1.2 Accessors

Methods are most often used as an interface between the fields of an object and the application program. Consider the example in Listing 1.4.

Listing 1.4 classAccessor.fsx:
Accessor methods interface with internal bindings.

type aClass () =
let mutable v = 1
member this.setValue (newValue : int) : unit =
v <- newValue
member this.getValue () : int = v

let a = aClass ()
printfn "%d" (a.getValue ())
a.setValue (2)
printfn "%d" (a.getValue ())

fsharpc --nologo classAccessor.fsx && mono classAccessor.exe

fsharpc --nologo classAccessor.fsx && mono classAccessor.exe

In the example, the data contained in objects of type aClass is stored in the mutable field v. Since only members can be accessed from an application, it is not possible to retrieve or change the data of these object of class aClass directly. We could have programmed v as a member instead, i.e., member this.v = 1, however, often we are in a situation, where there is a range of possible choices of data representation, details of which we do wish to share with an application program. E.g., implementation details of arrays are not important for our ability to use them in applications. What matters is that the members that work on the array elements are well defined and efficient. Thus, the example demonstrates how we can build two simple methods setValue and getValue to set and get the data stored v. By making a distinction between the internal representation and how members give access to the data, we retain the possibility to change the internal representation without having to reprogram all the application programs. Analogously, we can change the engine in a car from one type to another without having to change the car's interaction with the driver and the road: steering wheel, pedals, wheels etc.

Such functions are called *accessors*. Internal states with setters and getters are a typical construction, since they allow for complicated computations when states are read to and written from, and gives the designer of the class the freedom to change the internal representation while keeping the interface the same. Accessors are so common that F# includes a special syntax for them: Classes can be made to act like variables using member...with...and keywords and the special function bindings get() and set(), as demonstrated in Listing 1.5.

 \cdot accessors

Listing 1.5 classGetSet.fsx: Members can act as variables with the built-in get and set functions. 1 type aClass () = 2 let mutable v = 0 3 member this.value 4 with get () = v 5 and set (a) = v <- a 6 let a = aClass () 7 printfn "%d" a.value 9 a.value<-2 10 printfn "%d" a.value 1 \$ fsharpc --nologo classGetSet.fsx && mono classGetSet.exe 2 0 3 2

The expression defining get: () -> 'a and set: 'a -> (), where 'a is any type, can be any usual expression. The application calls the get and set as if the property were a mutable value. If set is omitted, then the property acts as a value rather than a variable, and values cannot be assigned to it in the application program.

Setters and getters are so common that F# has a short-hand for this using member val value = 0 with get, set, which creates the internal mutable value value, but this is discouraged in this text.

Defining an *Item* property with extended get and set makes objects act as indexed variables, as demonstrated in Listing 1.6.

```
Listing 1.6 classGetSetIndexed.fsx:
Properties can act as indexed variables with the built-in get and set func-
tions.
 type aClass (size : int) =
  let arr = Array.create<int> size 0
   member this.Item
     with get (ind : int) = arr.[ind]
     and set (ind : int) (p : int) = arr.[ind] <- p</pre>
let a = aClass (3)
printfn "%A" a
printfn "%d %d %d" a.[0] a.[1] a.[2]
a.[1] <- 3
printfn "%d %d %d" a.[0] a.[1] a.[2]
$ fsharpc --nologo classGetSetIndexed.fsx && mono
   classGetSetIndexed.exe
ClassGetSetIndexed+aClass
0 0 0
 0 3 0
```

Higher dimensional indexed properties are defined by adding more indexing arguments to

the definition of get and set, such as demonstrated in Listing 1.7.

```
Listing 1.7 classGetSetHigherIndexed.fsx:
Getters and setters for higher dimensional index variables.
type aClass (rows : int, cols : int) =
  let arr = Array2D.create<int> rows cols 0
  member this.Item
    with get (i : int, j : int) = arr.[i,j]
    and set (i : int, j : int) (p : int) = arr.[i,j] <- p
let a = aClass (3, 3)
printfn "%A" a
printfn "%d %d %d" a.[0,0] a.[0,1] a.[2,1]
a.[0,1] <- 3
printfn "%d %d %d" a.[0,0] a.[0,1] a.[2,1]
$ fsharpc --nologo classGetSetHigherIndexed.fsx
$ mono classGetSetHigherIndexed.exe
ClassGetSetHigherIndexed+aClass
0 0 0
0 3 0
```

