

1.1.1 Preface:

This program implements and extends the algorithm presented on the paper titled: “Does evolutionary plasticity evolve?” by Dr. Andreas Wagner. The program was written in C language, due to the large volume of data needed to be processed a higher level language would have had an immense overhead. Furthermore, it encompasses some new features not included in that paper. Instead of creating random gene interactions inside the Gene Regulatory Network (GRN), we have implemented the regulating regions of each gene (R1, R2), and through those 2 regions, we create the gene interactions inside the GRN. In addition, individuals who reach maturity periodically, are not discarded like the base paper, but handled as special cases called: cyclic equilibriums. Finally, in addition to the 2 models of recombination which are implemented, there are options for neutral or not selection as well as the number of parents required to leave progeny.

1.1.2 Background:

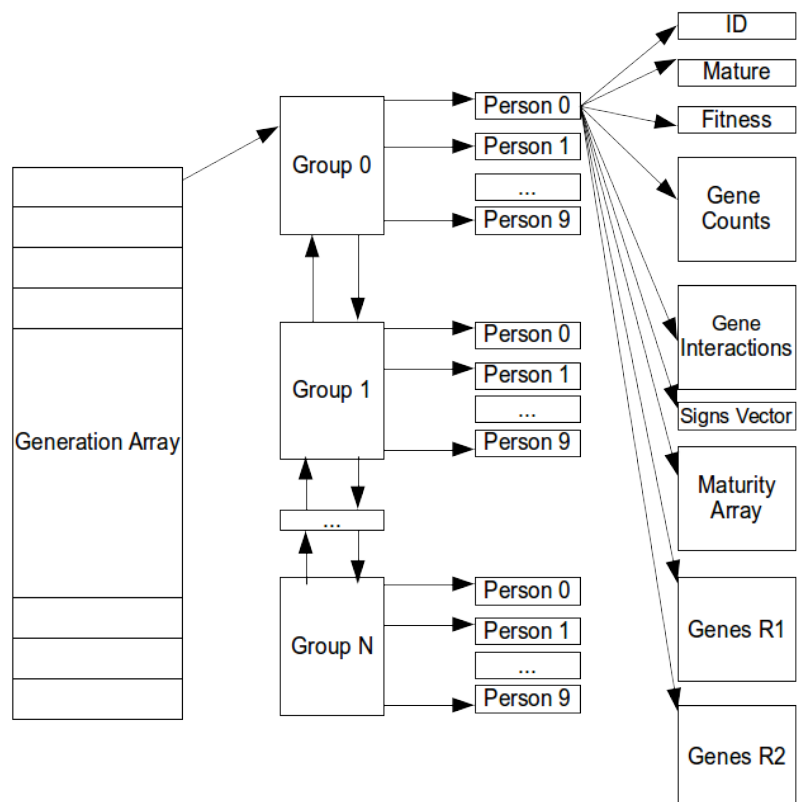
In 1996, Dr. Andreas Wagner publishes his paper: Does evolutionary plasticity evolve? From the early stages of development in each organism, a large number of interactions take place. Those interactions occur at the lowest levels as mutations. Those changes do not affect the organism immediately but instead are buffered. This phenomenon is called “epigenetic stability”. Variation in epigenetic stability can occur though. The research continues by modeling the transcriptional regulators that mutually regulate each other’s expression. Due to constraints in computer resources, the researcher was forced to experiment with a low number of vertices in the network and to find solutions to modeling problems. Through the advances of technology, we were capable of remodeling that research and adding new features.

1.2.1 Initialization of Population:

Each generation has N number of individuals. For acceleration purposes, those N individuals are then grouped into groups of 10. The groups are part of a doubly-linked list to accommodate changes in population sizes from one generation to the next, in case of an event. Each individual holds different kind of records.

Finally, each generation is stored into an array of pointers, called Generation_Array, each entry points to the population of a generation.

Using the above schema we are capable of finding the information for any individual with 2 hops, 1 from the generation to the group and from the group to our goal. For clarity purposes, check adjacent figure.



