# Report of Experiment ExpC. 3-Symmetry: Replay.

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**Exploratory Analysis** 

#### **Abstract**

This experiment tests exact replication and stochastic replication for xegaRun of R-package xega. In the experiment, the 3-symmetry problem is solved by grammar-based genetic programming for fixed seeding and for Rs system seeding (option replay of xegaRun).



#### Contents I

- 1 Design of Experiment
- 2 Exploratory Analysis
  - Do we **always** solve the 3 symmetry problem?
  - Time of Treatments in Seconds
  - Number of Generations of Treatments
- 3 Testing of Effects
  - Exact Replicability
  - Stochastic Replicability
- 4 A Summary
- 5 B Treatments
  - Treatment BoolT1SGPreplayXIII
  - Treatment BoolT1SGPreplayXIX
  - Treatment BoolT1SGPreplayZa



#### Contents II

■ Treatment BoolT1SGPreplayZb

6 C xega

#### **Definitions**

Design of Experiment

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**Exact replicability** of a computational experiment means that the experiment procudes in each trial **identical** numerical result. **Stochastic replicability** of a computational experiment means that the experiment procudes in each trial the same expected result.



The purpose of this computational experiment is to show the difference between **exact** and **stochastic** replicability of the experiment.

The **problem environment** is the 3-symmetry problem: Finding a boolean expression (with and, or, and not) which is TRUE for symmetric 3-bit strings.

The **solution method** is grammar-based genetic programming (option algorithm="sgp" of xegaRun). The **solver** used is xegaRun from the R-package xega.

The experiment consists of 4 treatments, two for each choice of seeding.



#### Common Parameters of Experiment ExpC

|                       | Parameter Value    |
|-----------------------|--------------------|
| Experiment            | ExpC               |
| Problem.Environment   | 3-Symmetry Problem |
| Optimize              | Minimize!          |
| Algorithm             | sgp                |
| Max.Depth.of.DTs      | 7                  |
| Grammar               | AndOrNotTuned1.txt |
| Evaluation.Method     | Deterministic      |
| Execution. $Model$    | MultiCore          |
| Verbose               | 1                  |
| Semantics             | byValue            |
| Report.Eval.Errors    | TRUE               |
| Termination.Condition | AbsoluteError      |
| Termination.Eps       | -0.1               |
| Worst Fitness         | -8                 |
| Gene.Map              | Bin2Dec            |
|                       |                    |

Table: Common Parameters of Experiment ExpC (Part 1)



#### Common Parameters of Experiment ExpC

| -                 | Parameter Value |
|-------------------|-----------------|
| Init.Gene         | InitGene        |
|                   |                 |
| Codons            | 120             |
| Codon.Precision   | LCM             |
| Population.Size   | 50              |
| Max.Generations   | 5000            |
| Crossover.Rate    | 0.2             |
| Mutation.Rate     | 0.4             |
| IV.Crossover.Rate | Const           |
| Crossover.Rate.2  | 0.4             |
| IV.Mutation.Rate  | Const           |
| Mutation.Rate.2   | 0.8             |

Table: Common Parameters of Experiment ExpC (Part 2)



# Parameters of Treatments of Experiment ExpC

|   | Treatment           | Trials | Replay |
|---|---------------------|--------|--------|
| 1 | BoolT1SGPreplayXIII | 50     | 13     |
| 2 | BoolT1SGPreplayXIX  | 50     | 19     |
| 3 | BoolT1SGPreplayZa   | 100    | 0      |
| 4 | BoolT1SGPreplayZb   | 100    | 0      |

Table: Parameters of Treatments of Experiment ExpC



# The Production Table of Experiment ExpC

|    | LHS       | RHS  |
|----|-----------|--|
| 1  | <fe></fe> | <f0></f0>  |
| 2  | <fe $>$   | <f1>(<fe>)</fe></f1>   |
| 3  | <fe $>$   | <f2>(<fe>,<fe>)</fe></fe></f2>                                   |
| 4  | <fe $>$   | OR(AND( <f0>,<f0>),AND(NOT(<f0>),NOT(<f0>)))</f0></f0></f0></f0> |
| 5  | <f2></f2> | ÓR   |
| 6  | <f2></f2> | AND  |
| 7  | <f2></f2> | OR   |
| 8  | <f1></f1> | NOT  |
| 9  | <f0></f0> | D1   |
| 10 | <f0></f0> | D2   |
| 11 | <f0></f0> | D3   |

Table: The Production Table of Experiment ExpC



Treatments 1 and 2 test the seeding of the random number generator in xegaRun:

Repetition of a treatment should produce exactly the same result.

But different seeds should lead to different results.

Treatments 3 and 4 use the system seed of the random number generator:

Repetitions produce random results.

We expect that for enough trials both treatments have the same mean performance.



