

$$3. \int 3x^2 (x^3 - 5)^7 dx$$

$$u = x^3 - 5$$

$$\frac{du}{dx} = 3x^2$$

$$\int \frac{du}{dx} (u)^7 dx$$

$$\int u^7 du$$

$$\frac{1}{8} u^8 + C$$

$$\frac{1}{8} (x^3 - 5)^8 + C$$

$$\int x (x^2 + 1)^8 dx$$

$$u = x^2 + 1$$

$$du = 2x$$

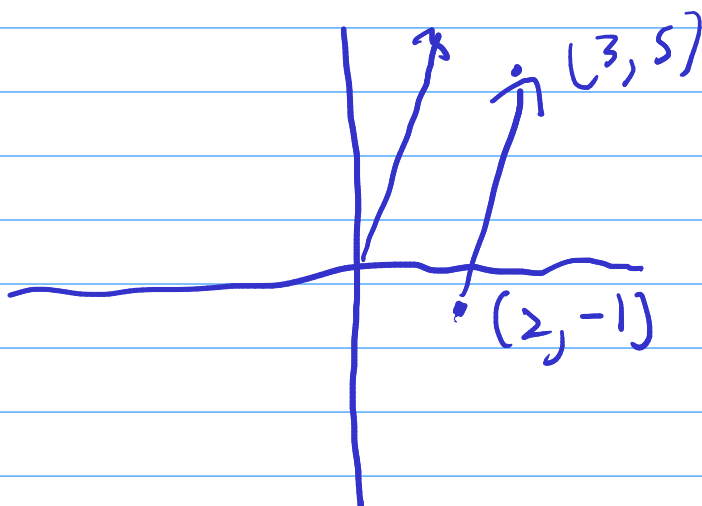
$$\int \frac{1}{2} \cdot 2x (x^2 + 1)^8 dx$$

$$\int \frac{1}{2} \frac{du}{dx} (u)^8 dx$$

$$\int \frac{1}{2} u^8 du$$

$$\frac{1}{18} u^9 + C$$

$$\frac{1}{18} (x^2 + 1)^9 + C$$



Component

$$\langle 1, 6 \rangle$$

$$\uparrow \uparrow$$

$$\uparrow + 6\uparrow$$

Standard
unit
vector

11. Let $\vec{u} = \langle 1, -2 \rangle$ and $\vec{v} = \langle 1, 1 \rangle$.

(a) Find $\vec{u} + \vec{v}$, $\vec{u} - \vec{v}$, $2\vec{u} - 3\vec{v}$.

(b) Sketch the above vectors on the same axes, along with \vec{u} and \vec{v} .

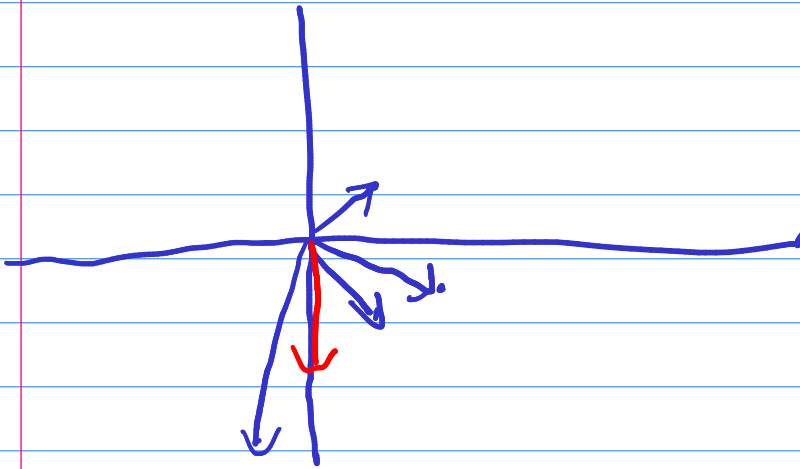
(c) Find \vec{x} where $\vec{u} + \vec{x} = 2\vec{v} - \vec{x}$.