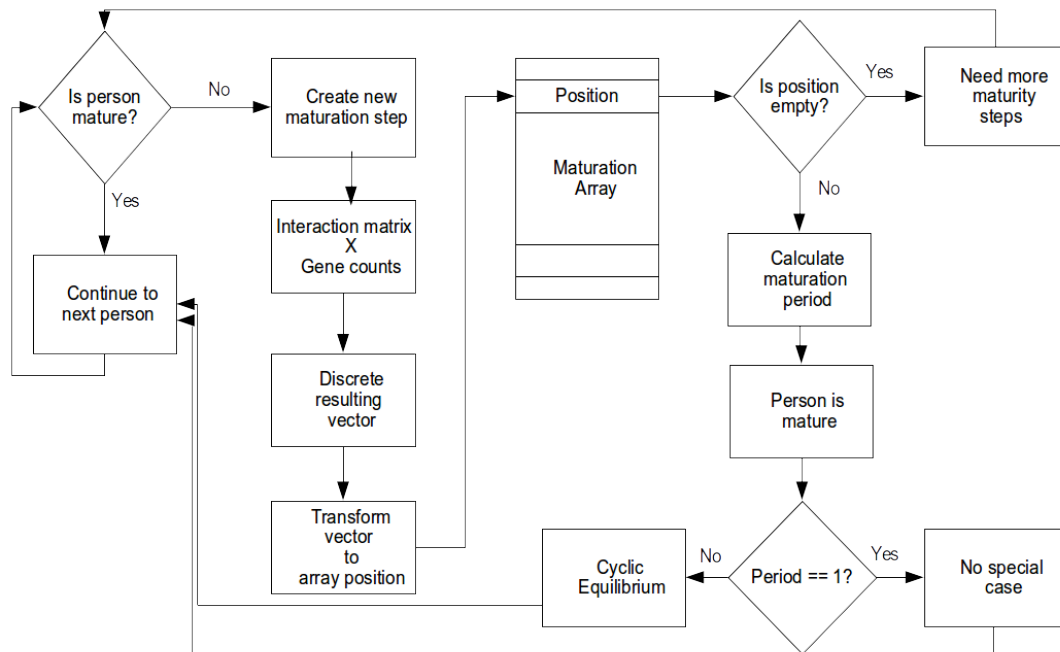
1.2.2 Initialization of each Individual:

Each member of the population, is represented with a structure holding many different elements. ID is the personal number of that member inside his group. The mature field is a boolean variable, indicating whether or not the member has reached maturity or not. Fitness is a float number in the range of 0 and 1. The closer fitness is to 1 the more chances the individual has to leave progeny. Gene counts is an array of integers, with each cell representing the expression of the corresponding gene. Its values are randomly selected from the range of specified by the user at the beginning of each run. The Maturity array has room for 1024 integers and at this stage it is empty. It is used in the maturation process of the individual and in calculating the personal period of maturity. Genes R1 and Genes R2 are 2 arrays of 10 integers each which are filled with random positive integers from the range given by the user.

Lastly, is the creation of the Gene Interactions Array. Each cell of this square matrix, stores the result of the following operation: From every integer M in R1, take the last bit. Do the same for every integer L in R2. Compare those 2 bits. If the produced pair is 11 then we have a positive interaction. If the pair is 00 we have a negative interaction. The other 2 pairs (01,10) indicate no regulation. The strength of those interactions are calculated by the number of set bits in the respective R1,R2. Store those interactions at the Gene Interactions Array at the M,L cell. We continue the same operation until the array is full.

1.3 Maturation:

Maturation Process



After creating the population, we proceed to the stage of maturation of the population. We create maturity steps for the whole population, by multiplying the gene_interactions matrix and the vector_of_signs (initialized to 1). The result is then made discrete, if its positive it gets 1, if

its zero or negative it gets 0. We use those bits to create the new vector of signs and through concatenation of those bits we create an integer. This integer is used to indicate the position in the maturity array, in which we place the number of the maturity step.

If the position is empty, it indicates that this particular version of the vector of signs is for the first time encountered and we need more maturity steps. Before creating another maturity step, the current maturity step number is saved in the maturity array. If the position in the maturity array is not empty that means that the individual is now mature and its maturity period is the number of the current step – the number of the step present at the cell. Since personal maturity has been achieved, the individual is excluded from further maturity steps. This process continues until all the population is mature.