Do we always solve the 3 symmetry problem?

#### Observation

In this experiment, the 3-symmetry problem is **always** correctly solved.

**Evidence:** In all trials of all treatments the optimal fitness of 0 was reached. See next table.



Do we always solve the 3 symmetry problem?

# Fitness (Number of errors).

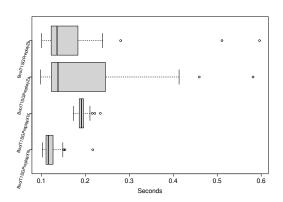
|    | Treatment           | Trials | Variable | min  | mean | sd   | max  |
|----|---------------------|--------|----------|------|------|------|------|
| 1  | BoolT1SGPreplayXIII | 50     | Fitness  | 0.00 | 0.00 | 0.00 | 0.00 |
| 5  | BoolT1SGPreplayXIX  | 50     | Fitness  | 0.00 | 0.00 | 0.00 | 0.00 |
| 9  | BoolT1SGPreplayZa   | 100    | Fitness  | 0.00 | 0.00 | 0.00 | 0.00 |
| 13 | BoolT1SGPreplayZb   | 100    | Fitness  | 0.00 | 0.00 | 0.00 | 0.00 |

Table: Fitness (Number of errors).



B Treatments

### 3-Symmetry: Replay.



# Time (s).

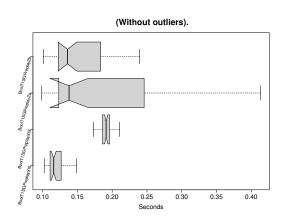
|    | Treatment           | Trials | Variable | min  | mean | sd   | max  |
|----|---------------------|--------|----------|------|------|------|------|
| 2  | BoolT1SGPreplayXIII | 50     | Seconds  | 0.10 | 0.12 | 0.02 | 0.22 |
| 6  | BoolT1SGPreplayXIX  | 50     | Seconds  | 0.17 | 0.19 | 0.01 | 0.23 |
| 10 | BoolT1SGPreplayZa   | 100    | Seconds  | 0.10 | 0.18 | 0.11 | 0.58 |
| 14 | BoolT1SGPreplayZb   | 100    | Seconds  | 0.10 | 0.16 | 0.08 | 0.60 |

Table: Time (s).



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# 3-Symmetry: Replay.



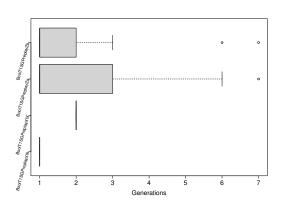
#### Conclusion

The execution time (in seconds) does not allow to identify deterministic results, because it may depend on other system activity e.g. I/O operations.

**Evidence:** The time variation in execution time for all treatments.



# 3-Symmetry: Replay.





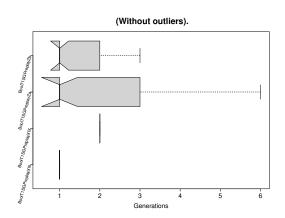
#### Generations

|    | Treatment           | Trials | Variable    | min  | mean | sd   | max  |
|----|---------------------|--------|-------------|------|------|------|------|
| 3  | BoolT1SGPreplayXIII | 50     | Generations | 1.00 | 1.00 | 0.00 | 1.00 |
| 7  | BoolT1SGPreplayXIX  | 50     | Generations | 2.00 | 2.00 | 0.00 | 2.00 |
| 11 | BoolT1SGPreplayZa   | 100    | Generations | 1.00 | 1.84 | 1.43 | 7.00 |
| 15 | BoolT1SGPreplayZb   | 100    | Generations | 1.00 | 1.60 | 1.21 | 7.00 |

Table: Generations



### 3-Symmetry: Replay.



#### Observation

The number of generations needed allows to recognize randomness because of non-zero standard deviation.

The number of generations indicates determinism, if the standard deviation is 0.



Exact Replicability

Distribution of the variable Generations for repeated trials.

|   | Treatment           | Trials | Variable    | min  | mean | sd   | max  |
|---|---------------------|--------|-------------|------|------|------|------|
| 3 | BoolT1SGPreplayXIII | 50     | Generations | 1.00 | 1.00 | 0.00 | 1.00 |
| 7 | BoolT1SGPreplayXIX  | 50     | Generations | 2.00 | 2.00 | 0.00 | 2.00 |

Table: Distribution of the variable Generations for repeated trials.



Exact Replicability

#### Result

Each treatment is deterministic.

#### **Evidence:**

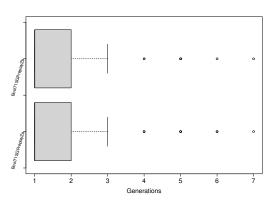
The standard deviation *sd* of each treatment is 0.00 (for any number of trials).

