

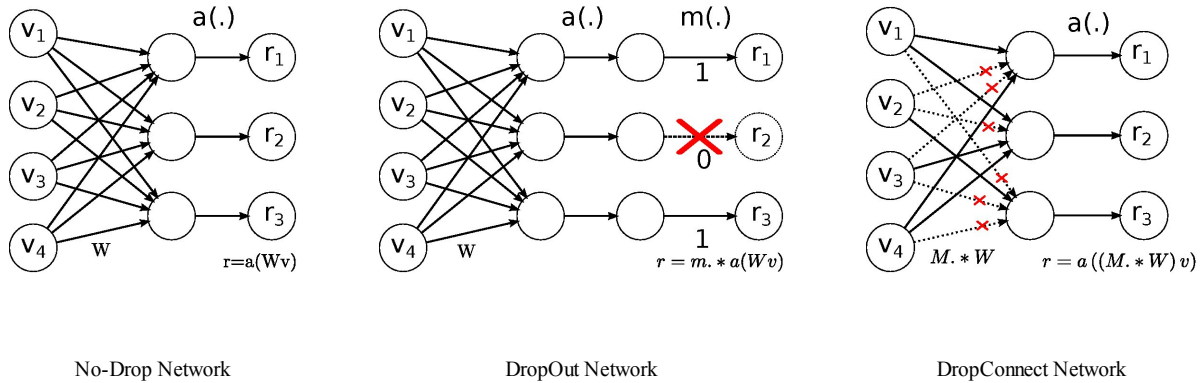
Regularization of Neural Networks using DropConnect

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Introduction

We introduce DropConnect, a generalization of Hinton's [Dropout](#) for regularizing large fully-connected layers within neural networks. When training with Dropout, a randomly selected subset of activations are set to zero within each layer. DropConnect instead sets a randomly selected subset of *weights* within the network to zero. Each unit thus receives input from a random subset of units in the previous layer. We derive a bound on the generalization performance of both Dropout and DropConnect.



Motivation

Training Network with Dropout:

Each element of a layer's output is kept with probability p , otherwise being set to 0 with probability $1 - p$. If we further assume neural activation function with $a(0) = 0$, such as *tanh* and *relu* (\star is element-wise multiplication):

$$r = m \star a(Wv) = a(m \star Wv)$$

Training Network with DropConnect:

Generalization of Dropout in which each connection, rather than each output unit, can be dropped with probability $1 - p$:

$$r = a((M \star W)v)$$

where M is weight mask, W is fully-connected layer weights and v is fully-connected layer inputs.

Mixture Model Interpretation

DropConnect Network is a mixture model of $2^{|M|}$ neural network classifiers $f(x; \theta, M)$:

$$o = \mathbf{E}_M[f(x; \theta, M)] = \sum_M p(M) f(x; \theta, M)$$

It is not hard to show stochastic gradient descent with random mask M for each data improves the lower bound of mixture model

Inference

Dropout Network Inference (mean-inference):

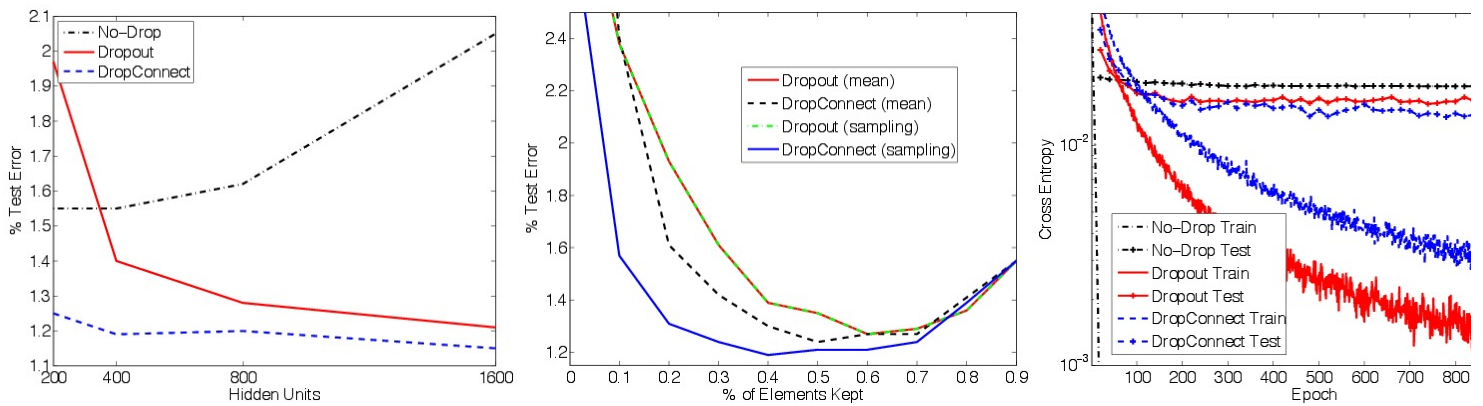
$$\mathbf{E}_M[a(M \star W)v] \approx a(\mathbf{E}_M[(M \star W)v]) = a(pWv)$$

