Problems 6: Reaching definitions

In the following code (quadruples), state which definition(s) reach line i and which definitions reach line i.

First step (gen and kill sets):

			gen	kill
1:	c = 6;		1	13
2:	d = 7;		2	14
3 :	e = 1;		3	
4:	i = 100;		4	15
5 :	if (i>0) goto 17;			
6 :	t1 = i*4;	(<i>i</i>)	6	
7:	t2 = a+t1;		7	
8:	t3 = M[t2];		8	
9:	t4 = t3-c;		9	
10:	M[t2] = t4;			
11:	b = 5;		11	
12:	t5 = b*4;		12	
13:	c = M[t5];		13	1
14:	d = b-e;	(<i>ii</i>)	14	2
15 :	i = i-1;		15	4
16:	goto 5;			
17:	<pre>write(d);</pre>			

 $pred(5) = \{4,16\}, pred(17) = \{5\}$

Find the in and out sets:

in				out
	1:	c = 6;		1
1	2:	d = 7;		1,2
1,2	3 :	e = 1;		1,2,3
1,2,3	4:	i = 100;		1,2,3,4
1,2,3,4,6,7,8,9,11,12,13,14,	155:	if (i>0) goto	17;	1,2,3,4,6,7,8,9,11,12,13,14,15
1,2,3,4,6,7,8,9,11,12,13,14,	156:	t1 = i*4;	(<i>i</i>)	1,2,3,4,6
1,2,3,4,6	7:	t2 = a+t1;		1,2,3,4,6,7
1,2,3,4,6,7	8:	t3 = M[t2];		1,2,3,4,6,7,8
1,2,3,4,6,7,8	9:	t4 = t3-c;		1,2,3,4,6,7,8,9
1,2,3,4,6,7,8,9	10:	M[t2] = t4;		1,2,3,4,6,7,8,9
1,2,3,4,6,7,8,9	11:	b = 5;		1,2,3,4,6,7,8,9,11
1,2,3,4,6,7,8,9,11	12:	t5 = b*4;		1,2,3,4,6,7,8,9,11,12
1,2,3,4,6,7,8,9,11,12	13:	c = M[t5];		2,3,4,6,7,8,9,11,12,13
2,3,4,6,7,8,9,11,12,13	14:	d = b-e;	(<i>ii</i>)	3,4,6,7,8,9,11,12,13,14
3,4,6,7,8,9,11,12,13,14	15:	i = i-1;		3,6,7,8,9,11,12,13,14,15
3,6,7,8,9,11,12,13,14,15	16:	goto 5;		3,6,7,8,9,11,12,13,14,15
1,2,3,4	17:	write(d);		1,2,3,4

To save time (in exam?), look only at the variables that are used in lines (i) and (ii), $\{i, b, e\}$, and ignore definitions of other variables:

in				out
	1:	c = 6;		
	2:	d = 7;		
	3 :	e = 1;		3
3	4:	i = 100;		3,4
3,4,11,15	5 :	if (i>0) goto 17;	;	3,4,11,15
3,4,11,15	6 :	t1 = i*4;	(i)	3,4,11,15
3,4,11,15	7:	t2 = a+t1;		3,4,11,15
3,4,11,15	8:	t3 = M[t2];		3,4,11,15
3,4,11,15	9:	t4 = t3-c;		3,4,11,15
3,4,11,15	10:	M[t2] = t4;		3,4,11,15
3,4,11,15	11:	b = 5;		3,4,11,15
3,4,11,15	12:	t5 = b*4;		3,4,11,15
3,4,11,15	13:	c = M[t5];		3,4,11,15
3,4,11,15	14:	d = b-e;	(<i>ii</i>)	3,4,11,15
3,4,11,15	15 :	i = i-1;		3,11,15
3,11,15	16:	goto 5;		3,11,15
3,4	17:	<pre>write(d);</pre>		3,4