# Learning to Program with F#

Jon Sporring

Department of Computer Science, University of Copenhagen

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# 1 | Preface

This book has been written as an introduction to programming for novice programmers. It is used in the first programming course at the University of Copenhagen's bachelor in computer science program. It has been typeset in LATEX, and all programs have been developed and tested in Mono version 5.10.1.57.

Jon Sporring Associate Professor, Ph.d. Department of Computer Science, University of Copenhagen 2018-09-20

# 2 | Introduction

Programming is a creative process in which exciting problems may be solved and new tools and applications may be created. With programming skills, you can create high-level applications to run on a mobile device that interact with other users, databases, and artificial intelligence; you may create programs that run on supercomputers for simulating weather systems on alien planets or social phenomena in the internet economy; and you may create programs that run on small custom-made hardware for controlling your home appliances.

## 2.1. How to Learn to Solve Problems by Programming

In order to learn how to program, there are a couple of steps that are useful:

- 1. Choose a programming language: A programming language, such as F#, is a vocabulary and a set of grammatical rules for instructing a computer to perform a certain task. It is possible to program without a concrete language, but your ideas and thoughts must still be expressed in some fairly rigorous way. Theoretical computer scientists typically do not rely on computers nor programming languages but uses mathematics to prove properties of algorithms. However, most computer scientists program using a computer, and with a real language you have the added benefit of checking your algorithm, and hence your thoughts, rigorously on a real computer. This book teaches a subset of F#. The purpose is not to be a reference guide to this language but to use it as a vessel to teach you, the reader, how to convert your ideas into programs.
- 2. Learn the language: A computer language is a structure for thought, and it influences which thoughts you choose to express as a program, and how you choose to do it. Any conversion requires you to acquire a sufficient level of fluency in order for you to be able to make programs. You do not need to be a master in F# nor to know every corner of the language, and you will expand your knowledge as you expose yourself to solving problems in the language, but you must invest an initial amount of time and energy in order to learn the basics of the language. This book aims at getting you started quickly, which is why we intentionally teach just a small subset of F#. On the internet and through other works you will be able to learn much more.
- 3. Practice: In order to be a good programmer, the most essential step is: practice, practice, practice! It has been estimated that to master anything, then you have to have spent at least 10000 hours practicing, so get started logging hours! It of course matters, how you practice. This book teaches a number of different programming themes. The point is that programming is thinking, and the scaffold you use shapes

#### 2. Introduction

your thoughts. It is therefore important to recognize this scaffold and to have the ability to choose one which suits your ideas and your goals best. The best way to expand your abilities is to sharpen your present abilities, push yourself into new territory, and try something new. Do not be afraid to make errors or be frustrated at first. These are the experiences that make you grow.

4. Solve real problems: I have found that using my programming skills in real situations with customers demanding specific solutions, has forced me to put the programming tools and techniques that I use into perspective. Sometimes a task requires a cheap and fast solution, other times customers want a long-perspective solution with bug fixes, upgrades, and new features. Practicing solving real problems helps you strike a balance between the two when programming. It also allows makes you a more practical programmer, by allowing you to recognize its applications in your everyday experiences. Regardless, real problems create real programmers.

#### 2.2. How to Solve Problems

Programming is the act of solving a problem by writing a program to be executed on a computer. A general method for solving problems, given by George Pólya [9] and adapted to programming, is:

**Understand the problem:** To solve any problem it is crucial that the problem formulation is understood. What is to be solved? Do you understand everything in the description of the problem? Is all information for finding the solution available or is something missing?

**Design a plan:** Good designs lead to programs are faster to implement, easier to find errors in, and easier to update in the future. Before you start typing a program consider things like: What are the requirements and constraints for the program? Which components should the program have? How are these components supposed to work together? Designing often involves drawing a diagram of the program and writing program sketches on paper.

Implement the plan: Implementation is the act of transforming a program design into code. A crucial part of any implementation is choosing which programming language to use. Furthermore, the solution to many problems will have a number of implementations which vary in how much code they require, to which degree they rely on external libraries, which programming style they are best suited for, what machine resources they require, and how long time they take to run on a computer. With a good design, the coding is usually easy, since the design will have uncovered the major issues and found solutions for these, but sometimes implementation reveals new problems, which require rethinking the design. Most often the implementation step also require a careful documentation of key aspects of the code, e.g., a user manual for the user, and internal notes for fellow programmers that are to maintain and update the code in the future.

Reflect on the result: A crucial part of any programming task is ensuring that the program solves the problem sufficiently. Ask yourself questions such as: What are the program's errors, is the documentation of the code sufficient and relevant for its intended use? Is the code easily maintainable and extendable by other programmers? Which parts of your method would you avoid or replicate in future programming sessions? Can you reuse some of the code you developed in other programs?

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Programming is a very complicated process, and Pólya's list is a useful guide but not a fail-safe approach. Always approach problem-solving with an open mind.

## 2.3. Approaches to Programming

This book focuses on several fundamentally different approaches to programming:

Imperative programming emphasizes how a program shall accomplish a solution and focusses less on what the solution is. A cooking recipe is an example of the spirit of imperative programming, where the recipe emphasizes what should be done in each step rather than describing the result. For example, a recipe for bread might tell you to first mix yeast and water, then add flour, etc. In imperative programming what should be done are called statements and in the recipe analogy, the steps are the statements. Statements influence the computer's states, in the same way that adding flour changes the state of our dough. Almost all computer hardware is designed to execute low-level programs written in imperative style. Imperative programming builds on the Turing machine [10]. As a historical note, the first major language was FORTRAN [6] which emphasized an imperative style of programming.

· imperative programming

· statement

Declarative programming emphasizes what a program shall accomplish but not how. We will consider Functional programming as an example of declarative programming. A functional programming language evaluates functions and avoids state changes. The program consists of expressions instead of statements. As an example, the function  $f(x) = x^2$  takes a number x, evaluates the expression  $x^2$ , and returns the resulting number. Everything about the function may be characterized by the relation between the input and output values. Functional programming has its roots in lambda calculus [1]. The first language emphasizing functional programming was Lisp [7].

· declarative programming

 $\begin{array}{c} \cdot \, \text{functional} \\ \, \text{programming} \end{array}$ 

 $\cdot \ function$ 

 $\cdot \ expression$ 

· structured programming

Structured programming emphasizes organization of programs in units of code and data. For example, a traffic light may consist of a state (red, yellow, green), and code for updating the state, i.e., switching from one color to the next. We will focus on Object-oriented programming as the example of structured programming. Object-oriented programming is a type of programming, where the code and data are structured into objects. E.g., a traffic light may be an object in a traffic-routing program. The first object-oriented programming language was Simula 67 developed by Dahl and Nygaard at the Norwegian Computing Center in Oslo [2].

**Event-driven programming**, which is often used when dynamically interacting with the

are often programmed using call-back functions, which are small programs that are

· Object-oriented programming

 $\cdot \ object$ 

· event-driven programming

real world. This is useful, for example, when programming graphical user interfaces, where programs will often need to react to a user clicking on the mouse or to text arriving from a web-server to be displayed on the screen. Event-driven programs

 $\cdot$  call-back functions

Most programs do not follow a single programming paradigm as, e.g., one of the above, but are a mix. Nevertheless, this book will treat each paradigm separately to emphasize its advantages and disadvantages.

ready to run when events occur.

## 2.4. Why Use F#

This book uses F#, also known as Fsharp, which is a functional first programming language, meaning that it is designed as a functional programming language that also supports imperative and object-oriented programming. It was originally developed for Microsoft's .Net platform but is available as open source for many operating systems through Mono. As an introduction to programming, F# is a young programming language still under development, with syntax that at times is a bit complex. Still, it offers a number of advantages:

- Interactive and compile mode: F# has an interactive and a compile mode of operation. In interactive mode you can write code that is executed immediately in a manner similar to working with a calculator, while in compile mode you combine many lines of code possibly in many files into a single application, which is easier to distribute to people who are not F# experts and is faster to execute.
- **Indentation for scope:** F# uses indentation to indicate scope. Some lines of code belong together and should be executed in a certain order and may share data. Indentation helps in specifying this relationship.
- **Strongly typed:** F# is strongly typed, reducing the number of runtime errors. That is, F# is picky, and will not allow the programmer to mix up types such as numbers and text. This is a great advantage for large programs.
- **Multi-platform:** F# is available on Linux, Mac OS X, Android, iOS, Windows, GPUs, and browsers via the Mono platform.
- Free to use and open source: F# is supported by the Fsharp foundation (http://fsharp.org) and sponsored by Microsoft.
- **Assemblies:** F# is designed to be able to easily communicate with other .Net and Mono programs through the language-independent, platform-independent bytecode called Common Intermediate Language (CIL) organized as assemblies. Thus, if you find that certain parts of a program are easy to express in F# and others in C++, then you will be able to combine these parts later into a single program.
- **Modern computing:** F# supports all aspects of modern computing including Graphical User Interfaces, Web programming, Information rich programming, Parallel algorithms, . . .
- Integrated development environments (IDE): F# is supported by major IDEs such as Visual Studio (https://www.visualstudio.com) and Xamarin Studio (https://www.xamarin.com).

#### 2.5. How to Read This Book

Learning to program requires mastering a programming language, however, most programming languages contain details that are rarely used or used in contexts far from a specific programming topic. Hence, this book only includes a subset of F# but focuses on language structures necessary to understand several common programming paradigms: Imperative programming mainly covered in Chapters 6 to 11, functional programming mainly covered

#### 2. Introduction

in Chapters 13 to 16, object-oriented programming in Chapters 20 and 22, and event-driven programming in Chapter 23. A number of general topics are given in the appendix for reference. For further reading please consult http://fsharp.org.

#### 3 Executing F# Code

#### 3.1. Source Code

F# is a functional first programming language, meaning that it has strong support for functional programming, but also supports imperative and object-oriented programming.

F# has two modes of execution, interactive and compiled. Interactive mode allows the interactive mode user to interact with F# as a dialogue: The user writes statements, and F# responds immediately. Interactive mode is well suited for small experiments or back-of-an-envelope calculations, but not for programming in general. In compile mode, the user writes a complete program, which is translated or compiled using the F# compiler into a compiled file. The compiled file can be run or executed as a stand-alone program using a virtual machine called mono. In both the interactive and compile mode, F# statements are translated into something that can be executed on the computer. A major difference is that in interactive mode, the translation is performed everytime the program is executed, while in compiled mode the translation is performed only once.

· compile mode

Both interactive and compile modes can be accessed via the *console*, see Appendix A for  $\cdot$  console more information on the console. The interactive system is started by calling fsharpi at the command prompt in the console, while compilation is performed with fsharpc, and execution of the compiled code is performed using the mono command.

F# programs come in many forms, which are identified by suffixes. The source code is an  $\cdot$  source code F# program written in human-readable form using an editor. F# recognizes the following types of source code files:

.fs An implementation file, e.g., myModule.fs

· implementation file

.fsi A signature file, e.g., myModule.fsi

· signature file

.fsx A script file, e.g., gettingStartedStump.fsx

· script file

.fsscript Same as .fsx, e.g., gettingStartedStump.fsscript

Compiled code is source code translated into a machine-readable language, which can be executed by a machine. Compiled F# code is either:

.dll A library file, e.g., myModule.dll

· library file

.exe A stand-alone executable file, e.g., gettingStartedStump.exe

· executable file

The implementation, signature, and script files are all typically compiled to produce an executable file, in which case they are called *scripts*, but can also be entered into the · scripts interactive system, in which case these are called *script-fragments*. The implementation · script-fragment and signature files are special kinds of script files used for building libraries. Libraries in F# are called modules, and they are collections of smaller programs used by other programs, which will be discussed in detail in Chapter 9.

## 3.2. Executing Programs

Programs may either be executed by the interpreter or by compiling and executing the compiled code. In Mono the interpreter is called fsharpi and can be used in two ways: interactively, where a user enters one or more script-fragments separated by the ";;" characters, or to execute a script file treated as a single script-fragment. <sup>1</sup>

To illustrate the difference between interactive and compile mode, consider the program in Listing 3.1.

```
Listing 3.1 gettingStartedStump.fsx:
A simple demonstration script.
let a = 3.0
 do printfn "%g" a
```

The code declares a value a to be the decimal value 3.0 and finally prints it to the console. The do printfn is a statement for displaying the content of a value to the screen, and "%g" is a special notation to control how the value is printed. In this case, it is printed as a decimal number. This and more will be discussed at length in the following chapters. For now, we will concentrate on how to interact with the F# interpreter and compiler.

An interactive session is obtained by starting the console, typing the fsharpi command, typing the lines of the program, and ending the script-fragment with ";;". The dialogue in Listing 3.2 demonstrates the workflow. What the user types has been highlighted by a box.

 $<sup>^{1}</sup>$ Jon: Too early to introduce lexeme: "F# uses many characters which at times are given special meanings, e.g., the characters ";;" is compound character denoting the end of a script-fragment. Such possibly compound characters are called lexemes."

# Listing 3.2: An interactive session. \$ fsharpi F# Interactive for F# 4.1 (Open Source Edition) Freely distributed under the Apache 2.0 Open Source License For help type #help;; let a = 3.0do printfn "%g" a;; val a : float = 3.0val it : unit = () > (#quit;;)

We see that after typing fsharpi, the program starts by stating details about itself. Then F# writes > indicating that it is ready to receive commands. The user types let a = 3.0 and presses enter, to which the interpreter responds with -. This indicates that the line has been received, that the script-fragment is not yet completed, and that it is ready to receive more input. When the user types do printfn "%g" a;; followed by enter, then by ";;" the interpreter knows that the script-fragment is completed, it interprets the script-fragment, responds with 3 and some extra information about the entered code, and with > to indicate that it is ready for more script-fragments. The interpreter is stopped when the user types #quit;;. It is also possible to stop the interpreter by typing ctrl-d.

The interactive session results in extra output on the type inference performed. In List- $\cdot$ type inference ing 3.2 F# states that the name a has type float and the value 3.0. Likewise, the do .type statement F# refers to by the name it, and it has the type unit and value (). Types are very important to F# since they define how different program pieces fit together like lego bricks. They are a key ingrediens for finding errors in programs, also known as debugging, · debugging and much of the rest of this book is concerned with types.

Instead of running fsharpi interactively, we can write the script-fragment from Listing 3.1 into a file, here called gettingStartedStump.fsx. This file can be interpreted directly by fsharpi as shown in Listing 3.3.

```
Listing 3.3: Using the interpreter to execute a script.
  fsharpi gettingStartedStump.fsx
3
```

Notice that in the file, ";;" is optional. We see that the interpreter executes the code and prints the result on screen without the extra type information as compared to Listing 3.2.

Finally, the file containing Listing 3.1 may be compiled into an executable file with the program fsharpc, and run using the program mono from the console. This is demonstrated in Listing 3.4.

# Listing 3.4: Compiling and executing a script. \$ fsharpc gettingStartedStump.fsx F# Compiler for F# 4.1 (Open Source Edition) Freely distributed under the Apache 2.0 Open Source License mono gettingStartedStump.exe

The compiler takes gettingStartedStump.fsx and produces gettingStarted.exe, which can be run using mono.

Both the interpreter and the compiler translates the source code into a format which can be executed by the computer. While the compiler performs this translation once and stores the result in the executable file, the interpreter translates the code every time the code is executed. Thus, to run the program again with the interpreter, it must be retranslated as "\$fsharpi gettingStartedStump.fsx". In contrast, compiled code does not need to be recompiled to be run again, only re-executed using "\$ mono gettingStartedStump.exe". On a MacBook Pro, with a 2.9 GHz Intel Core i5, the time the various stages take for this script are:

Command	Time
fsharpi gettingStartedStump.fsx	1.88s
fsharpc gettingStartedStump.fsx	1.90s
mono gettingStartedStump.exe	0.05s

I.e., executing the script with fsharpi is slightly faster than by first compiling it with fsharpc and then executing the result with mono (1.88s < 0.05s + 1.90s), if the script were to be executed only once, but every future execution of the script using the compiled version requires only the use of mono, which is much faster than fsharpi (1.88s  $\gg 0.05$ s).

Executing programs with the interpreted directly from a file and compiling and executing the program is much preferred for programming complete programs, since the starting state is well defined, and since this better supports unit-testing, which is a method for · unit-testing debugging programs. Thus, prefer compiling over interpretation.

Advice

# 4 | Quick-start Guide

Programming is the art of solving problems by writing a program to be executed by a computer. For example, to solve the following problem,

```
Problem 4.1
What is the sum of 357 and 864?
```

we have written the programshown in Listing 4.1.

```
Listing 4.1 quickStartSum.fsx:
A script to add 2 numbers and print the result to the console.

1 let a = 357
2 let b = 864
3 let c = a + b
4 do printfn "%A" c

1 $fsharpc --nologo quickStartSum.fsx && mono quickStartSum.exe
2 1221
```

In the box the above, we see our program was saved as a script in a file called quickStartSum.fsx, and in the console we executed the program by typing the command fsharpc --nologo quickStartSum.fsx && mono quickStartSum.exe. The result is then printed in the console to be 1221. Here, as in the rest of this book, we have used the optional flag --nologo, which informs fsharpc not to print information about its version etc., thus making the output shorter. The && notation tells the console to first run the command on the left, and if that did not report any errors, then run the command on the right. This could also have been performed as two separate commands to the console, and throughout this book we will use the above shorthand when convenient.

To solve the problem, we made program consisting of several lines, where each line was an expressions. The first expression, let a = 357, in line 1 used the let keyword to bind the value 357 to the name a. This is called a let-binding and makes the name synonymous with the value. Another notable point is that F# identifies 357 as an integer number, which is F#'s preferred number type, since computations on integers are very efficient, and since integers are very easy to communicate to other programs. In line 2 we bound the value 864 to the name b, and to the name c we bound the result of evaluating the sum a + b in line 3. Line 4 is a do-binding, as noted by the keyword do. Do-bindings are also sometimes called statements, and the do keyword is optional in F#. Here the value of c was printed to the console followed by a newline with the printfn function. A function

 $\cdot$  expression

·let

· keyword

· binding

 $\cdot$  let-binding

· integer number

· do-binding

· do

 $\cdot$  statements

· printfn

 $\cdot$  function

#### 4. Quick-start Guide

in F# is an entity that takes zero or more arguments and returns a value. The function printfn is very special, since it can take any number of arguments and returns the special value "()" which has type unit. The do tells F# to ignore this value. Here printfn has been used with 2 arguments: "%A" and c. Notice that in contrast to many other languages, F# does not use parentheses to frame the list of arguments, nor does it use commas to separate them. In general, the printfn function always has 1 or more arguments, and the first is a format string. A string is a sequence of characters starting and ending with double quotation marks. E.g., let s = "this is a string of characters" binds the string "this is..." to the name s. For the printfn function, the format string may be any string, but if it contains format character sequences, such as %A, then format character sequence are replaced by the arguments to printfn which follows the format string. The format string must match the value type, that is, here c is of type integer, whereas the  $\cdot$  type format string %A matches many types.

Types are a central concept in F#. In the script 4.1 we bound values of integer type to names. There are several different integer types in F#, here we used the one called int. The values were not declared to have these types, instead the types were inferred by F#. · type declaration Typing these bindings line by line in an interactive session, we see the inferred types as . type inference shown in Listing 4.2.

· format string

 $\cdot$  string

```
Listing 4.2: Inferred types are given as part of the response from the
interpreter.
> let a = 357;;
 val a : int = 357
> let b = 864;;
 val b : int = 864
> let c = a + b;;
 val c : int = 1221
> do printfn "%A" c;;
 val it : unit = ()
```

The interactive session displays the type using the val keyword followed by the name used val in the binding, its type, and its value. Since the value is also responded, the last printfn statement is superfluous. However, it is ill-advised to design programs to be run in Advice an interactive session, since the scripts need to be manually copied every time it is to be run, and since the starting state may be unclear. Notice that printfn is automatically bound to the name it of type unit and value "()". F# insists on binding  $\cdot$ it all statements to values, and in lack of an explicit name, it will use it. Rumor has it that  $\cdot$  () it is an abbreviation for "irrelevant".

The following problem,

```
Problem 4.2
What is the sum of 357.6 and 863.4?
```

uses decimal point numbers instead of integers. These numbers are called floating point · decimal point numbers, and their internal representation is quite different to integer numbers used pre- . floating point viously. Likewise, algorithms used to perform arithmetic are quite different from integers.

Now the program would look like Listing 4.3.

```
Listing 4.3 quickStartSumFloat.fsx:
Floating point types and arithmetic.

1 let a = 357.6
2 let b = 863.4
3 let c = a + b
4 do printfn "%A" c

1 $ fsharpc --nologo quickStartSumFloat.fsx && mono quickStartSumFloat.exe
2 1221.0
```

On the surface, this could appear as an almost negligible change, but the set of integers and the set of real numbers (floats) require quite different representations in order to be effective on a computer, and as a consequence, the implementation of their operations, such as addition, are very different. Thus, although the response is an integer, it has type float which is indicated by 1221.0 and which is not the same as 1221. F# is very picky about types, and generally does not allow types to be mixed, as demonstrated in the interactive session in Listing 4.4.

We see that binding a name to a number without a decimal point is inferred to be an integer, while when binding to a number with a decimal point the type is inferred to be a float, and that our attempt of adding an integer and floating point value gives an error. The error message contains much information. First, it states that the error is in stdin(4,13), which means that the error was found on standard-input at line 4 and column 13. Since the program was executed using fsharpi quickStartSumFloat.fsx, here standard input means the file quickStartSumFloat.fsx shown in Listing 4.3. The corresponding line and column are also shown in Listing 4.4. After the file, line, and column number, F# informs us of the error number and a description of the error. Error numbers are an underdeveloped feature in Mono and should be ignored. However, the verbal description often contains useful information for debugging. In the example we are informed that there is a type mismatch in the expression, i.e., since a is an integer, F# expected b to be one too. Debugging is the process of solving errors in programs, and here we can solve the error by either making a into a float or b into an int. The right solution depends on the application.

· error message

 $\cdot$  debugging

F# is a functional first programming language, and one implication of this is that names have a lexical scope. A scope is the lines in a program where a binding is valid, and lexical · lexical scope scope means that to find the value of a name, F# looks for the value in the above lines. Furthermore, at the outermost level, rebinding is not allowed. If attempted, then F# will return an error as shown in Listing 4.5.

```
Listing 4.5 quickStartRebindError.fsx:
A name cannot be rebound.
let a = 357
let a = 864
$ fsharpc --nologo -a quickStartRebindError.fsx
quickStartRebindError.fsx(2,5): error FS0037: Duplicate
   definition of value 'a'
```

However, if the same code is executed in an interactive session, then rebinding does not cause an error, as shown in Listing 4.6.

```
Listing 4.6: Names may be reused when separated by the lexeme ";;".
> let a = 357;;
val a : int = 357
> let a = 864;;
val a : int = 864
```

The difference is that the ";;" lexeme is used to specify the end of a script-fragment. A ';; lexeme is a letter or word, which F# considers as an atomic unit. Script-fragments may · lexeme be defined both in scripts and in interactive mode, and rebinding is not allowed at the ·script-fragment outermost level in script-fragments. Even with the ";;" lexeme, rebinding is not allowed in compile-mode. In general, avoid rebinding of names.

Advice

In F#, functions are also values, and we may define a function sum as part of the solution  $\cdot$  function to the above program, as shown in Listing 4.7.

```
Listing 4.7 quickStartSumFct.fsx:
A script to add 2 numbers using a user-defined function.
let sum x y = x + y
let c = sum 357 864
do printfn "%A" c
$ fsharpc --nologo quickStartSumFct.fsx && mono
   quickStartSumFct.exe
1221
```

Functions are useful to encapsulate code, such that we can focus on the transformation · encapsulate of data by a function while ignoring the details on how this is done. Functions are also

useful for code reuse, i.e., instead of repeating a piece of code in several places, such code can be encapsulated in a function and replaced with function calls. This makes debugging and maintenance considerably simpler. Entering the function into an interactive session will illustrate the inferred type the function sum has: val sum: x:int -> y:int -> int. The "->" is the mapping operator in the sense that functions are mappings between sets. The type of the function sum, should be read as val sum: x:int -> (y:int -> int), that is, sum takes an integer and returns a function, which takes an integer and returns an integer. This is an example of a higher-order function.

Type inference in F# may cause problems, since the type of a function is inferred based on the context in which it is defined. E.g., in an interactive session, defining the sum in one scope on a single line will default the types to integers, F#'s favorite type. Thus, if the next script-fragment uses the function with floats, then we will get an error message as shown in Listing 4.8.

# Listing 4.8: Types are inferred in blocks, and F# tends to prefer integers. val sum : x:int -> y:int -> int let c = sum 357.6 863.4;; let c = sum 357.6 863.4;; stdin(3,13): error FS0001: This expression was expected to have type 'int' but here has type 'float'

A remedy is to define the function in the same script-fragment as it is used, such as shown in Listing 4.9.

```
Listing 4.9: Type inference is per script-fragment.

1 > let sum x y = x + y
2 - let c = sum 357.6 863.4;;
3 val sum : x:float -> y:float -> float
4 val c : float = 1221.0
```

Alternatively, the types may be explicitly stated as shown in Listing 4.10.

```
Listing 4.10: Function argument and return types may be stated explicitly.

1 > let sum (x : float) (y : float) : float = x + y;;

2 val sum : x:float -> y:float -> float

3 > let c = sum 357.6 863.4;;

5 val c : float = 1221.0
```

The function sum has two arguments and a return type, and in Listing 4.10 we have specified all three. This is done using the ":" lexeme, and to resolve confusion, we must use parentheses around the arguments, such as (y : float), otherwise F# would not be

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able to understand whether the type annotation was for the argument or the return value. Often it is sufficient to specify just some of the types, since type inference will enforce the remaining types. E.g., in this example, the "+" operator is defined for identical types, so specifying the return value of sum to be a float implies that the result of the "+" operator is a float, and therefore that its arguments must be floats, and finally then that the arguments for sum must be floats. However, in this book we advocate the following advice: specify Advice types unless explicitly working with generic functions.

In this chapter, we have scratched the surface of learning how to program by concentrating on a number of key programming concepts and how they are expressed in the F# language. In the following chapters, we will expand the description of F# with features used in all programming approaches.

# $5 \mid \text{Using F} \# \text{ as a Calculator}$

In this chapter, we will exclusively use the interactive mode to illustrate basic types and operations in F#.

## 5.1. Literals and Basic Types

All programs rely on processing of data, and an essential property of data is its type. A · type literal is a fixed value like the number 3, and if we type the number 3 in an interactive · literal session at the input prompt, then F# responds as shown in Listing 5.1.

```
Listing 5.1: Typing the number 3.

1 > 3;;
2 val it : int = 3
```

What this means is that F# has inferred the type to be int and bound it to the identifier  $\cdot$  int it. For more on binding and identifiers see Chapter 6. Types matter, since the operations  $\cdot$  it that can be performed on integers, are quite different from those that can be performed on, e.g., strings. Therefore, the number 3 has many different representations as shown in Listing 5.2.

```
Listing 5.2: Many representations of the number 3 but using different types.

1 > 3;;
2 val it : int = 3

4 > 3.0;;
5 val it : float = 3.0

6 7 > '3';;
8 val it : char = '3'

9 > "3";;
10 > "3";;
11 val it : string = "3"
```

Each literal represents the number 3, but their types are different, and hence they are quite different values. The types int for integer numbers, float for floating point numbers, bool for Boolean values, char for characters, and string for strings of characters are the most

· bool · char · string

Metatype	Type name	Description	
Boolean	<u>bool</u>	Boolean values true or false	
Integer	<u>int</u>	Integer values from -2,147,483,648 to 2,147,483,647	
	byte	Integer values from 0 to 255	
	sbyte	Integer values from -128 to 127	
	int8	Synonymous with sbyte	
	uint8	Synonymous with byte	
	int16	Integer values from -32768 to 32767	
	uint16	Integer values from 0 to 65535	
	int32	Synonymous with int	
	uint32	Integer values from 0 to 4,294,967,295	
	int64	Integer values from -9,223,372,036,854,775,808 to	
		9,223,372,036,854,775,807	
	uint64	Integer values from 0 to 18,446,744,073,709,551,615	
Real <u>float</u> 64-b		64-bit IEEE 754 floating point value from $-\infty$ to $\infty$	
	double	Synonymous with float	
	single	A 32-bit floating point type	
	float32	Synonymous with single	
	decimal	A floating point data type that has at least 28 significant	
		digits	
Character char Unicode character		Unicode character	
	string	Unicode sequence of characters	
None	unit	The value ()	
Object	obj	An object	
Exception	exn	An exception	

Table 5.1.: List of some of the basic types. The most commonly used types are underlined. For a description of integer see Appendix B.1, for floating point numbers see Appendix B.2, for ASCII and Unicode characters see Appendix C, for objects see Chapter 20, and for exceptions see Chapter 18.

common types of literals. A table of all *basic types* predefined in F# is given in Table 5.1. · basic types In addition to these built-in types, F# is designed such that it is easy to define new types.

