30.15 IMPORTANT JOINT DISTRIBUTIONS

(i) The probability of picking six tickets of the same colour is given by

$$\Pr(\text{six of the same colour}) = 3 \ge \frac{6!}{6!0!0!} (\frac{1}{3})^6 (\frac{1}{3})^0 (\frac{1}{3})^0 = \frac{1}{243}.$$

The factor of 3 is present because there are three different colours.

(ii) The probability of picking five tickets of one colour and one ticket of another colour is

Pr
(five of one colour; one of another) = 3 x 2 x
$$\frac{6!}{5!1!0!}$$