



第二章 深度前馈网络

深度前馈网络

主要内容

- 01 CNN反向传播
- 02 深度前馈网络
- 03 TensorFlow

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 $z^{(l+1)} = W^{(l)}a^{(l)} + b^{(l)}$ $a^{(l+1)} = f(z^{(l+1)})$

CNN反向传播

CNN反向传播

全链接: 前向传播与反向回馈

Square Euclidean Distance (regression)

$$J_{i} = \frac{1}{2} \sum_{i=1}^{N} (y_{i} - \hat{y}_{i})^{2}$$

$$J(W, b; x, y) = \frac{1}{2} \|h_{W, b}(x) - y\|^2$$

$$= \left[\frac{1}{m}\sum_{i=1}^{m}\left(\frac{1}{2}\left\|h_{W,b}(x^{(i)}) - y^{(i)}\right\|^{2}\right)\right] + \frac{\lambda}{2}\sum_{l=1}^{n_{l}-1}\sum_{i=1}^{s_{l}}\sum_{j=1}^{s_{l+1}}\left(W_{ji}^{(l)}\right)^{2}$$

更新迭代:

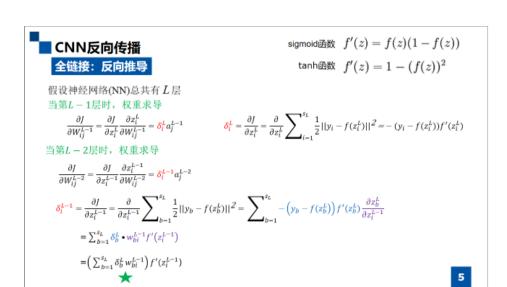
更新迭代:
$$W_{ij}^{(l)} = W_{ij}^{(l)} - \alpha \frac{\partial}{\partial W_{ij}^{(l)}} J(W,b) \qquad \qquad \frac{\partial}{\partial W_{ij}^{(l)}} J(W,b) = \left[\frac{1}{m} \sum_{i=1}^{m} \frac{\partial}{\partial W_{ij}^{(l)}} J(W,b;x^{(i)},y^{(i)}) \right] + \lambda W_{ij}^{(l)}$$

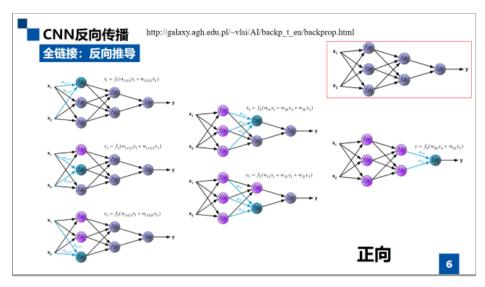
$$b_{i}^{(l)} = b_{i}^{(l)} - \alpha \frac{\partial}{\partial b_{i}^{(l)}} J(W,b) \qquad \qquad \frac{\partial}{\partial b_{i}^{(l)}} J(W,b) = \frac{1}{m} \sum_{i=1}^{m} \frac{\partial}{\partial b_{i}^{(l)}} J(W,b;x^{(i)},y^{(i)})$$

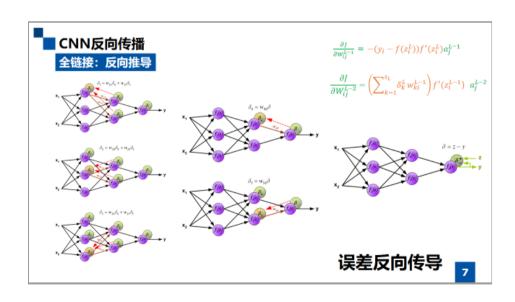
$$\frac{\partial}{\partial b_i^{(l)}} J(W, b) = \frac{1}{m} \sum_{i=1}^m \frac{\partial}{\partial b_i^{(l)}} J(W, b; x^{(i)}, y^{(i)})$$

