Formal Verification of a Contract Signing Protocol

CS3211 Project 1

Task

Allows a set of participants to exchange messages with each other in order to arrive at a state in which each of them has a pre-agreed contract signed by others

An important property of contract signing protocols is fairness: no participant should be left in the position of having sent another participant his signature on the contract but not having received the others' signatures.



Party 1

 P_1 = public key sk(P_1) = private key



Contract

ct = contract id



Party 2

 P_2 = public key sk(P_2) = private key



T = public key sk(T) = private key

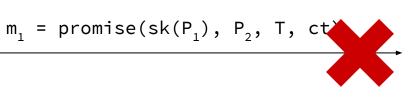
Regular Scenario



| $m_1 = promise(sk(P_1), P_2, T, ct)$ |
|--|
| $m_2 = promise(sk(P_2), P_1, T, ct)$ |
| m ₃ = sign(sk(P ₁), ct) |
| m ₄ = sign(sk(P ₂), ct) |

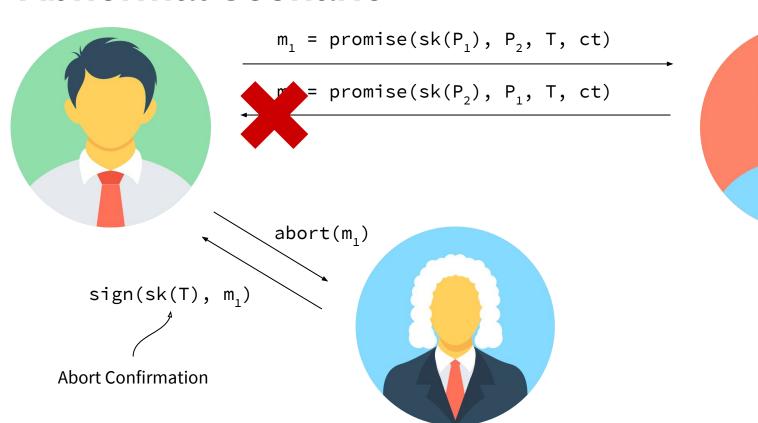




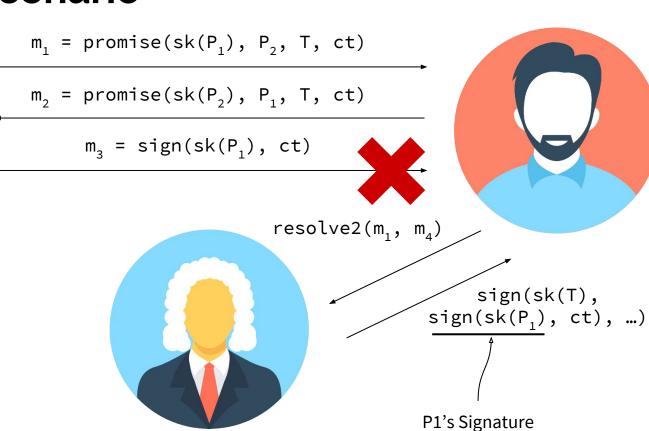


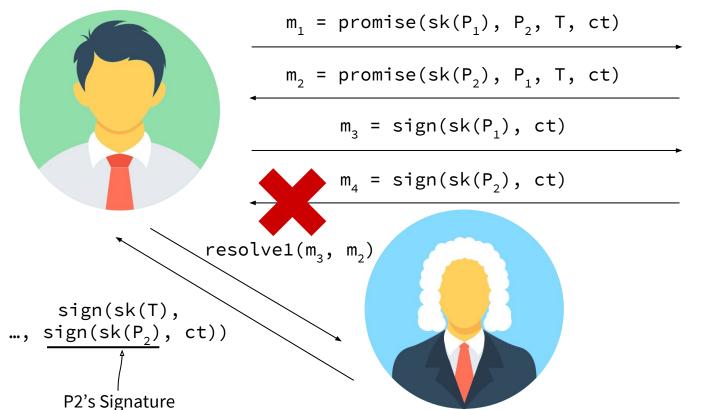














Abusefree Optimistic Contract Signing Protocol

J. A. Garay, M. Jakobsson, and P. D. MacKenzie (1999)

Implementation

P1() P2()

```
// P1
var p1State = GENERATE;
var p1RecPromise = EMPTY;
var p1RecSign = EMPTY;
var p1Promise;
var p1Sign;
var p1Sign;
var p1TrustedConfirmation = EMPTY;

[p1State == GENERATE]P1GenerateValues()
[]
[p1State == SENDPROMISE]P1SendPromise()
[]
[p1State == RECPROMISE]P1ReceivePromise()
[]
[p1State == SENDSIGN]P1SendSign()
[]
[p1State == RECSIGN]P1ReceiveSign()
```

[p1State == END | p1State == QUIT]Skip;

RSA Signing

Classroom RSA used to simulate the generation of promise and signature.

P1 or P2 promise is their private key encrypted by Trusted Party's public key.