Only 1 solution is found by repeated trials.

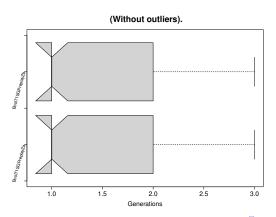
Different seeds (may) result in different results: One treatment needs 1 generation, the other 2 generations to reach the optimum.



Comparing a treatment and its repetition. Hypothesis: Equal expected mean number of generations.



Comparing a treatment and its repetition. Hypothesis: Equal expected mean number of generations.



Distribution of the variable Generations for repeated trials.

|   | Treatment         | Trials | Variable    | min  | mean | sd   | max  |
|---|-------------------|--------|-------------|------|------|------|------|
| 3 | BoolT1SGPreplayZa | 100    | Generations | 1.00 | 1.84 | 1.43 | 7.00 |
| 7 | BoolT1SGPreplayZb | 100    | Generations | 1.00 | 1.60 | 1.21 | 7.00 |

Table: Distribution of the variable Generations for repeated trials.



# Test of $H_0$ : Means of treatments BoolT1SGPreplayZa and BoolT1SGPreplayZb of variable Generations are equal.

For variable Generations of treatments BoolT1SGPreplayZa and BoolT1SGPreplayZb of experiment ExpC:

**Hypothesis 0**: mean(Generations of BoolT1SGPreplayZa)=1.84 - mean(Generations of BoolT1SGPreplayZb)=1.6 is equal to 0.

is tested at a significance level 0.05 against:

 $\label{eq:hypothesis} \begin{tabular}{ll} Hypothesis 1: mean (Generations of BoolT1SGPreplayZa) = 1.84 - mean (Generations of BoolT1SGPreplayZb) = 1.6 is not equal to 0. \end{tabular}$ 

Outliers of treatment BoolT1SGPreplayZa are not removed (coef=0). Outliers of treatment BoolT1SGPreplayZb are not removed (coef=0).

The test-statistic W of the Wilcoxon rank sum test with continuity correction is 5382 with a p-value of 0.259 . Since the p-value 0.259 is above the significance level  $\alpha=0.05$ , for variable Generations of treatments BoolT1SGPreplayZa and BoolT1SGPreplayZb of experiment ExpC **Hypothesis 0**: mean(Generations of BoolT1SGPreplayZa)=1.84 - mean(Generations of BoolT1SGPreplayZb)=1.6 is equal to 0. is **accepted**.



# Test of $H_0$ : Means of treatments BoolT1SGPreplayZa and BoolT1SGPreplayZb of variable Generations are equal.

For variable Generations of treatments BoolT1SGPreplayZa and BoolT1SGPreplayZb of experiment ExpC:

**Hypothesis 0**: mean(Generations of BoolT1SGPreplayZa)=1.39 - mean(Generations of BoolT1SGPreplayZb)=1.29 is equal to 0.

is tested at a significance level 0.05 against:

 $\label{eq:hypothesis} \begin{tabular}{ll} Hypothesis 1: mean (Generations of BoolT1SGPreplayZa) = 1.39 - mean (Generations of BoolT1SGPreplayZb) = 1.29 is not equal to 0. \end{tabular}$ 

12 outliers of treatment BoolT1SGPreplayZa are removed (coef=1.5). 8 outliers of treatment BoolT1SGPreplayZb are removed (coef=1.5).

The test-statistic W of the Wilcoxon rank sum test with continuity correction is 4228 with a p-value of 0.493 . Since the p-value 0.493 is above the significance level  $\alpha=0.05$ , for variable Generations of treatments BoolT1SGPreplayZa and BoolT1SGPreplayZb of experiment ExpC **Hypothesis 0**: mean(Generations of BoolT1SGPreplayZa)=1.39 - mean(Generations of BoolT1SGPreplayZb)=1.29 is equal to 0. is **accepted**.



#### Result

Each treatment produces a sample drawn from the **same** random process.

#### **Evidence:**

The standard deviation sd of each treatment is **not** 0.00 (for any number of trials).

The treatments find 14 and 12 **different, but equivalent** boolean expressions. (See solution tables in section B Treatments.) Different seeds (may) result in **different samples**:

The hypothesis test **supports** the conjecture that the sample means of the variable Generations of the treatments are equal. This implies that the two treatments come from the same rank

This implies that the two treatments come from the same random process.



