

ΜΕΡΟΣ 1

Ερώτημα 1

Η μαθηματική Αποδείξη:

$$\begin{aligned}
 G(u) &= \sum_{x=0}^{2N-1} g(x) W_{2N}^{xu} = \sum_{x=0}^{N-1} f(x) W_{2N}^{xu} + \sum_{x=N}^{2N-1} f(2N-1-x) W_{2N}^{xu} \stackrel{m=2N-1-x}{=} \sum_{x=0}^{N-1} f(x) W_{2N}^{xu} + \sum_{m=N-1}^0 f(m) W_{2N}^{(2N-1-m)u} = \\
 &= \sum_{x=0}^{N-1} f(x) (W_{2N}^{xu} + W_{2N}^{(2N-1-x)u}) = \sum_{x=0}^{N-1} f(x) (W_{2N}^{xu} + W_{2N}^{2Nu} W_{2N}^{-xu} W_{2N}^{-xu}) = \cos \phi = (e^{-j\phi} + e^{j\phi}) \\
 &\stackrel{W_{2N}^{2Nu} = 1}{=} \sum_{x=0}^{N-1} f(x) (W_{2N}^{xu} + W_{2N}^{-xu} W_{2N}^{xu}) = W_{2N}^{-u/2} \sum_{x=0}^{N-1} f(x) \left(e^{-j \frac{2\pi}{2N} \left(\frac{u}{2} + xu \right)} + e^{j \frac{2\pi}{2N} \left(\frac{u}{2} + xu \right)} \right) = \\
 &= W_{2N}^{-u/2} \sum_{x=0}^{N-1} f(x) 2 \cos \left(\frac{\pi}{2N} u (2x+1) \right) = \frac{2}{W(u)} e^{j \frac{\pi}{2N} u} F(u) = \\
 &= \frac{W(u)}{2} G(u) e^{-j \frac{\pi}{2N} u}, \text{ για } u=0, 1, 2, \dots, N-1
 \end{aligned}$$

Ερώτημα 2

```

f part one.m x | f mydct.m x | f mydct2.m x
1 function F = mydct(f)
2 % Metatrepw to f se sthlh gia na douleuw panta me sthlh
3 f = f(:);
4 N = length(f);
5 % Theloume h g na einai h f kai h anapodh f
6 g = [f; flip(f)];
7
8 G=fft(g);
9
10 w_0=1/sqrt(N);
11 w_greater=sqrt(2)/sqrt(N);
12 for u=1:N
13     F(u)=G(u)*exp(-j*pi*(u-1)/(2*N));
14     if u==1
15         F(u)=F(u)*w_0/2;
16     else
17         F(u)=F(u)*w_greater/2;
18     end
19 end
20
21 end

```

Ερώτημα 3

```
f mydct.m × | f mydct2.m ×
1 function F = mydct2(f)
1
2 rows = size(f,1);
3 columns = size(f,2);
4
5 % DCT se kathe grammh
6 for w=1:rows
7 | nf(w,:) = mydct(f(w,:)).'; % Transpose gia na ginei ksana sei
8 end
9 % DCT se kathe sthlh
10 for w=1:columns
11 | F(:,w) = mydct(nf(:,w));
12 end
13
14 end
15
```