P1 or P2 signature is the contract signed (encrypted) by their private key.

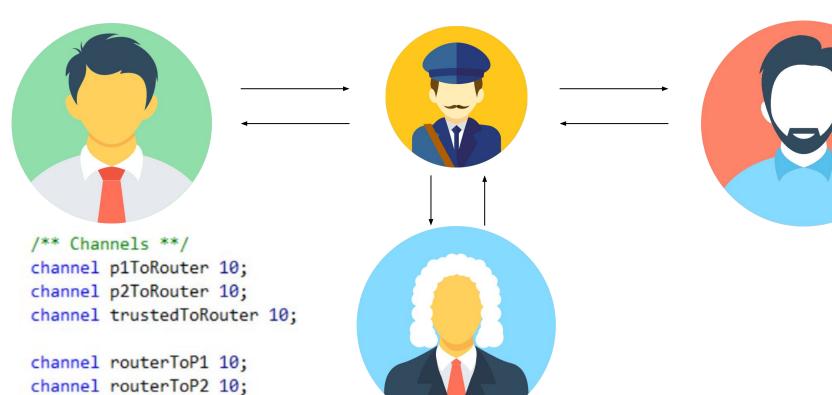
```
p1GeneratePromise{p1Promise = call(Pow, P1PRIVATE, TRUSTPUBLIC) % TRUSTMOD}
-> p1GenerateSignature{p1Sign = call(Pow, CONTRACT, P1PRIVATE) % P1MOD}
```

Trusted party can obtain P1 or P2's private key by decrypting the promise with their private key, and use it to sign the contract to form P1 or P2's signature.

```
generateP1Private{generatedPrivate = call(Pow, data2, TRUSTPRIVATE) % TRUSTMOD}
generateP1Signature{generatedSignature = call(Pow, CONTRACT, generatedPrivate) % P1MOD}
generateResolve2Confirmation{confirmation = call(Pow, generatedSignature, TRUSTPRIVATE) % TRUSTMOD}
```

Router(): A Middleman

channel routerToTrusted 10;





```
// Router and Attacker
RouterSelector() =
    secureRouter{routerState = SECURE} -> Router()
[]
    attacker{routerState = ATTACKER} -> Attacker();

Router() =
    p1ToRouter?src.dest.msgtype.data1.data2.ct -> Forward(src, dest, msgtype, data1, data2, ct)
[]
    p2ToRouter?src.dest.msgtype.data1.data2.ct -> Forward(src, dest, msgtype, data1, data2, ct)
[]
    trustedToRouter?src.dest.msgtype.data1.data2.ct -> Forward(src, dest, msgtype, data1, data2, ct);
```

```
Forward(src, dest, msgtype, data1, data2, ct) =
    if (dest == P2IP)
        routerToP2!src.dest.msgtype.data1.data2.ct
        -> Router()
    else if (dest == P1IP)
        routerToP1!src.dest.msgtype.data1.data2.ct
        -> Router()
    else if (dest == TRUSTEDIP)
        routerToTrusted!src.dest.msgtype.data1.data2.ct
        -> Router()
    } else {
        Router()
    };
```



