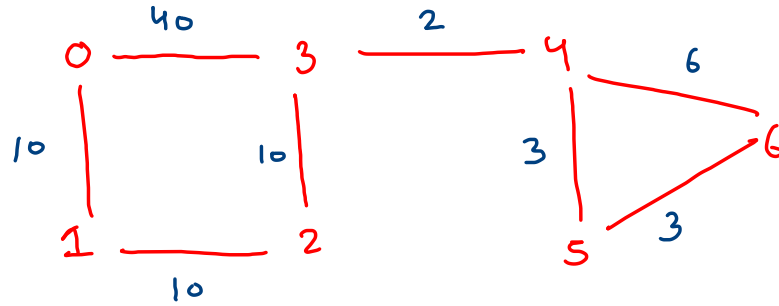


graphs
|
vertices
|
edges



undirected
weighted
graph

$$V = 7$$

$$0, 1, 2, 3, 4, 5, 6$$

$$E = 8$$

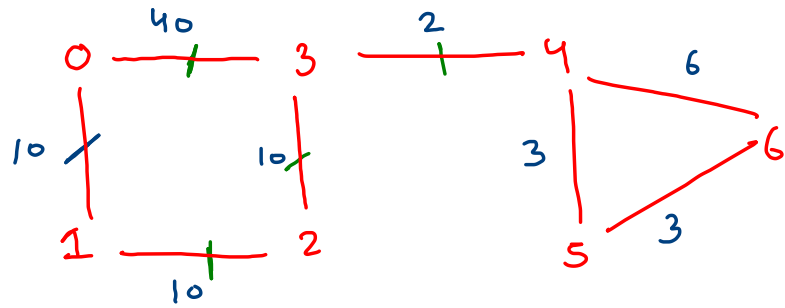
$$0-1, 0-3, \dots$$

$$src = 0$$

$$dest = 6$$

(i) min stations

(ii) shortest path cost

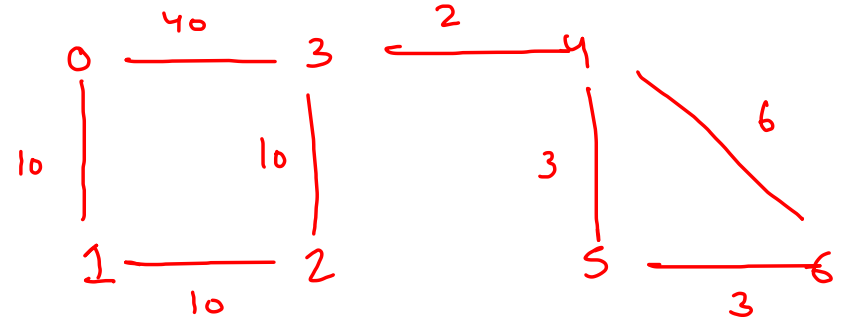


Adjacency matrix

	0	1	2	3	4	5	6
0	∞	10	∞	40	∞	∞	∞
1	10	∞	10	∞	∞	∞	∞
2	∞	10	∞	10	∞	∞	∞
3	40	∞	10	∞	2	∞	∞
4	∞	∞	∞	2	∞	3	6
5	∞	∞	∞	∞	3	∞	3
6	∞	∞	∞	∞	6	3	∞

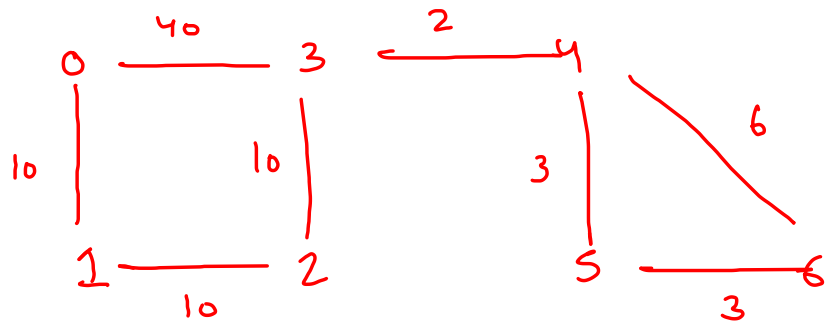
	0	1	2	3	4	5	6
0	∞	10	∞	40	∞	∞	∞
1	10	∞	10	∞	∞	∞	∞
2	∞	10	∞	10	∞	∞	∞
3	40	∞	10	∞	2	∞	∞
4	∞	∞	∞	2	∞	3	6
5	∞	∞	∞	∞	3	∞	3
6	∞	∞	∞	∞	6	3	∞