Humans like to use the decimal number system for representing numbers. Decimal numbers are base 10, which means that a value is represented as two sequences of decimal digits separated by a decimal point, where each digit d has a position and a value  $d \in \{0, 1, 2, \ldots, 9\}$ . The part before the decimal point is called the whole part and the part after is called the fractional part of the number. An integer is a number with only a whole part and neither a decimal point nor a fractional part. As an example 35.7 is a decimal number, whose value is  $3 \cdot 10^1 + 5 \cdot 10^0 + 7 \cdot 10^{-1}$ , and 128 is an integer, whose value is  $1 \cdot 10^2 + 2 \cdot 10^1 + 8 \cdot 10^0$ . In F#, a decimal number is called a floating point number. Floating point numbers may alternatively be given using scientific notation, such as 3.5e-4 and 4e2, where the e-notation is translated to a value as  $3.5e-4 = 3.5 \cdot 10^{-4} = 0.00035$ , and  $4e2 = 4 \cdot 10^2 = 400$ .

The basic unit of information in almost all computers is the binary digit or *bit* for short. Internally, programs and data are all represented as bits, hence F# has a strong support for binary numbers. A *binary number* consists of a sequence of binary digits separated by a decimal point, where each digit can have values  $b \in \{0,1\}$ , and the base is 2. E.g., the binary number  $101.01_2 = 1 \cdot 2^2 + 0 \cdot 2^1 + 1 \cdot 2^0 + 0 \cdot 2^{-1} + 1 \cdot 2^{-2} = 5.25$ . Subscripts are often used to indicate the base of a number, e.g.,  $101.01_2$  and  $101.01_{10}$  are different numbers. Since base 10 is so common, the subscript for base 10 numbers is often omitted.

- · decimal number
- · base
- · decimal point
- $\cdot$  digit
- · whole part
- · fractional part
- $\cdot$  integer
- · floating point number
- · scientific notation
- $\cdot$  bit
- $\cdot$  binary number

Character	Escape sequence	Description
BS	\b	Backspace
LF	\n	Line feed
CR	\r	Carriage return
HT	\t	Horizontal tabulation
\	\\	Backslash
"	\"	Quotation mark
,	\'	Apostrophe
BEL	\a	Bell
$\operatorname{FF}$	\f	Form feed
VT	\v	Vertical tabulation
	\uXXXX,	Unicode character ('X' is any hexadecimal digit, and
	\UXXXXXXX,	'D' is any decimal digit)
	\DDD	

Table 5.2.: Escape characters. The escapecode \DDD is sometimes called a tricode.

Binary numbers are closely related to octal and hexadecimal numbers. Octals uses 8 as basis and hexadecimals use 16 as basis. Each octal digit can be represented by exactly three bits, and each hexadecimal digit can represented by exactly four bits. The hexadecimal digits use 0-9 to represent the values 0-9 and a-f in lower or alternatively upper case to represent the values 10-15. Thus, Octals and hexadecimals conveniently serve as shorthand for the much longer binary representation. As examples, the octal number  $37_8$  is  $3 \cdot 8^1 + 7 \cdot 8^0 = 31$ , and the hexadecimal number  $f3_{16}$  is  $15 \cdot 16^1 + 3 \cdot 16^0 = 243$ .

To denote integers in bases different than 10, F# uses the prefix '0b' for binary, '0o' for octal, and '0x' for hexadecimal numbers. For example, the value 367<sub>10</sub> may be written as an integer 367, as a binary number 0b101101111, as a octal number 0o557, and as a hexadecimal number 0x16f. In F#, the character sequences 0b12 and ff are not recognized as numbers.

A character is a Unicode code point, and character literals are enclosed in single quotation · character marks. Appendix C.3 contains more details on code points. The character type in F# is · Unicode denoted *char*. Examples of characters are 'a', 'D', '3', and examples of non-characters are · code point '23' and 'abc'. Some characters, such as the tabulation character, do not have a visual . char representation. These can still be represented as a character using escape sequences. A character escape sequence starts with "\" followed by letter for simple escapes such as \t for tabulation and \n for newline. Escape sequences can also be a numerical representation of a code point, and three versions exist: The trigraph \DDD, where D is a decimal digit, is used to specify the first 256 code points, the hexadecimal escape codes \uXXXX, where X is a hexadecimal digit, is used to specify the first 65536 code points, and \UXXXXXXX is used to specify any of the approximately  $4.3 \cdot 10^9$  possible code points. All escape sequences are shown in Table 5.2. Examples of char representations of the letter 'a' are: 'a', '\097', '\u0061', '\U00000061'.

A string is a sequence of characters enclosed in double quotation marks. Examples are "a", "this is a string", and "-&#\@". Note that the string "a" and the character 'a' are not the same. Some strings are so common that they are given special names: One or more spaces " " is called whitespace, and both "\n" and "\n" are called newline. The escape-character "\" may be used to break a line in two. This and other examples are shown in Listing 5.3.

· hexadecimal number

· escape sequences

· whitespace

Type	syntax	Examples	Value
int, int32	<int hex="" or=""></int>	3, 0x3	3
	<int hex="" or="">l</int>	31, 0x31	
uint32	<int hex="" or="">u</int>	3u	3
	<int hex="" or="">ul</int>	3ul	
byte, uint8	<int hex="" or="">uy</int>	97uy	97
	' <char>'B</char>	'a'B	
byte[]	" <string>"B</string>	"a\n"B	[ 97uy; 10uy ]
	@" <string>"B</string>	@"a\n"B	[ 97uy; 92uy; 110uy ]
sbyte, int8	<int hex="" or="">y</int>	Зу	3
int16	<int hex="" or="">s</int>	3s	3
uint16	<int hex="" or="">us</int>	3us	3
int64	<int hex="" or="">L</int>	3L	3
uint64	<int hex="" or="">UL</int>	3UL	3
	<int hex="" or="">uL</int>	3uL	
float, double	<float></float>	3.0	3.0
	<hex>LF</hex>	0x013fLF	9.387247271e-323
single, float32	<float>F</float>	3.0F	3.0
	<float>f</float>	3.0f	3.0
	<hex>lf</hex>	0x013f1f	4.4701421e-43f
decimal	<float int="" or="">M</float>	3.0M,3M	3.0
	<float int="" or="">m</float>	3.0m,3m	
string	" <string>"</string>	"a \"quote\".\n"	a "quote". <newline></newline>
	@" <string>"</string>	@"a ""quote"".\n"	a "quote". $\n$ .
	""" <string>"""</string>	"""a "quote".\n"""	a "quote". $\n$

Table 5.3.: List of literal types. The syntax notation <> means that the programmer replaces the brackets and content with a value of the appropriate form. The [||] notation means that the value is an array, see Section 11.3 for details.

Note that the response from fsharpi is shown in double quotation marks, but this is not part of the string.

F# supports *literal types*, where the type of a literal is indicated as a prefix or suffix as  $\cdot$  literal type shown in Table 5.3.

The literal type is closely connected to how the values are represented internally. For example, a value of type int32 use 32 bits and can be both positive and negative, while a uint32 value also use 32 bits, but is unsigned. A byte is an 8-bit number, and sbyte is a signed 8-bit number. Values of type float use 64 bits, while float32 only uses 32 bits. The number of bits used to represent numbers directly relates to the range and precession these types can represent. This is summarized in Table 5.1 and discussed in more detail in Appendix B. String literals may be *verbatim* by the @-notation or triple double quotation marks, meaning that the escape sequences are not converted to their code point. The two types of string verbatim treat quotation marks differently, as illustrated in the table. Further examples are shown in Listing 5.4.

verbatim

```
Listing 5.4: Named and implied literals.
   > 3;;
   val it : int = 3
   > 4u;;
   val it : uint32 = 4u
   > 5.6;;
   val it : float = 5.6
   > 7.9f;;
   val it : float32 = 7.9000001f
   > 'A';;
   val it : char = 'A'
   > 'B'B;;
   val it : byte = 66uy
   > "ABC";;
20
   val it : string = "ABC"
21
   > 0"abc\nde";;
   val it : string = "abc\nde"
```

Many basic types are compatible, and the type of a literal may be changed by typecasting. · typecasting An example of casting to a float is shown in Listing 5.5.

```
Listing 5.5: Casting an integer to a floating point number.

1 > float 3;;
2 val it : float = 3.0
```

When float is given an argument, then it acts as a function rather than a type, and for the integer 3 it returns the floating point number 3.0. For more on functions see Chapter 6. Boolean values are often treated as the integer values 0 and 1, but no short-hand function names exist for their conversions. Instead, use functions from the System.Convert family of functions, as demonstrated in Listing 5.6.

```
Listing 5.6: Casting booleans.

> System.Convert.ToBoolean 1;;
val it : bool = true

> System.Convert.ToBoolean 0;;
val it : bool = false

> System.Convert.ToInt32 true;;
val it : int = 1

> System.Convert.ToInt32 false;;
val it : int = 0
```

Here System.Convert.ToBoolean is the identifier of a function ToBoolean, which is a *member* of the *class* Convert that is included in the *namespace* System. Namespaces, classes, and members will be discussed in Chapter 9.

 $\cdot$  member

 $\cdot$  class

 $\cdot$  namespace

Typecasting is often a destructive operation, e.g., typecasting a float to int removes the fractional part without rounding as shown in Listing 5.7.

```
Listing 5.7: Fractional part is removed by downcasting.

1 > int 357.6;;
2 val it : int = 357
```

Here we type casted to a lesser type, in the sense that the set of integers is a subset of floating point numbers, and this is called *downcasting*. The opposite is called *upcasting* and is often non-destructive, as Listing 5.5 showed. Since floating point numbers are a superset of integers, the value is retained. As a side note, *rounding* a number y.x, where y is the *whole part* and x is the *fractional part*, is the operation of mapping numbers in the interval  $y.x \in [y.0, y.5)$  to y, and those in  $y.x \in [y.5, y+1)$  to y+1. This can be performed by downcasting, as shown in Listing 5.8.

 $\cdot \ down casting$ 

 $\cdot$  upcasting

 $\cdot$  rounding

· whole part

· fractional part

```
Listing 5.8: Rounding by modified downcasting.

1 > int (357.6 + 0.5);;
2 val it : int = 358
```

I.e., 357.6 + 0.5 = 358.1 and removing the fractional part by downcasting results in 358, which is the correct answer.

# 5.2. Operators on Basic Types

Expressions are the basic building block of all F# programs, and this section will discuss operator expressions on basic types. A typical calculation, such used in Listing 5.8, is

$$\underbrace{357.6}_{\text{operand}} \quad \underbrace{+}_{\text{operand}} \quad \underbrace{0.5}_{\text{operand}} \tag{5.1}$$

is an example of an arithmetic expression, and the above expression consists of two operands

and an operator. Since this operator takes two operands, it is called a binary operator. • operator The expression is written using infix notation, since the operands appear on each side of . binary operator the operator.

 $\cdot$  infix notation

In order to discuss general programming structures, we will use a simplified language to describe valid syntactical structures. In this simplified language, the syntax of basic binary operators is shown in the following.

```
Listing 5.9: Syntax for a binary expression.
<expr><op><expr>
```

Here <expr> is any expression supplied by the programmer, and <op> is a binary infix operator. F# supports a range of arithmetic binary infix operators on its built-in types, such as addition, subtraction, multiplication, division, and exponentiation, using the "+", "-", "\*", "/", "\*\*" lexemes, respectively. Not all operators are defined for all types, e.g., addition is defined for integer and float types as well as for characters and strings, but multiplication is only defined for integer and floating-point types. A complete list of builtin operators on basic types is shown in Table E.1 and E.2, and a range of mathematical functions is shown in Table E.3. Note that expressions can themselves be arguments to expressions, and thus, 4+5+6 is also a legal statement. This is called recursion, which means that a rule or a function is used by the rule or function itself in its definition. See Chapter 13 for more on recursive functions.

 $\cdot$  recursion

Unary operators take only one argument and have the syntax:

```
Listing 5.10: A unary expressions.
<op><expr>
```

An example of a unary operator is -3, where - here is used to negate a positive integer. Since the operator appears before the operand, it is a prefix operator.

· prefix operator

The concept of precedence is an important concept in arithmetic expressions. If paren- · precedence theses are omitted in Listing 5.8, then F# will interpret the expression as (int 357.6) + 0.5, which is erroneous since the addition of an integer with a float is undefined. This is an example of precedence, i.e., function evaluation takes precedence over addition which means that function evaluation is performed first and addition second. Consider the arithmetic expression shown in Listing 5.11.

```
Listing 5.11: A simple arithmetic expression.
> 3 + 4 * 5;;
 val it : int = 23
```

Here, the addition and multiplication functions are shown in infix notation with the operator lexemes "+" and "\*". To arrive at the resulting value 23, F# has to decide in which order to perform the calculation. There are 2 possible orders, 3 + (4 \* 5) and (3 +4) \* 5 that gives different results. For integer arithmetic, the correct order is, of course,

<sup>&</sup>lt;sup>1</sup>Jon: minor comment on indexing and slice-ranges.

#### 5. Using F# as a Calculator

Operator	Associativity	Description
+ <expr>, -<expr>,</expr></expr>	Left	Unary identity, negation, and bitwise negation op-
~~~ <expr></expr>		erators
f <expr></expr>	Left	Function application
<expr> ** <expr></expr></expr>	Right	Exponentiation
<expr> * <expr>,</expr></expr>	Left	Multiplication, division and remainder
<expr> / <expr>,</expr></expr>		
<expr> % <expr></expr></expr>		
<expr> + <expr>,</expr></expr>	Left	Addition and subtraction binary operators
<expr> - <expr></expr></expr>		
<expr> ^^^ <expr></expr></expr>	Right	Bitwise exclusive or
<expr> &lt; <expr>,</expr></expr>	Left	Comparison operators, bitwise shift, and bitwise
<expr> &lt;= <expr>,</expr></expr>		'and' and 'or'.
<expr> &gt; <expr>,</expr></expr>		
<expr> &gt;= <expr>,</expr></expr>		
<pre><expr> = <expr>,</expr></expr></pre>		
<expr> &lt;&gt; <expr>,</expr></expr>		
<expr> &lt;&lt;&lt; <expr>&gt;,</expr></expr>		
<expr> &gt;&gt;&gt; <expr>,</expr></expr>		
<pre><expr> &amp;&amp;&amp; <expr>;</expr></expr></pre>		
<pre><expr>     <expr>,</expr></expr></pre>		
<expr> &amp;&amp; <expr></expr></expr>	Left	Boolean and
<expr>    <expr></expr></expr>	Left	Boolean or

Table 5.4.: Some common operators, their precedence, and their associativity. Rows are ordered from highest to lowest precedences, such that <\*expr\*> \* <\*expr\*> has higher precedence than <\*expr\*> + <\*expr\*>. Operators in the same row have the same precedence. Full table is given in Table E.5.

multiplication before addition, and we say that multiplication takes precedence over addition. Every atomic operation that F# can perform is ordered in terms of its precedence, and for some common built-in operators shown in Table 5.4, the precedence is shown by the order they are given in the table.

Associativity describes the order in which calculations are performed for binary operators of the same precedence. Some operator's associativity are given in Table 5.4. In the table we see that "\*" is left associative, which means that 3.0 \* 4.0 \* 5.0 is evaluated as (3.0 \* 4.0) \* 5.0. Conversely, \*\* is right associative, so 4.0\*\*3.0\*\*2.0 is evaluated as 4.0\*\*(3.0\*\*2.0). For some operators, like multiplication, association matters little, e.g., 4\*3\*2 = 4\*(3\*2) = (4\*3)\*2, and for other operators, like exponentiation, association makes a huge difference, e.g.,  $4^{(3^2)} \neq (4^3)^2$ . Examples of this is shown in Listing 5.12.

a	Ъ	a && b	a    b	not a
false	false	false	false	true
false	true	false	true	true
true	false	false	true	false
true	true	true	true	false

Table 5.5.: Truth table for boolean 'and', 'or', and 'not' operators. Value 0 is false and 1 is true.

Advice

Whenever in doubt of association or any other basic semantic rules, it is a good idea to use parentheses. It is also a good idea to test your understanding of the syntax and semantic rules by making a simple script.

#### 5.3. Boolean Arithmetic

Boolean arithmetic is the basis of almost all computers and particularly important for controlling program flow, which will be discussed in Chapter 8. Boolean values are one of 2 possible values, true or false, which is also sometimes written as 1 and 0. Basic operations on Boolean values are 'and', 'or', and 'not', which in F# are written respectively as the binary operators &&, ||, and the function not. Since the domain of Boolean values is so small, all possible combination of input on these values can be written on the tabular form, known as a truth table, and the truth tables for the basic Boolean operators and functions are shown in Table 5.5. A good mnemonic for remembering the result of the 'and' and 'or' operators is to use 1 for true, 0 for false, multiplication for the Boolean 'and' operator, and addition for the Boolean 'or' operator, e.g., true and false in this mnemonic translates to  $1 \cdot 0 = 0$ , and the result translates back to the Boolean value false. In F#, the truth table for the basic Boolean operators can be produced by a program, as shown in Listing 5.13.

 $\cdot$  and  $\cdot$  or  $\cdot$  not

· truth table

## Listing 5.13: Boolean operators and truth tables. > printfn "a b a\*b a+b not a" printfn "%A %A %A %A %A" false false (false && false) (false || false) (not false) printfn "%A %A %A %A %A" false true (false && true) (false || true) (not false) printfn "%A %A %A %A %A" true false (true && false) (true || false) (not true) printfn "%A %A %A %A %A" true true (true && true) (true || true) (not true);; a b a\*b a+b not a false false false true false true false true true true false false true false

Here, we used the printfn function to present the results of many expressions on something that resembles a tabular form. The spacing produced using the printfn function is not elegant, and in Section 6.5 we will discuss better options for producing more beautiful output. Notice that the arguments for printfn was given on the next line with indentation. The indentation is an important part of telling F# which part of what you write belong together. This is an example of the so-called lightweight syntax. Generally, F# ignores newlines and whitespaces except when using the lightweight syntax. The difference between verbose and lightweight syntax is discussed in Chapter 6.

# 5.4. Integer Arithmetic

true true true false

val it : unit = ()

The set of integers is infinitely large, but since all computers have limited resources, it is not possible to represent it in its entirety. The various integer types listed in Table 5.1 are finite subsets reduced by limiting their ranges. An in-depth description of integer implementation can be found in Appendix B. The type int is the most common type.

Table E.1–E.3 give examples of operators and functions pre-defined for integer types. Notice that fewer functions are available for integers than for floating point numbers. For most addition, subtraction, multiplication, and negation, the result is straightforward. However, performing arithmetic operations on integers requires extra care, since the result may cause overflow and underflow. For example, an sbyte is specified using the "y"-literal and can · overflow hold values [-128...127]. This causes problems in the example in Listing 5.14.

· underflow

```
Listing 5.14: Adding integers may cause overflow.
> 100y;;
val it : sbyte = 100y
> 30y;;
val it : sbyte = 30y
> 100y + 30y;;
val it : sbyte = -126y
```

#### 5. Using F# as a Calculator

Here 100 + 30 = 130, which is larger than the biggest sbyte, and the result is an overflow. Similarly, we get an underflow, when the arithmetic result falls below the smallest value storable in an sbyte, as demonstrated in Listing 5.15.

# Listing 5.15: Subtracting integers may cause underflow. > -100y - 30y;;val it : sbyte = 126y

I.e., we were expecting a negative number but got a positive number instead.

The overflow error in Listing 5.14 can be understood in terms of the binary representation of integers: In binary,  $130 = 10000010_2$ , and this binary pattern is interpreted differently as byte and sbyte, see Listing 5.16.

## Listing 5.16: The leftmost bit is interpreted differently for signed and unsigned integers, which gives rise to potential overflow errors.

```
> 0b10000010uy;;
val it : byte = 130uy
> 0b10000010y;;
val it : sbyte = -126y
```

That is, for signed bytes, the left-most bit is used to represent the sign, and since the addition of  $100 = 01100100_2$  and  $30 = 000111110_b$  is  $130 = 10000010_2$ , which causes the left-most bit to be used, this is wrongly interpreted as a negative number when stored in an sbyte. Similar arguments can be made explaining underflows.

The operator discards the fractional part after division, and the *integer remainder* operator · integer division calculates the remainder after integer division, as demonstrated in Listing 5.17.

· integer remainder

```
Listing 5.17: Integer division and remainder operators.
```

```
> 7 / 3;;
val it : int = 2
> 7 % 3;;
val it : int = 1
```

Together, the integer division and remainder can form a lossless representation of the original number, see Listing 5.18.

## Listing 5.18: Integer division and remainder is a lossless representation of an integer, compare with Listing 5.17.

```
> (7 / 3) * 3;;
val it : int = 6
> (7 / 3) * 3 + (7 % 3);;
val it : int = 7
```

Here we see that integer division of 7 by 3 followed by multiplication by 3 is less than 7, and that the difference is 7 % 3.

Notice that neither overflow nor underflow error gave rise to an error message, which is why such bugs are difficult to find. Dividing any non-zero number by 0 is infinite, which is also outside the domain of any of the integer types, but in this case, F# casts an *exception*, · exception as shown in Listing 5.19.

The output looks daunting at first sight, but the first and last lines of the error message are the most important parts, which tell us what exception was cast and why the program stopped. The middle contains technical details concerning which part of the program caused the error and can be ignored for the time being. Exceptions are a type of *runtime error*, and are discussed in Chapter 18

· runtime error

Integer exponentiation is not defined as an operator but is available as the built-in function pown. This function is demonstrated in Listing 5.20 for calculating  $2^5$ .

```
Listing 5.20: Integer exponent function.

1 > pown 2 5;;
2 val it : int = 32
```

For binary arithmetic on integers, the following operators are available: <leftExpr> <<< <rr>
 <rightExpr>, which shifts the bit pattern of <leftExpr> <rightExpr> positions to the left while inserting 0's to right; <leftExpr> >>> <rightExpr>, which shifts the bit pattern of <leftExpr> <rightExpr> positions to the right while inserting 0's to left; ~~~ <expr> returns a new integer, where all 0 bits are changed to 1 bits and vice-versa; <expr> &&& <expr> returns the result of taking the Boolean 'and' operator position-wise; <expr> ||| <expr> returns the result of taking the Boolean 'or' operator position-wise; and <expr> ~~ <expr> returns the result of the Boolean 'xor' operator defined by the truth table in Table 5.6.

· xor · exclusive or

a	Ъ	a ^^^ b
false	false	false
false	true	true
true	false	true
true	true	false

Table 5.6.: Boolean exclusive or truth table.

## 5.5. Floating Point Arithmetic

Like integers, the set of reals is also infinitely large, hence, floating point types are finite subsets reduced by sampling the space of reals. An in-depth description of floating point implementations can be found in Appendix B. The type float is the most common type.

Table E.1–E.3 give examples of operators and functions pre-defined for floating point types. Note that the remainder operator for floats calculates the remainder after division and discards the fractional part, see Listing 5.21.

The remainder for floating point numbers can be fractional, but division, discarding fractional part, and the remainder is still a lossless representation of the original number, as demonstrated in Listing 5.22.

```
Listing 5.22: Floating point division, downcasting, and remainder is a loss-less representation of a number.
```

```
1  > float (int (7.0 / 2.5));;
2  val it : float = 2.0
3
4  > (float (int (7.0 / 2.5))) * 2.5;;
5  val it : float = 5.0
6
7  > (float (int (7.0 / 2.5))) * 2.5 + 7.0 % 2.5;;
8  val it : float = 7.0
```

Arithmetic using float will not cause over- and underflow problems, since the IEEE 754 standard includes the special numbers  $\pm \infty$  and NaN. As shown in Listing 5.23, no exception is thrown.

#### Listing 5.23: Floating point numbers include infinity and Not-a-Number.

```
> 1.0/0.0;;
val it : float = infinity
> 0.0/0.0;;
val it : float = nan
```

However, the float type has limited precision, since there is only a finite number of numbers that can be stored in a float. E.g., addition and subtraction can give surprising results, as demonstrated in Listing 5.24.

```
Listing 5.24: Floating point arithmetic has finite precision.
> 357.8 + 0.1 - 357.9;;
val it : float = 5.684341886e-14
```

That is, addition and subtraction associates to the left, hence the expression is interpreted as (357.8 + 0.1) - 357.9 and we see that we do not get the expected 0. The reason is that the calculation is done stepwise, and in the process, the numbers are represented using the imprecise floating point standard. Thus, 357.8 + 0.1 is represented as a number close to but not identical to what 357.9 is represented as, and thus, when subtracting these two representations, we get a very small nonzero number. Such errors tend to accumulate, and comparing the result of expressions of floating point values should, therefore, be treated with care. Thus, equivalence of two floating point expressions should only be Advice considered up to sufficient precision, e.g., comparing 357.8 + 0.1 and 357.9 up to 1e-10 precision should be tested as, abs ((357.8 + 0.1) - 357.9) < 1e-10.

## 5.6. Char and String Arithmetic

Addition is the only operator defined for characters. Nevertheless, character arithmetic is often done by casting to an integer. A typical example is the conversion of character case, e.g., to convert the lowercase character 'z' to uppercase. Here, we use the ASCIIbetical order, add the difference between any Basic Latin Block letters in upper- and lowercase as · ASCIIbetical order integers, and cast back to char, see Listing 5.25.

```
Listing 5.25: Converting case by casting and integer arithmetic.
> char (int 'z' - int 'a' + int 'A');;
 val it : char = 'Z'
```

I.e., the code point difference between upper and lower case for any alphabetical character 'a' to 'z' is constant, hence we can change case by adding or subtracting the difference between any corresponding character. Unfortunately, this does not generalize to characters from other languages.

A large collection of operators and functions exist for string. The simplest is concatenation using the "+" operator, as demonstrated in Listing 5.26.

# Listing 5.26: Example of string concatenation. > "hello" + " " + "world";; val it : string = "hello world"

Characters and strings cannot be concatenated, which is why the above example used the string of a space " " instead of the space character ' '. The characters of a string may be indexed as using the . [] notation. This is demonstrated in Listing 5.27. · . []

```
Listing 5.27: String indexing using square brackets.
> "abcdefg".[0];;
val it : char = 'a'
> "abcdefg".[3];;
val it : char = 'd'
> "abcdefg".[3..];;
val it : string = "defg"
> "abcdefg".[..3];;
val it : string = "abcd"
> "abcdefg".[1..3];;
val it : string = "bcd"
> "abcdefg".[*];;
val it : string = "abcdefg"
```

Notice that the first character has index 0, and to get the last character in a string, we use the string's length property. This is done as shown in Listing 5.28.