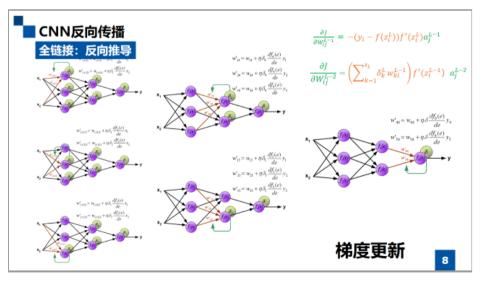
$$b_i^{(l)} = b_i^{(l)} - \alpha \frac{\partial}{\partial b_i^{(l)}} J(W, b)$$

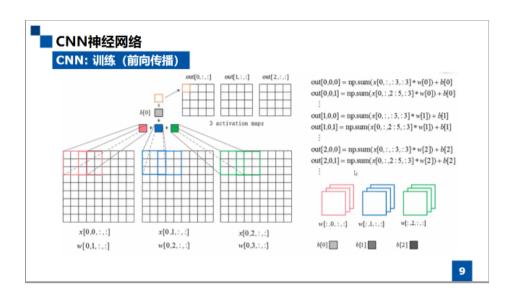
$$rac{\partial}{\partial b_i^{(l)}}J(W,b) = rac{1}{m}\sum_{i=1}^mrac{\partial}{\partial b_i^{(l)}}J(W,b;x^{(i)},y^{(i)})$$

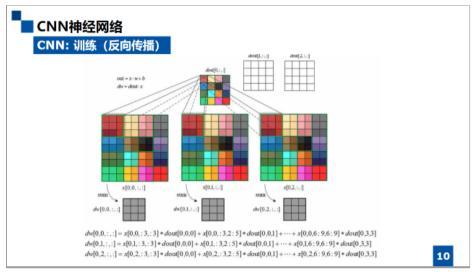


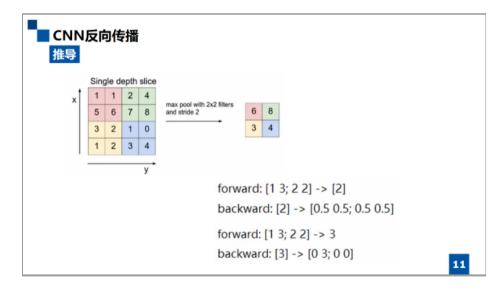
















深度前馈网络

通用近似定理

定理 4.1 - 通用近似定理 (Universal Approximation Theorem) [Cybenko, 1989, Hornik et al., 1989]: 令 φ(·) 是一个非常数、 有界、单调递增的连续函数, I_d 是一个d维的单位超立方体 $[0,1]^d$, $C(\mathcal{I}_d)$ 是定义在 \mathcal{I}_d 上的连续函数集合。对于任何一个函数 $f \in$ $C(\mathcal{I}_d)$,存在一个整数m,和一组实数 $v_i,b_i \in \mathbb{R}$ 以及实数向量 $\mathbf{w}_i \in \mathbb{R}^d$, $i = 1, \dots, m$, 以至于我们可以定义函数

$$F(\mathbf{x}) = \sum_{i=1}^{m} v_i \varphi(\mathbf{w}_i^T \mathbf{x} + b_i), \quad (4.33)$$

作为函数f的近似实现,即

$$|F(\mathbf{x}) - f(\mathbf{x})| < \epsilon, \forall \mathbf{x} \in \mathcal{I}_d.$$
 (4.34)

其中 $\epsilon > 0$ 是一个很小的正数。

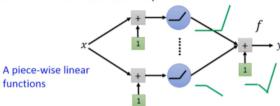
根据通用近似定理,对于具有线性输出层和至少一个使用"挤压"性 质的激活函数的隐藏层组成的前馈神经网络、只要其隐藏层神经元的 数量足够,它可以以任意的精度来近似任何从一个定义在实数空间中 的有界闭集函数。

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■ 深度前馈网络

通用近似定理

· Given a shallow network structure with one hidden layer with ReLU activation and linear output



Given a L-Lipschitz function f*

functions

How many neurons are needed to approximate f*?