$$\langle 2, -1 \rangle$$

$$\langle 0, -3 \rangle$$

$$\langle 2, -4 \rangle - \langle 3, 3 \rangle$$

$$\langle -1, -7 \rangle$$

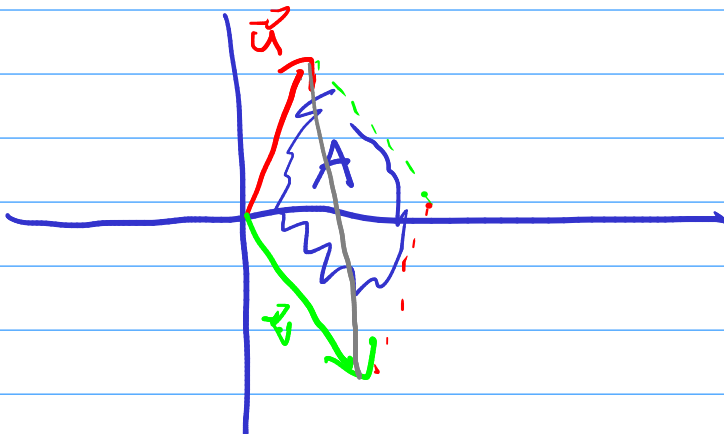


$$\langle 1, -2 \rangle + \vec{x} = \langle 2, 2 \rangle - \vec{x}$$

$$\langle 1, -2 \rangle + 2\vec{x} = \langle 2, 2 \rangle$$

$$2\vec{x} = \langle 1, 4 \rangle$$

$$\vec{x} = \langle \frac{1}{2}, 2 \rangle$$

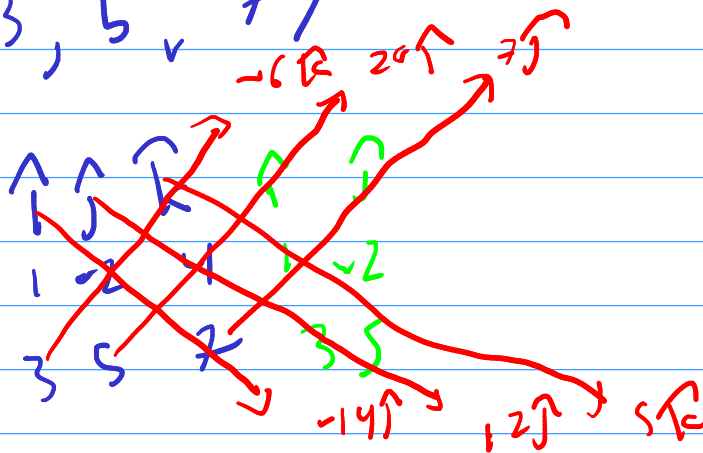


$$\frac{1}{2} ab \sin \theta$$

$$\|\vec{u}\| \|\vec{v}\| \cdot \sin \theta$$

$$\langle 1, -2, 4 \rangle$$

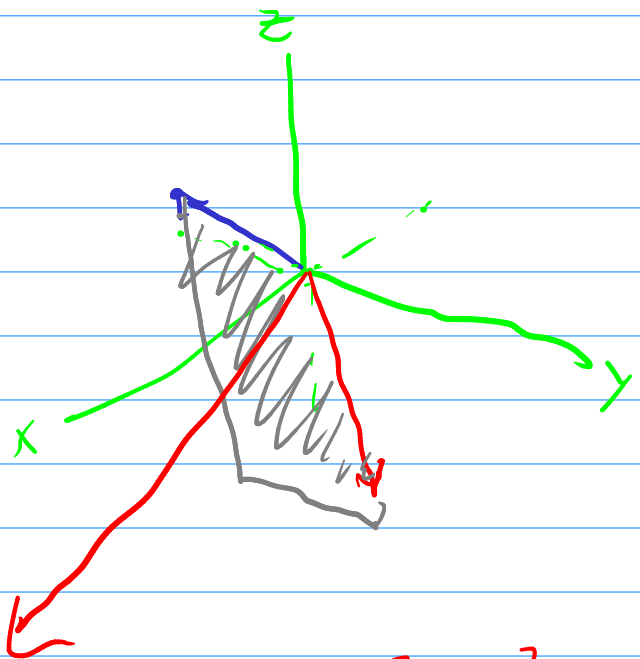
$$\langle 3, 5, -7 \rangle$$



$$-14\hat{i} + 12\hat{j} + 5\hat{k} - (-6\hat{k} + 20\hat{i} + 7\hat{j})$$

$$-34\hat{i} + 5\hat{j} + 11\hat{k}$$

$$\langle -34, 5, 11 \rangle$$



$$(\vec{u} + \vec{v}) \times \vec{w} = \vec{u} \times \vec{w} + \vec{v} \times \vec{w}$$

$$\vec{w} \times (\vec{u} + \vec{v}) = \vec{w} \times \vec{u} + \vec{w} \times \vec{v}$$

$$\mathbb{R}^2 : x \text{ o } y$$

$$\mathbb{R}^3 : x \text{ o } y \text{ o } z$$

$$\vec{p} = \langle 3, 1, 4 \rangle \quad \vec{r}(t) = \vec{p} + t\vec{d}$$

$$\vec{d} = \langle 2, 1, 2 \rangle$$

$$\langle 3+2t, 1+t, 4+2t \rangle$$
$$\frac{x-3}{2} = \frac{y-1}{1} = \frac{z-4}{2}$$