Message Encoding

| Msgtype: | Promise | Sign | Abort | Resolve1 | Resolve2 | Abort Confirmation | Resolve Confirmation |
|----------|-----------|-----------|-----------|-----------|-----------|-----------------------|-------------------------|
| field1: | Source IP | | | | | | |
| field2: | Dest IP | | | | | | |
| field3: | Msg Type | | | | | | |
| field4: | Promise | Signature | P1Promise | P1Sign | p2Sign | Confirmation | Confirmation |
| field5: | EMPTY | EMPTY | EMPTY | P2Promise | P1Promise | EMPTY | Auth |
| field6: | CONTRACT | | | | | | |



```
P1GenerateValues() =
```

p1GeneratePromise{p1Promise = call(Pow, P1PRIVATE, TRUSTPUBLIC) % TRUSTMOD}

- -> p1GenerateSignature{p1Sign = call(Pow, CONTRACT, P1PRIVATE) % P1MOD}
- -> p1SetStateSP{p1State = SENDPROMISE}
- -> P1();

P2GenerateValues() =

p2GeneratePromise{p2Promise = call(Pow,P2PRIVATE,TRUSTPUBLIC) % TRUSTMOD}

- -> p2GenerateSignature{p2Sign = call(Pow,CONTRACT,P2PRIVATE) % P2MOD}
- -> p2SetStateRP{p2State = RECPROMISE}
- -> P2();



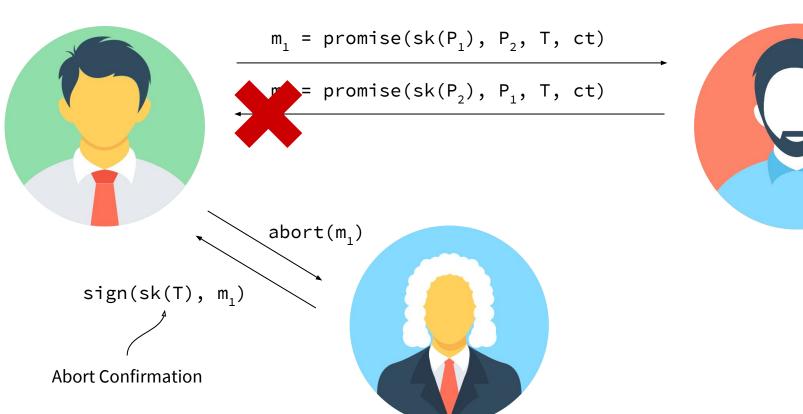
```
P1SendPromise() =
    p1ToRouter!P1IP.P2IP.PROMISETYPE.p1Promise.EMPTY.CONTRACT
    -> p1SetStateRP{p1State = RECPROMISE}
    -> P1()
    []
    p1ToRouter!P1IP.P2IP.PROMISETYPE.EMPTY.EMPTY.EMPTY
    -> p1Terminate{p1State = QUIT}
    -> P1();
```

P1ReceivePromise() = routerToP1?src.dest.msgtype.data1.data2.ct
-> P1ReceivePromiseAction(src, dest, msgtype, data1, data2, ct);

```
P2ReceivePromise() = routerToP2?src.dest.msgtype.data1.data2.ct
    -> P2ReceivePromiseAction(src, dest, msgtype, data1, data2, ct);
P2ReceivePromiseAction(src, dest, msgtype, data1, data2, ct) =
    if(msgtype != PROMISETYPE | ct != CONTRACT | data1 == EMPTY)
        p2SetStateE{p2State = END}
        -> P2()
    else
        p2StoreReceivedPromise{p2RecPromise = data1}
        -> p2SetStateSP{p2State = SENDPROMISE}
        -> P2()
```

```
P2ReceiveSign() = routerToP2?src.dest.msgtype.data1.data2.ct
-> P2ReceiveSignAction(src, dest, msgtype, data1, data2, ct);
```







```
P1ReceivePromiseAction(src, dest, msgtype, data1, data2, ct) =
    if (msgtype != PROMISETYPE || ct != CONTRACT || data1 == EMPTY)

{
    p1ToRouter!P1IP.TRUSTEDIP.ABORTTYPE.p1Promise.EMPTY.CONTRACT // send abort if invalid promise received
    -> routerToP1?f1.f2.f3.f4.f5.f6 // receive abort confirmation from trusted party
    -> P1ReceiveTrustedAbortConfirmation(f1, f2, f3, f4, f5, f6) // validate abort confirmation
    }
    else
    {
        p1StoreReceivedPromise{p1RecPromise = data1}
```

