F# is tuned to work with collections of data, and there are several built-in types of collections with various properties making them useful for different tasks. Examples include strings, lists, and arrays. Strings were discussed in ?? and will be revisited here in more details

The data structures discussed below all have operators, properties, methods, and modules to help you write elegant programs using them.

Properties and methods are common object-oriented terms used in conjunction with the discussed functionality. They are synonymous with values and functions and will be discussed in ??. Properties and methods for a value or variable are called using the dot notation, i.e., with the "."-lexeme. For example, "abcdefg".Length is a property and is equal to the length of the string, and "abcdefg".ToUpper() is a method and creates a new string where all characters have been converted to upper case.

The data structures also have accompanying modules with a wealth of functions and where some are mentioned here. Further, the data structures are all implemented as classes offering even further functionality. The modules are optimized for functional programming, see ??—??, while classes are designed to support object-oriented programming, see ??—??.

In the following, a brief overview of many properties, methods, and functions is given by describing their name and type-definition, and by giving a short description and an example of their use. Several definitions are general and works with many different types. To describe this we will use the notation of generic types, see ??. The name of a generic type starts with the "'" lexeme, such as 'T. The implication of the appearance of a generic type in, e.g., a function's type-definition, is that the function may be used with any real type such as int or char. If the same generic type name is used in several places in the type-definition, then the function must use a real type consistently. For example, The List.fromArray function has type arr:'T [] -> 'T list, meaning that it takes an array of some type and returns a list of the same type.

See the F# Language Reference at https://docs.microsoft.com/en-us/dotnet/fsharp/ for a full description of all available functionality including variants of those included here.

1.1 Strings

Strings have been discussed in ??, the content of which will be briefly revisited here followed by a description of some of the many supporting built-in functions in F# on strings.

A string is a sequence of characters. Each character is represented using UTF-16, see ?? for further details on the unicode standard. The type string is an alias for System.string. String literals are delimited by double quotation marks "" and inside the delimiters, character escape sequences are allowed (see ??), which are replaced by the corresponding character code. Examples are "This is a string", "\tTabulated string", "A \"quoted\" string", and "". Strings may span several lines, and new lines inside strings are part of the string unless the line is ended with a backslash. Strings may be verbatim by preceding the string with "@", in which case escape sequences are not replaced, but two double quotation marks are an escape sequence which is replaced by a one double quotation mark. Examples of "@"-verbatim strings are: @"This is a string", @"\tNon-tabulated string", @"A ""quoted"" string", and @"". Alternatively, a verbatim string may be delimited by three double quotation marks. Examples of """"-verbatim strings are: """This is a string""", """\tNon-tabulated string""", """A "quoted" string""", and """".
Strings may be indexed using the . [] notation, as demonstrated in ??.

1.1.1 String Properties and Methods

Strings have a few properties which are values attached to each string and accessed using the "." notation. The only to be mentioned here is:

IndexOf(): str:string -> int. Returns the index of the first occurrence of s or -1, if str does not appear in the string.

```
Listing 1.1: IndexOf()

1 > "Hello World".IndexOf("World");;
2 val it : int = 6
```

Length: int. Returns the length of the string.

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```
Listing 1.2: Length

| > "abcd".Length;;
| val it : int = 4
```

ToLower(): unit -> string. Returns a copy of the string where each letter has been converted to lower case.

```
Listing 1.3: ToLower()

1 > "aBcD".ToLower();;

2 val it : string = "abcd"
```

ToUpper(): unit -> string. Returns a copy of the string where each letter has been converted to upper case.

```
Listing 1.4: ToUpper()

1 > "aBcD".ToUpper();;
2 val it : string = "ABCD"
```

Trim(): unit -> string. Returns a copy of the string where leading and trailing whitespaces have been removed.

```
Listing 1.5: Trim()

1 > " Hello World ".Trim();;
2 val it : string = "Hello World"
```

Split(): unit -> string []. Splits a string of words separated by spaces into an array of words. See Section 1.3 for more information about arrays.

```
Listing 1.6: Split()

1 > "Hello World".Split();;
2 val it : string [] = [|"Hello"; "World"|]
```

1.1.2 The String Module

The String module offers many functions for working with strings. Some of the most powerful ones are listed below, and they are all higher-order functions.

String.collect: f:(char -> string) -> str:string -> string. Creates a new string whose characters are the results of applying f to each of the characters of str and concatenating the resulting strings.

```
Listing 1.7: String.collect

> String.collect (fun c -> (string c) + ", ") "abc";;

val it : string = "a, b, c, "
```

String.exists: f:(char -> bool) -> str:string -> bool. Returns true if any character in str evaluates to true when using f.

