

# DEEP RL AT THE EDGE OF THE STATISTICAL PRECIPICE

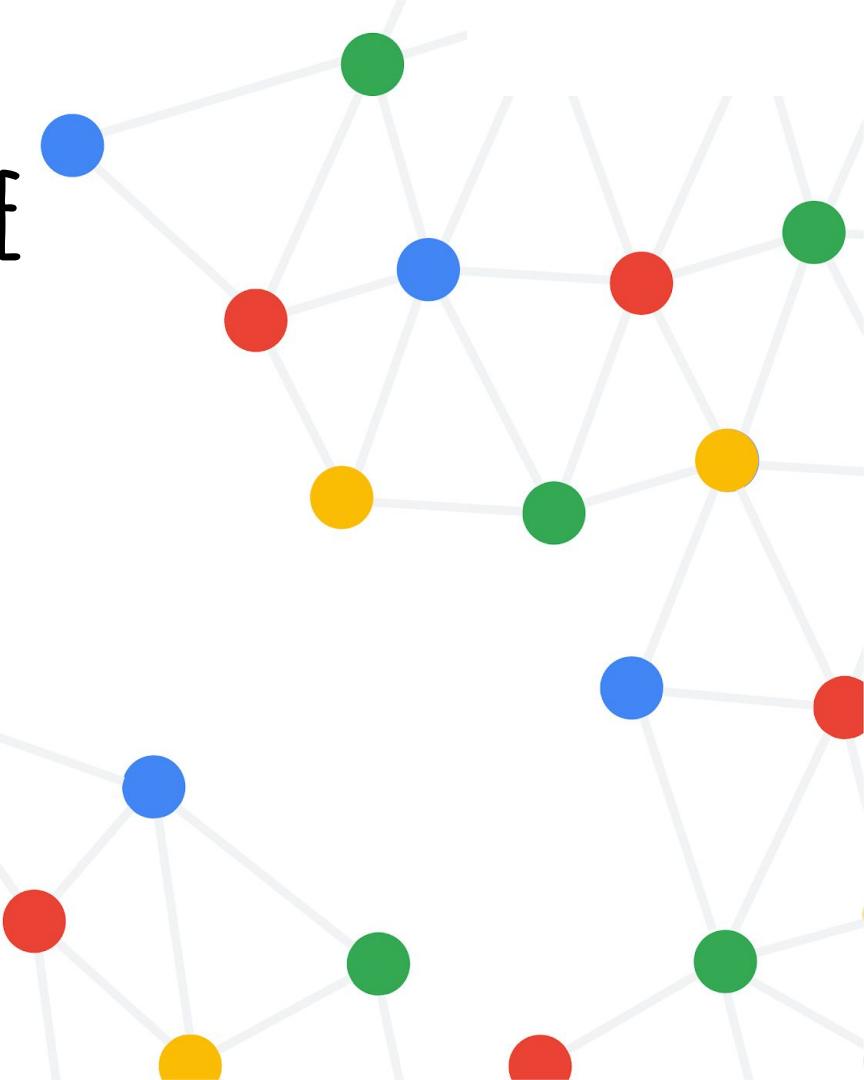
NEURIPS 2021 (ORAL)



[agarwl.github.io/rliable](https://agarwl.github.io/rliable)

Google Research

Mila



# TL;DR

This work calls for a change in how we evaluate performance on reinforcement learning benchmarks, for which we present more reliable protocols, easily applicable with *\*even a handful of runs\**, to prevent unreliable results from stagnating the field.

Few extra lines of code for reliable evaluation:  
[github.com/google-research/rliable](https://github.com/google-research/rliable)

# Assessing Progress in Deep RL



Evaluate aggregate performance on a  
suite of tasks.



# Point estimates are prevalent.

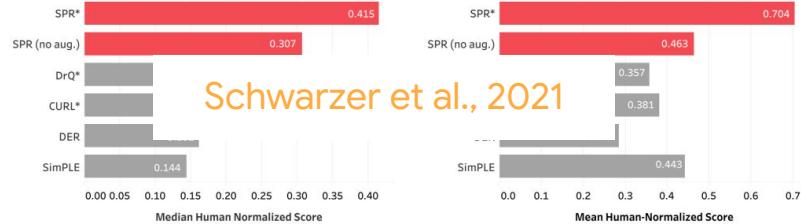
Distributional RL (ICML'17)

	Mean	Median	> H.B.	> DQN
DQN	228%	79%	24	0
DDQN				43
DUEL.	Bellemare et al., 2017			50
PRIOR.	434%	124%	39	48
PR. DUEL.	592%	172%	39	44
C51	<b>701%</b>	<b>178%</b>	<b>40</b>	<b>50</b>
UNREAL <sup>†</sup>	880%	250%	-	-

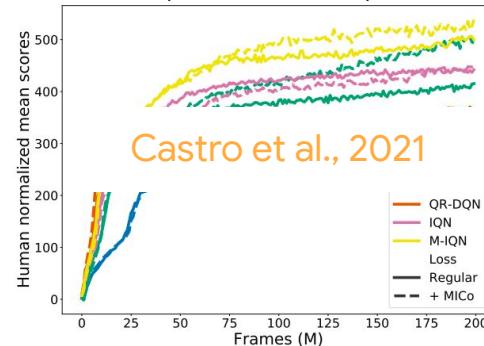
Offline RL (ICML'20)

Offline agent	Median	> DQN
DQN (Nature)	83.4%	17
DQN (	41	
Ensem	Agarwal et al., 2020	
Averag	39	
QR-DQN	43	
REM	118.9%	45
	<b>123.8%</b>	<b>49</b>

Self-predictive representations (ICLR'21)



MiCo State Abstraction (NeurIPS'21)



Castro et al., 2021

# Point estimates are prevalent.

Distributional RL (ICML'17)

	Mean	Median	> H.B.	> DQN
DQN	228%	79%	24	0
DDQN				43
DUEL.				50
PRIOR.	434%	124%	39	
PR. DUEL.	592%	172%	30	
C51	701%			
UNREAL <sup>†</sup>				

Offline RL (ICML'20)

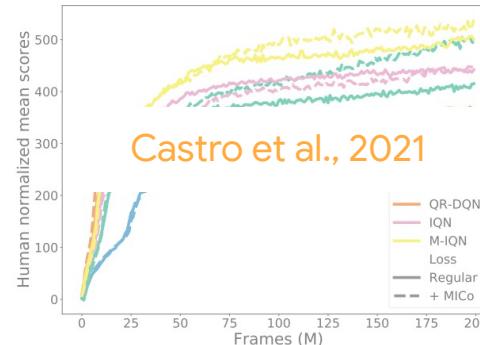
Offline agent	Median	> DQN
DQN (Nature)	83.4%	17
DQN (SAC)	111.1%	41
Ensem		39
Averag		43
QR-DQN	118.9%	45
REM	123.8%	49

Self-predictive representations (ICLR'21)



Schwarzer et al., 2021

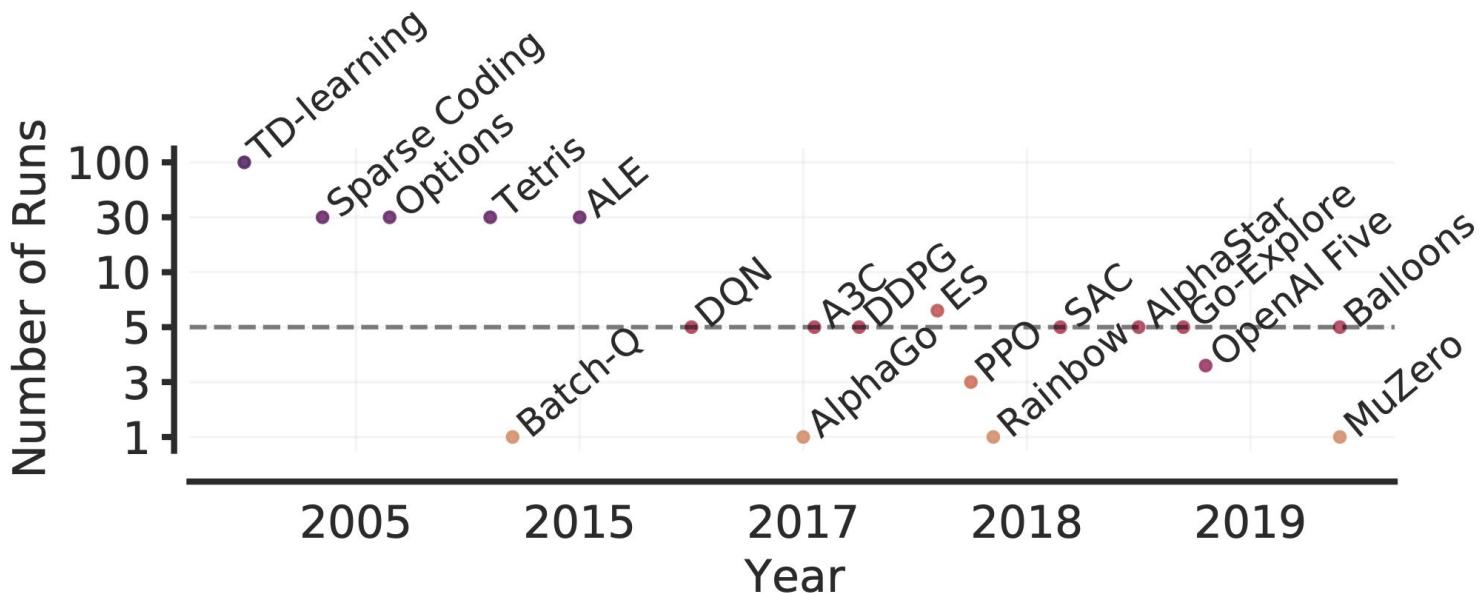
State Abstraction (NeurIPS'21)



Castro et al., 2021

Ignores statistical uncertainty in results.

