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## invariance theorem

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The invariance theorem states that a universal Turing machine provides an optimal means of description, up to a constant. Formally, for every Turing machine  $M$  there exists a constant  $c$  such that for all binary strings  $x$  we have

$$C_U(x) \leq C_M(x) + c.$$

Here,  $C_U$  means the complexity with respect to the universal Turing machine and  $C_M$  means the complexity with respect to  $M$ .

This follows trivially from the definition of a universal Turing machine, taking  $c = l(< M >)$  as the length of the encoding of  $M$ .

The invariance theorem holds likewise for prefix and conditional complexities.