```
Listing 5.28: String length attribute and string indexing.
> "abcdefg".Length;;
val it : int = 7
> "abcdefg".[7-1];;
val it : char = 'g'
```

Since index counting starts at 0, and since the string length is 7, the index of the last character is 6. There is a long list of built-in functions in System. String for working with strings, some of which will be discussed in Section 11.1.

The dot notation is an example of Structured programming, where technically speaking, · dot notation the string "abcdefg" is an immutable object of class string, [] is an object method, and object Length is a property. For more on objects, classes, and methods, see Chapter 20.

 $\cdot$  class

 $\cdot$  method

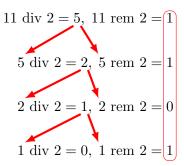
Strings are compared letter by letter. For two strings to be equal, they must have the same length and all the letters must be identical. E.g., "abs" = "absalon" is false, while "abs" = "abs" is true. The "<>" operator is the boolean negation of the "=" operator, e.g., "abs" <> "absalon" is true, while "abs" <> "abs" is false. For the "<", "<=", ">", and ">=" operators, the strings are ordered alphabetically, such that "abs" < "absalon" && "absalon" < "milk" is true, that is, the "<" operator on two strings is true if the left operand should come before the right when sorting alphabetically. The algorithm for deciding the boolean value of leftOp < rightOp is as follows: we start by examining the first character, and if leftOp.[0] and rightOp.[0] are different, then leftOp < rightOp is equal to leftOp.[0] < rightOp.[0]. E.g., "milk" < "abs" is the same as 'm' < 'a', which is false, since the letter 'm' does not come before the letter 'a' in the alphabet, or more precisely, the codepoint of 'm' is not less than the codepoint of 'a'. If leftOp.[0] and rightOp.[0] are equal, then we move on to the next letter and repeat the investigation, e.g., "abe" < "abs" is true, since "ab" = "ab" is true and 'e' < 's' is true. If we reach the end of either of the two strings, then the shorter word is smaller than the longer word, e.g., "abs" < "absalon" is true, while "abs" < "abs" is false. The "<=", ">", ">", and ">=" operators are defined in a similar manner.

### 5.7. Programming Intermezzo: Hand Conversion Between Decimal and Binary Numbers

Conversion of integers between decimal and binary form is a key concept one must grasp in order to understand some of the basic properties of calculations on the computer. Converting from binary to decimal is straightforward if using the power-of-two algorithm, i.e., given a sequence of n+1 binary digits  $b_i$  written as  $b_n b_{n-1} \dots b_0$ , and where  $b_n$  and  $b_0$  are the most and least significant bits respectively, then the decimal value is calculated as,

$$v = \sum_{i=0}^{n} b_i 2^i \tag{5.2}$$

For example,  $10011_2 = 1 + 2 + 16 = 19$ . Converting from decimal to binary is a little more complex, but a simple divide-by-two algorithm exists. The key to understanding the divide-by-two algorithm is to realize that dividing a number by two is equivalent to shifting its binary representation one position to the right. E.g.,  $10 = 1010_2$  and  $10/2 = 5 = 101_2$ . Odd numbers have  $b_0 = 1$ , e.g.,  $11_{10} = 1011_2$  and  $11_{10}/2 = 5.5 = 101.1_2$ . Hence, if we divide any number by two and get a non-integer number, then its least significant bit was 1. Another way to express this is to say that the least significant bit is the remainder after integer division by two. Sequential application of this idea leads directly to the divide-by-two algorithm. E.g., if we were to convert the number  $11_{10}$  in decimal form to binary form, we would perform the following steps:



Here we used div and rem to signify the integer division and remainder operators. The algorithm stops when the result of integer division is zero. Reading off the remainder from below and up, we find the sequence 1011<sub>2</sub>, which is the binary form of the decimal

number  $11_{10}$ . Using the interactive mode, we can perform the same calculation, as shown in Listing 5.29.

Thus, by reading the second integer-response from printfn from below and up, we again obtain the binary form of  $11_{10}$  to be  $1011_2$ . For integers with a fractional part, the divide-by-two algorithm may be used on the whole part, while multiply-by-two may be used in a similar manner on the fractional part.

In this chapter, we will see how we can bind expressions to identifiers either as new constants, functions, or operators, how this saves time when building large programs, and how this makes programs easier to read and debug. As an example, consider the following problem,

### Problem 6.1

For given set constants a, b, and c, solve for x in

$$ax^2 + bx + c = 0 (6.1)$$

To solve for x we use the quadratic formula from elementary algebra,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a},\tag{6.2}$$

which gives the general solution for any values of the coefficients. Here, we will assume a positive discriminant,  $b^2 - 4ac > 0$ . In order to write a program where the code may be reused later, we define a function discriminant: float -> float -> float -> float, that is, a function that takes 3 arguments, a, b, and c, and calculates the discriminant. Likewise, we will define positiveSolution: float -> float -> float -> float and negativeSolution: float -> float -> float, that also take the polynomial's coefficients as arguments and calculate the solution corresponding to choosing the positive and negative sign for  $\pm$  in the equation. Details on function definition is given in Section 6.2. Our solution thus looks like Listing 6.1.

### Listing 6.1 identifiers Example. fsx: Finding roots for quadratic equations using function name binding. let discriminant a b c = b \*\* 2.0 - 4.0 \* a \* c let positiveSolution a b c = (-b + sqrt (discriminant a b c)) /(2.0 \* a)let negativeSolution a b c = (-b - sqrt (discriminant a b c)) / (2.0 \* a)let a = 1.0let b = 0.0let c = -1.0let d = discriminant a b c let xp = positiveSolution a b c let xn = negativeSolution a b c do printfn "0 = %A \* x \*\* 2.0 + %A \* x + %A" a b c do printfn " has discriminant %A and solutions %A and %A" d xn xp \$ fsharpc --nologo identifiersExample.fsx && mono identifiersExample.exe 0 = 1.0 \* x \*\* 2.0 + 0.0 \* x + -1.0has discriminant 4.0 and solutions -1.0 and 1.0

Here, we have further defined names of values a, b, and c which are used as inputs to our functions, and the results of function application are bound to the names d, xn, and xp. The names of functions and values given here are examples of identifiers, and with these, we may reuse the quadratic formulas and calculated values later, while avoiding possible typing mistakes and reducing the amount of code which needs to be debugged.

The use of identifiers is central in programming. For F#, not to be confused with built-in functionality, identifiers must follow a specific set of rules:

· identifier

### Identifier

- Identifiers are used as names for values, functions, types etc.
- They must start with a Unicode letter or underscore ', but can be followed by zero or more of letters, digits, and a range of special characters except for SP, LF, and CR (space, line feed, and carriage return). See Appendix C.3 for more on codepoints that represents letters.
- They can also be a sequence of identifiers separated by a period.
- They cannot be keywords, see Table 6.1.

Examples of identifiers are: a, the Character 9, Next\_Word, \_tok, and f.sharp.rocks. Since programmers often work in multilingual environment dominated by the English language it is advicable to restrict identifiers to use letters from the English alphabet, Advice numbers, period, and ' '. However, the number of possible identifiers is enormous. The full definition refers to the Unicode general categories described in Appendix C.3, and there are currently 19.345 possible Unicode code points in the letter category and 2.245 possible Unicode code points in the special character category.

Type	Keyword
Regular	abstract, and, as, assert, base, begin, class, default,
	delegate, do, done, downcast, downto, elif, else, end,
	exception, extern, false, finally, for, fun, function,
	global, if, in, inherit, inline, interface, internal, lazy,
	let, match, member, module, mutable, namespace, new, null, of,
	open, or, override, private, public, rec, return, sig, static,
	struct, then, to, true, try, type, upcast, use, val, void, when,
	while, with, and yield.
Reserved	atomic, break, checked, component, const, constraint, constructor, continue, eager, fixed, fori, functor, include, measure, method, mixin, object, parallel, params, process, protected, pure, recursive, sealed, tailcall, trait, virtual, and volatile.
Symbolic	<pre>let!, use!, do!, yield!, return!,  , -&gt;, &lt;-, ., :, (, ), [, ], [&lt;, &gt;], [ ,  ], {, }, ', #, :?&gt;, :?, :&gt;,, ::, :=, ;;, ;, =, _, ?, ??, (*), &lt;@, @&gt;, &lt;@@, and @@&gt;.</pre>
Reserved symbolic	~ and `

Table 6.1.: Table of (possibly future) keywords and symbolic keywords in F#.

Identifiers may be used to carry information about their intended content and use, and careful selection of identifiers can aid programmers to communicate thoughts about the code. Thus, identifiers are often a word or several concatenated words conveying some relevant meaning. For example, in the function definition let discriminant a b c = b \*\* 2.0 - 4.0 \* a \* c, the function identifier has been chosen to be discriminant. F# places no special significance to the word 'discriminant', and the program would work exactly the same had the function been called let f a b c = b \*\* 2.0 - 4.0 \* a \* c. However, to programmers, the word 'discriminant' informs us of the intended role of the function and thus is much preferred. This is a general principle: identifier names should be chosen to reflect their semantic value. The arguments a, b, and c are short, but adheres to a textbook tradition of elementary algebra. Again, we might as well have used, let discriminant c a b = a \*\* 2.0 - 4.0 \* c \* b, which is semantically identical to the original expression, but due to tradition, this would confuse most readers of the code. Thus, identifier names should be chosen consistently with the readers' traditions. Finally, identifiers are often concatenations of words, as positiveSolution in Listing 6.1. Concatenations can be difficult to read. Without the capitalization of the second word, we would have had positive solution. This is readable at most times, but takes longer time to understand in general. Typical solutions are to use a separator, such as positive\_solution, lower camel case also known as mixed case as in the example positiveSolution, and upper camel case also known as pascal case as PositiveSolution. In this book, we use lower camel case except where F# requires a capital first letter. Again, the choice does not influence what a program does, only how readable it is to a fellow programmer. The important part is that identifier names consisting of concatenated words are often preferred over names with few character, and concatenation should be emphasized, e.g., by camel casing. Choosing the length of identifier names is a balancing act, since when working with large programs, very long identifier names can be tiresome to write, and a common practice is that the length of identifier names is proportional to the complexity of the program. I.e., complex programs use long names, simple programs use short names. What is complex and what is simple is naturally in the eye of the beholder, but when you program, remember that a future reader of the program most likely has not had time to work with the problem as long as the programmer, thus

Advice

Advice

 $\cdot$  lower camel case

 $\cdot$  mixed case

 $\cdot$  upper camel case

 $\cdot$  pascal case

Advice

choose identifier names as if you were to explain the meaning of a program to Advice a knowledgeable outsider.

Another key concept in F# is expressions. An expression can be a mathematical expression, such as 3\*5, a function application, such as f3, and many other things. Central in this chapter is the binding of values and functions to identifiers, which is done with the keyword let, e.g., let a = 1.0.

Expressions are the main workhorse of F# and have an enormous variety in how they may be written. We will in this book gradually work through some of the more important facets.

 $\cdot$  expression

### **Expressions**

- An Expression is a computation such as 3 \* 5.
- They can be value bindings between identifiers and expressions that evaluate to a value or a function, see Sections 6.1 and 6.2.
- They can be do-bindings that produce side-effects and whose result are ignored, see Section 6.2
- They can be assignments to variables, see Section 6.1.
- They can be a sequence of expressions separated with the ";" lexeme. ٠;
- ٠: • They can be annotated with a type by using the ":" lexeme.

Before we begin a deeper discussion on bindings, note that F# adheres to two different syntaxes: verbose and lightweight. In the verbose syntax, newlines and whitespaces are generally ignored, while in lightweight syntax, certain keywords and lexemes may be replaced by newlines and whitespaces. The lightweight syntax is the most common, but the syntaxes may be mixed, and we will highlight the options, when relevant.

· verbose syntax

· lightweight syntax

### 6.1. Value Bindings

Binding identifiers to literals, or expressions that are evaluated to be values, is called *value*binding, and examples are let a = 3.0 and let  $b = \cos 0.9$ . Value bindings have the  $\cdot$  value-binding following syntax:

```
Listing 6.2:
            Value binding expression.
let <valueIdent> = <bodyExpr> [in <expr>]
```

The let keyword binds a value-identifier <valueIdent> with an expression <bodyExpr> ·let that evaluates to a value. The following square bracket notation [] means that the enclosed is optional, and F# is able to identify whether or not the optional part is used by whether or not the *in* keyword is present in the binding expression. If the *in* keyword is used, then the value-identifier is a local definition in the following <expr> expression but in the following lines. For lightweight syntax, the in keyword is replaced with a newline, and the binding is valid in the following lines at the level of scope of the value-binding, or deeper, lexically.

· lexically

The value identifier annotated with a type by using the ":" lexeme followed by the name of : a type, e.g., int. The "\_" lexeme may be used as a value-identifier. This lexeme is called :— the *wildcard* pattern, and for value-bindings it means that <code><bodyExpr></code> is evaluated, but · wildcard the result is discarded. See Chapter 15 for more details on patterns.

For example, letting the identifier **p** be bound to the value 2.0 and using it in an expression is done as shown in Listing 6.3.

```
Listing 6.3 letValue.fsx:
The identifier p is used in the expression following the keyword.

1 let p = 2.0 in do printfn "%A" (3.0 ** p)

1 $ fsharpc --nologo letValue.fsx && mono letValue.exe
2 9.0
```

F# will ignore most newlines between lexemes, i.e., the above is equivalent to writing as shown in Listing 6.4.

```
Listing 6.4 letValueLF.fsx:
Newlines after make the program easier to read.

1 let p = 2.0 in
2 do printfn "%A" (3.0 ** p)

1 $ fsharpc --nologo letValueLF.fsx && mono letValueLF.exe
2 9.0
```

F# also allows for an alternative notation called *lightweight syntax*, where e.g., the in · lightweight syntax keyword is replaced with a newline, and the expression starts on the next line at the same column as let starts in, i.e., the above is equivalent to Listing 6.5.

```
Listing 6.5 letValueLightWeight.fsx:
Lightweight syntax does not require the keyword, but the expression must be aligned with the keyword.

1 let p = 2.0
2 do printfn "%A" (3.0 ** p)

1 $ fsharpc --nologo letValueLightWeight.fsx
2 $ mono letValueLightWeight.exe
3 9.0
```

The same expression in interactive mode will also show with the inferred types, as shown in Listing 6.6.

### Listing 6.6: Interactive mode also outputs inferred types. 1 > let p = 2.0 2 - do printfn "%A" (3.0 \*\* p);; 3 9.0 4 val p : float = 2.0 5 val it : unit = ()

By the val keyword in the line val p: float = 2.0, we see that p is inferred to be of type float and bound to the value 2.0. The inference is based on the type of the right-hand-side which is float. Identifiers may be defined to have a type using the ":" lexeme, but the types on the left-hand-side and right-hand-side of the "=" lexeme must be identical. Mixing types gives an error, as shown in Listing 6.7.

```
Listing 6.7 letValueTypeError.fsx:
Binding error due to type mismatch.

let p : float = 3
do printfn "%A" (3.0 ** p)

$ fsharpc --nologo letValueTypeError.fsx && mono letValueTypeError.exe

letValueTypeError.fsx(1,17): error FS0001: This expression was expected to have type
'float'
but here has type
'int'
```

Here, the left-hand-side is defined to be an identifier of type float, while the right-hand-side is a literal of type integer.

An expression can be a sequence of expressions separated by the lexeme ";", see Listing 6.8.

```
Listing 6.8 letValueSequence.fsx:
A value-binding for a sequence of expressions.

1 let p = 2.0 in do printfn "%A" p; do printfn "%A" (3.0 ** p)

1 $ fsharpc --nologo letValueSequence.fsx && mono letValueSequence.exe
2 2.0
3 9.0
```

The lightweight syntax automatically inserts the ";" lexeme at newlines, hence using the lightweight syntax, the above is the same as shown in Listing 6.9.

### Listing 6.9 letValueSequenceLightWeight.fsx: A value-binding for a sequence using lightweight syntax. 1 let p = 2.0 2 do printfn "%A" p 3 do printfn "%A" (3.0 \*\* p) 1 \$ fsharpc --nologo letValueSequenceLightWeight.fsx 2 \$ mono letValueSequenceLightWeight.exe 3 2.0 4 9.0

A key concept of programming is scope. In F#, the scope of a value-binding is lexically. • scope This means that when F# seeks the value bound to a name, it looks left and upward in the program text for its let-binding in the present or higher scopes, see Listing 6.10 for an example.

```
Listing 6.10 letValueScopeLower.fsx:
Redefining identifiers is allowed in lower scopes.

1 let p = 3 in let p = 4 in do printfn " %A" p;

1 $ fsharpc --nologo letValueScopeLower.fsx && mono letValueScopeLower.exe
2 4
```

Some special bindings are mutable, in which case F# uses the dynamic scope, that is, the value of a binding is defined by when it is used. This will be discussed in Section 6.7.

Scopes are given levels, and scopes may be nested, where the nested scope has a level one lower than its parent.<sup>1</sup> F# distinguishes between the top and lower levels, and at the top level in the lightweight syntax, redefining values is not allowed, as shown in Listing 6.11.

```
Listing 6.11 letValueScopeLowerError.fsx:
Redefining identifiers is not allowed in lightweight syntax at top level.

1 let p = 3
2 let p = 4
3 do printfn "%A" p;

1 $ fsharpc --nologo -a letValueScopeLowerError.fsx

2 letValueScopeLowerError.fsx(2,5): error FS0037: Duplicate definition of value 'p'
```

However, using parentheses, we create a block, i.e., a  $nested\ scope$ , and then redefining is · block allowed, as demonstrated in Listing 6.12. · nested scope

<sup>&</sup>lt;sup>1</sup>Jon: Drawings would be good to describe scope

## Listing 6.12 letValueScopeBlockAlternative3.fsx: A block may be created using parentheses. 1 ( 2 let p = 3 3 let p = 4 4 do printfn "%A" p 5 ) 1 \$ fsharpc --nologo letValueScopeBlockAlternative3.fsx 2 \$ mono letValueScopeBlockAlternative3.exe 3 4

Nevertheless, avoid reusing names unless it's in a deeper scope.

Advice

Inside the block in Listing 6.12 we used indentation, which is good practice, but not required here.

Bindings inside a nested scope are not available outside, as shown in Listing 6.13.

```
Listing 6.13 letValueScopeNestedScope.fsx:
Bindings inside a scope are not available outside.

let p = 3
(
let q = 4
do printfn "%A" q
)
do printfn "%A %A" p q

fsharpc --nologo -a letValueScopeNestedScope.fsx

letValueScopeNestedScope.fsx(6,22): error FS0039: The value or constructor 'q' is not defined. Maybe you want one of the following:
p
```

Nesting is a natural part of structuring code, e.g., through function definitions to be discussed in Section 6.2 and flow control structures to be discussed in Chapter 8. Blocking code by nesting is a key concept for making robust code that is easy to use by others, without the user necessarily needing to know the details of the inner workings of a block of code.

Defining blocks is used for controlling the extent of a lexical scope of bindings. For example, adding a second printfn statement, as in Listing 6.14, will print the value 4, last bound to the identifier p, since F# interprets the above as let p=3 in let p=4 in (printfn "%A" p; printfn "%A" p).

### Listing 6.14 letValueScopeBlockProblem.fsx: Overshadowing hides the first binding. 1 let p = 3 in let p = 4 in do printfn "%A" p; do printfn "%A" p 1 \$ fsharpc --nologo letValueScopeBlockProblem.fsx 2 \$ mono letValueScopeBlockProblem.exe 3 4 4 4

Had we intended to print the two different values of p, then we should have created a block as in Listing 6.15.

```
Listing 6.15 letValueScopeBlock.fsx:

Blocks allow for the return to the previous scope.

1 let p = 3 in (let p = 4 in do printfn "%A" p); do printfn "%A" p;

1 $ fsharpc --nologo letValueScopeBlock.fsx && mono letValueScopeBlock.exe

2 4
3 3
```

### 6.2. Function Bindings

A function is a mapping between an input and output domain. A key advantage of using functions when programming is that they encapsulate code into smaller units, that are easier to debug and may be reused. F# is a functional first programming language and offers a number of alternative methods for specifying parameters, which will be discussed in this section. Binding identifiers to functions follows a syntax similar to value-binding,

```
Listing 6.16: Function binding expression

1 let <funcIdent> <arg> {<arg>} | () = <bodyExpr> [in <expr>]
```

Here <funcIdent> is an identifier and is the name of the function, <arg> is zero or more identifiers, that bind to the value used when calling the function, and which is to be used in the body of the function, the expression <bodyExpr>. The | notation denotes a choice, i.e., either that on the left-hand-side or that on the right-hand-side. Thus let f x = x \* x and let f () = 3 are valid function bindings, but let f = 3 would be a value binding, not a function binding. The arguments and the function may be annotated with a type, in which case for arguments we write

where <type> is a name of an existing type. The argument types are given in parentheses, and the return type is given last.

Functions are a key concept in F#, and in this chapter we will discuss the very basics. Recursive functions will be discussed in Chapter 8 and higher-order functions in Chapter 16.

An example of defining a function and using it in interactive mode is shown in Listing 6.18.

```
Listing 6.18: An example of a binding of an identifier and a function.

1 > let sum (x : float) (y : float) : float = x + y in

2 - let c = sum 357.6 863.4 in

3 - do printfn "%A" c;;

4 1221.0

5 val sum : x:float -> y:float -> float

6 val c : float = 1221.0

7 val it : unit = ()
```

Here we see that the function is interpreted to have the type val sum: x:float -> y:float -> float. The "->" lexeme means a mapping between sets, in this case, floats. The function is also a higher order function, to be discussed in detail below, and here it suffices to think of sum as a function that takes 2 floats as argument and returns a float.

Not all types need to be declared, just a sufficient number for F# to be able to infer the types for the full statement. For the example, one is sufficient, and we could just have declare the type of the result, as in Listing 6.19.

```
Listing 6.19 letFunctionAlterantive.fsx:
Not every type needs to be declared.

1 let sum x y : float = x + y
```

Or even just one of the arguments, as in Listing 6.20.

```
Listing 6.20 letFunctionAlterantive2.fsx:
Just one type is often enough for F# to infer the rest.

1 let sum (x : float) y = x + y
```

In both cases, since the + operator is only defined for operands of the same type, declaring · operator the type of either arguments or result implies the type of the remainder. As for values, · operand lightweight syntax automatically inserts the keyword in and the lexeme ";", as shown in Listing 6.21.

### Listing 6.21 letFunctionLightWeight.fsx: Lightweight syntax for function definitions. let sum x y : float = x + ylet c = sum 357.6 863.4do printfn "%A" c \$ fsharpc --nologo letFunctionLightWeight.fsx \$ mono letFunctionLightWeight.exe 1221.0

Arguments need not always be inferred to types, but may be of the generic type when type safety is ensured, as shown in Listing 6.22.

· type safety

```
Listing 6.22: Type safety implies that a function will work for any type.
> let second x y = y
- let a = second 3 5
- do printfn "%A" a
- let b = second "horse" 5.0
- do printfn "%A" b;;
val second : x:'a -> y:'b -> 'b
val a : int = 5
val b : float = 5.0
 val it : unit = ()
```

Here, the function second does not use the first argument x, which therefore can be of any type, and which F#, therefore, calls 'a. The type of the second element, y, can also be of any type and not necessarily the same as x, so it is called 'b. Finally, the result is the same type as y, whatever it is. This is an example of a generic function, since it will work • generic function on any type.

A function may contain a sequence of expressions but must return a value. E.g., the quadratic formula may be written as shown in Listing 6.23.

### Listing 6.23 identifiers Example Advance.fsx: A function may contain sequences of expressions. let solution a b c sgn = let discriminant a b c = b \*\* 2.0 - 2.0 \* a \* c let d = discriminant a b c (-b + sgn \* sqrt d) / (2.0 \* a)let a = 1.0let b = 0.0let c = -1.0let xp = solution a b c +1.0let xn = solution a b c -1.0do printfn "0 = %A \* x \*\* 2.0 + %A \* x + %A" a b c do printfn " has solutions %A and %A" xn xp \$ fsharpc --nologo identifiersExampleAdvance.fsx \$ mono identifiersExampleAdvance.exe 0 = 1.0 \* x \*\* 2.0 + 0.0 \* x + -1.0has solutions -0.7071067812 and 0.7071067812

Here, we used the lightweight syntax, where the "=" identifies the start of a nested scope, and F# identifies the scope by indentation. The amount of space used for indentation does not matter, but all lines in the same scope must use the same amount. The scope ends before the first line with the previous indentation or none. Notice how the last expression is not bound to an identifier, but is the result of the function, i.e., in contrast to many other languages, F# does not have an explicit keyword for returning values, but requires a final expression, which will be returned to the caller of the function. Note also that since the function discriminant is defined in the nested scope of solution, and because the scope ends before let a = 1.0, discriminant cannot be called outside solution.

Lexical scope and function definitions can be a cause of confusion, as the following example  $\cdot$  lexical scope in Listing 6.24 shows.<sup>2</sup>

```
Listing 6.24 lexicalScopeNFunction.fsx:
Lexical scope means that f(z) = 3x and not 4x at the time of calling.

1 let testScope x =
2 let a = 3.0
3 let f z = a * z
4 let a = 4.0
5 f x
6 do printfn "%A" (testScope 2.0)

1 $ fsharpc --nologo lexicalScopeNFunction.fsx
2 $ mono lexicalScopeNFunction.exe
3 6.0
```

Here, the value-binding for a is redefined after it has been used to define a helper function f. So which value of a is used when we later apply f to an argument? To resolve the

<sup>&</sup>lt;sup>2</sup>Jon: Add a drawing or possibly a spell-out of lexical scope here.

confusion, remember that value-binding is lexically defined, i.e., the binding let f z =a \* z uses the value of a as it is defined by the ordering of the lines in the script, not dynamically by when f was called. Hence, think of lexical scope as substitution of Advice an identifier with its value or function immediately at the place of definition. Since a and 3.0 are synonymous in the first lines of the program, the function f is really defined as let f z = 3.0 \* z.

Functions do not need a name, but may be declared as an anonymous function using the · anonymous function fun keyword and the "->" lexeme, as shown in Listing 6.25.

· fun

· ->

```
Listing 6.25 functionDeclarationAnonymous.fsx:
Anonymous functions are functions as values.
let first = fun x y -> x
do printfn "%d" (first 5 3)
$ fsharpc --nologo functionDeclarationAnonymous.fsx
  mono functionDeclarationAnonymous.exe
5
```

Here, a name is bound to an anonymous function which returns the first of two arguments. The difference to let first x y = x is that anonymous functions may be treated as values, meaning that they may be used as arguments to other functions and the new values may be reassigned to their identifiers when mutable, as will be discussed in Section 6.7. A common use of anonymous functions is as arguments to other functions, as demonstrated in Listing 6.26.