# Statistical uncertainty exacerbated by small number of runs in Deep RL



So, what could go wrong with ignoring  
statistical uncertainty?

# Case Study: Atari 100k benchmark

- Evaluate performance after 100k training steps (~ 2-3 hrs of gameplay)
  - Aggregate results on 26 Atari games

**Score Normalization**

$$\text{Normalized Score} = \frac{\text{score} - \text{min score}}{\text{target score} - \text{min score}}$$

*target score corresponds to a sufficient performance, for instance human level performance*

*min score usually corresponds to the performance of a random agent*

Source: [A visual introduction to RLlib](#) by Antonin Raffin

Kaiser, L., Babaeizadeh, M., Milos, P., Osinski, B., Campbell, R. H., Czechowski, K., ... & Michalewski, H. (2019). Model-based reinforcement learning for atari. *arXiv preprint arXiv:1903.00374*.

# Case Study: Atari 100k benchmark

- Evaluate performance when trained for 100k interactions (~ 2-3 hrs of gameplay)
  - Aggregate results on 26 Atari games
- Comparison using **Median Human Normalized Scores**
  - Typically 3-5 runs per game
  - $\text{Median}\left(\frac{1}{N} \sum_{n=1}^N x_{1,n}, \frac{1}{N} \sum_{n=1}^N x_{2,n}, \dots, \frac{1}{N} \sum_{n=1}^N x_{M,n},\right)$

$$\text{Median}\left(\frac{1}{N} \sum_{n=1}^N x_{1,n}, \frac{1}{N} \sum_{n=1}^N x_{2,n}, \dots, \frac{1}{N} \sum_{n=1}^N x_{M,n},\right)$$

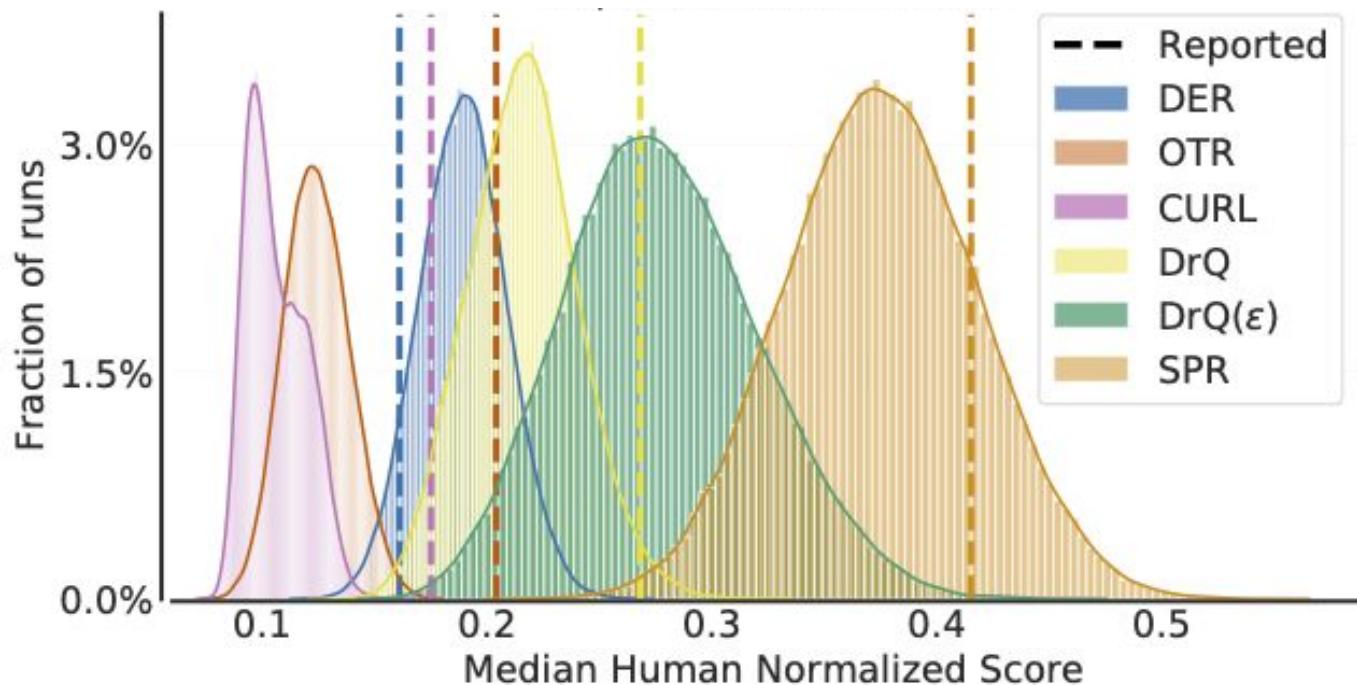
 Score on game 1 on run 'n'

# Case Study: Experimental Setup

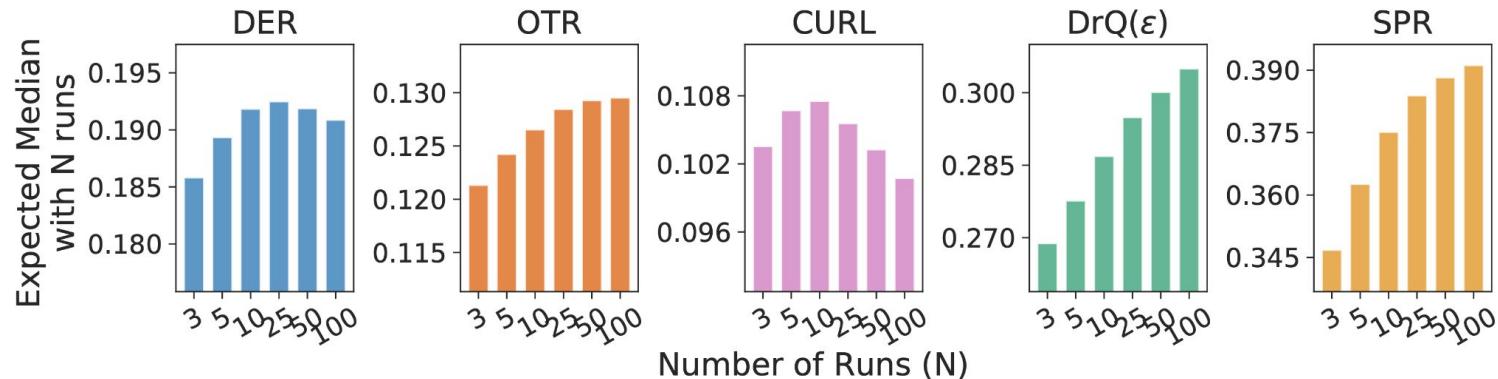
- Evaluate **100 independent runs** for 5 algorithms:
  - DER, OTR, DrQ, CURL, and SPR
- We have **26 games × 100 scores/game** per algorithm.
  - Subsample scores with replacement to 3–100 runs.

1. van Hasselt, Hado, Matteo Hessel, and John Aslanides. "When to use parametric models in reinforcement learning?" *NeurIPS* (2019).
2. Kielak, Kacper. "Do recent advancements in model-based deep reinforcement learning really improve data efficiency?." *arXiv preprint arXiv:2003.10181* (2020).
3. Kostrikov, Ilya, Denis Yarats, and Rob Fergus. "Image augmentation is all you need: Regularizing deep reinforcement learning from pixels." *ICLR* (2021).
4. Srinivas, Aravind, Michael Laskin, and Pieter Abbeel. "CURL: Contrastive unsupervised representations for reinforcement learning." *ICML* (2020).
5. Schwarzer, Max, Ankesh Anand, Rishab Goel, R. Devon Hjelm, Aaron Courville, and Philip Bachman. "Data-efficient reinforcement learning with momentum predictive representations." *ICLR* (2021).