```
Listing 1.8: String.exists

1 > String.exists (fun c -> c = 'd') "abc";;
2 val it : bool = false
```

String.forall: f:(char -> bool) -> str:string -> bool. Returns true if all characters in str evalutes to true when using f.

```
Listing 1.9: String.forall

1 > String.forall (fun c -> c < 'd') "abc";;
2 val it : bool = true
```

String.init: n:int -> f:(int -> string) -> string. Creates a new string with length n and whose characters are the result of applying f to each index of that string.

```
Listing 1.10: String.init

1 > String.init 5 (fun i -> (string i) + ", ");;
2 val it : string = "0, 1, 2, 3, 4, "
```

String.iter: f:(char -> unit) -> str:string -> unit. Applies f to each char-

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acter in str.

```
Listing 1.11: String.iter

> String.iter (fun c -> printfn "%c" c) "abc";;
a
b
c
val it : unit = ()
```

String.map: f:(char -> char) -> str:string -> string. Creates a new string whose characters are the results of applying f to each of the characters of str.

```
Listing 1.12: String.map

1 > let toUpper c = c + char (int 'A' - int 'a')
2 - String.map toUpper "abcd";;
3 val toUpper : c:char -> char
4 val it : string = "ABCD"
```

1.2 Lists

Lists are unions of immutable values of the same type. A list can be expressed as a sequence expression,

```
Listing 1.13: The syntax for a list using the sequence expression.
```

```
1 [[<expr>{; <expr>}]]
```

For example, [1; 2; 3] is a list of integers, ["This"; "is"; "a"; "list"] is a list of strings, [(fun x -> x); (fun x -> x*x)] is a list of functions, and [] is the empty list. Lists may also be given as ranges,

Listing 1.14: The syntax for a list using the range expressions.

```
1 [<expr> .. <expr> [.. <expr>]]
```

where <expr> in range expressions must be of integers, floats, or characters. Examples

are [1 .. 5], [-3.0 .. 2.0], and ['a' .. 'z']. Range expressions may include a step size, thus, [1 .. 2 .. 10] evaluates to [1; 3; 5; 7; 9].

A list type is identified with the *list* keyword, such that a list of integers has the type int list. Like strings, lists may be indexed using the ". []" notation, the lengths of lists is retrieved using the *Length* property, and we may test whether a list is empty by using the *IsEmpty* property. These features are demonstrated in Listing 1.15.

Listing 1.15 listIndexing.fsx: Lists are indexed as strings and has a Length property.

```
let printList (lst : int list) : unit =
  for i = 0 to lst.Length - 1 do
    printf "%A " lst.[i]
  printfn ""

let lst = [3; 4; 5]
  printfn "lst = %A, lst.[1] = %A" lst lst.[1]
  printfn "lst.Length = %A, lst.isEmpty = %A" lst.Length
    lst.IsEmpty
  printList lst

$ fsharpc --nologo listIndexing.fsx && mono
    listIndexing.exe
lst = [3; 4; 5], lst.[1] = 4
lst.Length = 3, lst.isEmpty = false
3 4 5
```

F# implements lists as linked lists, as illustrated in Figure 1.1. As a consequence, in-



Figure 1.1: A list is a linked list: Here is illustrated the linked list of ["This"; "is"; "a"; "list"].

dexing element i has computational complexity $\mathcal{O}(i)$. The computational complexity of an operation is a description of how long a computation will take without considering the hardware it is performed on. The notation is sometimes called Big-O notation or Landau notation. In the present case, the complexity is $\mathcal{O}(i)$, which means that the complexity is linear in i and indexing element i+1 takes 1 unit longer than indexing element i when i is very large. The size of the unit is on purpose unspecified and depends on implementation and hardware details. Nevertheless, Big-O notation

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is a useful tool for reasoning about the efficiency of an operation. F# has access to the list's elements only by traversing the list from its beginning. I.e., to obtain the value of element i, F# starts with element 0, follows the link to element 1 and so on, until element i is reached. To reach element i+1 instead, we would need to follow 1 more link, and assuming that following a single link takes some constant amount of time we find that the computational complexity is $\mathcal{O}(i)$. Compared to arrays, to be discussed below, this is slow, which is why **indexing lists should be avoided.**

Notice especially that lists are zero-indexed, and thus, the last element in a list lst is lst.Length -1. This is a very common source of error! Therefore, indexing in lists using for-loops is supported using a special notation with the *in* keyword,

```
Listing 1.16: For-in loop with in expression.

for <ident> in <list> do <bodyExpr> [done]
```

In for-in loops, the loop runs through each element of the st>, and assigns it to the identifier <ident>. This is demonstrated in Listing 1.17.