```
Listing 6.26 functionDeclarationAnonymousAdvanced.fsx:
Anonymous functions are often used as arguments for other functions.
let apply f x y = f x y
let mul = fun a b \rightarrow a * b
do printfn "%d" (apply mul 3 6)
 $ fsharpc --nologo functionDeclarationAnonymousAdvanced.fsx
 $ mono functionDeclarationAnonymousAdvanced.exe
 18
```

Note that here apply is given 3 arguments: the function mul and 2 integers. It is not given the result of mul 3 6, since that would not match the definition of apply. Anonymous Advice functions and functions as arguments are powerful concepts, but tend to make programs harder to read, and their use should be limited.

The result of one function is often used as an argument of another. This is function composition, and an example is shown in Listing 6.27.

### Listing 6.27 functionComposition.fsx: Composing functions using intermediate bindings. let f x = x + 1let g x = x \* xlet a = f 2let b = g alet c = g (f 2)do printfn "a = %A, b = %A, c = %A" a b c \$ fsharpc --nologo functionComposition.fsx \$ mono functionComposition.exe a = 3, b = 9, c = 9

In the example we combine two functions f and g by storing the result of f 2 in a and using that as argument of g. This is the same as g (f 2), and in the later case, the compile creates a temporary value for f 2. Such compositions are so common in F# that a special set of operators has been invented, called the *piping* operators: "/>" and "</". They are · piping used as demonstrated in Listing 6.28.

. |>

. < |

```
Listing 6.28 functionPiping.fsx:
Composing functions by piping.
let f x = x + 1
let g x = x * x
let a = g (f 2)
let b = 2 | > f | > g
let c = g < | (f < | 2)
do printfn "a = %A, b = %A, c = %A" a b c
$ fsharpc --nologo functionPiping.fsx && mono
   functionPiping.exe
 a = 9, b = 9, c = 9
```

The example shows regular composition, left-to-right, and right-to-left piping. The word piping is a picturial description of data as if it were flowing through pipes, where functions are connection points of pipes distributing data in a network. The three expressions in Listing 6.28 perform the same calculation. The left-to-right piping in line 5 corresponds to the left-to-right reading direction, i.e., the value 2 is used as argument to f, and the result is used as argument to g. In contrast, right-to-left piping in line 6 has the order of arithmetic composition as line 4. Unfortunately, since the piping operators are leftassociative, without the parenthesis in line 6 g < | f < | 2, F# would read the expression as (g < | f) < | 2. That would have been an error, since g takes an integer as argument, not a function. F# can also define composition on a function level. Further discussion on this is deferred to Chapter 16. The piping operator comes in four variants: "||>", "<||", "|||>", and "<|||". These allow for piping between pairs and triples to functions of 2 and 3 arguments, see Listing 6.29 for an example.

### Listing 6.29 functionTuplePiping.fsx: Tuples can be piped to functions of more than one argument. let f x = printfn "%A" x let g x y = printfn "%A %A" x y let h x y z = printfn "%A %A %A" x y z 1 |> f (1, 2) | | > g $(1, 2, 3) \mid \mid \mid > h$ \$ fsharpc --nologo functionTuplePiping.fsx \$ mono functionTuplePiping.exe 1 1 2 1 2 3

The example demonstrates right-to-left piping, left-to-right works analogously.<sup>3</sup>

A procedure is a generalization of the concept of functions, and in contrast to functions, · procedure procedures need not return values. This is demonstrated in Listing 6.30.

```
Listing 6.30 procedure.fsx:
A procedure is a function that has no return value, and in F\# returns "()".
let printIt a = printfn "This is '%A'" a
do printIt 3
do printIt 3.0
$ fsharpc --nologo procedure.fsx && mono procedure.exe
This is '3'
This is '3.0'
```

In F#, this is automatically given the unit type as the return value. Procedural thinking is useful for encapsulation of scripts, but is prone to side-effects. For this reason, it is  $\cdot$  encapsulation adviced to prefer functions over procedures. More on side-effects in Section 6.7.

 $\cdot$  side-effects Advice

· first-class citizens

values: They may be passed as arguments, returned from a function, and bound to a name. For first-class citizens, the name it is bound to does not carry significance to the language, as, e.g., illustrated with the use of anonymous functions. Technically, a function is stored as a closure. A closure is a description of the function, its arguments, its expression, and

In F#, functions (and procedures) are first-class citizens, which means that functions are

the environment at the time it was created, i.e., the triple (args, exp, env). Consider the listing in Listing 6.31.

· closure

<sup>&</sup>lt;sup>3</sup>Jon: Tuples have not yet been introduced!

# Listing 6.31 functionFirstClass.fsx: The function ApplyFactor has a non-trivial closure. 1 let mul x y = x \* y 1 let factor = 2.0 1 let applyFactor fct x = 1 let a = fct factor x 5 string a 6 do printfn "%g" (mul 5.0 3.0) 6 do printfn "%s" (applyFactor mul 3.0) 1 \$ fsharpc --nologo functionFirstClass.fsx && mono functionFirstClass.exe 2 15 3 6

It defines two functions mul and applyFactor, where the latter is a higher order function taking another function as an argument and uses part of the environment to produce its result. The two closures are:

The function mul does not use its environment, and everything needed to evaluate its expression are values for its arguments. The function applyFactor also takes two arguments, a function and a value. It uses factor from the environment, thus this is stored in its closure. When mul is given as an argument in Listing 6.31 line 8, then it is its closure which is given to applyFactor, and the closure contains everything that applyFactor requires to use mul. Likewise, if applyFactor is given as argument to yet another function, then its closure includes the relevant part of its environment at the time of definition, factor, such that when applyFactor is applied to two arguments, then its closure contains everything needed to evaluate its expression.

### 6.3. Operators

Operators are functions, and in F#, the infix multiplication operator + is equivalent to the function (+), as shown in Listing 6.32.

## Listing 6.32 addOperatorNFunction.fsx: Operators have function equivalents. 1 let a = 3.0 2 let b = 4.0 3 let c = a + b 4 let d = (+) a b 5 do printfn "%A plus %A is %A and %A" a b c d 1 \$ fsharpc --nologo addOperatorNFunction.fsx 2 \$ mono addOperatorNFunction.exe 3 3.0 plus 4.0 is 7.0 and 7.0

All operators have this option, and you may redefine them and define your own operators, but in F# names of user-defined operators are limited:

- A unary operator name can be: "+", "-", "+.", "-.", "%", "&", "&", "~", "~~", ..., ... unary operator "~~~", ..., apostropheOp. Here apostropheOp is an operator name starting with "!" and followed by one or more of either "!", "%", "&", "\*", "+", "-", ".", "/", "<", "=", ">", "@", "~", "|", "~", but apostropheOp cannot be "!=".

The precedence rules and associativity of user-defined operators follow the rules for which they share prefixes with built-in rules, see Table E.5. E.g., .\*, +++, and <+ are valid operator names for infix operators, they have precedence as ordered, and their associativities are all left. Using ~ as the first character in the definition of an operator makes the operator unary and will not be part of the name. Examples of definitions and use of operators are,

```
Listing 6.33 operator Definitions.fsx:
Operators may be (re)defined by their function equivalent.
let (.*) x y = x * y + 1
printfn "%A" (3 .* 4)
let (+++) x y = x * y + y
printfn "%A" (3 +++ 4)
let (<+) x y = x < y + 2.0
printfn "%A" (3.0 <+ 4.0)
let (^+.) x = x+1
printfn "%A" (+.1)
$ fsharpc --nologo operatorDefinitions.fsx
$ mono operatorDefinitions.exe
13
16
 true
 2
```

Operators beginning with \* must use a space in its definition. For example, without a

space ( \* would be confused with the beginning of a comment (\*, see Chapter 7 for more on comments in the code.

Beware, redefining existing operators lexically redefines all future uses of the operators for all types, hence it is not a good idea to redefine operators, but better to define Advice **new ones.** In Chapter 20 we will discuss how to define type-specific operators, including prefix operators.

### 6.4. Do Bindings

Aside from let bindings that binds names with values or functions, sometimes we just need to execute code. This is called a do binding or, alternatively, a statement. The syntax is as follows:

· do binding  $\cdot$  statement

```
Listing 6.34: Syntax for do bindings.
 [do ]<expr>
```

The expression <expr> must return unit. The keyword do is optional in most cases, but using it emphasizes that the expression is not a function that returns a useful value. Procedures are examples of such expressions, and a very useful family of procedures are the printf family described below. In the remainder of this book, we will refrain from using the do keyword.

### 6.5. The Printf Function

A common way to output information to the console is to use one of the family of printf · printf commands. These functions are special, since they take a variable number of arguments, and the number is decided by the first argument - the format string. The syntax for the printf commands are as follows:

```
Listing 6.35: printf statement.
printf <format-string> {<ident>}
```

The formatString is a string (simple or verbatim) with placeholders. The function printf prints formatString to the console, where all placeholder have been replaced by the values of the corresponding arguments formatted as specified. For example, in printfn "1 2 %d" 3, the format String is "1 2 %d" and the placeholder is %d. When executed, printf will replace %d with the following argument, 3, and print the result to the console: 1 2 3. There are specifiers for all the basic types, and more, as elaborated in Table 6.2. The placeholder can be parametrized, e.g., the placeholder string \%s will print a right-aligned string which that is eight characters wide and padded with spaces, as needed. For floating point numbers, %8f will print a number that is exactly seven digits and a decimal point, making eight characters in total. Zeros are added after the decimal point, as needed. Alternatively, we may specify the number of digits after the decimal point, such that \%8.1f will print a floating point number, aligned to the right, with one

Specifier	Type	Description
%b	bool	replaces with boolean
		value
%s	string	
%с	char	
%d, %i	basic integer	
%u	basic unsigned integers	
%x	basic integer	formatted as unsigned
		hexadecimal with lower
		case letters
%X	basic integer	formatted as unsigned
		hexadecimal with upper
		case letters
%0	basic integer	formatted as unsigned oc-
		tal integer
%f, %F,	basic floats	formatted on decimal
		form
%e, %E,	basic floats	formatted on scientific
		form. Lower case uses "e"
		while upper case uses "E"
		in the formatting.
%g, %G,	basic floats	formatted on the shortest
		of the corresponding dec-
0/2-2		imal or scientific form.
%M	decimal	
%0	Objects ToString method	
%A	any built-in types	formatted as a literal type
%a	Printf.TextWriterFormat ->'a -> ()	
%t	(Printf.TextWriterFormat -> ()	

Table 6.2.: Printf placeholder string

digit after the decimal point padded with spaces, as needed. The default is for the value to be right justified in the field, but left justification can be specified by the - character. For number types, you can specify their format by "0" for padding the number with zeros to the left when right justifying the number; "+" to explicitly show a plus sign for positive numbers; SP to enforce a space, where there otherwise would be a plus sign for positive numbers. The placeholder parameter may also be given as an argument to printf which case the placeholder should use the \* character instead of an integer.

Examples of placeholder parametrization are shown in Listing 6.36.

### Listing 6.36 printfExample.fsx: Examples of printf and some of its formatting options. let pi = 3.1415192let hello = "hello" printf "An integer: %d\n" (int pi) printf "A float %f on decimal form and on %e scientific form\n" pi pi printf "A char '%c' and a string \"%s\"\n" hello.[0] hello printf "Float using width 8 and 1 number after the decimal: $\n"$ printf " \"%8.1f\" \"%8.1f\"\n" pi -pi printf " \"%08.1f\" \"%08.1f\"\n" pi -pi printf " \"% 8.1f\" \"% 8.1f\"\n" pi -pi printf " \"%-8.1f\" \"%-8.1f\"\n" pi -pi printf " \"%+8.1f\" \"%+8.1f\"\n" pi -pi printf " \"%8s\"\n\"%-8s\"\n" "hello" "hello" \$ fsharpc --nologo printfExample.fsx && mono printfExample.exe An integer: 3 A float 3.141519 on decimal form and on 3.141519e+000 scientific form A char 'h' and a string "hello" Float using width 8 and 1 number after the decimal: 3.1" " -3.1" "000003.1" "-00003.1" 3.1" " -3.1" "3.1 " "-3.1 " +3.1" " -3.1" " hello" "hello "

Not all combinations of flags and identifier types are supported, e.g., strings cannot have the number of integers after the decimal point specified. The placeholder types "%A", "%a", and "%t" are special for F#, examples of their use are shown in Listing 6.37.

```
Listing 6.37 printfExampleAdvance.fsx:

Custom format functions may be used to specialise output.

1 let noArgument writer = printf "I will not print anything"
2 let customFormatter writer arg = printf "Custom formatter got:
\"%A\"" arg
3 printf "Print examples: %A, %A, %A\n" 3.0m 3uy "a string"
4 printf "Print function with no arguments: %t\n" noArgument
5 printf "Print function with 1 argument: %a\n" customFormatter
3.0

1 $ fsharpc --nologo printfExampleAdvance.fsx
$ mono printfExampleAdvance.exe
Print examples: 3.0M, 3uy, "a string"
Print function with no arguments: I will not print anything
Print function with 1 argument: Custom formatter got: "3.0"
```

The %A is special in that all built-in types, including tuples, lists, and arrays to be discussed

Function	Example	Description
printf	printf "%d apples" 3	Prints to the console, i.e., stdout
printfn		As printf and adds a newline.
fprintf	fprintf stream "%d apples" 3	Prints to a stream, e.g., stderr and
		stdout, which would be the same as
		printf and eprintf.
fprintfn		As fprintf but with added new-
		line.
eprintf	eprintf "%d apples" 3	Prints to stderr
eprintfn		As eprintf but with added new-
		line.
sprintf	printf "%d apples" 3	Return printed string
failwithf	failwithf "%d failed apples" 3	Prints to a string and used for rais-
		ing an exception.

Table 6.3.: The family of printf functions.

in Chapter 11, can be printed using this formatting string, but notice that the formatting performed includes the named literal string. The two formatting strings %t and %a are options for user-customizing the formatting and will not be discussed further.

Beware, formatString is not a string but a Printf.TextWriterFormat, so to predefine a formatString as, e.g., let str = "hello %s" in printf str "world", will be a type error.

The family of printf is shown in Table 6.3. The function fprintf prints to a stream, e.g., stderr and stdout, of type System.IO.TextWriter. For the moment it is sufficient to think of both stderr and stdout to be the console. Streams will be discussed in further detail in Chapter 19. The function failwithf is used with exceptions, see Chapter 18 for more details. The function has a number of possible return value types, and for testing, the *ignore* function ignores it all, e.g., ignore (failwithf "%d failed apples" 3).

·ignore

### 6.6. Reading from the Console

The printf and printfn functions allow us to write text on the screen. A program often needs to ask a user to input data, e.g., by typing text on a keyboard. Text typed on the keyboard is accessible through the stdin stream, and F# provides several library functions for capturing text typed on the keyboard. In the following section, we will briefly discuss the System.Console.ReadLine function. For more details and other methods of input see Chapters 19 and 23.

The function System.Console.ReadLine takes a unit value as an argument and returns the string the user typed. The program will not advance until the user presses newline. An example of a program that multiplies two floating point numbers supplied by a user is given in Listing 6.38,

### Listing 6.38 userDialoguePrintf.fsx: Interacting with a user using ReadLine. 1 printfn "To perform the multiplication of a and b" 2 printf "Enter a: " 3 let a = float (System.Console.ReadLine ()) 4 printf "Enter b: " 5 let b = float (System.Console.ReadLine ()) 6 printfn "a \* b = %A" (a \* b)

and an example dialogue is shown in Listing 6.39.

```
Listing 6.39: An example dialogue of running Listing 6.38. What the user typed has been framed in red boxes.

1  $ fsharpc --nologo userDialoguePrintf.fsx && mono userDialoguePrintf.exe
2  To perform the multiplication of a and b
3  Enter a: 3.5
4  Enter b: 7.4
5  a * b = 25.9
```

Note that the string is immediately cast to floats such that we can multiply the input using the float multiplication operator. This also implies that if the user inputs a non-number, then mono will halt with an error message.

### 6.7. Variables

Identifiers may be mutable, which means that the it may be rebound to a new value. Mutable identifiers are specified using the *mutable* keyword with the following syntax:

·mutable

```
Listing 6.40: Syntax for defining mutable values with an initial value.

1 let mutable <ident> = <expr> [in <expr>]
```

Changing the value of an identifier is called *assignment* and is done using the "<-" lexeme.  $\cdot$  assignment Assignments have the following syntax:<sup>4</sup>

```
Listing 6.41: Value reassignment for mutable variables.

1 <ident> <- <ident>
```

Mutable data is synonymous with the term variable. A variable is an area in the computer's · mutable data working memory associated with an identifier and a type, and this area may be read from · variable and written to during program execution, see Listing 6.42 for an example.

<sup>&</sup>lt;sup>4</sup>Jon: Discussion on heap and stack should be added here.

### Listing 6.42 mutableAssignReassingShort.fsx: A variable is defined and later reassigned a new value. 1 let mutable x = 5 2 printfn "%d" x 3 x <- -3 4 printfn "%d" x 1 \$ fsharpc --nologo mutableAssignReassingShort.fsx 2 \$ mono mutableAssignReassingShort.exe 3 5 4 -3

Here, an area in memory was denoted x, initially assigned the integer value 5, hence the type was inferred to be int. Later, this value of x was replaced with another integer using the "<-" lexeme. The "<-" lexeme is used to distinguish the assignment from the comparison operator. For example, the statement a = 3 in Listing 6.43 is not an assignment but a comparison which is evaluated to be false.

```
Listing 6.43: It is a common error to mistake "=" and "<-" lexemes for mutable variables.

1 > let mutable a = 0
2 - a = 3;;
3 val mutable a : int = 0
4 val it : bool = false
```

However, it is important to note that when the variable is initially defined, then the "=" operator must be used, while later reassignments must use the "<-" expression.

Assignment type mismatches will result in an error, as demonstrated in Listing 6.44.

```
Listing 6.44 mutableAssignReassingTypeError.fsx:
Assignment type mismatching causes a compile-time error.

1 let mutable x = 5
2 printfn "%d" x
3 x <- -3.0
4 printfn "%d" x

1 $ fsharpc --nologo mutableAssignReassingTypeError.fsx

2 mutableAssignReassingTypeError.fsx(3,6): error FS0001: This expression was expected to have type
4     'int'
5 but here has type
6     'float'
7 $ mono mutableAssignReassingTypeError.exe
8 Cannot open assembly 'mutableAssignReassingTypeError.exe': No such file or directory.
```

I.e., once the type of an identifier has been declared or inferred, it cannot be changed.

A typical variable is a counter of type integer, and a typical use of counters is to increment them, see Listing 6.45 for an example.

## Listing 6.45 mutableAssignIncrement.fsx: Variable increment is a common use of variables. 1 let mutable x = 5 // Declare a variable x and assign the value 5 to it 2 printfn "%d" x 3 x <- x + 1 // Increment the value of x 4 printfn "%d" x 1 \$ fsharpc --nologo mutableAssignIncrement.fsx 2 \$ mono mutableAssignIncrement.exe 3 5 4 6

Using variables in expressions, as opposed to the left-hand-side of an assignment operation, reads the value of the variable. Thus, when using a variable as the return value of a function, then the value is copied from the local scope of the function to the scope from which it is called. This is demonstrated in Listing 6.46.

```
Listing 6.46: Returning a mutable variable returns its value.

1 > let g () =
2 - let mutable y = 0
3 - y
4 - printfn "%d" (g ());;
5 0
6 val g : unit -> int
7 val it : unit = ()
```

In the example we see that the type is a value, and not mutable.

Variables implement dynamic scope, that is, the value of an identifier depends on *when* it is used. This is in contrast to lexical scope, where the value of an identifier depends on *where* it is defined. As an example, consider the script in Listing 6.24 which defines a function using lexical scope and returns the number 6.0, however, if a is made mutable, then the behavior is different, as shown in Listing 6.47.

### Listing 6.47 dynamicScopeNFunction.fsx: Mutual variables implement dynamic scope rules. Compare with Listing 6.24. let testScope x = let mutable a = 3.0 let f z = a \* za < -4.0f x printfn "%A" (testScope 2.0) \$ fsharpc --nologo dynamicScopeNFunction.fsx mono dynamicScopeNFunction.exe 8.0

Here, the response is 8.0, since the value of a changed before the function f was called.

### 6.8. Reference Cells

F# has a variation of mutable variables called reference cells. Reference cells have the built-  $\cdot$  reference cells in function ref and the operators "!" and ":=", where ref creates a reference variable,  $\cdot$  ref and the "!" and the ":=" operators respectively reads and writes its value. An example := of using reference cells is given in Listing 6.48.

```
Listing 6.48 refCell.fsx:
Reference cells are variants of mutable variables.
let x = ref 0
printfn "%d" !x
x := !x + 1
printfn "%d" !x
  fsharpc --nologo refCell.fsx && mono refCell.exe
0
 1
```

Reference cells are different from mutable variables, since their content is allocated on *The* Heap. The Heap is a global data storage that is not destroyed when a function returns, The Heap which is in contrast to the call stack, also known as The Stack. The Stack maintains all . call stack the local data for a specific instance of a function call, see Section 13.2 for more details. As a consequence, when a reference cell is returned from a function, then it is the reference to the location on The Heap, which is returned as a value. Since this points outside the local data area of the function, this location is still valid after the function returns, and the variable stored there is accessible to the caller. This is illustrated in Figure 6.1

· The Stack

Reference cells may cause *side-effects*, where variable changes are performed across independent scopes. Some side-effects are useful, e.g., the printf family changes the content of the screen, and the screen is outside the scope of the caller. Another example of a useful side-effect is a counter shown in Listing 6.49.

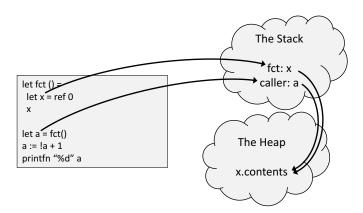


Figure 6.1.: A reference cell is a pointer to The Heap, and the content is not destroyed when its reference falls out of scope.

```
Listing 6.49 refEncapsulation.fsx:

An increment function with a local state using a reference cell.

let incr =
let counter = ref 0
fun () ->
counter := !counter + 1
!counter
printfn "%d" (incr ())
printfn "%d" (incr ())
printfn "%d" (incr ())

f fsharpc --nologo refEncapsulation.fsx && mono
refEncapsulation.exe

1
2
3
3
```

Here incr is an anonymous function with an internal state counter. At first glance, it may be surprising that incr () does not return the value 1 at every call. The reason is that the value of the incr is the closure of the anonymous function fun () -> counter := ..., which is

```
\texttt{incr}: (\texttt{args}, \texttt{exp}, \texttt{env}) = \big((), \big( \underbrace{\texttt{counter}}_{!} : \texttt{= !counter + 1} \big), (\texttt{counter} \rightarrow \texttt{ref 0}) \big). \quad (6.5)
```

Thus, counter is only initiated once at the initial binding, while every call of incr () updates its value on The Heap. Such a programming structure is called *encapsulation*, · encapsulation since the counter state has been encapsulated in the anonymous function, and the only way to access it is by calling the same anonymous function. In general, it is advisable to use encapsulation to hide implementation details irrelevant to the user of the Advice code.

The incr example in Listing 6.49 is an example of a useful side-effect. An example to be avoided is shown in Listing 6.50.

# Listing 6.50 refSideEffect.fsx: Intertwining independent scopes is typically a bad idea. 1 let updateFactor factor = 2 factor := 2 3 let multiplyWithFactor x = 1 let a = ref 1 2 updateFactor a 3 !a \* x 9 printfn "%d" (multiplyWithFactor 3) 1 \$ fsharpc --nologo refSideEffect.fsx && mono refSideEffect.exe 2 6

In the example, the function updateFactor changes a variable in the scope of the function multiplyWithFactor. The code style is prone to errors, since the computations are not local at the place of writing, i.e., in multiplyWithFactor, and if updateFactor were defined in a library, then the source code may not be available. Better style of programming is shown in Listing 6.51.

```
Listing 6.51 refWithoutSideEffect.fsx:
A solution similar to Listing 6.50 without side-effects.

1 let updateFactor () = 2
3 let multiplyWithFactor x = let a = ref 1 a := updateFactor () !a * x

9 printfn "%d" (multiplyWithFactor 3)

1 $ fsharpc --nologo refWithoutSideEffect.fsx $ mono refWithoutSideEffect.exe 6
```

Here, there can be no doubt in multiplyWithFactor that the value of a is changing. Side-effects do have their use, but should, in general, be avoided at almost all costs, and it is advised to minimize the use of side effects.

Advice

Reference cells give rise to an effect called *aliasing*, where two or more identifiers refer to · aliasing the same data, as illustrated in Listing 6.52.

## Listing 6.52 refCellAliasing.fsx: Aliasing can cause surprising results and should be avoided. 1 let a = ref 1 2 let b = a 3 printfn "%d, %d" !a !b 4 b := 2 5 printfn "%d, %d" !a !b 1 \$ fsharpc --nologo refCellAliasing.fsx && mono refCellAliasing.exe 2 1, 1 3 2, 2

Here, a is defined as a reference cell, and by defining b to be equal to a, we have created an alias. This can be very confusing since as the example shows, changing the value of b causes a to change as well. Aliasing is a variant of side-effects, and aliasing should be Advice avoided at all costs.

Since F# version 4.0, the compiler has automatically converted mutable variables to reference cells, where needed. E.g., Listing 6.49 can be rewritten using a mutable variable, as shown in Listing 6.53.

```
Listing 6.53 mutableEncapsulation.fsx:
Local mutable content can be indirectly accessed outside its scope.

1 let incr =
2 let mutable counter = 0
3 fun () ->
4 counter <- counter + 1
5 counter
6 printfn "%d" (incr ())
7 printfn "%d" (incr ())
8 printfn "%d" (incr ())
1 $ fsharpc --nologo mutableEncapsulation.fsx
2 $ mono mutableEncapsulation.exe
3 1
4 2
5 3
```

Reference cells are preferred over mutable variables for encapsulation, in order to avoid confusion.

### 6.9. Tuples

Tuples are a direct extension of constants. They are immutable and have neither concatenations nor indexing operations. Tuples are unions of immutable types and have the following syntax:

```
Listing 6.54: Tuples are list of expressions separated by commas.

1 <expr>{, <expr>}
```

Tuples are identified by the "," lexeme and often enclosed in parentheses, but that is not required. An example is a triple, also known as a 3-tuple, (2,true,"hello"). In interactive mode, the type of tuples is demonstrated in Listing 6.55.

```
Listing 6.55: Tuple types are products of sets.

1 > let tp = (2, true, "hello")
2 - printfn "%A" tp;;
3 (2, true, "hello")
4 val tp : int * bool * string = (2, true, "hello")
5 val it : unit = ()
```

The values 2, true, and "hello" are members, and the number of elements of a tuple is · member its length. From the response of F#, we see that the tuple is inferred to have the type · length int \* bool \* string. The "\*" denotes the Cartesian product between sets. Tuples can be products of any types and follow the lexical scope rules like value and function bindings. Notice also that a tuple may be printed as a single entity by the %A placeholder. In the example we bound tp to the tuple. The opposite is also possible, as demonstrated in Listing 6.56.

```
Listing 6.56: Definition of a tuple.

1 > let deconstructNPrint tp =
2 - let (a, b, c) = tp
3 - printfn "tp = (%A, %A, %A)" a b c
4 -
5 - deconstructNPrint (2, true, "hello")
6 - deconstructNPrint (3.14, "Pi", 'p');;
7 tp = (2, true, "hello")
8 tp = (3.14, "Pi", 'p')
9 val deconstructNPrint : 'a * 'b * 'c -> unit
10 val it : unit = ()
```

In this example, a function is defined that takes 1 argument, a 3-tuple. If we wanted a function with 3 arguments, then the function binding should have been let deconstructNPrint a b c = .... The value binding let (a, b, c) = tp, binds a tuple with 3 named members to a value, thus deconstructing it in terms of its members. This is called pattern matching and will be discussed in further details in Chapter 15. Since we used the \%A placeholder in the printfn function, the function can be called with 3-tuples of different types. F# informs us that the tuple type is variable by writing 'a \* 'b \* 'c. The "'" notation means that the type can be decided at run-time, see Section 14.6 for more on variable types.

Pairs or 2-tuples are so common that F# includes two built-in functions, fst and snd, to  $\cdot fst$  extract the first and second element of a pair. This is demonstrated in Listing 6.57.

### Listing 6.57 pair.fsx: Deconstruction of pairs with the built-in functions fst and snd. 1 let pair = ("first", "second") 2 printfn "fst(pair) = %s, snd(pair) = %s" (fst pair) (snd pair) 1 \$ fsharpc --nologo pair.fsx && mono pair.exe 2 fst(pair) = first, snd(pair) = second

Tuples of equal lengths can be compared, and the comparison is defined similarly to string comparison. Tuples of equal length are compared element by element. E.g., (1,2) = (1,3) is false, while (1,2) = (1,2) is true. The "<>" operator is the boolean negation of the "=" operator. For the "<", "<=", ">", and ">=" operators, the strings are ordered lexicographically, such that ('a', 'b', 'c') < ('a', 'b', 's') && ('a', 'b', 's') < ('c', 'o', 's') is true, that is, the "<" operator on two tuples is true if and only if the left operand should come before the right when sorting alphabetically. See Listing 6.58 for an example.

