

n = no. of elements
in pq.

add $\rightarrow \log n$

remove $\rightarrow \log n$

peek $\rightarrow O(1)$

25

6

19

8

7

24

15

39

11

```
for(int i=0; i < n; i++) {  
    pq.add(arr[i]);  
}
```

$\rightarrow n \log n$

```
int[] ans = new int[k];  
int idx = k-1;
```

+

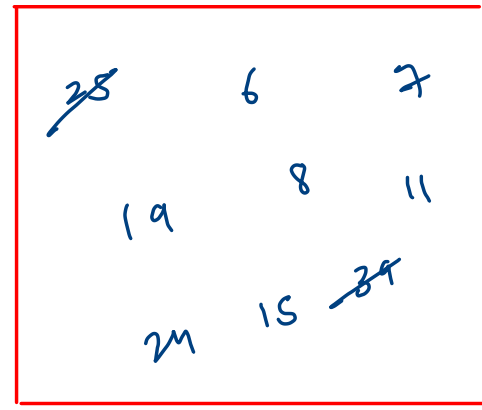
```
while(k-- > 0) {  
    ans[idx] = pq.remove();  
    idx--;  
}
```

$\rightarrow k \log n$

+

```
for(int i=0; i < ans.length; i++) {  
    System.out.println(ans[i]);  
}
```

$\rightarrow k$



24	25	39
----	----	----

$n \log k$

$k = 3$

25 6 19 8 7 24 15 39 11
~~↑~~ ~~↑~~ ~~↑~~ ~~↑~~ ~~↑~~ ~~↑~~ ~~↑~~ ~~↑~~ ~~↑~~

24

```
for(int i=0; i < arr.length; i++) {  
    if(pq.size() < k) {  
        pq.add(arr[i]);  
    }  
    else {  
        if(pq.peek() < arr[i]) {  
            pq.remove();  
            pq.add(arr[i]);  
        }  
    }  
}
```

$n \log k$

```
//print ans  
while(pq.size() > 0) {  
    System.out.println(pq.remove());  
}
```

$k \log k$

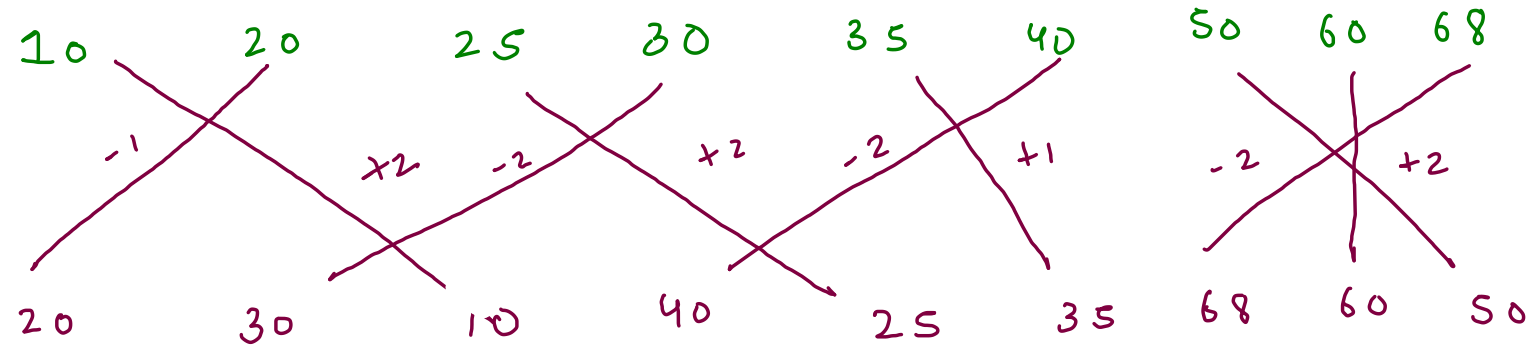
24 25 39

25 24
39

K-sorted array

$K = 2$

$K = 2$



Input: 20 30 10 40 25 35 68 60 50

Input: 20 30 10 40 25 35 50 68 60

10 20 25 30 35 40 50 60 68

~~50, 60~~
~~68~~

```
PriorityQueue<Integer> pq = new PriorityQueue<>();

//fill pq with k+1
for(int i=0; i <= k; i++) {
    pq.add(arr[i]);
}

for(int i=k+1; i < arr.length; i++) {
    System.out.println(pq.remove());
    pq.add(arr[i]);
}

//print rem k+1 elements in pq
while(pq.size() > 0) {
    System.out.println(pq.remove());
}
```