DropConnect Network Inference (sampling):

$\mathbf{E}_M[a(M \star W)v] \approx \mathbf{E}_u[a(u)]$ where $u \sim \mathcal{N}(pWv, p(1-p)(W \star W)(v \star v))$, i.e. each neuron activation are approximated by a Gaussian distribution via moment matching.

Experiment Results

Experiment with [MNIST](#) dataset using 2-layer fully connected neural network:



(a) Prevent overfitting as the size of connected layers increase

(b) Varying the drop-rate in a 400-400 network

(c) Convergence properties of the train/test set

Evaluate DropConnect model for regularizing deep neural network of various popular image classification datasets:

Image Classification Error(%) of DropConnect v.s. Dropout

DataSet	DropConnect	Dropout	Previous best result(2013)
MNIST	0.21	0.27	0.23
CIFAR-10	9.32	9.83	9.55
SVHN	1.94	1.96	2.80
NORB-full-2fold	3.23	3.03	3.36

Implementation Details

Performance comparison between different implementation of DropConnect layer on NVidia GTX 580 GPU relative to 2.67Ghz Intel Xeon (compiled with -O3 flag). Input and output dimension is 1024 and mini-batch size is 128 (You might not get exactly the same number with my code on your machine):

Efficient Implementation of DropConnect

Implementation	Mask Weight	Total Time(ms)	Speedup
CPU	float	3401.6	1.0 X
CPU	bit	1831.1	1.9 X
GPU	float(global memory)	35.0	97.2 X
GPU	float(tex1D memory)	27.2	126.0 X
GPU	bit(tex2D memory)	8.2	414.8 X

Total Time includes: fprop, bprop and update for each mini-batch

Thus, efficient implementation: 1) encode connection information in bits 2) Aligned 2D memory bind to 2D texture for fast query connection status. Texture memory cache hit rate of our implementation is close to 90%.

Why DropConnect Regularize Network

Rademacher Complexity of Model: $\max |W_s| \leq B_s, \max |W| \leq B, k$ is the number of classes, $\hat{R}_\ell(\mathcal{G})$ is the Rademacher complexity of the feature extractor, n and d are the dimensionality of the input and output of the DropConnect layer respectively:

$$\hat{R}_\ell(\mathcal{F}) \leq p(2\sqrt{k}dB_s n\sqrt{d}B_h) \hat{R}_\ell(\mathcal{G})$$

Special Cases of p :

1. $p = 0$: the model complexity is zero, since the input has no influence on the output.
2. $p = 1$: it returns to the complexity of a standard model.
3. $p = 1/2$: all sub-models have equal preference.

Reference

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International Conference on Machine Learning 2013 ([10 pages PDF](#)) [Supplementary Material](#) [Slides](#)

[CUDA code](#) (code Sep-20-2013 update [changelog](#))

Reproduce Experiment Results

The full project code is [here](#) in case you want to repeat some of the experiments in our paper. Please refer to [here](#) for how to compile the code. Some examples to run the code is [here](#). Unfortunately, the code is a little bit unorganized and I might clean up in the future. Important trained models and config files are also available [here](#) (Updated Dec-16-2013).

Zygmunt from [FastML](#) has successfully reproduce experiment result on CIFAR-10 on [Kaggle CIFAR-10 leaderboard](#) in his artical [Regularizing neural networks with dropout and with DropConnect](#).

A summary of question and my answer for hacking my uncleaned code is [Here](#) .