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 $\max_{0 \le x \le 1} |f(x) - f^*(x)| \le \varepsilon$

 $\int_{0}^{1} |f(x) - f^{*}(x)|^{2} dx \le \epsilon$

深度前馈网络

通用近似定理

- Given a L-Lipschitz function f*
 - How many neurons are needed to approximate f*?

L-Lipschitz Function (smooth)

$$||f(x_1) - f(x_2)|| \le L||x_1 - x_2||$$
Output Input

change change

L=1 for "1 – Lipschitz"



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深度前馈网络

通用近似定理

- Given a L-Lipschitz function f*
 - How many neurons are needed to approximate f*?

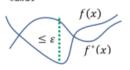
$$f \in N(K)$$
 The function space defined by the network with K neurons.

Given a small number $\varepsilon > 0$

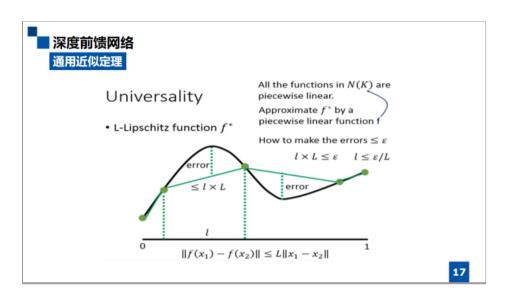
What is the number of K such that

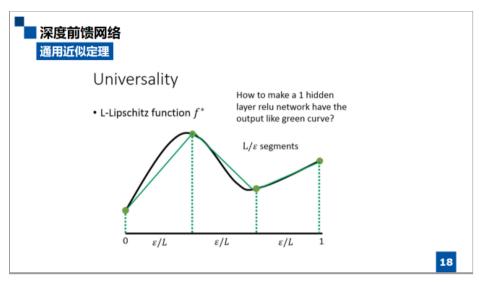
Exist
$$f \in N(K)$$
, $\max_{0 \le x \le 1} |f(x) - f^*(x)| \le \varepsilon$

The difference between f(x)and $f^*(x)$ is smaller than ε .

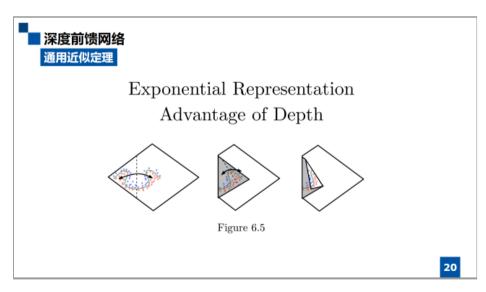


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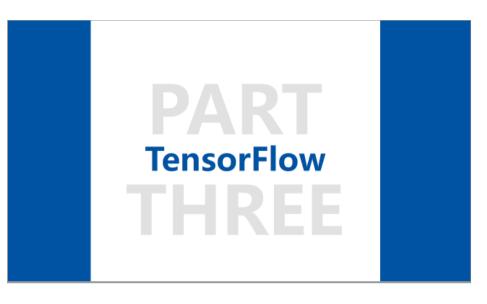




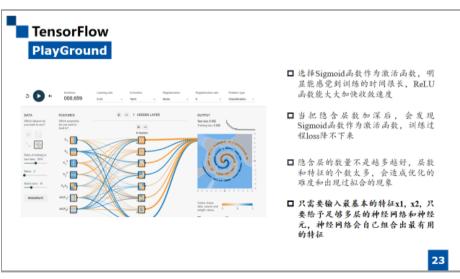


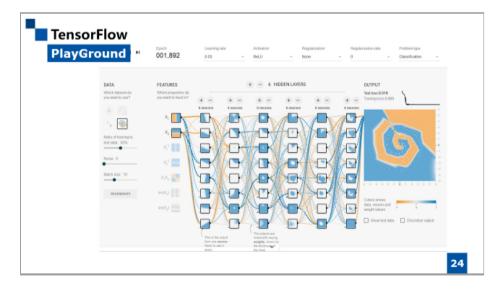


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安装

1. Windows CPU版:

环境: python 3.5, 3.6(64位)

