

Sanket Vinod Agarwal

Assignment 3

Git: <https://github.tamu.edu/agarwal-220196/FreeRTOS.git>

Task set 1:

T1(15, 1, 14) T2(20, 2, 26) T3(22, 3) (Period, Execution time, Deadline)

Let f be the frame size.

Requirement 1: $f \geq 3$ (max execution time)

Requirement 2: $H = \text{LCM}(15, 20, 22) = 660$

Possible f candidates $\{22, 20, 15, 12, 11, 10, 6, 5, 4, 3, 2, 1\}$

Requirement 3: $2f - \gcd(p_i, f) \leq D_i$

f	T1 (15, 1, 14)	T2 (20, 2, 26)	T3 (22, 3)
22	$44 - 1 \leq 14$ (false)	NA	NA
20	$40 - 5 \leq 14$ (false)	NA	NA
15	$30 - 15 \leq 14$ (false)	NA	NA
12	$24 - 3 \leq 14$ (false)	NA	NA
11	$22 - 1 \leq 14$ (false)	NA	NA
10	$20 - 5 \leq 14$ (false)	NA	NA
6	$12 - 3 \leq 14$	$12 - 2 \leq 20$	$12 - 2 \leq 22$
5	$10 - 5 \leq 14$	$10 - 5 \leq 26$	$10 - 1 \leq 22$

Since 6 satisfies all the three requirements above, the largest possible frame size is 6.

Task set 2:

T1(4, 1) T2(5, 2, 7) T3(20, 5) (Period, Execution time, Deadline)

Let f be the frame size.

Requirement 1: $f \geq 5$ (max execution time)

Requirement 2: $H = \text{LCM}(4, 5, 20) = 20$

Possible f candidates = $\{20, 10, 5, 4, 2, 1\}$

Requirement 3: $2f - \gcd(p_i, f) \leq D_i$

f	T1 (4,1)	T2 (5,2,7)	T3(20,5)
20	$40 - 4 \leq 20$ (false)		
10	$20 - 2 \leq 20$ (false)		
5	$10 - 1 \leq 4$ (false)		
4	$8 - 4 \leq 4$	$8 - 1 \leq 5$ (false)	
2	$4 - 2 \leq 4$	$4 - 1 \leq 5$	$4 - 2 \leq 20$

Largest frame of 2 violates requirement 2. It is possible only when T3 is split into parts.

Task set 3:

T1(5, 0.1) T2(7, 1) T3(12, 6) T4(45, 9) (Period, Execution time, Deadline)

Let f be the frame size.

Requirement 1: $f \geq 9$ (max execution time)

Requirement 2: $H = \text{LCM}(5, 7, 12, 45) = 1260$

Possible f candidates = { 45, 42, 36, 35, 30, 28, 21, 20, 18, 15, 14, 12, 10, 9, 7, 6, 5, 4, 3, 2 }

Requirement 3: $2f - \gcd(p_i, f) \leq D_i$

f	T1(5,0.1)	T2(7,1)	T3(12,6)	T4(45,9)
45	$50-5 \leq 5$ (False)			
42	$84-1 \leq 5$ (false)			
36	$72-1 \leq 5$ (False)			
35	$70-5 \leq 5$ (false)			
30	$60-5 \leq 5$ (false)			
28	$56-1 \leq 5$ (false)			
21	$42-1 \leq 5$ (false)			
20	$40-5 \leq 5$ (false)			
18	$36-1 \leq 5$ (false)			
15	$30-5 \leq 5$ (false)			
14	$28-1 \leq 5$ (false)			
12	$24-1 \leq 5$ (false)			
10	$20-5 \leq 5$ (false)			
9	$18-1 \leq 5$ (false)			
7	$14-1 \leq 5$ (false)			
6	$12-1 \leq 5$ (false)			
5	$10-5 \leq 5$ True	$10-1 \leq 7$ (false)		
4	$8-1 \leq 5$ (false)			
3	$6-1 \leq 5$ True	$6-1 \leq 7$ True	$6-3 \leq 12$ True	$6-3 \leq 45$ True

To satisfy requirement 2, Task 3 and task 4 must be split up to accommodate largest possible frame size of 3