```
Listing 1.17 listFor.fsx:

The - loops are preferred over - loops.

1 let printList (lst : int list) : unit =

for elm in lst do

printf "%A " elm

printfn ""

5 printList [3; 4; 5]

1 $ fsharpc --nologo listFor.fsx && mono listFor.exe

2 3 4 5
```

Using for-in-expressions remove the risk of off-by-one indexing errors, and thus, for-in is to be preferred over for-to.

Lists support slicing identically to strings, as demonstrated in Listing 1.18.

Listing 1.18: Examples of list slicing. Compare with ??.

Lists may be concatenated using either the "@" concatenation operator or the "::" cons operators. The difference is that "@" concatenates two lists of identical types, while "::" concatenates an element and a list of identical types. This is demonstrated in Listing 1.19.

val it : char list = ['a'; 'b'; 'c'; 'd'; 'e'; 'f'; 'g']

Listing 1.19: Examples of list concatenation.

val it : char list = ['b'; 'c'; 'd']

> lst.[1..3];;

> lst.[*];;

Since lists are represented as linked lists, the cons operator is very efficient and has computational complexity $\mathcal{O}(1)$, while concatenation has computational complexity $\mathcal{O}(n)$, where n is the length of the first list.

It is possible to make multidimensional lists as lists of lists, as shown in Listing 1.20.

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Listing 1.20 listMultidimensional.fsx:

A ragged multidimensional list, built as lists of lists, and its indexing.

```
let a = [[1;2];[3;4;5]]
let row = a.Item 0 in printfn "%A" row
let elm = row.Item 1 in printfn "%A" elm
let elm = (a.Item 0).Item 1 in printfn "%A" elm

fsharpc --nologo listMultidimensional.fsx
mono listMultidimensional.exe
[1; 2]
2
2
2
```

The example shows a ragged multidimensional list, since each row has a different number of elements. This is also illustrated in Figure 1.2.

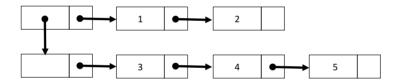


Figure 1.2: A list is a ragged linked list: Here is illustrated the linked list of [[1;2];[3;4;5]].

The indexing of a particular element is slow due to the linked list implementation of lists, which is why arrays are often preferred for two- and higher-dimensional data structures, see Section 1.3.

1.2.1 List Properties

Lists support a number of properties, some of which are listed below.

Head: Returns the first element of a list.

```
Listing 1.21: Head

1 > [1; 2; 3]. Head;;
2 val it : int = 1
```

IsEmpty: Returns true if the list is empty.

```
Listing 1.22: IsEmpty

1 > [1; 2; 3].IsEmpty;;
2 val it : bool = false
```

Length: Returns the number of elements in the list.

```
Listing 1.23: Length

1 > [1; 2; 3].Length;;
2 val it : int = 3
```

Tail: Returns the list, except for its first element.

```
Listing 1.24: Tail

1 > [1; 2; 3].Tail;;
2 val it : int list = [2; 3]
```

1.2.2 The List Module

The built-in List module contains a wealth of functions for lists, some of which are briefly summarized below:

List.collect: f:('T -> 'U list) -> lst:'T list -> 'U list. Applies f to each element in lst and return a concatenated list of the results.

```
Listing 1.25: List.collect

| Listing 1.25: List.collect | State | Sta
```

List.contains: elm: 'T -> lst: 'T list -> bool. Returns true or false depending on whether or not elm is contained in lst.

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Listing 1.26: List.contains 1 > List.contains 3 [1; 2; 3];; 2 val it : bool = true

List.filter: f:('T -> bool) -> lst:'T list -> 'T list. Returns a new list with all the elements of lst for which f evaluates to true.

```
Listing 1.27: List.filter

1 > List.filter (fun x -> x % 2 = 1) [0 .. 9];;
2 val it : int list = [1; 3; 5; 7; 9]
```

List.find: f:('T -> bool) -> lst:'T list -> 'T. Returns the first element of lst for which f is true.

```
Listing 1.28: List.find

1 > List.find (fun x -> x % 2 = 1) [0 .. 9];;
2 val it : int = 1
```

List.findIndex: f:('T -> bool) -> lst:'T list -> int. Returns the index of the first element of lst for which f is true.