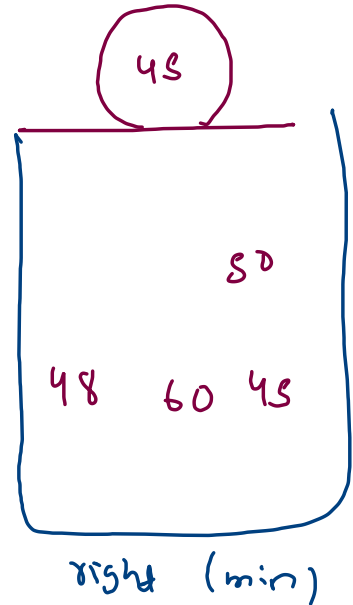
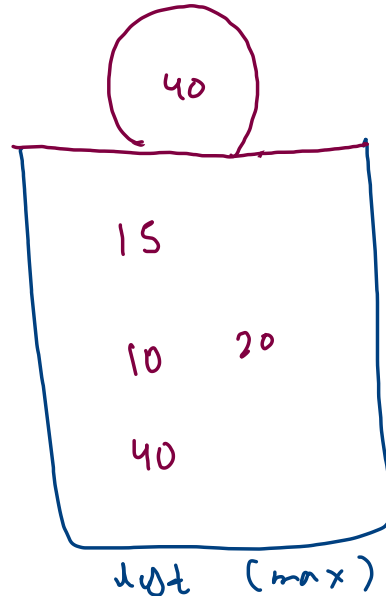
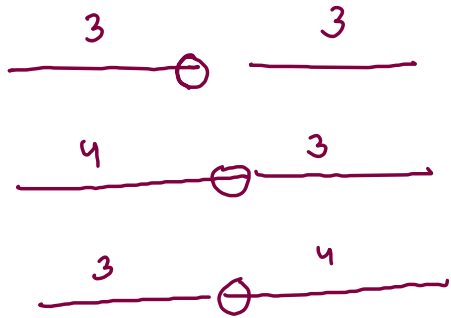
5 9 2 10 1 12 6

mpq. peek() \rightarrow median

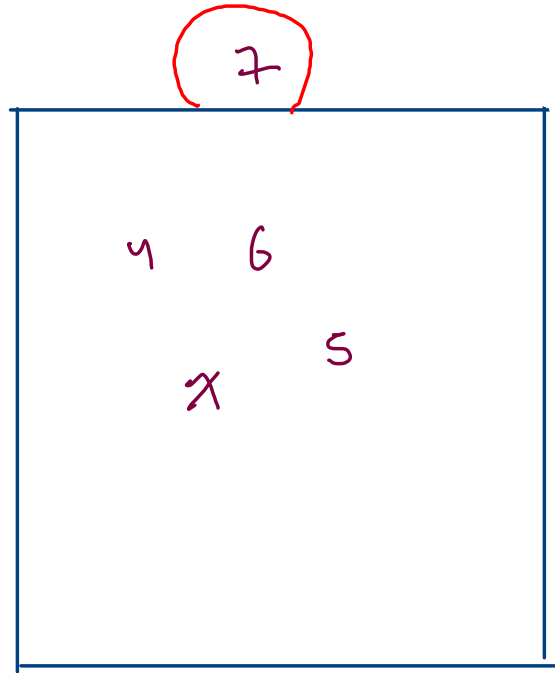
mpq. add() \rightarrow addition

mpq. remove() \rightarrow remove

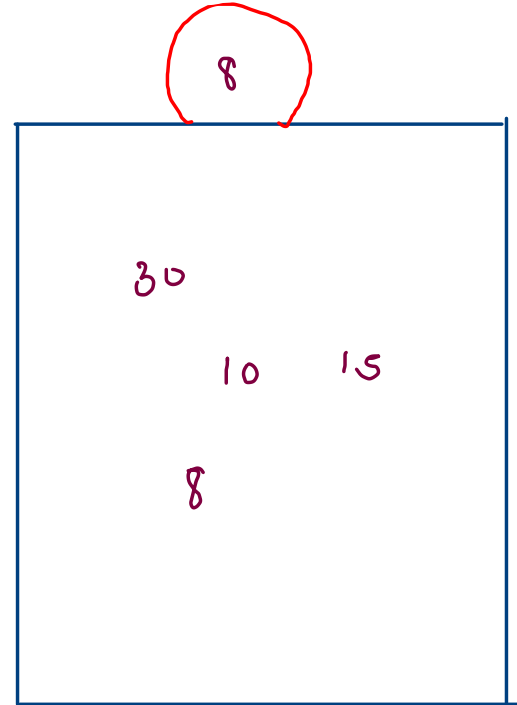
10 15 20 40 45 50 60 48



10 5 15 8 6 4 30 7
~~↑~~ ~~↑~~ ~~↑~~ ~~↑~~ ~~↑~~ ~~↑~~ ~~↑~~ ~~↑~~ °



left (max)



right (min)

```

public void add(int val) {
    if(size() == 0) {
        left.add(val);
    }
    else if(left.size() > 0 && val <= left.peek()) {
        left.add(val);
    }
    else{
        right.add(val);
    }

    //balance
    if(left.size() - right.size() == 2) {
        //remove from left, add in right
        right.add(left.remove());
    }
    else if(right.size() - left.size() == 2) {
        //remove from right, add in left
        left.add(right.remove());
    }
}

