

Expanding the proof rule base of AtelierB automated prover - Research Proposal

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Abstract—AtelierB is a tool for formal software development through refinement, using the B-method. It incorporates an automated prover, which has been recognized as the most thorough prover for B set theory, and has been used as a basis for many others. Nevertheless it has multiple shortcomings. Various approaches have been suggested and taken to improve its performance, including extensions to the proof rule base, created by the users. In this work we aim to create such an extension, ensuring that all added rules are sound and well-reasoned. We also aim to identify any limitations of this approach. The secondary goal is to improve the robustness of the software without straying from pure B method, and taking into account the ease of use. As a metric of our success, we use the benchmarks proposed by Conchon and Iguernala [1].

Index Terms—B method, formal verification

I. INTRODUCTION

THE aim of formal specification and verification is to ensure the correctness of software. While overall less popular than quality assurance through testing, it is most commonly used in safety-critical areas, such as air traffic control, railway routing, or medical cyber-physical systems, or where testing is too costly or puts the users at risk. It allows for certifying that a given piece of software works as intended, and is error-free.

In some industries, such as railway, it is demanded by the regulations to provide a certificate of correctness for any piece of software. While not required, it is strongly suggested to use formal verification methods, such as B or Z, and indeed they make satisfying the regulations easier. [2]

A. The B-method

Various methods and approaches have been developed. In this project, we shall focus on the classical B-method, allowing for formal specification through refinement of abstract machines. In the earliest stages of the development process, an abstract machine is created, that satisfies the requirements. It is a construct based on 1st order logic and set theory. At this point, there is no reasoning

about the order of operations and timeline - no loops, no sequential actions. Additionally the machine may, and often will have some nondeterministic elements.

The abstract machine is then refined step by step, until the nondeterminism is eliminated. The final stage of the refinement process is the implementation, which is a much more concrete description of the system, ready to be translated into code. Thus it has to be entirely deterministic, and use simple data types, such as numerical values or arrays, but not sets. While limiting, it brings us very close to the actual coding, and in fact some tools are capable of code generation from the implementation machine.

The B-method allows us to do much more than turning an initial specification into an auto-generated (and because of that often low quality) code. It gives us means of documenting the whole software development process, and certifying that the final product indeed meets the requirements.

B. AtelierB tool

The tool to support all stages of software development with B-method is AtelierB, created by ClearSy. In particular it includes a powerful automated prover. We will inspect it and the proof process very closely, as the work in this project is expected to rely on it entirely.

After creating the specification, we can generate proof obligations (POs). They are statements about the consistency of the types of variables, well-definedness and other things that are implied by our definitions or methods. In a correct piece of software, all of the POs should be demonstrated to hold. If there is a PO that can't be proved to hold by any means, it indicates that there exists an error in the specification.

An easy example to demonstrate it is a bag, from which we pick an item one by one. The operation to pick an item guarantees some return value, so a proof obligation generated by the tool may require us to check that the bag is never empty when this operation is called.

It is expected that about 75% of the POs will be demonstrated automatically, and only 5% of them will require more than 10 s (i.e. proof force 1 or higher) [3].

The remaining POs will need user input to be discharged. This is done through the automated prover, with the user choosing which rule or tactic to apply, simplifying the hypothesis and in general nudging the prover and pointing it in the right direction.

C. Limitations of the prover

It is important to understand that the prover can only generate proof obligations and demonstrate that they are satisfied, but is incapable of proving that they are not - this problem is undecidable. In other words, each proof obligation can only be proved or unproved, and the latter can happen for one of two reasons. It is quite likely that a PO is true, but the program cannot prove it automatically because of its complexity. However, the unproved obligations also include the ones that are false and point to errors in the specification.

Finally, it has to be stressed that adding user-created rules is not advised, and should be avoided, however that may not always be possible. The tools available are not perfect and additionally may not be tailored to the particular scenario. All added rules must be proven to be correct, before one can rely on them. Although the prover has some capability for demonstrating a rule by reducing and rewriting it into a simpler form, new rules often have to be validated by hand. There is nothing stopping users from adding incorrect rules, and especially ones that do not deal with all possible test cases are often not shown to be false easily.

II. RELATED WORKS

A. Applications of B-method

B-method is commonly used in European Railway industry, from traffic management systems to developing platform door controllers [5].

An example of using classical B-method in a large scale industrial project is given by F. Badeau and A. Amelot [7]. They have aided Siemens Transportation Systems to develop an shuttle rail service at Paris-Charles de Gaulle Airport. The fully automatic metro line began its operation in April 2007, and has been functioning since then, with one more metro line added in June 2007.