# What if I report performance using a different set of runs?

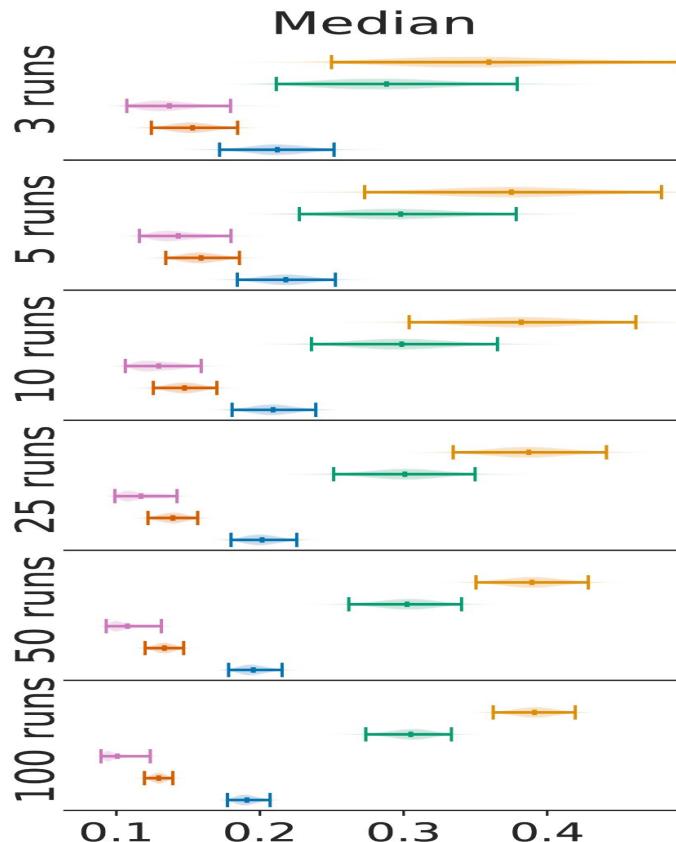


# Median scores are substantially biased!



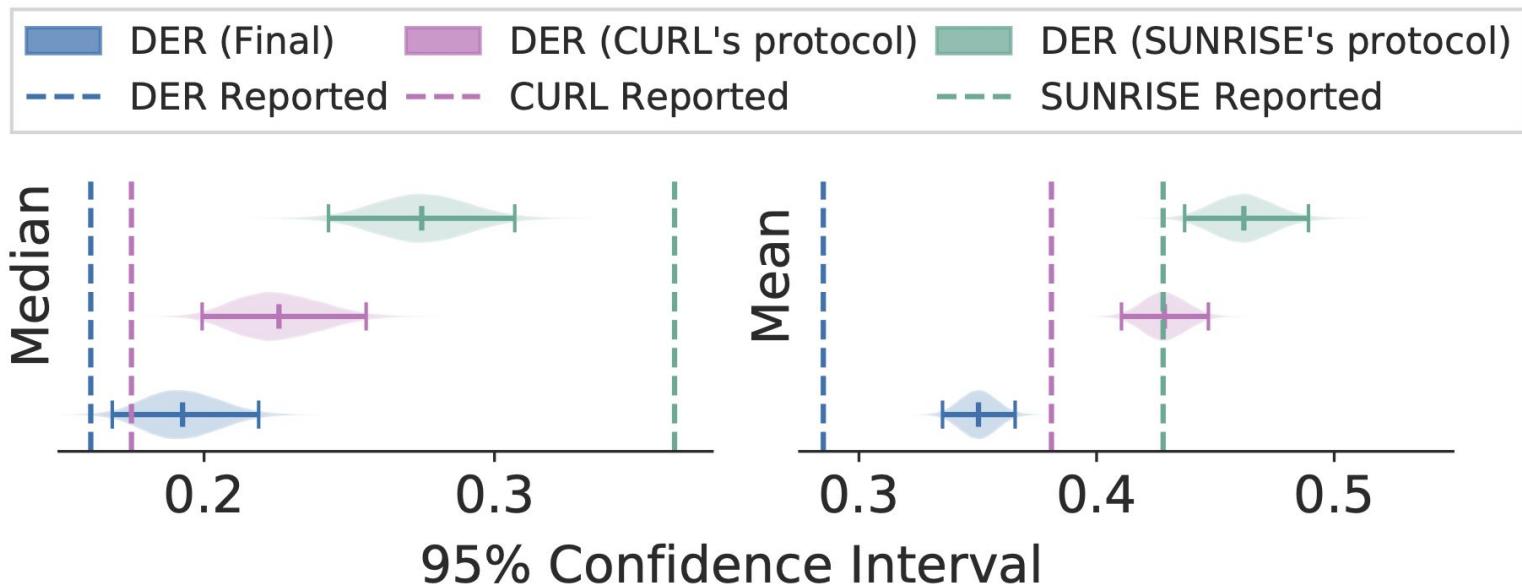
$$\text{Median}(\mathbb{E}[X_1], \dots, \mathbb{E}[X_M]) \neq \mathbb{E}\left[\text{Median}\left(\frac{1}{N} \sum_{n=1}^N X_{1,n}, \dots, \frac{1}{N} \sum_{n=1}^N X_{M,n}\right)\right]$$

# How many runs for negligible uncertainty?



Even 30-50 runs may not suffice for certain comparisons.

# Changes in evaluation protocols invalidates comparisons to prior work.



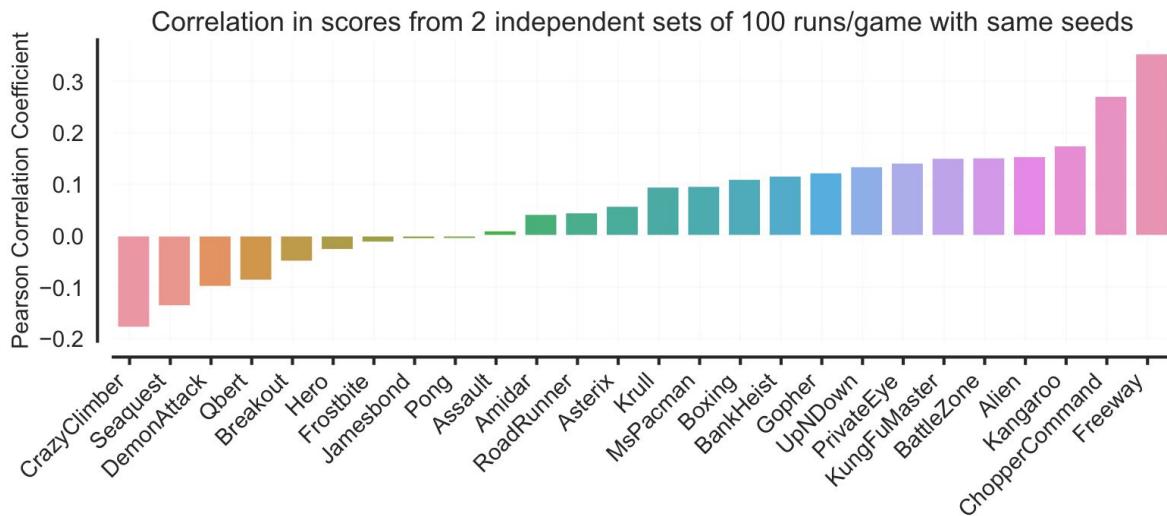
Also \*see\*: Mauro Birattari and Marco Dorigo. How to assess and report the performance of a stochastic algorithm on a benchmark problem: mean or best result on a number of runs? Optimization letters, 2007.

# How to reliably evaluate performance?

# How to reliably evaluate performance?

~~Just Fix Random Seeds?~~ Not a solution.

- Why prefer one set of seeds over another?
- Often can't fix randomness in practice (different hardware, non-determinism in GPUs)



# How to reliably evaluate performance?

~~Evaluate More Runs?~~ Not feasible.

- 5 runs on 50 Atari games for 200M frames takes 1000+ GPU days.
- More complex RL benchmarks -- quite expensive to evaluate even a few runs.



# How to reliably evaluate performance \*with a handful of runs\*?

~~Is statistical significance testing the solution?~~ Not really.

- Dichotomous (significant vs not significant)
- Widely misinterpreted.
- Often hide effect sizes (such as size of improvement over baseline).

Fun fact: Main statistics journal in USA bans thresholding p-values!

[1] Amrhein, Valentin, Sander Greenland, and Blake McShane. "Scientists rise up against statistical significance." *Nature* (2019) .

[2] Wasserstein, Ronald L., Allen L. Schirm, and Nicole A. Lazar. "Moving to a world beyond "p< 0.05"." *The American Statistician* (2019).

