

# Assignment 2

EE24BTECH11002 - Agamjot Singh

SECTION - B JEE MAIN/AIEEE

- 20) Let  $a, b, c$  be such that  $b(a + c) \neq 0$  if

$$\begin{vmatrix} a & a+1 & a-1 \\ b & b+1 & b-1 \\ c & c-1 & c+1 \end{vmatrix} +$$

$$\begin{vmatrix} a+1 & b+1 & c-1 \\ a-1 & b-1 & c+1 \\ (-1)^{n+2}a & (-1)^{n+1}b & (-1)^nc \end{vmatrix} = 0$$

(2009)

, then the value of  $n$  is:

- a) any even integer                      b) any odd integer
- c) any integer                          d) zero

- 21) The number of  $3 \times 3$  non-singular matrices with four entries as 1 and all other entries as 0, is (2010)

- a) 5    b) 6
- c) at least 7                                d) less than 4

- 22) Let  $\mathbf{A}$  be a  $2 \times 2$  matrix with non-zero entries and let  $\mathbf{A}^2 = \mathbf{I}$ , where  $\mathbf{I}$  is  $2 \times 2$  identity matrix. Define  $Tr(\mathbf{A})$ - sum of diagonal elements of  $\mathbf{A}$  and  $|\mathbf{A}|$  - determinant of matrix  $\mathbf{A}$ .

**Statement - 1:**  $Tr(\mathbf{A}) = 0$ .

**Statement - 2:**  $|A| = 1$

(2010)

- a) Statement - 1 is true, Statement - 2 is true; Statement - 2 is **not** a correct explanation for Statement-1.  
b) Statement - 1 is true, Statement - 2 is false.  
c) Statement - 1 is false, Statement - 2 is true.  
d) Statement - 1 is true, Statement - 2 is true; Statement - 2 is a correct explanation for Statement-1.

- 23) Consider the system of linear equations;

$$\begin{array}{rcl} x_1 + 2x_2 + x_3 & = & 3 \\ 2x_1 + 3x_2 + x_3 & = & 3 \\ 3x_1 + 5x_2 + 2x_3 & = & 1 \end{array}$$

(2010)

- a) exactly 3 solutions
- b) a unique solution
- c) no solution
- d) infinite number of solutions

- 24) The number of values of  $k$  for which the linear equations  $4x + ky + 2z = 0$ ,  $kx + 4y + z = 0$  and  $2x + 2y + z = 0$  possess a non zero solution is (2011)

- a) 2                      b) 1                      c) zero                      d) 3

- 25) Let  $\mathbf{A}$  and  $\mathbf{B}$  be two symmetrix matrices of order 3.

**Statement - 1:**  $\mathbf{A}(\mathbf{B}\mathbf{A})$  and  $(\mathbf{A}\mathbf{B})\mathbf{A}$  are symmetric matrices.

**Statement - 2:** **AB** is symmetric matrix if matrix multiplication of **A** with **B** is commutative.

- a) Statement - 1 is true, Statement - 2 is true; Statement - 2 is **not** a correct explanation for Statement-1.

- b) Statement - 1 is true, Statement - 2 is false.  
 c) Statement - 1 is false, Statement - 2 is true.  
 d) Statement - 1 is true, Statement - 2 is true; Statement - 2 is a correct explanation for Statement-1.

26) Let

$$\mathbf{A} = \begin{pmatrix} 1 & 0 & 0 \\ 2 & 1 & 0 \\ 3 & 2 & 1 \end{pmatrix}$$

If  $\mathbf{u}_1$  and  $\mathbf{u}_2$  are column matrices such that

$$\mathbf{A}\mathbf{u}_1 = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$$

and

$$\mathbf{A}\mathbf{u}_2 = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$$

, then  $\mathbf{u}_1 + \mathbf{u}_2$  is equal to:

(2012)

a)

$$\begin{pmatrix} -1 \\ 1 \\ 0 \end{pmatrix}$$

b)

$$\begin{pmatrix} -1 \\ 1 \\ -1 \end{pmatrix}$$

c)

$$\begin{pmatrix} -1 \\ -1 \\ 0 \end{pmatrix}$$

d)

$$\begin{pmatrix} 1 \\ -1 \\ -1 \end{pmatrix}$$

27) Let  $\mathbf{P}$  and  $\mathbf{Q}$  be  $3 \times 3$  matrices  $\mathbf{P} \neq \mathbf{Q}$ . If  $\mathbf{P}^3 = \mathbf{Q}^3$  and  $\mathbf{P}^2\mathbf{Q} = \mathbf{Q}^2\mathbf{P}$  then determinant of  $(\mathbf{P}^2 + \mathbf{Q}^2)$  is equal to (2012)

a) -2

b) 1

c) 0

d) -1

28) If

$$\mathbf{P} = \begin{pmatrix} 1 & \alpha & 3 \\ 1 & 3 & 3 \\ 2 & 4 & 4 \end{pmatrix}$$

is the adjoint of a  $3 \times 3$  matrix  $\mathbf{A}$  and  $|\mathbf{A}| = 4$ , then  $\alpha$  is equal to:

(JEEM2014)

a) 4

b) 11

c) 5

d) 0

29) If  $\alpha, \beta \neq 0$  and  $f(n) = \alpha^n + \beta^n$  and

$$\begin{vmatrix} 3 & 1+f(1) & 1+f(2) \\ 1+f(1) & 1+f(2) & 1+f(3) \\ 1+f(2) & 1+f(3) & 1+f(4) \end{vmatrix}$$

$= K(1-\alpha)^2(1-\beta)^2(\alpha-\beta)^2$ , then  $K$  is equal to

(JEEM2014)

a) 1

b) -1

c)  $\alpha\beta$

d)  $\frac{1}{\alpha\beta}$

30) If  $\mathbf{A}$  is a  $3 \times 3$  non-singular matrix such that  $\mathbf{A}\mathbf{A}' = \mathbf{A}'\mathbf{A}$  and  $\mathbf{B} = \mathbf{A}^{-1}\mathbf{A}'$ , then  $\mathbf{B}\mathbf{B}'$  equals:

(JEEM2014)

a)  $\mathbf{B}^{-1}$

b)  $(\mathbf{B}^{-1})'$

c)  $\mathbf{I} + \mathbf{B}$

d)  $\mathbf{I}$

31) The set of all values of  $\lambda$  for which the system of linear equations:

$$\begin{aligned} 2x_1 - 2x_2 + x_3 &= \lambda x_1 \\ 2x_1 - 3x_2 + 2x_3 &= \lambda x_2 \\ -x_1 + 2x_2 &= \lambda x_3 \end{aligned}$$

has a non-trivial solution

(JEEM2015)

- a) contains two elements
- b) contains more than two elements
- c) is an empty set
- d) is a singleton

32) If

$$\mathbf{A} = \begin{pmatrix} 1 & 2 & 2 \\ 2 & 1 & -2 \\ a & 2 & b \end{pmatrix}$$

is a matrix satisfying the equation  $\mathbf{A}\mathbf{A}^T = 9\mathbf{I}$ , where  $\mathbf{I}$  is  $3 \times 3$  identity matrix, then the ordered pair  $(a, b)$  is equal to:

(JEEM2015)

- a)  $(2, 1)$
- b)  $(-2, -1)$
- c)  $(2, -1)$
- d)  $(-2, 1)$

33) The system of linear equations

$$\begin{aligned} x + \lambda y - z &= 0 \\ \lambda x - y - z &= 0 \\ x + y - \lambda z &= 0 \end{aligned}$$

has a non-trivial solution for:

(JEEM2016)

- a) exactly two values of  $\lambda$
- b) exactly three values of  $\lambda$
- c) infinitely many values of  $\lambda$
- d) exactly one value of  $\lambda$

34) If

$$\mathbf{A} = \begin{pmatrix} 5a & -b \\ 3 & 2 \end{pmatrix}$$

and  $\mathbf{A}\text{adj}(\mathbf{A}) = \mathbf{A}\mathbf{A}^T$ , then  $5a + b$  is equal to:

(JEEM2016)

- a) 4
- b) 13
- c) -1
- d) 5

35) Let  $k$  be an integer such that triangle with vertices  $(k, -3k)$ ,  $(5, k)$ ,  $(-k, 2)$  has area 28 sq. units. Then the orthocentre of this triangle is at the point:

(JEEM2017)

- a)  $(2, \frac{1}{2})$
- b)  $(2, \frac{-1}{2})$
- c)  $(1, \frac{3}{4})$
- d)  $(1, \frac{-3}{4})$

36) Let  $\omega$  be a complex number such that  $2\omega + 1 = z$  where  $z = \sqrt{-3}$ . If

$$\begin{vmatrix} 1 & 1 & 1 \\ 1 & -\omega^2 - 1 & \omega^2 \\ 1 & \omega^2 & \omega^7 \end{vmatrix} = 3k$$

, then  $k$  is equal to:

(JEEM2017)

- (a) 1
- (b)  $-z$

(c)  $z$

(d)  $-1$