

অনুশীলনী ৪.২

১। সূত্রের সাহায্যে নিচের রাশিগুলোর ঘন নির্ণয় কর :

- (ক) $3x + y$ (খ) $x^2 + y$ (গ) $5p + 2q$ (ঘ) $a^2b + c^2d$ (ঙ) $6p - 7$
 (চ) $ax - by$ (ছ) $2p^2 - 3r^2$ (জ) $x^3 + 2$ (ঝ) $2m + 3n - 5p$
 (ঞ) $x^2 - y^2 + z^2$ (ট) $a^2b^2 - c^2d^2$ (ঠ) $a^2b - b^3c$ (ড) $x^3 - 2y^3$
 (ঢ) $11a - 12b$ (ণ) $x^3 + y^3$

(ক) $3x + y$

সমাধান :

$$\begin{aligned}(3x + y)^3 &= (3x)^3 + 3 \times (3x)^2 \times y + 3 \times (3x) \times (y)^2 + (y)^3 \\&= 27x^3 + 3 \times 9x^2 \times y + 3 \times 3x \times y^2 + y^3 \\&= 27x^3 + 27x^2y + 9xy^2 + y^3\end{aligned}$$

(খ) $x^2 + y$

সমাধান :

$$\begin{aligned}(x^2 + y)^3 &= (x^2)^3 + 3 \times (x^2)^2 \times y + 3 \times (x^2) \times (y)^2 + (y)^3 \\&= x^6 + 3 \times x^4 \times y + 3 \times x^2 \times y^2 + y^3 \\&= x^6 + 3x^4y + 3x^2y^2 + y^3\end{aligned}$$

(গ) $5p + 2q$

সমাধান :

$$\begin{aligned}(5p + 2q)^3 &= (5p)^3 + 3 \times (5p)^2 \times 2q + 3 \times (5p) \times (2q)^2 + (2q)^3 \\&= 125p^3 + 3 \times 25p^2 \times 2q + 3 \times 5p \times 4q^2 + 8q^3 \\&= 125p^3 + 150p^2q + 60pq^2 + 8q^3\end{aligned}$$

(ঘ) $a^2b + c^2d$

সমাধান :

$$\begin{aligned}(a^2b + c^2d)^3 &= (a^2b)^3 + 3 \times (a^2b)^2 \times c^2d + 3 \times (a^2b) \times (c^2d)^2 + (c^2d)^3 \\&= a^6b^3 + 3 \times a^4b^2 \times c^2d + 3 \times a^2b \times c^4d^2 + c^6d^3 \\&= a^6b^3 + 3a^4b^2c^2d + 3a^2bc^4d^2 + c^6d^3\end{aligned}$$

(ঙ) $6p - 7$

সমাধান :

$$\begin{aligned}(6p - 7)^3 &= (6p)^3 - 3 \times (6p)^2 \times 7 + 3 \times (6p) \times (7)^2 - (7)^3 \\&= 216p^3 - 3 \times 36p^2 \times 7 + 3 \times 6p \times 49 - 343 \\&= 216p^3 - 756p^2q + 882pq^2 - 343\end{aligned}$$

(চ) $ax - by$

সমাধান :

$$\begin{aligned}(ax - by)^3 &= (ax)^3 - 3 \times (ax)^2 \times by + 3 \times (ax) \times (by)^2 - (by)^3 \\&= a^3x^3 - 3 \times a^2x^2 \times by + 3 \times ax \times b^2y^2 - b^3y^3 \\&= a^3x^3 - 3a^2bx^2y + 3ab^2xy^2 - b^3y^3\end{aligned}$$

(ছ) $2p^2 - 3r^2$

সমাধান :

$$\begin{aligned}(2p^2 - 3r^2)^3 &= (2p^2)^3 - 3 \times (2p^2)^2 \times 3r^2 + 3 \times (2p^2) \times (3r^2)^2 - (3r^2)^3 \\&= 8p^6 - 3 \times 4p^4 \times 3r^2 + 3 \times 2p^2 \times 9r^4 - 27r^6 \\&= 8p^6 - 36p^4r^2 + 54p^2r^4 - 27r^6\end{aligned}$$