\Rightarrow



\rightarrow waste of space

$\rightarrow V \leq 1000$



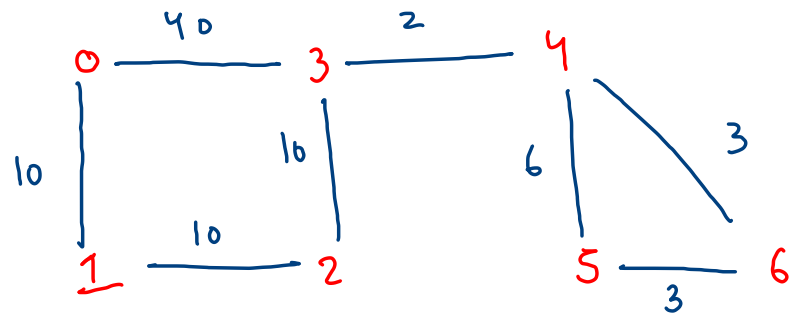
Adjacency list :

`ArrayList < Edge > [] graph;`

0	→ (0-3 @ 40), (0-1 @ 10)
1	→ (1-0 @ 10), (1-2 @ 10)
2	→ (2-1 @ 10), (2-3 @ 10)
3	→ (3-0 @ 40), (3-2 @ 10), (3-4 @ 2)
4	→ (4-3 @ 2), (4-5 @ 3), (4-6 @ 6)
5	→ (5-4 @ 3), (5-6 @ 3)
6	→ (6-4 @ 6), (6-5 @ 3)

✓
✓
✓
✓
✓
✓
✓
0 -> 0 - 1 @ 10, 0 - 3 @ 40,
1 -> 1 - 0 @ 10, 1 - 2 @ 10,
2 -> 2 - 1 @ 10, 2 - 3 @ 10,
3 -> 3 - 0 @ 40, 3 - 2 @ 10, 3 - 4 @ 2,
4 -> 4 - 3 @ 2, 4 - 5 @ 6, 4 - 6 @ 3,
5 -> 5 - 4 @ 6, 5 - 6 @ 3,
6 -> 6 - 4 @ 3, 6 - 5 @ 3,

```
addEdge(graph,0,1,10);  
addEdge(graph,0,3,40);  
addEdge(graph,1,2,10);  
addEdge(graph,2,3,10);  
addEdge(graph,3,4,2);  
addEdge(graph,4,5,6);  
addEdge(graph,4,6,3);  
addEdge(graph,5,6,3);
```



```

public static void display(ArrayList<Edge>[] graph) {
    for(int v=0; v < graph.length; v++) {
        System.out.print(v + " -> ");
        for(int e=0; e < graph[v].size(); e++) {
            Edge edge = graph[v].get(e);
            System.out.print(edge.src + " - " + edge.nbr + " @ " + edge.wt + ", ");
        }
        System.out.println();
    }
}

```

0	→ (0-3 @ 40), (0-1 @ 10)
1	→ (1-0 @ 10), (1-2 @ 10)
2	→ (2-1 @ 10), (2-3 @ 10)
3	→ (3-0 @ 40), (3-2 @ 10), (3-4 @ 2)
4	→ (4-3 @ 2), (4-5 @ 3), (4-6 @ 6)
5	→ (5-4 @ 3), (5-6 @ 3)
6	→ (6-4 @ 6), (6-5 @ 3)

0 → (0-3 @ 40), (0-1 @ 10)

1 → (1-0 @ 10), (1-2 @ 10)