```
Listing 6.58 tupleCompare.fsx:
Tuples comparison is similar to string comparison.
let lessThan (a, b, c) (d, e, f) =
   if a <> d then a < d
   elif b <> e then b < d
   elif c <> f then c < f
   else false
let printTest x y =
  printfn "%A < %A is %b" x y (lessThan x y)</pre>
let a = ('a', 'b', 'c');
let b = ('d', 'e',
                    'f');
let c = ('a', 'b', 'b');
let d = ('a', 'b', 'd');
printTest a b
printTest a c
printTest a d
$ fsharpc --nologo tupleCompare.fsx && mono tupleCompare.exe
('a', 'b', 'c') < ('d', 'e', 'f') is true
('a', 'b', 'c') < ('a', 'b', 'b') is false
 ('a', 'b', 'c') < ('a', 'b', 'd') is true
```

The algorithm for deciding the boolean value of (a1, a2) < (b1, b2) is as follows: we start by examining the first elements, and if a1 and b1 are different, then the result of (a1, a2) < (b1, b2) is equal to the result of a1 < b1. If a1 and b1 are equal, then we move on to the next letter and repeat the investigation. The "<=", ">", and ">=" operators are defined similarly."

Binding tuples to mutables does not make the tuple mutable. This is demonstrated in Listing 6.59.

### Listing 6.59 tupleOfMutables.fsx: A mutable changes value, but the tuple defined by it does not refer to the new value. let mutable a = 1 let mutable b = 2 let c = (a, b)printfn "%A, %A, %A" a b c a < -3printfn "%A, %A, %A" a b c \$ fsharpc --nologo tupleOfMutables.fsx && mono tupleOfMutables.exe 1, 2, (1, 2) 3, 2, (1, 2)

However, it is possible to define a mutable variable of type tuple such that new tuple values can be assigned to it, as shown in Listing 6.60.

```
Listing 6.60 mutable Tuple.fsx:
A mutable tuple can be assigned a new value.
let mutable pair = 1,2
printfn "%A" pair
pair <- (3,4)
printfn "%A" pair
$ fsharpc --nologo mutableTuple.fsx && mono mutableTuple.exe
 (1, 2)
 (3, 4)
```

Mutable tuples are value types, meaning that binding to new names makes copies, not aliases, as demonstrated in Listing 6.61.

```
Listing 6.61 mutable Tuple Value.fsx:
A mutable tuple is a value type.
let mutable pair = 1,2
let mutable aCopy = pair
pair <- (3,4)
printfn "%A %A" pair aCopy
 $ fsharpc --nologo mutableTupleValue.fsx && mono
   mutableTupleValue.exe
 (3, 4) (1, 2)
```

The use of tuples shortens code and highlights semantic content at a higher level, e.g., instead of focusing on the elements, tuples focus on their union. While this may look elegant and short there is the risk of obfuscation, i.e., writing compact code that is difficult  $\cdot$  obfuscation to read, where an unprepared reader of the code may not easily understand the computation

nor appreciate its elegance without an accompanying explanation. Hence, always keep an Advice eye out for compact and concise ways to write code, but never at the expense of readability.

### In-code Documentation 7

Documentation is a very important part of writing programs, since it is most unlikely that you will be writing really obvious code. Moreover, what seems obvious at the point of writing may be mystifying months later to the author and to others. Documentation serves several purposes:

- 1. Communicate what the code should be doing.
- 2. Highlight big insights essential for the code.
- 3. Highlight possible conflicts and/or areas where the code could be changed later.

The essential point is that coding is a journey in problem-solving, and proper documentation is an aid in understanding the solution and the journey that lead to it. Documentation is most often a mixture of in-code documentation and accompanying documents. Here, we will focus on in-code documentation which arguably causes problems in multi-language environments and run the risk of bloating code.

F# has two different syntaxes for comments. Comments can be block comments: 1

```
Listing 7.1: Block comments.
(*<any text>*)
```

The comment text ( $\langle$ any text $\rangle$ ) can be any text and is stilled parsed by F# as keywords and basic types, implying that (\* a comment (\* in a comment \*) \*) and (\* "\*)" \*) are valid comments, while (\* " \*) is invalid.

Alternatively, comments may also be line comments,

```
Listing 7.2: Line comments.
 //<any text>
```

where the comment text ends after the first newline.

The F# compiler has an option for generating Extensible Markup Language (XML) files · Extensible Markup from scripts using the C# documentation comments tags<sup>2</sup>. The XML documentation starts

Language

 $\cdot XML$ 

<sup>&</sup>lt;sup>1</sup>Jon: color of '\*' is wrong.

 $<sup>^2</sup>$ For specification of C# documentations comments see ECMA-334 3rd Edition, Annex E, Section 2: http://www.ecma-international.org/publications/files/ECMA-ST/Ecma-334.pdf

### 7. In-code Documentation

Tag	Description
<c></c>	Set text in a code-font.
<code></code>	Set one or more lines in code-font.
<example></example>	Set as an example.
<exception></exception>	Describe the exceptions a function can throw.
<li><li>t&gt;</li></li>	Create a list or table.
<para></para>	Set text as a paragraph.
<pre><param/></pre>	Describe a parameter for a function or constructor.
<pre><paramref></paramref></pre>	Identify that a word is a parameter name.
<pre><permission></permission></pre>	Document the accessibility of a member.
<remarks></remarks>	Further describe a function.
<returns></returns>	Describe the return value of a function.
<see></see>	Set as link to other functions.
<seealso></seealso>	Generate a See Also entry.
<summary></summary>	Main description of a function or value.
<typeparam></typeparam>	Describe a type parameter for a generic type or method.
<typeparamref></typeparamref>	Identify that a word is a type parameter name.
<value></value>	Describe a value.

Table 7.1.: Recommended XML tags for documentation comments, from ECMA-334 3rd Edition, Annex E, Section 2.

with a triple-slash ///, i.e., a lineComment and a slash, which serve as comments for the code construct that follows immediately after. XML consists of tags which always appear in pairs, e.g., the tag "tag" would look like <tag> ... </tag>. F# accept any tags, but recommends those listed in Table 7.1. If no tags are used, then it is automatically assumed to be a <summary>. An example of a documented script is shown in Listing 7.3. is:

#### Listing 7.3 commentExample.fsx: Code with XML comments. /// The discriminant of a quadratic equation with parameters a, b, and c let discriminant a b c = b \*\* 2.0 - 4.0 \* a \* c /// <summary>Find x when 0 = ax^2+bx+c.</summary> /// <remarks > Negative discriminants are not checked. </remarks > /// <example> The following code: /// <code> /// let a = 1.0/// let b = 0.0/// let c = -1.0/// let xp = (solution a b c +1.0)/// printfn "0 = $\%.1fx^2 + \%.1fx + \%.1f => x_+ = \%.1f$ " a b с хр /// </code> prints $\langle c \rangle 0 = 1.0 x^2 + 0.0 x + -1.0 = x_+ = 0.7 \langle /c \rangle$ to /// the console. /// </example> /// <param name="a">Quadratic coefficient.</param> /// <param name="b">Linear coefficient.</param> /// <param name="c">Constant coefficient.</param> /// <param name="sgn">+1 or -1 determines the solution.</param> /// <returns>The solution to x.</returns> let solution a b c sgn = let d = discriminant a b c (-b + sgn \* sqrt d) / (2.0 \* a)let a = 1.0let b = 0.0let c = -1.0let xp = (solution a b c +1.0)printfn "0 = $%.1fx^2 + %.1fx + %.1f => x_+ = %.1f$ " a b c xp

Mono's fsharpc command may be used to extract the comments into an XML file, as demonstrated in Listing 7.4.

```
Listing 7.4, Converting in-code comments to XML.

1  $ fsharpc --doc:commentExample.xml commentExample.fsx
2  F# Compiler for F# 4.0 (Open Source Edition)
3  Freely distributed under the Apache 2.0 Open Source License
```

This results in an XML file with the content shown in Listing 7.5.

\$ fsharpc --nologo commentExample.fsx && mono

 $0 = 1.0x^2 + 0.0x + -1.0 \Rightarrow x_+ = 1.0$ 

commentExample.exe

Listing 7.5, An XML file generated by fsharpc. <?xml version="1.0" encoding="utf-8"?> <doc> <assembly><name>commentExample</name></assembly> <members> <member name="M:CommentExample.solution(System.Double,System.</pre> Double,System.Double,System.Double)"> <summary>Find x when 0 = ax^2+bx+c.</summary> <remarks>Negative discriminants are not checked. <example> The following code: <code> let a = 1.0let b = 0.0let c = -1.0let xp = (solution a b c +1.0)printfn "0 =  $\%.1fx^2 + \%.1fx + \%.1f => x_+ = \%.1f$ " a b c хp </code> prints  $\langle c \rangle 0 = 1.0x^2 + 0.0x + -1.0 \Rightarrow x_+ = 0.7 \langle c \rangle$  to the console. </example> <param name="a">Quadratic coefficient.</param> <param name="b">Linear coefficient.</param> <param name="c">Constant coefficient.</param> <param name="sgn">+1 or -1 determines the solution. <returns>The solution to x.</returns> </member> <member name="M:CommentExample.discriminant(System.Double,</pre> System.Double,System.Double)"> <summary> The discriminant of a quadratic equation with parameters a, b, and c </summary> </member> </members> </doc>

The extracted XML is written in C# type by convention, since F# is part of the Mono and .Net framework that may be used by any of the languages using Assemblies. Besides the XML inserted in the script, the XML has added the <?xml ...> header, <doc>, <assembly>, <members>, and <member> tags. The header and the <doc> tag are standards for XML. The extracted XML is geared towards documenting big libraries of codes and thus highlights the structured programming organisation, see Chapters 9 and 20, and <assembly>, <members>, and <member> are indications for where the functions belong in the hierarchy. As an example, the prefix M:CommentExample. indicates that the method is in the namespace commentExample, which in this case is the name of the file. Furthermore, the function type val solution: a:float -> b:float -> c:float -> sgn:float -> float is in the XML documentation

M: Comment Example. solution (System. Double, System. Double, System. Double, System. Double),

which is the C# equivalent.

An accompanying program in the Mono suite is mdoc, whose primary use is to perform a

#### 7. In-code Documentation

syntax analysis of an assembly and generate a scaffold XML structure for an accompanying document. With the -i flag, it is further possible to include the in-code comments as initial descriptions in the XML. The XML may be updated gracefully by mdoc as the code develops, without destroying manually entered documentation in the accompanying documentation. Finally, the XML may be exported to HTML.

The primary use of the mdoc command is to analyze compiled code and generate an empty XML structure with placeholders to describe functions, values, and variables. This structure can be updated and edited as the program develops, and the edited XML files can be exported to *Hyper Text Markup Language* (*HTML*) files and viewed in any browser. Using the console, all of this is accomplished by the procedure shown in Listing 7.6, and the result is shown in Figure 7.1.

· Hyper Text Markup Language

 $\cdot$  HTML

```
Listing 7.6, Converting an XML file to HTML.
$ mdoc update -o commentExample -i commentExample.xml
   commentExample.exe
New Type: CommentExample
Member Added: public static double determinant (double a,
   double b, double c);
Member Added: public static double solution (double a, double
   b, double c, double sgn);
Member Added: public static double a { get; }
Member Added: public static double b { get; }
Member Added: public static double c { get; }
Member Added: public static double xp { get; }
Namespace Directory Created:
New Namespace File:
Members Added: 6, Members Deleted: 0
$ mdoc export-html -out commentExampleHTML commentExample
.CommentExample
```

A full description of how to use mdoc is found here<sup>3</sup>.

 $<sup>^3</sup>$ http://www.mono-project.com/docs/tools+libraries/tools/monodoc/generating-documentation/

#### solution Method

Find x when  $0 = ax^2+bx+c$ .

#### **Syntax**

[Microsoft.FSharp.Core.CompilationArgumentCounts(Mono.Cecil.CustomAttributeArgument[])] public static double solution (double a, double b, double c, double sgn)

#### **Parameters**

```
a Quadratic coefficient.
```

Linear coefficient.

c Constant coefficient. sgn

+1 or -1 determines the solution.

#### Returns

The solution to x.

#### Remarks

Negative discriminants are not checked.

#### Example

The following code:

```
Example

let a = 1.0
let b = 0.0
let c = -1.0
let xp = (solution a b c +1.0)
printfn "0 = %.lfx^2 + %.lfx + %.lf => x_+ = %.lf" a b c xp

prints 0 = 1.0x^2 + 0.0x + -1.0 => x_+ = 0.7 to the console.
```

#### Requirements

Namespace:

Assembly: commentExample (in commentExample.dll)
Assembly Versions: 0.0.0.0

Figure 7.1.: Part of the HTML documentation as produced by mdoc and viewed in a browser.

# 8 | Controlling Program Flow

Non-recursive functions encapsulate code and allow for control of execution flow. That is, if a piece of code needs to be executed many times, then we can encapsulate it in the body of a function and call this function several times. In this chapter, we will look at more general control of flow via loops and conditional execution. Recursion is another mechanism for controlling flow, but this is deferred to Chapter 13.

#### 8.1. While and For Loops

Many programming constructs need to be repeated, and F# contains many structures for repetition. A while-loop has the following syntax:

 $\cdot$  while

```
Listing 8.1: While loop.

while <condition> do <expr> [done]
```

The  $condition < condition > is an expression that evaluates to true or false. A while-loop <math>\cdot$  condition repeats the < expr > expression as long as the condition is true. Using lightweight syntax, the block following the do keyword up to and including the do keyword may be replaced  $\cdot$  do by a newline and indentation.

The program in Listing 8.5 is an example of a while-loop which counts from 1 to 10.

```
Listing 8.2 countWhile.fsx:
Count to 10 with a counter variable.

1 let mutable i = 1 in while i <= 10 do printf "%d " i; i <- i +
    1 done;
printf "\n"

1 $ fsharpc --nologo countWhile.fsx && mono countWhile.exe
2 1 2 3 4 5 6 7 8 9 10
```

The variable i is customarily called the counter variable. The counting is done by performing the following computation: In line 1, the counter variable is first given an initial value of 1. Then execution enters the while-loop and examines the condition. Since  $1 \le 10$ , the condition is true, and execution enters the body of the loop. The body prints the value of the counter to the screen and increases the counter by 1. Then execution returns to the

top of the while-loop. Now the condition is  $2 \le 10$ , which is also true, and so execution enters the body and so on until the counter has reached the value 11, in which case the condition  $11 \le 10$  is false, and execution continues in line 2.

In lightweight syntax, this would be as shown in Listing 8.3.

```
Listing 8.3 countWhileLightweight.fsx:
Count to 10 with a counter variable using lightweight syntax.
let mutable i = 1
while i <= 10 do
   printf "%d " i
   i <- i + 1
printf "\n"
 $ fsharpc --nologo countWhileLightweight.fsx
 $ mono countWhileLightweight.exe
 1 2 3 4 5 6 7 8 9 10
```

Notice that although the expression following the condition is preceded with a do keyword, and do <expr> is a do binding, the keyword do is mandatory.

Counters are so common that a special syntax has been reserved for loops using counters. These are called *for*-loops. For-loops come in several variants, and here we will focus on • for the one using an explicit counter. Its syntax is:

```
Listing 8.4: For loop.
for <ident> = <firstExpr> to <lastExpr> do <bodyExpr> [done]
```

A for-loop initially binds the counter identifier <ident> to be the value <firstExpr>. Then execution enters the body, and <bodyExpr> is evaluated. Once done, the counter is increased, and execution evaluates <bodyExpr> once again. This is repeated as long as the counter is not greater than <lastExpr>. As for while-loops, when using lightweight syntax the block following the do keyword up to and including the done keyword may be replaced  $\cdot do$ by a newline and indentation.

· done

The counting example from Listing 8.2 using a for-loop is shown in Listing 8.5

```
Listing 8.5 count.fsx:
Counting from 1 to 10 using a -loop.
for i = 1 to 10 do printf "%d " i done
printfn ""
 $ fsharpc --nologo count.fsx && mono count.exe
 1 2 3 4 5 6 7 8 9 10
```

As this interactive script demonstrates, the identifier i takes all the values between 1 and 10, but in spite of its changing state, it is not mutable. Note also that the return value of

#### 8. Controlling Program Flow

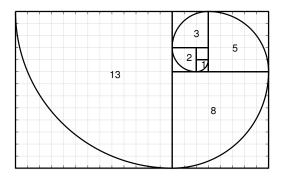


Figure 8.1.: The Fibonacci spiral is an approximation of the golden spiral. Each square has side lengths of successive Fibonacci numbers, and the curve in each square is the circular arc with a radius of the square it is drawn in.

the for expression is "()", like the printf functions. The lightweight equivalent is shown in Listing 8.6.

```
Listing 8.6 countLightweight.fsx:

Counting from 1 to 10 using a -loop using the lightweight syntax.

1 for i = 1 to 10 do
2 printf "%d " i
3 printfn ""

1 $ fsharpc --nologo countLightweight.fsx && mono countLightweight.exe
2 1 2 3 4 5 6 7 8 9 10
```

To further compare for- and while-loops, consider the following problem.

#### Problem 8.1

Write a program that calculates the n'th Fibonacci number.

Fibonacci numbers is a sequence of numbers starting with 1, 1, and where the next number is calculated as the sum of the previous two. Hence the first ten numbers are: 1, 1, 2, 3, 5, 8, 13, 21, 34, 55. Fibonacci numbers are related to Golden spirals shown in Figure 8.1. Often the sequence is extended with a preceding number 0, to be  $0, 1, 1, 2, 3, \ldots$ , which we will do here as well.

We could solve this problem with a for-loop, as shown in Listing 8.7.

#### Listing 8.7 fibFor.fsx: The *n*'th Fibonacci number calculated using a for-loop. let fib n = let mutable pair = (0, 1) for i = 2 to n do pair <- (snd pair, (fst pair) + (snd pair))</pre> snd pair printfn "fib(1) = %d" (fib 1) printfn "fib(2) = %d" (fib 2) printfn "fib(3) = %d" (fib 3) printfn "fib(10) = %d" (fib 10) \$ fsharpc --nologo fibFor.fsx && mono fibFor.exe fib(1) = 1fib(2) = 1fib(3) = 2fib(10) = 55

The basic idea of the solution is that if we are given the (n-1)'th and (n-2)'th numbers, the n'th number is trivial to compute. And assuming that fib(1) and fib(2) are given, then it is trivial to calculate fib(3). For fib(4), we only need fib(3) and fib(2), hence we may disregard fib(1). Thus, we realize that we can cyclicly update the previous, current, and next values by shifting values until we have reached the desired fib(n). This is implement in Listing 8.7 as the function fib, which takes an integer n as argument and returns the n'th Fibonacci number. The function does this iteratively using a for-loop, where i is the counter value, and pair is the pair of the i-1'th and i'th Fibonacci numbers. In the body of the loop, the i'th and i+1'th numbers are assigned to pair. The for-loop automatically updates i for next iteration. When n < 2 the body of the for-loop is not evaluated, and 1 is returned. This is of course wrong for n < 1, but we will ignore this for now.

Listing 8.8 shows a program similar to Listing 8.7 using a while-loop instead of for-loop.

#### Listing 8.8 fibWhile.fsx: The *n*'th Fibonacci number calculated using a while-loop. let fib (n : int) : int = let mutable pair = (0, 1) let mutable i = 1while i < n do pair <- (snd pair, fst pair + snd pair) i <- i + 1 snd pair printfn "fib(1) = %d" (fib 1) printfn "fib(2) = %d" (fib 2) printfn "fib(3) = %d" (fib 3) printfn "fib(10) = %d" (fib 10) \$ fsharpc --nologo fibWhile.fsx && mono fibWhile.exe fib(1) = 1fib(2) = 1fib(3) = 2fib(10) = 55

The programs are almost identical. In this case, the for-loop is to be preferred, since more lines of code typically mean more chances of making a mistake. However, while-loops are somewhat easier to argue correctness about.

The correctness of fib in Listing 8.8 can be proven using a loop invariant. An invariant · loop invariant is a statement that is always true at a particular point in a program, and a loop invariant . invariant is a statement which is true at the beginning and end of a loop. In line 4 in Listing 8.8, we may state the invariant: The variable pair is the pair of the i-1'th and i'th Fibonacci numbers. This is provable by induction:

Base case: Before entering the while loop, i is 1, pair is (0, 1). Thus, the invariant is true.

**Induction step:** Assuming that pair is the i-1'th and i'th Fibonacci numbers, the body first assigns a new value to pair as the i'th and i + 1'th Fibonacci numbers, then increases i by one such that at the end of the loop the pair again contains the the i-1'th and i'th Fibonacci numbers.

Thus, since our invariant is true for the first case, and any iteration following an iteration where the invariant is true, is also true, then it is true for all iterations.

Thus we know that the second value in pair holds the value of the i'th Fibonacci number, and since we further may prove that i = n when line 7 is reached, then it is proven that fib returns the n'th Fibonacci number.

While-loops also allow for logical structures other than for-loops, such as the case when the number of iteration cannot easily be decided when entering the loop. As an example, consider a slight variation of the above problem, where we wish to find the largest Fibonacci number less or equal some number. A solution to this problem is shown in Listing 8.9.

#### Listing 8.9 fibWhileLargest.fsx: Search for the largest Fibonacci number less than a specified number. let largestFibLeq n = let mutable pair = (0, 1) while snd pair <= n do pair <- (snd pair, fst pair + snd pair) fst pair for i = 1 to 10 do printfn "largestFibLeq(%d) = %d" i (largestFibLeq i) \$ fsharpc --nologo fibWhileLargest.fsx && mono fibWhileLargest.exe largestFibLeq(1) = 1largestFibLeq(2) = 2largestFibLeq(3) = 3largestFibLeq(4) = 3largestFibLeq(5) = 5largestFibLeq(6) largestFibLeq(7) = 5largestFibLeq(8) = 8largestFibLeq(9) = 8largestFibLeq(10) = 8

The strategy here is to iteratively calculate Fibonacci numbers until we've found one larger than the argument n, and then return the previous. This could not be calculated with a for-loop.

#### 8.2. Conditional Expressions

Programs often contain code which should only be executed under certain conditions. This can be expressed with **if**-expressions, whose syntax is as follows.

```
Listing 8.10: Conditional expressions.

if <cond> then <expr> {elif <cond> then <expr>} [else <expr>]
```

The condition <code><con></code> is an expression resulting in a Boolean value, and there can be zero or more <code>elif</code> conditions, as indicated by <code>{}</code>. Each expression <code><expr></code> is called a <code>branch</code>, and all branches must have the same type, such that regardless of which branch is chosen, the type of the result of the conditional expression is the same. Then the expression of the first if-branch, whose condition is true, is evaluate. If all conditions are false then the <code>else-branch</code> is evaluated. If no <code>else</code> expression is present, then "()" will be returned. See Listing 8.11 for a simple example.

·if

# Listing 8.11 condition.fsx: Conditions evaluate their branches depending on the value of the condition. if true then printfn "hi" else printfn "bye" if false then printfn "hi" else printfn "bye" fsharpc --nologo condition.fsx && mono condition.exe hi bye

The lightweight syntax allows for newlines entered everywhere, but indentation must be used to express scope.

To demonstrate conditional expressions, let us write a program which writes the sentence "I have n apple(s)", where the plural 's' is added appropriately for various n's. This is done in Listing 8.12, using the lightweight syntax.

```
Listing 8.12 conditionalLightweight.fsx:
Using conditional expression to generate different strings.
let applesIHave n =
   if n < -1 then
     "I owe " + (string -n) + " apples"
   elif n < 0 then
     "I owe " + (string -n) + " apple"
   elif n < 1 then
     "I have no apples"
   elif n < 2 then
     "I have 1 apple"
   else
     "I have " + (string n) + " apples"
printfn "%A" (applesIHave -3)
printfn "%A" (applesIHave -1)
printfn "%A" (applesIHave 0)
printfn "%A" (applesIHave 1)
printfn "%A" (applesIHave 2)
printfn "%A" (applesIHave 10)
$ fsharpc --nologo conditionalLightWeight.fsx
$ mono conditionalLightWeight.exe
"I owe 3 apples"
"I owe 1 apple"
"I have no apples"
 "I have 1 apple"
 "I have 2 apples"
 "I have 10 apples"
```

The sentence structure and its variants give rise to a more compact solution, since the language to be returned to the user is a variant of "I have/owe no/number apple(s)", i.e., certain conditions determine whether the sentence should use "have" and "owe" and so forth. So, we could instead make decisions on each of these sentence parts, and then built the final sentence from its parts. This is accomplished in the following example:

Listing 8.13 conditionalLightweightAlt.fsx: Using sentence parts to construct the final sentence. let applesIHave n = let haveOrOwe = if n < 0 then "owe" else "have"</pre> let pluralS = if (n = 0) || (abs n) > 1 then "s" else "" let number = if n = 0 then "no" else (string (abs n)) "I " + haveOrOwe + " " + number + " apple" + pluralS printfn "%A" (applesIHave -3) printfn "%A" (applesIHave -1) printfn "%A" (applesIHave 0) printfn "%A" (applesIHave 1) printfn "%A" (applesIHave 2) printfn "%A" (applesIHave 10) \$ fsharpc --nologo conditionalLightWeightAlt.fsx \$ mono conditionalLightWeightAlt.exe "I owe 3 apples" "I owe 1 apple" "I have no apples" "I have 1 apple" "I have 2 apples" "I have 10 apples"

While arguably shorter, this solution is also denser, and most likely more difficult to debug and maintain.

Note that both elif and else branches are optional, which may cause problems. For example, both let a = if true then 3 and let a = if true then 3 elif false then 4 will be invalid, since F# is not smart enough to realize that the type of the expression is uniquely determined. Instead, F# looks for the else to ensure all cases have been covered, and that a always will be given a unique value of the same type regardless of the branch taken in the conditional statement. Hence, let a = if true then 3 else 4 is the only valid expression of the 3. In practice, F# assumes that the omitted branch returns "()", and thus it is fine to say let a = if true then () and if true then printfn "hej". Nevertheless, it is good practice in F# to always include an else branch.

# 8.3. Programming Intermezzo: Automatic Conversion of Decimal to Binary Numbers

Using loops and conditional expressions, we are now able to solve the following problem:

#### Problem 8.2

Given an integer on decimal form, write its equivalent value on the binary form.

To solve this problem, consider odd numbers: They all have the property that the least significant bit is 1, e.g.,  $1_2 = 1,101_2 = 5$ , in contrast to even numbers such as  $110_2 = 6$ . Division by 2 is equal to right-shifting by 1, e.g.,  $1_2/2 = 0.1_2 = 0.5, 101_2/2 = 10.1_2 = 0.5$ 

 $2.5, 110_2/2 = 11_2 = 3$ . Thus, through dividing by 2 and checking the remainder, we may sequentially read off the least significant bit. This leads to the algorithm shown in Listing 8.14.

#### Listing 8.14 dec2bin.fsx: Using integer division and remainder to write any positive integer in binary form. let dec2bin n =if n < 0 then "Illegal value" elif n = 0 then"0b0" else let mutable v = nlet mutable str = "" while v > 0 do str <- (string (v % 2)) + str v <- v / 2 "0b" + str printfn "%4d -> %s" -1 (dec2bin -1) printfn "%4d -> %s" 0 (dec2bin 0) for i = 0 to 3 do printfn "%4d -> %s" (pown 10 i) (dec2bin (pown 10 i)) \$ fsharpc --nologo dec2bin.fsx && mono dec2bin.exe -1 -> Illegal value 0 -> 0b01 -> 0b1 10 -> 0b1010 100 -> 0b1100100 1000 -> 0b1111101000

In the code, the states v and str are iteratively updated until str finally contains the desired solution.

To prove that Listing 8.14 calculates the correct sequence, we use induction. First we realize that for v < 1, the while-loop is skipped, and the result is trivially true. We will concentrate on line 9 in Listing 8.14 and will prove the following loop invariant: The string str contains all the bits of n to the right of the bit pattern remaining in variable v.

Base case n = 000...000x: If n only uses the lowest bit, then n = 0 or n = 1. If n = 0, then it is trivially correct. Considering the case n = 1: Before entering into the loop,  $\mathbf{v}$  is 1, and  $\mathbf{str}$  is the empty string, so the invariant is true. The condition of the while-loop is 1 > 0, so execution enters the loop. Since integer division of 1 by 2 gives 0 with remainder 1,  $\mathbf{str}$  is set to "1" and  $\mathbf{v}$  to 0. Now we reexamine the while-loop's condition, 0 > 0, which is false, so we exit the loop. At this point,  $\mathbf{v}$  is 0 and  $\mathbf{str}$  is "1", so all bits have been shifted from  $\mathbf{n}$  to  $\mathbf{str}$ , and none are left in  $\mathbf{v}$ . Thus the invariant is true. Finally, the program returns "0b1".

**Induction step:** Consider the case of n > 1, and assume that the invariant is true when entering the loop, i.e., that m bits already have been shifted to str and that  $n > 2^m$ .

#### 8. Controlling Program Flow

In this case, v contains the remaining bits of n, which is the integer division v = n / 2\*\*m. Since  $n > 2^m$ , v is non-zero, and the loop conditions is true, so we enter the loop body. In the loop body we concatenate the rightmost bit of v to the left of str using v % 2, and right-shift v one bit to the right with v <- v / 2. Thus, when returning to the condition the invariant is true, since the right-most bit in v has been shifted to str. This continues until all bits have been shifted to str and v = 0, in which case the loop terminates, and "0b"+str is returned.

Thus we have proven that dec2bin correctly converts integers to strings representing binary numbers.

# 9 | Organising Code in Libraries and Application Programs

In this chapter, we will focus on a number of ways to make the code available as library · library functions in F#. A library is a collection of types, values, and functions that an application program can use. A library does not perform calculations on its own.

F# includes several programming structures to organize code in libraries: Modules, namespaces, and classes. In this chapter, we will describe modules and namespaces. Classes will be described in detail in Chapter 20.

#### 9.1. Modules

An F# module, not to be confused with a Common Language Infrastructure module (see  $\cdot$  module Appendix D), is a programming structure used to organize type declarations, values, functions, etc.

Every implementation and script file in F# implicitly defines a module, and the module name is given by the filename. Consider the script file Meta.fsx shown in Listing  $9.1.^1$ 

```
Listing 9.1 Meta.fsx:
A script file defining the apply function.

