REFORMULATE AS A TRANSITION MATRIX

$$\frac{dA}{dH} = -k_1 A + k_2 B$$

$$\frac{dB}{dH} = k_1 A - k_2 B$$

IMAGINE ONE MOLECULE OF "A"

$$P(A \rightarrow B; \Delta t) = k, \Delta t \leftarrow CHOSE SMALL Dt (OTHERUSE P>1!) RULE OF THUMBP(A \rightarrow A; \Delta t) = (1-P_{A \rightarrow B}) RATE.$$

$$P(8\rightarrow A; \Delta t) = k_2 \Delta t$$

$$A(t+at) = A \cdot P_{AA} + B \cdot P_{GA}$$

 $B(t+at) = A \cdot P_{AB} + B \cdot P_{BB}$

EXAMPLE WITH REAL NUMBERS:

$$A(t=0) = 5 \qquad P_{AB} = 100 \times 0.001 = 0.7$$

$$A \rightleftharpoons B \qquad E_1 = 100 \text{ s}^{-1}$$

$$E_2 \qquad P_{BA} = 10 \times 0.001 = 0.01$$

$$P_{BB} = 1-P_{BA} = 0.99$$

$$At = 0.001 \text{ s}$$

$$P_{BB} = 1-P_{BA} = 0.99$$

$$\begin{bmatrix}
0.9 & 0.01 \\
0.1 & 0.99
\end{bmatrix}
\begin{bmatrix}
5 \\
0.1
\end{bmatrix}
\rightarrow 5(0.9) + 0(0.01)
= 4.5
= 0.5 (ONSERVATION 5.0 CONSERVATION 5.0$$

$$\begin{bmatrix}
0.9 & 0.01 \\
6.1 & 0.99
\end{bmatrix}
\begin{bmatrix}
4.5 \\
0.5
\end{bmatrix}
\rightarrow
\begin{bmatrix}
4.5(0.9) + 0.5(0.01) \\
4.5(0.1) + 0.5(0.99)
\end{bmatrix}
=
\begin{bmatrix}
4.055 \\
0.945 \\
5.000
\end{bmatrix}$$

FIND Be (B) AT EQUILBRIUM).

 $\frac{Be}{Keq} + Be = 5 \qquad Ae = Be/Keq$ $Be(\bot + 1) = 5$

Be = 5 × Kea +++ Kea

Ae+Be=5; Keg=Be/Ae

 $= 5 \frac{ke_{q}}{1+ke_{q}}$ = 5.10 = 4.5454 = Re 10+1

WHAT DOES THIS GO TO OVER LONG TIMES?

- WHAT VALUE FOR (B) YIELDS Be WHEN FED INTO MARKOV MATRIX?

$$A \cdot P_{AA} + B \cdot P_{BA} = Ae$$

$$A \cdot P_{AB} + B \cdot P_{BB} = Be$$

$$A \cdot P_{AB} = Be - B \cdot P_{BB}$$

$$A = \frac{Be}{P_{AB}} - \frac{B \cdot P_{BB}}{P_{AB}}$$

$$A \cdot P_{AA} + B \cdot P_{BA} = Ae$$

$$\frac{Be}{P_{AB}} - \frac{B \cdot P_{BB}}{P_{AB}} P_{AA} + B \cdot P_{BA} = Ae$$

$$B(P_{BA} - P_{BB} \cdot P_{AA}) = A_e - B_e(P_{AA}/P_{AB})$$

$$B = \frac{Ae - Be(P_{AA}/P_{AB})}{P_{BA} - \frac{P_{BB} \cdot P_{AA}}{P_{AB}}} = 4.5454 \neq Be!$$

WHEN APPLIED MANY TIMES MATRIX CONVERGES ON AE AND BE!

STACK COOL FEATURE:

$$V_{1} = T \cdot V_{0}$$

$$V_{2} = T \cdot V_{1} = T \cdot (T \cdot V_{0})$$

$$V_{3} = T \cdot V_{2} = T \cdot (T \cdot V_{1}) = T \cdot (T \cdot (T \cdot V_{0}))$$