-> p1SetStateSS{p1State = SENDSIGN}

-> P1()



```
// Trusted Party
TrustedParty() = routerToTrusted?src.dest.msgtype.data1.data2.ct
    -> TrustedPartyAction(src, dest, msgtype, data1, data2, ct);
 TrustedPartyAction(src, dest, msgtype, data1, data2, ct) =
  **other if conditions omitted for brevity
 else if (msgtype == ABORTTYPE)
     setStatusAbort{trustedStatus = ABORTED}
     -> storeContract{trustedContract = ct}
     -> generateAbortConfirmation{confirmation = call(Pow, data1, TRUSTPRIVATE) % TRUSTMOD}
     -> trustedToRouter!TRUSTEDIP.src.ABORTCONFIRMATION.confirmation.EMPTY.CONTRACT
     -> TrustedParty()
```



```
P1ReceiveTrustedAbortConfirmation(src, dest, msgtype, data1, data2, ct) =
    if (msgtype == RESOLVECONFIRMATION | p1Promise!= call(Pow,data1,TRUSTPUBLIC)%TRUSTMOD)
        p1AbortFail{p1State = END}
        -> P1()
    else if (msgtype == ABORTCONFIRMATION)
        p1StoreAbortConfirmation{p1TrustedConfirmation = data1}
        -> p1SetStateE{p1State = END}
        -> P1()
    };
```



```
P1ReceivePromiseAction(src, dest, msgtype, data1, data2, ct) =
    if (msgtype != PROMISETYPE || ct != CONTRACT || data1 == EMPTY)

{
    p1ToRouter!P1IP.TRUSTEDIP.ABORTTYPE.p1Promise.EMPTY.CONTRACT // send abort if invalid promise received
    -> routerToP1?f1.f2.f3.f4.f5.f6 // receive abort confirmation from trusted party
    -> P1ReceiveTrustedAbortConfirmation(f1, f2, f3, f4, f5, f6) // validate abort confirmation
}
else

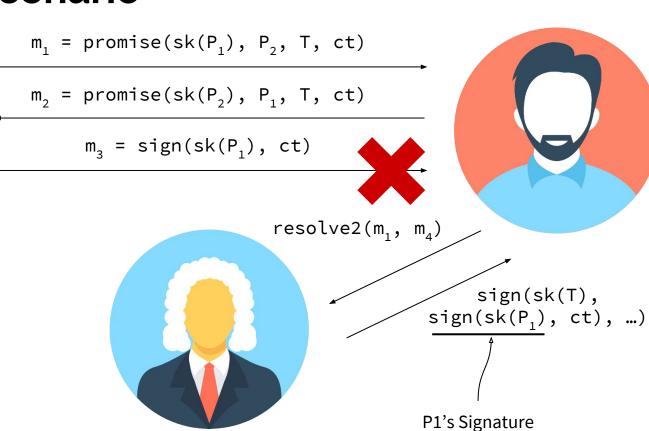
{
    p1StoreReceivedPromise{p1RecPromise = data1}
    -> p1SetStateSS{p1State = SENDSIGN}
```

-> P1()

```
P1SendSign() =
    p1ToRouter!P1IP.P2IP.SIGNTYPE.p1Sign.EMPTY.CONTRACT
    -> p1SetStateRS{p1State = RECSIGN}
    -> P1()
    p1ToRouter!P1IP.P2IP.SIGNTYPE.EMPTY.EMPTY.EMPTY
    -> p1Terminate{p1State = QUIT}
```