Ερώτημα 4

```
f part_one.m x | f mydct.m x | f mydct2.m x
8 clear;
7
6 A = [ 1 9 17 25 -33 41 49 57;
5 2 1 8 2 4 2 58;
4 2 10 18 26 34 2 0 8;
3 -2 15 18 26 34 2 0 58;
2 0 1 18 26 34 40 5 5;
1 2 1 18 26 14 19 5 8;
0 2 0 8 26 2 42 0 5;
9 2 1 8 26 4 4 0 58;
8 ];
7
6 result_one = mydct2(A)
5 result_two = dct2(A)
4
3 % Sygkrinoume th diafora
2 diff = result_one - result_two;
1 disp(max(abs(diff(:)))));
9
```

```
octave:4> part_one
result_one =

119.2500 + 0i -54.1605 + 0.00001i -9.6158 + 0.00001i -36.0808 - 0.00001i 16.2500 + 0.00001i -0.1630 - 0.00001i 18.5953 + 0.00001i -22.9164 - 0.00001i
18.5425 + 0.00001i -24.6043 + 0.00001i 32.5545 + 0.00001i -13.9155 - 0.00001i -15.8537 - 0.00001i 11.0636 + 0.00001i -15.5476 - 0.00001i 11.0531 + 0.00001i
-0.5112 - 0.00001i -28.4547 + 0.00001i 48.3005 + 0i -15.5545 - 0.00001i -15.4518 + 0i 26.3929 - 0.00001i 5.1930 + 0.00001i -23.2009 + 0i
4.4372 + 0.00001i -7.0215 + 0.00001i -3.7716 - 0.00001i 20.1821 + 0.00001i -35.2870 - 0.00001i 25.6450 + 0.00001i 13.4060 + 0i -18.9336 - 0.00001i
18.0000 + 0i -16.1397 + 0.00001i 12.5012 - 0.00001i -17.5758 - 0.00001i 7.0000 + 0.00001i -7.8741 - 0.00001i 8.6223 + 0.00001i -13.6281 - 0.00001i
2.3805 + 0.00001i 9.9076 + 0.00001i -7.3007 + 0.00001i -1.7419 - 0.00001i -4.6151 - 0.00001i -2.1959 + 0.00001i 7.7902 - 0.00001i -20.1112 - 0.00001i
-3.8472 - 0.00001i 18.5763 + 0.00001i -11.5570 + 0.00001i -7.4778 - 0.00001i 4.5061 - 0.00001i 1.6213 + 0.00001i -1.5505 + 0i -0.9455 + 0.00001i
-4.7377 + 0.00001i 16.1662 + 0.00001i -30.7670 - 0.00001i 28.5261 + 0.00001i -15.9159 - 0.00001i 7.1105 - 0.00001i 8.1046 + 0.00001i -9.3819 - 0.00001i

result_two =

119.2500 -54.1605 -9.6158 -36.0808 16.2500 -0.1630 18.5953 -22.9164
18.5425 -24.6043 32.5545 -13.9155 -15.8537 11.0636 -15.5476 11.0531
-0.5112 -28.4547 48.3005 -15.5545 -15.4518 26.3929 5.1930 -23.2009
4.4372 -7.0215 -3.7716 20.1821 -35.2870 25.6450 13.4060 -18.9336
18.0000 -16.1397 12.5012 -17.5758 7.0000 -7.8741 8.6223 -13.6281
2.3805 9.9076 -7.3007 -1.7419 -4.6151 -2.1959 7.7902 -20.1112
-3.8472 18.5763 -11.5570 -7.4778 4.5061 1.6213 -1.5505 -0.9455
-4.7377 16.1662 -30.7670 28.5261 -15.9159 7.1105 8.1046 -9.3819

1.4233e-14
octave:5>
```

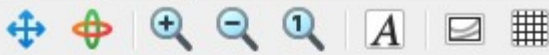
ΜΕΡΟΣ 2





Figure 3

File Edit Tools



$Q = 2 * Q1$, PSNR = 29.31 dB



(47.913, 61.727)



Entropy of original image: 7.0097

=====

$Q = 1 * Q_1$

=====

Entropy of $|F_{\text{hat}}(u,v)|$: 0.6042

Number of zero coefficients: 55852

PSNR: 31.7487 dB

=====

$Q = 2 * Q_1$

=====

Entropy of $|F_{\text{hat}}(u,v)|$: 0.4510

Number of zero coefficients: 59349

PSNR: 29.3111 dB

=====

$Q = 3 * Q_1$

=====

Entropy of $|F_{\text{hat}}(u,v)|$: 0.3749

Number of zero coefficients: 60789

PSNR: 28.0489 dB

octave:5> █