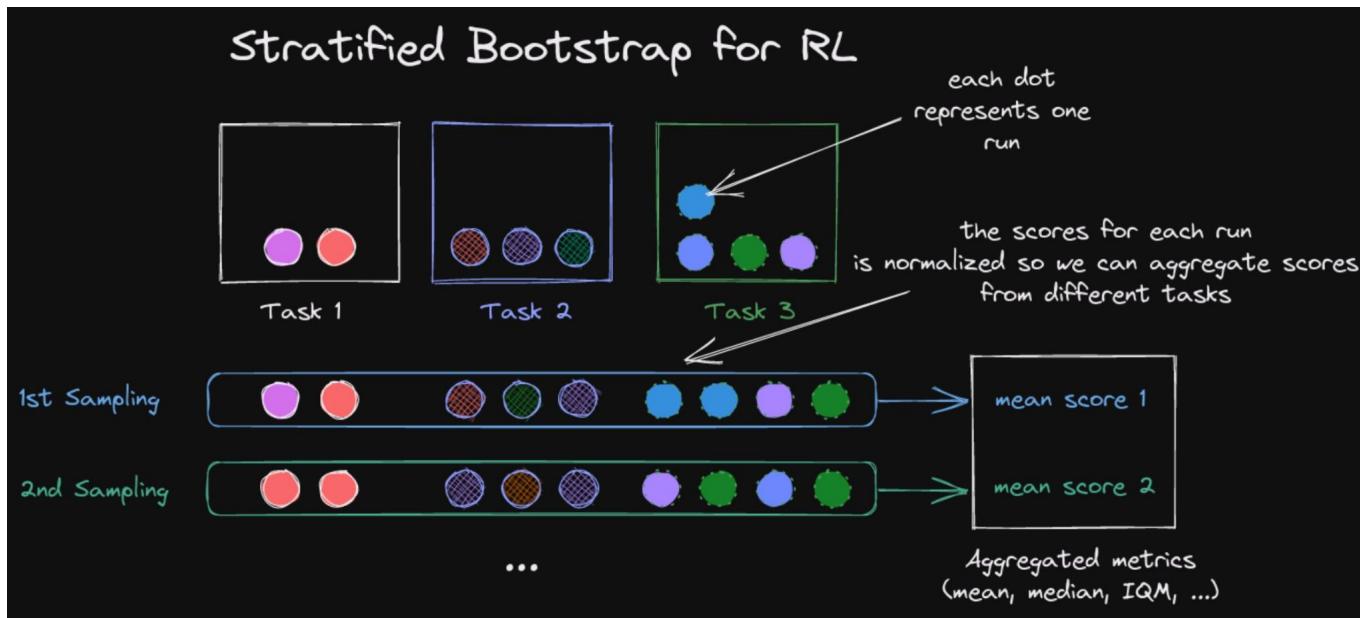
# How to reliably evaluate performance \*with a handful of runs\*?

Desiderata	Current evaluation approach	Our recommendation
Uncertainty in aggregate performance	Point estimates	<b>Interval estimates</b>
Variability in performance across tasks and runs	Tables with task mean scores	<b>Performance Profiles</b>
Aggregate metrics for overall performance	Mean / Median	<b>Interquartile Mean (IQM), Prob. of Improvement</b>

# Interval Estimates: Stratified Bootstrap Confidence Intervals

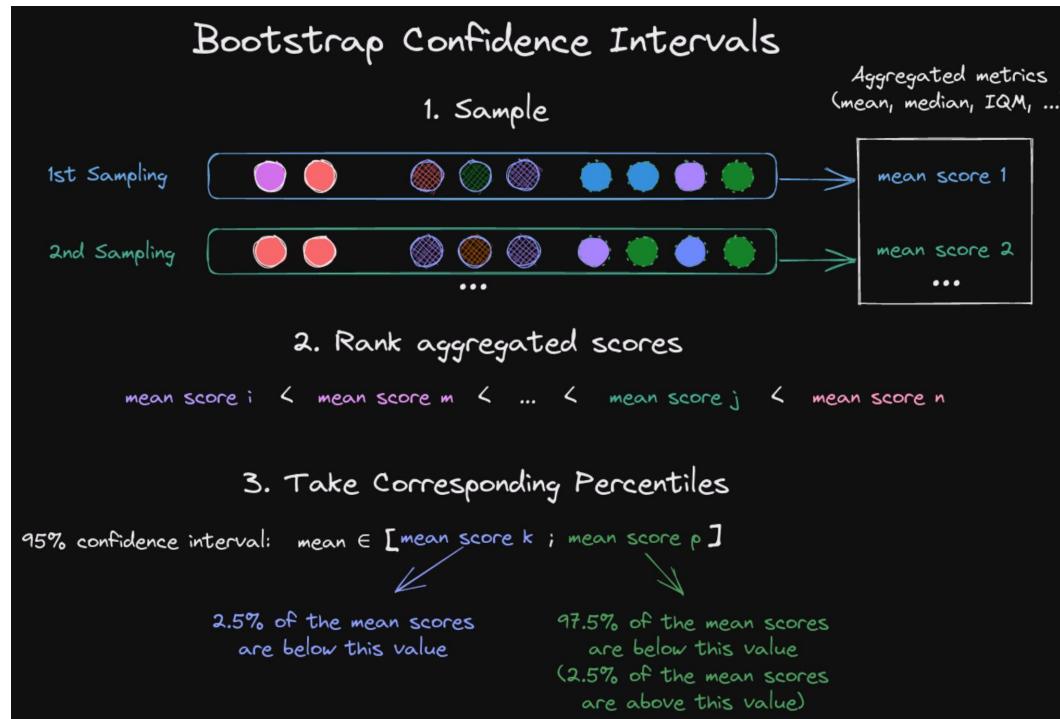
- “If we repeat the experiment with different runs, what aggregate score are we expected to get?”

# Interval Estimates: Stratified Bootstrap Confidence Intervals



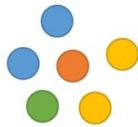
Source: [A visual introduction to RLiable](#) by Antonin Raffin

# Stratified Bootstrap Confidence Intervals: How does it work?



# Interval Estimates: Stratified Bootstrap Confidence Intervals

Single task with N runs



Task 1

- Only N random samples
- Bootstrapping CIs don't make sense with  $N \leq 5$ !

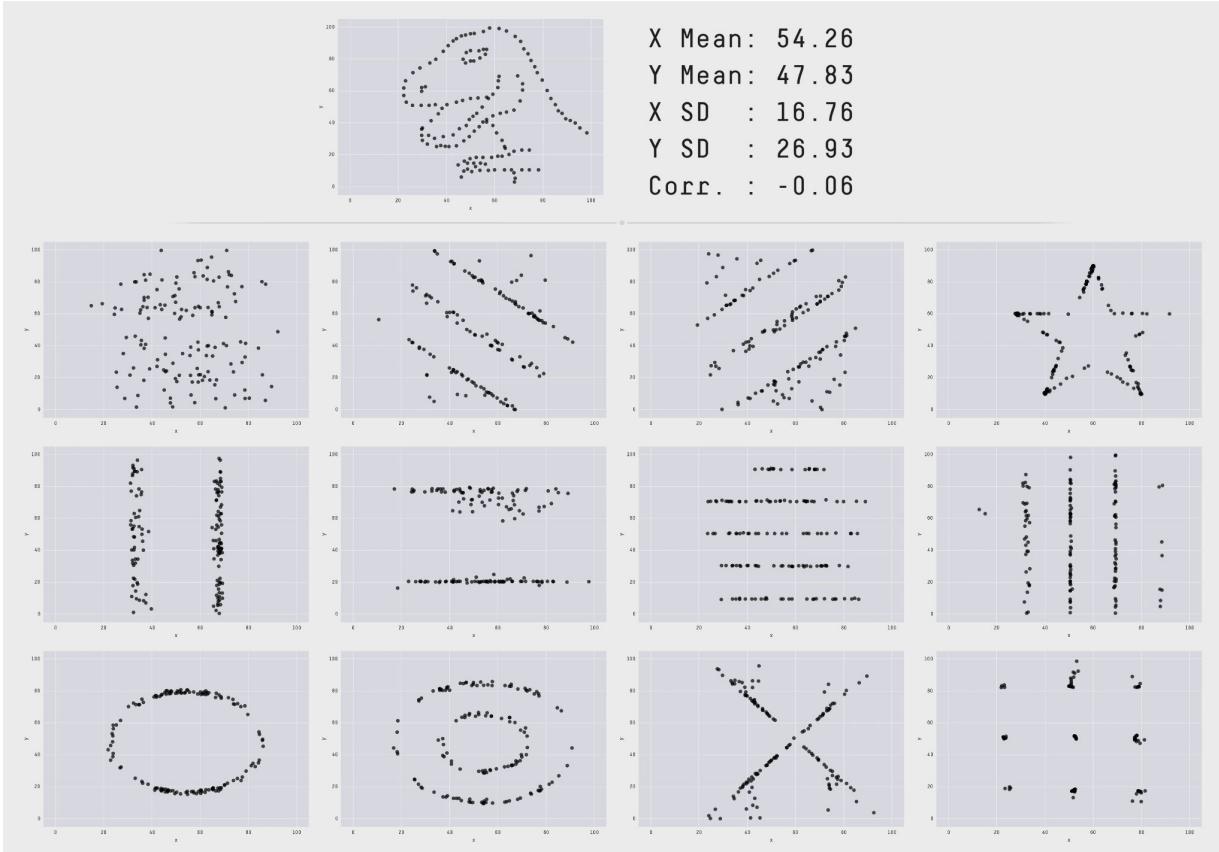
M tasks with N runs



Task 1      Task 2      ...      Task M

- $N * M$  random samples
- Bootstrapping results in reasonably accurate CIs with  $N \geq 5$ !

# Aggregate metrics hide task variability!



Source: Same Stats, Different Graphs.  
<https://www.autodesk.com/research/publications/same-stats-different-graphs>.