For the majority of the population, the maturity period is 1, but for a small fraction of the population this is not the case. In those cases, a cyclic equilibrium is encountered. It doesn't affect the maturation process but it affects the fitness calculation process following.

1.4 Fitness Calculation:

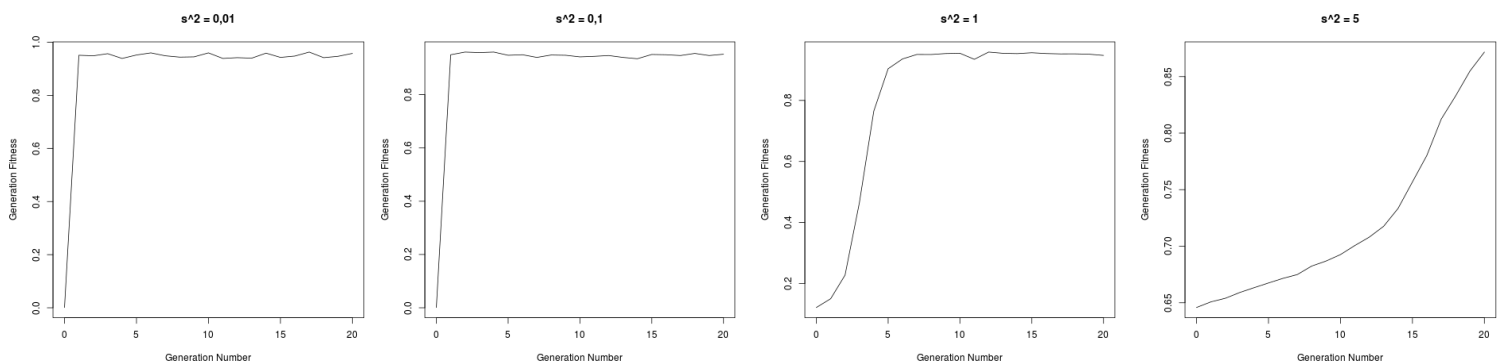
Each mature person now has a discrete vector consisting of 0s and 1s. For the individuals with a personal maturation period of 1, we proceed by calculating the euclidean distance between the personal signs vector and the optimal vector. For those who present a cyclic maturity equilibrium a different approach is used. If a person has an M maturation period, we create M maturation steps. Those steps create M vectors of signs. For every vector, we calculate the euclidean distance. The personal distance of the person is the mean of those distances. The personal fitness is then calculated with this formula:

$$\text{fitness} = e^{(-l \cdot \text{distance})}$$

The lambda is indirectly given by the user since $l = 1/s^2$ and s^2 is user-defined. The smaller the s^2 the bigger the increase in fitness from one generation to the next. This happens because a small s^2 makes any differences between the optimal vector and the personal vector of signs matter more. As a result, an individual with 1 difference dominates an individual with 2 differences. A big s^2 makes the simulation run without large leaps in fitness, because it is more tolerable to differences between the vectors.

After calculating the fitness of the whole population, the program divides the sum of the individual fitness with the number of individual to get a normalized percentage. The closer to 1 it gets the more adapted to its environment the population is.

The following graphs display the leaps of fitness while demonstrating the effects of different s^2 values.



1.5 Implementation of Forwarding:

Once a population is mature, it starts to create the next generation. There are 3 factors guiding this phase. The number of parents, the fitness of the parents, and which model dictates how the recombinations of the genes of the parents work.