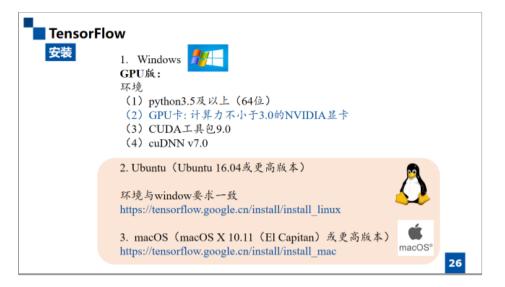
本地pip安装:

pip3 install --upgrade tensorflow

Anaconda安装:

- (1) 创建一个名为tensorflow的conda环境 conda create -n tensorflow pip python = 3.5
- (2) 激活conda activate tensorflow环境
- (3) 在conda环境中安装TensorFlow pip install --ignore-installed --upgrade tensorflow

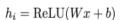
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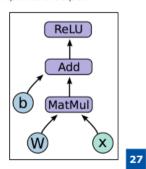




Basic concepts

- · Express a numeric computation as a graph.
- · Graph nodes are operations which have any number of inputs and outputs
- · Graph edges are tensors which flow between nodes



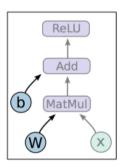




 $h_i = \text{ReLU}(Wx + b)$

Variables are 0-ary stateful nodes which output their current value. (State is retained across multiple executions of a graph.)

(parameters, gradient stores, eligibility traces, ...)



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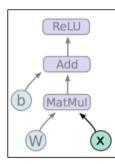
TensorFlow

Basic concepts

$$h_i = \text{ReLU}(Wx + b)$$

Placeholders are 0-ary nodes whose value is fed in at execution time.

(inputs, variable learning rates, ...)



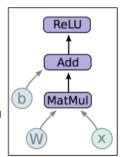
TensorFlow

Basic concepts

$$h_i = \text{ReLU}(Wx + b)$$

Mathematical operations:

MatMul: Multiply two matrix values. Add: Add elementwise (with broadcasting). ReLU: Activate with elementwise rectified linear function.



TensorFlow

Basic concepts

- 1.Create model weights, includina initialization
- $a.W \sim Uniform(-1, 1); b = 0$ 2.Create input placeholder x
- a.m * 784 input matrix 3.Create computation graph

 $h_i = \text{ReLU}(Wx + b)$

- import tensorflow as tf
- b = tf.Variable(tf.zeros((100,))) W = tf.Variable(tf.random_uniform((784, 100), -1, 1))
- 2 x = tf.placeholder(tf.float32, (None, 784)) h_i = tf.nn.relu(tf.matmul(x, W) + b) 3

Just Run It!

sess = tf.Session() sess.run(tf.initialize_all_variables()) sess.run(h i, {x: np.random.random(64, 784)})

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TensorFlow

Basic concepts

1.Build a graph

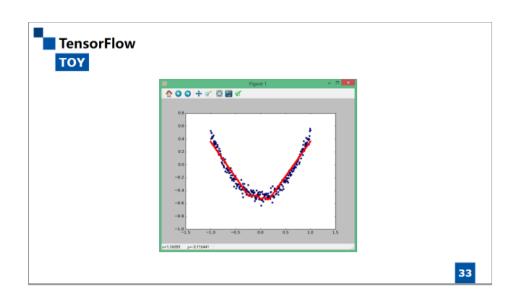
- a. Graph contains parameter specifications, model architecture, optimization process, ...
- b. Somewhere between 5 and 5000 lines