1.3 Objects are Reference Types

Objects are reference type values, implying that copying objects copies their references, not their values, and their content is stored on $The\ Heap$, see ??. Consider the example \cdot The Heap in Listing 1.8.

```
Listing 1.8 classReference.fsx:
Objects assignment can cause aliasing.

type aClass () =
let mutable v = 0
member this.value with get () = v and set (a) = v <- a

let a = aClass ()
let b = a
a.value <- 2
printfn "%d %d" a.value b.value

fsharpc --nologo classReference.fsx && mono classReference.exe
2 2 2
```

Thus, the binding to b in line 6 is an alias to a, not a copy, and changing object a also changes b! This is a common cause of error, and you should **think of objects as arrays.** Advice For this reason, it is often seen that classes implement a copy function returning a new object with copied values, e.g., Listing 1.9.

Listing 1.9 classCopy.fsx: A copy method is often needed. Compare with Listing 1.8. type aClass () = let mutable v = 0 member this.value with get () = v and set (a) = v <- a member this.copy () = let o = aClass () o.value <- v o let a = aClass () let b = a.copy () a.value<-2 printfn "%d %d" a.value b.value fsharpc --nologo classCopy.fsx && mono classCopy.exe 2 0

In the example, we see that since **b** now is a copy, we do not change it by changing **a**. This is called a *copy constructor*.

· copy constructor

1.4 Static Classes

Classes can act as modules and hold data which is identical for all objects of its type. These are defined using the *static*-keyword. And since they do not belong to a single object, but are shared between all objects, they are defined without the self-identifier and accessed using the class name, and they cannot refer to the arguments of the constructor. For example, consider a class whose objects each hold a unique identification number (id): When an object is instantiated, the object must be given the next available identification number. The next available id could be given as an argument to the constructor, however, this delegates the task of maintaining the uniqueness of ids to the application program. It is better to use a static field and delegate the administration of ids completely to the constructors, as demonstrated in Listing 1.10.

static@static

Listing 1.10 classStatic.fsx: Static fields and members are identical to all objects of the type. type student (name : string) = static let mutable nextAvailableID = 0 // A global id for all objects let studentID = nextAvailableID // A per object id do nextAvailableID <- nextAvailableID + 1</pre> member this.id with get () = studentID member this.name = name static member nextID = nextAvailableID // A global member let a = student ("Jon") // Students will get unique ids, when instantiated let b = student ("Hans") printfn "%s: %d, %s: %d" a.name a.id b.name b.id printfn "Next id: %d" student.nextID // Accessing the class's member \$ fsharpc --nologo classStatic.fsx && mono classStatic.exe Jon: 0, Hans: 1 Next id: 2

Notice in line 2 that a static field nextAvailableID is created for the value to be shared by all objects. The initialization of its value is only performed once, at the beginning of program execution. However, every time an object is instantiated, the value of nextAvailableID is copied to the object's field studentID in line 3, and nextAvailableID is updated. The static field can be accessed with a static accessor, as demonstrated in line 7. Notice how this definition does not include a self-identifier, and that the member is accessible from the application in line 11 using the class' name, in both cases since it is not a member of any particular object.

1.5 Recursive Members and Classes

The members of a class are inherently recursive: static and non-static methods may recurse using the self identifier and other members regardless of their lexicographical scope. This is demonstrated in Listing 1.11.