P1ReceiveSign() = routerToP1?src.dest.msgtype.data1.data2.ct
-> P1ReceiveSignAction(src, dest, msgtype, data1, data2, ct);





```
P2ReceiveSign() = routerToP2?src.dest.msgtype.data1.data2.ct
    -> P2ReceiveSignAction(src, dest, msgtype, data1, data2, ct);
P2ReceiveSignAction(src, dest, msgtype, data1, data2, ct) =
    if(msgtype != SIGNTYPE || ct != CONTRACT || data1 == EMPTY || call(Pow, data1, P1PUBLIC) % P1MOD != CONTRACT)
        p2ToRouter!P2IP.TRUSTEDIP.RESOLVE2TYPE.p2Sign.p2RecPromise.CONTRACT // send resolve2 if invalid sign received
        -> routerToP2?f1.f2.f3.f4.f5.f6 // receive resolve2 confirmation from trusted party
        -> P2ReceiveTrustedResolve2Confirmation(f1, f2, f3, f4, f5, f6) // validate resolve2 confirmation
    else
        p2StoreReceivedSign{p2RecSign = data1}
        -> p2SetStateSS{p2State = SENDSIGN}
```

-> P2()



```
// Trusted Party
TrustedParty() = routerToTrusted?src.dest.msgtype.data1.data2.ct
-> TrustedPartyAction(src, dest, msgtype, data1, data2, ct);
```



```
TrustedPartyAction(src, dest, msgtype, data1, data2, ct) =
```

**other if conditions omitted for brevity

```
else if(msgtype == RESOLVE2TYPE)
{
    setStatusResolved2{trustedStatus = RESOLVED2}
    -> storeContract{trustedContract = ct}
    -> generateP1Private{generatedPrivate = call(Pow, data2, TRUSTPRIVATE) % TRUSTMOD}
    -> generateP1Signature{generatedSignature = call(Pow, CONTRACT, generatedPrivate) % P1MOD}
    -> generateResolve2Confirmation{confirmation = call(Pow, generatedSignature, TRUSTPRIVATE) % TRUSTMOD}
    -> generateAuth{auth=call(Pow, data1, TRUSTPRIVATE) % TRUSTMOD}
    -> trustedToRouter!TRUSTEDIP.src.RESOLVECONFIRMATION.confirmation.auth.CONTRACT
    -> TrustedParty()
```

```
P2ReceiveTrustedResolve2Confirmation(src, dest, msgtype, data1, data2, ct) =
    if(msgtype == ABORTCONFIRMATION||call(Pow,data2,TRUSTPUBLIC)% TRUSTMOD != p2Sign)
        resolve2Fail{p2State = END}
        -> P2()
   else if(msgtype == RESOLVECONFIRMATION)
        p2StoreResolve2Confirmation{p2TrustedConfirmation = data1}
        -> p2GetP1Sign{p2RecSign = call(Pow, p2TrustedConfirmation, TRUSTPUBLIC) % TRUSTMOD}
        -> p2SetStateE{p2State = END}
        -> P2()
    };
```



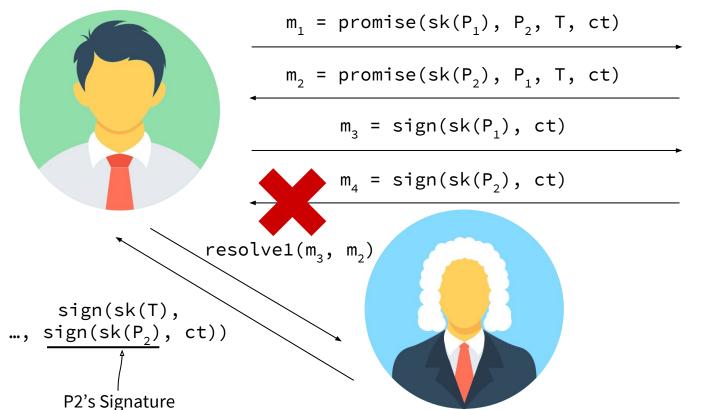
```
P2ReceiveSign() = routerToP2?src.dest.msgtype.data1.data2.ct
    -> P2ReceiveSignAction(src, dest, msgtype, data1, data2, ct);
P2ReceiveSignAction(src, dest, msgtype, data1, data2, ct) =
    if(msgtype != SIGNTYPE || ct != CONTRACT || data1 == EMPTY || call(Pow, data1, P1PUBLIC) % P1MOD != CONTRACT)
        p2ToRouter!P2IP.TRUSTEDIP.RESOLVE2TYPE.p2Sign.p2RecPromise.CONTRACT // send resolve2 if invalid sign received
        -> routerToP2?f1.f2.f3.f4.f5.f6 // receive resolve2 confirmation from trusted party
        -> P2ReceiveTrustedResolve2Confirmation(f1, f2, f3, f4, f5, f6) // validate resolve2 confirmation
    else
        p2StoreReceivedSign{p2RecSign = data1}
        -> p2SetStateSS{p2State = SENDSIGN}
```

