Assignment 1

EE24BTECH11002 - Agamjot Singh*

C. MCQs with One Correct Answer

5) The general solution of the trigonometric equation $\sin x + \cos x = 1$ is given by:

(1981 - 2Marks)

- (a) $x = 2n\pi$; $n = 0, \pm 1, \pm 2 \dots$
- (b) $x = 2n\pi + \frac{\pi}{2}$; $n = 0, \pm 1, \pm 2 \dots$ (c) $x = n\pi + (-1)^n \frac{\pi}{4} \frac{\pi}{4}$; $n = 0, \pm 1, \pm 2 \dots$
- (d) none of these
- 6) The value of the expression $\sqrt{3}$ cosec 20° sec 20° is equal to

(1988 - 2Marks)

(a) 2

(b) $2\frac{\sin 20^{\circ}}{\sin 40^{\circ}}$

(c) 4

- (d) $4\frac{\sin 20^{\circ}}{\sin 40^{\circ}}$
- 7) The general solution of $\sin x - 3\sin 2x + \sin 3x = \cos x - 3\cos 2x + \cos 3x$ (1989 - 2Marks)
 - (a) $n\pi + \frac{\pi}{8}$
- (b) $\frac{n\pi}{2} + \frac{\pi}{8}$
- (c) $(-1)^n \frac{n\pi}{2} + \frac{\pi}{8}$ (d) $2n\pi + \cos^{-1} \frac{3}{2}$
- 8) The equation $(\cos p 1) x^2 + (\cos p) x + \sin p =$ 0 in the variable x, has real roots. Then p can take any value in the interval

(1990 - 2Marks)

- (a) $(0, 2\pi)$
- (b) $(-\pi, 0)$
- (c) $\left(-\frac{\pi}{2},\frac{\pi}{2}\right)$
- (d) $(0,\pi)$
- 9) Number of solutions of the equation $\tan x + \sec x = 2\cos x$ lying in the interval $(0, 2\pi)$ is

(1993 - 1Marks)

- (a) 0
- (b) 1
- (c) 2
- (d) 3
- 10) Let $0 < x < \frac{\pi}{4}$ then $(\sec 2x \tan 2x)$ equals (1994)

- (a) $\tan\left(x \frac{\pi}{4}\right)$ (b) $\tan\left(\frac{\pi}{4} x\right)$
- (c) $\tan\left(x + \frac{\pi}{4}\right)$ (d) $\tan^2\left(x + \frac{\pi}{4}\right)$
- 11) Let n be a positive integer such that $\sin \frac{\pi}{2n} + \cos \frac{\pi}{2n} = \frac{\sqrt{n}}{2}$. Then

(1994)

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- (a) $6 \le n \le 8$
- (b) $4 < n \le 8$
- (c) $4 \le n \le 8$
- (d) 4 < n < 8
- 12) If ω is an imaginary cube root of unity then the value of

$$\sin\left(\left(\omega^{10} + \omega^{23}\right)\pi - \frac{\pi}{4}\right) \text{ is} \tag{1994}$$

- (a) $-\frac{\sqrt{3}}{2}$ (b) $-\frac{1}{\sqrt{2}}$ (c) $-\frac{1}{\sqrt{2}}$ (d) $\frac{\sqrt{3}}{2}$
- 13) $3(\sin x \cos x)^4 + 6(\sin x + \cos x)^4$ $4(\sin^6 x + \cos^6 x) =$ (1995S)
 - (a) 11
- (b) 12
- (c) 13
- (d) 14
- 14) The general values of θ satisfying the equation $2\sin^2\theta - 3\sin\theta - 2 = 0$ is

(1995S)

- (a) $n\pi + (-1)^n \frac{\pi}{6}$ (b) $n\pi + (-1)^n \frac{\pi}{2}$
- (c) $n\pi + (-1)^n \frac{5\pi}{6}$ (d) $n\pi + (-1)^n \frac{7\pi}{6}$
- 15) $\sec^2 \theta = \frac{4xy}{(x+y)^2}$ is true if and only if (1996 - 1Mark)
 - (a) x + y = 0
- (b) $x = y, x \neq 0$
- (c) x = y
- (d) $x \neq 0, y \neq 0$
- 16) In a triangle **PQR**, \angle **R** = $\frac{\pi}{2}$. If $\tan \frac{P}{2}$ and $\tan \frac{Q}{2}$ are the roots of the equation $ax^2 + bx + c =$ 0 ($a \neq 0$) then

(1999 - 2Marks)

(a)
$$a + b = c$$
 (b) $b + c = a$

(c)
$$a + c = b$$
 (d) $b = c$

- 17) Let $f(\theta) = \sin \theta (\sin \theta + \sin 3\theta)$. Then $f(\theta)$ is (2000S)
 - (a) ≥ 0 only when θ (b) ≤ 0 for all real $\theta \geq 0$
 - (c) ≥ 0 for all real θ (d) ≤ 0 only when $\theta \leq 0$
- 18) The number of distinct real roots of

$$\begin{vmatrix} \sin x & \cos x & \cos x \\ \cos x & \sin x & \cos x \\ \cos x & \cos x & \sin x \end{vmatrix}$$
 (1)

(2001S)

- (a) 0 (b) 2 (c) 1 (d) 3
- 19) The maximum value of $(\cos \alpha_1) (\cos \alpha_2) (\cos \alpha_3) ... (\cos \alpha_n)$ under the restrictions

$$0 \le \alpha_1, \alpha_2, ..., \alpha_n \le \frac{\pi}{2} \tag{2}$$

and

$$(\cot \alpha_1)(\cot \alpha_2)(\cot \alpha_3)...(\cot \alpha_n) = 1$$
 (3) (2001S)

(a) $\frac{1}{2^{\frac{n}{2}}}$ (b) $\frac{1}{2^n}$ (c) $\frac{1}{2^n}$ (d) 1