Listing 1.11 classRecursion.fsx:

Members can recurse without the keyword and refer to other members regardless of their lexicographical scope.

```
type twice (v : int) =
static member fac n = if n > 1 then n * (twice.fac (n-1))
else 1 // No rec
member this.copy = this.twice // No lexicographical scope
member this.twice = 2*v

let a = twice (2)
let b = twice.fac 3
printfn "%A %A %A" a.copy a.twice b

fsharpc --nologo classRecursion.fsx && mono
classRecursion.exe
4 4 6
```

For mutually recursive classes, the keyword and must be used, as shown in Listing 1.12. and

```
Listing 1.12 classAssymetry.fsx:
Mutually recursive classes are defined using the keyword.
type anInt (v : int) =
  member this.value = v
  member this.add (w : aFloat) : aFloat = aFloat ((float
   this.value) + w.value)
and aFloat (w : float) =
  member this.value = w
  member this.add (v : anInt) : aFloat = aFloat ((float
   v.value) + this.value)
let a = anInt (2)
let b = aFloat (3.2)
let c = a.add b
let d = b.add a
printfn "%A %A %A %A" a.value b.value c.value d.value
$ fsharpc --nologo classAssymetry.fsx && mono
   classAssymetry.exe
2 3.2 5.2 5.2
```

Here anInt and aFloat hold an integer and a floating point value respectively, and they both implement an addition of anInt an aFloat that returns and aFloat. Thus, they are mutually dependent and must be defined in the same type definition using and.

1.6 Function and Operator Overloading

It is often convenient to define different methods that have the same name, but with functionalities that depend on the number and type of arguments given. This is called overloading, and F# supports method overloading. An example is shown in Listing 1.13. · overloading

Listing 1.13 classOverload.fsx:

Overloading methods set : int -> () and set : int * int -> () is permitted, since they differ in argument number or type.

```
type Greetings () =
  let mutable greetings = "Hi"
  let mutable name = "Programmer"
  member this.str = greetings + " " + name
  member this.setName (newName : string) : unit =
    name <- newName
  member this.setName (newName : string, newGreetings :
  string) : unit =
    greetings <- newGreetings
    name <- newName
let a = Greetings ()
printfn "%s" a.str
a.setName ("F# programmer")
printfn "%s" a.str
a.setName ("Expert", "Hello")
printfn "%s" a.str
$ fsharpc --nologo classOverload.fsx && mono classOverload.exe
Hi Programmer
Hi F# programmer
Hello Expert
```

In the example we define an object which can produce greetings strings of the form <greeting> <name>, using the str member. It has a default greeting "Hi" and name "Programmer", but the name can be changed by calling the setName accessor with one argument, and both greeting and name can be changed by calling the overloaded setName with two arguments. Overloading in class definition is allowed as long as the arguments differ in number or type.

In Listing 1.12, the notation for addition is less than elegant. For such situations, F# supports operator overloading. All usual operators may be overloaded (see ??), and in · operator overloading contrast to regular operator overloading, the compiler uses type inference to decide which function is to be called. All operators have a functional equivalence, and to overload the binary "+" and unary "-" operators, we overload their functional equivalence (+) and (~-) as static members. This is demonstrated in Listing 1.14.

Listing 1.14 classOverloadOperator.fsx: Operators can be overloaded using their functional equivalents.

```
type anInt (v : int) =
  member this.value = v
  static member (+) (v : anInt, w : anInt) = anInt (v.value +
  static member (~-) (v : anInt) = anInt (-v.value)
and aFloat (w : float) =
  member this.value = w
  static member (+) (v : aFloat, w : aFloat) = aFloat (v.value
  + w.value)
  static member (+) (v : anInt, w : aFloat) =
    aFloat ((float v.value) + w.value)
  static member (+) (w : aFloat, v : anInt) = v + w // reuse
  static member (~-) (v : aFloat) = aFloat (-v.value)
let a = anInt (2)
let b = anInt (3)
let c = aFloat (3.2)
let d = a + b // anInt + anInt
let e = c + a // aFloat + anInt
let f = a + c // anInt + aFloat
let g = -a // unitary minus anInt
let h = a + -b // anInt + unitary minus anInt
printf "a=%A, b=%A, c=%A, d=%A" a.value b.value c.value d.value
printf ", e=%A, f=%A, g=%A, h=%A" e.value f.value g.value
  h.value
$ fsharpc --nologo classOverloadOperator.fsx
$ mono classOverloadOperator.exe
a=2, b=3, c=3.2, d=5, e=5.2, f=5.2, g=-2, h=-1
```