2.Initialize a session

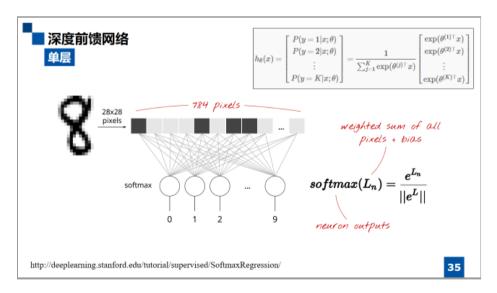
3.Fetch and feed data with Session.run

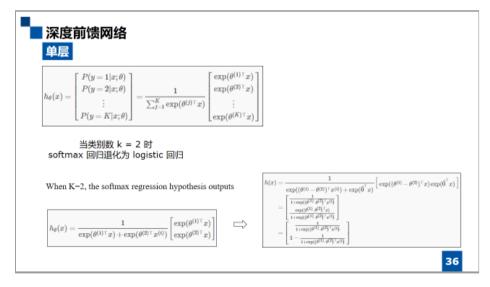
- a. Compilation, optimization, etc. happens at this step
- you probably won't notice

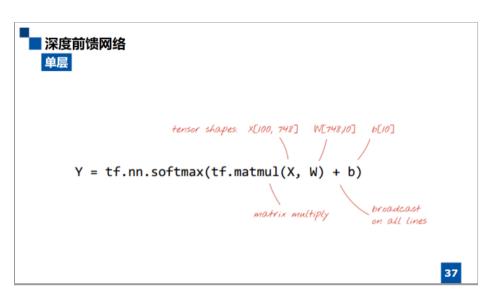
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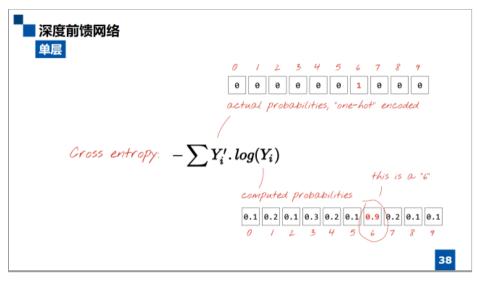












```
import tensorflow as tf

X = tf.placeholder(tf.float32, [None, 28, 28, 1])

W = tf.Variable(tf.zeros([784, 10]))

b = tf.Variable(tf.zeros([10]))

Z8 x 28 grayscale images

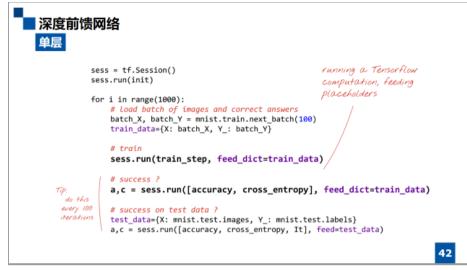
init = tf.initialize_all_variables()

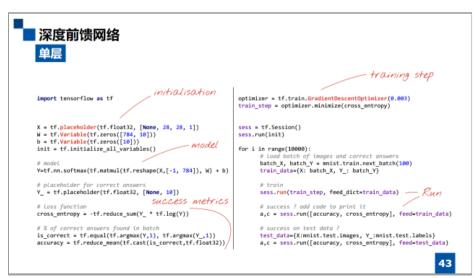
Training = computing variables W and b
```

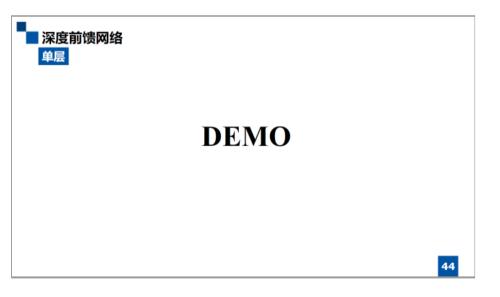
```
# model
Y = tf.nn.softmax(tf.matmul(tf.reshape(X, [-1, 784]), W) + b)
# placeholder for correct answers
Y_ = tf.placeholder(tf.float32, [None, 10])
# loss function
cross_entropy = -tf.reduce_sum(Y_ * tf.log(Y))
# % of correct answers found in batch
is_correct = tf.equal(tf.argmax(Y,1), tf.argmax(Y_,1))
accuracy = tf.reduce_mean(tf.cast(is_correct, tf.float32))
```

