

- 10 pairs of random massless leptons
4 momenta are {vec p, E}

In[812]:= **pairs**

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Out[812]= {{ {21.691, -12.223, -7.6778, 26.055}, {30.149, 27.176, -27.178, 48.848}},
  {{-8.1957, -7.3859, -3.0376, 11.443}, {19.244, -7.2294, 28.897, 35.463}},
  {{2.8428, -2.3513, 0.13646, 3.6917}, {7.6949, 18.795, 25.084, 32.275}},
  {{28.192, 0.74774, 4.8632, 28.618}, {8.0718, 1.5359, 0.037766, 8.2167}},
  {{6.898, -19.743, -36.677, 42.221}, {1.336, 1.3785, -0.93809, 2.1367}},
  {{-26.931, -0.062688, 21.151, 34.244}, {1.5524, 4.9809, 9.0425, 10.44}},
  {{9.9862, -15.769, -11.921, 22.147}, {8.2757, 1.9508, 5.1564, 9.9439}},
  {{-6.3636, -6.1292, 4.7521, 10.032}, {-1.4069, -1.5201, -3.0108, 3.6544}},
  {{-10.007, 18.829, 6.3049, 22.236}, {2.4327, -2.479, 4.074, 5.3536}},
  {{32.456, -24.36, 7.6178, 41.29}, {-17.126, 1.8017, 16.718, 24.001}} }
```

- the invariant mass of the first particle listed

In[824]:= **dot[pairs[[1, 1]], pairs[[1, 1]]]**

Out[824]= 2.2737×10^{-13}

- sums Q for each pair

```
Out[813]= {{ {51.84, 14.953, -34.856, 74.903}, {11.048, -14.615, 25.859, 46.906},
  {10.538, 16.444, 25.22, 35.967}, {36.264, 2.2837, 4.901, 36.835},
  {8.234, -18.365, -37.615, 44.357}, {-25.379, 4.9182, 30.194, 44.684},
  {18.262, -13.818, -6.7641, 32.091}, {-7.7705, -7.6493, 1.7414, 13.687},
  {-7.574, 16.35, 10.379, 27.589}, {15.33, -22.558, 24.336, 65.291}} }
```

- normalized hatZ 4-vectors for each pair
The formula is $\text{hatZ} = Z^\mu / \sqrt{-Z^\mu Z_\mu}$

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Table[ qnow = pairs[[p, 1]] + pairs[[p, 2]] ;  
  hatz[qnow], {p, Length[pairs]}]
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```
Out[814]= {{ {0., 0., 1.1298, -0.52574}, {0., 0., 1.1986, 0.66079},
  {0., 0., 1.4026, 0.98354}, {0., 0., 1.009, 0.13425}, {0., 0., 1.8868, -1.6},
  {0., 0., 1.3566, 0.91666}, {0., 0., 1.023, -0.21563},
  {0., 0., 1.0082, 0.12827}, {0., 0., 1.0793, 0.40602}, {0., 0., 1.0777, 0.40167}} }
```

- Check every hatZ is 4D orthogonal to every Q
and every one is normalized

```
Out[816]= {0.,  $3.5527 \times 10^{-15}$ , 0.,  $8.8818 \times 10^{-16}$ , 0., 0.,  $-8.8818 \times 10^{-16}$ ,  $-8.8818 \times 10^{-16}$ ,  $1.7764 \times 10^{-15}$ , 0.}
```

```
Out[817]= {-1., -1., -1., -1., -1., -1., -1., -1., -1., -1.}
```

- The lepton momentum differences $\text{diff}=(k_1-k_2)/2$ for each pair

```
Out[818]= {{ {-4.2286, -19.7, 9.75, -11.396}, {-13.72, -0.078233, -15.967, -12.01},
  {-2.4261, -10.573, -12.474, -14.292}, {10.06, -0.3941, 2.4127, 10.201},
  {2.781, -10.561, -17.869, 20.042}, {-14.242, -2.5218, 6.0544, 11.902},
  {0.85527, -8.8599, -8.5385, 6.1015}, {-2.4783, -2.3045, 3.8815, 3.1889},
  {-6.2197, 10.654, 1.1155, 8.4411}, {24.791, -13.081, -4.5502, 8.6444}} }
```

- res= cos theta = hat difference dot hat z
hat difference = $\text{diff}^\mu / \sqrt{-\text{diff}_\mu \text{diff}^\mu}$

```
Out[819]= {-0.26078, 0.6479, 0.414, -0.60219, 0.2714, 0.26425, 0.69212, -0.86663, 0.24525, 0.30964}
```

- here's a histogram of 1000 such $\cos \theta$'s
the error bars are root-n points in the bin

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In[798]:= histo[.1, res]
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