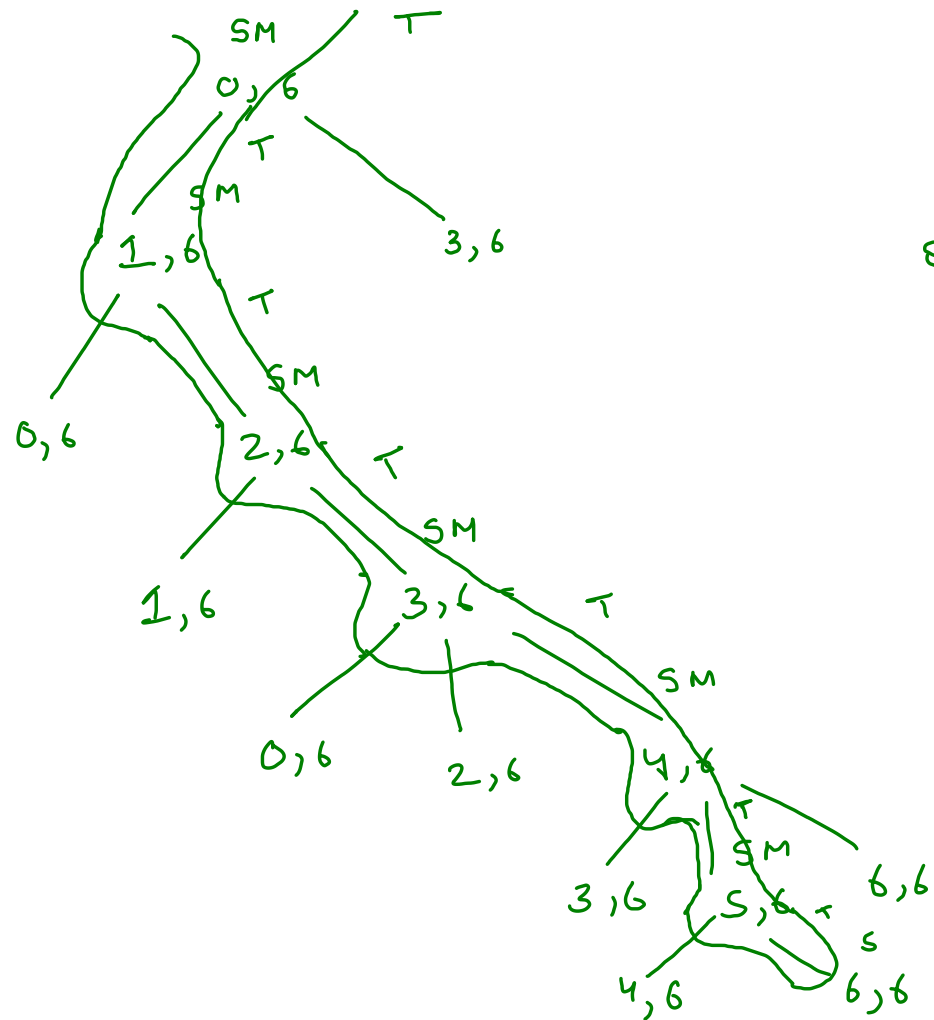
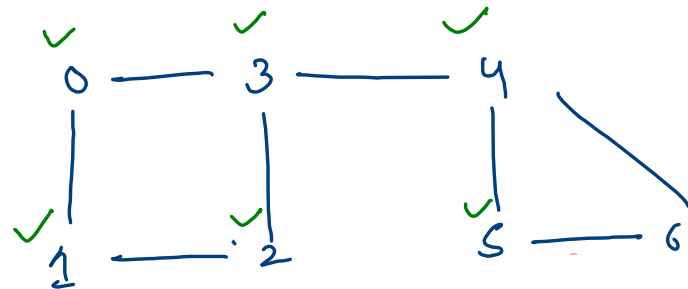
2 →

haspath

```

public static boolean hasPath(ArrayList<Edge>[] graph, int src, int dest, boolean[] vis) {
    S [ if(src == dest) {
        return true;
    }
    MC vis[src] = true;
    nbr [ for(Edge edge : graph[src]) {
        int nbr = edge.nbr;
        if(vis[nbr] == false) {
            boolean hpNtoD = hasPath(graph, nbr, dest);
            if(hpNtoD == true) {
                return true;
            }
        }
    }
    return false;
}