#### Summary of statistics of experiment ExpC.

|    | Treatment           | Trials | Variable           | min    | mean   | sd    | max    |
|----|---------------------|--------|--------------------|--------|--------|-------|--------|
| 4  | BoolT1SGPreplayXIII | 50     | Evaluations        | 50.00  | 50.00  | 0.00  | 50.00  |
| 8  | BoolT1SGPreplayXIX  | 50     | <b>Evaluations</b> | 100.00 | 100.00 | 0.00  | 100.00 |
| 12 | BoolT1SGPreplayZa   | 100    | <b>Evaluations</b> | 50.00  | 92.00  | 71.68 | 350.00 |
| 16 | BoolT1SGPreplayZb   | 100    | <b>Evaluations</b> | 50.00  | 80.00  | 60.72 | 350.00 |
| 1  | BoolT1SGPreplayXIII | 50     | Fitness            | 0.00   | 0.00   | 0.00  | 0.00   |
| 5  | BoolT1SGPreplayXIX  | 50     | Fitness            | 0.00   | 0.00   | 0.00  | 0.00   |
| 9  | BoolT1SGPreplayZa   | 100    | Fitness            | 0.00   | 0.00   | 0.00  | 0.00   |
| 13 | BoolT1SGPreplayZb   | 100    | Fitness            | 0.00   | 0.00   | 0.00  | 0.00   |
| 3  | BoolT1SGPreplayXIII | 50     | Generations        | 1.00   | 1.00   | 0.00  | 1.00   |
| 7  | BoolT1SGPreplayXIX  | 50     | Generations        | 2.00   | 2.00   | 0.00  | 2.00   |
| 11 | BoolT1SGPreplayZa   | 100    | Generations        | 1.00   | 1.84   | 1.43  | 7.00   |
| 15 | BoolT1SGPreplayZb   | 100    | Generations        | 1.00   | 1.60   | 1.21  | 7.00   |
| 2  | BoolT1SGPreplayXIII | 50     | Seconds            | 0.10   | 0.12   | 0.02  | 0.22   |
| 6  | BoolT1SGPreplayXIX  | 50     | Seconds            | 0.17   | 0.19   | 0.01  | 0.23   |
| 10 | BoolT1SGPreplayZa   | 100    | Seconds            | 0.10   | 0.18   | 0.11  | 0.58   |
|    |                     |        |                    |        |        |       |        |

Table: Summary of statistics of experiment ExpC. (Part 1)



A Summary

### Summary of statistics of experiment ExpC.

|    | Treatment         | Trials | Variable | min  | mean | sd   | max  |
|----|-------------------|--------|----------|------|------|------|------|
| 14 | BoolT1SGPreplayZb | 100    | Seconds  | 0.10 | 0.16 | 0.08 | 0.60 |

Table: Summary of statistics of experiment ExpC. (Part 2)



#### Parameters of treatment: BoolT1SGPreplayXIII

|                | Parameter Values                  |
|----------------|-----------------------------------|
| tRNG           | L'Ecuyer-CMRG Inversion Rejection |
| tReplay        | 0                                 |
| experimentName | ExpC                              |
| treatmentName  | BoolT1SGPreplayXIII               |
| trials         | 50                                |
| everyK         | 10                                |
| outpath        | data                              |
| batchPath      |                                   |
| tVerbose       | 1                                 |

Table: Parameters of treatment: BoolT1SGPreplayXIII



# Parameters of treatment BoolT1SGPreplayXIII passed to xegaRun

| -            | Parameter Values                                       |
|--------------|--|
| penv         | 3-Symmetry Problem                                     |
| grammar      | /home/dj2333/dev/cran/kSymmetry/BNF/AndOrNotTuned1.txt |
| replay       | 13   |
| algorithm    | sgp  |
| maxdepth     | 7  |
| max          | FALSE  |
| worstFitness | -8   |
| popsize      | 50   |
| generations  | 5000   |
| crossrate    | 0.2  |
| mutrate      | 0.4  |
| ivmutrate    | Const  |
| mutrate2     | 0.8  |
| ivcrossrate  | Const  |
| crossrate2   | 0.4  |

Table: Parameters of treatment BoolT1SGPreplayXIII passed to xegaRun (Part 1)



# Parameters of treatment BoolT1SGPreplayXIII passed to xegaRun

|                      | Parameter Values |
|----------------------|------------------|
|                      |                  |
| scalefactor          | Uniform          |
| genemap              | Bin2Dec          |
| initgene             | InitGene         |
| selection            | SUS              |
| mateselection        | SUS              |
| replication          | Kid2             |
| crossover            | Cross2Gene       |
| mutation             | MutateGene       |
| accept               | All              |
| reportEvalErrors     | TRUE             |
| codons               | 120              |
| codonPrecision       | LCM              |
| terminationEps       | -0.1             |
| terminationCondition | AbsoluteError    |
| evalmethod           | Deterministic    |

Table: Parameters of treatment BoolT1SGPreplayXIII passed to xegaRun (Part 2)