Thus, writing v + w is equivalent to writing anInt.(+) (v, w). Presently, the former is to be preferred, but at times, e.g., when using functions as arguments, it is useful to be able to refer to an operator by its function-equivalent. Note that the functional equivalence of the multiplication operator (*) shares a prefix with the begin block comment lexeme "(*", which is why the multiplication function is written as (*). Note also that unitary operators have a special notation using the "~"-lexeme, as illustrated in the above example for unitary minus. With the unitary minus, we are able to subtract objects of anInt by first negating the right-hand operand and then adding the result to the left-hand operand. In contrast, the binary minus would have been defined as static member (-) (v: anInt, w : aFloat) = anInt ((float v.value) - w.value).

In Listing 1.14, notice how the second (+) operator overloads the first by calling the first with the proper order of arguments. This is a general principle: avoid duplication of Advice code, reuse of existing code is almost always preferred. Here it is to be preferred for two reasons. Firstly, if we discover a mistake in the multiplication code, then we need only correct it once, which implies that both multiplication methods are corrected once and reduces the chance of introducing new mistakes by attempting to correct old ones. Secondly, if we later decide to change the internal representation, then we only need to update one version of the multiplication function, hence we reduce programming time and risk of errors as well.

Beware that operator overloading outside class definitions overwrites all definitions of the operator. E.g., overloading (+) (v, w) outside a class will influence integer, real, string, etc. Thus, operator overloading should only be done inside class definitions.

Advice

1.7 Additional Constructors

Like methods, constructors can also be overloaded by using the new keyword. E.g., the \cdot new@new example in Listing 1.13 may be modified, such that the name and possibly greeting is set at object instantiation rather than by using the accessor. This is illustrated in Listing 1.15.

```
Listing 1.15 classExtraConstructor.fsx:
Extra constructors can be added, using
type classExtraConstructor (name : string, greetings : string)
  static let defaultGreetings = "Hello"
  // Additional constructors are defined by new ()
  new (name : string) =
     classExtraConstructor (name, defaultGreetings)
  member this.name = name
  member this.str = greetings + " " + name
let s = classExtraConstructor ("F#") // Calling additional
let t = classExtraConstructor ("F#", "Hi") // Calling primary
   constructor
printfn "%A, %A" s.str t.str
  fsharpc --nologo classExtraConstructor.fsx
$ mono classExtraConstructor.exe
 "Hello F#", "Hi F#"
```

The top constructor that does not use the new-keyword is called the primary constructor. • primary constructor The body of the additional constructor must call the primary constructor, and the body cannot extend the primary constructor's fields and functions. It is useful to think of the Advice primary constructor as a superset of arguments and the additional ones as subsets or specializations. As regular scope rules dictate, the additional constructor has access to the primary constructor's bindings. However, in order to access the object's members, the self identifier has to be explicitly declared, using the as-keyword in the header. E.g., writing new(x: float, y: float) as alsoThis = However beware. Even though the body of the additional constructor now may access the property alsoThis.x, this value has first been created once the primary constructor has been called. E.g., calling the primary constructor in the additional constructor as new(x: float, y: float) as alsoThis = classExtraConstructor(fst alsoThis.x, y, defaultSeparator) will cause an exception at runtime. Code may be executed in additional constructors: Before the call to the primary constructor, let and do statements are allowed. If code is to be executed after the primary constructor has been called, then it must be preceded by the then keyword, as shown in ??.