-> P2()



```
P2SendSign() =
    p2ToRouter!P2IP.P1IP.SIGNTYPE.p2Sign.EMPTY.CONTRACT
    -> p2SetStateE{p2State = END}
    -> P2()
    []
```

- p2ToRouter!P2IP.P1IP.SIGNTYPE.EMPTY.EMPTY.EMPTY
- -> p2Terminate{p2State = QUIT}
- -> P2();







```
P1ReceiveSignAction(src, dest, msgtype, data1, data2, ct)=

if (msgtype != SIGNTYPE || ct != CONTRACT || data1 == EMPTY || call(Pow, data1, P2PUBLIC) % P2MOD != CONTRACT)

{

p1ToRouter!P1IP.TRUSTEDIP.RESOLVE1TYPE.p1Sign.p1RecPromise.CONTRACT // send resolve1 if invalid sign received
-> routerToP1?f1.f2.f3.f4.f5.f6 // receive resolve1 confirmation from trusted party
-> P1ReceiveTrustedResolve1Confirmation(f1, f2, f3, f4, f5, f6) // validate resolve1 confirmation
}

else

{

p1StoreReceivedSign{p1RecSign = data1}
-> p1SetStateE{p1State = END}
-> P1()
```

```
// Trusted Party
TrustedParty() = routerToTrusted?src.dest.msgtype.data1.data2.ct
     -> TrustedPartyAction(src, dest, msgtype, data1, data2, ct);
TrustedPartyAction(src, dest, msgtype, data1, data2, ct) =
 **other if conditions omitted for brevity
else if(msgtype == RESOLVE1TYPE)
    setStatusResolved1{trustedStatus = RESOLVED1}
    -> storeContract{trustedContract = ct}
    -> generateP2Private{generatedPrivate=call(Pow,data2,TRUSTPRIVATE)%TRUSTMOD}
    -> generateP2Signature{generatedSignature=call(Pow,CONTRACT,generatedPrivate)%P2MOD}
    -> generateResolved1Confirmation{confirmation=call(Pow,generatedSignature,TRUSTPRIVATE)%TRUSTMOD}
    -> generateAuth{auth=call(Pow, data1, TRUSTPRIVATE) % TRUSTMOD}
    -> trustedToRouter!TRUSTEDIP.src.RESOLVECONFIRMATION.confirmation.auth.CONTRACT
    -> TrustedParty()
```

};