#### Parameters of treatment BoolT1SGPreplayXIII passed to xegaRun

|                | Parameter Values |
|----------------|------------------|
| executionModel | MultiCore        |
| verbose        | 1                |
| batch          | FALSE            |
| semantics      | byValue          |
| path           |                  |

Table: Parameters of treatment BoolT1SGPreplayXIII passed to xegaRun (Part 3)



Treatment: BoolT1SGPreplayXIII

|   | Treatment           | Trials | Variable    | min   | mean  | sd   | max   |
|---|---------------------|--------|-------------|-------|-------|------|-------|
| 4 | BoolT1SGPreplayXIII | 50     | Evaluations | 50.00 | 50.00 | 0.00 | 50.00 |
| 1 | BoolT1SGPreplayXIII | 50     | Fitness     | 0.00  | 0.00  | 0.00 | 0.00  |
| 3 | BoolT1SGPreplayXIII | 50     | Generations | 1.00  | 1.00  | 0.00 | 1.00  |
| 2 | BoolT1SGPreplayXIII | 50     | Seconds     | 0.10  | 0.12  | 0.02 | 0.22  |

Table: Treatment: BoolT1SGPreplayXIII



The Solution Table of Treatment BoolT1SGPreplayXIII of Experiment ExpC. Fit: 0. Unique Shortest Solutions: 1.

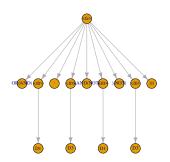
Solution

OR(AND(D1, D3), AND(NOT(D1), NOT(D3)))

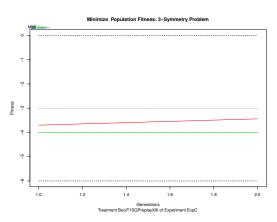
Table: The Solution Table of Treatment BoolT1SGPreplayXIII of Experiment ExpC. Fit: 0. Unique Shortest Solutions: 1.



#### The Derivation Tree of a Solution of Treatment BoolT1SGPreplayXIII of Experiment ExpC



# Plot of last xegaRun for Treatment BoolT1SGPreplayXIII of Experiment ExpC





#### Parameters of treatment: BoolT1SGPreplayXIX

|                | Parameter Values                  |
|----------------|-----------------------------------|
| tRNG           | L'Ecuyer-CMRG Inversion Rejection |
| tReplay        | 0                                 |
| experimentName | ExpC                              |
| treatmentName  | BoolT1SGPreplayXIX                |
| trials         | 50                                |
| everyK         | 10                                |
| outpath        | data                              |
| batchPath      |                                   |
| tVerbose       | 1                                 |

Table: Parameters of treatment: BoolT1SGPreplayXIX



## Parameters of treatment BoolT1SGPreplayXIX passed to xegaRun

|              | Parameter Values                                       |
|--------------|--|
| penv         | 3-Symmetry Problem                                     |
| grammar      | /home/dj2333/dev/cran/kSymmetry/BNF/AndOrNotTuned1.txt |
| replay       | 19   |
| algorithm    | sgp  |
| maxdepth     | 7  |
| max          | FALSE  |
| worstFitness | -8   |
| popsize      | 50   |
| generations  | 5000   |
| crossrate    | 0.2  |
| mutrate      | 0.4  |
| ivmutrate    | Const  |
| mutrate2     | 0.8  |
| ivcrossrate  | Const  |
| crossrate2   | 0.4  |

Table: Parameters of treatment BoolT1SGPreplayXIX passed to xegaRun (Part 1)



#### Parameters of treatment BoolT1SGPreplayXIX passed to xegaRun

|                      | Parameter Values |
|----------------------|------------------|
| scalefactor          | Uniform          |
| genemap              | Bin2Dec          |
| initgene             | InitGene         |
| selection            | SUS              |
| mateselection        | SUS              |
| replication          | Kid2             |
| crossover            | Cross2Gene       |
| mutation             | MutateGene       |
| accept               | All              |
| reportEvalErrors     | TRUE             |
| codons               | 120              |
| codonPrecision       | LCM              |
| terminationEps       | -0.1             |
| terminationCondition | AbsoluteError    |
| evalmethod           | Deterministic    |
|                      |                  |

Table: Parameters of treatment BoolT1SGPreplayXIX passed to xegaRun (Part 2)



#### Parameters of treatment BoolT1SGPreplayXIX passed to xegaRun

|                | Parameter Values |
|----------------|------------------|
| executionModel | MultiCore        |
| verbose        | 1                |
| batch          | FALSE            |
| semantics      | byValue          |
| path           |                  |

Table: Parameters of treatment BoolT1SGPreplayXIX passed to xegaRun (Part 3)



