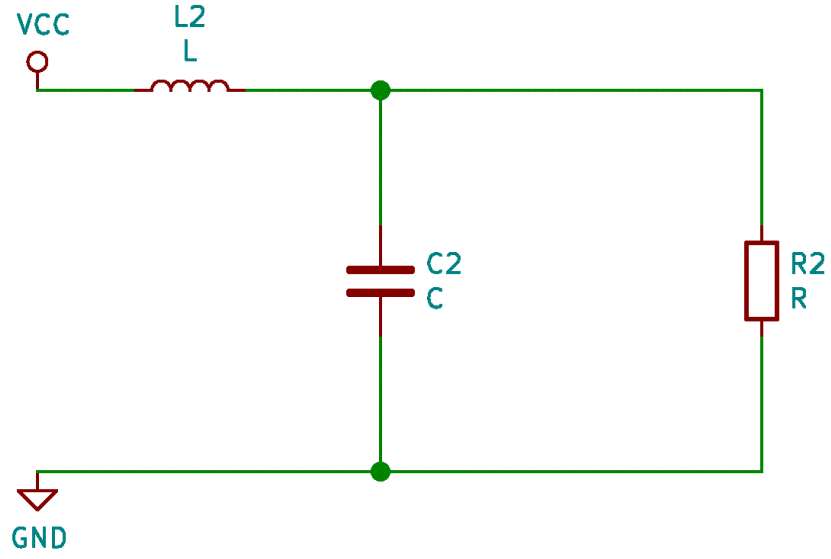


on phase:



$$V_{in} = V_L + V_o$$

$$V_{in} = L \frac{dI_L}{dt} + V_o \quad (1)$$

where $V_o = V_c = V_r$

$$I_L = I_c + I_r$$

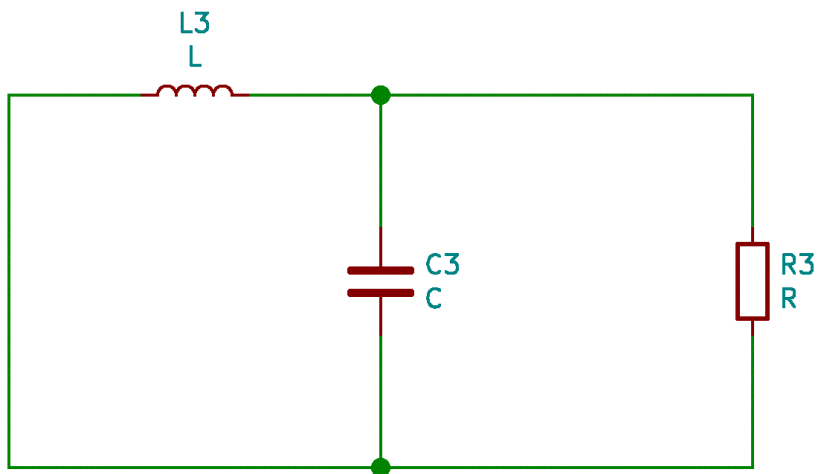
$$I_L = C \frac{dV_o}{dt} + \frac{V_o}{R} \quad (2)$$

subst 2 in 1

$$V_{in} = L \frac{d}{dt} \left(C \frac{dV_o}{dt} + \frac{V_o}{R} \right) + V_o$$

$$V_{in} = LC \frac{d^2 V_o}{dt^2} + \frac{L}{R} \frac{dV_o}{dt} + V_o \quad (3)$$

off phase



$$\begin{aligned} V_L &= V_o \\ L \frac{di_L}{dt} &= V_o \end{aligned} \tag{4}$$

$$\begin{aligned} I_L &= I_c + I_r \\ I_L &= C \frac{dV_o}{dt} + \frac{V_o}{R} \end{aligned} \tag{5}$$

subst 5 in 4

$$\begin{aligned} L \frac{d}{dt} \left(C \frac{dV_o}{dt} + \frac{V_o}{R} \right) &= V_o \\ LC \frac{d^2 V_o}{dt^2} + \frac{L}{R} \frac{dV_o}{dt} &= V_o \\ LC \frac{d^2 V_o}{dt^2} + \frac{L}{R} \frac{dV_o}{dt} - V_o &= 0 \end{aligned} \tag{6}$$