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theory of formal languages

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Note: This entry is very rough at the moment, and requires work. I mainly wrote it to help motivate other entries and to organize entries on this topic and point out holes in our coverage. Right now, it is mainly a list of entries, many of which have not been written yet. Under the first heading, there is short paragraph. Eventually, there should be such a paragraph under each entry and a bibliography at the end. However, this is a lot of work for one person, so this entry is world editable in the hope that others who are knowledgeable in this topic will contribute their expertise.

1 Basic concepts and terminology

Loosely speaking, a formal language is a language whose structure can be specified with mathematical precision. The study of formal languages is not only interesting as a mathematical discipline in its own right, but also because of its relevance to the foundations of mathematics, its applications, and surprising connections with other branches of mathematics.

- alphabet
- automaton
- concatenation
- derivation
- grammar
- homomorphism of languages
- isomorphism of languages
- language
- abstract family of languages (AFL)
- reversal or mirror image
- initial symbol
- production

- rewriting rule
- semantics
- syntax
- terminal symbol
- non-terminal symbol
- word

2 Classification of languages

- Chomsky Hierarchy
- regular language
- context-free language
- context-sensitive language
- phrase-structure language
- type-3 language
- type-2 language
- type-1 language
- type-0 language

3 Regular (type 3) languages

- regular expression
- Kleene star
- Kleene algebra
- left-linear grammar
- right-linear grammar
- finite automaton

4 Context-free (type 2) languages

- Chomsky normal form
- derivation tree
- intersection of context-free and regular languages is context-free
- leftmost derivation
- rightmost derivation
- Greibach normal form
- pumping lemma
- pushdown automaton
- deterministic pushdown automaton
- a language is context-free iff it can be recognized by a pushdown automaton
- Earley's algorithm
- ambiguous grammar
- [http://planetmath.org/LLkLL\(k\)](http://planetmath.org/LLkLL(k)) grammar
- left-factored grammar
- [http://planetmath.org/LRkLR\(k\)](http://planetmath.org/LRkLR(k)) grammar
- every $LR(k)$ grammar can be recognized by a deterministic pushdown automaton
- every language which can be recognized by a deterministic pushdown automaton can be described by an $LR(1)$ grammar

5 Context-sensitive (type 1) languages

- Kuroda normal form
- length-increasing grammar
- a language is context-sensitive iff it can be generated by a length-increasing grammar
- linear bounded automaton
- a language is context-sensitive iff it can be recognized by a linear bounded automaton

6 Phrase-structure (type 0) languages

- recursive language
- recursively enumerable language, co-recursively enumerable language
- language that is neither recursively enumerable, nor co-recursively enumerable
- every phrase-structure language is recursively enumerable

7 Other types of languages and automata that describe them

- star-free language versus aperiodic finite automaton
- a star-free language is regular, but not conversely
- mildly context-sensitive language versus embedded pushdown automaton
- tree-adjoining grammar
- languages generated by tree-adjoining grammars are exactly the mildly context-sensitive languages

- a context-free language is mildly context-sensitive, but not conversely
- indexed language versus nested stack automaton
- a mildly context-sensitive language is indexed, but not conversely
- an indexed language is context-sensitive, but not conversely

8 Connection to group and semigroup theory

- finitely presented group
- automatic group
- <http://planetmath.org/SemiThueSystem> semi-Thue system
- Post system
- word problem
- Post correspondence problem
- conjugacy problem

9 Decidability

- membership problem
- emptiness problem
- recursively enumerable language
- recursive language

10 Special languages

- Dyck language
- derivation language