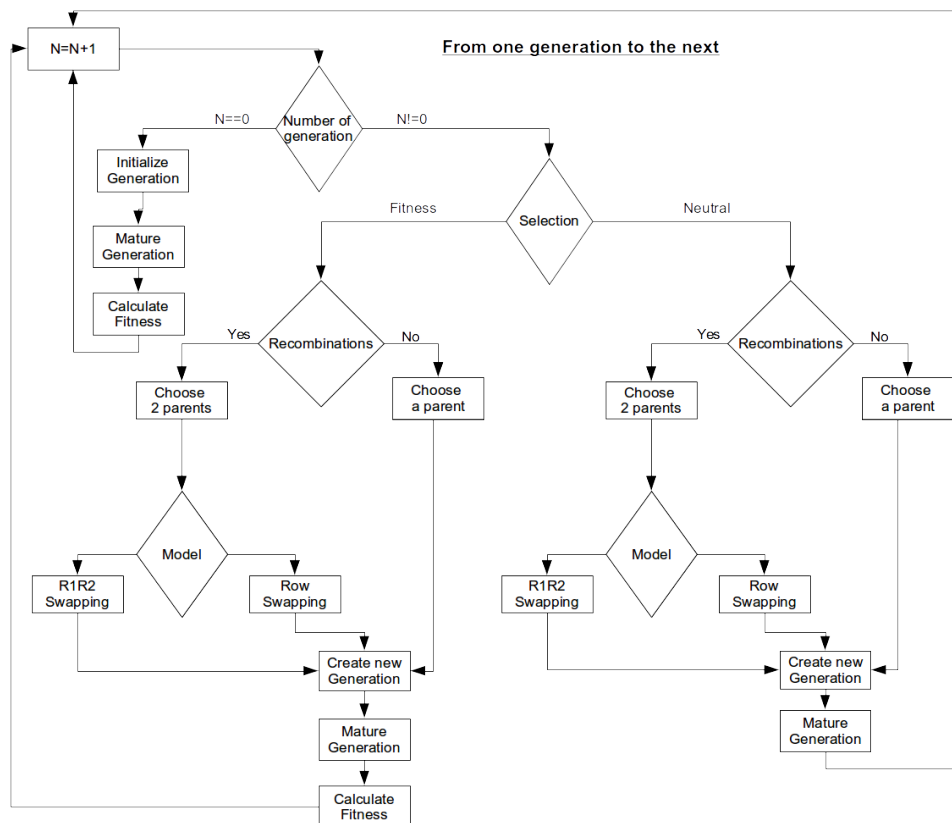
If the number of parents is 1, there are no combinations and the gene interaction matrix passes from parent to child. If a pair is needed to create a new individual then there are combinations of the parents which follow 2 models:

If the model of Dr. Wagner is followed then a random number C is selected from 0 to number of genes. The child inherits from the first parent C columns and from the second parent the remainder columns.

If our model is followed, 2 random numbers R , C are selected from 0 to number of genes. The top-left part of the gene interactions matrix is inherited from the first parent and the bottom-right part of the matrix is inherited by the second parent. The top-right part is filled with the interactions emerging from $R1$ of the first parent and $R2$ of the second parent, while the bottom left part is emerging from the $R2$ of the first parent in conjunction with the $R1$ of the second parent. Detailed explanation of these interactions at 1.2.1 paragraph.

A big factor for the creation of the next generation is if the fitness of the potential parent plays a role in his selection. If it doesn't, the population's fitness remains almost unchanged no matter how many generations we simulate. If the fitness of the parent plays a role, then a more fitted father has a much stronger possibility of passing his genes to the next generation. So as the simulation progresses we see that the fitness of the population is nearly 1. It can never reach it, due to unfavorable mutations and the combinations but it hovers close enough.

The following diagram displays a typical run of the simulation:



1.6 Mutations:

After the creation the new generation and before its maturity some mutations represent themselves. Those mutations affect the inherited R1,R2 arrays of random members of the population. The number of mutations per person is a Poisson distribution using as variable the mutation rate given by the user. Each mutation affects an cell in the R1 array or the R2 array. The selected for mutation cell contains an integer which is then made binary. A random selection is subsequently made for the bit that will be mutated. The mutation is represented by changing the bit to 1 if it was originally 0 and 1 if it was 0. The last bit of the binary integer represents the interaction of this gene with the GRN. Due to that fact, the chance for the last bit to change is 1%. The remaining 99% is distributed equal to the other bits. The resulting mutated integer is then placed back in its original place.