# Performance Variability: Tables with per-task scores?

Game	Random	Human	SimPLe	DER	OTRainbow	CURL	DrQ	SPR (no Aug)	SPR
Alien	227.8	7127.7	616.9	739.9	824.7	558.2	771.2	<b>847.2</b>	801.5
Amidar	5.8	1719.5	88.0	<b>188.6</b>	82.8	142.1	102.8	142.7	176.3
Assault	222.4	742.0	527.2	431.2	351.9	600.6	452.4	<b>665.0</b>	571.0
Asterix	210.0	8503.3	<b>1128.3</b>	470.8	628.5	734.5	603.5	820.2	977.8
Bank Heist	14.2	753.1	34.2	51.0	182.1	131.6	168.9	<b>425.6</b>	380.9
BattleZone	2360.0	37187.5	5184.4	10124.6	4060.6	14870.0	12954.0	10738.0	<b>16651.0</b>
Boxing	0.1	12.1	9.1	0.2	2.5	1.2	6.0	12.7	<b>35.8</b>
Breakout	1.7	30.5	16.4	1.9	9.8	4.9	16.1	12.9	<b>17.1</b>
ChopperCommand	811.0	7387.8	<b>1246.9</b>	861.8	1033.3	1058.5	780.3	667.3	974.8
Crazy Climber	10780.5	35829.4	<b>62583.6</b>	16185.3	21327.8	12146.5	20516.5	43391.0	42923.6
Demon Attack	152.1	1971.0	208.1	508.0	711.8	817.6	<b>1113.4</b>	370.1	545.2
Freeway	0.0	29.6	20.3	<b>27.9</b>	25.0	26.7	9.8	16.1	24.4
Frostbite	65.2	4334.7	254.7	866.8	231.6	1181.3	331.1	1657.4	<b>1821.5</b>
Gopher	257.6	2412.5	771.0	349.5	<b>778.0</b>	669.3	636.3	774.5	715.2
Hero	1027.0	30826.4	2656.6	6857.0	6458.8	6279.3	3736.3	5707.4	<b>7019.2</b>
Jamesbond	29.0	302.8	125.3	301.6	112.3	<b>471.0</b>	236.0	367.2	365.4
Kangaroo	52.0	3035.0	323.1	779.3	605.4	872.5	940.6	1359.5	<b>3276.4</b>
Krull	1598.0	2665.5	<b>4539.9</b>	2851.5	3277.9	4229.6	4018.1	3123.1	3688.9
Kung Fu Master	258.5	22736.3	<b>17257.2</b>	14346.1	5722.2	14307.8	9111.0	15469.7	13192.7
Ms Pacman	307.3	6951.6	<b>1480.0</b>	1204.1	941.9	1465.5	960.5	1247.7	1313.2
Pong	-20.7	14.6	<b>12.8</b>	-19.3	1.3	-16.5	-8.5	-16.0	-5.9
Private Eye	24.9	69571.3	58.3	97.8	100.0	<b>218.4</b>	-13.6	52.6	124.0
Qbert	163.9	13455.0	<b>1288.8</b>	1152.9	509.3	1042.4	854.4	606.6	669.1
Road Runner	11.5	7845.0	5640.6	9600.0	2696.7	5661.0	8895.1	10511.0	<b>14220.5</b>
Seaquest	68.4	42054.7	<b>683.3</b>	354.1	286.9	384.5	301.2	580.8	583.1
Up N Down	533.4	11693.2	3350.3	2877.4	2847.6	2955.2	3180.8	6604.6	<b>28138.5</b>

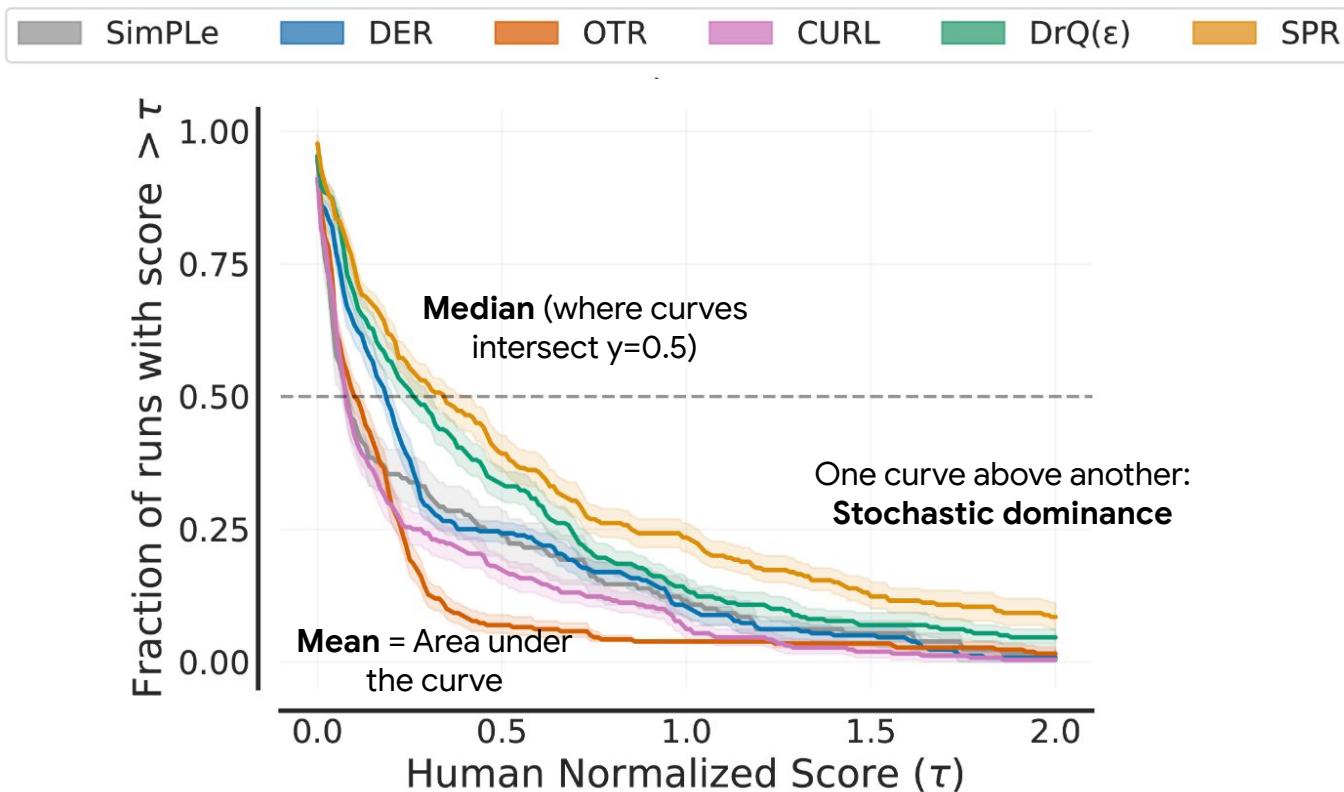
- Overwhelming beyond a few tasks
- Standard deviations frequently omitted
- Mean scores present incomplete picture for non-gaussian distributions!

## A better approach: Performance profiles with CIs

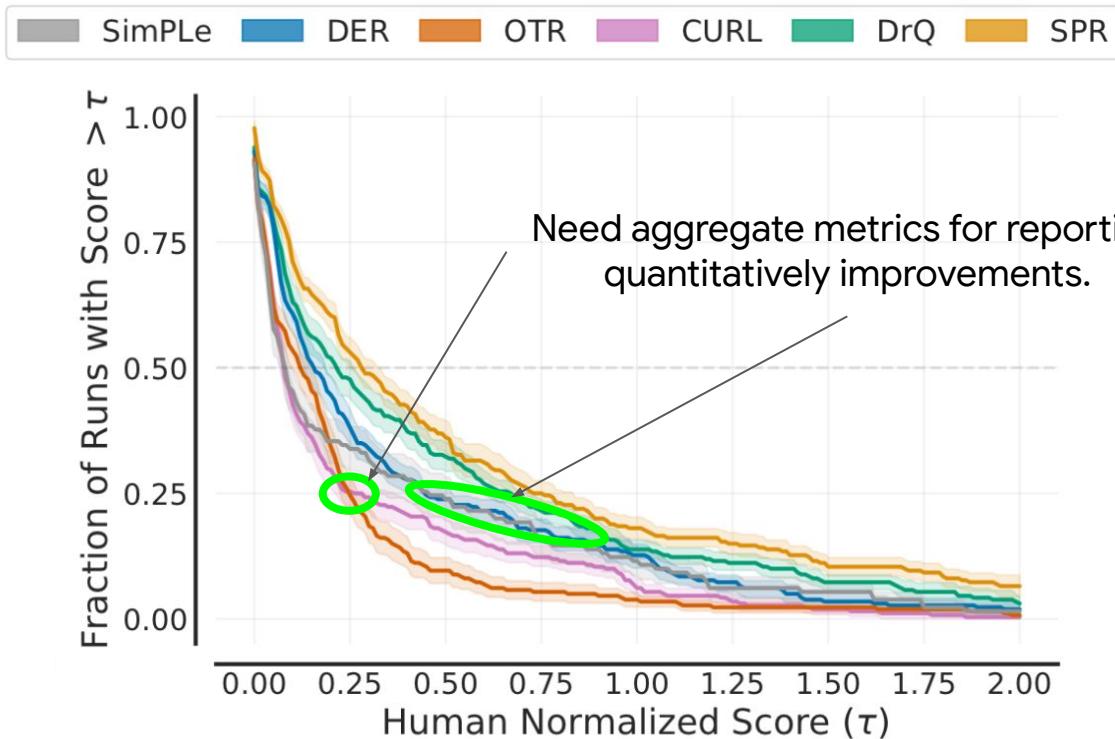
$$p(\tau) = \frac{1}{NM} \sum_{m=1}^M \sum_{n=1}^N \mathbf{1}[X_{n,m} > \tau]$$

- Typically used for comparing solve times of different optimization methods.
- Robust to outlier runs/tasks.
- Robust to small changes in performance across all tasks.