(জ) $x^3 + 2$

সমাধান :

$$\begin{aligned}(x^3 + 2)^3 &= (x^3)^3 + 3 \times (x^3)^2 \times 2 + 3 \times (x^3) \times (2)^2 + (2)^3 \\&= x^9 + 3 \times x^6 \times 2 + 3 \times x^3 \times 4 + 8 \\&= x^9 + 6x^6 + 12x^3 + 8\end{aligned}$$

(ঝ) $2m + 3n - 5p$

সমাধান :

$$\begin{aligned}(2m + 3n - 5p)^3 &= \{(2m + 3n) - (5p)\}^3 \\&= (2m + 3n)^3 - 3 \times (2m + 3n)^2 \times (5p) + 3 \times (2m + 3n) \times (5p)^2 - (5p)^3 \\&= \{(2m)^3 + 3 \times (2m)^2 \times 3n + 3 \times (2m) \times (3n)^2 + (3n)^3\} \\&\quad - 15p \times \{(2m)^2 + 2 \times 2m \times 3n + (3n)^2\} + 3 \times (2m + 3n) \times 25p^2 - 125p^3\end{aligned}$$

$$\begin{aligned}
 &= 8m^3 + 9n \times 4m^2 + 6m \times 9n^2 + 27n^3 - 15p \times \{4m^2 - 12mn + 9n^2\} \\
 &\quad + 75p^2 \times (2m + 3n) - 125p^3 \\
 &= 8m^3 + 36nm^2 + 54mn^2 + 27n^3 - 60pm^2 + 180mnp - 135n^2p \\
 &\quad + 150mp^2 + 225np^2 - 125p^3 \\
 &= 8m^3 + 27n^3 - 125p^3 + 36nm^2 - 60pm^2 + 54mn^2 + 150mp^2 - 135n^2p + 225np^2 - 180mnp
 \end{aligned}$$

(এ) $x^2 - y^2 + z^2$

সমাধান :

$$(x^2 - y^2 + z^2)^3$$

$$= \{(x^2 - y^2) + (z^2)\}^3$$

$$\begin{aligned}
 &= (x^2 - y^2)^3 + 3(x^2 - y^2)^2 z^2 + 3(x^2 - y^2)(z^2)^2 + (z^2)^3 \\
 &= \{(x^2)^3 - 3(x^2)^2 y^2 + 3x^2(y^2)^2 - (y^2)^3\} + 3(x^2 - y^2)^2 z^2 + 3(x^2 - y^2)(z^2)^2 + (z^2)^3 \\
 &= x^6 - 3x^4 y^2 + 3x^2 y^4 - y^6 + 3z^2 \{(x^2)^2 - 2x^2 y^2 + (y^2)^2\} + 3z^4(x^2 - y^2) + z^6 \\
 &= x^6 - 3x^4 y^2 + 3x^2 y^4 - y^6 + 3x^4 z^2 - 6x^2 y^2 z^2 + 3y^6 z^2 + 3z^4 x^2 - 3z^4 y^2 + z^6 \\
 &= x^6 - y^6 + z^6 - 3x^4 y^2 + 3x^2 y^4 + 3x^4 z^2 - 6x^2 y^2 z^2 + 3y^6 z^2 + 3x^2 z^4 - 3y^2 z^4
 \end{aligned}$$

(ট) $a^2 b^2 - c^2 d^2$

সমাধান :

$$\begin{aligned}
 (a^2 b^2 - c^2 d^2)^3 &= (a^2 b^2)^3 - 3 \times (a^2 b^2)^2 \times c^2 d^2 + 3 \times (a^2 b^2) \times (c^2 d^2)^2 - (c^2 d^2)^3 \\
 &= a^6 b^6 - 3a^4 b^4 c^2 d^2 + 3a^2 b^2 c^4 d^4 - c^6 d^6
 \end{aligned}$$

(ঠ) $a^2 b - b^3 c$

সমাধান :

$$\begin{aligned}
 (a^2 b - b^3 c)^3 &= (a^2 b)^3 - 3 \times (a^2 b)^2 \times b^3 c + 3 \times (a^2 b) \times (b^3 c)^2 - (b^3 c)^3 \\
 &= a^6 b^3 - 3a^4 b^2 b^3 c + 3a^2 b b^6 c^2 - b^9 c^3 \\
 &= a^6 b^3 - 3a^4 b^5 c + 3a^2 b^7 c^2 - b^9 c^3
 \end{aligned}$$

