Class Test -II (JAN, - 2023) 2AMRCI- Applied Mathematics -II (B.E. lyr ETC A, B)

Time: 70 min.

Maximum Marks:

Note: Attempt all four questions. Questions must be solved at one place. Each step should clear and well defined.

Solve the differential equation $\frac{d^2y}{dx^2} - 2\frac{dy}{dx} + 2y = \sinh x + \sin \sqrt{2}x$. Q.1

Q.2 Solve the differential equation
$$x^2 \frac{d^2y}{dx^2} - 3x \frac{dy}{dx} + 5y = x \log x$$
.

Form the Partial differential equations Q.3

(i)
$$x^2 + y^2 + (z - a)^2 = b^2$$
 (ii) $f(x + y + z, x^2 + y^2 + z^2) = 0$.

Q.4 Find the general solution of $x(z^2 - y^2) \frac{\partial z}{\partial x} + y(x^2 - z^2) \frac{\partial z}{\partial y} = z(y^2 - z^2)$.

BE -I (E & I) CLASS TEST - 2 2AMRC1: Applied Mathematics-II

Time: 70 min

Note: Attempt any FOUR questions.

Max Marks: 20

Q1) Derive the partial differential equation by eliminating the arbitrary function:

$$z = (x + y) f(x^2 - y^2)$$

- Q2) Solve the following equation: $(D^3 = 2D^2D^4)z = 2e^{2x} + 3x^2y$
- Q3) Solve by the method of separation of variables: du/dx = 2 du/dt + u, where $u(x, 0) = 6e^{-3x}$
- Q4) Find all eigen values and eigen vectors of the matrix $A = \begin{bmatrix} 2 & -1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2 \end{bmatrix}$.
- Q5) Verify Cayley-Hamilton theorem for the matrix $A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 5 \\ 3 & 5 & 6 \end{bmatrix}$ and

express $A^8 - 11A^7 - 4A^6 + A^5 + A^4 - 11A^3 - 3A^2 + 2A + 1$ as a quadratic polynomial in Λ .