# Performance Profiles for a bird's-eye view!



# What if one algorithm doesn't dominate another?



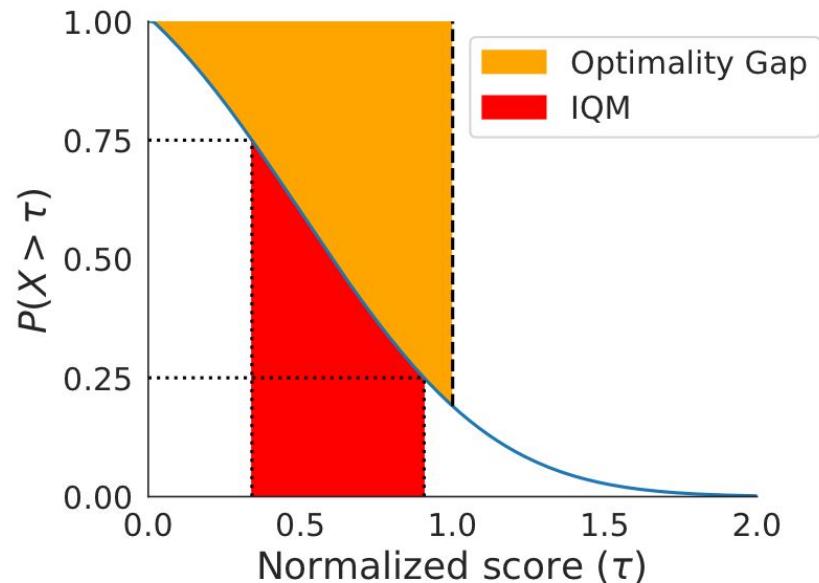
# Existing Metrics are Deficient!

- **Median:** High variability and not robust -- score of 0 on half of the tasks does not change it.
- **Mean:** Easily dominated by a few outlier tasks.

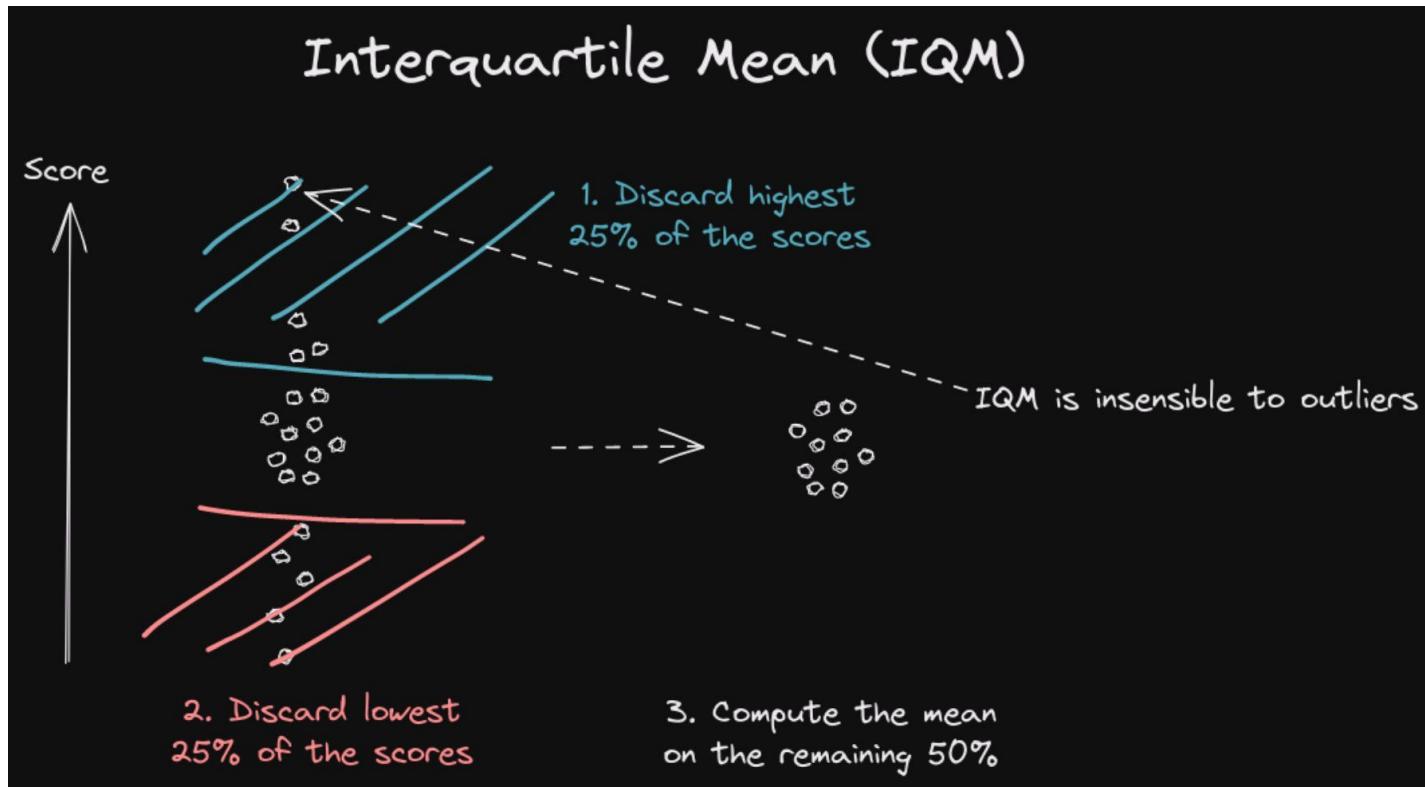
Need better aggregate metrics that are robust, not dominated by outliers and have small uncertainty.

# Robust and Efficient Aggregate Metrics

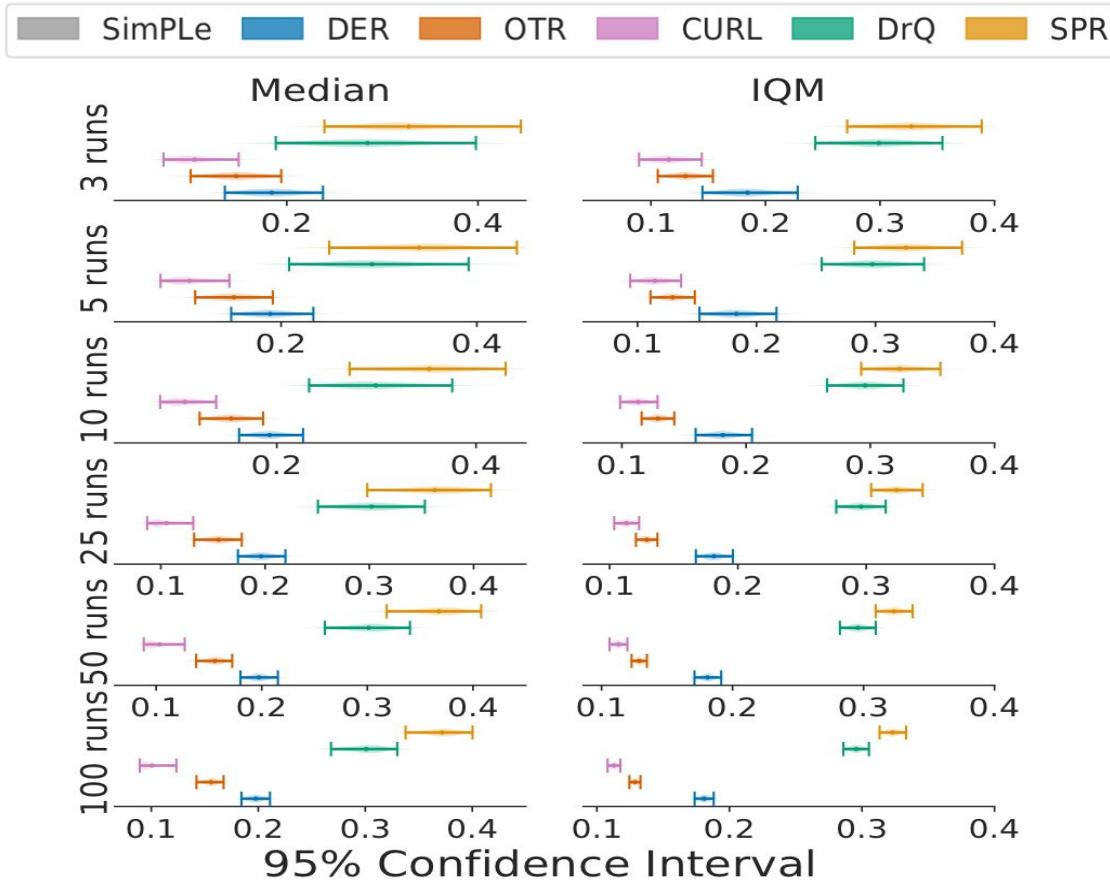
- Median → **Interquartile Mean (IQM)**
  - Averages middle 50% scores across all runs and tasks
  - Best of both worlds: Median, Mean: 50%, 0% trimmed mean
- Mean → **Optimality Gap**
  - How far an algorithm is from optimal performance