(ড) $x^3 - 2y^3$

সমাধান :

$$\begin{aligned}(x^3 - 2y^3)^3 &= (x^3)^3 - 3 \times (x^3)^2 \times 2y^3 + 3 \times (x^3) \times (2y^3)^2 - (2y^3)^3 \\ &= x^9 - 6x^6y^3 + 12x^3y^6 - 8y^9\end{aligned}$$

(ঢ) $11a - 12b$

সমাধান :

$$\begin{aligned}(11a - 12b)^3 &= (11a)^3 - 3 \times (11a)^2 \times 12b + 3 \times (11a) \times (12b)^2 - (12b)^3 \\ &= 1331a^3 - 4356a^2b + 4752ab^2 - 1728b^3\end{aligned}$$

(ণ) $x^3 + y^3$

সমাধান :

$$\begin{aligned}(x^3 + y^3)^3 &= (x^3)^3 + 3 \times (x^3)^2 \times y^3 + 3 \times (x^3) \times (y^3)^2 + (y^3)^3 \\ &= x^9 + 3x^6y^3 + 3x^3y^6 + y^9\end{aligned}$$

২। সরল কর :

(ক) $(3x + y)^3 + 3(3x + y)^2(3x - y) + 3(3x + y)(3x - y)^2 + (3x - y)^3$

(খ) $(2p + 5q)^3 + 3(2p + 5q)^2(5q - 2p) + 3(2p + 5q)(5q - 2p)^2 + (5q - 2p)^3$

(গ) $(x + 2y)^3 - 3(x + 2y)^2(x - 2y) + 3(x + 2y)(x - 2y)^2 - (x - 2y)^3$

(ঘ) $(6m + 2)^3 - 3(6m + 2)^2(6m - 4) + 3(6m + 2)(6m - 4)^2 + (6m - 4)^3$

(ঙ) $(x - y)^3 + (x + y)^3 + 6x(x^2 - y^2)$

(ক) $(3x + y)^3 + 3(3x + y)^2(3x - y) + 3(3x + y)(3x - y)^2 + (3x - y)^3$

সমাধান :

ধরি, $3x + y = a$

এবং $3x - y = b$

$$\begin{aligned}\therefore \text{প্রদত্ত রাশি} &= a^3 + 3a^2b + 3ab^2 + b^3 \\ &= (a + b)^3 \\ &= (3x + y + 3x - y)^3 \\ &= (6x)^3 \\ &= 216x^3\end{aligned}$$

$$(খ) (2p + 5q)^3 + 3(2p + 5q)^2(5q - 2p) + 3(2p + 5q)(5q - 2p)^2 + (5q - 2p)^3$$

সমাধান :

$$\text{ধরি, } 2p + 5q = a$$

$$\text{এবং } 5q - 2p = b$$

$$\therefore a + b = 2p + 5q + 5q - 2p \\ = 10q$$

$$\therefore \text{প্রদত্ত রাশি} = a^3 + 3a^2b + 3ab^2 + b^3 \\ = (a + b)^3 \\ = (10q)^3 \\ = 1000q^3$$

$$(গ) (x + 2y)^3 - 3(x + 2y)^2(x - 2y) + 3(x + 2y)(x - 2y)^2 - (x - 2y)^3$$

সমাধান :

$$\text{ধরি, } x + 2y = a$$

$$\text{এবং } x - 2y = b$$

$$\therefore a - b = (x + 2y) - (x - 2y) \\ = x + 2y - x + 2y \\ = 4y$$

$$\therefore \text{প্রদত্ত রাশি} = a^3 - 3a^2b + 3ab^2 - b^3 \\ = (a - b)^3 \\ = (4y)^3 \\ = 64y^3$$

$$(ঘ) (6m + 2)^3 - 3(6m + 2)^2(6m - 4) + 3(6m + 2)(6m - 4)^2 + (6m - 4)^3$$

সমাধান :

$$\text{ধরি, } 6m + 2 = a$$

$$\text{এবং } 6m - 4 = b$$

$$\therefore a - b = (6m + 2) - (6m - 4) \\ = 6m + 2 - 6m + 4 \\ = 6$$

$$\begin{aligned}\therefore \text{প্রদত্ত রাশি} &= a^3 - 3a^2b + 3ab^2 - b^3 \\ &= (a - b)^3 \\ &= (6)^3 \\ &= 216\end{aligned}$$