```



src = 0

dest = 6

hasPath

src = 4

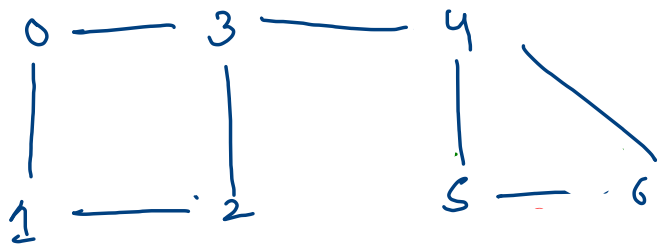
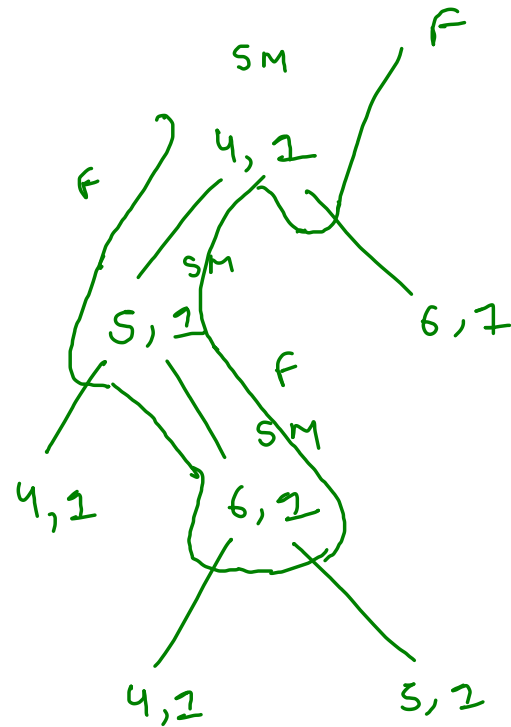
dest = 1

```

public static boolean hasPath(ArrayList<Edge>[] graph, int src, int dest, boolean[] vis) {
    s[
    if(src == dest) {
        return true;
    }
    m[ vis[src] = true;
    for(Edge edge : graph[src]) {
        int nbr = edge.nbr;
        if(vis[nbr] == false) {
            boolean hpNtoD = hasPath(graph, nbr, dest, vis);
            if(hpNtoD == true) {