```
Listing 1.29: List.findIndex

1 > List.findIndex (fun x -> x = 'k') ['a' .. 'z'];;
2 val it : int = 10
```

List.fold: f:('S -> 'T -> 'S) -> elm:'S -> lst:'T list -> 'S. Updates an accumulator iteratively by applying f to each element in lst. The initial value of the accumulator is elm. For example, when lst consists of n+1 elements List.fold calculates:

```
f (... (f (f elm lst.[0]) lst.[1]) ...) lst.[n].
```

Listing 1.30: List.fold

```
1 > let addSquares acc elm = acc + elm*elm
2 - List.fold addSquares 0 [0 .. 9];;
3 val addSquares : acc:int -> elm:int -> int
4 val it : int = 285
```

List.foldBack: $f:('T \rightarrow 'S \rightarrow 'S) \rightarrow lst:'T list \rightarrow elm:'S \rightarrow 'S$.

Updates an accumulator iteratively backwards by applying f to each element in lst. The initial value of the accumulator is elm. For exampel, when lst consists of n+1 elements List.foldBack calculates:

```
f lst.[0] (f lst.[1] (...(f lst.[n] elm) ...)).
```

Listing 1.31: List.foldBack

```
1 > let addSquares elm acc = acc + elm*elm
2 - List.foldBack addSquares [0 .. 9] 0;;
3 val addSquares : elm:int -> acc:int -> int
4 val it : int = 285
```

List.forall: f:('T -> bool) -> lst:'T list -> bool. Returns true if all elements in lst are true when f is applied to them.

```
Listing 1.32: List.forall
```

```
> List.forall (fun x -> x % 2 = 1) [0 .. 9];;
val it : bool = false
```

List.head: lst:'T list -> int. Returns the first element in lst. An exception is raised if lst is empty. See ?? for more on exceptions.

```
Listing 1.33: List.head
```

```
1 > List.head [1; -2; 0];;
2 val it : int = 1
```

List.init: m:int -> f:(int -> 'T) -> 'T list. Create a list with m elements and whose value is the result of applying f to the index of the element.

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Listing 1.34: List.init 1 > List.init 10 (fun i -> i * i);; 2 val it : int list = [0; 1; 4; 9; 16; 25; 36; 49; 64; 81]

List.isEmpty: lst:'T list -> bool. Returns true if lst is empty.

```
Listing 1.35: List.isEmpty

1 > List.isEmpty [1; 2; 3];;
2 val it : bool = false
```

List.iter: f:('T -> unit) -> lst:'T list -> unit. Applies f to every element in lst.

```
Listing 1.36: List.iter

1 > List.iter (fun x -> printfn "%A " x) [0; 1; 2];;
2 0
3 1
4 2
5 val it : unit = ()
```

List.map: f:('T -> 'U) -> lst:'T list -> 'U list. Returns a list as a concatenation of applying f to every element of lst.

```
Listing 1.37: List.map

1 > List.map (fun x -> x*x) [0 .. 9];;
2 val it : int list = [0; 1; 4; 9; 16; 25; 36; 49; 64; 81]
```

List.ofArray: arr:'T [] -> 'T list. Returns a list whose elements are the same as arr. See Section 1.3 for more on arrays.

```
Listing 1.38: List.ofArray

> List.ofArray [|1; 2; 3|];;
val it : int list = [1; 2; 3]
```

List.rev: lst:'T list -> 'T list. Returns a new list with the same elements as in lst but in reversed order.

```
Listing 1.39: List.rev

1 > List.rev [1; 2; 3];;
2 val it : int list = [3; 2; 1]
```

List.sort: lst:'T list -> 'T list. Returns a new list with the same elements as in lst but where the elements are sorted.

```
Listing 1.40: List.sort

1 > List.sort [3; 1; 2];;
2 val it : int list = [1; 2; 3]
```

List.tail: 'T list -> 'T list. Returns a new list identical to 1st but without its first element. An Exception is raised if 1st is empty. See ?? for more on exceptions.

```
Listing 1.41: List.tail

1 > List.tail [1; 2; 3];;
2 val it : int list = [2; 3]

3 > let a = [1; 2; 3] in List.tail a;;
5 val it : int list = [2; 3]
```

List.toArray: lst:'T list -> 'T []. Returns an array whose elements are the same as lst. See Section 1.3 for more on arrays.

1.3 Arrays

Listing 1.42: List.toArray 1 > List.toArray [1; 2; 3];; 2 val it : int [] = [|1; 2; 3|]

List.unzip: lst:('T1 * 'T2) list -> 'T1 list * 'T2 list. Returns a pair of lists of all the first elements and all the second elements of lst, respectively.