 ${\sf Treatment\ BoolT1SGPreplayXIX}$ 

#### Treatment: BoolT1SGPreplayXIX

|   | Treatment          | Trials | Variable    | min    | mean   | sd   | max    |
|---|--------------------|--------|-------------|--------|--------|------|--------|
| 8 | BoolT1SGPreplayXIX | 50     | Evaluations | 100.00 | 100.00 | 0.00 | 100.00 |
| 5 | BoolT1SGPreplayXIX | 50     | Fitness     | 0.00   | 0.00   | 0.00 | 0.00   |
| 7 | BoolT1SGPreplayXIX | 50     | Generations | 2.00   | 2.00   | 0.00 | 2.00   |
| 6 | BoolT1SGPreplayXIX | 50     | Seconds     | 0.17   | 0.19   | 0.01 | 0.23   |

Table: Treatment: BoolT1SGPreplayXIX



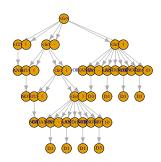
The Solution Table of Treatment BoolT1SGPreplayXIX of Experiment ExpC. Fit: 0. Unique Shortest Solutions: 1.

|   | Solution  |
|---|---|
| 1 | AND(NOT(NOT(OR(AND(D1, D1), AND(NOT(D1), NOT(D3))))), |
|   | OR(AND(D3, D1), AND(NOT(D3), NOT(D1))))               |

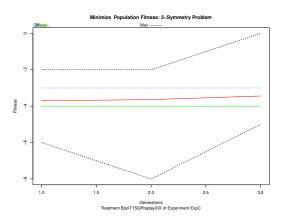
Table: The Solution Table of Treatment BoolT1SGPreplayXIX of Experiment ExpC. Fit: 0. Unique Shortest Solutions: 1.



# The Derivation Tree of a Solution of Treatment BoolT1SGPreplayXIX of Experiment $\ensuremath{\mathsf{ExpC}}$



## Plot of last xegaRun for Treatment BoolT1SGPreplayXIX of Experiment ExpC





#### Parameters of treatment: BoolT1SGPreplayZa

|                | Parameter Values                  |
|----------------|-----------------------------------|
| tRNG           | L'Ecuyer-CMRG Inversion Rejection |
| tReplay        | 0                                 |
| experimentName | ExpC                              |
| treatmentName  | BoolT1SGPreplayZa                 |
| trials         | 100                               |
| everyK         | 10                                |
| outpath        | data                              |
| batchPath      |                                   |
| tVerbose       | 1                                 |

Table: Parameters of treatment: BoolT1SGPreplayZa



#### Parameters of treatment BoolT1SGPreplayZa passed to xegaRun

| -            | Parameter Values                                       |
|--------------|--|
| penv         | 3-Symmetry Problem                                     |
| grammar      | /home/dj2333/dev/cran/kSymmetry/BNF/AndOrNotTuned1.txt |
| replay       | 0  |
| algorithm    | sgp  |
| maxdepth     | 7  |
| max          | FALSE  |
| worstFitness | -8   |
| popsize      | 50   |
| generations  | 5000   |
| crossrate    | 0.2  |
| mutrate      | 0.4  |
| ivmutrate    | Const  |
| mutrate2     | 0.8  |
| ivcrossrate  | Const  |
| crossrate2   | 0.4  |

Table: Parameters of treatment BoolT1SGPreplayZa passed to xegaRun (Part 1)



## Parameters of treatment BoolT1SGPreplayZa passed to xegaRun

| ameter Values Uniform Bin2Dec InitGene |
|--|
| Bin2Dec<br>InitGene                    |
| InitGene                               |
|  |
|  |
| SUS                                    |
| SUS                                    |
| Kid2                                   |
| Cross2Gene                             |
| MutateGene                             |
| All                                    |
| TRUE                                   |
| 120                                    |
| LCM                                    |
| -0.1                                   |
| AbsoluteError                          |
| Deterministic                          |
|  |

Table: Parameters of treatment BoolT1SGPreplayZa passed to xegaRun (Part 2)



#### Parameters of treatment BoolT1SGPreplayZa passed to xegaRun

|                | Parameter Values |
|----------------|------------------|
| executionModel | MultiCore        |
| verbose        | 1                |
| batch          | FALSE            |
| semantics      | byValue          |
| path           |                  |

Table: Parameters of treatment BoolT1SGPreplayZa passed to xegaRun (Part 3)



Treatment: BoolT1SGPreplayZa

|    | Treatment         | Trials | Variable    | min   | mean  | sd    | max    |
|----|-------------------|--------|-------------|-------|-------|-------|--------|
| 12 | BoolT1SGPreplayZa | 100    | Evaluations | 50.00 | 92.00 | 71.68 | 350.00 |
| 9  | BoolT1SGPreplayZa | 100    | Fitness     | 0.00  | 0.00  | 0.00  | 0.00   |
| 11 | BoolT1SGPreplayZa | 100    | Generations | 1.00  | 1.84  | 1.43  | 7.00   |
| 10 | BoolT1SGPreplayZa | 100    | Seconds     | 0.10  | 0.18  | 0.11  | 0.58   |

Table: Treatment: BoolT1SGPreplayZa



B Treatments

The Solution Table of Treatment BoolT1SGPreplayZa of Experiment ExpC. Fit: 0. Unique Shortest Solutions: 14.