Listing 1.16 classDoThen.fsx:

The optional - and --keywords allow for computations before and after the primary constructor is called.

```
type classDoThen (aValue : float) =
  // "do" is mandatory to execute code in the primary
  constructor
  do printfn " Primary constructor called"
  // Some calculations
  do printfn " Primary done" (* *)
  new() =
    // "do" is optional in additional constructors
    printfn " Additional constructor called"
    classDoThen (0.0)
    // Use "then" to execute code after construction
    then
      printfn " Additional done"
  member this.value = aValue
printfn "Calling additional constructor"
let v = classDoThen ()
printfn "Calling primary constructor"
let w = classDoThen (1.0)
$ fsharpc --nologo classDoThen.fsx && mono classDoThen.exe
Calling additional constructor
  Additional constructor called
  Primary constructor called
  Primary done
  Additional done
Calling primary constructor
  Primary constructor called
  Primary done
```

The do-keyword is often understood to be implied by F#, e.g., in front of all printf-statements, but in the above examples they are required where used. This may change in future releases of F#. F# allows for many additional constructors, but they must be distinguishable by type.

1.8 Programming Intermezzo: Two Dimensional Vectors

Consider the following problem.

Problem 1.1

A Euclidean vector is a geometric object that has a direction, a length, and two operations: vector addition and scalar multiplication, see ??. Define a class for a vector in two dimensions.

An essential part in designing a solution for the above problem is to decide which representation to use internally for vectors. The Cartesian representation of a vector is as a tuple of real values (x, y), where x and y are real values, and where we can imagine that

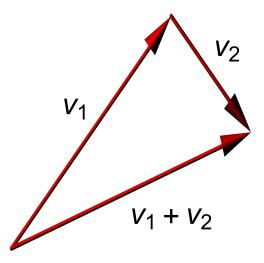


Figure 1.3: Illustration of vector addition in two dimensions.

the tail of the vector is in the origin, and its tip is at the coordinate (x, y). For vectors on Cartesian form,

$$\vec{v} = (x, y), \tag{1.1}$$

the basic operations are defined as

$$\vec{v}_1 + \vec{v}_2 = (x_1 + x_2, y_1 + y_2), \tag{1.2}$$

$$a\vec{v} = (ax, ax),\tag{1.3}$$

$$\operatorname{dir}(\vec{v}) = \tan\frac{y}{x}, \ x \neq 0, \tag{1.4}$$

$$\operatorname{len}(\vec{v}) = \sqrt{x^2 + y^2},\tag{1.5}$$

where x_i and y_i are the elements of vector \vec{v}_i , a is a scalar, and dir and len are the direction and length functions, respectively. The polar representation of vectors is also a tuple of real values (θ, l) , where θ is the vector's angle from the x-axis and l is the vector's length. This representation is closely tied to the definition of a vector, and has the constraint that $0 \le \theta < 2\pi$ and $0 \le l$. This representation reminds us that vectors do not have a position. For vectors on polar form,

$$\vec{v} = (\theta, l), \tag{1.6}$$

their basic operations are defined as

$$x(\theta, l) = l\cos(\theta),\tag{1.7}$$

$$y(\theta, l) = l\sin(\theta),\tag{1.8}$$

$$\vec{v}_1 + \vec{v}_2 = (x(\theta_1, l_1) + x(\theta_2, l_2), y(\theta_1, l_1) + y(\theta_2, l_2))$$
(1.9)

$$a\vec{v} = (\theta, al), \tag{1.10}$$

where θ_i and l_i are the elements of vector \vec{v}_i , a is a scalar, and x and y are the Cartesian coordinate functions.

So far in our analysis, we have realized that:

• both the Cartesian and polar representations use a pair of reals to represent the vector,

- both require functions to calculate the elements of the other representation,
- the polar representation is invalid for negative lengths, and
- the addition operator under the polar representation is also more complicated and essentially requires access to the Cartesian representation.