1.7 Events:

There are 2 types of events: increase of population and a decrease in population. The decrease of population is implemented without any difficulty by removing the groups needed in the end of the doubly-linked list. Due to the randomness of the individual in each group, the general fitness of the population, if calculated, does not change.

The increase of the population is handled by creating new groups of individuals, by the last generation, and adding those groups at the tail of the list. The next step is to mature those new groups. Then if fitness-based selection is active then the fitness of the population improves and we need to recalculate this fitness when all the new individuals have been created.

1.8 User's guide:

The program at the end of the run outputs data to text files. Each text file contains different kind of data from the simulation and for readability and consistency purposes follows a simple prototype. At the beginning of each new generation's data, the number of the generation, the number of individuals and the number of genes are reported. After that, follows the personal data of each member of the population. It's worth noting that, when the fitness of an individual doesn't affect the possibility of leaving offspring, the fitness text file is empty. Also, take in account that both R1R2 and counts text files do not differentiate between different individuals of the same generation, but since the number of genes is known we can easily find out the data belonging to each one.

1.9 Limitations:

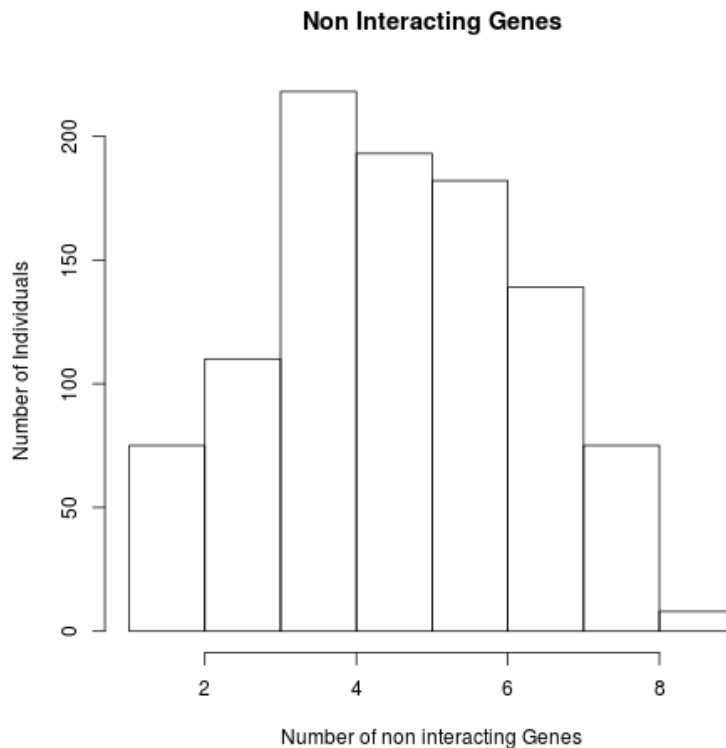
There is a hard limit (10) to the number of genes each person can have. This was selected because for more genes, the personal maturity array had to have a size of 2^N of genes. As a consequence of the memory requirements, a limit had to chosen. That limit is 10 genes per person. Otherwise there are no limitations as to how big a sample we want to simulate. The use of the double-hop system ensure an acceptable computational speed.

2.1 Results:

First and foremost, on fitness-based models the population reaches a level of fitness of 0.90 and then it plateaus. The model cannot simulate a generation fitness of 1, due to the existence of random mutations. As expected, simulations run on neutral evolution do not have this trait, instead the general fitness of the population hovers on a level set by the initial random start.

Secondly, the size of the population plays a vital role. Due to the random initialization process followed in all simulations, when the sample from where to draw potential parents decreases, the upwards leaps in generation fitness also decrease. As an example a sample of 1000 individuals reaches 0.9 generation fitness in 1 generation where as a sample of 100 individuals reaches that same percentage after 5 forward generations.

In the final forward generation, the number of non interacting genes is also important. At tests run, with 1000 individuals and 10 genes per individual, almost half of the genes do not regulate or are regulated by other genes.



The graph above shows that result. It is worth noting that, although some parts of the population have a half-filled interaction matrix, none have a completely empty one. So we conclude that there are at least some gene interactions persisting through all the events.