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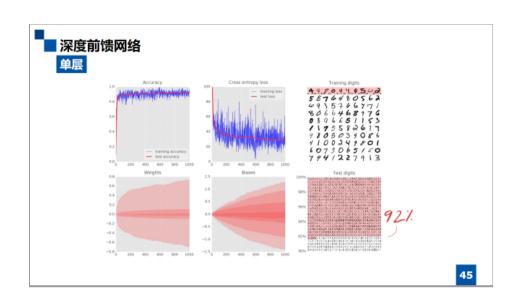


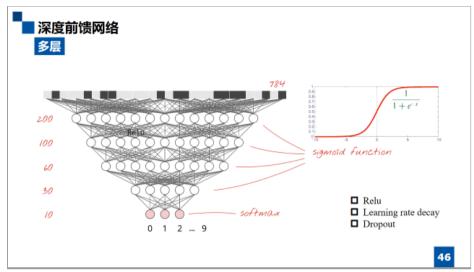


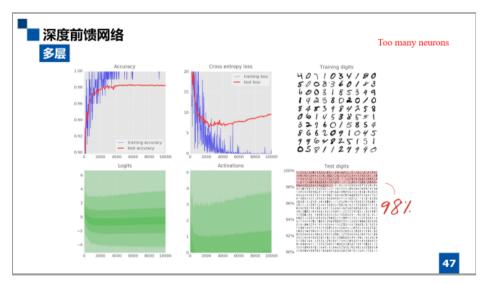


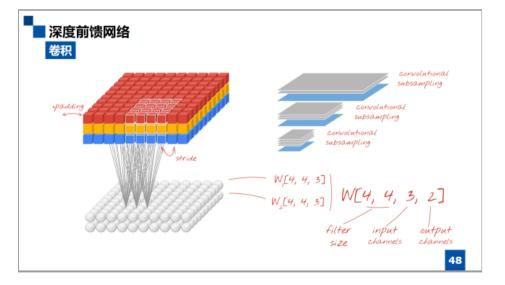


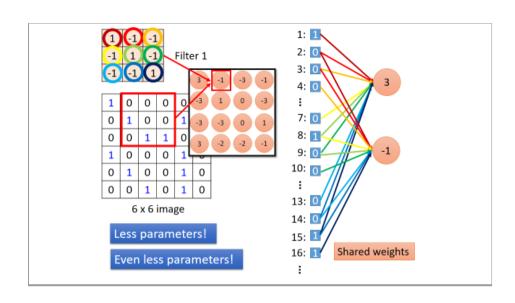
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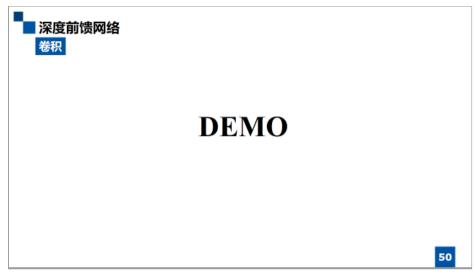


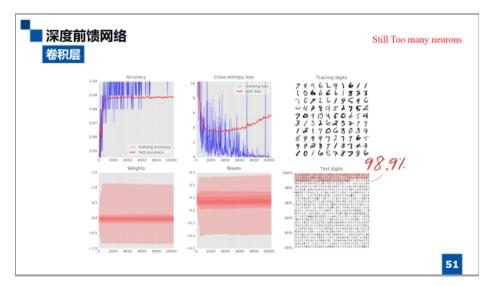


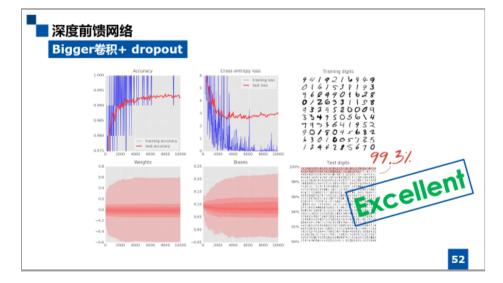
















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