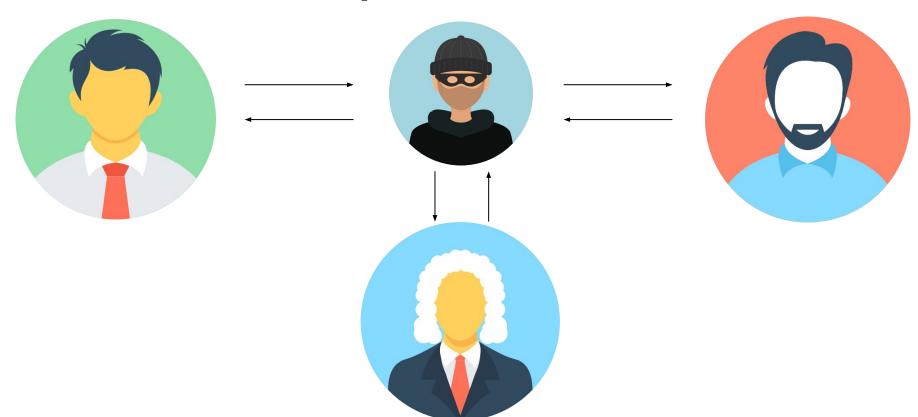


```
P1ReceiveTrustedResolve1Confirmation(src, dest, msgtype, data1, data2, ct) =
    if (msgtype == ABORTCONFIRMATION||call(Pow,data2,TRUSTPUBLIC)% TRUSTMOD != p1Sign)
        resolve1Fail{p1State = END}
        -> P1()
    else if (msgtype == RESOLVECONFIRMATION)
        p1StoreResolve1Confirmation{p1TrustedConfirmation = data1}
        -> p1GetP2Sign{p1RecSign = call(Pow, p1TrustedConfirmation, TRUSTPUBLIC) % TRUSTMOD}
        -> p1SetStateE{p1State = END}
        -> P1()
    };
```

Attacker

All the messages are sent over public network. That is, there is an attacker controlling the network, and can block, inject, alter and read messages over the network.

Attacker(): A Compromised Router



```
// Router and Attacker
RouterSelector() =
    secureRouter{routerState = SECURE} -> Router()
    attacker{routerState = ATTACKER} -> Attacker();
Router() =
    p1ToRouter?src.dest.msgtype.data1.data2.ct -> Forward(src, dest, msgtype, data1, data2, ct)
    p2ToRouter?src.dest.msgtype.data1.data2.ct -> Forward(src, dest, msgtype, data1, data2, ct)
    trustedToRouter?src.dest.msgtype.data1.data2.ct -> Forward(src, dest, msgtype, data1, data2, ct);
Attacker() =
    p1ToRouter?src.dest.msgtype.data1.data2.ct -> AttackerForward(src, dest, msgtype, data1, data2, ct)
   p2ToRouter?src.dest.msgtype.data1.data2.ct -> AttackerForward(src, dest, msgtype, data1, data2, ct)
    trustedToRouter?src.dest.msgtype.data1.data2.ct -> AttackerForward(src, dest, msgtype, data1, data2, ct);
```

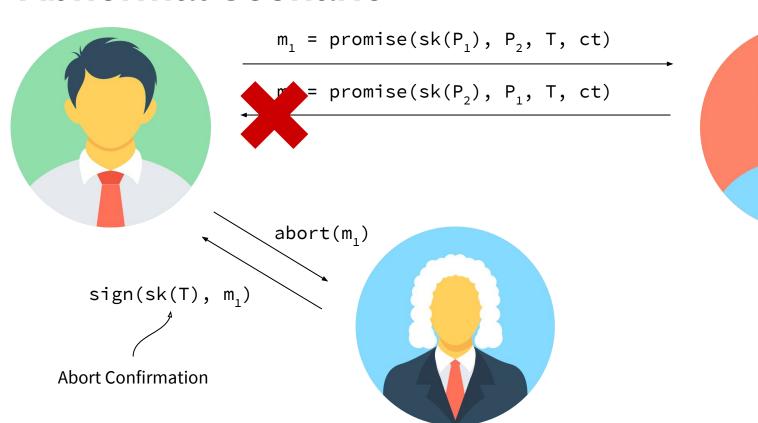
```
AttackerForward(src, dest, msgtype, data1, data2, ct) =
   if(dest == P2IP)
       routerToP2!src.dest.msgtype.data1.data2.ct
       -> Attacker()
       routerToP2!GARBAGE.GARBAGE.GARBAGE.GARBAGE.GARBAGE
       -> Attacker()
   else if (dest == P1IP)
       routerToP1!src.dest.msgtype.data1.data2.ct
       -> Attacker()
       routerToP1!GARBAGE.GARBAGE.GARBAGE.GARBAGE.GARBAGE
       -> Attacker()
   else if(dest == TRUSTEDIP)
       routerToTrusted!src.dest.msgtype.data1.data2.ct
       -> Attacker()
       routerToTrusted!GARBAGE.GARBAGE.GARBAGE.GARBAGE.GARBAGE
       -> Attacker()
    } else {
       Attacker()
   };
```

