

Assignment 2

EE24BTECH11002 - Agamjot Singh

SECTION - B JEE MAIN/AIEEE

20) Let a, b, c be such that $b(a + c) \neq 0$ if

$$\begin{vmatrix} a & a+1 & a-1 \\ b & b+1 & b-1 \\ c & c-1 & c+1 \end{vmatrix} +$$

$$\begin{vmatrix} a+1 & b+1 & c-1 \\ a-1 & b-1 & c+1 \\ (-1)^{n+2}a & (-1)^{n+1}b & (-1)^nc \end{vmatrix} = 0$$

(2009)

, then the value of n is:

- a) any even integer b) any odd integer
- c) any integer d) zero

21) The number of 3×3 non-singular matrices with four entries as 1 and all other entries as 0, is (2010)

- a) 5 b) 6
- c) at least 7 d) less than 4

22) Let \mathbf{A} be a 2×2 matrix with non-zero entries and let $\mathbf{A}^2 = \mathbf{I}$, where \mathbf{I} is 2×2 identity matrix. Define

$Tr(\mathbf{A})$ - sum of diagonal elements of \mathbf{A} and

$|\mathbf{A}|$ - determinant of matrix \mathbf{A} .

Statement - 1: $Tr(\mathbf{A}) = 0$.

Statement - 2: $|\mathbf{A}| = 1$

(2010)

- a) Statement - 1 is true, Statement - 2 is true; Statement - 2 is **not** a correct explanation for Statement-1.
b) Statement - 1 is true, Statement - 2 is false.
c) Statement - 1 is false, Statement - 2 is true.
d) Statement - 1 is true, Statement - 2 is true; Statement - 2 is a correct explanation for Statement-1.

23) Consider the system of linear equations;

$$\begin{array}{rcl} x_1 + 2x_2 + x_3 & = & 3 \\ 2x_1 + 3x_2 + x_3 & = & 3 \\ 3x_1 + 5x_2 + 2x_3 & = & 1 \end{array}$$

(2010)

- a) exactly 3 solutions
- b) a unique solution
- c) no solution
- d) infinite number of solutions

24) The number of values of k for which the linear equations $4x + ky + 2z = 0$, $kx + 4y + z = 0$ and $2x + 2y + z = 0$ possess a non zero solution is (2011)

- a) 2 b) 1 c) zero d) 3

25) Let \mathbf{A} and \mathbf{B} be two symmetrix matrices of order 3.

Statement - 1: $\mathbf{A}(\mathbf{B}\mathbf{A})$ and $(\mathbf{A}\mathbf{B})\mathbf{A}$ are symmetric matrices.

Statement - 2: \mathbf{AB} is symmetric matrix if matrix multiplication of \mathbf{A} with \mathbf{B} is commutative.

- a) Statement - 1 is true, Statement - 2 is true; Statement - 2 is **not** a correct explanation for Statement-1.

- b) Statement - 1 is true, Statement - 2 is false.
 c) Statement - 1 is false, Statement - 2 is true.
 d) Statement - 1 is true, Statement - 2 is true; Statement - 2 is a correct explanation for Statement-1.

26) Let

$$\mathbf{A} = \begin{pmatrix} 1 & 0 & 0 \\ 2 & 1 & 0 \\ 3 & 2 & 1 \end{pmatrix}$$

If \mathbf{u}_1 and \mathbf{u}_2 are column matrices such that

$$\mathbf{A}\mathbf{u}_1 = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$$

and

$$\mathbf{A}\mathbf{u}_2 = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$$

, then $\mathbf{u}_1 + \mathbf{u}_2$ is equal to:

(2012)

a)

$$\begin{pmatrix} -1 \\ 1 \\ 0 \end{pmatrix}$$

b)

$$\begin{pmatrix} -1 \\ 1 \\ -1 \end{pmatrix}$$

c)

$$\begin{pmatrix} -1 \\ -1 \\ 0 \end{pmatrix}$$

d)

$$\begin{pmatrix} 1 \\ -1 \\ -1 \end{pmatrix}$$

27) Let \mathbf{P} and \mathbf{Q} be 3×3 matrices $\mathbf{P} \neq \mathbf{Q}$. If $\mathbf{P}^3 = \mathbf{Q}^3$ and $\mathbf{P}^2\mathbf{Q} = \mathbf{Q}^2\mathbf{P}$ then determinant of $(\mathbf{P}^2 + \mathbf{Q}^2)$ is equal to (2012)

a) -2

b) 1

c) 0

d) -1

28) If

$$\mathbf{P} = \begin{pmatrix} 1 & \alpha & 3 \\ 1 & 3 & 3 \\ 2 & 4 & 4 \end{pmatrix}$$

is the adjoint of a 3×3 matrix \mathbf{A} and $|\mathbf{A}| = 4$, then α is equal to:

(JEEM2014)

a) 4

b) 11

c) 5

d) 0

29) If $\alpha, \beta \neq 0$ and $f(n) = \alpha^n + \beta^n$ and

$$\begin{vmatrix} 3 & 1+f(1) & 1+f(2) \\ 1+f(1) & 1+f(2) & 1+f(3) \\ 1+f(2) & 1+f(3) & 1+f(4) \end{vmatrix}$$

$= K(1-\alpha)^2(1-\beta)^2(\alpha-\beta)^2$, then K is equal to

(JEEM2014)

a) 1

b) -1

c) $\alpha\beta$

d) $\frac{1}{\alpha\beta}$

30) If \mathbf{A} is a 3×3 non-singular matrix such that $\mathbf{A}\mathbf{A}' = \mathbf{A}'\mathbf{A}$ and $\mathbf{B} = \mathbf{A}^{-1}\mathbf{A}'$, then $\mathbf{B}\mathbf{B}'$ equals:

(JEEM2014)

a) \mathbf{B}^{-1}

b) $(\mathbf{B}^{-1})'$

c) $\mathbf{I} + \mathbf{B}$

d) \mathbf{I}

31) The set of all values of λ for which the system of linear equations:

$$\begin{aligned} 2x_1 - 2x_2 + x_3 &= \lambda x_1 \\ 2x_1 - 3x_2 + 2x_3 &= \lambda x_2 \\ -x_1 + 2x_2 &= \lambda x_3 \end{aligned}$$

has a non-trivial solution

(JEEM2015)

- a) contains two elements
- b) contains more than two elements
- c) is an empty set
- d) is a singleton

32) If

$$\mathbf{A} = \begin{pmatrix} 1 & 2 & 2 \\ 2 & 1 & -2 \\ a & 2 & b \end{pmatrix}$$

is a matrix satisfying the equation $\mathbf{AA}^T = 9\mathbf{I}$, where \mathbf{I} is 3×3 identity matrix, then the ordered pair (a, b) is equal to:

(JEEM2015)

- a) (2, 1)
- b) (-2, -1)
- c) (2, -1)
- d) (-2, 1)

33) The system of linear equations

$$\begin{aligned} x + \lambda y - z &= 0 \\ \lambda x - y - z &= 0 \\ x + y - \lambda z &= 0 \end{aligned}$$

has a non-trivial solution for:

(JEEM2016)

- a) exactly two values of λ
- b) exactly three values of λ
- c) infinitely many values of λ
- d) exactly one value of λ

34) If

$$\mathbf{A} = \begin{pmatrix} 5a & -b \\ 3 & 2 \end{pmatrix}$$

and $\mathbf{AA} = \mathbf{AA}^T$, then $5a + b$ is equal to:

(JEEM2016)

- a) 4
- b) 13
- c) -1
- d) 5

35) Let k be an integer such that triangle with vertices $(k, -3k)$, $(5, k)$, $(-k, 2)$ has area 28 sq. units. Then the orthocentre of this triangle is at the point:

(JEEM2017)

- a) $(2, \frac{1}{2})$
- b) $(2, \frac{-1}{2})$
- c) $(1, \frac{3}{4})$
- d) $(1, \frac{-3}{4})$

36) Let ω be a complex number such that $2\omega + 1 = z$ where $z = \sqrt{-3}$. If

$$\begin{vmatrix} 1 & 1 & 1 \\ 1 & -\omega^2 - 1 & \omega^2 \\ 1 & \omega^2 & \omega^7 \end{vmatrix} = 3k$$

, then k is equal to:

(JEEM2017)

- (a) 1
- (b) $-z$

(c) z

(d) -1