```
Listing 1.43: List.unzip

1 > List.unzip [(1, 'a'); (2, 'b'); (3, 'c')];;
2 val it : int list * char list = ([1; 2; 3], ['a'; 'b'; 'c'])

3 4 >
```

List.zip: lst1: 'T1 list -> lst2: 'T2 list -> ('T1 * 'T2) list.

Returns a list of pairs, where elements in lst1 and lst2 are iteratively paired.

```
Listing 1.44: List.zip

| List.zip [1; 2; 3] ['a'; 'b'; 'c'];;
| val it : (int * char) list = [(1, 'a'); (2, 'b'); (3, 'c')]
```

1.3 Arrays

One dimensional *arrays*, or just arrays for short, are mutable lists of the same type and follow a similar syntax as lists. Arrays can be stated as a *sequence expression*,

```
Listing 1.45: The syntax for an array using the sequence expression.

[[[<expr>{; <expr>}]]]
```

E.g., [|1; 2; 3|] is an array of integers, [|"This"; "is"; "an"; "array"|] is an array of strings, [|(fun x -> x); (fun x -> x*x)|] is an array of functions, [||] is the empty array. Arrays may also be given as ranges,

Listing 1.46: The syntax for an array using the range expression.

```
[|<expr> .. <expr> [.. <expr>]|]
```

but arrays of range expressions must be of <expr> integers, floats, or characters. Examples are [|1 .. 5|], [|-3.0 .. 2.0|], and [|'a' .. 'z'|]. Range expressions may include a step size, thus, [|1 .. 2 .. 10|] evaluates to [|1; 3; 5; 7; 9|].

The array type is defined using the array keyword or alternatively the "[]" lexeme. Like strings and lists, arrays may be indexed using the ". []" notation. Arrays cannot be resized, but are mutable, as shown in Listing 1.47.

Listing 1.47 arrayReassign.fsx: Arrays are mutable in spite of the missing keyword.

```
let square (a : int array) =
   for i = 0 to a.Length - 1 do
        a.[i] <- a.[i] * a.[i]

let A = [| 1; 2; 3; 4; 5 |]
   printfn "%A" A
   square A
   printfn "%A" A

f sharpc --nologo arrayReassign.fsx && mono
        arrayReassign.exe
[|1; 2; 3; 4; 5|]
   [|1; 4; 9; 16; 25|]</pre>
```

Notice that in spite of the missing mutable keyword, the function square still has the side-effect of squaring all entries in A. F# implements arrays as chunks of memory and indexes arrays via address arithmetic. I.e., element i in an array, whose first element is in memory address α and whose elements fill β addresses each, is found at address $\alpha+i\beta$. Hence, indexing has computational complexity of $\mathcal{O}(1)$, but appending and prepending values to arrays and array concatenation requires copying the new and existing values to a fresh area in memory and thus has computational complexity $\mathcal{O}(n)$, where n is the total number of elements. Thus, indexing arrays is fast, but cons and concatenation is slow and should be avoided.

Arrays support *slicing*, that is, indexing an array with a range result in a copy of the array with values corresponding to the range. This is demonstrated in Listing 1.48.

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Listing 1.48: Examples of array slicing. Compare with Listing 1.18 and ??.

```
> let arr = [|'a' ... 'g'|];;
val arr : char [] = [|'a'; 'b'; 'c'; 'd'; 'e'; 'f'; 'g'|]

> arr.[0];;
val it : char = 'a'

> arr.[3];;
val it : char = 'd'

> arr.[3..];;
val it : char [] = [|'d'; 'e'; 'f'; 'g'|]

> arr.[..3];;
val it : char [] = [|'a'; 'b'; 'c'; 'd'|]

> arr.[1..3];;
val it : char [] = [|'b'; 'c'; 'd'|]

> arr.[*];;
val it : char [] = [|'a'; 'b'; 'c'; 'd'; 'e'; 'f'; 'g'|]
```

As illustrated, the missing start or end index imply from the first or to the last element, respectively.

Arrays do not have explicit operator support for appending and concatenation, instead the Array namespace includes an Array.append function, as shown in Listing 1.49.

Listing 1.49 arrayAppend.fsx:

Two arrays are appended with Array.append.

```
1 let a = [|1; 2;|]
2 let b = [|3; 4; 5|]
3 let c = Array.append a b
4 printfn "%A, %A, %A" a b c

1 $ fsharpc --nologo arrayAppend.fsx && mono arrayAppend.exe
2 [|1; 2|], [|3; 4; 5|], [|1; 2; 3; 4; 5|]
```

Arrays are reference types, meaning that identifiers are references and thus suffer

from aliasing, as illustrated in Listing 1.50.

Listing 1.50 arrayAliasing.fsx:

Arrays are reference types and suffer from aliasing.