Full System

```
System() = P1() || | P2() || TrustedParty() || RouterSelector();
```

Demo

Abnormal Scenario



Assertions

Implementation Checking

```
#define noattacker (routerState == SECURE);
#define withattacker (routerState == ATTACKER);

/***** Implementation Checking *****/
// 1. P2 only sends promise when it receives valid P1 promise
#define p2receivesbadpromise (p2RecPromise != p1Promise && p2State != QUIT);
#define p2sendpromise (p2State == RECSIGN);
#assert System |= []([]p2receivesbadpromise && noattacker -> !p2sendpromise);

// 2. P1 only sends signature when it receives valid P2 Promise
#define p1receivesbadpromise (p1RecPromise != p2Promise && p1State != QUIT);
#define p1sendsign (p1State == RECSIGN);
#assert System |= []([]p1receivesbadpromise && noattacker -> !p1sendsign);
```

Should pass if our implementation of the protocol is correct

Verification of Protocol

```
/***** Protocol Verification *****/
// 3. Both processes eventually end or quit
#define processesend (p1State == END | p1State == QUIT) && (p2State == QUIT | p2State == END);
#assert System reaches processesend;
// 4. If P1 sends signature, both parties will eventually get signature
#define bothreceivesign (p1RecSign == p2Sign && p2RecSign == p1Sign);
#assert System |= [](p1sendsign && noattacker -> <>bothreceivesign);
// 5. If P1 receives P2's promise and doesn't quit, it will get P2's signature
     Covers both success scenario and resolvel
#define p1receivep2promise (p1RecPromise == p2Promise && p1State != QUIT);
#define p1receivep2sign (p1RecSign == p2Sign);
#assert System |= []([]p1receivep2promise && noattacker -> <>p1receivep2sign);
// 6. If P2 receives P1's promise and doesn't quit, it will get P1's signature
     Covers both success scenario and resolve2
#define p2receivep1promise (p2State != QUIT && p2RecPromise == p1Promise);
#define p2receivep1sign (p2RecSign == p1Sign);
#assert System |= []([]p2receivep1promise && noattacker -> <>p2receivep1sign);
```

Verification of Protocol

```
// 7. If trusted party has once aborted, neither party will receive signature
#define trustedstatusaborted (trustedStatus == ABORTED);
#assert System |= [](trustedstatusaborted -> []!bothreceivesign);

// 8. If trusted party has once resolved, he will not entertain aborts
#define trustedstatusresolve (trustedStatus == RESOLVED1 || trustedStatus == RESOLVED2);
#define trustedstatusabort (trustedStatus == ABORTED);
#define abortconfirmation (p1TrustedConfirmation == call(Pow, p1Promise, TRUSTPRIVATE) % TRUSTMOD);
#assert System |= [](trustedstatusresolve -> []!abortconfirmation);

// 9. After trusted party has aborted, P1 will eventually receive abort confirmation
#assert System |= [](trustedstatusabort && noattacker -> <>abortconfirmation);
```

Should pass if protocol works as described

Verification of Protocol (with Attacker)

```
/***** Protocol Verification with Attacker *****/
// 10. Assertion 4 with attacker
#assert System |= [](p1sendsign && withattacker -> <>bothreceivesign);

// 11. 12. Assertion 5 and 6 with attacker
#assert System |= []([]p1receivep2promise && withattacker -> <>p1receivep2sign);
#assert System |= []([]p2receivep1promise && withattacker -> <>p2receivep1sign);
```

Should pass if protocol works as described even with an attacker

Limitations

- 1. RSA Signing
- 2. Attacker Behaviour