# Visual introduction to IQM



# IQM leads to smaller confidence intervals



# Am I better than the baseline?

We can compute probability of improvement of algorithm X over Y.

$$P(X > Y) = \frac{1}{M} \sum_{m=1}^M P(X_m > Y_m)$$

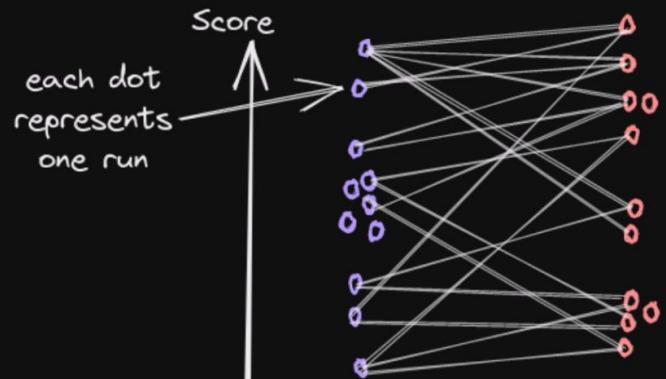


Performance on task X.

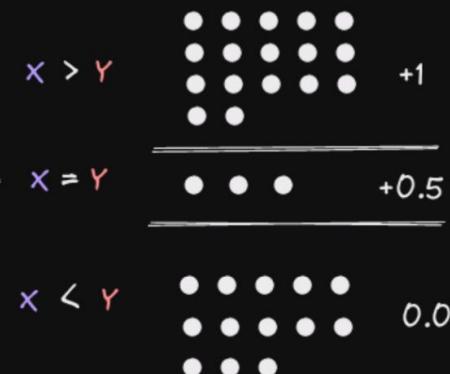
# Probability of Improvement

## Probability of Improvement on a task $m$

1. Compare each run from  $X$  to each run from  $Y$



2. Compute wins, losses and draws



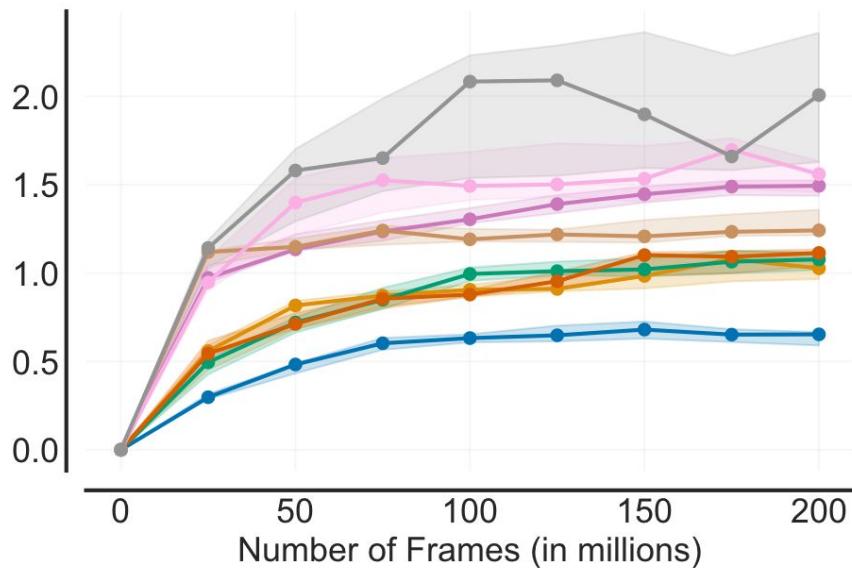
3. Divide by the number of comparisons to obtain  $P(X > Y)$