```
1 let a = [|1; 2; 3|];
2 let b = a
3 a.[0] <- 0
4 printfn "a = %A, b = %A" a b;;

1 $ fsharpc --nologo arrayAliasing.fsx && mono arrayAliasing.exe
2 a = [|0; 2; 3|], b = [|0; 2; 3|]</pre>
```

1.3.1 Array Properties and Methods

Some important properties and methods for arrays are:

Clone(): 'T []. Returns a copy of the array.

Listing 1.51: Clone

```
1 > let a = [|1; 2; 3|];
2 - let b = a.Clone()
3 - a.[0] <- 0
4 - printfn "a = %A, b = %A" a b;;
5 a = [|0; 2; 3|], b = [|1; 2; 3|]
6 val a : int [] = [|0; 2; 3|]</pre>
```

Length: int. Returns the number of elements in the array.

val b : obj = [|1; 2; 3|]

val it : unit = ()

1.3 Arrays

1.3.2 The Array Module

There are quite a number of built-in procedures for arrays in the Array module, some of which are summarized below.

Array.append: arr1:'T [] -> arr2:'T [] -> 'T []. Creates an new array whose elements are a concatenated copy of arr1 and arr2.

```
Listing 1.53: Array.append

| Array.append [|1; 2;|] [|3; 4; 5|];;
| val it : int [] = [|1; 2; 3; 4; 5|]
```

Array.contains: elm:'T -> arr:'T [] -> bool. Returns true if arr contains elm.

```
Listing 1.54: Array.contains

1 > Array.contains 3 [|1; 2; 3|];;
2 val it : bool = true
```

Array.exists: f:('T -> bool) -> arr:'T [] -> bool. Returns true if any application of f evaluates to true when applied to the elements of arr.

```
Listing 1.55: Array.exists

1 > Array.exists (fun x -> x % 2 = 1) [|0 .. 2 .. 4|];;
2 val it : bool = false
```

Array.filter: f:('T -> bool) -> arr:'T [] -> 'T []. Returns an array of elements from arr who evaluate to true when f is applied to them.

```
Listing 1.56: Array.filter

1 > Array.filter (fun x -> x % 2 = 1) [|0 .. 9|];;
2 val it : int [] = [|1; 3; 5; 7; 9|]
```

Array.find: f:('T -> bool) -> arr:'T [] -> 'T. Returns the first element in arr for which f evaluates to true. The KeyNotFoundException exception is raised if no element is found. See ?? for more on exceptions.

Listing 1.57: Array.find > Array.find (fun x -> x % 2 = 1) [|0 .. 9|];; val it : int = 1

Array.findIndex: f:('T -> bool) -> arr:'T [] -> int. Returns the index of the first element in in arr for which f evaluates to true. If none are found, then the System.Collections.Generic.KeyNotFoundException exception is raised. See ?? for more on exceptions.

```
Listing 1.58: Array.findIndex

1 > Array.findIndex (fun x -> x = 'k') [|'a' .. 'z'|];;
2 val it : int = 10
```

Array.fold: f:('S -> 'T -> 'S) -> elm:'S -> arr:'T [] -> 'S. Updates an accumulator iteratively by applying f to each element in arr. The initial value of the accumulator is elm. For example, when arr consists of n+1 elements Array.fold calculates:

```
f (... (f (f elm arr.[0]) arr.[1]) ...) arr.[n].
```

Listing 1.59: Array.fold

```
> let addSquares acc elm = acc + elm*elm

- Array.fold addSquares 0 [|0 .. 9|];;

val addSquares : acc:int -> elm:int -> int

val it : int = 285
```

Array.foldBack: f:('T -> 'S -> 'S) -> arr:'T [] -> elm:'S -> 'S. Updates an accumulator iteratively backwards by applying f to each element in arr. The initial value of the accumulator is elm. For exampel, when arr consists of n+1 elements Array.foldBack calculates:

```
f arr.[0] (f arr.[1] (...(f arr.[n] elm) ...)).
```

21 1.3 Arrays

Listing 1.60: Array.foldBack 1 > let addSquares elm acc = acc + elm*elm 2 - Array.foldBack addSquares [|0 .. 9|] 0;; 3 val addSquares : elm:int -> acc:int -> int 4 val it : int = 285

Array.forall: f:('T -> bool) -> arr:'T [] -> bool. Returns true if f evaluates to true for every element in arr.

```
Listing 1.61: Array.forall

1 > Array.forall (fun x -> (x % 2 = 1)) [|0 .. 9|];;
2 val it : bool = false
```

Array.init: m:int -> f:(int -> 'T) -> 'T []. Create an array with m elements and whose value is the result of applying f to the index of the element.