                return true;
            }
        }
    }
    return false;
}

```

nbr




```

S | if(src == dest) {
  |   System.out.println(psf);
  |   return;
M | vis[src] = true;
  |
  | for(Edge edge : graph[src]) {
  |   int nbr = edge.nbr;
  |
  |   if(vis[nbr] == false) {
  |     printAllPaths(graph, nbr, dest, psf + nbr, vis);
  |   }
  | }

```

0 1 2 3 4 5 6

0 1 2 3 4 6

src = 0

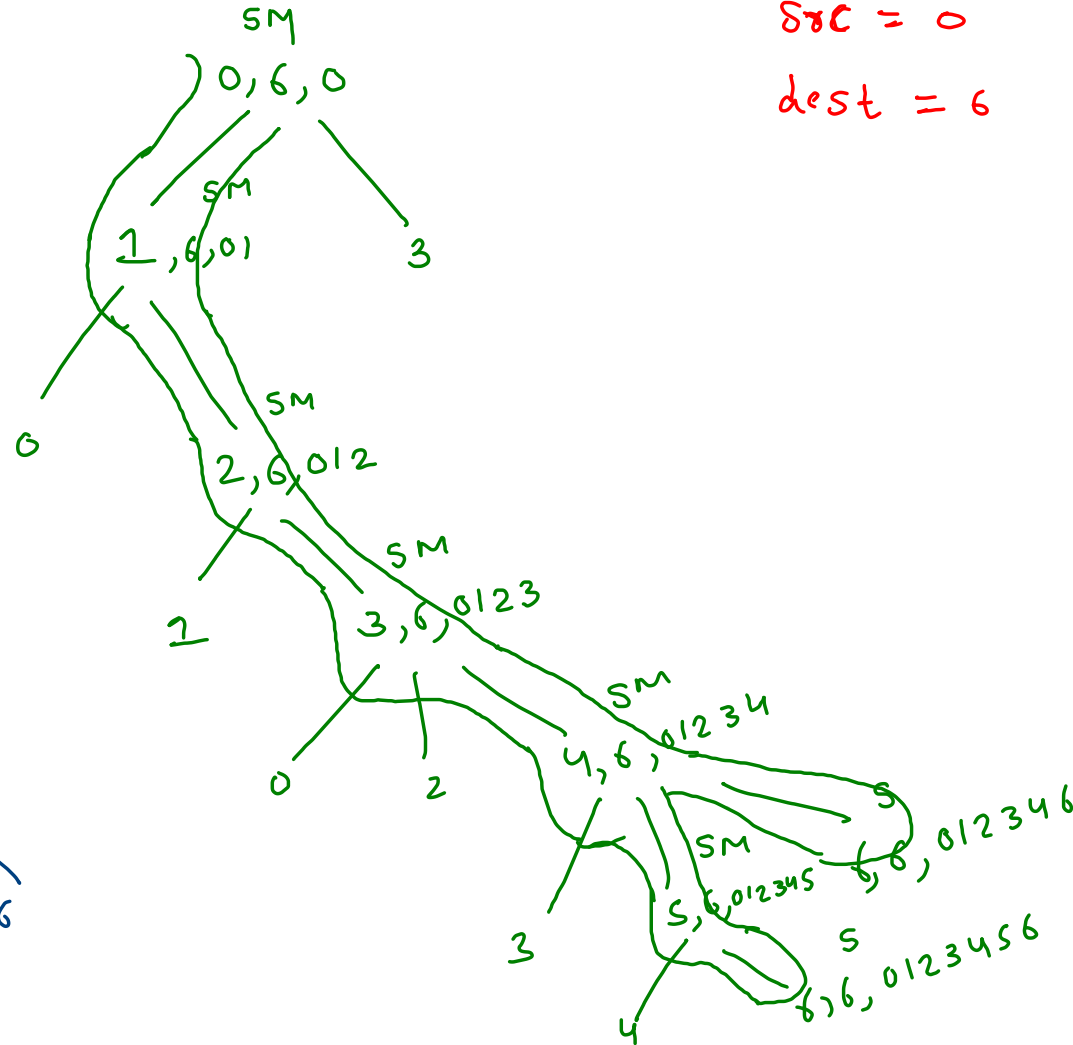
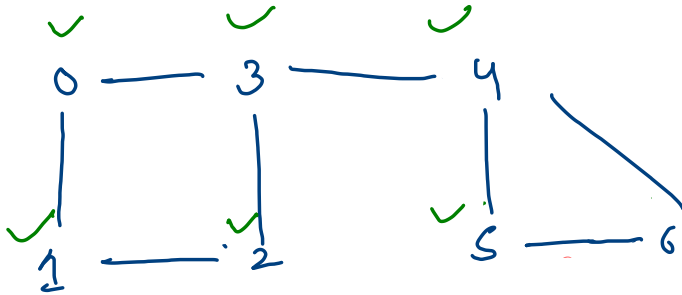
dest = 6