$$(ঙ) (x - y)^3 + (x + y)^3 + 6x(x^2 - y^2)$$

সমাধান :

$$\begin{aligned}(x - y)^3 + (x + y)^3 + 6x(x^2 - y^2) \\ = (x - y)^3 + (x + y)^3 + 3 \times 2x \times (x - y)(x + y)\end{aligned}$$

$$\text{ধরি, } x - y = a$$

$$\text{এবং } x + y = b$$

$$\begin{aligned}\therefore a + b &= x - y + x + y \\ &= 2x \\ &= 6\end{aligned}$$

$$\begin{aligned}\therefore \text{প্রদত্ত রাশি} &= (x - y)^3 + (x + y)^3 + 3 \times 2x \times (x - y)(x + y) \\ &= a^3 + b^3 + 3(a + b)ab \\ &= a^3 + b^3 + 3ab(a + b) \\ &= (a + b)^3 \\ &= (2x)^3 \\ &= 8x^3\end{aligned}$$

৩।

$$a + b = 8 \text{ এবং } ab = 15 \text{ হলে, } a^3 + b^3 \text{ এর মান কত?}$$

সমাধান :

$$\text{দেওয়া আছে, } a + b = 8$$

$$\text{এবং } ab = 15$$

$$\begin{aligned}\therefore \text{প্রদত্ত রাশি} &= a^3 + b^3 \\ &= (a + b)^3 - 3ab(a + b) \\ &= (8)^3 - 3 \times 15 \times 8 \\ &= 512 - 360 \\ &= 152\end{aligned}$$

৪। $x + y = 2$ হলে, দেখাও যে, $x^3 + y^3 + 6xy = 8$

সমাধান :

দেওয়া আছে, $x + y = 2$

দেখাতে হবে যে, $x^3 + y^3 + 6xy = 8$

বামপক্ষ $x^3 + y^3 + 6xy$

$$= x^3 + y^3 + 3xy.2$$

$$= x^3 + y^3 + 3xy(x + y) [\because 2 = x + y]$$

$$= (x + y)^3$$

$$= (2)^3$$

$$= 8$$

= ডানপক্ষ

$$\therefore x^3 + y^3 + 6xy = 8 \text{ (দেখানো হলো)}$$

৫। $2x + 3y = 13$ এবং $xy = 6$ হলে, $8x^3 + 27y^3$ এর মান নির্ণয় কর।

সমাধান :

দেওয়া আছে, $2x + 3y = 13$

এবং $xy = 6$

$$\therefore \text{প্রদত্ত রাশি} = 8x^3 + 27y^3$$

$$= (2x)^3 + (3y)^3$$

$$= (2x + 3y)^3 - 3 \times 2x \times 3y \times (2x + 3y)$$

$$= (13)^3 - 18xy(13)$$

$$= (13)^3 - 18 \times 6 \times 13$$

$$= 2197 - 1404$$

$$= 793$$

নির্ণেয় মান 793.

৬। $p - q = 5$, $pq = 3$ হলে, $p^3 - q^3$ এর মান নির্ণয় কর।

সমাধান :

দেওয়া আছে, $p - q = 5$

এবং $pq = 3$

$$\begin{aligned}\therefore \text{প্রদত্ত রাশি} &= p^3 - q^3 \\ &= (p - q)^3 + 3pq(p - q) \\ &= (5)^3 + 3 \times 3 \times (5) \\ &= 125 + 45 \\ &= 170\end{aligned}$$

নির্ণেয় মান 170.

৭। $x - 2y = 3$ হলে, $x^3 - 8y^3 - 18xy$ এর মান নির্ণয় কর?

সমাধান :

দেওয়া আছে, $x - 2y = 3$

$$\begin{aligned}\therefore \text{প্রদত্ত রাশি} &= x^3 - 8y^3 - 18xy \\ &= (x)^3 - (2y)^3 - 3 \times (x) \times (2y) \times 3 \\ &= (x)^3 - (2y)^3 - 3 \times x \times (2y)(x - 2y) \quad [\because 3 = x - 2y] \\ &= (x - 2y)^3 \\ &= (3)^3 \\ &= 27\end{aligned}$$

নির্ণেয় মান 27.

