

CS210 Assignment-1

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1 Maximum Values of n for which $fib(n)$ can be computed in a given Time Interval

- Recursive fibonacci Rfib

Time	.001s	.01s	.1s	1s	5s	60s	600s
Maximum Value of n	24	28	35	40	43	48	53

- Iterative fibonacci Ifib

Function	.001s	.01s	.1s	1s	5s	60s	600s
Maximum value of n	5.6×10^4	1.4×10^6	1.4×10^7	1.5×10^8	7.8×10^8	9.0×10^9	9.0×10^{10}

- Clever Fibonacci Clever-algo-fib

Function	.001s	.01s	.1s	1s	5s	60s	600s
Maximum Value of n	$> 10^{18}$	$> 10^{18}$	$> 10^{18}$	$> 10^{18}$	$> 10^{18}$	$> 10^{18}$	$> 10^{18}$

2 Time Complexity

Function	Slope by graph	Order	Calculated Steps for n
rfib	0.4745	$O(1.607^n)$	-
ifib	6.8×10^{-5}	$O(n)$	$3n$
cleverfib	3.274×10^{-8}	$O(\log(n))$	$35\log(n)+11$

3 Inference

- rfib is exponentially growing function wrt n so graph of n vs log of time gives a straight line with slope 0.47 . one can easily verify that no. of steps is $> 2^{.5n}$.from order we can say this sequence of time for larger n is similar to fibonacci series
- while Ifib is linear in time and efficient than rfib
- the cleverfib is most efficient in all three and takes less than a milisecond for whole long long int range hence we are getting a very less slope of the curve

4 Graphs

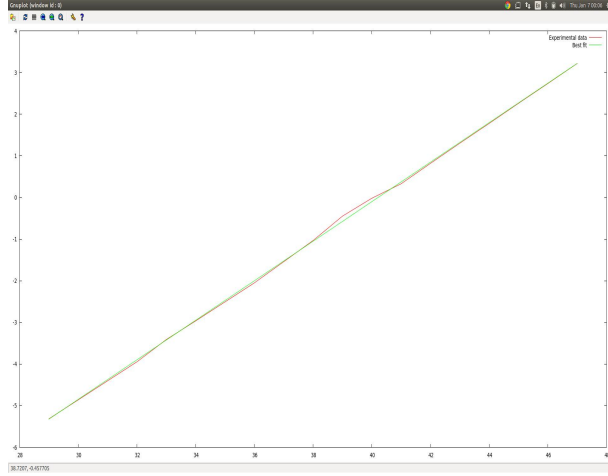


Figure 1: Log (Time taken by Rfib) as a function of n

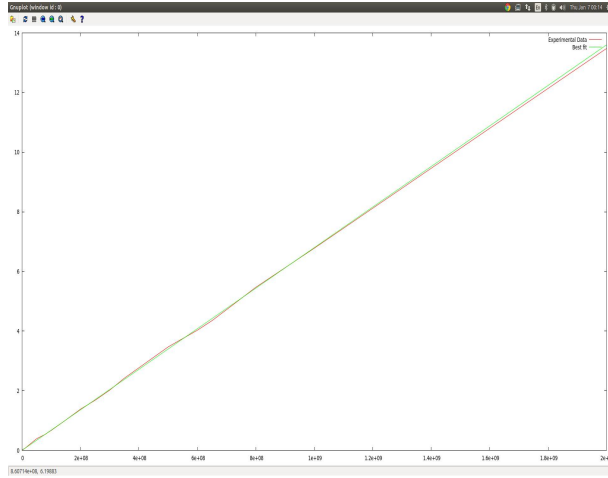


Figure 2: Time taken by ifib as a function of n

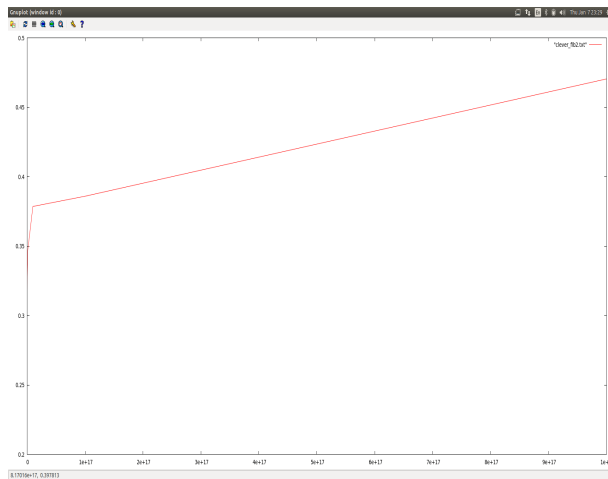


Figure 3: Time(in 10^{-5} s) taken by clever-algo-fib as a function of $\log(n)$