1 type floatFunction = float -> float -> float
2 let apply (f : floatFunction) (x : float) (y : float) : float
= f x y
```

Here, we have implicitly defined a module with the name Meta. Another script file may now use this function, which is accessed using the "." notation, i.e., Meta.apply will refer to this function in other programs. An application program could be as the one shown in Listing 9.3.

<sup>&</sup>lt;sup>1</sup>Jon: Type definitions have not been introduced at this point!

### Listing 9.2 MetaApp.fsx: Defining a script calling the module. let add : Meta.floatFunction = fun x y -> x + y let result = Meta.apply add 3.0 4.0 printfn "3.0 + 4.0 = %A" result

In the exmple above, we have explicitly used the module's type definition for illustration purposes. A shorter and possibly simpler program would have been to define add as let add x y = x + y, since F#'s type system will infer the implied type. However, explicit definitions of types is recommended for readability. Hence, an alternative to the above example's use of anonymous functions is: let add (x: float) (y: float): float = x + y. To compile the module and the application program, we write as demonstrated in Listing 9.3.

```
Listing 9.3: Compiling both the module and the application code. Note
that file order matters when compiling several files.
```

```
$ fsharpc --nologo Meta.fsx MetaApp.fsx && mono MetaApp.exe
3.0 + 4.0 = 7.0
```

Since the F# compiler reads through the files once, the order of the filenames in the compile command is very important. Hence, the script containing the module and function definitions must be to the left of the script containing their use. Notice also that if not otherwise specified, the F# compiler produces an .exe file derived from the last filename in the list of filenames.

We may also explicitly define the module name using the *module* with the following syntax, ·module

```
Listing 9.4: Outer module.
module <ident>
<script>
```

Here, the identifier <ident> is a name not necessarily related to the filename, and the script <script> is an expression. An example is given in Listing 9.20.

```
Listing 9.5 MetaExplicit.fsx:
Explicit definition of the outermost module.
module Meta
type floatFunction = float -> float -> float
let apply (f : floatFunction) (x : float) (y : float) : float
```

Since we have created a new file, where the module Meta is explicitly defined, we can use the same application program. This is demonstrated in Listing 9.6.

#### Listing 9.6: Changing the module definition to explicit naming has no effect on the application nor the compile command.

```
fsharpc --nologo MetaExplicit.fsx MetaApp.fsx && mono
  MetaApp.exe
3.0 + 4.0 = 7.0
```

Since MetaExplicit.fsx explicitly defines the module name, apply is not available to an application program as MetaExplicit.apply. It is recommended that module names Advice are defined explicitly, since filenames may change due to external conditions. In other words, filenames are typically set from the perspective of the filesystem. The user may choose to change names to suit a filesystem structure, or different platforms may impose different file naming conventions. Thus, direct linking of filenames with the internal workings of a program is a needless complication of structure.

The definitions inside a module may be accessed directly from an application program, omitting the "."-notation, by use of the open keyword,

·open

```
Listing 9.7: Open module.
open <ident>
```

We can modify MetaApp.fsx, as shown in Listing 9.9.

```
Listing 9.8 MetaAppWOpen.fsx:
Avoiding the "."-notation by the
                                  keyword.
open Meta
let add : floatFunction = fun x y -> x + y
let result = apply add 3.0 4.0
printfn "3.0 + 4.0 = %A" result
```

In this case, the namespace of our previously defined module is included into the scope of the application functions, and its types, values, functions, etc. can be used directly, as shown in Listing 9.9.

```
Listing 9.9: How the application program opens the module has no effect
on the module code nor compile command.
```

```
fsharpc --nologo MetaExplicit.fsx MetaAppWOpen.fsx && mono
  MetaAppWOpen.exe
3.0 + 4.0 = 7.0
```

The open-keyword should be used sparingly, since including a library's definitions into the application scope can cause surprising naming conflicts, because the user of a library typically has no knowledge of the inner workings of the library. E.g., the user may accidentally use code defined in the library, but with different type and functionality than intended, which the type system will use to deduce types in the application program, and therefore will either give syntax or runtime errors that are difficult to understand. This problem is · namespace pollution known as namespace pollution, and for clarity, it is recommended to use the open-

Advice

**keyword sparingly**. Note that for historical reasons, the phrase 'namespace pollution' is used to cover pollution both due to modules and namespaces.

Modules may also be nested, in which case the nested definitions must use the "="-sign and must be appropriately indented.

```
Listing 9.10: Nested modules.

1 module <ident> = <script>
```

In lightweight syntax, a newline may be entered before the script <script>, and the script must be indented. An example is shown in Listing 9.11.

```
Listing 9.11 nestedModules.fsx:
Modules may be nested.

1 module Utilities
2 let PI = 3.1415
3 module Meta =
4 type floatFunction = float -> float -> float
5 let apply (f : floatFunction) (x : float) (y : float) :
6 float = f x y
7 module MathFcts =
7 let add : Meta.floatFunction = fun x y -> x + y
```

In this case, Meta and MathFcts are defined at the same level and said to be siblings, while Utilities is defined at a higher level. In this relation, the former two are said to be the children of the latter. Note that the nesting respects the lexical scope rules, such that the constant PI is directly accessible in both modules Meta and MathFcts, as is the module Meta in MathFcts, but not MathFcts in Meta. The "."-notation is reused to index deeper into the module hierarchy, as the example in Listing 9.12 shows.

```
Listing 9.12 nestedModulesApp.fsx:
Applications using nested modules require additional usage of the "." notation to navigate the nesting tree.

let add: Utilities.Meta.floatFunction = fun x y -> x + y
let result = Utilities.Meta.apply Utilities.MathFcts.add 3.0
Utilities.PI
printfn "3.0 + 4.0 = %A" result
```

Modules can be recursive using the rec-keyword, meaning that in our example we can make the outer module recursive, as demonstrated in Listing  $9.13.^2$ 

<sup>&</sup>lt;sup>2</sup>Jon: Dependence on version 4.1 and higher.

#### Listing 9.13 nestedRecModules.fsx: Mutual dependence on nested modules requires the keyword in the module definition. module rec Utilities module Meta = type floatFunction = float -> float -> float let apply (f : floatFunction) (x : float) (y : float) : float = f x ymodule MathFcts = let add : Meta.floatFunction = fun x y -> x + y

The consequence is that the modules Meta and MathFcts are accessible in both modules, but compilation will now give a warning since soundness of the code will first be checked at runtime. In general, it is advised to avoid programming constructions whose Advice validity cannot be checked at compile-time.

#### 9.2. Namespaces

An alternative way to structure code in modules is to use a namespace, which can only · namespace hold modules and type declarations and only works in compiled mode. Namespaces are defined as explicitly defined outer modules, using the namespace keyword in accordance with the following syntax.

·namespace

```
Listing 9.14: Namespace.
namespace <ident>
<script>
```

An example is given in Listing 9.15.

```
Listing 9.15 namespace.fsx:
Defining a namespace is similar to explicitly named modules.
namespace Utilities
type floatFunction = float -> float -> float
module Meta =
   let apply (f : floatFunction) (x : float) (y : float) :
   float = f x y
```

Notice that when organizing code in a namespace, the first line of the file, other than comments and compiler directives, must be the one starting with namespace.

As for modules, the content of a namespace is accessed using the "." notation, as demonstrated in Listing 9.17.

#### Listing 9.16 namespaceApp.fsx:

The "."-notation lets the application program access functions and types in a namespace.

```
let add : Utilities.floatFunction = fun x y -> x + y
let result = Utilities.Meta.apply add 3.0 4.0
printfn "3.0 + 4.0 = %A" result
```

Likewise, the compilation is performed in the same way as for modules, see Listing 9.17.

Listing 9.17: Compilation of files including namespace definitions uses the same procedure as modules.

```
1  $ fsharpc --nologo namespace.fsx namespaceApp.fsx && mono
    namespaceApp.exe
2  3.0 + 4.0 = 7.0
```

Hence, from an application point of view, it is not immediately possible to see that Utilities is defined as a namespace and not a module. However, in contrast to modules, namespaces may span several files. E.g., we may add a third file extending the Utilities namespace with the MathFcts module, as demonstrated in Listing 9.18.

#### Listing 9.18 namespaceExtension.fsx:

Namespaces may span several files. Here is shown an extra file which extends the Utilities namespace.

```
namespace Utilities
module MathFcts =
let add : floatFunction = fun x y -> x + y
```

To compile, we now need to include all three files in the right order, see Listing 9.19.

Listing 9.19: Compilation of namespaces defined in several files requires careful consideration of order, since the compiler reads once and only once through the files in the order they are given.

```
$ fsharpc --nologo namespace.fsx namespaceExtension.fsx
    namespaceApp.fsx && mono namespaceApp.exe
2 3.0 + 4.0 = 7.0
```

The order matters, since namespaceExtension.fsx relies on the definition of floatFunction in the file namespace.fsx. You can use extensions to extend existing namespaces included with the F# compiler. $^{34}$ 

Namespaces may also be nested. In contrast to modules, nesting is defined using the "." notation. That is, to create a child namespace more of Utilities, we must use initially write namespace Utilities.more. Indentation is ignored in the namespace line, thus

<sup>&</sup>lt;sup>3</sup>Jon: Something about intrinsic and optional extension https://docs.microsoft.com/en-us/dotnet/fsharp/language-reference/type-extensions.

<sup>&</sup>lt;sup>4</sup>Jon: Perhaps something about the global namespace global.

left-most indentation is almost always used. Namespaces follow lexical scope rules, and identically to modules, namespaces containing mutually dependent children can be declared using the rec keyword, e.g., namespace rec Utilities.

#### 9.3. Compiled Libraries

Libraries may be distributed in compiled form as .dll files. This saves the user from having to recompile a possibly large library every time library functions needs to be compiled with an application program. In order to produce a library file from MetaExplicitModuleDefinition.fsx and then compile an application program, we first use the compiler's -a option to produce the .dll. A demonstration is given in Listing 9.20.

```
Listing 9.20: A stand-alone .dll file is created and used with special compile commands.

1 $ fsharpc --nologo -a MetaExplicit.fsx
```

This produces the file MetaExplicit.dll, which may be linked to an application by using the -r option during compilation, see Listing 9.21.<sup>5</sup>

```
Listing 9.21: The library is linked to an application during compilation to produce runnable code.

1  $ fsharpc --nologo -r MetaExplicit.dll MetaApp.fsx && mono MetaApp.exe
2  3.0 + 4.0 = 7.0
```

A library can be the result of compiling a number of files into a single .dll file. .dll-files may be loaded dynamically in script files (.fsx-files) by using the #r directive, as ·#r directive illustrated in Listing 9.23.

```
Listing 9.22 MetaHashApp.fsx:

The .dll file may be loaded dynamically in .fsx script files and in interactive mode. Nevertheless, this usage is not recommended.

### "MetaExplicit.dll"

let add : Meta.floatFunction = fun x y -> x + y

let result = Meta.apply add 3.0 4.0

printfn "3.0 + 4.0 = %A" result
```

We may now omit the explicit mentioning of the library when compiling, as shown in Listing 9.23.

<sup>&</sup>lt;sup>5</sup>Jon: This is the MacOS option standard, Windows is slightly different.

Listing 9.23: When using the #r directive, then the .dll file need not be explicitly included in the list of files to be compiled.

```
fsharpc --nologo MetaHashApp.fsx && mono MetaHashApp.exe
3.0 + 4.0 = 7.0
```

The #r directive is also used to include a library in interactive mode. However, for the code to be compiled, the use of the #r directive requires that the filesystem path to the library is coded inside the script. As for module names, direct linking of filenames with the internal workings of a program is a needless complication of structure, and it is recommended Advice not to rely on the use of the #r directive.

In the above listings we have compiled script files into libraries. However, F# has reserved  $\cdot$  script files the .fs filename suffix for library files, and such files are called implementation files. .implementation files In contrast to script files, implementation files do not support the #r directive. When compiling a list of implementation and script files, all but the last file must explicitly define a module or a namespace.

Both script and implementation files may be augmented with signature files. A signature signature files file contains no implementation, only type definitions. Signature files offer three distinct features:

- 1. Signature files can be used as part of the documentation of code, since type information is of paramount importance for an application programmer to use a library.
- 2. Signature files may be written before the implementation file. This allows for a higher-level programming design that focuses on which functions should be included and how they can be composed.
- 3. Signature files allow for access control. Most importantly, if a type definition is not available in the signature file, then it is not available to the application program. Such definitions are private and can only be used internally in the library code. More fine-grained control related to classes is available and will be discussed in Chapter 20.

Signature files can be generated automatically using the --sig:<filename> compiler directive. To demonstrate this feature, we will first move the definition of add to the implementation file, see Listing 9.28.

```
Listing 9.24 MetaWAdd.fs:
An implementation file including the add function.
module Meta
type floatFunction = float -> float -> float
let apply (f : floatFunction) (x : float) (y : float) : float
 let add (x : float) (y : float) : float = x + y
```

A signature file may be automatically generated, as shown in Listing 9.25.

#### Listing 9.25: Automatic generation of a signature file at compile time.

```
$ fsharpc --nologo --sig:MetaWAdd.fsi MetaWAdd.fs

MetaWAdd.fs(4,48): warning FS0988: Main module of program is empty: nothing will happen when it is run
```

The warning can safely be ignored, since at this point it is not our intention to produce runnable code. The above listing has generated the signature file in Listing 9.26.

# Listing 9.26 MetaWAdd.fsi: An automatically generated signature file from MetaWAdd.fs. module Meta type floatFunction = float -> float -> float val apply: f:floatFunction -> x:float -> y:float -> float val add: x:float -> y:float -> float

We can generate a library using the automatically generated signature file by writing fsharpc -a MetaWAdd.fsi MetaWAdd.fs, which is identical to compiling the .dll file without the signature file. However, if we remove, e.g., the type definition for add in the signature file, then this function becomes private to the module and cannot be accessed outside. Hence, using the signature file in Listing 9.27, and recompiling the .dll with Listing 9.24 does not generates errors.

```
Listing 9.27 MetaWAddRemoved.fsi:
Removing the type defintion for add from MetaWAdd.fsi.

1 module Meta
2 type floatFunction = float -> float -> float
3 val apply : f:floatFunction -> x:float -> y:float -> float
```

```
Listing 9.28: Automatic generation of a signature file at compile time.

$ fsharpc --nologo -a MetaWAddRemoved.fsi MetaWAdd.fs
```

However, when using the newly created MetaWAdd.dll with an application that does not itself supply a definition of add, we get a syntax error, since add now is inaccessible to the application program. This is demonstrated in Listing 9.29 and 9.30.

```
Listing 9.29 MetaWOAddApp.fsx:
A version of Listing 9.3 without a definition of add.

1 let result = Meta.apply add 3.0 4.0
2 printfn "3.0 + 4.0 = %A" result
```

#### 9. Organising Code in Libraries and Application Programs

#### Listing 9.30: Automatic generation of a signature file at compile time.

```
$ fsharpc --nologo -r MetaWAdd.dll MetaWOAddApp.fsx

MetaWOAddApp.fsx(1,25): error FS0039: The value or constructor
  'add' is not defined.
```

# 10 Testing Programs

A software bug is an error in a computer program that causes it to produce an incorrect result or behave in an unintended manner. The term 'bug' was used by Thomas Edison in  $1878^1$ , but made popular in computer science by Grace Hopper, who found a moth interfering with the electronic circuits of the Harward Mark II electromechanical computer and coined the term bug for errors in computer programs. The original bug is shown in  $\cdot$  but Figure 10.1. Software is everywhere, and errors therein have a huge economic impact on our society and can threaten lives<sup>2</sup>.

The ISO/IEC organizations have developed standards for software testing<sup>3</sup>. To illustrate basic concepts of software quality, consider a hypothetical route planning system. Essential factors of its quality are:

 $\cdot$  functionality

**Functionality:** Does the software compile and run without internal errors. Does it solve the problem it was intended to solve? E.g., does the route planning software find a suitable route from point a to b?

· reliability

**Reliability:** Does the software work reliably over time? E.g., does the route planning software work when there are internet dropouts?

· usability

**Usability:** Is the software easy and intuitive to use by humans? E.g., is it easy to enter addresses and alternative routes in the software's interface?

· efficiency

<sup>&</sup>lt;sup>3</sup>ISO/IEC 9126, International standard for the evaluation of software quality, December 19, 1991, later replaced by ISO/IEC 25010:2011

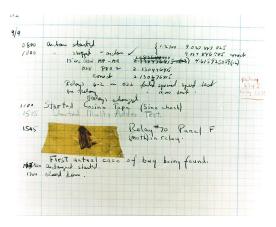


Figure 10.1.: The first computer bug, caught by Grace Hopper, U.S. Naval Historical Center Online Library Photograph NH 96566-KN.

 $<sup>^{1}</sup> https://en.wikipedia.org/wiki/Software\_bug, possibly http://edison.rutgers.edu/NamesSearch/DocImage.php3?DocId=LB003487$ 

 $<sup>^2 \</sup>verb|https://en.wikipedia.org/wiki/List_of_software_bugs|$ 

#### 10. Testing Programs

**Efficiency:** How many computer and human resources does the software require? E.g., does it take milliseconds or hours to find a requested route? Can the software run on a mobile platform with limited computer speed and memory?

· maintainability

Maintainability: In case of the discovery of new bugs, is it easy to test and correct the software? Is it easy to extend the software with new functionality? E.g., is it easy to update the map with updated roadmaps and new information? Can the system be improved to work both for car drivers and bicyclists?

· portability

**Portability:** Is it easy to port the software to new systems such as new server architecture and screen sizes? E.g., if the routing software originally was written for IOS devices, will it be easy to port to Android systems?

The above-mentioned concepts are ordered based on the requirements of the system. Functionality and reliability are perhaps the most important concepts, since if the software does not solve the specified problem, then the software design process has failed. However, many times the problem definition will evolve along with the software development process. But as a bare minimum, the software should run without internal errors and not crash under a well-defined set of circumstances. Furthermore, it is often the case that software designed for the general public requires a lot of attention to the usability of the software, since in many cases non-experts are expected to be able to use the software with little or no prior training. On the other hand, software used internally in companies will be used by a small number of people who become experts in using the software, and it is often less important that the software is easy to understand by non-experts. An example is text processing software like Microsoft Word versus Gnu Emacs and LaTeX. Word is designed to be used by non-experts for small documents such as letters and notes and relies heavily on interfacing with the system using click-interaction. On the other hand, Emacs and LaTeX are for experts for longer and professionally typeset documents and relies heavily on keyboard shortcuts and text-codes for typesetting document entities.

The purpose of software testing is to find bugs. When errors are found, then we engage in  $\cdot$  software testing debugging, which is the process of diagnosing and correcting bugs. Once we have a failed software test, i.e., one that does not find any bugs, then we have strengthened our belief in the software, but it is important to note that software testing and debugging rarely removes all bugs, and with each correction or change of software there is a fair risk new bugs being introduced. It is not exceptional that the testing-software is as large as the software being tested.

· debugging

In this chapter, we will focus on two approaches to software testing which emphasize functionality: white-box and black-box testing. An important concept in this context is unit testing, where the program is considered in smaller pieces, called units, and for which accompanying programs for testing can be made which test these units automatically. Black-box testing considers the problem formulation and the program interface, and can typically be written early in the software design phase. In contrast, white-box testing considers the program text, and thus requires the program to be available. Thus, there is a tendency for black-box test programs to be more stable, while white-box testing typically is developed incrementally alongside the software development.

 $\cdot$  white-box testing · black-box testing · unit testing

To illustrate software testing, we'll start with a problem:

#### Problem 10.1

Given any date in the Gregorian calendar, calculate the day of the week.

Facts about dates in the Gregorian calendar are:

- Combinations of dates and weekdays repeat themselves every 400 years.
- The typical length of the months January, February, ... follow the knuckle rule, i.e., January belongs to the index knuckle, February to the space between the index and the middle finger, and August restarts or starts on the other hand. All knuckle months have 31 days, all spacing months have 30 days except February, which has 29 days on leap years and 28 days all other years.
- A leap year is a multiple of 4, except if it is also a multiple of 100 but not of 400.

Many solutions to the problem have been discovered, and here we will base our program on Gauss' method, which is based on integer division and calculates the weekday of the 1st of January of a given year. For any other date, we will count our way through the weeks from the previous 1st of January. The algorithm relies on an enumeration of weekdays starting with Sunday = 0, Monday  $= 1, \ldots$ , and Saturday = 6. Our proposed solution is shown in Listing 10.1.4

#### Listing 10.1 date2Day.fsx: A function that can calculate day-of-week from any date in the Gregorian let januaryFirstDay (y : int) = let a = (y - 1) % 4let b = (y - 1) % 100let c = (y - 1) % 400(1 + 5 \* a + 4 \* b + 6 \* c) % 7let rec sum (lst : int list) j = if 0 <= j && j < lst.Length then</pre> lst.[0] + sum lst.[1..] (j - 1) else 0 let date2Day d m y = let dayPrefix = ["Sun"; "Mon"; "Tues"; "Wednes"; "Thurs"; "Fri"; "Satur"] let feb = if (y % 4 = 0) && ((y % 100 <> 0) || (y % 400 = 0)) then 29 else 28 let daysInMonth = [31; feb; 31; 30; 31; 30; 31; 30; 31; 30; 31] let dayOne = januaryFirstDay y let daysSince = (sum daysInMonth (m - 2)) + d - 1 let weekday = (dayOne + daysSince) % 7; dayPrefix.[weekday] + "day"

#### 10.1. White-box Testing

White-box testing considers the text of a program. The degree to which the text of the · white-box testing program is covered in the test is called the *coverage*. Since our program is small, we have · coverage the opportunity to ensure that all functions are called at least once, which is called *function* 

<sup>&</sup>lt;sup>4</sup>Jon: This example relies on lists, which has not been introduced yet.

coverage, and we will also be able to test every branching in the program, which is called • function coverage branching coverage. If both are fulfilled, we say that we have statement coverage. The branching coverage procedure is as follows:

- · statement coverage
- 1. Decide which units to test: The program shown in Listing 10.1 has 3 functions, and we will consider these each as a unit, but we might as well just have chosen date2Day as a single unit. The important part is that the union of units must cover the whole program text, and since date2Day calls both januaryFirstDay and sum, designing test cases for the latter two is superfluous. However, we may have to do this anyway when debugging, and we may choose at a later point to use these functions separately, and in both cases, we will be able to reuse the testing of the smaller units.
- 2. Identify branching points: The function januaryFirstDay has no branching function, sum has one, and depending on the input values, two paths through the code may be used, and date2Day has one where the number of days in February is decided. Note that in order to test this, our test-date must be March 1 or later. In this example, there are only examples of if-branch points, but they may as well be loops and pattern matching expressions. In the Listing 10.2 it is shown that the branch points have been given a comment and a number.