The first step in shaping our solution is to decide on file structure: For conceptual separation, we choose to use a library and an application file. F# wants files to define namespaces or modules, so we choose the library to be a Geometry module, which implements the vector class to be called vector. Furthermore, when creating vector objects we would like to give the application program the ability to choose either Cartesian or polar form. This is can be done using discriminated unions. Discriminated unions allow us to tag values of possibly identical form, but they also lead to longer programs. Thus, we will also provide an additional constructor on implicit Cartesian form, since this is the most common representation of vectors.

· discriminated unions

A key point when defining libraries is to consider their interface with the application program. Hence, our second step is to write an application using the yet to be written library in order to get a feel for how such an interface could be. This is demonstrated in the application program ??.

```
Listing 1.17 vectorApp.fsx:
An application using the library in ??.

1 open Geometry
2 let v = vector(Cartesian (1.0,2.0))
3 let w = vector(Polar (3.2,1.8))
4 let p = vector()
5 let q = vector(1.2, -0.9)
6 let a = 1.5
7 printfn "%A * %A = %A" a v (a * v)
8 printfn "%A + %A = %A" v w (v + w)
9 printfn "vector() = %A" p
10 printfn "vector(1.2, -0.9) = %A" q
11 printfn "v.dir = %A" v.dir
12 printfn "v.len = %A" v.len
```

The application of the vector class seems natural, makes use of the optional discriminated unions, uses the infix operators "+" and "*" in a manner close to standard arithmetic, and interacts smoothly with the printf family. Thus, we have further sketched requirements to the library with the emphasis on application.

After a couple of trials, our library implementation has ended up as shown in ??.

Listing 1.18 vector.fs: A library serving the application in ??. module Geometry type Coordinate = Cartesian of float * float // (x, y) | Polar of float * float // (dir, len) type vector(c : Coordinate) = let (_x, _y, _dir, _len) = match c with Cartesian $(x, y) \rightarrow$ (x, y, atan2 y x, sqrt (x * x + y * y))| Polar (dir, len) when len \geq = 0.0 -> (len * cos dir, len * sin dir, dir, len) | Polar (dir, _) -> failwith "Negative length in polar representation." new(x : float, y : float) = vector(Cartesian (x, y)) new() =vector(Cartesian (0.0, 0.0)) $member this.x = _x$ member this.y = _y member this.len = _len member this.dir = _dir static member val left = "(" with get, set static member val right = ")" with get, set static member val sep = ", " with get, set static member (*) (a : float, v : vector) : vector = vector(Polar (v.dir, a * v.len)) static member (*) (v : vector, a : float) : vector = static member (+) (v : vector, w : vector) : vector = vector(Cartesian (v.x + w.x, v.y + w.y)) override this.ToString() = sprintf "%s%A%s%A%s" vector.left this.x vector.sep this.y vector.right

Realizations achieved during writing this code are: Firstly, in order to implement a vector class using discriminated unions, we had to introduce a constructor with helper variables $_{\tt x}$, $_{\tt y}$, etc. The consequence is that the Cartesian and polar representation is evaluated once and only once every time an object is created. Unfortunately, discriminated unions do not implement guards on subsets, so we still have to cast an exception when the application attempts to create an object with a negative length. Secondly, for the ToString override we have implemented static members for typesetting vectors, since it seems more appropriate that all vectors should be typeset identically. Changing typesetting thus respects dynamic scope.

The output of our combined library and application is shown in ??.

Listing 1.19: Compiling and running the code from ?? and ??.

\$ fsharpc --nologo vector.fs vectorApp.fsx && mono vectorApp.exe 2 1.5 * (1.0, 2.0) = (1.5, 3.0) 3 (1.0, 2.0) + (-1.796930596, -0.1050734582) = (-0.7969305964,

vector() = (0.0, 0.0) vector(1.2, -0.9) = (1.2, -0.9)

v.dir = 1.107148718 v.len = 2.236067977

1.894926542)

The output is as expected, and for the vector class, our solution seems to be a good compromise between versatility and syntactical bloating.