$$V_{1} = T^{1} \cdot V_{0}$$

$$V_{2} = T^{1} \cdot V_{0}$$

$$V_{3} = T \cdot V_{1} = T \cdot (T \cdot V_{0})$$

$$V_{4} = T^{1} \cdot V_{0}$$

$$V_{5} = T^{1} \cdot V_{0}$$

$$V_{6} = T^{1} \cdot V_{0}$$

$$V_{7} = T^{1} \cdot V_{0}$$

$$V_{8} = T^{1} \cdot V_{0}$$

$$V_{8} = T^{1} \cdot V_{0}$$

$$V_{9} = T^{1} \cdot V_{0}$$

$$V_{1} = T^{1} \cdot V_{0}$$

$$V_{1} = T^{1} \cdot V_{0}$$

$$V_{2} = T^{1} \cdot V_{0}$$

$$V_{3} = T^{1} \cdot V_{0}$$

$$V_{4} = T^{1} \cdot V_{0}$$

$$V_{5} = T^{1} \cdot V_{0}$$

$$V_{7} = T^{1} \cdot V_{0}$$

$$V_{8} = T^{1} \cdot V_{0}$$

$$V_{8} = T^{1} \cdot V_{0}$$

$$V_{8} = T^{1} \cdot V_{0}$$

$$V_{9} = T^{1} \cdot V_{0}$$

$$V_{9} = T^{1} \cdot V_{0}$$

$$V_{1} = T^{1} \cdot V_{0}$$

$$V_{1} = T^{1} \cdot V_{0}$$

$$V_{2} = T^{1} \cdot V_{0}$$

$$V_{3} = T^{1} \cdot V_{0}$$

$$V_{4} = T^{1} \cdot V_{0}$$

$$V_{5} = T^{1} \cdot V_{0}$$

$$V_{7} = T^{1} \cdot V_{0}$$

$$V_{8} = T^{1} \cdot V_{0}$$

$$V_{8} = T^{1} \cdot V_{0}$$

$$V_{8} = T^{1} \cdot V_{0}$$

$$V_{9} = T^{1} \cdot V_{0}$$

$$V_{9} = T^{1} \cdot V_{0}$$

$$V_{1} = T^{1} \cdot V_{0}$$

$$V_{1} = T^{1} \cdot V_{0}$$

$$V_{2} = T^{1} \cdot V_{0}$$

$$V_{3} = T^{1} \cdot V_{0}$$

$$V_{4} = T^{1} \cdot V_{0}$$

$$V_{5} = T^{1} \cdot V_{0}$$

$$V_{7} = T^{1} \cdot V_{0}$$

$$V_{8} = T^{1} \cdot V_{0}$$

$$V_{8} = T^{1} \cdot V_{0}$$

$$V_{9} = T^{1} \cdot V_{0}$$

$$V_{1} = T^{1} \cdot V_{0}$$

$$V_{1} = T^{1} \cdot V_{0}$$

$$V_{2} = T^{1} \cdot V_{0}$$

$$V_{3} = T^{1} \cdot V_{0}$$

$$V_{4} = T^{1} \cdot V_{0}$$

$$V_{5} = T^{1} \cdot V_{0}$$

$$V_{7} = T^{1} \cdot V_{0}$$

$$V_{7} = T^{1} \cdot V_{0}$$

$$V_{8} = T^{1} \cdot V_{0}$$

$$V_{8} = T^{1} \cdot V_{0}$$

$$V_{1} = T^{1} \cdot V_{0}$$

$$V_{1} = T^{1} \cdot V_{0}$$

$$V_{2} = T^{1} \cdot V_{0}$$

$$V_{3} = T^{1} \cdot V_{0}$$

$$V_{4} = T^{1} \cdot V_{0}$$

$$V_{5} = T^{1} \cdot V_{0}$$

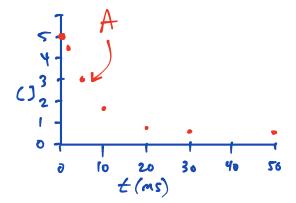
$$V_{7} = T^{1} \cdot V_{0}$$

$$V_{7} = T^{1} \cdot V_{0}$$

$$V_{7} = T^{1} \cdot V_{0}$$

$$V_{8} = T^{1}$$

50: 0.448 4.532



CAN MAKE ARBITRARILY COMPLICATED:

$$P_{AA} = (I - P_{AB} - P_{AC})$$
 $P_{AB} = k_1 \Delta t$
 $P_{AC} = \omega$

$$P_{BB} = (1 - P_{BA} - P_{BC})$$

$$P_{BA} = K_1 \text{ St}$$

$$P_{BC} = K_2 \text{ St}$$

$$P_{CC} = (I - P_{CB} - P_{CA})$$

$$P_{CB} = K_{-2} \Delta t$$

$$P_{CA} = \emptyset$$

KEY POINTS:

- @ FORMULATE MATRIX OF TRANSITION PEDBS (COWMAS SUM TO 1)
- 2 NHEN APPLIED TO VECTOR OF CONCENTRATIONS
 - GIVES NEW CONC AFTER STEP At.
 - CODIERVES MASS
 - CAN BE EXTENDED TO ANY TIME BY RAISHY T TO POHOR HAT
 - TENDS TO EQUILIBRIUM AS Z -> 00