```

```

public int remove() {
    if(size() == 0) {
        System.out.println("Underflow");
        return -1;
    }

    if(left.size() >= right.size()) {
        return left.remove();
    }
    else {
        return right.remove();
    }
}

```

```

public int peek() {
    if(size() == 0) {
        System.out.println("Underflow");
        return -1;
    }

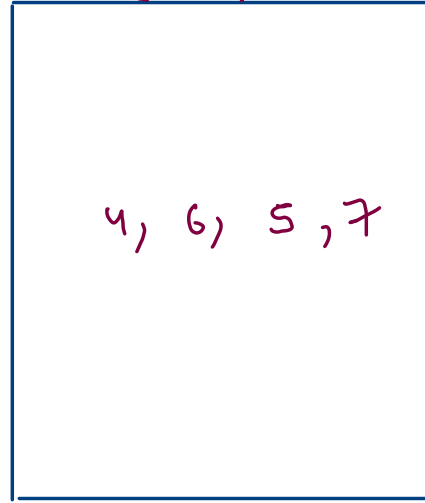
    if(left.size() >= right.size()) {
        return left.peek();
    }
    else {
        return right.peek();
    }
}

```

10 5 15 8 6 4 30 7 20 40

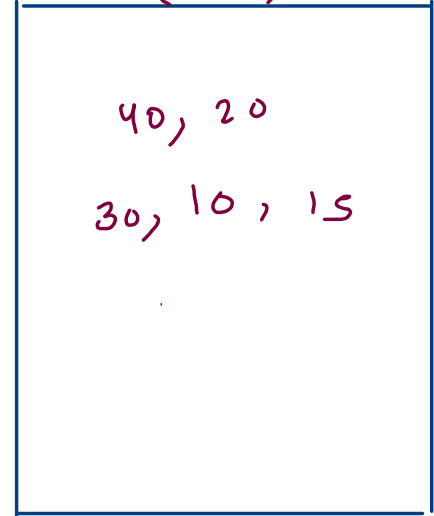
↗ ↗ ↗ ↗ ↗ ↗ ↗ ↗ ↗ ↗

7



left (max)

10



right (min)

k = 4

Pair:

val

idx

li

u ₀	→	2	5	7	9	11
u ₁	→	1	3	13	19	
u ₂	→	5	12	16	18	20
u ₃	→	4	6	10		

(val - idx - li)

PO

md → 1 2 3 4 5 5 6 7 9 10 11

(2 - 0 - 0)	(5 - 1 - 0)
(1 - 0 - 1)	(3 - 1 - 1)
(5 - 0 - 2)	(13 - 2 - 1)
(4 - 0 - 3)	(7 - 2 - 8)
(6 - 1 - 3)	(12 - 1 - 2)
(10 - 2 - 3)	(9 - 3 - 0)
(11 - 4 - 0)	

$l_0 \rightarrow$ ~~2~~ ~~7~~ ~~9~~ ~~11~~ .
 $l_1 \rightarrow$ ~~1~~ ~~3~~ ~~19~~ .
 $l_2 \rightarrow$ ~~5~~ ~~12~~ ~~16~~ ~~18~~ ~~20~~ .
 $l_3 \rightarrow$ ~~4~~ ~~6~~ ~~10~~ .

$(val - idx - li)$

```

//fill pq with each list's first element
for(int i=0; i < lists.size(); i++) {
    Pair p = new Pair(lists.get(i).get(0),0,i);
    pq.add(p);
}

while(pq.size() > 0) {
    Pair top = pq.remove();
    rv.add(top.val);

    int nli = top.li;
    int nidx = top.idx + 1;

    if(nidx < lists.get(nli).size()) {
        int nval = lists.get(nli).get(nidx);
        Pair p = new Pair(nval,nidx,nli);
        pq.add(p);
    }
}
  
```

1 2 3 4 5 6
 7 9 10 11 12 16
 18 19 20

merged list.

~~2 - 0 - 0~~ ~~3 - 2 - 1~~
~~1 - 0 - 1~~ ~~7 - 2 - 0~~
~~5 - 0 - 2~~ ~~19 - 2 - 1~~
~~4 - 0 - 3~~ ~~6 - 2 - 3~~
~~12 - 1 - 2~~ ~~10 - 2 - 3~~
~~11 - 3 - 6~~ ~~9 - 2 - 6~~
~~18 - 3 - 2~~ ~~16 - 2 - 2~~
~~20 - 4 - 2~~