```
Listing 1.62: Array.init

| Array.init 10 (fun i -> i * i);;
| val it : int [] = [|0; 1; 4; 9; 16; 25; 36; 49; 64; 81|]
```

Array.isEmpty: arr:'T [] -> bool. Returns true if arr is empty.

```
Listing 1.63: Array.isEmpty

1 > Array.isEmpty [||];;
2 val it : bool = true
```

Array.iter: f:('T -> unit) -> arr:'T [] -> unit. Applies f to each element of arr.

Listing 1.64: Array.iter 1 > Array.iter (fun x -> printfn "%A " x) [|0; 1; 2|];; 2 0 3 1 4 2 5 val it : unit = ()

Array.map: f:('T -> 'U) -> arr:'T [] -> 'U []. Creates an new array whose elements are the results of applying f to each of the elements of arr.

```
Listing 1.65: Array.map

> Array.map (fun x -> x * x) [|0 .. 9|];;

val it : int [] = [|0; 1; 4; 9; 16; 25; 36; 49; 64; 81|]
```

Array.ofList: lst:'T list -> 'T []. Creates an array whose elements are copied from lst.

```
Listing 1.66: Array.ofList

1 > Array.ofList [1; 2; 3];;
2 val it : int [] = [|1; 2; 3|]
```

Array.rev: arr:'T [] -> 'T []. Creates a new array whose elements are identical to arr but in reverse order.

```
Listing 1.67: Array.rev

| Array.rev [|1; 2; 3|];;
| val it : int [] = [|3; 2; 1|]
```

Array.sort: arr:'T[] -> 'T []. Creates a new array with the same elements as in arr but in sorted order

Array.toList: arr:'T [] -> 'T list. Creates a new list whose elements are copied from arr.

```
Listing 1.69: Array.toList

1 > Array.toList [|1; 2; 3|];;
2 val it : int list = [1; 2; 3]
```

Array.unzip: arr:('T1 * 'T2) [] -> 'T1 [] * 'T2 []. Returns a pair of arrays of all the first elements and all the second elements of arr, respectively.

```
Listing 1.70: Array.unzip

| Array.unzip [|(1, 'a'); (2, 'b'); (3, 'c')|];;
| val it : int [] * char [] = ([|1; 2; 3|], [|'a'; 'b'; 'c'|])
```

Array.zip: arr1:'T1 [] -> arr2:'T2 [] -> ('T1 * 'T2) []. Returns a list of pairs, where elements in arr1 and arr2 are iteratively paired.

```
Listing 1.71: Array.zip

| Array.zip [|1; 2; 3|] [|'a'; 'b'; 'c'|];;
| val it : (int * char) [] = [|(1, 'a'); (2, 'b'); (3, 'c')|]
```

1.4 Multidimensional Arrays

Multidimensional arrays can be created as arrays of arrays (of arrays ...). These are known as jagged arrays, since there is no inherent guarantee that all sub-arrays are of the same size. The example in Listing 1.72 is a jagged array of increasing width.

Listing 1.72 arrayJagged.fsx:

An array of arrays. When row lengths are of non-equal elements, then it is a jagged array.

```
1 let arr = [|[|1|]; [|1; 2|]; [|1; 2; 3|]|]
2
3 for row in arr do
4   for elm in row do
5     printf "%A " elm
6     printf "\n"

1 $ fsharpc --nologo arrayJagged.fsx && mono arrayJagged.exe
2 1
3 1 2
4 1 2 3
```

Indexing arrays of arrays is done sequentially, in the sense that in the above example, the number of outer arrays is a.Length, a.[i] is the i'th array, the length of the i'th array is a.[i].Length, and the j'th element of the i'th array is thus a.[i].[j]. Often 2-dimensional rectangular arrays are used, which can be implemented as a jagged array, as shown in Listing 1.73.

Listing 1.73 arrayJaggedSquare.fsx: A rectangular array.