# Re-evaluating Evaluation

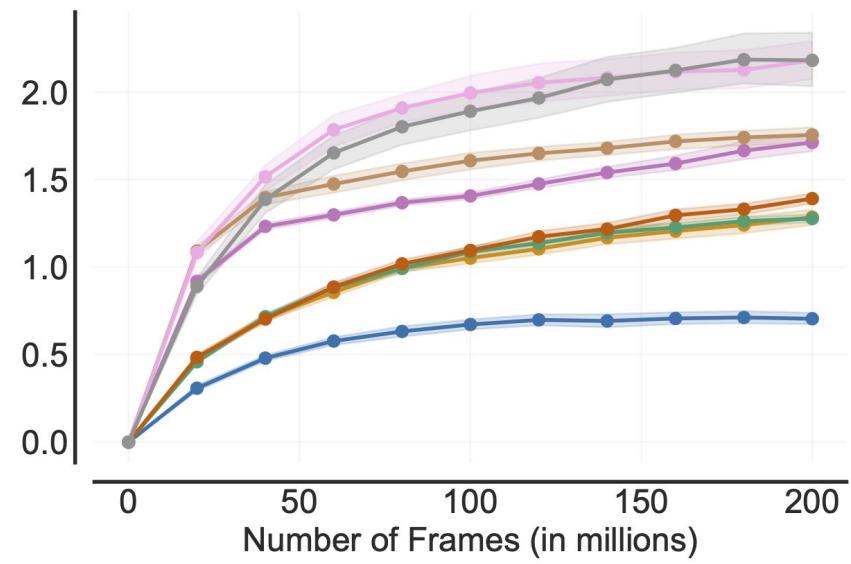
# Re-evaluating algorithms on ALE



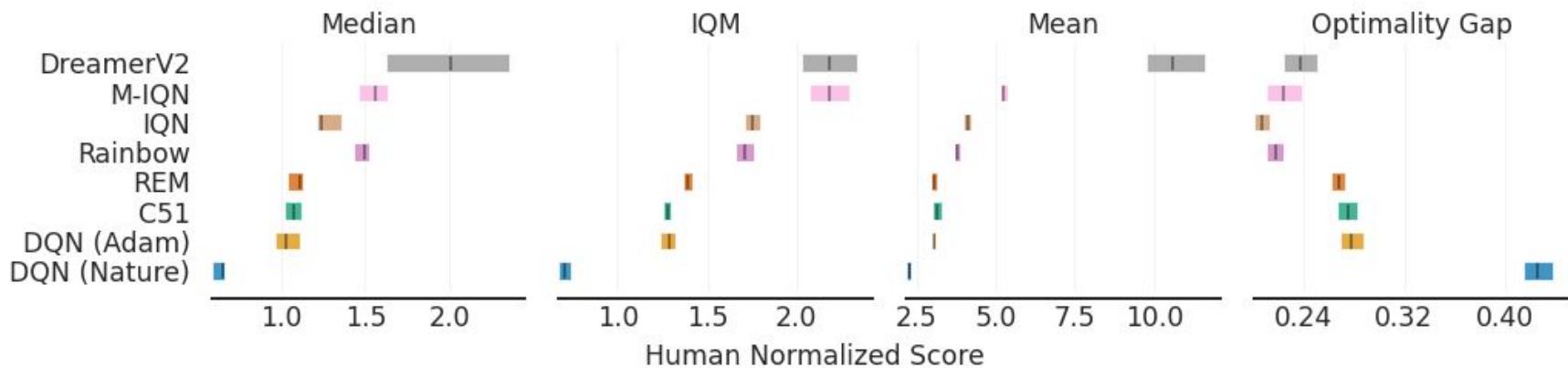
## Median Scores



## IQM Scores

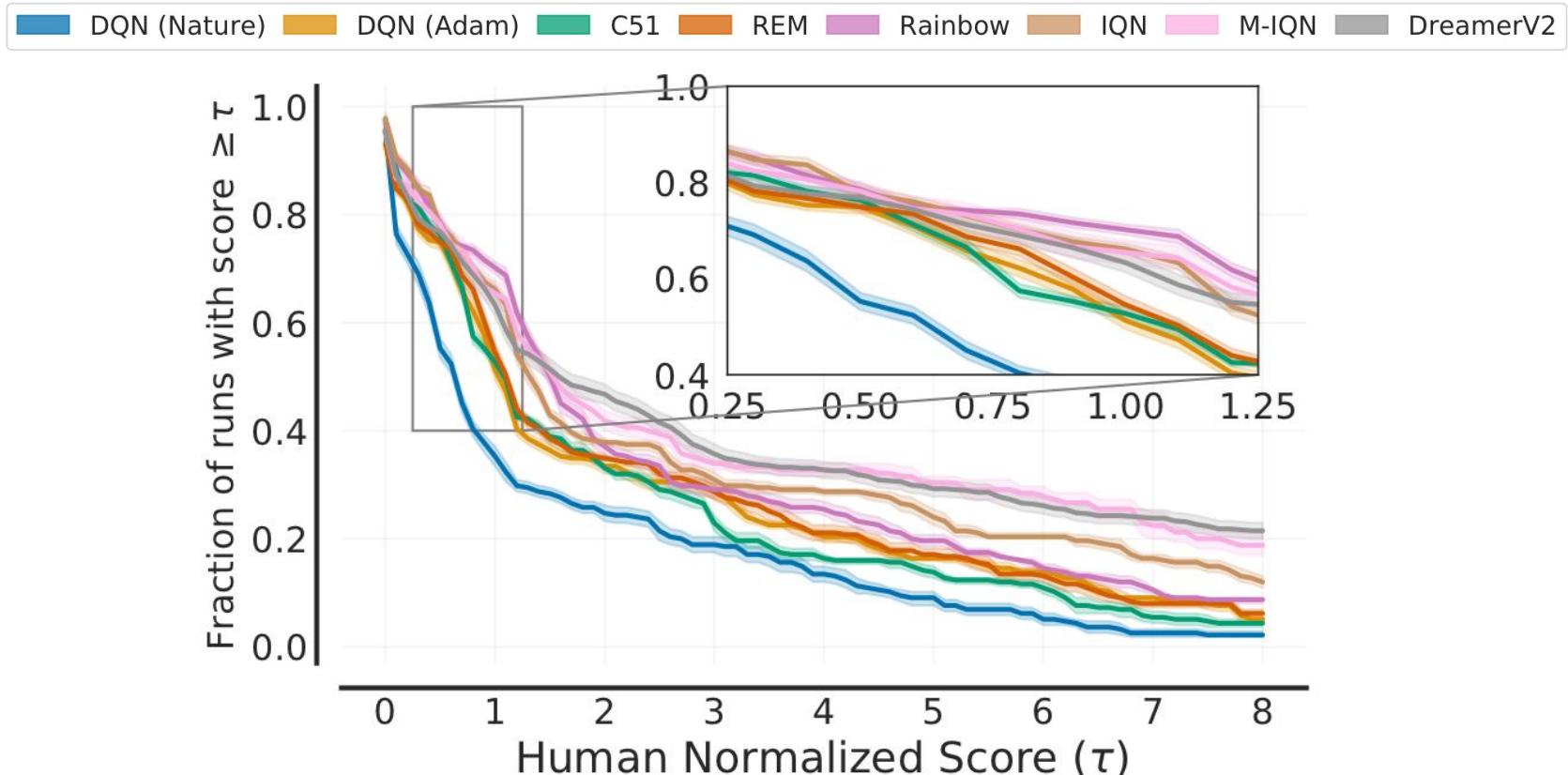


# ALE: Interval estimates

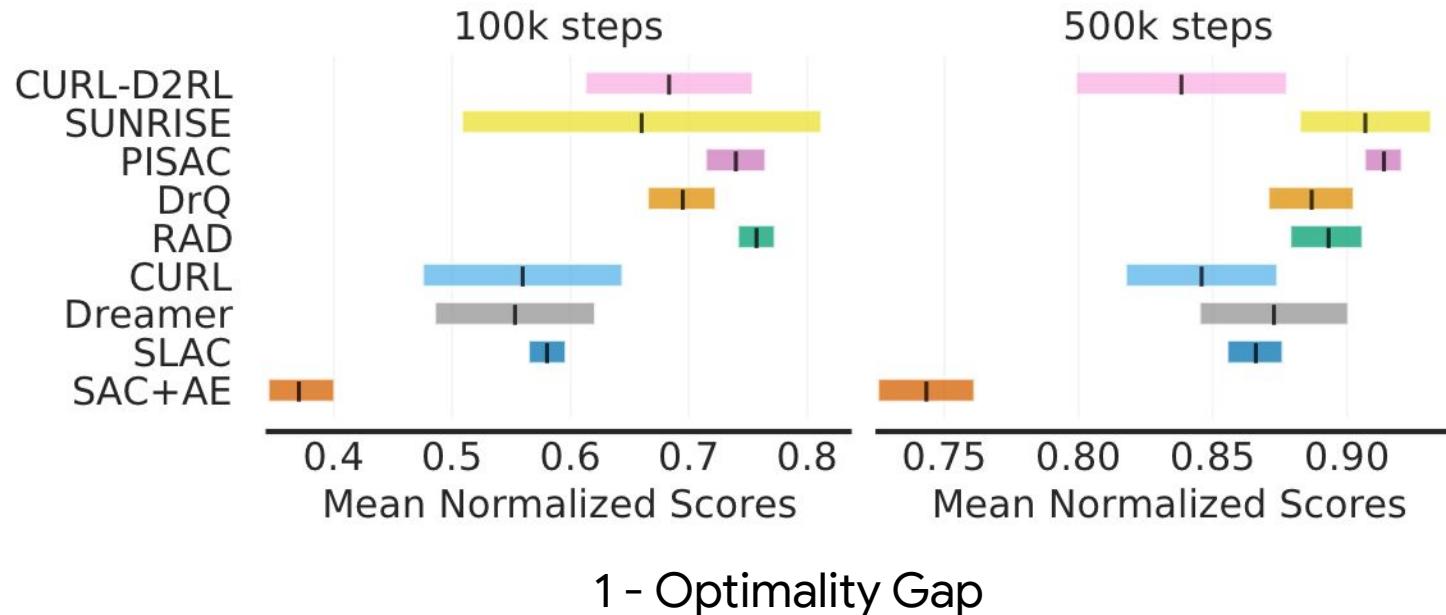


Performance Ranking changes depending on the metric!

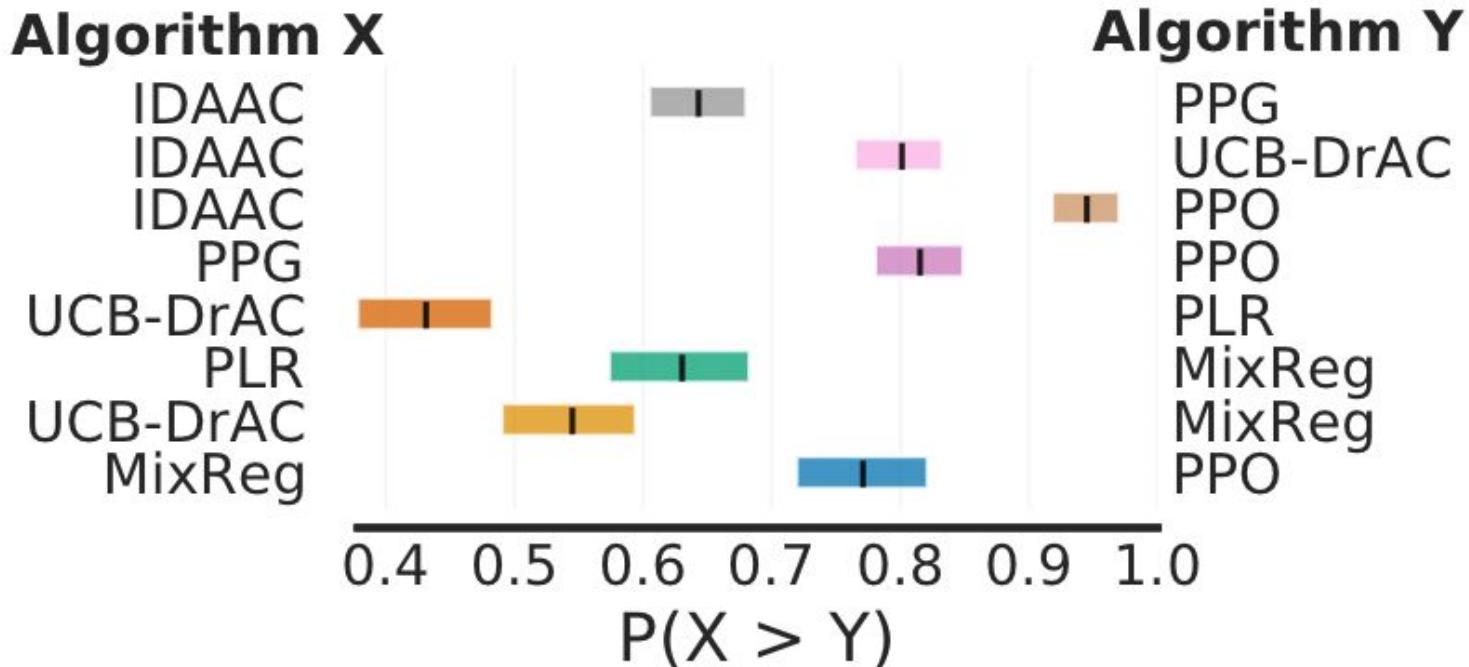
# ALE: Performance Profiles



# Re-evaluating algorithms on DM Control



# Proctgen: Average Probability of Improvement



# Takeaways

- Use **interval estimates** as opposed to point estimates.
- More is more: **Performance profiles** for qualitative summarization.
- Use better aggregate performance measures such as **interquartile mean** (IQM) and prob. of improvement.
- Provide individual runs for better statistical comparisons.

See [bit.ly/statistical\\_precipice\\_colab](https://bit.ly/statistical_precipice_colab) for jumpstart. Thank you!



Just as a rock-climber can skirt the edge  
of the steepest precipices, it seems  
likely that ongoing progress in RL will  
require greater experimental discipline.

See [agarwl.github.io/rliable](https://agarwl.github.io/rliable).