৮। $4x - 3 = 5$ হলে, প্রমাণ কর যে, $64x^3 - 27 - 180x = 125$

সমাধান :

দেওয়া আছে, $4x - 3 = 5$

প্রমাণ করতে হবে যে, $64x^3 - 27 - 180x = 125$

বামপক্ষ $64x^3 - 27 - 180x$

$$\begin{aligned} &= (4x)^3 - (3)^3 - 180x \\ &= (4x - 3)^3 + 3 \cdot 4x \cdot 3(4x - 3) - 180x \\ &= (5)^3 + 36x \cdot (5) - 180x \end{aligned}$$

$$= 125 + 180x - 180x$$

$$= 125$$

$$= \text{ডানপক্ষ}$$

$$\therefore \text{বামপক্ষ} = \text{ডানপক্ষ} \text{ (প্রামাণিত)}$$

৯।

$a = -3$ এবং $b = 2$ হলে, $8a^3 + 36a^2b + 54ab^2 + 27b^3$ এর মান নির্ণয় কর

সমাধান :

দেওয়া আছে, $a = -3$

এবং $b = 2$

$$\begin{aligned}\therefore \text{প্রদত্ত রাশি} &= 8a^3 + 36a^2b + 54ab^2 + 27b^3 \\ &= (2a)^3 + 3.(2a)^2.3b + 3.2a.(3b)^2 + (3b)^3 \\ &= (2a + 3b)^3 \\ &= \{2(-3) + 3(2)\}^3 \\ &= (-6 + 6)^3 \\ &= (0)^3 \\ &= 0\end{aligned}$$

নির্ণেয় মান 0.

১০।

$a = 7$ হলে, $a^3 + 6a^2 + 12a + 1$ এর মান নির্ণয় কর

সমাধান :

দেওয়া আছে, $a = 7$

$$\begin{aligned}\therefore \text{প্রদত্ত রাশি} &= a^3 + 6a^2 + 12a + 1 \\ &= (a)^3 + 3.(a)^2.2 + 3.a.(2)^2 + (2)^3 - 7 \\ &= (a + 2)^3 - 7 \\ &= \{7 + 2\}^3 - 7 \\ &= (9)^3 - 7 \\ &= 729 - 7 \\ &= 722\end{aligned}$$

নির্ণেয় মান 722.

સમાધાન :

$$\therefore \text{প্রদত্ত রাশি} = x^3 - 12x + 48x - 64$$

$$\begin{aligned} &= (x)^3 - 3.(x)^2.4 + 3.x.(4)^2 - (4)^3 \\ &= (x - 4)^3 \\ &= \{5 - 4\}^3 \\ &= (1)^3 \\ &= 1 \end{aligned}$$

নির্ণেয় মান 1.

সমাধান :

প্রমাণ করতে হবে যে, $a^6 + b^6 + 3a^2b^2c^2 = c^6$

$$\begin{aligned} \text{বামপক্ষ} &= a^6 + b^6 + 3a^2b^2c^2 \\ &= (a^2)^3 + (b^2)^3 + 3a^2b^2c^2 \\ &= (a^2 + b^2)^3 - 3a^2b^2(a^2 + b^2) + 3a^2b^2c^2 \\ &= (c^2)^3 - 3a^2b^2(c^2) + 3a^2b^2c^2 \\ &= c^6 \\ &= \text{ডানপক্ষ} \end{aligned}$$

\therefore বামপক্ষ = ডানপক্ষ (প্রমাণিত)

সমাধান :

দেওয়া আছে, $x + \frac{1}{x} = 4$

প্রমাণ করতে হবে যে, $x^3 + \frac{1}{x^3} = 52$

$$\begin{aligned}\text{বামপক্ষ} &= x^3 + \frac{1}{x^3} \\&= (x)^3 + \left(\frac{1}{x}\right)^3 \\&= \left(x + \frac{1}{x}\right)^3 - 3x \frac{1}{x} \left(x + \frac{1}{x}\right) \\&= (4)^3 - 3(4) \\&= 64 - 12 \\&= 52 \\&= \text{ডানপক্ষ}\end{aligned}$$

∴ বামপক্ষ = ডানপক্ষ (প্রমাণিত)

১৪। $a - \frac{1}{a} = 5$ হলে, $a^3 - \frac{1}{a^3}$ এর মান কত?

