

# Multiple substitutions

- The model assumes that point mutations alter one nucleotide at a time, hence most of the instantaneous rates:
  - (3134/3761 or 84.2% in the case of the universal genetic code) are 0.
- This restriction, however, does not mean that the model disallows any substitutions that involve multiple nucleotides (e.g., **ACT**  $\Rightarrow$  **AGG**).
  - This can be further relaxed with models supporting multiple nucleotide changes.
- Such substitutions must simply be realized via several single nucleotide steps, e.g., **ACT**  $\Rightarrow$  **AGT**  $\Rightarrow$  **AGG**
- In fact the  $(i, j)$  element of  $\mathbf{T}(t) = \exp(\mathbf{Q}t)$  sums the probabilities of all such possible pathways of duration  $t$ , including reversions
- Compare this to the naive NG86 parsimony approach.

# Alignment-wide estimates

- Using standard MLE approaches it is straightforward to obtain point estimates of  $dN/dS := \beta/\alpha$
- Can also easily test whether or not  $dN/dS > 1$ , or  $< 1$  using the likelihood ratio test (LRT)
- Codon models also support the concepts of synonymous and non-synonymous distances between sequences using standard properties of Markov processes (exponentially distributed waiting times)