```
let pownArray (arr : int array array) p =
  for i = 1 to arr.Length - 1 do
    for j = 1 to arr.[i].Length - 1 do
      arr.[i].[j] <- pown arr.[i].[j] p
let printArrayOfArrays (arr : int array array) =
  for row in arr do
    for elm in row do
      printf "%3d " elm
    printf "\n"
let A = [|[|1 ... 4|]; [|1 ... 2 ... 7|]; [|1 ... 3 ... 10|]|]
pownArray A 2
printArrayOfArrays A
$ fsharpc --nologo arrayJaggedSquare.fsx && mono
  arrayJaggedSquare.exe
  1
      2
         3
  1
      9
         25
             49
  1
     16
         49 100
```

Note that the for-in cannot be used in pownArray, e.g.,

for row in arr do for elm in row do elm <- pown elm p done done,

since the iterator value elm is not mutable, even though arr is an array.

Square arrays of dimensions 2 to 4 are so common that F# has built-in modules for their support. Here, we will describe Array2D. The workings of Array3D and Array4D are very similar. A generic Array2D has type 'T [,], and it is indexed also using the [,] notation. The Array2D.length1 and Array2D.length2 functions are supplied by the Array2D module for obtaining the size of an array along the first and second dimension. Rewriting the with jagged array example in Listing 1.73 to use Array2D gives a slightly simpler program, which is shown in Listing 1.74.

Listing 1.74 array2D.fsx:

Creating a 3 by 4 rectangular array of integers.

```
let arr = Array2D.create 3 4 0
for i = 0 to (Array2D.length1 arr) - 1 do
for j = 0 to (Array2D.length2 arr) - 1 do
arr.[i,j] <- j * Array2D.length1 arr + i
printfn "%A" arr

$ fsharpc --nologo array2D.fsx && mono array2D.exe
[[0; 3; 6; 9]
[1; 4; 7; 10]
[2; 5; 8; 11]]</pre>
```

Note that the printf supports direct printing of the 2-dimensional array. Array2D arrays support slicing. The "*" lexeme is particularly useful to obtain all values along a dimension. This is demonstrated in Listing 1.75.

Listing 1.75: Examples of Array2D slicing. Compare with Listing 1.74.

```
> let arr = Array2D.init 3 4 (fun i j -> i + 10 * j);;
val arr : int [,] = [[0; 10; 20; 30]
                     [1; 11; 21; 31]
                      [2; 12; 22; 32]]
> arr.[2,3];;
val it : int = 32
> arr.[1..,3..];;
val it : int [,] = [[31]
                     [32]]
> arr.[..1,*];;
val it : int [,] = [[0; 10; 20; 30]
                     [1; 11; 21; 31]]
> arr.[1,*];;
val it : int [] = [|1; 11; 21; 31|]
> arr.[1..1,*];;
val it : int [,] = [[1; 11; 21; 31]]
```

Note that in almost all cases, slicing produces a sub-rectangular 2 dimensional array, except for arr. [1,*], which is an array, as can be seen by the single "[". In contrast,

A. [1..1,*] is an Array2D. Note also that printfn typesets 2 dimensional arrays as [[...]] and not [|[| ... |]|], which can cause confusion with lists of lists.

Multidimensional arrays have the same properties and methods as arrays, see Section 1.3.1.

1.4.1 The Array2D Module

There are quite a number of built-in procedures for arrays in the Array2D namespace, some of which are summarized below.

copy: arr:'T [,] -> 'T [,]. Creates a new array whose elements are copied from arr.

create: m:int -> n:int -> v:'T -> 'T [,]. Creates an m by n array whose elements are set to v.

```
Listing 1.77: Array2D.create

1 > Array2D.create 2 3 3.14;;
2 val it : float [,] = [[3.14; 3.14; 3.14]
3 [3.14; 3.14; 3.14]]
```

init: m:int -> n:int -> f:(int -> int -> 'T) -> 'T [,]. Creates an m by n array whose elements are the result of applying f to the index of an element.

iter: f:('T -> unit) -> arr:'T [,] -> unit. Applies f to each element of arr.

```
1 > let arr = Array2D.init 3 4 (fun i j -> i + 10 * j)
2 - Array2D.iter (fun elm -> printf "%A " elm) arr
3 - printfn "";;
4 0 10 20 30 1 11 21 31 2 12 22 32
5 val arr : int [,] = [[0; 10; 20; 30]
```

[1; 11; 21; 31]

[2; 12; 22; 32]]
val it : unit = ()

Listing 1.79: Array2D.iter

length1: arr: 'T [,] -> int. Returns the length the first dimension of arr.

Listing 1.80: Array2D.length1

```
> let arr = Array2D.create 2 3 0.0 in Array2D.length1
arr;;
val it : int = 2
```

length2: arr: 'T [,] -> int. Returns the length of the second dimension of arr.

Listing 1.81: Array2D.forall length2

```
1 > let arr = Array2D.create 2 3 0.0 in Array2D.length2
    arr;;
2 val it : int = 3
```

map: f:('T -> 'U) -> arr:'T [,] -> 'U [,]. Creates a new array whose elements are the results of applying f to each of the elements of arr.

###