সমাধান :

দেওয়া আছে, $a - \frac{1}{a} = 5$

প্রদত্ত রাশি $= a^3 - \frac{1}{a^3}$

$$\begin{aligned}&= (a)^3 - \left(\frac{1}{a}\right)^3 \\&= \left(a - \frac{1}{a}\right)^3 + 3a \frac{1}{a} \left(a - \frac{1}{a}\right) \\&= (5)^3 + 3(5) \\&= 125 + 15 \\&= 140\end{aligned}$$

নির্ণেয় মান 140.

- (ক) $(a^2 + b^2)(a^4 - a^2b^2 + b^4)$ (খ) $(ax - by)(a^2x^2 + abxy + b^2y^2)$
 (গ) $(2ab^2 - 1)(4a^2b^4 + 2ab^2 + 1)$ (ঘ) $(x^2 + a)(x^4 - ax^2 + a^2)$
 (ঙ) $(7a + 4b)(49a^2 - 28ab + 16b^2)$ (চ) $(2a - 1)(4a^2 + 2a + 1)(8a^3 + 1)$
 (ছ) $(x + a)(x^2 - ax + a^2)(x - a)(x^2 + ax + a^2)$
 (জ) $(5a + 3b)(25a^2 - 15ab + 9b^2)(125a^3 - 27b^3)$

(ক) $(a^2 + b^2)(a^4 - a^2b^2 + b^4)$

সমাধান :

$$\begin{aligned} & (a^2 + b^2)(a^4 - a^2b^2 + b^4) \\ &= (a^2 + b^2)\{(a^2)^2 - a^2b^2 + (b^2)^2\} \\ &= (a^2)^3 + (b^2)^3 \\ &= a^6 + b^6 \end{aligned}$$

(খ) $(ax - by)(a^2x^2 + abxy + b^2y^2)$

সমাধান :

$$\begin{aligned} & (ax - by)(a^2x^2 + abxy + b^2y^2) \\ &= (ax - by)\{(ax)^2 + abxy + (by)^2\} \\ &= (ax)^2 + (by)^2 \\ &= a^2x^2 + b^2y^2 \end{aligned}$$

(গ) $(2ab^2 - 1)(4a^2b^4 + 2ab^2 + 1)$

সমাধান :

$$\begin{aligned} & (2ab^2 - 1)(4a^2b^4 + 2ab^2 + 1) \\ &= (2ab^2 - 1)\{(2ab^2)^2 + 2ab^2 \cdot 1 + (1)^2\} \\ &= (2ab^2)^3 - (1)^3 \\ &= 8a^3b^6 - 1 \end{aligned}$$

$$(ঘ) (x^2 + a)(x^4 - ax^2 + a^2)$$

সমাধান :

$$\begin{aligned} & (x^2 + a)(x^4 - ax^2 + a^2) \\ &= (x^2 + a)\{(x^2)^2 - x^2 \cdot a + (a)^2\} \\ &= (x^2)^3 + (a)^3 \\ &= x^6 + a^3 \end{aligned}$$

$$(ঙ) (7a + 4b)(49a^2 - 28ab + 16b^2)$$

সমাধান :

$$\begin{aligned} & (7a + 4b)(49a^2 - 28ab + 16b^2) \\ &= (7a + 4b)\{(7a)^2 - 7a \times 4b + (4b)^2\} \\ &= (7a)^3 + (4b)^3 \\ &= 343a^3 + 64b^3 \end{aligned}$$

$$(চ) (2a - 1)(4a^2 + 2a + 1)(8a^3 + 1)$$

সমাধান :

$$\begin{aligned} & (2a - 1)(4a^2 + 2a + 1)(8a^3 + 1) \\ &= (2a - 1)\{(2a)^2 + 2a \times 1 + (1)^2\}(8a^3 + 1) \\ &= \{(2a)^3 - (1)^3\}(8a^3 + 1) \\ &= (8a^3 - 1)(8a^3 + 1) \\ &= (8a^3)^2 - (1)^2 \\ &= 64a^6 - 1 \end{aligned}$$

$$(ছ) (x + a)(x^2 - ax + a^2)(x - a)(x^2 + ax + a^2)$$

সমাধান :