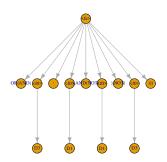
Solution

OR(AND(D3, D1), AND(NOT(D1), NOT(D3)))

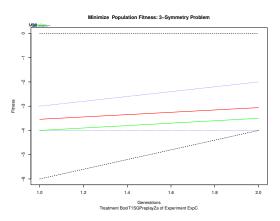
Table: The Solution Table of Treatment BoolT1SGPreplayZa of Experiment ExpC. Fit: 0. Unique Shortest Solutions: 14.



# The Derivation Tree of a Solution of Treatment BoolT1SGPreplayZa of Experiment ExpC



#### Plot of last xegaRun for Treatment BoolT1SGPreplayZa of Experiment ExpC





#### Parameters of treatment: BoolT1SGPreplayZb

|                | Parameter Values                  |
|----------------|-----------------------------------|
| tRNG           | L'Ecuyer-CMRG Inversion Rejection |
| tReplay        | 0                                 |
| experimentName | ExpC                              |
| treatmentName  | BoolT1SGPreplayZb                 |
| trials         | 100                               |
| everyK         | 10                                |
| outpath        | data                              |
| batchPath      |                                   |
| tVerbose       | 1                                 |

Table: Parameters of treatment: BoolT1SGPreplayZb



## Parameters of treatment BoolT1SGPreplayZb passed to xegaRun

|              | Parameter Values                                       |
|--------------|--|
| penv         | 3-Symmetry Problem                                     |
| grammar      | /home/dj2333/dev/cran/kSymmetry/BNF/AndOrNotTuned1.txt |
| replay       | 0  |
| algorithm    | sgp  |
| maxdepth     | 7  |
| max          | FALSE  |
| worstFitness | -8   |
| popsize      | 50   |
| generations  | 5000   |
| crossrate    | 0.2  |
| mutrate      | 0.4  |
| ivmutrate    | Const  |
| mutrate2     | 0.8  |
| ivcrossrate  | Const  |
| crossrate2   | 0.4  |

Table: Parameters of treatment BoolT1SGPreplayZb passed to xegaRun (Part 1)



## Parameters of treatment BoolT1SGPreplayZb passed to xegaRun

|                      | Parameter Values |
|----------------------|------------------|
|                      |                  |
| scalefactor          | Uniform          |
| genemap              | Bin2Dec          |
| initgene             | InitGene         |
| selection            | SUS              |
| mateselection        | SUS              |
| replication          | Kid2             |
| crossover            | Cross2Gene       |
| mutation             | MutateGene       |
| accept               | All              |
| reportEvalErrors     | TRUE             |
| codons               | 120              |
| codonPrecision       | LCM              |
| terminationEps       | -0.1             |
| terminationCondition | AbsoluteError    |
| evalmethod           | Deterministic    |

Table: Parameters of treatment BoolT1SGPreplayZb passed to xegaRun (Part 2)



#### Parameters of treatment BoolT1SGPreplayZb passed to xegaRun

|                | Parameter Values |
|----------------|------------------|
| executionModel | MultiCore        |
| verbose        | 1                |
| batch          | FALSE            |
| semantics      | byValue          |
| path           |                  |

Table: Parameters of treatment BoolT1SGPreplayZb passed to xegaRun (Part 3)



Treatment: BoolT1SGPreplayZb

|    | Treatment         | Trials | Variable    | min   | mean  | sd    | max    |
|----|-------------------|--------|-------------|-------|-------|-------|--------|
| 16 | BoolT1SGPreplayZb | 100    | Evaluations | 50.00 | 80.00 | 60.72 | 350.00 |
| 13 | BoolT1SGPreplayZb | 100    | Fitness     | 0.00  | 0.00  | 0.00  | 0.00   |
| 15 | BoolT1SGPreplayZb | 100    | Generations | 1.00  | 1.60  | 1.21  | 7.00   |
| 14 | BoolT1SGPreplayZb | 100    | Seconds     | 0.10  | 0.16  | 0.08  | 0.60   |

Table: Treatment: BoolT1SGPreplayZb



The Solution Table of Treatment BoolT1SGPreplayZb of Experiment ExpC. Fit: 0. Unique Shortest Solutions: 12.