This example is the most illustrative one, as the authors provide a clear breakdown of what work went into proving both the abstract and the concrete models. They have generated over 43 thousand proof obligations, 97% of which were proven automatically. While it is a quite good result, at this scale it leaves over 700 POs to be proven by hand, and according to the authors, their average rate was proving manually around 15 obligations

per day. It demonstrates just how time consuming it is to work with a tool that isn't as automatic as one claims to be.

More importantly, the authors had the need for 290 new proof rules. They have discovered that the Predicate Prover in AtelierB was very useful in validating them. 84% have been done by the tool. It is a pity that more details on this aren't provided.

In the formal model of railway stations proposed by K. Reichl *et al.* [4], an evolution of B-method called Event-B is used, as it allows for modelling systems as a whole, including hardware. Nevertheless the underpinning theory and relying on first order logic and set theory is common to both B and Event-B. Event-B also requires Rodin tool, rather than AtelierB, however in their work, the authors have used AtelierB prover in addition to Rodin's one.

B. Available models

C. Methods for verifying proof rules

D. Case studies

[Verification of ProB goes here]

III. PROJECT AIMS

A secondary aim of the project is to understand and assess the limitations of this approach to improve the functionality of automated provers.

It is expected that over the course of this project, new questions and ideas will arise. Some, but not all may be pursued, while others will be identified as areas for further research.

A. Choice of Scenarios

To recognize the most commonly problematic proof obligations, we will collect a few scenarios created by various research groups or companies. This will ensure that the issues with the prover will not be user-specific.

The most important criteria in choosing third party models will be created using only B-method (and not extensions to it, such as Event-B), and that they will be well-documented, especially in terms of tools used for verification.

As it has been identified in the literature review, the industry that most commonly uses the B-method in practice is Railway, and there are models available online [cite]. However, it is well within the scope of this project to assess if there are problems common to different scenarios.

Thus, the railway industry will be the primary focus, however we will compare the improvements made across a range of scenarios, not limited to this area.

B. Metrics

C. Expected learning outcomes

D. Appropriateness of Research Methods

IV. PROJECT MANAGEMENT

A. Methodology

B. Timeline

Key dates, as listed by the CS907 Dissertation Project website, are:

- **19th January:** Registration of dissertation topics
- **16th February:** Submission of project proposals
- **24-28th April:** Project presentations
- **6th July:** Submission of interim reports
- **14th September:** Submission of dissertation

It is also important to take into account dates of terms, which are 9th January to 18th March for the Spring Term, and 24th April to 1st July for the Summer term, with the university examinations commencing on or after the 15th May, and being spread over a period of about two weeks. Therefore, it is to be expected that little progress will be made during Spring Term and especially in May, with the bulk of the work being done over holiday and after the examination period.

The Gantt chart in Fig. X shows an estimate of the project's timeline.

C. Progress

D. Constraints and Risks

1) *Copyrights for AtelierB software:* Atelier B is a closed source project, however it is distributed free of charge, for any purpose including teaching and research. ClearSy does not forbid users from making modifications to their software, however any modified software will be excluded from their maintenance service policy.

2) *Requirement for knowledge outside the subject area:* The B-method relies heavily on first order logic and Zermelo-Fraenkel set theory, and especially the latter is beyond the scope of the course (MSc in Computer Science). Fortunately, this area has been covered in depth during my previous degree (BA in Mathematics).

3) *Risk of data loss or machine failure:* A GitHub repository has been set up to contain a remote back up of the work done so far, thus also safeguarding against theft or loss of data storage devices. It has the additional benefits of allowing work from multiple machines, and convenient tracking of changes. The address of the repository is: <https://github.com/agata-borkowska/dissertation>.

This is a reasonable precaution we have deemed it to be sufficient, provided the changes are committed whenever significant progress has been made.

4) *Time estimates:* This project is intended to be flexible, and following an agile approach. It is fully expected that over the course of this project, new questions will occur, and we may or may not choose to pursue them. Thus, it should be noted that the presented timeline is very rough. There are however a couple of milestones, such as the end of performing a review of existing methods and scenarios, and the beginning of benchmarking, which should not be postponed. To this end, time to work on the project will be scheduled and adhered to, and progress will be reported to the Supervisor.

Additionally, regular meetings with the Supervisor will aid with keeping it on track, Her advice will also be helpful in assessing if the pace of work is sufficient.

Therefore, mistakes in the estimates of time taken to complete tasks are not a severe issue.

V. CONCLUDING REMARKS

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