```
Listing 10.2 date2DayAnnotated.fsx:
In white-box testing, the branch points are identified.
// Unit: januaryFirstDay
let januaryFirstDay (y : int) =
  let a = (y - 1) \% 4
   let b = (y - 1) \% 100
   let c = (y - 1) \% 400
   (1 + 5 * a + 4 * b + 6 * c) \% 7
// Unit: sum
let rec sum (lst : int list) j =
   (* WB: 1 *)
   if 0 <= j && j < lst.Length then</pre>
     lst.[0] + sum lst.[1..] (j - 1)
   else
     0
// Unit: date2Day
let date2Day d m y =
   let dayPrefix =
     ["Sun"; "Mon"; "Tues"; "Wednes"; "Thurs"; "Fri";
   "Satur"]
   (* WB: 1 *)
   let feb = if (y % 4 = 0) && ((y % 100 <> 0) || (y % 400
   = 0)) then 29 else 28
   let daysInMonth = [31; feb; 31; 30; 31; 30; 31; 30;
   31; 30; 31]
   let dayOne = januaryFirstDay y
   let daysSince = (sum daysInMonth (m - 2)) + d - 1
   let weekday = (dayOne + daysSince) % 7;
   dayPrefix.[weekday] + "day"
```

3. For each unit, produce an input set that tests each branch: In our example, the branch points depend on a Boolean expression, and for good measure, we are going

#### 10. Testing Programs

to test each term that can lead to branching. Thus,

Unit	Branch	Condition	Input	Expected
				out-
				put
januaryFirstDay	0	-	2016	5
sum	1	0 <= j && j < lst.Length		
	1a	true && true	[1; 2; 3] 1	3
	1b	false && true	[1; 2; 3] -1	0
	1c	true && false	[1; 2; 3] 10	0
	1d	false && false	-	-
date2Day	1	(y % 4 = 0)		
		&& ((y % 100 <> 0)		
		(y % 400 = 0))		
	-	true && (true    true)	-	-
	1a	true && (true    false)	8 9 2016	Thursday
	1b	true && (false    true)	8 9 2000	Friday
	1c	true && (false    false)	8 9 2100	Wednesday
	-	false && (true    true)	-	-
	1d	false && (true    false)	8 9 2015	Tuesday
	-	false && (false    true)	-	-
	-	false && (false    false)	-	-

The impossible cases have been intentionally blank, e.g., it is not possible for j < 0 and j > n for some positive value n.

4. Write a program that tests all these cases and checks the output, e.g.,

#### Listing 10.3 date2DayWhiteTest.fsx: The tests identified by white-box analysis. The program from Listing 10.2 has been omitted for brevity. printfn "White-box testing of date2Day.fsx" printfn " Unit: januaryFirstDay" printfn " Branch: 0 - %b" (januaryFirstDay 2016 = 5) printfn " Unit: sum" printfn " Branch: 1a - %b'' (sum [1; 2; 3] 1 = 3) printfn " Branch: 1b - %b'' (sum [1; 2; 3] -1 = 0) Branch: 1c - %b" (sum [1; 2; 3] 10 = 0) printfn " printfn " Unit: date2Day" printfn " Branch: 1a - %b" (date2Day 8 9 2016 = "Thursday") printfn " Branch: 1b - %b" (date2Day 8 9 2000 = "Friday") printfn " Branch: 1c - %b" (date2Day 8 9 2100 = "Wednesday") Branch: 1d - %b" (date2Day 8 9 2015 = printfn " "Tuesday") \$ fsharpc --nologo date2DayWhiteTest.fsx && mono date2DayWhiteTest.exe White-box testing of date2Day.fsx Unit: januaryFirstDay Branch: 0 - true Unit: sum Branch: 1a - true Branch: 1b - true Branch: 1c - true Unit: date2Day Branch: 1a - true Branch: 1b - true Branch: 1c - true Branch: 1d - true

Notice that the output of the tests is organized such that they are enumerated per unit, hence we can rearrange as we like and still uniquely refer to a unit's test. Also, the output of the test program produces a list of tests that should return true or success or a similar positively loaded word, but without further or only little detail, such that we at a glance can identify any test that produced unexpected results.

After the white-box testing has failed to find errors in the program, we have some confidence in the program, since we have run every line at least once. It is, however, in no way a guarantee that the program is error free, which is why white-box testing is often accompanied with black-box testing to be described next.

#### 10.2. Black-box Testing

In black-box testing, the program is considered a black box, and no knowledge is required about how a particular problem is solved. In fact, it is often useful not to have that

#### 10. Testing Programs

knowledge at all. It is rarely possible to test all input to a program, so in black-box testing, the solution is tested for typical and extreme cases based on knowledge of the problem. The procedure is as follows:

- 1. Decide on the interface to use: It is useful to have an agreement with the software developers about what interface is to be used, e.g., in our case, the software developer has made a function date2Day d m y where d, m, and y are integers specifying the day, month, and year.
- 2. Make an overall description of the tests to be performed and their purpose:
  - 1 a consecutive week, to ensure that all weekdays are properly returned
  - 2 two set of consecutive days across boundaries that may cause problems: across a new year, and across a regular month boundary.
  - 3 a set of consecutive days across February-March boundaries for a leap and non-leap year
  - 4 four dates after February in a non-leap year, a non-multiple-of-100 leap year, a multiple-of-100-but-not-of-400 non-leap year, and a multiple-of-400 leap year.

Given no information about the program's text, there are other dates that one could consider as likely candidates for errors, but the above is judged to be a fair coverage.

3. Choose a specific set of input and expected output relations on the tabular form:

Test number	Input	Expected output
1a	1 1 2016	Friday
1b	2 1 2016	Saturday
1c	3 1 2016	Sunday
1d	4 1 2016	Monday
1e	5 1 2016	Tuesday
1f	6 1 2016	Wednesday
1g	7 1 2016	Thursday
2a	31 12 2014	Wednesday
2b	1 1 2015	Thursday
2c	30 9 2017	Saturday
2d	1 10 2017	Sunday
3a	28 2 2016	Sunday
3b	29 2 2016	Monday
3c	1 3 2016	Tuesday
3d	28 2 2017	Tuesday
3e	1 3 2017	Wednesday
4a	1 3 2015	Sunday
4b	1 3 2012	Thursday
4c	1 3 2000	Wednesday
4d	1 3 2100	Monday

4. Write a program executing the tests, as shown in Listing 10.4 and 10.5.

## Listing 10.4 date2DayBlackTest.fsx: The tests identified by black-box analysis. The program from Listing 10.2 has been omitted for brevity.

```
let testCases = [
      ("A complete week",
       [(1, 1, 2016, "Friday");
        (2, 1, 2016, "Saturday");
        (3, 1, 2016, "Sunday");
        (4, 1, 2016, "Monday");
        (5, 1, 2016, "Tuesday");
        (6, 1, 2016, "Wednesday");
        (7, 1, 2016, "Thursday");]);
      ("Across boundaries",
       [(31, 12, 2014, "Wednesday");
        (1, 1, 2015, "Thursday");
        (30, 9, 2017, "Saturday");
(1, 10, 2017, "Sunday")]);
40
42
     ("Across Feburary boundary",
       [(28, 2, 2016, "Sunday");
(29, 2, 2016, "Monday");
43
        (1, 3, 2016, "Tuesday");
(28, 2, 2017, "Tuesday");
(1, 3, 2017, "Wednesday")]);
     ("Leap years",
       [(1, 3, 2015, "Sunday");
        (1, 3, 2012, "Thursday");
        (1, 3, 2000, "Wednesday");
        (1, 3, 2100, "Monday")]);
   printfn "Black-box testing of date2Day.fsx"
   for i = 0 to testCases.Length - 1 do
     let (setName, testSet) = testCases.[i]
     printfn " %d. %s" (i+1) setName
     for j = 0 to testSet.Length - 1 do
        let (d, m, y, expected) = testSet.[j]
        let day = date2Day d m y
        printfn "
                      test %d - %b" (j+1) (day = expected)
```

```
Listing 10.5: Output from Listing 10.4.
 $ fsharpc --nologo date2DayBlackTest.fsx && mono
   date2DayBlackTest.exe
Black-box testing of date2Day.fsx
   1. A complete week
     test 1 - true
     test 2 - true
     test 3 - true
     test 4 - true
     test 5 - true
     test 6 - true
     test 7 - true
   2. Across boundaries
     test 1 - true
     test 2 - true
     test 3 - true
     test 4 - true
   3. Across Feburary boundary
     test 1 - true
     test 2 - true
     test 3 - true
     test 4 - true
     test 5 - true
   4. Leap years
     test 1 - true
     test 2 - true
     test 3 - true
     test 4 - true
```

Notice how the program has been made such that it is almost a direct copy of the table produced in the previous step.

A black-box test is a statement of what a solution should fulfill for a given problem. Hence, it is a good idea to make a black-box test early in the software design phase, Advice in order to clarify the requirements for the code to be developed and take an outside view of the code prior to developing it.

After the black-box testing has failed to find errors in the program, we have some confidence in the program, since, from a user's perspective, the program produces sensible output in many cases. It is, however, in no way a guarantee that the program is error free.

#### 10.3. Debugging by Tracing

Once an error has been found by testing, the *debugging* phase starts. The cause of a bug can either be that the chosen algorithm is the wrong one for the job, or the implementation of it has an error. In the debugging process, we have to keep an open mind and not rely on assumptions, since assumptions tend to blind the reader of a text. A frequent source of errors is that the state of a program is different than expected, e.g., because the calculation performed is different than intended, or that the return of a library function is different than expected. The most important tool for debugging is *simplification*. This is similar to white-box testing, but where the units tested are very small. E.g., the suspected piece of code could be broken down into smaller functions or code snippets, which are given

well-defined input, and, e.g., use printfn statements to obtain the output of the code snippet. Another related technique is to use mockup code, which replaces parts of the code with code that produces safe and relevant results. If the bug is not obvious, then more rigorous techniques must be used, such as tracing. Some development interfaces have a built-in tracing system, e.g., fsharpi will print inferred types and some binding values. However, often the source of a bug is due to a misunderstanding of the flow of data through a program execution, and we will in the following introduce hand tracing as a technique · hand tracing to simulate the execution of a program by hand.

Consider the program in Listing 10.6. <sup>5</sup>

```
Listing 10.6 gcd.fsx:
The greatest common divisor of 2 integers.
 let rec gcd a b =
   if a < b then
     gcd b a
   elif b > 0 then
     gcd b (a % b)
   else
 let a = 10
 let b = 15
 printfn "gcd %d %d = %d" a b (gcd a b)
 $ fsharpc --nologo gcd.fsx && mono gcd.exe
 gcd 10 15 = 5
```

The program includes a function for calculating the greatest common divisor of 2 integers, and calls this function with the numbers 10 and 15. Hand tracing this program means that we simulate its execution and, as part of that, keep track of the bindings, assignments and input and output of the program. To do this, we need to consider code snippets' environments. E.g., to hand trace the above program, we start by noting the outer environment, called  $E_0$  for short. In line 1, the gcd identifier is bound to a function, hence we write:

· environment

$$E_0:$$
 gcd  $\rightarrow ((a,b), \text{gcd-body}, \varnothing)$ 

Function bindings like this one are noted as closures, which are triplets of the form (arguments, expression, environment). The symbol  $\varnothing$  denotes the empty environment. The closure is everything needed for the expression to be calculated. Here, we wrote gcd-body to denote everything after the equal sign in the function binding. Next, F# executes line 9 and 10, and we update our environment to reflect the bindings as,

$$E_0:$$
 $\gcd \to \big((a,b), \gcd\text{-body}, \varnothing\big)$ 
 $a \to 10$ 
 $b \to 15$ 

In line 11, the function is evaluated. This initiates a new environment  $E_1$ , and we update

<sup>&</sup>lt;sup>5</sup>Jon: This program uses recursion, which has not been introduced yet.

our trace as,

```
E_0:

\gcd \to ((a,b), \gcd\text{-body}, \varnothing)

a \to 10

b \to 15

line 11: \gcd a b \to ?

E_1:((a \to 10, b \to 15), \gcd\text{-body}, \varnothing)
```

where the new environment is noted to have gotten its argument names a and b bound to the values 10 and 15 respectively, and where the return of the function to environment  $E_0$  is yet unknown, so it is noted as a question mark. In line 2, the comparison a < b is checked, and since we are in environment  $E_1$ , this is the same as checking 10 < 15, which is true, so the program executes line 3. Hence, we initiate a new environment  $E_2$  and update our trace as,

$$E_0: \\ \gcd \to \big((a,b), \gcd\text{-body}, \varnothing\big) \\ a \to 10 \\ b \to 15 \\ \text{line 11: gcd a b} \to ? \\ E_1: \big((a \to 10, b \to 15), \gcd\text{-body}, \varnothing\big) \\ \text{line 3: gcd b a} \to ? \\ E_2: \big((a \to 15, b \to 10), \gcd\text{-body}, \varnothing\big)$$

where in the new environment, a and b are bound to the values 15 and 10 respectively. In  $E_2$ , 10 < 15 is false, so the program evaluates b > 0, which is true, hence line 5 is executed. This calls gcd once again, but with new arguments. Since a % b is parenthesized, it is evaluated before gcd is called.

Hence, we update our trace as,

$$E_0: \gcd \to ((a,b), \gcd\text{-body}, \varnothing)$$

$$a \to 10$$

$$b \to 15$$

$$\text{line 11: } \gcd \text{ a b} \to ?$$

$$E_1: ((a \to 10, b \to 15), \gcd\text{-body}, \varnothing)$$

$$\text{line 3: } \gcd \text{ b a} \to ?$$

$$E_2: ((a \to 15, b \to 10), \gcd\text{-body}, \varnothing)$$

$$\text{line 5: } \text{a \% b} \to 5$$

$$\text{line 5: } \gcd \text{ b (a \% b)} \to ?$$

$$E_3: ((a \to 10, b \to 5), \gcd\text{-body}, \varnothing)$$

Again we fall through to line 5, evaluate the remainder operator and initiate a new envi-

ronment,

$$E_0:$$

$$\gcd \to ((a,b), \gcd\text{-body}, \varnothing)$$

$$a \to 10$$

$$b \to 15$$

$$\text{line 11: } \gcd \text{ a b} \to ?$$

$$E_1: ((a \to 10, b \to 15), \gcd\text{-body}, \varnothing)$$

$$\text{line 3: } \gcd \text{ b a} \to ?$$

$$E_2: ((a \to 15, b \to 10), \gcd\text{-body}, \varnothing)$$

$$\text{line 5: } \text{a \% b} \to 5$$

$$\text{line 5: } \gcd \text{ b (a \% b)} \to ?$$

$$E_3: ((a \to 10, b \to 5), \gcd\text{-body}, \varnothing)$$

$$\text{line 5: } \text{a \% b} \to 0$$

$$\text{line 5: } \gcd \text{ b (a \% b)} \to ?$$

$$E_4: ((a \to 5, b \to 0), \gcd\text{-body}, \varnothing)$$

This time both a < b and b > 0 are false, so we fall through to line 7, and gcd from  $E_4$  returns its value of a, which is 5, so we scratch  $E_4$  and change the question mark in  $E_3$  to 5,

$$E_0: \gcd \to \big((a,b), \gcd\text{-body}, \varnothing\big)$$

$$a \to 10$$

$$b \to 15$$

$$\text{line 11: } \gcd \text{ a b} \to ?$$

$$E_1: \big((a \to 10, b \to 15), \gcd\text{-body}, \varnothing\big)$$

$$\text{line 3: } \gcd \text{ b a} \to ?$$

$$E_2: \big((a \to 15, b \to 10), \gcd\text{-body}, \varnothing\big)$$

$$\text{line 5: } \text{a \% b} \to 5$$

$$\text{line 5: } \gcd \text{ b (a \% b)} \to ?$$

$$E_3: \big((a \to 10, b \to 5), \gcd\text{-body}, \varnothing\big)$$

$$\text{line 5: } \text{a \% b} \to 0$$

$$\text{line 5: } \gcd \text{ b (a \% b)} \to ?$$

$$E_4: \big((a \to 5, b \to 0), \gcd\text{-body}, \varnothing\big)$$

Now, line 5 in  $E_3$  is also a return point of gcd, hence we scratch  $E_3$  and change the question

mark in  $E_2$  to 5,

$$E_0:$$

$$\gcd \to ((a,b), \gcd\text{-body}, \varnothing)$$

$$a \to 10$$

$$b \to 15$$

$$\text{line 11: } \gcd \text{ a b} \to ?$$

$$E_1: ((a \to 10, b \to 15), \gcd\text{-body}, \varnothing)$$

$$\text{line 3: } \gcd \text{ b a} \to ?$$

$$E_2: ((a \to 15, b \to 10), \gcd\text{-body}, \varnothing)$$

$$\text{line 5: } \text{a \% b} \to 5$$

$$\text{line 5: } \gcd \text{ b (a \% b)} \to ? 5$$

$$E_{\$}: ((a \to 10, b \to 5), \gcd\text{-body}, \varnothing)$$

$$\text{line 5: } \text{a \% b} \to 0$$

$$\text{line 5: } \gcd \text{ b (a \% b)} \to ? 5$$

$$E_{\$}: ((a \to 5, b \to 0), \gcd\text{-body}, \varnothing)$$

and likewise, for  $E_2$  and  $E_1$ ,

$$E_0:$$

$$\gcd \to ((a,b), \gcd\text{-body}, \varnothing)$$

$$a \to 10$$

$$b \to 15$$

$$\text{line 11: } \gcd \text{ a } b \to ? 5$$

$$\mathcal{E}_{1}:((a \to 10, b \to 15), \gcd\text{-body}, \varnothing)$$

$$\text{line 3: } \gcd \text{ b } a \to ? 5$$

$$\mathcal{E}_{2}:((a \to 15, b \to 10), \gcd\text{-body}, \varnothing)$$

$$\text{line 5: } a \% \text{ b} \to 5$$

$$\text{line 5: } \gcd \text{ b } (a \% \text{ b}) \to ? 5$$

$$\mathcal{E}_{3}:((a \to 10, b \to 5), \gcd\text{-body}, \varnothing)$$

$$\text{line 5: } a \% \text{ b} \to 0$$

$$\text{line 5: } \gcd \text{ b } (a \% \text{ b}) \to ? 5$$

$$\mathcal{E}_{4}:((a \to 5, b \to 0), \gcd\text{-body}, \varnothing)$$

Now we are able to continue the program in environment  $E_0$  with the printfn statement,

and we write,

```
E_0:
\gcd \to ((a,b), \gcd\text{-body}, \varnothing)
a \to 10
b \to 15
\text{line 11: } \gcd \text{ a } b \to \ 5
\text{line 11: } \operatorname{stdout} \to \ \operatorname{"gcd 10 15} = 5 \ \text{"}
\mathcal{E}_{\mathbf{k}}: ((a \to 10, b \to 15), \gcd\text{-body}, \varnothing)
\text{line 3: } \gcd \text{ b } a \to \ 5
\mathcal{E}_{\mathbf{k}}: ((a \to 15, b \to 10), \gcd\text{-body}, \varnothing)
\text{line 5: } a \% \text{ b} \to 5
\text{line 5: } \gcd \text{ b } (a \% \text{ b}) \to \ 5
\mathcal{E}_{\mathbf{k}}: ((a \to 10, b \to 5), \gcd\text{-body}, \varnothing)
\text{line 5: } a \% \text{ b} \to 0
\text{line 5: } \gcd \text{ b } (a \% \text{ b}) \to \ 5
\mathcal{E}_{\mathbf{k}}: ((a \to 5, b \to 0), \gcd\text{-body}, \varnothing)
```

which completes the hand tracing of gcd.fsx.

F# uses the lexical scope, which implies that besides function arguments, we also at times need to consider the environment at the place of writing. Consider the program in Listing 10.7.

```
Listing 10.7 lexicalScopeTracing.fsx:

Example of lexical scope and closure environment.

1 let testScope x =
2 let a = 3.0
3 let f z = a * z
4 let a = 4.0
5 f x
6 printfn "%A" (testScope 2.0)

1 $ fsharpc --nologo lexicalScopeTracing.fsx
2 $ mono lexicalScopeTracing.exe
3 6.0
```

To hand trace this, we start by creating the outer environment, define the closure for testScope, and reach line 6,

```
E_0:

testScope \rightarrow (x, \text{testScope-body}, \varnothing)

line 6: testScope 2.0 \rightarrow ?
```

We create a new environment for testScope and note the bindings,

$$E_0$$
:  
testScope  $\rightarrow$   $(x, \text{testScope-body}, \varnothing)$   
line 6: testScope  $2.0 \rightarrow ?$   
 $E_1: (x \rightarrow 2.0, \text{testScope-body}, \varnothing)$   
 $a \rightarrow 3.0$   
 $f \rightarrow (z, a * z, (a \rightarrow 3.0, x \rightarrow 2.0))$   
 $a \rightarrow 4.0$ 

Since we are working with lexical scope, **a** is noted twice, and its interpretation is by lexical order. Hence, the environment for the closure of **f** is everything above in  $E_1$ , so we add  $a \to 3.0$  and  $x \to 2.0$ . In line 5, **f** is called, so we create an environment based on its closure,

$$E_0$$
:  
testScope  $\rightarrow$   $(x, \text{testScope-body}, \varnothing)$   
line 6: testScope  $2.0 \rightarrow ?$   
 $E_1:(x \rightarrow 2.0, \text{testScope-body}, \varnothing)$   
 $a \rightarrow 3.0$   
 $f \rightarrow (z, a * z, (a \rightarrow 3.0, x \rightarrow 2.0))$   
 $a \rightarrow 4.0$   
line 5:  $f \times a \rightarrow ?$   
 $E_2:(z \rightarrow 2.0, a * z, (a \rightarrow 3.0, x \rightarrow 2.0))$ 

The expression in the environment  $E_2$  evaluates to 6.0, and unraveling the scopes we get,

$$E_0$$
:  
testScope  $\rightarrow$   $(x, \text{testScope-body}, \varnothing)$   
line 6: testScope  $2.0 \rightarrow \% 6.0$   
line 6: stdout  $\rightarrow$  "6.0"  
 $E_{1}:(x \rightarrow 2.0, \text{testScope-body}, \varnothing)$   
 $a \rightarrow 3.0$   
f  $\rightarrow (z, a * z, (a \rightarrow 3.0, x \rightarrow 2.0))$   
 $a \rightarrow 4.0$   
line 5: f x  $\rightarrow \% 6.0$   
 $E_{2}:(z \rightarrow 2.0, a * z, (a \rightarrow 3.0, x \rightarrow 2.0))$ 

For mutable binding, the scope is dynamic. For this, we need the concept of storage. Consider the program in Listing 10.8.

# Listing 10.8 dynamicScopeTracing.fsx: Example of lexical scope and closure environment. 1 let testScope x = 2 let mutable a = 3.0 3 let f z = a \* z 4 a <- 4.0 5 f x 6 printfn "%A" (testScope 2.0) 1 \$ fsharpc --nologo dynamicScopeTracing.fsx 2 \$ mono dynamicScopeTracing.exe 3 8.0

We add a storage area to our hand tracing, e.g., line 6,

```
Store: E_0: testScope \rightarrow (x, \text{testScope-body}, \varnothing) line 6: testScope 2.0 \rightarrow?
```

So when we generate environment  $E_1$ , the mutable binding is to a storage location,

```
Store: \alpha_1 \to 3.0
E_0:
\operatorname{testScope} \to (x, \operatorname{testScope-body}, \varnothing)
\operatorname{line} 6: \operatorname{testScope} 2.0 \to ?
E_1: (x \to 2.0, \operatorname{testScope-body}, \varnothing)
a \to \alpha_1
```

which is assigned the value 3.0 at the definition of a. Now, the definition of f is using the storage location,

```
Store: \alpha_1 \to 3.0
E_0:
\operatorname{testScope} \to (x, \operatorname{testScope-body}, \varnothing)
\operatorname{line} 6: \operatorname{testScope} 2.0 \to ?
E_1: (x \to 2.0, \operatorname{testScope-body}, \varnothing)
a \to \alpha_1
f \to (z, a * z, (a \to \alpha_1, x \to 2.0))
```

and in line 4, it is the value in the storage which is updated,

Store:  $\alpha_1 \to 3.04.0$   $E_0:$   $\operatorname{testScope} \to (x, \operatorname{testScope-body}, \varnothing)$   $\operatorname{line} 6: \operatorname{testScope} 2.0 \to ?$   $E_1: (x \to 2.0, \operatorname{testScope-body}, \varnothing)$   $a \to \alpha_1$   $f \to (z, a * z, (a \to \alpha_1, x \to 2.0))$ 

Hence,

Store:  

$$\alpha_1 \rightarrow 3:0 4.0$$
  
 $E_0$ :  
testScope  $\rightarrow (x, \text{testScope-body}, \varnothing)$   
line 6: testScope  $2.0 \rightarrow ?$   
 $E_1:(x \rightarrow 2.0, \text{testScope-body}, \varnothing)$   
 $a \rightarrow \alpha_1$   
 $f \rightarrow (z, a * z, (a \rightarrow \alpha_1, x \rightarrow 2.0))$   
line 5:  $f \times a \rightarrow ?$   
 $E_2:(z \rightarrow 2.0, a * z, (a \rightarrow \alpha_1, x \rightarrow 2.0))$ 

and the return value from f evaluated in environment  $E_2$  now reads the value 4.0 for a and returns 8.0. Hence,

Store: 
$$\alpha_1 \to 3.0 \ 4.0$$

$$E_0:$$

$$\operatorname{testScope} \to (x, \operatorname{testScope-body}, \varnothing)$$

$$\operatorname{line} 6: \ \operatorname{testScope} \ 2.0 \to \ 8.0$$

$$\operatorname{line} 6: \ \operatorname{stdout} \to \ 8.0"$$

$$E_{\mathbf{k}}: (x \to 2.0, \operatorname{testScope-body}, \varnothing)$$

$$a \to \alpha_1$$

$$f \to (z, a * z, (a \to \alpha_1, x \to 2.0))$$

$$\operatorname{line} 5: \ f \ x \to \ 8.0$$

$$E_{\mathbf{k}}: (z \to 2.0, a * z, (a \to \alpha_1, x \to 2.0))$$

By the above examples, it is seen that hand tracing can be used to study the flow of data through a program in detail. It may seem tedious in the beginning, but the care illustrated above is useful to ensure rigor in the analysis. Most will find that once accustomed to the method, the analysis can be performed rigorously but with less paperwork, and in conjunction with strategically placed debugging printfn statements, it is a very valuable tool for debugging.

## The Console in Windows, Α MacOS X, and Linux

Almost all popular operating systems are accessed through a user-friendly graphical user interface (GUI) that is designed to make typical tasks easy to learn to solve. As a computer programmer, you often need to access some of the functionalities of the computer, which, unfortunately, are sometimes complicated by this particular graphical user interface. The console, also called the terminal and the Windows command line, is the right hand of a console programmer. The console is a simple program that allows you to complete text commands. Almost all the tasks that can be done with the graphical user interface can be done in the console and vice versa. Using the console, you will benefit from its direct control of the programs we write, and in your education, you will benefit from the fast and raw information you get through the console.

- · graphical user interface
- $\cdot$  GUI
- $\cdot$  terminal
- · Windows command line

### A.1. The Basics

When you open a directory or folder in your preferred operating system, the directory · directory will have a location in the file system, whether from the console or through the operating system's graphical user interface. The console will almost always be associated with a particular directory or folder in the file system, and it is said that it is the directory that the console is in. The exact structure of file systems varies between Linux, MacOS X, and Windows, but common is that it is a hierarchical structure. This is illustrated in Figure A.1.

There are many predefined console commands, available in the console, and you can also make your own. In the following sections, we will review the most important commands in the three different operating systems. These are summarized in Table A.1.

### A.2. Windows

In this section we will discuss the commands summarized in Table A.1. Windows 7 and earlier versions: To open the console, press Start->Run in the lower left corner, and then type cmd in the box. In Windows 8 and 10, you right-click on the windows icon, choose Run or equivalent in your local language, and type cmd. Alternatively, you can type Windows-key + R. Now you should open a console window with a prompt showing something like Listing A.1.

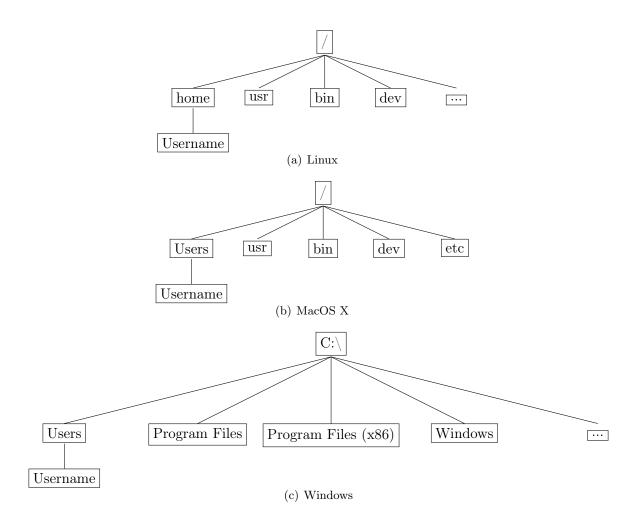


Figure A.1.: The top file hierarchy levels of common operating systems.

Windows	MacOS X/Linux	Description
dir	ls	Show content of present di-
		rectory.
cd <dir></dir>	cd <dir></dir>	Change present directory
		to <dir>.</dir>
mkdir <dir></dir>	mkdir <dir></dir>	Create directory <dir>.</dir>
rmdir <dir></dir>	rmdir <dir></dir>	Delete <dir> (Warning:</dir>
		cannot be reverted).
move <file> <file dir="" or=""></file></file>	mv <file> <file dir="" or=""></file></file>	Move <fil> to <file or<="" td=""></file></fil>
		dir>.
copy <file1> <file2></file2></file1>	cp <file1> <file2></file2></file1>	Create a new file called
		<pre><file2> as a copy of</file2></pre>
		<file1>.</file1>
del <file></file>	rm <file></file>	delete <file> (Warning:</file>
		cannot be reverted).
echo <string or="" variable=""></string>	echo <string or="" variable=""></string>	Write a string or content of
		a variable to screen.

Table A.1.: The most important console commands for Windows, MacOS X, and Linux.

· dir

 $\cdot$  cd

# Listing A.1: The Windows console. Microsoft Windows [Version 6.1.7601] Copyright (c) 2009 Microsoft Corporation. All rights reserved. C:\Users\sporring>

To see which files are in the directory, use *dir*, as shown in Listing A.2.

Listing A.2: Directory listing with dir. C:\Users\sporring>dir Volume in drive C has no label. Volume Serial Number is 94F0-31BD Directory of C:\Users\sporring 30-07-2015 15:23 <DIR> 30-07-2015 15:23 <DIR> 30-07-2015 14:27 <DIR> Contacts 30-07-2015 14:27 <DIR> Desktop 30-07-2015 17:40 <DIR> Documents 30-07-2015 15:11 <DIR> Downloads 30-07-2015 14:28 <DIR> Favorites 30-07-2015 14:27 <DIR> Links 30-07-2015 14:27 <DIR> Music 30-07-2015 14:27 <DIR> Pictures 30-07-2015 14:27 <DIR> Saved Games 30-07-2015 17:27 <DIR> Searches <DIR> 30-07-2015 14:27 Videos 0 File(s) 0 bytes 13 Dir(s) 95.004.622.848 bytes free C:\Users\sporring>

We see that there are no files and thirteen directories (DIR). The columns tell from left to right: the date and time of their creation, the file size or if it is a folder, and the name file or directory name. The first two folders "." and ".." are found in each folder and refer to this folder as well as the one above in the hierarchy. In this case, the folder "." is an alias for C:\Users\sporring and ".." for C:\Users.

Use cd to change directory, e.g., to Documents, as in Listing A.3.

