



In addition, we also have  $M_2$  and  $p_2/p_1$  as functions of  $M_1$  from the earlier normal-shock analysis. Combining these produces the relation between the  $p_{o2}$  measured by the pitot probe, the static  $p_1$ , and the required flow Mach number  $M_1$ . After some manipulation, the result is the *Rayleigh Pitot tube formula*.

$$\frac{p_{o2}}{p_1} = \frac{p_{o2}}{p_2} \frac{p_2}{p_1} = \left( \frac{(\gamma+1)^2 M_1^2}{4\gamma M_1^2 - 2(\gamma-1)} \right)^{\gamma/(\gamma-1)} \frac{1 - \gamma + 2\gamma M_1^2}{\gamma+1} \quad (4)$$

The figure shows  $p_{o2}/p_1$  versus  $M_1$ , compared with the isentropic ratio  $p_{o1}/p_1$ .

$$\frac{p_{o1}}{p_1} = \left( 1 + \frac{\gamma-1}{2} M_1^2 \right)^{\gamma/(\gamma-1)} \quad (5)$$

Only the latter is plotted for  $M_1 < 1$ , where there is no bow shock, and so equation (4) does not apply. The effect of the pitot bow shock's total pressure loss, indicated by the difference  $p_{o1} - p_{o2}$ , becomes substantial at larger Mach numbers.

Ideally, we would like to have the pitot formula (4) give  $M_1$  as an explicit function of the pitot/static pressure ratio  $p_{o2}/p_1$ . However, this is not possible due to its complexity, so a numerical solution is required. The function is also readily available in table form.