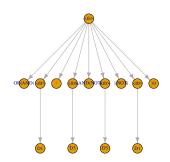
Solution

OR(AND(D3, D1), AND(NOT(D1), NOT(D3)))

Table: The Solution Table of Treatment BoolT1SGPreplayZb of Experiment ExpC. Fit: 0. Unique Shortest Solutions: 12.



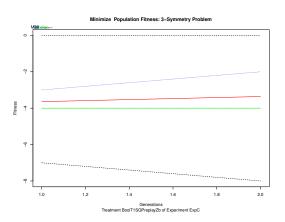
# The Derivation Tree of a Solution of Treatment BoolT1SGPreplayZb of Experiment ExpC





 ${\sf Treatment\ BoolT1SGPreplayZb}$ 

# Plot of last xegaRun for Treatment BoolT1SGPreplayZb of Experiment ExpC





|                | Parameter Values                                       |
|----------------|--|
| penv           | 3-Symmetry Problem                                     |
| grammar        | /home/dj2333/dev/cran/kSymmetry/BNF/AndOrNotTuned1.txt |
| max            | FALSE  |
| algorithm      | sgp  |
| popsize        | 50   |
| generations    | 5000   |
| crossrate      | 0.2  |
| mutrate        | 0.4  |
| elitist        | TRUE   |
| replay         | 13   |
| maxdepth       | 7  |
| maxtrials      | 5  |
| codons         | 120  |
| codonBits      | 0  |
| codonPrecision | LCM  |

Table: All parameters of xegaRun of treatment BoolT1SGPreplayXIII (Part 1)



|                  | Parameter Values |
|------------------|------------------|
| maxPBias         | 0.01             |
| evalmethod       | Deterministic    |
| evalrep          | 1                |
| reportEvalErrors | TRUE             |
| genemap          | Bin2Dec          |
| decoder          | DecodeGene       |
| crossrate2       | 0.4              |
| ivcrossrate      | Const            |
| crossover        | Cross2Gene       |
| uCrossSwap       | 0.2              |
| mincrossdepth    | 1                |
| maxcrossdepth    | 7                |
| ivmutrate        | Const            |
| mutrate2         | 0.8              |
| bitmutrate       | 0.005            |

Table: All parameters of xegaRun of treatment BoolT1SGPreplayXIII (Part 2)



|                      | Parameter Values |
|----------------------|------------------|
| hitmutrate2          |                  |
| 5                    | 0.01             |
| maxmutdepth          | 3                |
| minmutinsertiondepth | 1                |
| maxmutinsertiondepth | 7                |
| lambda               | 0.05             |
| ma×2opt              | 100              |
| scalefactor1         | 0.9              |
| scalefactor2         | 0.3              |
| scalefactor          | Uniform          |
| cutoffFit            | 0.5              |
| mutation             | MutateGene       |
| replication          | Kid2             |
| initgene             | InitGene         |
| offset               | 1                |
| eps                  | 0.01             |

Table: All parameters of xegaRun of treatment BoolT1SGPreplayXIII (Part 3)



|                       | Parameter Values |
|-----------------------|------------------|
| tournamentSize        | 2                |
| selectionBias         | 1.5              |
| maxTSR                | 1.5              |
| selection             | SUS              |
| mateselection         | SUS              |
| selectionContinuation | TRUE             |
| scaling               | NoScaling        |
| scalingThreshold      | 0                |
| scalingExp            | 1                |
| scalingExp2           | 1                |
| rdmWeight             | 1                |
| drMax                 | 2                |
| drMin                 | 0.5              |
| dispersionMeasure     | var              |
| scalingDelay          | 1                |

Table: All parameters of xegaRun of treatment BoolT1SGPreplayXIII (Part 4)



|                      | Parameter Values          |
|----------------------|---------------------------|
| accept               | All                       |
| alpha                | 0.99                      |
| beta                 | 2                         |
| cooling              | ExponentialMultiplicative |
| coolingPower         | 1                         |
| temp0                | 40                        |
| tempN                | 0.01                      |
| verbose              | 1                         |
| logevals             | FALSE                     |
| allsolutions         | FALSE                     |
| early                | FALSE                     |
| terminationCondition | AbsoluteError             |
| terminationEps       | -0.1                      |
| terminationThreshold | 0                         |
| worstFitness         | -8                        |

Table: All parameters of xegaRun of treatment BoolT1SGPreplayXIII (Part 5)



|                | Parameter Values |
|----------------|------------------|
| PACdelta       | 0.01             |
| fSpace         | Hilbert          |
| cores          | 16               |
| executionModel | MultiCore        |
| uParApply      | NULL             |
| Cluster        | NULL             |
| profile        | FALSE            |
| batch          | FALSE            |
| path           |                  |
| semantics      | byValue          |

Table: All parameters of xegaRun of treatment BoolT1SGPreplayXIII (Part 6)