```
Listing A.3: Change directory with cd.

1 C:\Users\sporring>cd Documents
2 C:\Users\sporring\Documents>
```

Note that some systems translate default filenames, so their names may be given different names in different languages in the graphical user interface as compared to the console.

You can use mkdir to create a new directory called, e.g., myFolder, as illustrated in List- · mkdir

ing A.4.

```
Listing A.4: Creating a directory with mkdir.
C:\Users\sporring\Documents>mkdir myFolder
C:\Users\sporring\Documents>dir
 Volume in drive C has no label.
 Volume Serial Number is 94F0-31BD
 Directory of C:\Users\sporring\Documents
30-07-2015 19:17 <DIR>
30-07-2015 19:17 <DIR>
             30-07-2015 19:17 <DIR>
              3 Dir(s) 94.656.638.976 bytes free
C:\Users\sporring\Documents>
```

By using dir we inspect the result.

Files can be created by, e.g., echo and redirection, as demonstrated in Listing A.5.

·echo  $\cdot$  redirection

```
Listing A.5: Creating a file with echo and redirection.
   C:\Users\sporring\Documents>echo "Hi" > hi.txt
   C:\Users\sporring\Documents>dir
          Volume in drive C has no label.
           Volume Serial Number is 94F0-31BD
          Directory of C:\Users\sporring\Documents
   30-07-2015 19:18 <DIR>
  30-07-2015 19:18 <DIR>
30-07-2015 19:17 <DIR>
30-07-2015 19:18
                                                                                              color c
                                                                                                                                                                                                                                        8 bytes
                                                                                                3 Dir(s) 94.656.634.880 bytes free
   C:\Users\sporring\Documents>
```

 $\cdot$  move To move the file hi.txt to the directory myFolder, use move, as shown in Listing A.6.

```
Listing A.6: Move a file with move.
C:\Users\sporring\Documents>move hi.txt myFolder
         1 file(s) moved.
C:\Users\sporring\Documents>
```

Finally, use *del* to delete a file and *rmdir* to delete a directory, as shown in Listing A.7. ·del

·rmdir

### Listing A.7: Delete files and directories with del and rmdir. C:\Users\sporring\Documents>cd myFolder C:\Users\sporring\Documents\myFolder>del hi.txt C:\Users\sporring\Documents\myFolder>cd .. C:\Users\sporring\Documents>rmdir myFolder C:\Users\sporring\Documents>dir Volume in drive C has no label. Volume Serial Number is 94F0-31BD Directory of C:\Users\sporring\Documents 30-07-2015 19:20 <DIR> 30-07-2015 19:20 <DIR> 0 File(s) 0 bytes 2 Dir(s) 94.651.142.144 bytes free C:\Users\sporring\Documents>

The commands available from the console must be in its search path. The search path can  $\cdot$  search path be seen using echo, as shown in Listing A.8.

The path can be changed using the Control panel in the graphical user interface. In Windows 7, choose the Control panel, choose System and Security  $\rightarrow$  System  $\rightarrow$  Advanced system settings  $\rightarrow$  Environment Variables. In Windows 10, you can find this window by searching for "Environment" in the Control panel. In the window's System variables box, double-click on Path and add or remove a path from the list. The search path is a list of paths separated by ";". Beware, Windows uses the search path for many different tasks, so remove only paths that you are certain are not used for anything.

A useful feature of the console is that you can use the tab-key to cycle through filenames. E.g., if you write cd followed by a space and tab a couple of times, then the console will suggest to you the available directories.

### A.3. MacOS X and Linux

MacOS X (OSX) and Linux are very similar, and both have the option of using bash as  $\cdot bash$  console. It is in the standard console on MacOS X and on many Linux distributions. A summary of the most important bash commands is shown in Table A.1. In MacOS X,

·ls

you find the console by opening Finder and navigating to Applications  $\rightarrow$  Utilities -> Terminal. In Linux, the console can be started by typing Ctrl + Alt + T. Some Linux distributions have other key-combinations such as Super + T.

Once opened, the console is shown in a window with content, as shown in Listing A.9.

```
Listing A.9: The MacOS console.

Last login: Thu Jul 30 11:52:07 on ttys000
FN11194:~ sporring$
```

"FN11194" is the name of the computer, the character  $\sim$  is used as an alias for the user's home directory, and "sporring" is the username for the user presently logged onto the system. Use ls to see which files are present, as shown in Listing A.10.

```
Listing A.10: Display a directory content with 1s.

1 FN11194:~ sporring$ 1s
2 Applications Documents Library Music Public
3 Desktop Downloads Movies Pictures
4 FN11194:~ sporring$
```

More details about the files are available by using flags to 1s as demonstrated in Listing A.11.

```
Listing A.11: Display extra information about files using flags to 1s.
FN11194: sporring$ ls -l
             6 sporring staff
                                 204 Jul 30 14:07 Applications
drwx----+ 32 sporring
                                1088 Jul 30 14:34 Desktop
                        staff
drwx----+ 76 sporring
                         staff
                                2584 Jul
                                           2 15:53 Documents
drwx ----+
            4 sporring
                        staff
                                 136 Jul 30 14:35 Downloads
drwx----0 63 sporring
                                2142 Jul 30 14:07 Library
                         staff
drwx----+ 3 sporring
                         staff
                                 102 Jun 29 21:48 Movies
drwx----+ 4 sporring
                         staff
                                 136 Jul
                                           4 17:40 Music
             3 sporring
drwx ----+
                         staff
                                 102 Jun 29 21:48 Pictures
drwxr-xr-x+
             5 sporring
                         staff
                                 170 Jun 29 21:48 Public
FN11194: sporring$
```

The flag -1 means long, and many other flags can be found by querying the built-in manual with man ls. The output is divided into columns, where the left column shows a number of codes: "d" stands for directory, and the set of three of optional "rwx" denote whether respectively the owner, the associated group of users, and anyone can respectively "r" - read, "w" - write, and "x" - execute the file. In all directories but the Public directory, only the owner can do any of the three. For directories, "x" means permission to enter. The second column can often be ignored, but shows how many links there are to the file or directory. Then follows the username of the owner, which in this case is sporring. The files are also associated with a group of users, and in this case, they all are associated with the group called staff. Then follows the file or directory size, the date of last change, and the file or directory name. There are always two hidden directories: "." and "..", where "." is an alias for the present directory, and ".." for the directory above. Hidden files will be shown with the -a flag.

Use cd to change to the directory, for example to Documents as shown in Listing A.12. · cd

```
Listing A.12: Change directory with cd.
FN11194:~ sporring$ cd Documents/
FN11194:Documents sporring$
```

Note that some graphical user interfaces translate standard filenames and directories to the local language, such that navigating using the graphical user interface will reveal other files and directories, which, however, are aliases.

You can create a new directory using mkdir, as demonstrated in Listing A.13.

·mkdir

```
Listing A.13: Creating a directory using mkdir.
FN11194:Documents sporring$ mkdir myFolder
FN11194:Documents sporring$ ls
myFolder
FN11194:tmp sporring$
```

A file can be created using echo and with redirection, as shown in Listing A.14.

· echo

 $\cdot$  redirection

```
Listing A.14: Creating a file with echo and redirection.
```

```
FN11194:Documents sporring$ echo "hi" > hi.txt
FN11194:Documents sporring$ ls
              myFolder
```

To move the file hi.txt into myFolder, use mv. This is demonstrated in Listing A.15. · mv

```
Listing A.15: Moving files with mv.
FN11194:Documents sporring$ echo mv hi.txt myFolder/
FN11194:Documents sporring$
```

To delete the file and the directory, use rm and rmdir, as shown in Listing A.16.

 $\cdot$ rm ·rmdir

```
Listing A.16: Deleting files and directories.
```

```
FN11194:Documents sporring$ cd myFolder/
FN11194:myFolder sporring$ rm hi.txt
FN11194:myFolder sporring$ cd ..
FN11194:Documents sporring$ rmdir myFolder/
FN11194:Documents sporring$ ls
FN11194:Documents sporring$
```

Only commands found on the search-path are available in the console. The content of the · search-path search-path is seen using the echo command, as demonstrated in Listing A.17.

### Listing A.17: The content of the search-path.

```
1 FN11194:Documents sporring$ echo $PATH
2 /Applications/Maple
        17/:/Applications/PackageMaker.app/Contents/MacOS/:
        /Applications/MATLAB_R2014b.app/bin/:/opt/local/bin:
        /opt/local/sbin:/usr/local/bin:/usr/bin:/usr/sbin:
        /sbin:/opt/X11/bin:/Library/TeX/texbin
3 FN11194:Documents sporring$
```

The search-path can be changed by editing the setup file for Bash. On MacOS X it is called ~/.profile, and on Linux it is either ~/.bash\_profile or ~/.bashrc. Here new paths can be added by adding the following line: export PATH="<new path>:<another new path>:\$PATH".

A useful feature of Bash is that the console can help you write commands. E.g., if you write fs followed by pressing the tab-key, and if Mono is in the search-path, then Bash will typically respond by completing the line as fsharp, and by further pressing the tab-key some times, Bash will show the list of options, typically fshpari and fsharpc. Also, most commands have an extensive manual which can be accessed using the man command. E.g., the manual for rm is retrieved by man rm.

# $\mathbf{B}$ Number Systems on the Computer

### **B.1.** Binary Numbers

Humans like to use the decimal number system for representing numbers. Decimal numbers · decimal number are base 10 meaning that a decimal number consists of a sequence of digits separated by a  $\cdot$  base decimal point, where each digit can have values  $d \in \{0, 1, 2, \dots, 9\}$  and the weight of each  $\cdot$  decimal point digit is proportional to its place in the sequence of digits with respect to the decimal point, i.e., the number  $357.6 = 3 \cdot 10^2 + 5 \cdot 10^1 + 7 \cdot 10^0 + 6 \cdot 10^{-1}$ , or in general, for a number consisting of digits  $d_i$  with n+1 and m digits to the left and right of the decimal point, the value v is calculated as:

$$v = \sum_{i=-m}^{n} d_i 10^i. (B.1)$$

The basic unit of information in almost all computers is the binary digit, or bit for short. A binary number consists of a sequence of binary digits separated by a decimal point, where each digit can have values  $b \in \{0,1\}$ , and the base is 2. The general equation is,

· binary number

$$v = \sum_{i=-m}^{n} b_i 2^i, \tag{B.2}$$

and examples are  $1011.1_2 = 1 \cdot 2^3 + 0 \cdot 2^2 + 1 \cdot 2^1 + 1 \cdot 2^0 + 1 \cdot 2^{-1} = 11.5$ . Notice that we use subscript 2 to denote a binary number, while no subscript is used for decimal numbers. The left-most bit is called the most significant bit, and the right-most bit is called the least significant bit. Due to typical organisation of computer memory, 8 binary digits is called a byte, and the term word is not universally defined but typically related to the computer architecture, a program is running on, such as 32 or 64 bits.

Other number systems are often used, e.g., octal numbers, which are base 8 numbers and have digits  $o \in \{0, 1, \dots, 7\}$ . Octals are useful short-hand for binary, since 3 binary digits map to the set of octal digits. Likewise, hexadecimal numbers are base 16 with digits  $h \in \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, a, b, c, d, e, f\}$ , such that  $a_{16} = 10$ ,  $b_{16} = 11$  and so on. Hexadecimals are convenient, since 4 binary digits map directly to the set of hexadecimal digits. Thus  $367 = 101101111_2 = 557_8 = 16f_{16}$ . A list of the integers 0–63 in various bases is given in Table B.1.

### · most significant bit

- · least significant bit
- · byte
- $\cdot$  word
- · octal number
- · hexadecimal number

### B.2. IEEE 754 Floating Point Standard

The set of real numbers, also called *reals*, includes all fractions and irrational numbers. It

### B. Number Systems on the Computer

Dec	Bin	Oct	Hex	Dec	Bin	Oct	Hex
0	0	0	0	32	100000	40	20
1	1	1	1	33	100001	41	21
2	10	2	2	34	100010	42	22
3	11	3	3	35	100011	43	23
4	100	4	4	36	100100	44	24
5	101	5	5	37	100101	45	25
6	110	6	6	38	100110	46	26
7	111	7	7	39	100111	47	27
8	1000	10	8	40	101000	50	28
9	1001	11	9	41	101001	51	29
10	1010	12	a	42	101010	52	2a
11	1011	13	b	43	101011	53	2b
12	1100	14	c	44	101100	54	2c
13	1101	15	d	45	101101	55	2d
14	1110	16	е	46	101110	56	2e
15	1111	17	f	47	101111	57	2f
16	10000	20	10	48	110000	60	30
17	10001	21	11	49	110001	61	31
18	10010	22	12	50	110010	62	32
19	10011	23	13	51	110011	63	33
20	10100	24	14	52	110100	64	34
21	10101	25	15	53	110101	65	35
22	10110	26	16	54	110110	66	36
23	10111	27	17	55	110111	67	37
24	11000	30	18	56	111000	70	38
25	11001	31	19	57	111001	71	39
26	11010	32	1a	58	111010	72	3a
27	11011	33	1b	59	111011	73	3b
28	11100	34	1c	60	111100	74	3c
29	11101	35	1d	61	111101	75	3d
30	11110	36	1e	62	111110	76	3e
31	11111	37	1f	63	111111	77	3f

Table B.1.: A list of the integers 0–63 in decimal, binary, octal, and hexadecimal.

is infinite in size both in the sense that there is no largest nor smallest number, and that between any 2 given numbers there are infinitely many numbers. Reals are widely used for calculation, but since any computer only has finite memory, there are infinitely many numbers which cannot be represent on a computer. Hence, any computation performed on a computer with reals must rely on approximations. *IEEE 754 double precision floating-point format (binary64)*, known as a *double*, is a standard for representing an approximation of reals using 64 bits. These bits are divided into 3 parts: sign, exponent and fraction,

$$s e_1 e_2 \dots e_{11} m_1 m_2 \dots m_{52}$$
,

· IEEE 754 double precision floating-point format

- · binary64
- · double

where s,  $e_i$ , and  $m_j$  are binary digits. The bits are converted to a number using the equation by first calculating the exponent e and the mantissa m,

$$e = \sum_{i=1}^{11} e_i 2^{11-i}, \tag{B.3}$$

$$m = \sum_{j=1}^{52} m_j 2^{-j}.$$
 (B.4)

I.e., the exponent is an integer, where  $0 \le e < 2^{11}$ , and the mantissa is a rational, where  $0 \le m < 1$ . For most combinations of e and m, the real number v is calculated as,

$$v = (-1)^{s} (1+m) 2^{e-1023}$$
(B.5)

with the exceptions that

	m = 0	$m \neq 0$
e = 0	$v = (-1)^s 0$ (signed zero)	$v = (-1)^s m 2^{1-1023}$ (subnormals)
$e = 2^{11} - 1$	$v = (-1)^s \infty$	$v = (-1)^s \text{ NaN (not a number)}$

 $\cdot$  subnormals

where  $e=2^{11}-1=11111111111_2=2047$ . The largest and smallest number that is not · NaN infinity is thus

 $\cdot$  not a number

$$e = 2^{11} - 2 = 2046, (B.6)$$

$$m = \sum_{i=1}^{52} 2^{-j} = 1 - 2^{-52} \simeq 1,$$
(B.7)

$$v_{\text{max}} = \pm (2 - 2^{-52}) 2^{1023} \simeq \pm 2^{1024} \simeq \pm 10^{308}.$$
 (B.8)

The density of numbers varies in such a way that when e - 1023 = 52, then

$$v = (-1)^{s} \left( 1 + \sum_{j=1}^{52} m_j 2^{-j} \right) 2^{52}$$
 (B.9)

$$= \pm \left(2^{52} + \sum_{j=1}^{52} m_j 2^{-j} 2^{52}\right) \tag{B.10}$$

$$= \pm \left(2^{52} + \sum_{j=1}^{52} m_j 2^{52-j}\right) \tag{B.11}$$

$$\stackrel{k=52-j}{=} \pm \left(2^{52} + \sum_{k=51}^{0} m_{52-k} 2^k\right),\tag{B.12}$$

which are all integers in the range  $2^{52} \le |v| < 2^{53}$ . When e - 1023 = 53, then the same calculation gives

$$v \stackrel{k=53-j}{=} \pm \left(2^{53} + \sum_{k=52}^{1} m_{53-k} 2^k\right),$$
 (B.13)

which are every second integer in the range  $2^{53} \le |v| < 2^{54}$ , and so on for larger values of e. When e - 1023 = 51, the same calculation gives,

$$v \stackrel{k=51-j}{=} \pm \left(2^{51} + \sum_{k=50}^{-1} m_{51-k} 2^k\right),$$
 (B.14)

### B. Number Systems on the Computer

which is a distance between numbers of 1/2 in the range  $2^{51} \le |v| < 2^{52}$ , and so on for smaller values of e. Thus we may conclude that the distance between numbers in the interval  $2^n \le |v| < 2^{n+1}$  is  $2^{n-52}$ , for  $-1022 = 1 - 1023 \le n < 2046 - 1023 = 1023$ . For subnormals, the distance between numbers is

$$v = (-1)^s \left(\sum_{j=1}^{52} m_j 2^{-j}\right) 2^{-1022}$$
(B.15)

$$= \pm \left(\sum_{j=1}^{52} m_j 2^{-j} 2^{-1022}\right) \tag{B.16}$$

$$= \pm \left(\sum_{j=1}^{52} m_j 2^{-j-1022}\right) \tag{B.17}$$

$$\stackrel{k=-j-1022}{=} \pm \left( \sum_{j=-1023}^{-1074} m_{-k-1022} 2^k \right), \tag{B.18}$$

which gives a distance between numbers of  $2^{-1074} \simeq 10^{-323}$  in the range  $0 < |v| < 2^{-1022} \simeq 10^{-308}$ .

### $\mathbf{C}$ Commonly Used Character Sets

Letters, digits, symbols, and space are the core of how we store data, write programs, and communicate with computers and each other. These symbols are in short called characters and represent a mapping between numbers, also known as codes, and a pictorial representation of the character. E.g., the ASCII code for the letter 'A' is 65. These mappings are for short called character sets, and due to differences in natural languages and symbols used across the globe, many different character sets are in use. E.g., the English alphabet contains the letters 'a' to 'z'. These letters are common to many other European languages which in addition use even more symbols and accents. For example, Danish has further the letters 'æ', 'ø', and 'å'. Many non-European languages have completely different symbols, where the Chinese character set is probably the most extreme, and some definitions contain 106,230 different characters, albeit only 2,600 are included in the official Chinese language test at the highest level.

Presently, the most common character set used is Unicode Transformation Format (UTF), whose most popular encoding schemes are 8-bit (UTF-8) and 16-bit (UTF-16). Many other character sets exist, and many of the later build on the American Standard Code for Information Interchange (ASCII). The ISO-8859 codes were an intermediate set of character sets that are still in use, but which is greatly inferior to UTF. Here we will briefly give an overview of ASCII, ISO-8859-1 (Latin 1), and UTF.

### C.1. ASCII

The American Standard Code for Information Interchange (ASCII) [8], is a 7 bit code tuned for the letters of the English language, numbers, punctuation symbols, control codes The first 32 codes are reserved for non-printable and space, see Tables C.1 and C.2. control characters to control printers and similar devices or to provide meta-information. The meaning of each control character is not universally agreed upon.

· American Standard Code for Information Interchange  $\cdot$  ASCII

The code order is known as ASCIIbetical order, and it is sometimes used to perform · ASCIIbetical order arithmetic on codes, e.g., an uppercase letter with code c may be converted to lower case by adding 32 to its code. The ASCIIbetical order also has a consequence for sorting, i.e., when sorting characters according to their ASCII code, 'A' comes before 'a', which comes before the symbol '{'.

x0+0x	00	10	20	30	40	50	60	70
00	NUL	DLE	SP	0	@	Р	(	p
01	SOH	DC1	!	1	A	Q	a	q
02	STX	DC2	"	2	В	R	b	r
03	ETX	DC3	#	3	С	S	c	s
04	EOT	DC4	\$	4	D	Т	d	t
05	ENQ	NAK	%	5	Е	U	е	u
06	ACK	SYN	&	6	F	V	f	v
07	BEL	ETB	,	7	G	W	g	w
08	BS	CAN	(	8	Н	X	h	X
09	НТ	EM	)	9	I	Y	i	У
0A	LF	SUB	*	:	J	Z	j	Z
0B	VT	ESC	+	;	K	[	k	{
0C	FF	FS	,	<	L	\	1	
0D	CR	GS	_	=	M	]	m	}
0E	SO	RS	•	>	N	^	n	~
0F	SI	US	/	?	О	_	О	DEL

Table C.1.: ASCII

### C.2. ISO/IEC 8859

The ISO/IEC 8859 report http://www.iso.org/iso/catalogue\_detail?csnumber=28245 defines 10 sets of codes specifying up to 191 codes and graphics characters using 8 bits. Set 1, also known as ISO/IEC 8859-1, Latin alphabet No. 1, or *Latin1*, covers many European languages and is designed to be compatible with ASCII, such that code for the printable characters in ASCII is the same in ISO 8859-1. Table C.3 shows the characters above 7e. Codes 00-1f and 7f-9f are undefined in ISO 8859-1.

Latin1

### C.3. Unicode

Unicode is a character standard defined by the Unicode Consortium, http://unicode.org, as the Unicode Standard. Unicode allows for 1,114,112 different codes. Each code is called a code point which represents an abstract character. However, not all abstract characters require a unit of several code points to be specified. Code points are divided into 17 planes, each with  $2^{16} = 65,536$  code points. Planes are further subdivided into named blocks. The first plane is called the Basic Multilingual plane and its block of the first 128 code points is called the Basic Latin block and is identical to ASCII, see Table C.1, and code points 128-255 are called the Latin-1 Supplement block, and are identical to the upper range of ISO 8859-1, see Table C.3. Each code-point has a number of attributes such as the Unicode general category. Presently more than 128,000 code points are defined as covering 135 modern and historical writing systems, and obtained at http://www.unicode.org/Public/UNIDATA/UnicodeData.txt, which includes the code point, name, and general category.

A Unicode code point is an abstraction from the encoding and the graphical representation of a character. A code point is written as "U+" followed by its hexadecimal number, and for the Basic Multilingual plane, 4 digits are used, e.g., the code point with the unique name LATIN CAPITAL LETTER A has the Unicode code point "U+0041", and is in this

- · Unicode Standard
- · code point
- · blocks
- · Basic Multilingual plane
- · Basic Latin block
- · Latin-1 Supplement block
- · Unicode general category

### C. Commonly Used Character Sets

Code	Description
NUL	Null
SOH	Start of heading
STX	Start of text
ETX	End of text
EOT	End of transmission
ENQ	Enquiry
ACK	Acknowledge
BEL	Bell
BS	Backspace
HT	Horizontal tabulation
LF	Line feed
VT	Vertical tabulation
FF	Form feed
CR	Carriage return
SO	Shift out
SI	Shift in
DLE	Data link escape
DC1	Device control one
DC2	Device control two
DC3	Device control three
DC4	Device control four
NAK	Negative acknowledge
SYN	Synchronous idle
ETB	End of transmission block
CAN	Cancel
EM	End of medium
SUB	Substitute
ESC	Escape
FS	File separator
GS	Group separator
RS	Record separator
US	Unit separator
SP	Space
DEL	Delete

Table C.2.: ASCII symbols.

text visualized as 'A'. More digits are used for code points of the remaining planes.

The general category is used to specify valid characters that do not necessarily have a visual representation but possibly transform text. Some categories and their letters in the first 256 code points are shown in Table C.5.

To store and retrieve code points, they must be encoded and decoded. A common encoding is UTF-8, which encodes code points as 1 to 4 bytes, and which is backward-compatible  $\,^{\circ}$  UTF-with ASCII and ISO 8859-1. Hence, in all 3 coding systems, the character with code 65 represents the character 'A'. Another popular encoding scheme is UTF-16, which encodes  $\,^{\circ}$  UTF-characters as 2 or 4 bytes, but which is not backward-compatible with ASCII or ISO 8859-1. UTF-16 is used internally in many compilers, interpreters, and operating systems.

### $C. \ Commonly \ Used \ Character \ Sets$

x0+0x	80	90	A0	В0	C0	D0	E0	F0
00			NBSP	0	À	Ð	à	ð
01			i	土	Á	Ñ	á	ñ
02			¢	2	Â	Ò	â	ò
03			£	3	Ã	Ó	ã	ó
04			¤	,	Ä	Ô	ä	ô
05			¥	$\mu$	Å	Õ	å	õ
06				$\P$	Æ	Ö	æ	ö
07			§	•	Ç	×	ç	÷
08				3	È	Ø	è	ø
09			©	1	É	Ù	é	ù
0a			<u>a</u>	Ō	Ê	Ú	ê	ú
0b			«	<b>»</b>	Ë	Û	ë	û
0c			Г	$\frac{1}{4}$	Ì	Ü	ì	ü
0d			SHY	$\frac{\frac{1}{4}}{\frac{1}{2}}$ $\frac{3}{4}$	Í	Ý	í	ý
0e			<u>R</u>	$\frac{3}{4}$	Î	Þ	î	þ
Of			_	i	Ϊ	ſŝ	ï	ÿ

Table C.3.: ISO-8859-1 (latin1) non-ASCII part. Note that the codes 7f-9f are undefined.

Code	Description
NBSP	Non-breakable space
SHY	Soft hypen

Table C.4.: ISO-8859-1 special symbols.

General	Code points	Name
cate-		
gory		
Lu	U+0041-U+005A,	Upper case letter
	U+00C0-U+00D6,	
	U+00D8-U+00DE	
Ll	$U+0061-U+007A,\ U+00B5,$	Lower case letter
	U+00DF-U+00F6,	
	U + 00F8 - U + 00FF	
Lt	None	Digraphic letter, with first part
		uppercase
Lm	None	Modifier letter
Lo	$\mathrm{U}{+}00\mathrm{AA},\mathrm{U}{+}00\mathrm{BA}$	Gender ordinal indicator
Nl	None	Letterlike numeric character
Pc	$\mathrm{U}{+}005\mathrm{F}$	Low line
Mn	None	Nonspacing combining mark
Mc	None	Spacing combining mark
Cf	U+00AD	Soft Hyphen

Table C.5.: Some general categories for the first 256 code points.

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