0 1 2 3 4 5 6

0 1 2 3 4 6

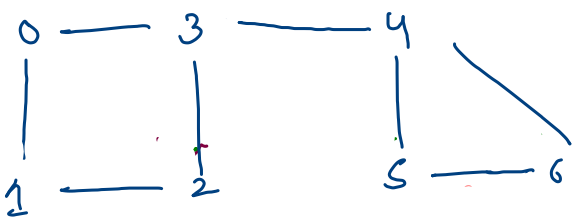
0 3 4 5 6

0 3 4 6

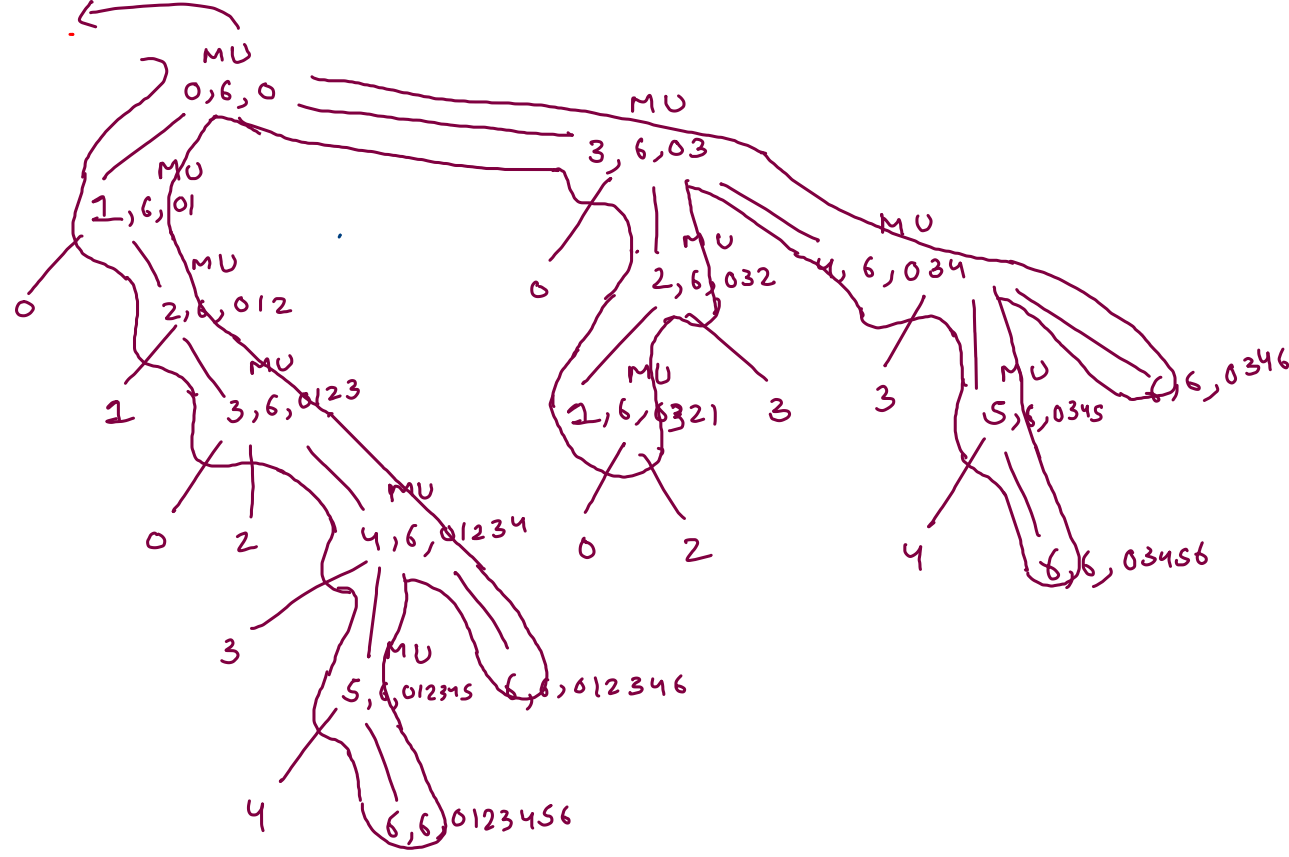


```
S | if(src == dest) {  
  |   System.out.println(psf);  
  |   return;  
M | }  
  |  
  | vis[src] = true;  
nbr |  
  | for(Edge edge : graph[src]) {  
  |   int nbr = edge.nbr;  
  |  
  |   if(vis[nbr] == false) {  
  |     printAllPaths(graph,nbr,dest,psf + nbr,vis);  
  |   }  
  | }  
V | vis[src] = false;
```

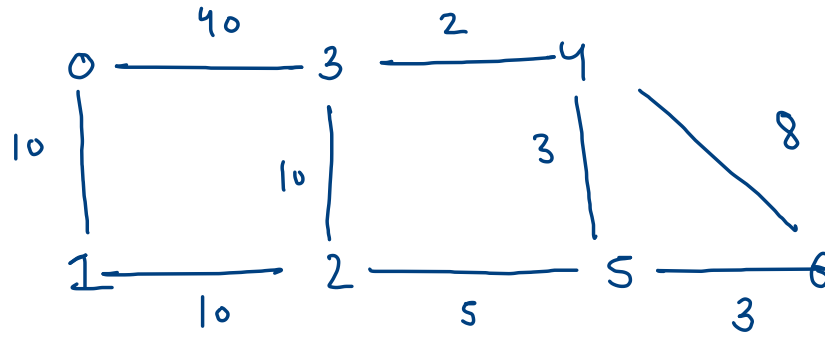
0123456
012346
03456
0346



src = 0
dest = 6



0 1 10
 1 2 10
 2 3 10
 0 3 40
 3 4 2
 4 5 3
 5 6 3
 4 6 8
 2 5 5



src = 0
 dest = 6

0 1 2 3 4 5 6 @ 38

0 1 2 3 4 6 @ 40

0 1 2 5 6 @ 28

0 1 2 5 4 6 @ 36

0 3 4 6 @ 50

0 3 4 5 6 @ 48

0 3 2 5 4 6 @ 66

0 3 2 5 6 @ 58

- ✓ Smallest Path = 01256@28
- ✓ Largest Path = 032546@66
- ✓ Just Larger Path than 30 = 012546@36
- ✓ Just Smaller Path than 30 = 01256@28
- ✓ 4th largest path = 03456@48

0 1 2 3 4 5 6 @ 38

0 1 2 3 4 6 @ 40

0 1 2 5 6 @ 28

0 1 2 5 4 6 @ 36

0 3 4 6 @ 50

0 3 4 5 6 @ 48

0 3 2 5 4 6 @ 66

0 3 2 5 6 @ 58

$\infty \xrightarrow{F} 66$ largest

$66 \xrightarrow{F} 58$ (2nd L)

$58 \xrightarrow{F} 50$ (3rd L)

$50 \xrightarrow{F} 48$ (4th L)