$$\begin{aligned} & (x + a)(x^2 - ax + a^2)(x - a)(x^2 + ax + a^2) \\ &= (x^3 + a^3)(x^3 - a^3) \\ &= (x^3)^2 - (a^3)^2 \\ &= x^6 - a^6 \end{aligned}$$

$$(জ) (5a + 3b)(25a^2 - 15ab + 9b^2)(125a^3 - 27b^3)$$

সমাধান :

$$\begin{aligned} & (5a + 3b)\{(5a)^2 - 5a \times 3b + (3b)^2\}\{125a^3 - 27b^3\} \\ & = \{(5a)^3 - (3b)^3\}(125a^3 - 27b^3) \\ & = (125a^3 + 27b^3)(125a^3 - 27b^3) \\ & = (125a^3)^2 - (27b^3)^2 \\ & = 15625a^6 - 729b^6 \end{aligned}$$

১৬। উৎপাদকে বিশ্লেষণ কর :

(ক) $a^3 + 8$

(খ) $8x^3 + 343$

(গ) $8a^4 + 27ab^3$

(ঘ) $8x^3 + 1$

(ঙ) $64a^3 + 125b^3$

(চ) $729a^3 - 64b^3c^6$

(ছ) $27a^3b^3 + 64b^3c^3$

(জ) $56x^3 - 189y^3$

(ক) $a^3 + 8$

সমাধান :

$$\begin{aligned} & a^3 + 8 \\ & = (a)^3 + (2)^3 \\ & = (a + 2)\{(a)^2 - a \times 2 + (2)^2\} \\ & = (a + 2)(a^2 - 2a + 4) \end{aligned}$$

(গ) $8a^4 + 27ab^2$

সমাধান :

$$\begin{aligned} & 8a^4 + 27ab^3 \\ & = a(8a^3 + 27b^3) \\ & = a\{(2a)^3 + (3b)^3\} \\ & = a(2a + 3)\{(2a)^2 - 2a \times 3 + (3)^2\} \\ & = a(2a + 3)(4a^2 - 6a + 9) \end{aligned}$$

(খ) $8x^3 + 343$

সমাধান :

$$\begin{aligned} & 8x^3 + 343 \\ & = (2x)^3 + (7)^3 \\ & = (x + 7)\{(2x)^2 - 2x \times 7 + (7)^2\} \\ & = (x + 7)(4x^2 - 14x + 49) \end{aligned}$$

(ঘ) $8x^3 + 1$

সমাধান :

$$\begin{aligned} & 8x^3 + 1 \\ & = (2x)^3 + (1)^3 \\ & = (2x + 1)\{(2x)^2 - 2x \times 1 + (1)^2\} \\ & = (2x + 1)(4x^2 - 2x + 1) \end{aligned}$$

(ঙ) $64a^3 + 125b^3$

সমাধান :

$$64a^3 + 125b^3$$

$$= (4a)^3 + (5b)^3$$

$$= (4a + 5b)\{(4a)^2 - 4a \times 5b + (5b)^2\}$$

$$= (4a + 5b)(16a^2 - 20ab + 25b^2)$$

(ছ) $27a^3b^3 + 64b^3c^3$

সমাধান :

$$27a^3b^3 + 64b^3c^3$$

$$= b^3\{(3a)^3 + (4c)^3\}$$

$$= b^3(3a + 4c)\{(3a)^2 - 3a \times 4c + (4c)^2\}$$

$$= b^3(3a + 4c)(9a^2 - 12ac + 16c^2)$$

(চ) $729a^3 - 64b^3c^6$

সমাধান :

$$729a^3 - 64b^3c^6$$

$$= (9a)^3 - (4bc^2)^3$$

$$= (9a - 4bc^2)\{(9a)^2 + 9a \times 4bc^2 + (4bc^2)^2\}$$

$$= (9a - 4bc^2)(81a^2 + 36abc^2 + 16b^2c^4)$$

(জ) $56x^3 - 189y^3$

সমাধান :

$$56x^3 - 189y^3$$

$$= 7(8x^3 - 27y^3)$$

$$= 7\{(2x)^3 - (3y)^3\}$$

$$= 7(2x - 3y)\{(2x)^2 + 2x \times 3y + (3y)^2\}$$

$$= 7(2x - 3y)(4x^2 + 6xy + 9y^2)$$